

Assignment: Design and Simulate the schematic and corresponding optimized layout of an inverter chain with optimized number of inverters to get the minimum delay for a load capacitance of 100 fF.

To find the number of stages

$$D = N f^{1/N} + P \quad [P=N \text{ for } N \text{ no. of stages}]$$

Differentiating with Respect to N

$$\frac{\partial D}{\partial N} = 0 \quad \text{we get}$$

$$-f^{1/N} \ln f^{1/N} + f^{1/N} + P_{inv} = 0$$

$$P_{inv} + \gamma(1 - \ln \gamma) = 0$$

Solving further we get

$$f^{1/N} = 2.718 \quad \text{--- (1)}$$

$$f = f_{MB} = \frac{100 \text{ fF}}{C_{gate}} \quad \text{--- (2)}$$

Input Gate Calculation:

from TSMC Data sheet we get $\alpha_c = 8.58 \times 10^{-3}$

$$\begin{aligned} \text{Ymos} \quad C_{gate} &= 8.58 \times 10^{-3} \times 270 \text{ nm} \times 180 \text{ nm} \\ &= 0.43 \text{ fF} \end{aligned} \quad \left[\begin{array}{l} \text{NMOS} \\ W = 270 \text{ nm} \\ L = 180 \text{ nm} \end{array} \right]$$

$$C_{gate} = 8.58 \times 10^{-3} \times 180 \times 5 \mu m$$

$$= 0.83 \text{ fF}$$

$$C_{gate} = 1.26 \text{ fF}$$

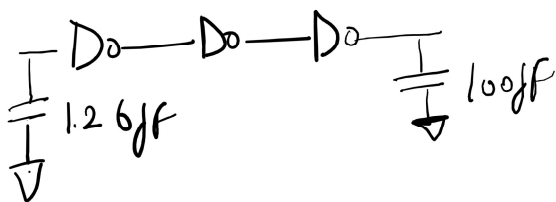
from equation (2)

$$F = 79.36$$

using equation (1)

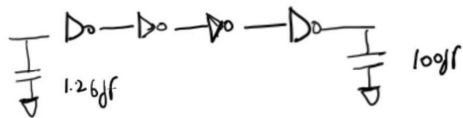
$$M = 3.98$$

for 3 stages



$$P_3 = 15.89$$

for $N=4$ stages:



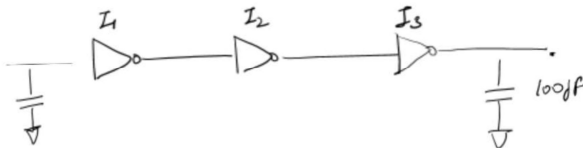
$$D_4 = 15.938$$

$D_3 < D_4$ \rightarrow So three stages will give the optimum results.

Since now we know that there are three stages we can calculate for the best stage effort

