## Assignment 1

Nitin Gangahar

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## Question 1

$$A_N = 1 + \frac{2}{N} \sum_{j=1}^{N} A_{j-1} for N > 0$$
 (1)

Multiplying both sides by N gives

$$NA_N = N + 2\sum_{j=1}^{N} A_{j-1} for N > 0$$
 (2)

This holds for N-1 as

$$(N-1)A_{N-1} = (N-1) + 2\sum_{j=1}^{N-1} A_{j-1} for N > 1$$
(3)

Subtracting the last two

$$NA_N = 1 + (N+1)A_{N-1} \tag{4}$$

Dividing both sides by N(N+1) gives

$$\frac{A_N}{N+1} = \frac{1}{N(N+1)} + \frac{A_{N-1}}{N} \tag{5}$$

Iterating

$$\frac{A_N}{N+1} = \sum_{k=2}^{N} \frac{1}{k(k+1)} + \frac{A_1}{2} \tag{6}$$

Assuming  $A_0 = 0$  as mentioned in the errata and solving the equation gives

 $A_N = N$ 

## Question 2