

# CS663: Digital Image Processing

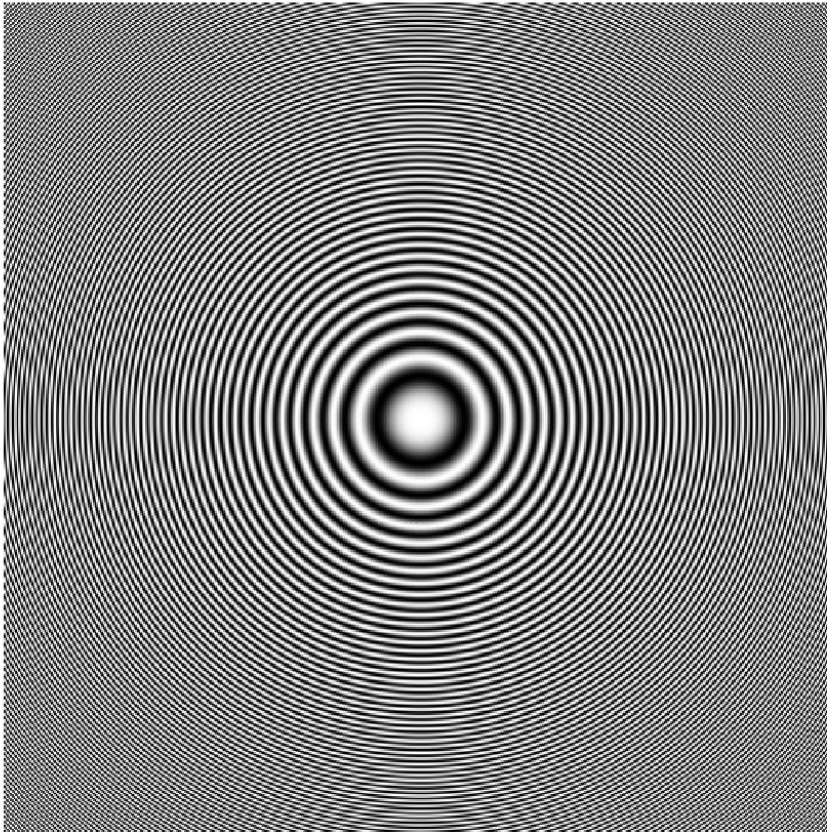
## Assignment 1 - Report

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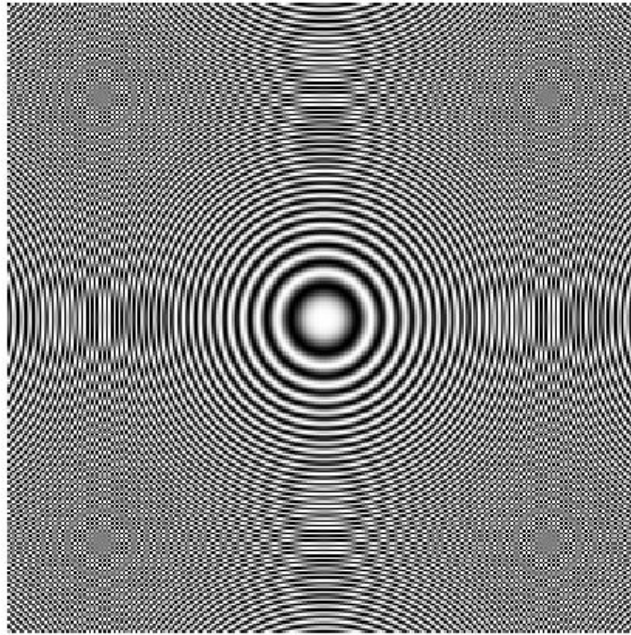
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### Question 1:

