

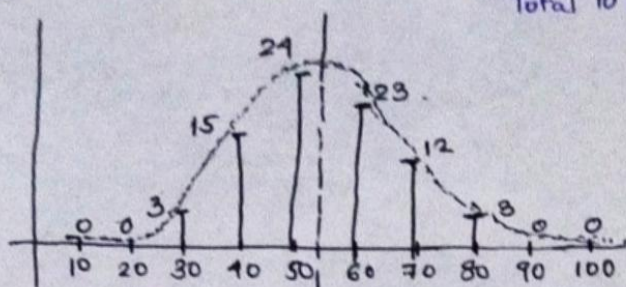
Standard Error of Mean (Standard Error)

Standard Error

- It is a measure of uncertainty in sample mean. Higher the standard error, higher is the uncertainty. High is we are less confident.

Distribution of marks achieved by the students in a class exam. (1 Question → 10 marks)
Total 10 Questions

MARKS	NO OF STUDENT
10	0
20	0
30	3
40	15
50	24
60	23
70	12
80	3
90	0
100	0
Total	80



Population mean.

$$SE(\bar{x}) = \frac{s}{\sqrt{n}}$$

$s \rightarrow$ standard deviation
 $n \rightarrow$ number of samples

Standard error \Rightarrow Population mean \neq Sample mean.

Population mean = 53/51

Sample mean = Most of the high quantity sample are 40, 50, 60, 70.

Q) You want to know the average IQ of statistics students.

Take 5 random students sit in IQ test = [127, 109, 121, 91, 109] $\bar{x} = 112.0$

So, 112 is the average IQ of student. How confident are you? Sample is too small?

Suppose for 50 students, $\bar{x} = 115.3$. How confident are you? Little bit more confident.

Then 500 students, $\bar{x} = 114.7$. I am very much confident.

So, higher the observation, confidence go up and up. So $SE(\bar{x}) = \frac{s}{\sqrt{n}}$ High the value of n , it will decrease SE.

So, for 5 student, suppose SD or $s = 12.72$, then $SE(\bar{x}) = \frac{12.72}{\sqrt{5}} = 5.69$.

n	Sample mean	Std error of sample mean	95% confidence interval
5	112.0	5.69	[96.2, 127.8]
50	115.3	1.74	[108.4, 115.6]
500	114.7	0.55	[110.8, 113.1]

$n = 5$

$\bar{x} = 112$

$SE(\bar{x}) = 5.69$

To find confidence interval, $\bar{x} \pm SE(\bar{x}) \pm t_{0.975, n-1}$

Here we use t test because normally IQ are normally distributed among human being & we use sample.

$= 112 \pm [5.69 \times t_{0.975, 4}] \Rightarrow$ one ans for $+$ and one ans for $-$.
 $= 96.2, 127.8$.

So, we can say that we are 95% confident that true mean lies between 96.2 and 127.8.

SAMPLE ERROR OF PROPORTION

One hundred voters are sampled, and 65 said they were voting for a major party. Find the standard error of sample proportion of major party voters and a 95% confidence interval.

$$p = \frac{65}{100} = 0.65$$

$$SE(p) = \sqrt{\frac{p(1-p)}{n}}$$

$$SE(p) = \sqrt{\frac{(0.65)(0.35)}{100}}$$

$$SE(p) = 0.0477$$

$$95\% \text{ confidence interval} = p \pm SE(p) \times Z_{0.975} =$$

Here Z is used because n is large, and according to central limit theorem when n is large, it follows normal distribution.

- Even if we don't know distribution of this set (voting majority party) It follow normal distribution

$$= 0.65 \pm 0.0477 \times 1.96 = [0.557, 0.743]$$

So we are 95% confident that between 55.7% and 74.3% of voters vote for majority party.