

A DISSECTION OF FOREGROUNDS IN EPOCH OF REIONIZATION OBSERVATIONS FROM THE MURCHISON WIDEFIELD ARRAY

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ABSTRACT

Detection of 21 cm emission of HI from the epoch of reionization, at redshifts $z > 6$, is limited primarily by foreground emission. We investigate the chromatic signatures of an all-sky foreground model imprinted by an instrumental transfer function. Using the delay spectrum technique **that maps the measurements to foreground object locations through signal delays between antenna pairs**, we demonstrate that the foreground signatures that have the largest impact on the HI signal arise from power received far away from the primary field of view. Comparing data from recent Murchison Widefield Array observations with simulations **broken down by types of emission**, we identify diffuse emission near the horizon as a significant contributing factor, even on wide antenna spacings **which are usually not sensitive to diffuse emission**. For signals entering through the primary field of view, compact emission dominates the foreground contamination. These two mechanisms imprint a characteristic *pitchfork* signature on the “foreground wedge” in Fourier space, **which is found to be generic to wide-field measurements**. Based on these results, we propose that selective down-weighting of data based on antenna spacing and time **can** mitigate foreground contamination substantially (up to a **factor** ~ 100 with negligible loss of sensitivity). **A dish-shaped antenna yields the most desirable features from a foreground contamination viewpoint, relative to a dipole or a phased array.**

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1. INTRODUCTION

At the end of the recombination epoch, the Universe was completely neutral. This period, referred to as the *Dark Ages* in the Universe’s history, is characterized by the localized accumulation of matter under the influence of gravity. And it ended with the formation of the first stars and galaxies which started emitting ultra-violet and X-ray radiation, thereby reionizing the neutral medium in their surroundings. This commenced the epoch of reionization (EoR) — a period of non-linear growth of matter density perturbations and astrophysical evolution. Studying the EoR holds the key to understanding this evolution.

Observations of redshifted 21 cm radiation generated by the spin flip transition of HI has been identified as a direct probe of the EoR (Sunyaev & Zeldovich 1972; Scott & Rees 1990; Madau et al. 1997; Tozzi et al. 2000; Iliev et al. 2002). Detecting this signal has recently emerged as a very promising experiment to fill the gaps in our understanding of the Universe’s history.

Sensitive instruments such as the Square Kilometre Array (SKA) are required for direct observation and tomography of redshifted HI. Numerous **pathfinders and precursors** to the SKA such as the Murchison Widefield Array (MWA; Lonsdale et al. 2009; Tingay et al. 2013; Bowman et al. 2013), the Low Frequency Array (LOFAR; van Haarlem et al. 2013), and the Precision Array for Probing the Epoch of Reionization (PAPER; Parsons et al. 2010) have become operational with enough sensitivity for a statistical detection of the EoR HI power spectrum (Bowman et al. 2006; Parsons et al. 2012a; Beardsley et al. 2013; Dillon et al. 2013; Thyagarajan et al. 2013; Pober et al. 2014). **The Hydrogen Epoch of Reionization Array²² (HERA) is currently under construction using new insights gained with the MWA and PAPER.**

A key challenge in the statistical detection of the redshifted HI 21 cm signal, via the spatial power spectrum of temperature fluctuations, arises from the contamination by Galactic and extragalactic foregrounds (see, e.g., Di Matteo et al. 2002; Zaldarriaga et al. 2004; Furlanetto et al. 2006; Ali et al. 2008; Bernardi et al. 2009, 2010; Ghosh et al. 2012). Morales & Hewitt (2004) show that the inherent isotropy and symmetry of the EoR signal in frequency and spatial wavenumber (k) space make it distinguishable from sources of contamination which are isolated to certain k modes by virtue of their inherent spectral smoothness (Morales et al. 2006; Bowman et al. 2009; Liu & Tegmark 2011; Parsons et al. 2012b; Dillon et al. 2013; Pober et al. 2013). **Since this contamination is expected to be several orders of magnitude stronger than the underlying EoR HI signal, it is critical to characterize foregrounds precisely in order to reduce their impact on EoR HI power spectrum detection sensitivity.**

Considerable effort has been and continues to be made towards understanding the k -space behavior of foreground signatures in the observed power spectrum and formulating robust estimators of the true power spectrum (Bowman et al. 2009; Liu et al. 2009; Datta et al. 2010; Liu & Tegmark 2011; Morales et al. 2012; Trott et al.

2012; Pober et al. 2013; Thyagarajan et al. 2013; Dillon et al. 2014; Liu et al. 2014a,b). **A model that provides a generic explanation for the observed foreground power spectrum has emerged, whereby the wide-field (and chromatic) response of the instrument causes the power in smooth spectrum foregrounds to occupy higher k -modes into the so-called ‘wedge’.** The conservative foreground strategy, referred to as *avoidance*, that has developed alongside this work is to discard k -modes which could be contaminated (for e.g., Parsons et al. 2014). The more aggressive alternative is to subtract a sky model and regain access to modes discarded by *avoidance*. In both cases, which parts of the sky are most critical to either *avoid* or *subtract* has remained largely uncertain. Here, we focus primarily on extending the *avoidance* strategy by identifying foreground components at greatest risk to “leak” from foreground modes to EoR modes and proposing a scheme for down-weighting these components.

Foregrounds with intrinsic deviations from spectral smoothness, instruments with high chromaticity, polarization leakage, calibration errors, or approximations in power spectrum analyses can contaminate the true EoR HI power spectrum. Here we use existing catalogs and a high fidelity instrumental model to capture both foreground and instrumental chromaticity. To decouple these effects from possible analysis effects, such as those pointed out by Hazelton et al. (2013), we compute power spectra using a ***Per-Baseline*** approach of Parsons et al. (2012b). This approximates the power spectrum as the inverse Fourier transform of the spectra generated by the instrument’s correlator.

After matching observations from the Murchison Widefield Array with instrumental simulations of the entire sky, we examine the **shape of the delay spectrum** of each baseline. We report two important findings: the foregrounds that most severely **obscure** the redshifted 21 cm power spectrum are not caused by emission in the central field of view, but rather by bright objects from near the horizon; and, diffuse Galactic emission plays a significant role hitherto unpredicted. We quantify these by separating the simulations into components based on type of foreground emission. We then arrive at a new method for minimizing the contribution of bright foregrounds which uses prior knowledge of the sky to down-weight adversely contaminated baselines. **We also examine the role of antenna shapes in determining foreground contamination and provide inputs on antenna design for future EoR experiments.**

In §2 we **provide a brief overview of the delay spectrum technique** (Parsons et al. 2012a,b). In §3, we describe the MWA setup, summarize the observing parameters, and present the resulting data. Simulations using these observing parameters are described in §4 and analyzed by sky location and type of emission in §5. In §6, we offer an initial description of a more precise foreground avoidance technique. **The role of antenna shapes in determining foreground contamination is explored in §7.** We present a summary of our work and findings in §8.

2. DELAY SPECTRUM

Interferometer array data known as *visibilities*, $V_{bf} \equiv V_{bf}(\mathbf{b}, f)$, represent correlations between time-series of

²² <http://reionization.org/>

electric fields measured by different antenna pairs with separation vectors \mathbf{b} and then Fourier transformed along the time axis to obtain a spectrum along the frequency (f) axis. If $I(\hat{\mathbf{s}}, f)$ and $A(\hat{\mathbf{s}}, f)$ are the sky brightness and antenna's directional power pattern, respectively, at different frequencies as a function of direction on the sky denoted by the unit vector ($\hat{\mathbf{s}}$), and $W_f \equiv W_f(f)$ denotes instrumental bandpass weights, then V_{bf} can be written as (with a slight adaptation from van Cittert (1934), Zernike (1938), and Thompson et al. (2001)):

$$V_{bf} = \iint_{\text{sky}} A(\hat{\mathbf{s}}, f) I(\hat{\mathbf{s}}, f) W_f e^{-i2\pi f \frac{\mathbf{b} \cdot \hat{\mathbf{s}}}{c}} d\Omega, \quad (1)$$

where, c is the speed of light, and $d\Omega$ is the solid angle element to which $\hat{\mathbf{s}}$ is the unit normal vector. We wish to **note** that this equation is valid **even for wide-field measurements where the sky cannot be approximated to be flat**.

The delay spectrum, $V_{b\tau} \equiv V_{b\tau}(\mathbf{b}, \tau)$, is defined as the inverse Fourier transform of V_{bf} along the frequency coordinate:

$$V_{b\tau} \equiv \int V_{bf} W'_f e^{i2\pi f \tau} df, \quad (2)$$

where, $W'_f \equiv W'_f(f)$ is a spectral weighting function which can be chosen to control the quality of the delay spectrum (Thyagarajan et al. 2013; Vedantham et al. 2012), and τ represents the signal delay between antenna pairs:

$$\tau = \frac{\mathbf{b} \cdot \hat{\mathbf{s}}}{c}. \quad (3)$$

$V_{b\tau}$ is expressed in observer's units as Jy Hz.

2.1. Resemblance to Spatial Power Spectrum

Equation 1 can be **equivalently re-expressed** as:

$$V_{uf} \equiv V_{uf}(\mathbf{u}, f) = \iint_{\text{sky}} A(\hat{\mathbf{s}}, f) I(\hat{\mathbf{s}}, f) W_f e^{-i2\pi \mathbf{u} \cdot \hat{\mathbf{s}}} d\Omega, \quad (4)$$

where, $\hat{\mathbf{s}}$ is measured with reference to a location on the sky referred to as the *phase center*, and $\mathbf{u} \equiv (u, v, w)$ denotes the spatial frequency vector. w is aligned parallel to the direction of the phase center, while u and v lie on the transverse plane perpendicular to it. For measurements that are constrained to lie on this plane, we can choose $w = 0$ without loss of generality and \mathbf{u} effectively reduces to $\mathbf{u} \equiv (u, v)$, a two-dimensional vector. Then, \mathbf{u} is directly related to the transverse spatial wavenumber mode as:

$$\mathbf{k}_\perp \equiv \frac{2\pi \mathbf{u}}{D}, \quad (5)$$

where, $D \equiv D(z)$ is the transverse comoving distance at redshift z .

Since we are concerned with a redshifted HI spectral line from cosmological distances, f is a measure of cosmological distance along the line of sight. η , which is the Fourier transform dual of f , is used to denote the spatial frequency along the line of sight and has units of time.

It is directly related to the line-of-sight wavenumber,

$$k_\parallel \approx \frac{2\pi \eta f_{21} H_0 E(z)}{c(1+z)^2}, \quad (6)$$

where, f_{21} is the rest frame frequency of the 21 cm spin flip transition of HI, and H_0 and $E(z) \equiv [\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda]^{1/2}$ are standard terms in cosmology. This approximation holds under the assumption that the redshift range (or frequency band) is small enough within which cosmological evolution is negligible. Thus,

$$V_{u\eta} \equiv V_{u\eta}(\mathbf{u}, \eta) \equiv \int V_{uf}(\mathbf{u}, f) W'_f e^{i2\pi f \eta} df \quad (7)$$

represents the true spatial Fourier representation of the three-dimensional sky brightness distribution. This approach has been discussed in detail in Morales & Hewitt (2004). The spatial power spectrum of EoR HI distribution, $P(\mathbf{k}_\perp, k_\parallel)$, and $V_{u\eta}$ are related by (Morales & Hewitt 2004; McQuinn et al. 2006; Parsons et al. 2012a):

$$P(\mathbf{k}_\perp, k_\parallel) \simeq |V_{u\eta}|^2 \left(\frac{A_e}{\lambda^2 \Delta B} \right) \left(\frac{D^2 \Delta D}{\Delta B} \right) \left(\frac{\lambda^2}{2k_B} \right)^2, \quad (8)$$

where, A_e is the effective area of the antenna, ΔB is the bandwidth, λ is the wavelength of the band center, and k_B is the Boltzmann constant. Thus, $V_{u\eta}$ inferred from observations, also in units of Jy Hz, can be converted into an equivalent cosmological HI power spectrum $P(\mathbf{k}_\perp, k_\parallel)$, in units of $\text{K}^2 \text{Mpc}^3$ or, more generally, $\text{K}^2(\text{Mpc}/h)^3$, where h is the Hubble constant factor.