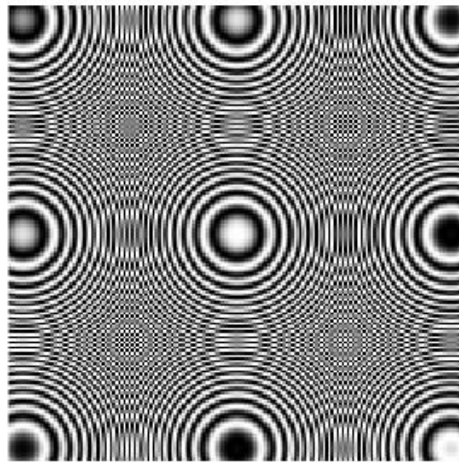
Original Image



**Shrunked Image by factor of 2**



**Shrunked Image by factor of 3**



**Original Image**



**Bilinear Interpolated Image**



**Original Image**

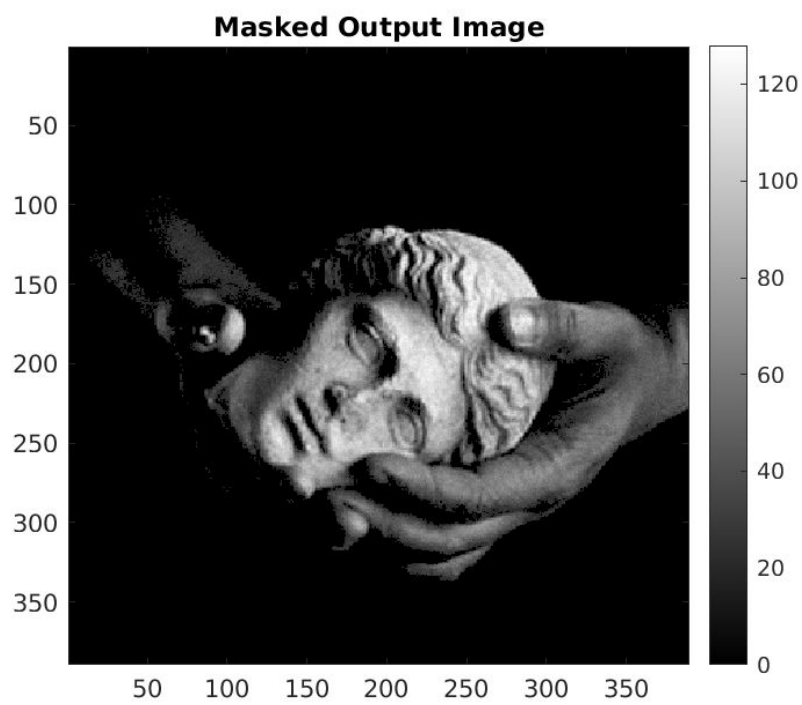
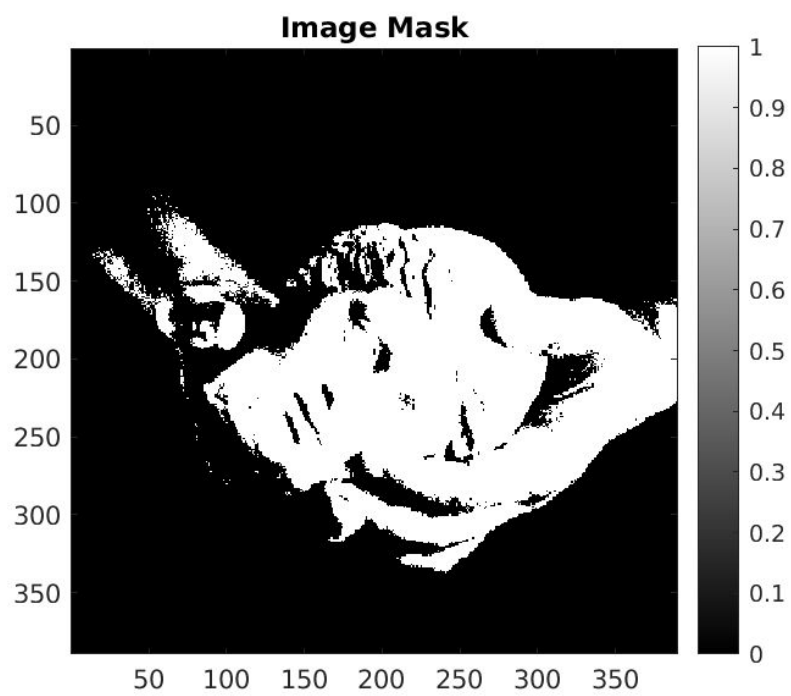