Best stage effort: $\sqrt[3]{75.31} = 4.23$

$$D_3 = 15.89$$



$$C_{in1} = \frac{C_{out} \times g_i}{f}$$

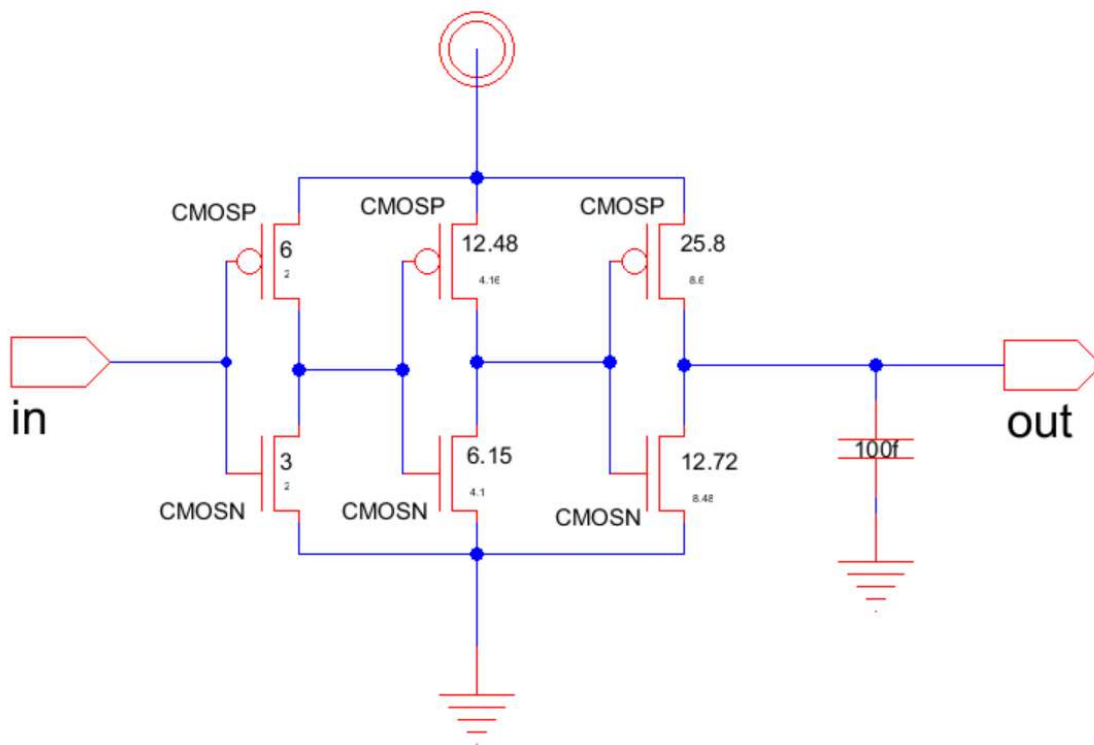
$$C_{in3} = 28.3 \text{ fF}$$

$$C_{in2} = 5.43 \text{ fF}$$

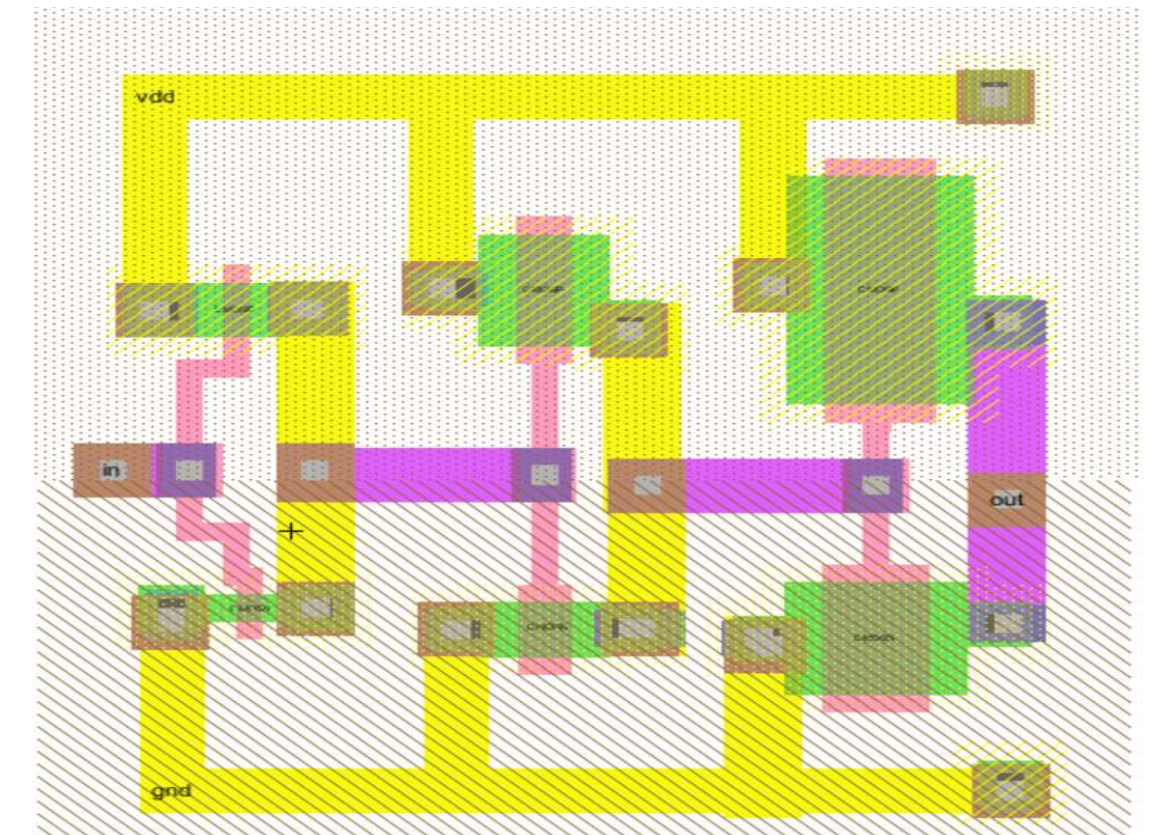
$$C_{in1} = 1.26 \text{ fF}$$

According to this the size of the inverter will be changed

SCHEMATIC



LAYOUT



OBSERVATION MADE:

CIRCUIT	DELAY(SECONDS)
SINGLE INVERTER (SCHEMATIC, CL=100fF)	2.82834e-009
INVERTER CHAIN(SCHEMATIC, CL=100fF)	1.21055e-009
INVERTER CHAIN(LAYOUT)	1.75892e-010

We can clearly observe that the Delay has reduced significantly upon increasing the stages to an optimum level as calculated above.