Without loss of generality, the phase center can be assumed to be the zenith relative to the local tangent plane. Then \mathbf{u} lies on this plane for measurements constrained to be on it. If the array of antennas are also coplanar lying on the local tangent plane, then $\mathbf{u} = \mathbf{b}/\lambda$. Under such circumstances, equations 1 and 3 closely resemble equations 4 and 7 respectively. However, they are not quite identical to each other. The difference is because \mathbf{b} is independent of frequency while \mathbf{u} is not. Parsons et al. (2012b) and Liu et al. (2014a) have discussed the mathematical correspondence between the two.

Foregrounds can be described in both the delay spectrum and Fourier frameworks. For our study, which primarily concerns with foreground characterization, we find the former to be simple and yet extremely useful, while maintaining a close correspondence with the latter despite subtle differences. In order to express a quantity derived from $V_{u\eta}$ that has units identical to that of the cosmological HI power spectrum, we define delay power spectrum:

$$P_d(\mathbf{k}_\perp, k_\parallel) \equiv |V_{b\tau}|^2 \left(\frac{A_e}{\lambda^2 \Delta B} \right) \left(\frac{D^2 \Delta D}{\Delta B} \right) \left(\frac{\lambda^2}{2k_B} \right)^2, \quad (9)$$

where, \mathbf{u} and η in equations 5 and 6 have been correspondingly replaced with \mathbf{b}/λ and τ respectively.

In summary, the delay spectrum, $V_{b\tau}$, is obtained from *visibilities* which are the basic data blocks measured by each antenna pair, using equations 1 and 2. $V_{b\tau}$ captures all the effects of EoR HI signal corruption caused by foregrounds and the instrument. At the same time, it

is closely related to the sought power spectrum $P(k_{\perp}, k_{\parallel})$ containing critical information about spatial scales.

Note that since *visibility* is a complex quantity, its **delay transform contains** positive and negative delays. Negative and positive delays correspond to the two hemispheres of the sky as transected by the antenna spacing vector. **Figure 1 illustrates the radio interferometer delays and conventions used in our paper.** \mathbf{b} is assumed to be on a coordinate system aligned with the local east, north (along local meridian) and upward (zenith) directions at the telescope site. Hence, a perfectly eastward oriented antenna spacing will observe objects in the eastern and the western skies at positive and negative delays, respectively. Similarly, an object in the northern sky will appear at a positive delay at an antenna spacing oriented northward. For all observations used in this study, we use the zenith as the phase center, for which $\tau \equiv 0$.

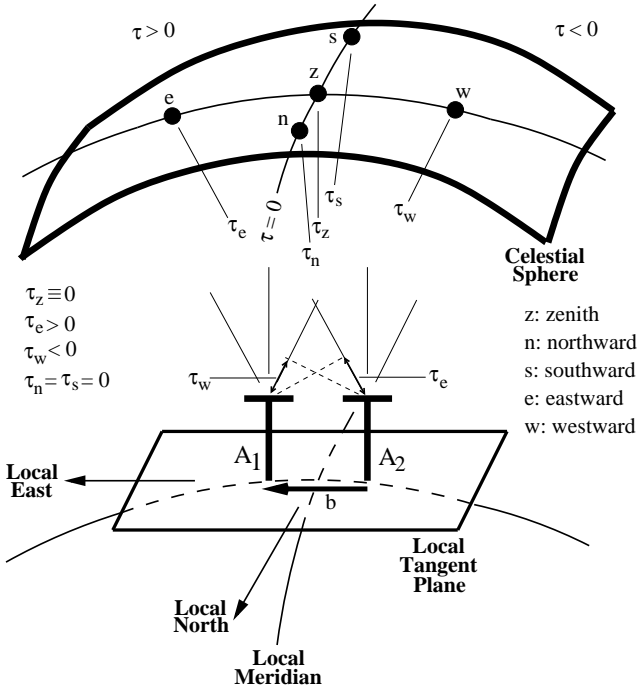


Figure 1. Illustration of radio interferometer delays and conventions used in this paper. Two antennas labeled as A_1 and A_2 are separated by vector \mathbf{b} on the local tangent plane. The local meridian, local north and local east are shown for reference. Points labeled as ‘z’, ‘n’, ‘s’, ‘e’ and ‘w’ on the celestial sphere denote zenith, northward, southward, eastward and westward positions, respectively. τ_z , τ_n , τ_s , τ_e and τ_w denote the respective delays measured between A_1 and A_2 . Throughout this paper, zenith is chosen as the phase center. Hence, $\tau_z \equiv 0$. If \mathbf{b} is oriented eastward as shown, then $\tau_e > 0$, $\tau_w < 0$, and $\tau_n = \tau_s = 0$. Conversely, if \mathbf{b} is oriented northward (not shown here), then $\tau_n > 0$, $\tau_s < 0$, and $\tau_e = \tau_w = 0$.

We give a brief overview of some parameters of Fourier space which is generic to all experiments that use a similar approach. Figure 2 illustrates the Fourier space, specific to the MWA, in which the delay (and power) spectra of HI from the EoR are presented in this paper. $|\mathbf{b}|$ and k_{\perp} , denoting spatial scales in the transverse direction (**tangent plane to the celestial sphere**), form the x -axis. $\tau \approx \eta \propto k_{\parallel}$, denoting spatial scales along line-of-sight form the y -axis.

Foreground emission maps to a wedge-shaped region in Fourier space, hereafter referred to as the *foreground wedge* (Datta et al. 2010), whose boundaries are determined by the antenna spacings and the light travel times across them. These boundaries, called horizon delay limits (Vedantham et al. 2012; Parsons et al. 2012b), are shown by solid lines. The spectral transfer function of the instrument convolves the *foreground wedge* and stretches it further (unshaded narrow strips bounded by solid and dashed lines) along τ -axis (Parsons et al. 2012b; Thyagarajan et al. 2013). The width of this narrow strip is inversely proportional to the operating bandwidth. The region of Fourier space excluding the *foreground wedge* and the narrow strips is the so-called *EoR window*, shown in light and medium shades. However, the instrument used in our study, namely the MWA, has a passband constructed using coarse channels with a characteristic shape giving rise to periodic gratings thereby resulting in repetitions of the *foreground wedge* at multiples of $0.78 \mu\text{s}$.

In the context of EoR studies in Fourier space, the HI power spectrum from the EoR is expected to decrease rapidly with $|\mathbf{k}|$. Hence, the brightest EoR signal will be observed on the shortest baselines and smallest delays. Thus the region of interest for EoR studies is slightly beyond the horizon delay limits (dashed lines) and inside the first grating on either side ($|\tau| \lesssim 0.78 \mu\text{s}$, dot-dashed lines) caused by the instrument’s spectral transfer function. We call this region with medium shade as the *EoR window* in this paper. The MWA EoR collaboration actively uses this as a test region in Fourier space for diagnostics on data quality.

For geometrical intuition, we restrict the orientation (θ_b , measured anti-clockwise from East) of all baselines to lie in the range $-67.5^\circ \leq \theta_b < 112.5^\circ$. Baselines oriented in the other half-plane measure conjugate visibilities with delays of equal magnitude but of opposite sign and hence are ignored in our analysis. **Note that visibilities from different baselines have not been averaged together in this analysis.**

3. EXAMPLE DATA

3.1. The Murchison Widefield Array (MWA)

MWA construction was completed in 2012 and, after commissioning, began its EoR observing program in 2013. In its final configuration the MWA is a 128-tile interferometer array capable of observing a 30.72 MHz instantaneous band anywhere in the range 80–300 MHz. Each tile is a phased array of 16 dipoles, each in the shape of a bow-tie. This yields a primary field of view $\gtrsim 20^\circ$ wide and multiple secondary lobes. The array is arranged as a centrally condensed core of ~ 300 m — there are many spacings in the range 5–50 m — and a radial density that falls off as the inverse of the radius, with the longest baselines at 3 km (Beardsley et al. 2012). Here we focus on antenna spacings $|\mathbf{b}| \leq 200$ m (spatial scales relevant to reionization) and a frequency range 170–200 MHz. The center frequency of 185 MHz corresponds to a redshift, $z \simeq 6.68$. **At this frequency, we use $A_e = 10.5 \text{ m}^2$.**

The MWA passband of width $\Delta B = 30.72$ MHz is divided coarsely into 24×1.28 MHz sub-bands with each sub-band weighted by a digital filter. The coarse channel shape is obtained using a 8-tap polyphase filter bank

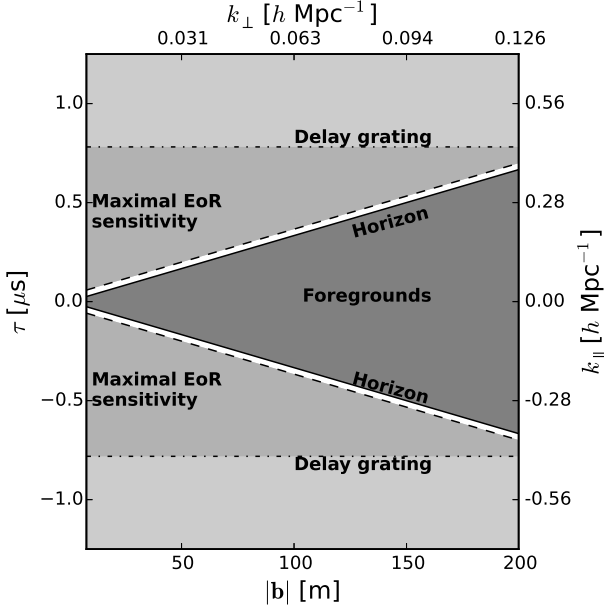


Figure 2. Fourier space in which delay (and power) spectra of EoR HI signals are presented. The x -axis is denoted by $|b|$ (antenna spacing) or k_{\perp} (transverse wavenumber). The y -axis denoted by τ (delay) or k_{\parallel} (line-of-sight wavenumber). Here, k_{\perp} and k_{\parallel} are obtained for a frequency of 185 MHz. The dark shaded region is referred to as the *foreground wedge* where smooth spectrum foregrounds reside. Its boundaries (solid lines), given by light travel time for corresponding antenna spacings, are referred to as horizon delay limits. Regions excluding the *wedge* and narrow extensions of the *wedge* (white unshaded strips) caused by convolution with the instrument’s spectral transfer function are expected to be relatively free of foreground contamination. Due to an undesirable grating pattern (dot-dashed lines) of the instrument used in this study, namely the MWA, we conservatively identify a restricted region of high EoR sensitivity (medium shade) and refer to it as the *EoR window* in this paper.

(PFB) and a Kaiser window with parameter $\beta = 5$. Each of these coarse bands consists of 32 fine channels of width 40 kHz each. After correcting for the shape of these coarse channels, the fine channels at the edges of these sub-bands are flagged because they are known to be contaminated by aliasing at a low level. Any spectral flags, or other known weights constitutes W_f in equation 1.

3.2. EoR Observations

The MWA is expected to be sensitive to the power spectrum of the HI signal over the redshift range $6 < z < 10$ (Thyagarajan et al. 2013; Beardsley et al. 2013). Over 600 hours have been currently observed using the MWA with the objective of characterizing the nature of the sources that are responsible for ionizing the IGM, charting the evolution of the global neutral fraction, and probing the nature of quasar emissions by constraining the properties of their ionized proximity zones.