**NearestNeighbor Interpolated Image**



**Question 2:**

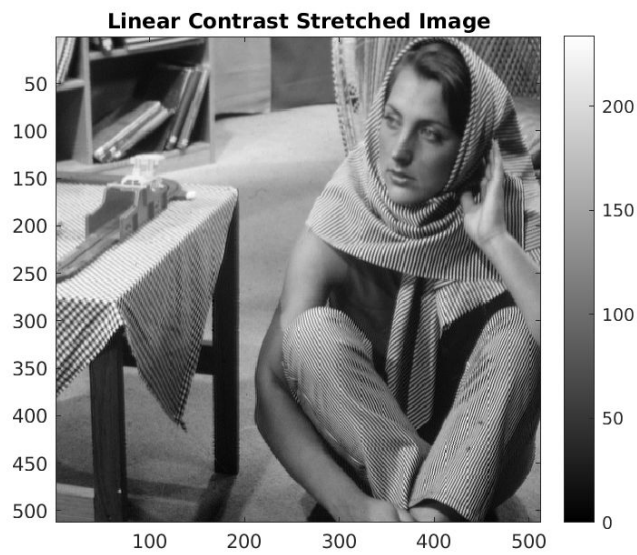
a)



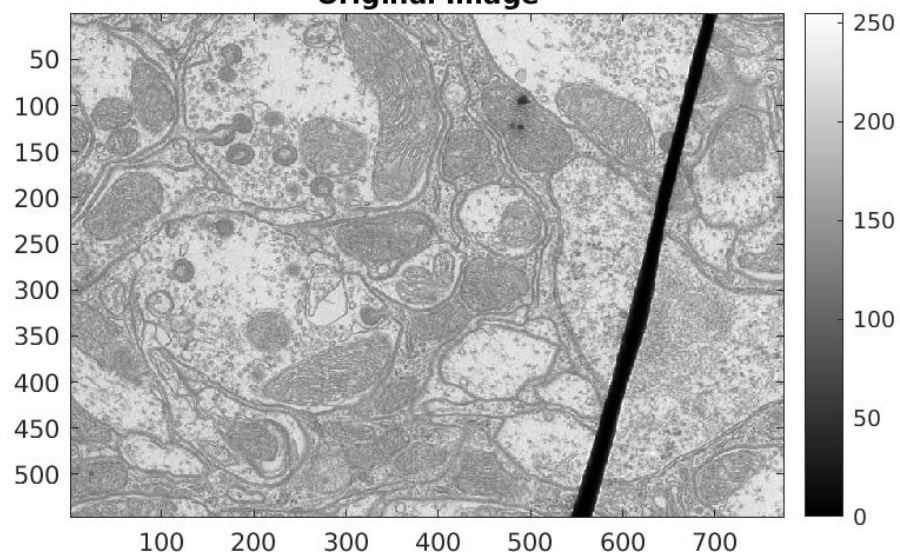
b) The formula used for interpolation of pixel  $r$  is:

$$r' = (r - I_{\min}) * (255 / (I_{\max} - I_{\min}))$$

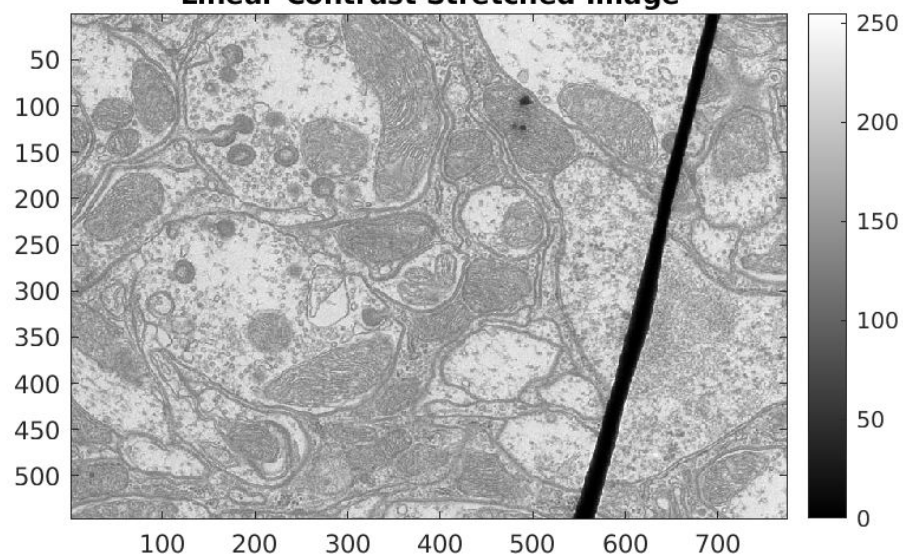
Here  $I_{\max}$  and  $I_{\min}$  are the maximum and minimum intensity values in the image respectively.



