

* PYQ Gate 2023 DL and TOC Lecture 7

Lecture 7

* Finding 1's and 2's complement

Base 2 \rightarrow 2's
 \rightarrow 1's

$$(101011.11)_2$$

$$2^6 - (101011.11)_2$$

2's complement \rightarrow

$$\begin{array}{r} 10000000 \ 00 \\ - 101011.11 \\ \hline 010100.01 \end{array}$$

1's complement

$$\begin{array}{r} 111111.11 \\ - 101011.11 \\ \hline 010100.00 \end{array}$$

* Subtraction using "8" and "(8-1)"'s complement

- why complements? we want to do subtraction using adder circuit.

Base 10

Subtraction using 8's complement

$$\begin{array}{r} 136 \rightarrow \text{minuend} \\ - 53 \rightarrow \text{subtrahend} \end{array} \quad \begin{array}{r} 136 \\ - 053 \end{array}$$

10's complement

$$\begin{array}{r} 1000 \\ - 053 \\ \hline 947 \end{array}$$

$$\begin{array}{r} 136 \\ + 947 \\ \hline 1083 \\ - 1000 \\ \hline 83 \end{array}$$

Ignore
Carry

Take 10's complement of subtrahend and add it to minuend

Case 1) If final carry generated then ans is positive & is given by after ignoring the carry

Case 2) If final carry is not generated then ans is negative and is in 10's complement form.

Case 1 ex

$$\begin{array}{r}
 46 \\
 - 25 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 46 \\
 + 100 \\
 - 25 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 46 \\
 + 75 \\
 \hline
 121
 \end{array}$$

Ignore this \rightarrow ans

Case 2 ex

$$\begin{array}{r}
 25 \\
 - 46 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 25 \\
 + 100 \\
 - 46 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 25 \\
 + 54 \\
 \hline
 79
 \end{array}
 \Rightarrow
 -(100 - 79) = -21 \text{ Ans}$$

Base 2

$$\begin{array}{r}
 101101 \\
 - 001011 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 101101 \\
 + 110101 \\
 \hline
 1100010
 \end{array}$$

Ignore this! \downarrow Ans

2's complement of subtrahend

Rule of 2's Complement Subtraction

Take 2's complement of subtrahend and add it to minuend [match digits]

→ If final carry is generated then ans is positive & is given by after ignoring the carry

→ But if carry is not generated then ans is negative & is 2's complement form.

* Subtraction using (2-1)'s Complement

Base 10

$$\begin{array}{r} 136 \\ - 43 \\ \hline 93 \end{array}$$

$$\begin{array}{r} 136 \\ 999 \\ - 043 \\ \hline \end{array}$$

$$\begin{array}{r} 136 \\ = + 956 \\ \hline 1092 \end{array}$$

$$\begin{array}{r} 092 \\ + 1 \\ \hline 93 \end{array} \quad \text{Ans}$$

end around
Carry

add
carry
in the last

Subtraction using 9's Complement

- Take 9's ^{$\Rightarrow (x-1)$'s} Complement of the subtrahend and add it to minuend
- If final carry is generated [end around carry] ans is positive and is given by this end around carry at the "last place"

$$\begin{array}{r}
 43 \\
 -136 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 43 \\
 999 \\
 -136 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 43 \\
 +863 \\
 \hline
 906
 \end{array}$$

$$(906 - 999) \Rightarrow -(999 - 906) = -93$$

- If carry is not generated then ans is -ve then and is in 9's Complement form. $(x-1)$'s

* Base 2

$$\begin{array}{r}
 1011011 \\
 -0011111 \\
 \hline
 \end{array}
 \Rightarrow
 \begin{array}{r}
 1011011 \\
 1110000 \\
 \hline
 11001011
 \end{array}$$

add here

~~110100~~

1001011

+ 1

1001100 Ans

$$\begin{array}{r}
 0001111 \\
 -1011011 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 0001111 \\
 0100100 \\
 \hline
 0110011
 \end{array}
 \Rightarrow
 \begin{array}{r}
 1111111 \\
 -0110011 \\
 \hline
 1001100
 \end{array}$$