The MWA targets two primary low-foreground fields for reionization observations. Here, we focus on the field at $RA = 0^h$, $Dec = -30^\circ$. The MWA tracks a patch of sky through antenna beams formed and steered electronically by controlling delay settings of the dipoles in

an MWA tile. The pointing system is capable of steering to points on a regular $\sim 7^\circ$ grid. During observations we allow the sky to drift across the nearest available pointing, shifting between grid points as necessary (once in ~ 30 minutes). This process is repeated throughout the course of the observation ≈ 4.86 hours. Figure 3 illustrates how the apparent pointing oscillates around the desired pointing direction.

The observations shown here were undertaken on 2013 August 23. We have chosen two, 112 second long sections from this night for detailed study. These were chosen to provide a selection of possible foreground and instrumental conditions. As an example of a nominal observing setup we choose a zenith pointing; as an example of poor foreground conditions, we choose a pointing when the field is ~ 2 hours from zenith. This pointing has a significantly higher secondary lobe structure and is observed when the bright galactic center is well above the horizon.

The *local sidereal time* (LST) at these two snapshots are shown in Figure 3 as vertical lines at **22.08 hours (wrapped to -1.92 hours in the figure)** and 0.09 hours, which are hereafter denoted as *off-zenith* and *zenith* pointings, respectively.

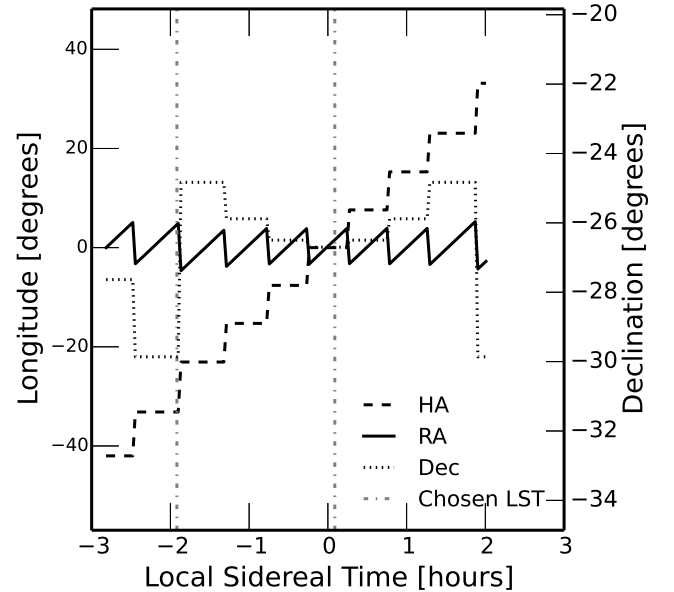


Figure 3. MWA tile beam pointing directions during the course of the observation. The x -axis refers to the *local sidereal time* (LST). The axis on the left refers to longitudes, namely, Right Ascension (RA) and Hour Angle (HA). Negative values of RA, HA, and LST are to be interpreted as having been wrapped around by 360° or 24 hours. The axis on the right refers to the declination of the pointing direction. The RA, HA, and declination are plotted with solid, dashed and dotted lines respectively. The sky is allowed to drift for ~ 30 mins before the beamformer delay settings change in a discrete step to center the beam around $RA = 0^h$, $Dec = -30^\circ$. Dot-dashed vertical lines show the LST of *off-zenith* and *zenith* pointings used in our study.

3.3. Initial Data Processing

The data are flagged²³ for interference (Offringa et al. 2010, 2012), removing 3% of the data and averaged in time and frequency from the raw 0.5 s, 40 kHz to 2s, 80 kHz. These data are then calibrated to a simulation of the sky containing 2420 point-like objects selected from the MWA Commissioning Survey (MWACS; Hurley-Walker et al. 2014). It has a flux density limit of 25 mJy and a declination range of -12° to -40° evenly covering the field of view of the observations reported here. The objects used in calibration are selected to lie inside the 5% contour of the primary lobe of the tile power pattern. The calibration algorithm – based on forward modeling software by Sullivan et al. (2012) and the calibration method described by Salvini & Wijnholds (2014) – computes complex gain solutions per channel per antenna averaged to two minute intervals. The solutions are fairly low signal-to-noise so we iteratively average along the antenna and frequency dimensions to capture the relatively independent passband and antenna-to-antenna variation. First, we average the channel gains over all antennas to obtain a high signal-to-noise measurement of the bandpass. After applying this single passband, we do a second round of calibration and fit second and first order polynomials for amplitude and phase respectively for each antenna. This flattens any residual variation in bandpass and removes small phase slopes due to variations in cable delay. Finally, we fit for an additional phase known to be caused by small reflections in a subset of cables.

3.4. Deconvolved Delay Spectrum

We obtain the delay spectrum of these calibrated visibilities by taking the delay transform of each baseline’s spectrum (equation 2) choosing W'_f to be a *Blackman-Harris* window function. The spectrum is multiplied by the additional weight of the flagged channels which occur rarely for interference and regularly every 1.28 MHz where the edges of coarse channels are known to have a small aliasing effect. In delay-space, these weights translate into a convolution by a grating point spread function (PSF) with gratings at multiples of $\tau = 0.78 \mu\text{s}$. We deconvolve this PSF using a one dimensional CLEAN algorithm (Taylor et al. 1999) as described for the delay axis by Parsons & Backer (2009); Parsons et al. (2012b). The CLEAN procedure iteratively finds and subtracts peak values convolved by the Fourier transform of the weights. We limit the selection of peaks to modes inside the horizon delay limit, corresponding to smooth spectrum objects in the visible sky hemisphere.

Figure 4 shows **delay power spectra** from MWA data after deconvolution along the delay axis. The principal feature is the *foreground wedge*, whose boundaries, marked by white lines, increase linearly with light travel time proportional to baseline length. Note that the wedge is not filled out uniformly. Each baseline has a different orientation that determines the response to different objects in the sky. It is this variation that we will explore below.

The *off-zenith* pointing **has notably higher power in the foreground wedge than in the zenith pointing**. This is shown later in §5.1 to be due to response of the array to the bright Galactic center and Galactic

plane in the westward sky. Consequently, the contamination into the *EoR window* is also higher, especially on short antenna spacings. Emission in the *zenith* pointing is more centrally concentrated **due to a zenith-centered power pattern and faster suppression of response away from zenith**, whereas the *off-zenith* pointing has a power pattern phased eastward of zenith and is also more responsive to emission farther away from the primary lobe relative to that in the *zenith* pointing. **The power pattern is discussed in detail in §4.1.**

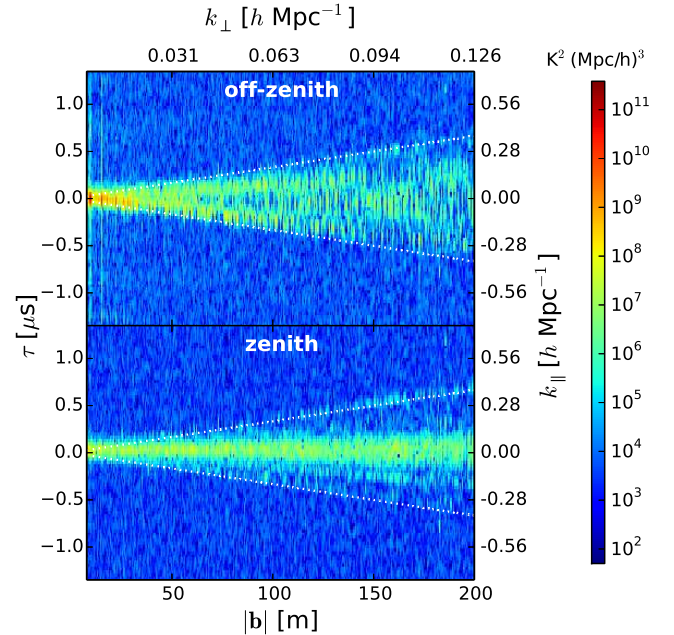


Figure 4. Delay power spectra of two observations of the EoR field (RA = 0^{h} , Dec = -30°) at an *off-zenith* pointing (top) when tiles have significant secondary lobes in the direction of the Galactic center and a *zenith* pointing (bottom) where secondary lobes are minimal and the Galaxy has set. **In both cases, the delay spectra are phased to the zenith and thus the foreground wedge boundaries are symmetric around $\tau = 0$.** For reference, the k -space equivalent of τ and $|b|$, namely, k_{\parallel} and k_{\perp} are shown at the axes on the right and top respectively. White lines mark the boundaries of foreground wedge determined by light travel time across each baseline. Smooth spectrum objects predominantly reside in this foreground wedge. The logarithmic color scale (shown at the right) is common to both panels.

4. SIMULATIONS

We describe the instrumental and foreground models we use in our simulations.

4.1. Instrument Model

The instrument model consists primarily of the tile power pattern, $A(\hat{s}, f)$ (see equation 1). It is modeled as a mutually-coupled 4-by-4 dipole array with the overall power pattern of each individual dipole calculated via finite element electromagnetic simulation (Sutinjo et al. 2014). To speed up simulations, we find that a phased array of isotropic radiators at a height of 0.3 m above an infinite ground plane provides a very good approximation to the full simulation, hence we use the idealized dipoles. We also assume that each individual dipole signal has random delay fluctuations of rms 0.05 ns, a number in

²³ <http://sourceforge.net/p/aoflagger>

line with the known repeatability and stability level of the analog signal chain (Bowman et al. 2007). Besides having the effect of adding a time-dependent uncertainty in the power pattern, these random delay fluctuations reduce the coherence in the phased addition of dipole signals resulting in deviations from predicted models of the power pattern, most prominently at its nulls. The power patterns so obtained are shown in Figure 5 for the pointings chosen in our study.

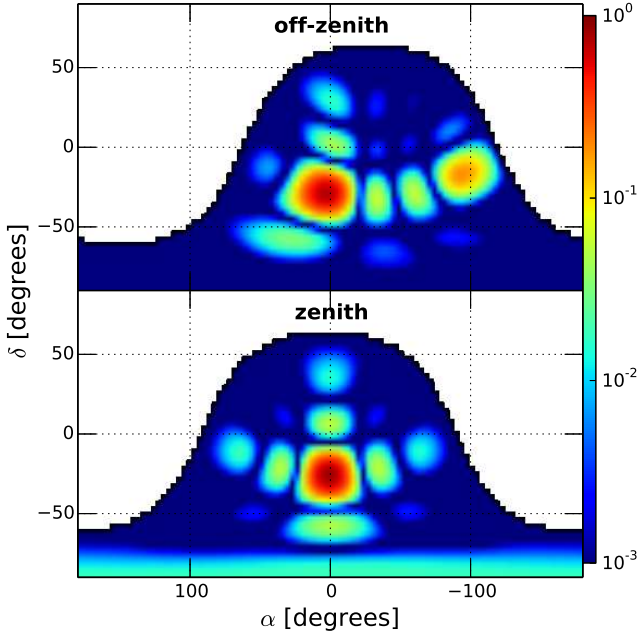


Figure 5. Models of MWA tile power pattern for *off-zenith* (top) and *zenith* pointings (bottom) at 185 MHz. An MWA tile is modeled as a 4×4 array of isotropic radiators placed 0.3 m above an infinite ground plane. Random fluctuations of rms 0.05 ns have been added to delay corrections during the phased addition of voltages from these isotropic radiators. The logarithmic color scale (shown on the right) is common to both panels.