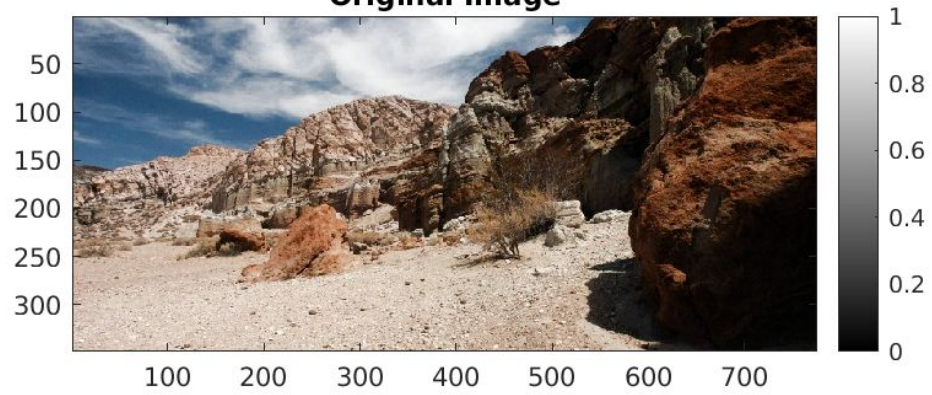
**Original Image**



**Linear Contrast Stretched Image**



**Original Image**

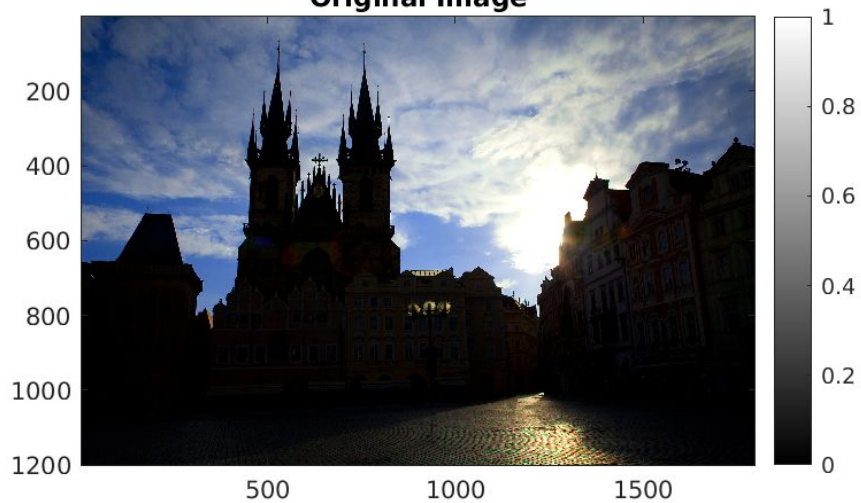


