

# Course Structure

- 1) Introduction
  - 2) Floating point Representation
  - 3) Basic of Computer system & Microoperations
  - 4) Instruction & Addressing Mode
  - 5) CPU , Data-path & Control unit
  - 6) I/O Organization
  7. Memory & cache
  - 8) Pipelining
- ] C A ] C O

## Basics

### Computer System Architecture

#### \* Sign Magnitude

$\begin{array}{c} S \mid m \mid n\text{-bits} \\ \downarrow \qquad \downarrow \\ \text{Sign} \qquad \text{Magnitude} \\ \leftarrow 0 \text{ +ve} \\ \rightarrow 1 \text{ -ve} \end{array}$	$\begin{array}{rcl} +5 & = & (0101)_2 \\ -5 & = & (\underline{\underline{1}}\underline{\underline{01}})_2 \\ \hline & = & \end{array}$ $\begin{array}{rcl} +0 & = & 0000 \\ -0 & = & 1000 \end{array}$
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#### 1's Complement

$\text{jo } 1 \text{ hai usko } 0 \text{ kro}, \text{ jo } 0 \text{ h usko }$	
$1 \text{ kro}$	$\xrightarrow{\text{most significant bit}} \xleftarrow{\text{least significant bit}}$
$+5 = (0101)$	$(11001) \rightarrow -6$
$-5 = 1010$	$1's \text{ complement}$ $00110 =$

$$+0 = 0000$$

$$+0 = 1111$$

$$\underline{-} \quad \underline{\text{p}} \quad \underline{-} \quad \underline{\text{p}} \quad \underline{-} \quad \underline{\text{p}}$$

\*  $2^{\text{'s}}$  complement

Take the 1's complement of value and plus one

$$+5 = (0101)_2$$

$\Downarrow$   
 $2^{\text{'s}}$  complement

$$\begin{array}{r} 1010 \\ +1 \\ \hline (1011)_2 = -5 \end{array}$$

$$\circ (11010)_2 = -6$$

$$\begin{array}{r} 00101 \\ +1 \\ \hline 00110 = +6 \end{array}$$

$$\underline{-} \quad \underline{\text{p}} \quad \underline{-} \quad \underline{\text{p}} \quad \underline{-} \quad \underline{\text{p}}$$

\* Stored program Architecture

The program which processor executes should be stored in a memory

$\rightarrow$  RAM

\* von-newmann's

\* Harvard  
Howard arch

## \* Floating point Representation

Why is it needed?

Example → 8 - bits

$$\text{Range} = 2^7 + (2^7 - 1) \cdot 2^{\text{1's comp}}$$

$$-128 \text{ to } +127$$

It provides larger range of numbers with limited no. of bits.

The number is represented in format:

S | E | M |

$$S = \begin{cases} 0 & +ve \\ 1 & -ve \end{cases}$$

E = exponent

M = Mantissa (fraction)

- Mantissa is signed normalized fraction (implicit/Explicit)
- Exponent is stored in biased form.

↳ unsigned value/number only

## \* Biased

[S | E | M]

Assume → 5 bits

Transform to unsigned 0 to 31

Range of a number with 5 bits }  $\Rightarrow -16$  to  $+15$  }  $\Rightarrow$

Original exponent (e)	stored exponent (E) excess -16
-16	0
-15	1
-14	2
{	:
0	16
:	,
31	}
+15	

$$E = e + 16 \rightarrow E = e + \text{bias}$$

bias = 16

if  $k$ -bits are used to store  $E \Rightarrow \text{Bias} = 2^k - 1$

### \* Normalization

$\rightarrow$  Explicit normalization  $\Rightarrow 0.10111 \times 2^3$

101.11

$\rightarrow$  Implicit normalization

\* In Explicit, after the point we "must" have "1"

$M = \text{Number after the point} = \frac{10111}{2^3}$   
 $E = 3 + \text{bias}$

In implicit normalization before point we must have '1'.

$$101.11 \longrightarrow 1.0111 \times 2^2$$

$$M = 0111$$

$$c = 2$$

$$E = 2 + \text{bias}$$

→ Explicit is the default normalization.

$$[S|2^{e+\text{bias}}|0111] \text{ explicit}$$

$$\rightarrow [S|2^{e+\text{bias}}|0111] \text{ implicit}$$

- Point is not stored
- Bits before point is not stored
- Base of system not stored

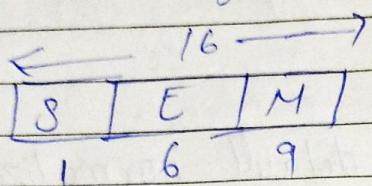
\* Value formula

[Something to the power of 0 is always 1.]

$$\text{Value (explicit)} = (-1)^s \times 0.M \times 2^{E-\text{bias}}$$

$$\text{Value (implicit)} = (-1)^s \times 1.M \times 2^{E-\text{bias}}$$

Q Consider a 16 bit register used to store floating point numbers. The mantissa is normalized signed fraction number. Exponent is represented in excess-32 form. What is the 16 bit value of  $(+19.25)_{10}$  in this register?



$$\text{Bias} = \cancel{32} \quad 32 = 2^k - 1 = 6$$

$$+(19.25)_{10} \quad \text{Sign} = +\text{ve}$$

$$S = 0$$

$$(10011.01)_2 \Rightarrow \text{explicit} = \frac{0.1001101 \times 2^5}{2^5}$$

Normalization

S	E	M	
0	10011	00110100	
↓	↓	↓	↓
4	B	3	4

$$E = 5 + 32 = 37$$

$$\cancel{32} = \\ 37 = (100101)$$

$$M = 1001101$$

$$(4B34)_{16}$$

$$\underline{0x4B34}$$

Representation of hexa decimal

What is the maximum value that can be represented in above register?

[S] E [M] Value =  $(-1)^0 \times 0.1111111 \times 2^{31}$

0 1 - - 1 / - - - - -

$$= (2^9 - 1) \times 2^{-9} \times 2^{31}$$

$$\Rightarrow 511 \times 2^{22}$$

What is the minimum value that can be represented in above register.

[S] E [M] Value =  $+0.1 \times 2^{0-32}$

0 0 0 - - 0 / 0 - - 0

$$= 1.0 \times 2^{-1} \times 2^{-32}$$

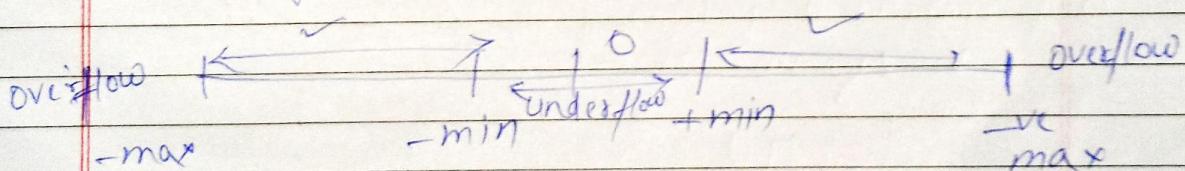
$$= +2^{-33}$$

What is the negative maximum possible value that can be represented above register

[S] E [M] Value =  $-2^{-33}$

1 0 0 - 0 / 0 - - 0

\* Range and precision



More bit in M  $\Rightarrow$  Better Precision

More bit in E  $\Rightarrow$  Better Range

gf cannot store 0

gf cannot store very small values (underflow)