Estimation of T_{sys} from MWA data is a subject of active investigation. For our work, we estimate thermal noise in the data using the rms of $V_{b\tau}$ obtained after *delay-deconvolution* across all antenna spacings for $|\tau| \geq 1 \mu\text{s}$ using the relations:

$$\Delta V_{b\tau}^{\text{rms}} = \sqrt{N_{\text{ch}}} \Delta V_{bf}^{\text{rms}} \Delta f, \text{ and} \quad (10)$$

$$\Delta V_{bf}^{\text{rms}} = \frac{2 k_B T_{\text{sys}}}{A_e \sqrt{2 \Delta f \Delta t}}, \quad (11)$$

where, $\Delta f = 80 \text{ kHz}$, $\Delta t = 112 \text{ s}$, and $N_{\text{ch}} = \Delta B / \Delta f$ is the number of frequency channels. The choice of threshold for τ is well outside the *foreground window*, where foreground contamination is negligible and thus yields a robust estimate of T_{sys} . We find the average system temperature to be $\sim 95 \text{ K}$ across all frequency channels and across all antenna pairs throughout the course of the observation. Hence, for our simulations, we use $T_{\text{sys}} = 95 \text{ K}$ to match the thermal noise observed in the data.

4.2. Foreground Model

The MWA has a very wide field of view ($\gtrsim 20^\circ$ at 185 MHz) and has non-negligible response all the way to the horizon. As already noted, foreground objects fill the *foreground wedge* with an amplitude which depends on the tile power gain in that direction, with objects at the horizon being closest to the boundaries of the *wedge*.

The degree to which these objects leak power into the spectral line-of-sight modes in the *EoR window* will be shown to depend primarily on the brightness of foregrounds near the boundaries of the *foreground wedge*. Thus, it is important to consider an all-sky model for foreground objects in evaluating the features seen in the power spectrum instead of restricting only to the primary field of view, a point also supported by Pober et al. (2015, in preparation).

We use an all-sky foreground emission model that includes both diffuse and bright compact components.

4.2.1. Diffuse Foreground Model

For the diffuse component, we use an all-sky radio foreground model (de Oliveira-Costa et al. 2008) to estimate the emission at 185 MHz. At this frequency, since this map is predominantly based on the 408 MHz map of Haslam et al. (1982) which has an angular resolution of 0.85° , we smoothed the 185 MHz map to the same resolution. However, to avoid any artifacts from sampling this map, we sample it at $\approx 27'$ intervals. We model the diffuse foreground spectra with a single spectral index at each pixel in the map, found by comparing model maps at 170 MHz and 200 MHz.

A low resolution version of the diffuse foreground model used is shown in Figure 6. Contours of the MWA tile power pattern shown in Figure 5 are also overlaid. Of notable significance in the *off-zenith* pointing is the presence of a portion of the Galactic plane and the bright Galactic center in the westward sky, where the MWA tile power gain is significant ($\gtrsim 12\%$). In the *zenith* pointing, the Galactic plane has set and the power pattern in that direction is at least 16 times smaller.

4.2.2. Compact Foreground Model

The model described in the preceding section is primarily a model of the diffuse foreground sky. While it contains faint compact emission blended in with the diffuse emission, **bright point sources have been removed** (de Oliveira-Costa et al. 2008). In order to supplement it with missing bright compact emission, we use classical radio source confusion estimates to determine the nominal flux density threshold and include point sources brighter than this threshold. It may be noted that slightly different criteria are in common use in radio astronomy to estimate radio source confusion (see Appendix of Thyagarajan et al. 2013, and references therein). For an angular resolution of 0.85° , using a conservative ' $S_c = 5\sigma_c$ ' criterion, we determine the flux density threshold to be $\approx 10 \text{ Jy}$. Other liberal criteria that yield a lower threshold carry a greater risk of double-counting point sources which might be already blended in with the diffuse sky model.

We use a combination of the NRAO VLA Sky Survey (NVSS; Condon et al. 1998) at 1.4 GHz and the Sydney University Molonglo Sky Survey (SUMSS; Bock et al. 1999; Mauch et al. 2003) at 843 MHz to provide

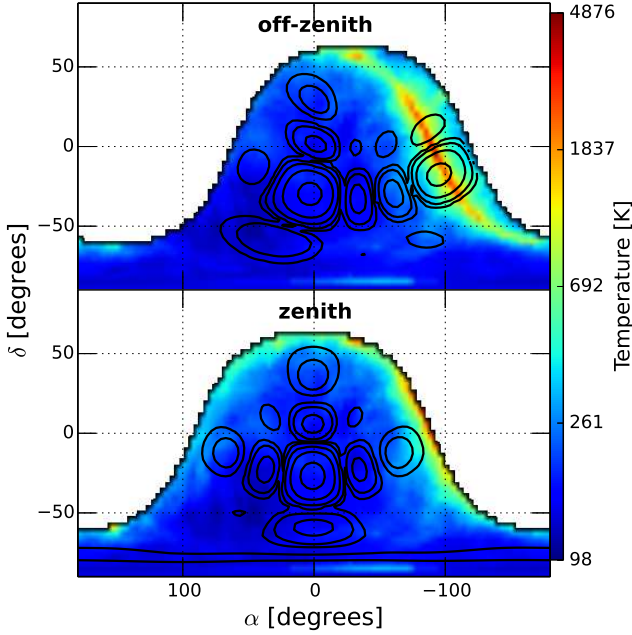


Figure 6. Sky brightness temperature of the diffuse foreground model at 185 MHz visible during *off-zenith* (top) and *zenith* (bottom) pointings. The color scale on the right is logarithmic and is common to both panels. Contours of power pattern shown in Figure 5 are overlaid. The contour levels shown are 0.00195, 0.00781, 0.0312, 0.125, and 0.5. The Galactic center and a portion of the Galactic plane are prominently visible during the *off-zenith* pointing and the MWA tile power gain is significant ($\gtrsim 12\%$) in that direction. In contrast, emission from the Galactic plane in *zenith* pointing is significantly lesser.

our point source catalog due to their complementary survey footprints covering the entire sky, and matched flux density sensitivity and angular resolution. The SUMSS catalog covers the sky with declination $\delta < -30^\circ$ with a limiting peak brightness of 6–10 mJy/beam and an angular resolution of $\sim 45''$. The NVSS covers the sky with $\delta > -40^\circ$ with a similar angular resolution and a limiting flux density of ≈ 2.5 mJy for point sources.

From the SUMSS catalog, we select **objects** whose deconvolved major axes are equal to $0''$, **thereby strictly selecting point sources**. From the NVSS catalog, we excluded objects that overlap with those in the SUMSS survey footprint. Point sources from NVSS were selected if the convolved major axes were not greater than $\approx 47''$, which matches the angular resolution of the survey. Using a mean spectral index of $\langle \alpha_{\text{sp}} \rangle = -0.83$ (flux density, $S(f) \propto f^{\alpha_{\text{sp}}}$) obtained by Mauch et al. (2003) for both NVSS and SUMSS catalog objects, we calculate the corresponding flux densities at 185 MHz, S_{185} . From this subset, we choose point sources with $S_{185} \geq 10$ Jy. The selection of such bright point sources is not affected by minor differences in flux density sensitivity of the two surveys. We verified that our selection criteria ensure a similar areal density of objects in the two surveys.

Based on these criteria, we selected 100 objects from the SUMSS catalog and 250 objects from the NVSS catalog. Together with the diffuse foreground model, we obtain an all-sky foreground model consisting of both compact and diffuse emission. Figure 7 shows the compact foreground emission model used in our study whose contours of the power pattern overlaid. The flux

densities of the point sources are indicated by the color scale.

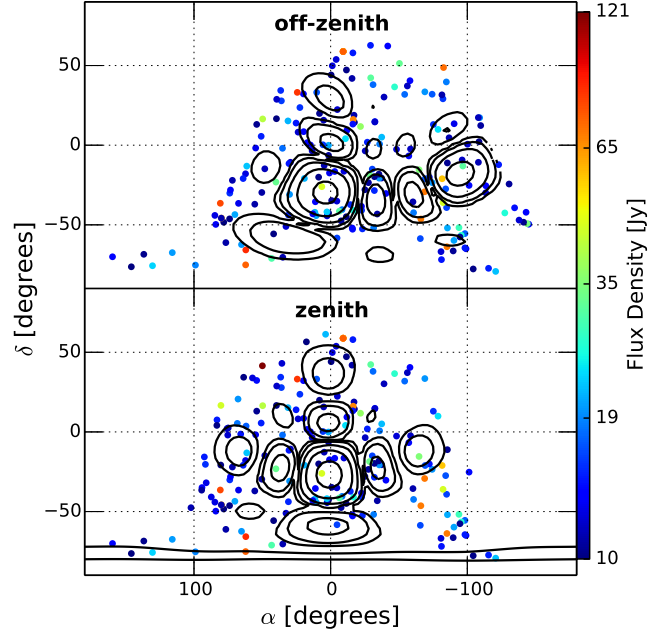


Figure 7. Flux densities of bright point sources at 185 MHz visible during *off-zenith* (top) and *zenith* (bottom) pointings. The color scale on the right is logarithmic and is common to both panels and corresponds to the color-coded filled circles. Contours of power pattern shown in Figure 5 are overlaid. The contour levels shown are 0.001953125, 0.0078125, 0.03125, 0.125, and 0.5.

It is worth emphasizing that the ideal foreground model is one with an angular resolution finer than that of the instrument that covers the whole sky at the observing frequency, a point we will revisit later. For this study, we note that our conclusions are not significantly affected despite minor differences in the thresholds from different radio source confusion estimates.

4.3. Comparison with Data

With the aforementioned foreground model, and instrumental and observational parameters, we simulate visibilities using equation 1. Figure 8 shows the **delay power spectra** from *off-zenith* and *zenith* pointings. Notice the qualitative agreement of amplitude and structure with those obtained from data shown in Figure 4. The Galactic center and the Galactic plane visible in the *off-zenith* pointing make it appear brighter in the *foreground wedge*.

In order to make a quantitative comparison of delay spectra obtained with MWA data and our simulations, we consider the uncertainty in the assumed spectral index of our foreground model. Our foreground models are derived from other higher frequency catalogs and sky maps. The inherent spread in spectral index increases the uncertainty while predicting fluxes at the observing frequency. Using simple error propagation, the fractional error in the delay spectrum **amplitude**, $|V_{b\tau}|$, caused by the spread in spectral index is $\sim \ln(f_{\text{orig}}/f) \Delta\alpha_{\text{sp}}$, where, f_{orig} is the original frequency at which the catalog or map was created, $f = 185$ MHz is the MWA observing frequency, and $\Delta\alpha_{\text{sp}}$ is the spread (HWHM)

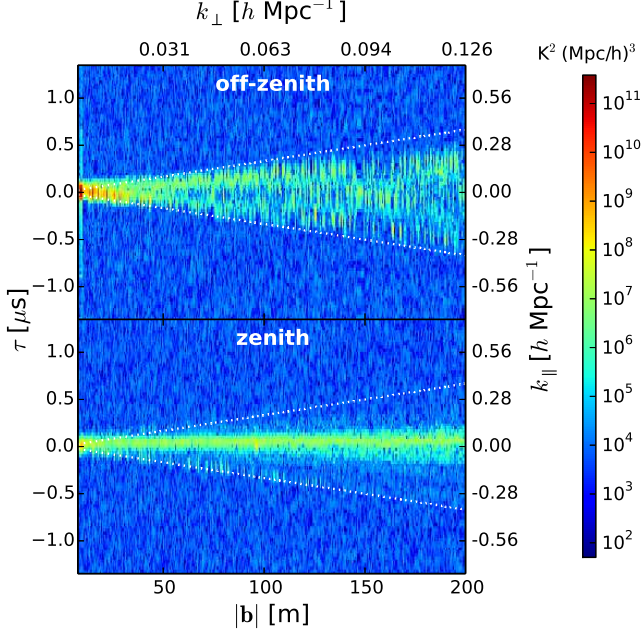


Figure 8. Same as Figure 4, but generated from simulated visibilities using the model described in §4. Note the similarity between the broad features to those in Figure 4.

in spectral index. From Mauch et al. (2003), we assume $\Delta\alpha_{\text{sp}} \approx 0.35$ for point sources from NVSS and SUMSS catalogs. Although the model of de Oliveira-Costa et al. (2008) yields a spectral index per direction on the sky, we could assume similar uncertainties exist in spectral indices of our diffuse sky model as well, which is predominantly derived from the 408 MHz map of Haslam et al. (1982). Thus, fractional errors in delay spectrum **amplitudes** from compact and diffuse components are $\sim 70\%$ and $\sim 30\%$ respectively.