**Linear Contrast Stretched Image**

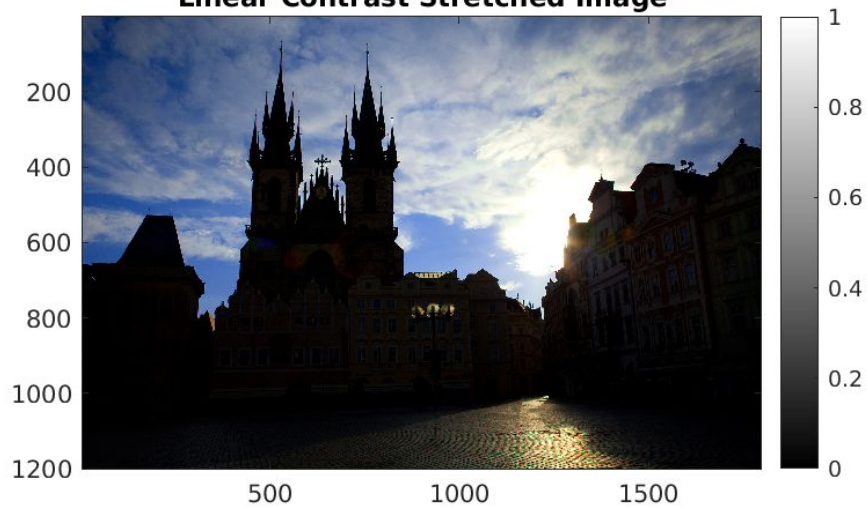




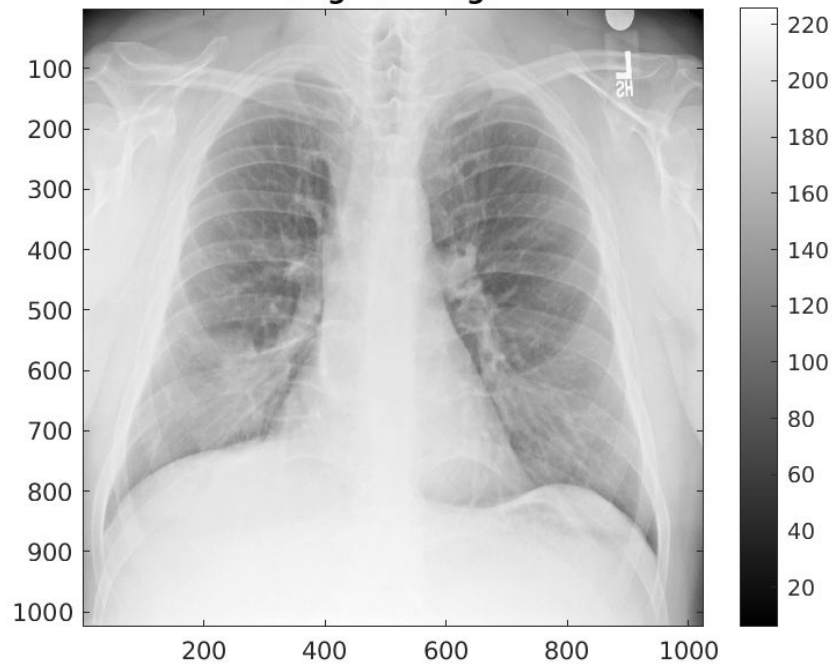
**Original Image**



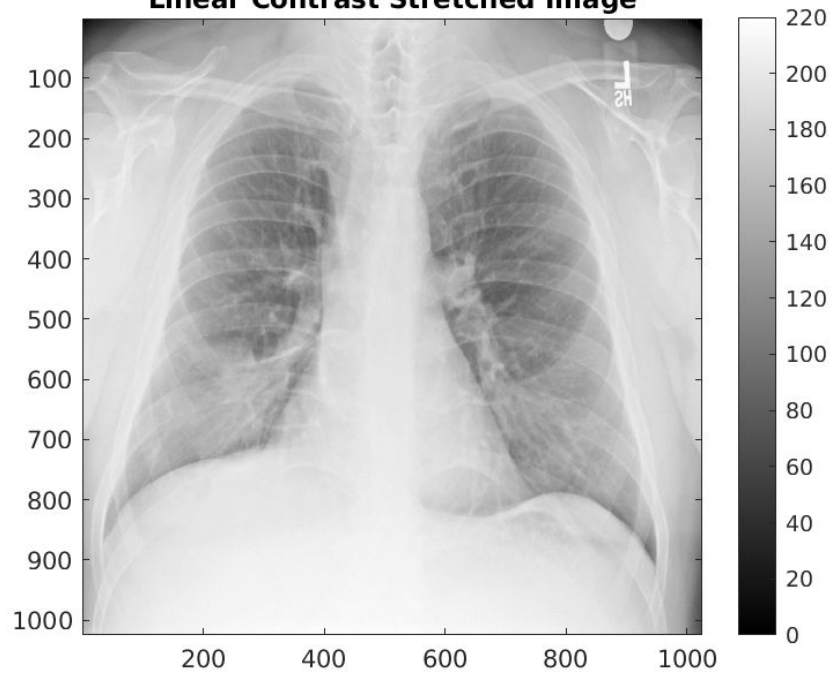
