

Assignment 1

Q1)
 $n = 10$
 $10 > 2$
 $12 \cdot 10^{25}$

$$n^{25^k} = 2$$

$$\frac{1}{25} k \log_2 n = 1$$

$$\log_2 n = 25^k$$

$$\log_{25} \log_2 n = k \log_{25} 25$$

$$k = \log_{25} \log_2 n$$

$$\boxed{O(\log(\log n))}$$

Q2)
 $i = 29$
 while i < n:
 $i = i^{23}$

$$\log_n (29)^{23^k} = \log_n n$$

$$\log_n (29)^{23^k} = 1$$

$$23^k \log_n (29) = 1$$

$$\log_n (29) = \frac{1}{23^k}$$

$$\boxed{k = \log_{23} (\log_{29} n)}$$

$$\boxed{O(\log(\log n))}$$

Q3) $i = 1$

while $i < n$:

$$\left\{ \begin{array}{l} i = 2 * i \\ i = 3 * i \end{array} \right.$$

$\rightarrow i = 6 * i$

$n = 40$

$i = 6 * 1$

$i = 6 * 6$

$i = 6 * 36$

$O(\log_6 40)$