In addition to intrinsic model uncertainty, delay spectra from simulations and data each have fluctuations due to thermal noise in the delay spectrum with rms $\sim 1.4 \times 10^7$ Jy Hz. We estimate the ratio of delay spectra from data and simulations as $\rho = |V_{b\tau}^{\text{D}}(\mathbf{b}, \tau)| / |V_{b\tau}^{\text{S}}(\mathbf{b}, \tau)|$, where superscripts D and S denote data and simulation, respectively. The median absolute deviation of $\log_{10} \rho$ inside the *foreground wedge* for both pointings is ≈ 0.28 . This corresponds to $\sim 90\%$ fractional difference between data and modeling on average with either pointing.

We also simulated delay spectra after assigning spectral indices drawn randomly from a *gaussian* distribution with a mean of $\langle\alpha_{\text{sp}}\rangle = -0.83$ and a HWHM of $\Delta\alpha_{\text{sp}} = 0.35$ to the point sources in our compact foreground model. These simulations typically yielded a median absolute deviation of ≈ 0.29 for $\log_{10} \rho$ indicating fractional differences of $\sim 95\%$. This demonstrates that a fractional deviation of $\sim 90\%$ observed between data and simulations is in line with expectations when the aforementioned uncertainty in foreground models, thermal noise fluctuations in measurements, and uncertainties in antenna power pattern due to random delay fluctuations are taken into account. Currently, we are primarily limited by the unavailability of all-sky foreground models at the observing frequency of 185 MHz.

These uncertainties are presented only to confirm the qualitative agreement already seen between Figures 4

and 8. These estimates are conservative. A full treatment of all uncertainties and deviations from ideal behavior such as frequency dependent errors in tile power pattern (Bernardi et al. 2015), calibration (Datta et al. 2010), data corruption due to interference, anisoplanatic wide-field imaging and ionospheric effects (Intema et al. 2009) will bring the simulations much closer in agreement with observations, but is beyond the scope of this paper. **Hereafter**, our primary objective is to explore in detail the foreground signatures embedded in the *foreground wedge*.

5. RESULTS

Having shown that the simulation matches the data to the level of expected uncertainties, we proceed to examine in further detail the key signatures seen in simulated delay spectra. A number of factors are responsible for the characteristics noted in the delay spectra obtained from data and through simulations. We address these factors below:

- **Sky Model:** Our model of the sky consists of compact and diffuse emission on diverse spatial scales as shown in Figures 6 and 7. It also consists of localized regions of strong emission such as the Galactic plane and Galactic center. In fact, the patch of sky for MWA observations is chosen from regions of low foreground emission. We will investigate the signatures of each component and their potential impact on *EoR window* contamination.
- **Baseline Orientation:** Since the spatial structure of our foreground model is not expected to be isotropic, we divide our antenna spacings by their orientation, θ_b . We use the **four following bins sweeping 45° each**: $-67.5^\circ \leq \theta_b < -22.5^\circ$, $-22.5^\circ \leq \theta_b < 22.5^\circ$, $22.5^\circ \leq \theta_b < 67.5^\circ$, and $67.5^\circ \leq \theta_b < 112.5^\circ$. The bin centers are oriented towards South-East, East, North-East, and North respectively. **While the bin boundaries are arbitrary, they were so chosen to allow bin centers to be aligned along the cardinal and ordinal directions in a half-plane.** Since delays depend on θ_b , binning by θ_b allows us to match **features of the delay power spectra** to different sky directions.
- **Tile Pointing and Power Pattern:** Since the MWA tiles are steered electronically, the tile power pattern tile changes in any observing mode that tracks the **pointing center**. In our study, we take into account the effect of the changing tile power pattern on the **delay power spectra** (Figure 5). The LST of our data ranges from ~ 21 hours through ~ 2 hours, and for our analysis we chose the *off-zenith* and *zenith* pointings shown in Figure 3.

In subsequent sections, we provide a detailed explanation of our results as a combination of factors noted above. Note that numerous features may overlap at different degrees of significance depending on combinations of parameters. We assign the features to their predominant causes. Secondly, we have used noiseless cases to clearly illustrate the observed foreground signatures. With the addition of noise in the visibilities, some of

the weaker features may not be as prominently visible. Since the foreground signatures are far too numerous **and subject to a multitude of parameters** like baseline length and orientation, power pattern, patch of sky under observation, and instrumental configuration, we highlight only some examples of the most notable features in the delay spectra of foreground emission.

5.1. Diffuse Foreground Signatures

Figure 9 shows the **delay power spectra** simulated with only the diffuse foreground model. The top and bottom panels correspond to *off-zenith* and *zenith* pointings, respectively.

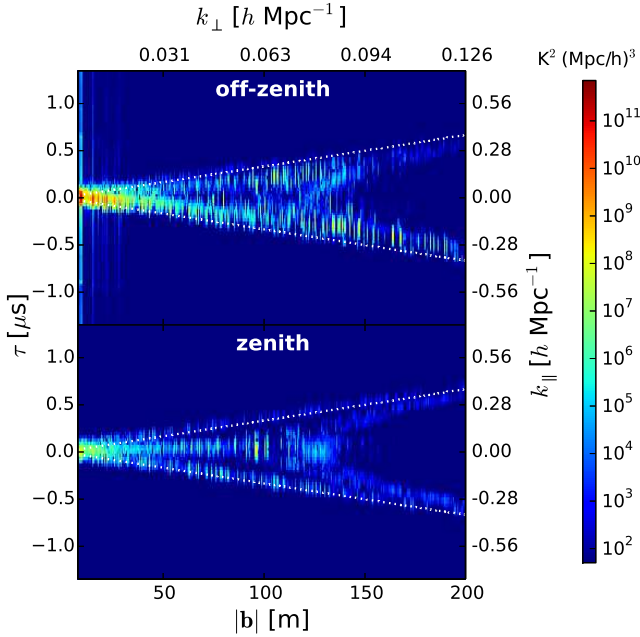


Figure 9. Simulated delay power spectra (in units of $K^2 \text{ (Mpc/h)}^3$) for *off-zenith* (top) and *zenith* (bottom) pointings for the diffuse foreground model without any thermal noise. White lines mark the boundaries of the *foreground wedge* determined by the horizon delay limit and antenna spacing. The axes and color scale are identical to those in Figures 4 and 8. In the *zenith* pointing, **delay power spectrum** from diffuse emission has a *two-pronged fork*-shaped structure and is present even at wide antenna spacings.

Here we examine in detail some examples of interesting features observed with the diffuse foreground model.

5.1.1. Galactic Center on Eastward Antenna Spacings

The most prominent signature seen in the *off-zenith* pointing (top panel of Figure 9) is due to the bright Galactic center situated on the western horizon co-located with one of the bright secondary lobes of the power pattern. It appears as a bright branch near the negative delay horizon delay limit. This feature is strongest at short antenna spacings and fades with increasing antenna spacing. The **bright** signature is absent in the *zenith* pointing (bottom panel, Figure 9) because the Galactic center is below the horizon.

5.1.2. Diffuse Emission Delay Spectra

Figure 9 also shows diffuse emission in the **primary field of view** manifesting in the *off-zenith*

pointing as a branch at $\tau > 0$, and at $\tau = 0$ in the *zenith* pointing. The former is seen at $\tau > 0$ because the primary lobe of the power pattern is centered eastward of zenith, whereas in the latter it is centered at zenith. As we see from Equation 1, each baseline measures a single spatial mode on the sky with an angular size scale inversely proportional to the length of the baseline projected in the direction of the emission. Thus, in the *zenith* pointing, the signature of the smooth sky model, the horizontal line at $\tau = 0$, fades away on antenna spacings $|b| \gtrsim 125 \text{ m}$ because the sky model is devoid of spatial structures on scales $\lesssim 0.75^\circ$.

5.1.3. Diffuse Emission on Wide Antenna Spacings

In typical radio interferometric measurements, due to the Fourier relation between sky brightness and measured visibilities, only short antenna spacings are sensitive to emission from large size scales such as the diffuse component in our study (angular scales $\gtrsim 0.85^\circ$). However, we note a very interesting signature of diffuse emission revealed at regions near the positive horizon delay limit in the *off-zenith* pointing, and at both horizon delay limits in the *zenith* pointing even on wide antenna spacings ($125 \text{ m} \lesssim |b| \leq 200 \text{ m}$). This is a consequence of wide-field measurements, where long baselines are foreshortened due to projection effects towards off-axis emission, especially near the horizon. Consequently, they become sensitive to diffuse emission on large size scales. This holds for short baselines as well and is evident at all LSTs in our simulations. Thus, diffuse emission from far off-axis directions manifests as an edge-heavy *two-pronged fork* across all baselines. It decreases in strength with increasing baseline length as expected but is present in all baseline orientations.

Thyagarajan et al. (2013) and Poher et al. (2013) have found a similar feature in their simulations and data respectively. In the latter, this feature is described as “edge brightening” and attributed to the Galactic plane near the horizon. From their discussion, it is unclear what fraction of power in that feature arises from ubiquitous diffuse emission. On the other hand, Thyagarajan et al. (2013) statistically modeled point sources below the confusion limit and attributed the feature to an increase in solid angles subtended by delay bins closer to the horizon limits thereby, enhancing the resulting integrated emission. This must be true for diffuse emission as well. Thus we argue the feature arises primarily due to an increase in sensitivity of long baselines to diffuse emission caused by foreshortening towards angles far off-axis. Consequently, the increased size scales (or solid angles) containing higher levels of integrated emission, and spatial scales inversely proportional to the foreshortened baseline lengths become matched.

5.2. Compact Foreground Signatures

Figure 10 shows the **delay power spectra** of the compact foreground sky model (see Figure 7) for *off-zenith* and *zenith* pointings in the top and bottom panels, respectively. In contrast to the **delay power spectra** of

diffuse emission, compact emission manifests as a center-heavy structure in either pointing.

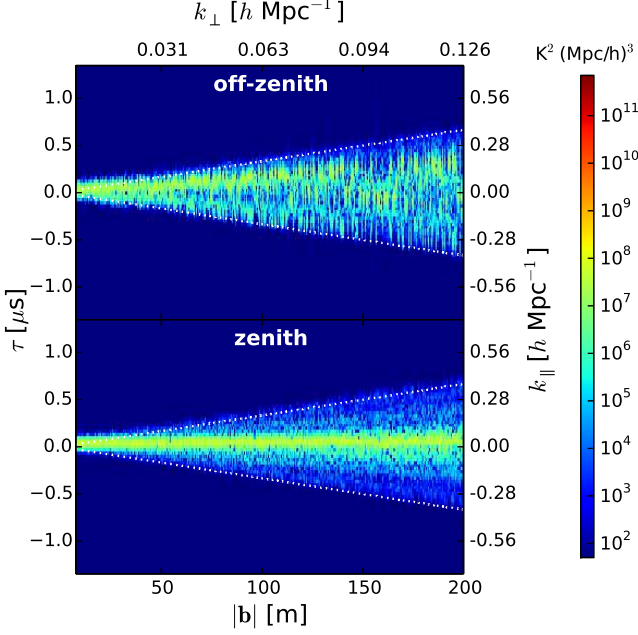


Figure 10. Same as Figure 9 but for a foreground model consisting of compact emission. Compact emission gives rise to centrally concentrated features and stays flat across antenna spacings in the foreground wedge.

The amplitude response of an interferometer to a point source is, to first order, flat with respect to baseline length. Since the primary lobe of the power pattern in the *off-zenith* pointing is centered eastward of zenith, the bulk of the compact foreground emission is seen in a branch with $\tau > 0$ corresponding to the position of the primary lobe of the power pattern. In the *zenith* pointing, compact emission from the same patch of sky is seen as a bright horizontal arm at $\tau = 0$ since the primary lobe of the power pattern is centered at zenith.

Foreground emission at $\tau = 0$ and $\tau < 0$ in the *off-zenith* pointing is caused by point sources co-located with secondary lobes of the power pattern. On the other hand, point sources co-located with secondary lobes of power pattern in the *zenith* pointing are revealed as faint but distinct branches at positive and negative delays depending on the orientation of antenna spacing and direction of emission on the sky.

5.3. The “Pitchfork”

Delay spectra from the foreground model in our study display a composite feature set drawn from the features of compact and diffuse foreground models. Here we compare the relative strengths of emission from different spatial scales in our composite foreground model.

When not dominated by the bright emission from the Galactic center, which happens only for certain pointings at certain times, the **delay power spectrum** of the combined foreground model is composed of diffuse and compact emission, **both of which are significant**. This is illustrated by a more detailed examination of the *zenith* pointing in our study.

Figure 11 shows delay spectra of three antenna pairs of different antenna spacings oriented northward during the *zenith* pointing; each is a different vertical slice of the two dimensional **delay power spectra** plots shown in Figures 4, 8, 9, and 10. The diffuse, compact, and composite components are shown as solid red, cyan, and black lines, respectively. The horizon delay limits are shown as a pair of vertical dotted lines. The gray shaded area denotes the envelope of expected uncertainty in the **delay power spectrum**. Uncertainty in emission in the *foreground wedge* (between the horizon delay limits) is dominated by the uncertainty in predicting the spectral index of compact foreground model, while thermal noise fluctuations dominate outside.

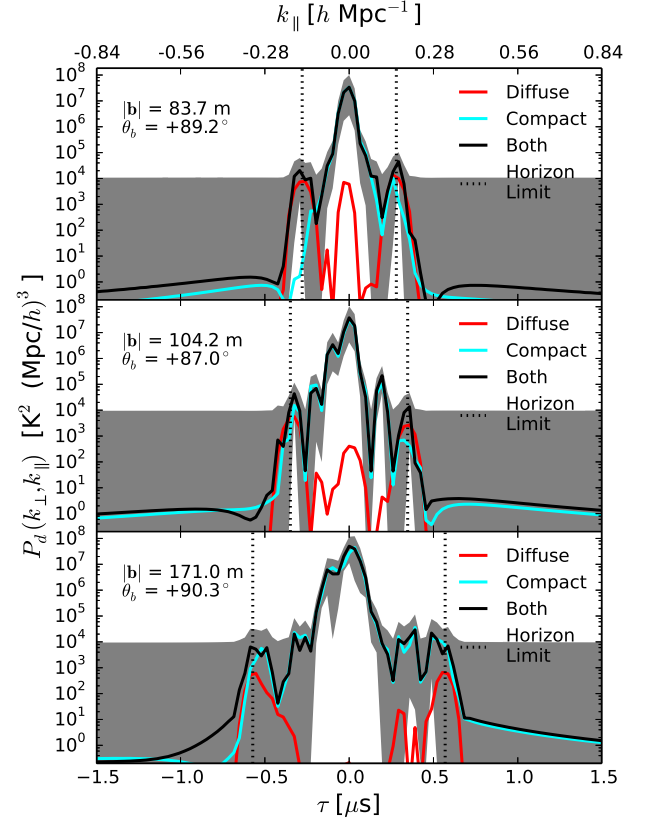


Figure 11. Simulated **delay power spectra** for three chosen northward oriented antenna spacings of length: ~ 84 m (*top*), ~ 104 m (*middle*), and ~ 171 m (*bottom*). The antenna spacing is specified in each panel along East, North and Upward directions. The solid red, cyan, and black lines denote contributions from diffuse, compact, and composite foreground models respectively. Vertical dotted lines mark the horizon delay limits. **Compact emission dominates the central regions of the delay power spectra while both components, especially diffuse emission on short antenna spacings, dominate near the horizon delay limits, giving rise to a pitchfork-shaped structure.** The shaded region denotes the envelope of uncertainty around the composite model delay power spectrum. This uncertainty is dictated by uncertainties in spectral indices of foreground models inside the delay horizon delay limits and by thermal noise fluctuations elsewhere.

The peak at $\tau = 0$ (corresponding to the primary lobe in the power pattern) with a value of $\sim 10^7$ – 10^8 $K^2(\text{Mpc}/h)^3$, independent of antenna spacing, is pre-

dominantly determined by compact emission. The corresponding peak at zero-delay from diffuse foreground model is $\sim 10^3$ times fainter and decreases rapidly with increase in antenna spacing. This is the response expected from different antenna spacings towards compact and diffuse emission.

Near the horizon delay limits at shorter antenna spacing, the diffuse component is brighter relative to the compact component. Here, diffuse emission does not decrease as rapidly with increasing antenna spacing as was seen at zero-delay. In fact, even on widely spaced antennas, diffuse emission in the **delay power spectrum** near the horizon delay limits exceeds that in the primary lobe by about three orders of magnitude. We attribute this to apparent shortening of antenna spacings projected in the direction of diffuse emission entering far from the primary field of view, thereby giving rise to the edge-heavy *two-pronged fork* feature discussed in §5.1.3.

Simulations with the complete foreground model show the combination of center-heavy features on all antenna spacings from compact emission, and edge-heavy features from both compact and diffuse emission especially the latter even on wide antenna spacings. This results in a characteristic *pitchfork* structure imprinted in the *foreground wedge* and should be evident in observations.

All these observations are consistent with those from Figures 9 and 10. The observability of the *pitchfork* signature predicted in this paper depends on the relative levels of uncertainty in the foreground model and fluctuations from thermal noise. In our simulations, since thermal noise in these very short duration snapshots is $\sim 10^4 \text{ K}^2(\text{Mpc}/h)^3$ and features near the horizon delay limits are also of comparable amplitudes, the *pitchfork* feature is not expected to be detected in a noisy scenario although this feature is marginally visible in the *zenith* pointing of observed data (see Figure 4). We attribute this to differences between our foreground model and the actual sky. Deeper observations should reveal the feature clearly.

We also note that increasing the antenna spacing results in progressively improving the resolution along the delay axis by increasing the number of delay bins inside the *foreground wedge*. This improves the localization of foreground objects whose signatures are imprinted in the **delay power spectrum**. For instance, there is an increase in the number of secondary peaks in the **delay power spectrum** between zero-delay and horizon delay limits as the antenna spacing increases from $\sim 84 \text{ m}$ to $\sim 171 \text{ m}$. In this case, these correspond to secondary lobes of the power pattern that lie between the primary lobe and the horizon along the local meridian. At short antenna spacings, due to relatively lower resolution along the delay axis inside the *foreground wedge* and a consequent loss of localization of foreground emission, these secondary peaks blend in with other major peaks and are not distinctly visible. These findings are consistent with the discussion in §5.2.

In summary, the brightest feature $\sim 10^{12} \text{ K}^2(\text{Mpc}/h)^3$ is that of the Galactic center in the *off-zenith* pointing co-located at a westward secondary lobe with a significantly high gain. The next brightest signature $\gtrsim 10^8 \text{ K}^2(\text{Mpc}/h)^3$ is caused by compact emission appearing to be concentrated in the inner regions of the *foreground wedge* (around $\tau = 0$) rather than towards the

boundaries. Diffuse emission co-located at the primary lobe of the power pattern is $\sim 10^3$ fainter relative to compact emission from the same region for a $\sim 84 \text{ m}$ antenna spacing. But unlike the latter, diffuse emission decreases rapidly by over four orders of magnitude as the antenna spacing is widened to $\sim 171 \text{ m}$. However, diffuse emission is significantly higher near horizon delay limits compared to that in the primary lobe of the power pattern as the antenna spacing is increased. This leads to edge-heavy features in the **delay power spectra**. Complemented by the center-heavy compact foreground features, we predict the presence of a *three-pronged pitchfork*-shaped signature in the **delay power spectrum** of the foreground sky. We identify evidence for presence of this signature in actual MWA data, although deeper observations are needed to more clearly reveal the effect.

6. APPLICATIONS

Here, we will investigate the susceptibility of particular antenna spacings to foreground contamination arising out of bright foreground objects located near the horizon and present a technique to substantially mitigate such contamination.

The Galactic center in the *off-zenith* pointing is one such example already available in our study. Figure 12a shows the sky model (*top*: compact component, *bottom*: diffuse component) in this pointing. The Galactic center is the most dominant source of foreground contamination from the diffuse sky model and is co-located with a bright secondary lobe of the power pattern near the western horizon. Figure 12b shows the sky mapped to delays registered by the baseline vectors, of length 100 m for instance, oriented northward (top panel) and eastward (bottom panel). Since the Galactic center is located in the western sky, this figure demonstrates that it is observed at $\tau < 0$ on a baseline vector oriented eastward and at $\tau = 0$ on a baseline vector oriented northward. Figure 12c shows the delay spectra on baselines oriented northward ($67.5^\circ \leq \theta_b < 112.5^\circ$) at the top and eastward ($-22.5^\circ \leq \theta_b < 22.5^\circ$) at the bottom. The Galactic center manifests itself most distinctly near the negative horizon delay limit on short eastward baselines in the **delay power spectrum** (bottom panel of Figure 12c). Consequently, the spillover caused by the instrument's spectral transfer function from the *foreground wedge* into the *EoR window* affects the northward baselines the least and is most severe in eastward baselines (particularly the short ones) evident by the bright vertical stripes of foreground contamination.

The **delay power spectrum** not only carries information on spatial scales of foreground emission but also offers the unique advantage of viewing the sky through a combination of antenna spacing vectors and the delay axis. With a foreground model known *a priori* in which structures and locations of very bright foreground objects such as the Galactic center or AGN are available, we can predict their response across antenna spacings as a function of observing parameters such as LST, power pattern, etc. This allows us to programmatically screen data for antenna spacings that are severely contaminated by foregrounds near the horizon delay limits. These can be weighted appropriately during data analysis. We demonstrate such a screening technique, whereby we use the bright object's location and structure to discard antenna

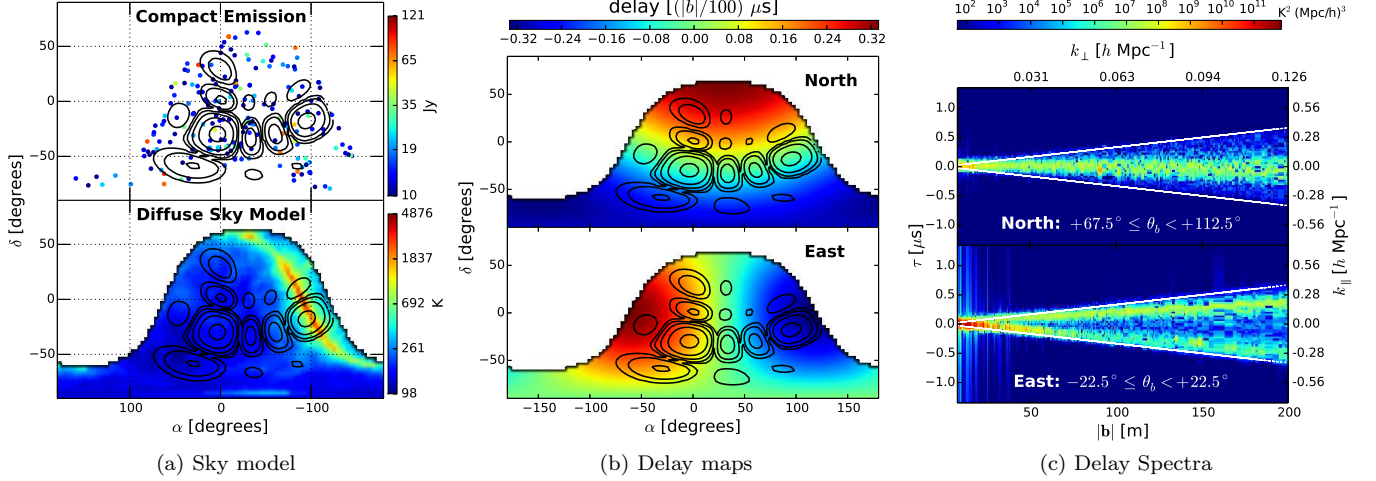


Figure 12. (a): Sky model showing compact (*top*) and diffuse (*bottom*) emission. Contours of power pattern are overlaid whose levels are identical to those in Figures 6 and 7. The Galactic center is very prominent in diffuse emission in the western sky and is co-located with a bright secondary lobe of the power pattern. (b): Sky hemisphere mapped to delays observed on antenna spacings with northward (*top*) and eastward (*bottom*) orientations. Color scale shown is for a 100 m antenna spacing. Delays vary linearly with antenna spacing length. The bright Galactic center in the western sky is recorded at $\tau = 0$ in northward antenna spacings and close to negative horizon delay limit on eastward antenna spacings. (c): Simulated delay spectra **power** on antenna spacings oriented northward (*top*) and eastward (*bottom*). White lines denote horizon delay limits. The bright Galactic center is prominently visible close to negative horizon delay limit, especially on short eastward antenna spacings. These are also the most severely contaminated by foreground spillover. The northward antenna spacings, on the other hand, are the least contaminated.

spacings of certain lengths and orientations to mitigate foreground contamination in the *EoR window*.

In our example, we discard eastward antenna spacings ($-22.5^\circ \leq \theta_b < 22.5^\circ$) of lengths $|\vec{b}| < 30$ m. **This was found to be the limit beyond which foreground contamination levels are insensitive to any further removal of wider antenna spacings.** Figure 13 shows the delay spectra obtained with all antenna spacings (top panel) and after applying our screening technique (bottom panel) on the *off-zenith* observation. Notice the remarkable reduction in foreground spillover into the *EoR window* via the removal of bright vertical stripes on short eastward antenna spacings. The color scale range has been adjusted relative to the previous figures to show this significant reduction in foreground contamination.

This screening technique can be generalized to optimize between foreground mitigation and loss of sensitivity from discarding data. Figure 14 shows how the typical foreground contamination²⁴ in the *EoR window* depends on the orientations and lengths of discarded antenna spacings. We choose antenna spacings oriented eastward to varying degrees of directedness, i.e., $-7.5^\circ \leq \theta_b < 7.5^\circ$ (solid circles), $-15^\circ \leq \theta_b < 15^\circ$ (solid squares), and $-22.5^\circ \leq \theta_b < 22.5^\circ$ (solid stars). Among antenna spacings that satisfy these criteria, we discard data from those whose lengths are shorter than $|\vec{b}|_{\text{max}}$ (x -axis) and show foreground contamination estimated in the *EoR window* from all remaining antenna spacings. In other words, these plots demonstrate the progress in mitigation as orientation and maximum length of discarded antenna spacings are varied. The fraction of discarded antenna spacings discarded relative to the total number is shown in dotted lines for different ranges of θ_b . It is seen that foreground contamination can be mit-

²⁴ Foreground contamination is measured by standard deviation of noiseless $P_d(\mathbf{k}_\perp, k_\parallel)$ from foregrounds in the *EoR window*.

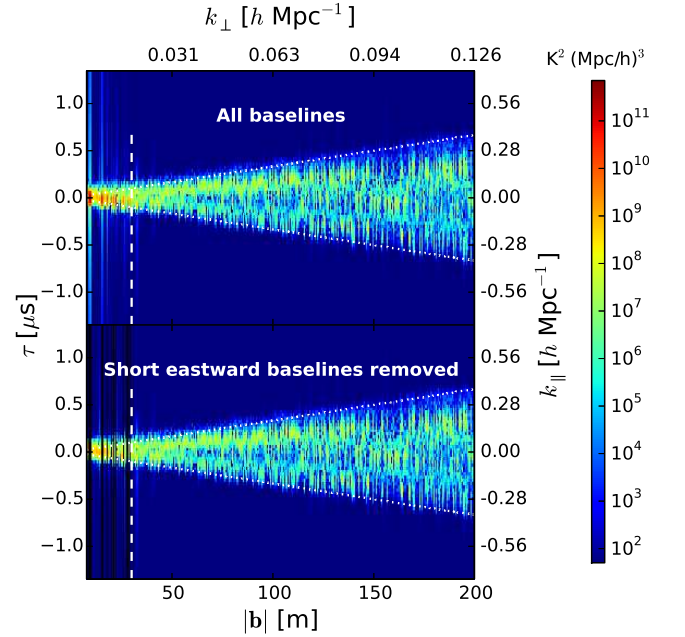


Figure 13. Simulated delay spectra **power** for the *off-zenith* pointing with all antenna spacings included (*top*) and with short eastward antenna spacings discarded (*bottom*). Discarded antenna spacings (black vertical stripes) have lengths $|\vec{b}| < 30$ m (leftward of vertical dashed line) and orientations $|\theta_b| < 22.5^\circ$. The spillover from the bright Galactic center near the negative horizon delay limit from the *foreground wedge* prominent when all antenna spacings are used is lowered by **nearly two orders** of magnitude when short eastward antenna spacings are discarded. Color scale has been adjusted to emphasize mitigation achieved in foreground contamination.

igated by a factor between ~ 2 ($|\theta_b| \leq 7.5^\circ$) and ~ 100 ($|\theta_b| \leq 22.5^\circ$). The latter limit is achieved with a mere 5% loss of data for $|\vec{b}|_{\text{max}} \simeq 30$ m. And discarding antenna spacings with lengths $|\vec{b}| \gtrsim 30$ m does not mit-

igate foreground contamination any further and would only lead to loss of sensitivity as the fraction of discarded baselines increases from $\sim 5\%$ to $\sim 25\%$. On the other hand, a bright point source at the same location will give rise to foreground contamination even on longer antenna spacings. Such cases will necessitate discarding more or, in the worst case, all of the eastward oriented antenna spacings. These results are specific to the MWA data. In general, the array configuration will be a significant factor in determining such thresholds.

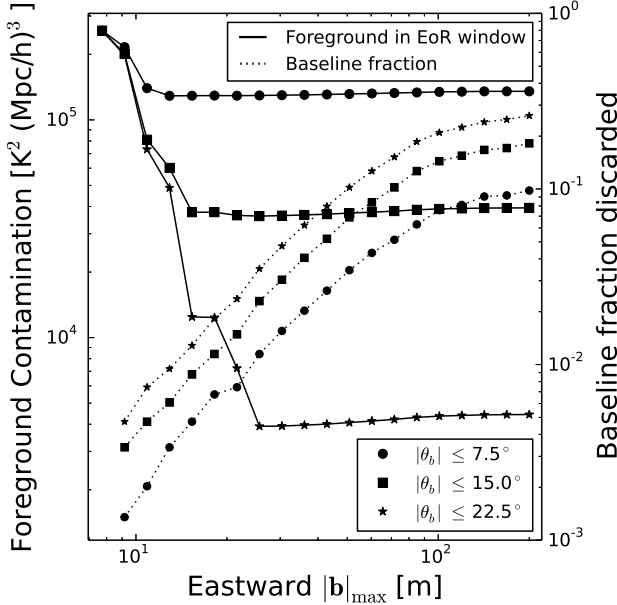


Figure 14. Drop in foreground contamination in the *EoR window*, and loss of data for the *off-zenith* pointing as a function of discarded baselines. Eastward baselines with varying degrees of directedness – $|\theta_b| < 7.5^\circ$ (solid circles), $|\theta_b| < 15^\circ$ (solid squares), and $|\theta_b| < 22.5^\circ$ (solid stars) – and lengths $|b| \leq |b|_{\max}$ (x -axis) are discarded. Loss of data (dotted lines) is measured by discarded baselines as a fraction of the total number for the corresponding cases. Foreground contamination in the *EoR window* (solid lines) drops by a factor ~ 2 ($|\theta_b| \leq 7.5^\circ$) to ~ 100 ($|\theta_b| \leq 22.5^\circ$). The latter limit can be achieved with a mere 5% loss of data at $|b|_{\max} \simeq 30$ m, and discarding longer baselines ($|b| \gtrsim 30$ m) has no effect in further reducing foreground contamination.

In principle, instead of discarding selected antenna spacings altogether, we could down-weight them based on an optimal scheme. For instance, the estimates of covariance computed from the delay transform bins can be naturally fed into the covariance-weighted power spectrum estimation techniques (Liu et al. 2014a,b). It could also be used to downweight or flag contaminated baselines in imaging applications. This technique provides a very simple and yet effective tool in adding a layer of control to mitigate effects of foreground contamination in EoR data analysis.

7. ROLE OF ANTENNA GEOMETRY

We now examine the influence of the antenna power pattern on the delay power spectrum (refer to equations 1 and 2). In the following analysis, we assume an ideal flat passband over the entire 30.72 MHz bandwidth while still applying

a *Blackman-Harris* window function. We also assume there are no random delay fluctuations in the MWA tile beamforming process.

7.1. Uniformly Illuminated Sky

Simulations of the response to a uniformly illuminated sky confirm that the *pitchfork* effect is independent of the specific foreground model chosen in our study. The brightness distribution on the sky was fixed to be a constant equal to the mean over the whole sky at 185 MHz with no spectral variation. This helps isolate the signatures of the antenna power pattern from those of the foregrounds.

Naïvely, only single element antennas are sensitive to a uniform brightness distribution while interferometers are not. However, an examination of equation 1 shows it resembles a Fourier transform when the sky brightness is expressed in a coordinate system of direction cosines (Taylor et al. 1999; Thompson et al. 2001). In such a framework, the solid angle subtended by a unit interval in direction cosine increases as the secant of the angle away from zenith, which is significant in wide-field measurements. A uniformly illuminated sky does not appear so in this frame. Therefore, a uniformly illuminated sky will excite wide-field interferometers.

Figure 15 shows the delay power spectra of such a sky model with the model power pattern of an ideal MWA tile. Although not identical, these delay power spectra closely resemble those obtained with the diffuse sky model (see Figure 9). This indicates that the delay power spectra seen from diffuse foregrounds is primarily explained by those of the underlying power pattern, with any additional variations arising out of anisotropic deviations of the diffuse foreground model from a uniformly illuminated sky.

The edge-heavy *two-pronged* features are evident, which are very similar to those seen earlier in the case of diffuse emission. As reasoned in §5.1.3, the foreshortening of long baselines causes them to be sensitive to emission from near the horizon.

Branches of foreground power seen at $\tau > 0$ and close to the negative horizon delay limit in the *off-zenith* pointing correspond to radiation received from the direction of the primary lobe and the far eastward sidelobe, respectively, in the power pattern. On the other hand, the symmetry of the delay power spectrum around $\tau = 0$ seen in the *zenith* pointing is as expected from a symmetric power pattern.

7.2. Experiments with Aperture Shapes

The power pattern of an antenna is determined by the shape of its aperture. Through the use of a few examples, we examine the role the geometrical shape of the aperture plays in shaping the characteristics of delay power spectrum. We consider the following antenna elements placed at the MWA tile locations:

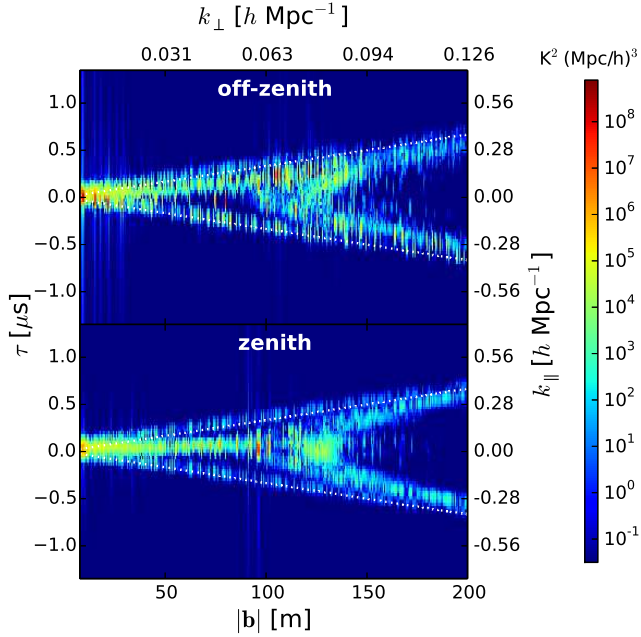


Figure 15. Similar to Figure 9 but for a uniform sky brightness model. The features bear a close resemblance to those obtained with the diffuse emission model. The edge-heavy *two-pronged* features arise from foreshortening of baselines which increases their sensitivity to emission from larger size scales from near the horizon. The symmetries around $\tau = 0$ or lack thereof correspond to symmetries in the power patterns of the respective pointings (see Figure 5).

- **Dipole:** An East–West dipole of length 0.74 m at a height 0.3 m above a ground plane. $A_e = (\lambda/2)^2$.
- **Phased Array:** A 4×4 array of isotropic radiators at a height 0.3 m above the ground plane placed in an arrangement similar to that in an MWA tile. $A_e = 16 (\lambda/2)^2$.
- **Dish:** Diameter of 14 m similar to that proposed for HERA, with $A_e \approx 154 \text{ m}^2$. The power pattern is simulated using an *Airy* pattern where its sensitivity beyond the horizon is forced to zero.

The power patterns of these antenna geometries at 185 MHz for the *zenith* pointing are shown in Figure 16a. It must be noted that the presence of a ground plane below the dipole and the phased array introduces a smoother suppression of sensitivity near the horizon, whereas this transition is abrupt in the case of the dish.

The delay power spectra for these antenna shapes are shown in Figure 16b. The occupancy of the power patterns in the sky hemisphere is clearly correlated with that in the delay spectra. The following visual correlations are also apparent — the strength of the primary lobe centered on the pointing center is correlated with the delay power spectrum centered on $\tau = 0$; and, the overall rate of decrease in the power sensitivity away from the pointing center is correlated with the rate of drop in power away from $\tau = 0$.

The levels of foreground contamination in the *EoR window* varies substantially across the different antenna shapes: $\sim 10^4 \text{ K}^2 (\text{Mpc}/h)^3$, $\lesssim 10^2 \text{ K}^2 (\text{Mpc}/h)^3$, and $< 1 \text{ K}^2 (\text{Mpc}/h)^3$ while using a dipole, phased array, and a dish, respectively. The severity of foreground contamination inside the *foreground wedge* both in strength and occupancy also evidently decreases as the antenna element is changed from a dipole to a phased array to a dish. For instance, notice that the foreground contamination in k -modes between the $k_{\parallel} = 0$ and the horizon limits decreases from $\sim 10^5 \text{ K}^2 (\text{Mpc}/h)^3$ in a phased array to $\sim 10 \text{ K}^2 (\text{Mpc}/h)^3$ in a dish. As a consequence, k -modes in the *foreground wedge* that may be deemed too contaminated for EoR studies in the case of a dipole or a phased array can potentially become accessible when using a dish.

Finally, a distinct feature common to all these aperture shapes is that the foreground contamination near the horizon delay limits even on wide antenna spacings is significant ($\gtrsim 10^5 \text{ K}^2 (\text{Mpc}/h)^3$). This is contrary to expectation for two reasons — the power pattern of the antenna near the horizon is negligible compared to the primary lobe region; and, a significant fraction of foreground emission near the horizon delay limits on wide antenna spacings arises from diffuse emission, to which usually only short antenna spacings are sensitive. We have argued that baselines are foreshortened towards the horizon and thus become sensitive to large size scales, thereby leading to significant integrated emission in delay bins close to the horizon limits. The prevalence of this feature across different antenna shapes demonstrates it is generic to all wide-field measurements, especially in EoR experiments. The amplitude of this effect, however, can be controlled via choice of antenna shape and through weighting of aperture illumination.

8. SUMMARY

Our primary motivation in this work is to understand how the various bright foregrounds will manifest in three dimensional power spectrum of HI from 21 cm reionization observations. When the signal is expressed in units of temperature variance, the dynamic range between bright foregrounds and the 21 cm signal is expected to be $\sim 10^8$; a detailed understanding of how foregrounds can corrupt the 21 cm power spectrum is therefore essential. This analysis extends previous work by simulating the entire sky rather than just the central field of view and by providing a comparison with early observations with the MWA. By making use of the delay spectrum technique to estimate the power spectrum, we are able to observe the effects of foregrounds while avoiding entanglements with more complex power spectrum estimators.

Simulating in many important respects the response of the MWA to an all-sky foreground model that consists of diffuse Galactic emission from de Oliveira-Costa et al. (2008) and bright point sources from the NVSS and SUMSS catalogs, we confirm that the modeled de-

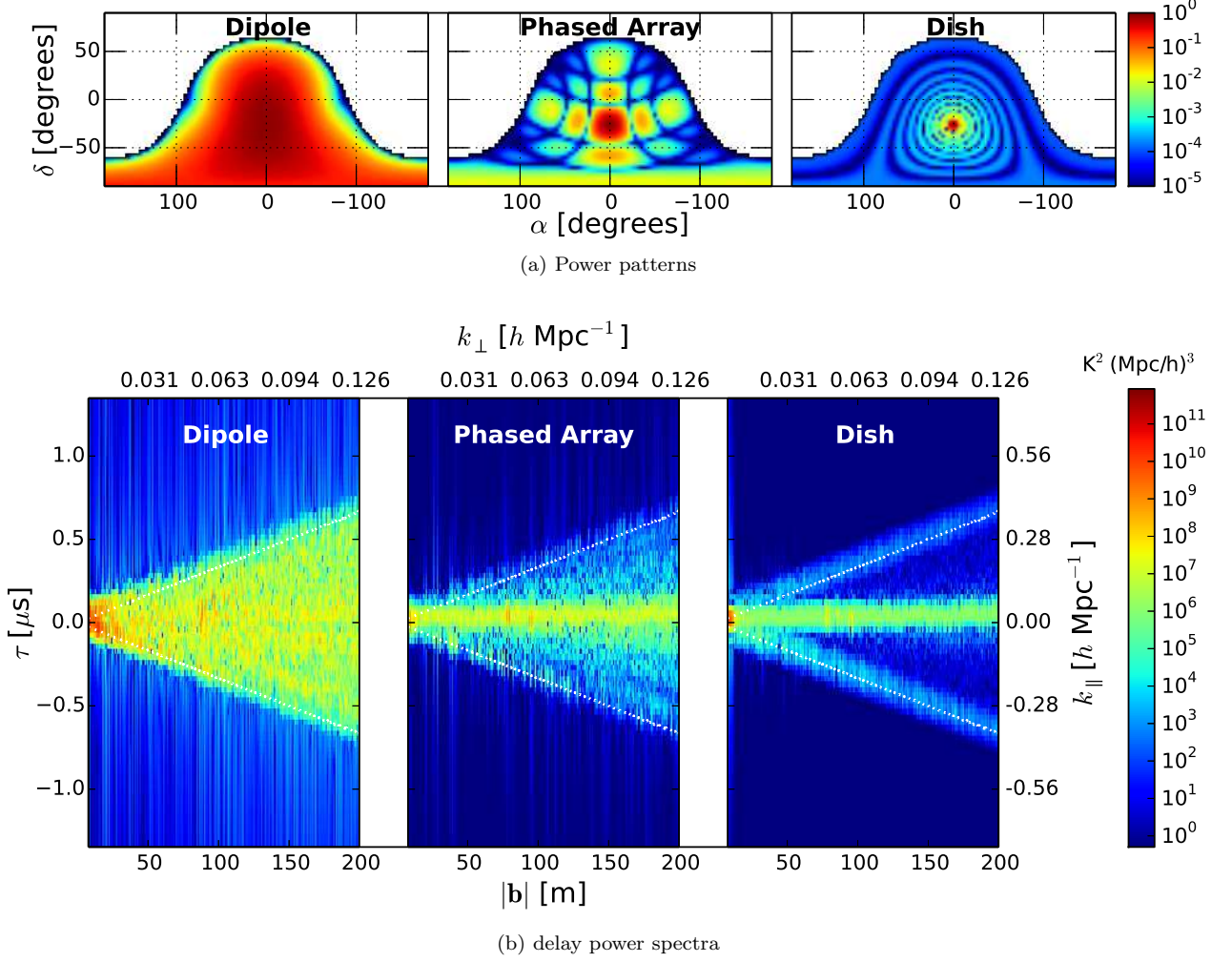


Figure 16. Power patterns (top panels) and simulated delay power spectra (bottom panels) for different antenna shapes at 185 MHz centered on zenith. Antenna shapes used are: dipole (left), phased array (middle), and dish (right). Refer to text for details. The strength and occupancy of the power patterns are correlated with those of delay power spectra. The *foreground wedge* and the *EoR window* are most severely contaminated in the case of the dipole while it is the least for the dish. The phased array has intermediate levels of contamination. Foreground power close to the horizon delay limits in all three cases are significant even on long baselines. The foreshortening of baselines towards the horizon makes them sensitive to foreground emission on large size scales. The amplitude of this feature is highest for the dipole and least for the dish and hence, strongly depends on the shape of the antenna element.

lay spectra are in agreement with data obtained with the MWA, to the extent allowed by levels of uncertainty known in the foreground models and thermal noise fluctuations in measurements.

Our simulations enable us to identify numerous signatures of different components of foreground emission seen in the delay spectra. We establish the relationship between these signatures and observing parameters such as antenna pointing and LST, instrument parameters such as antenna power pattern, and foreground parameters such as the nature of emission, spectral index, etc.

The bright Galactic center at the edge of the western horizon co-located with one of the far secondary lobes of MWA tile power pattern is the brightest source of foreground contamination in the *off-zenith* pointing. It manifests itself near the negative horizon delay limit in the **delay power spectrum** on antenna spacings oriented eastward.

As expected, diffuse emission in the primary lobe of the antenna power pattern is prominent on shorter antenna spacings. However, the most interesting result is

its footprint on wide antenna spacings near the horizon delay limits — an edge-heavy *two-pronged fork*-shaped signature. This is due to apparent shortening of wide antenna spacings in the direction of foreground emission far off-axis, thereby retaining their response to **emission on large size scales**. On the other hand, compact emission predominantly maps onto central regions of the *foreground wedge*. Features arising from compact emission co-located with primary and secondary lobes of the antenna power pattern have been identified. In general, **delay power spectrum** signatures of compact emission are center-heavy, in clear contrast to those from diffuse emission. A composite foreground model consisting of diffuse and compact foregrounds combines the characteristic individual shapes into a *pitchfork*-shaped structure in the *foreground wedge*. This will be distinctly visible when the thermal noise floor is sufficiently lowered, as longer observations are processed through the MWA analysis pipelines. **We conclude the pitchfork feature to be generic to all wide-field measurements, including EoR experiments.**

The role of antenna shape in determining the delay power spectrum was also studied. In contrast to a dipole and a phased array such as an MWA tile, a dish such as the one proposed for HERA is found to yield the least foreground contamination both in the foreground wedge and the EoR window and thus, preferable for EoR studies.

We also provide a simple and effective tool based on the delay spectrum technique **that can potentially mitigate foreground contamination by nearly two orders of magnitude in EoR data analysis by discarding or down-weighting data from antenna pairs most affected by foreground contamination, with negligible loss of sensitivity.** In conclusion, we find that inclusion of emission models, both diffuse and compact, all the way to the horizon is essential to explaining the observed power spectrum.

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