**Linear Contrast Stretched Image**

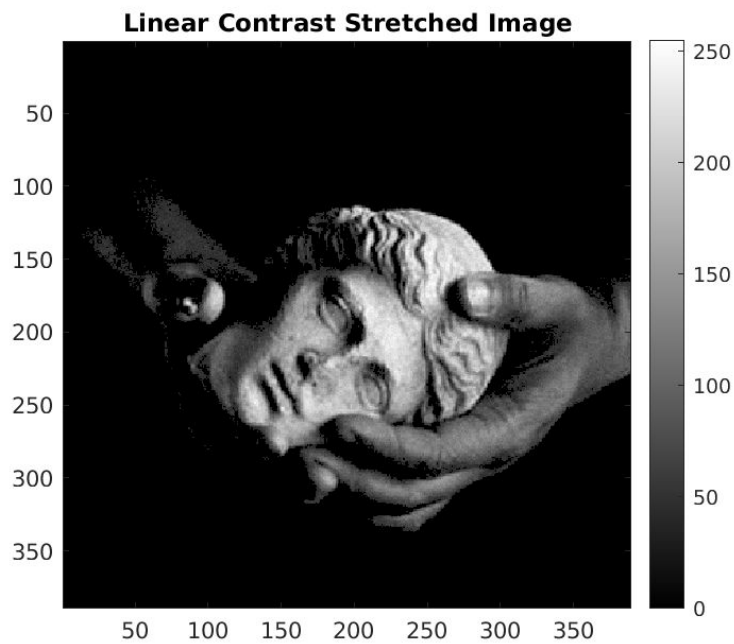


**Original Image**



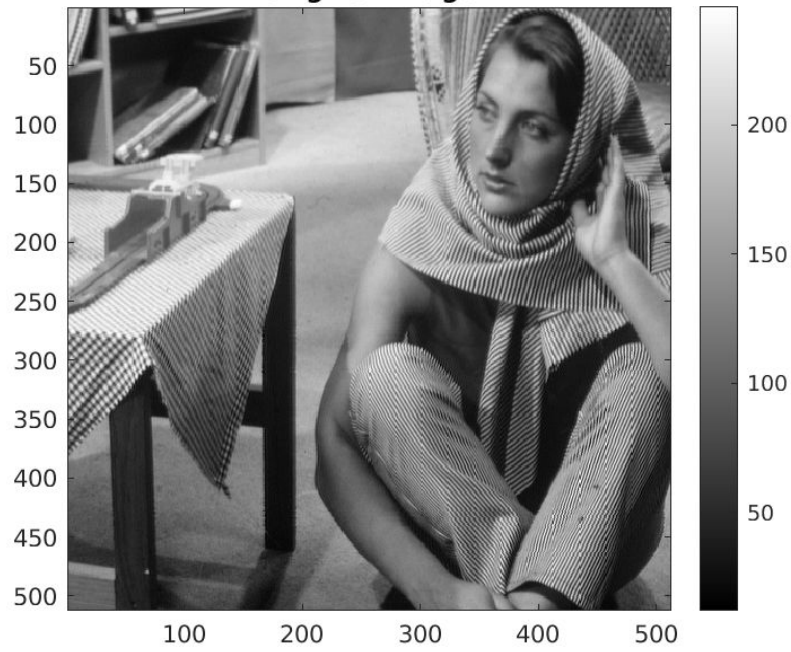
**Linear Contrast Stretched Image**





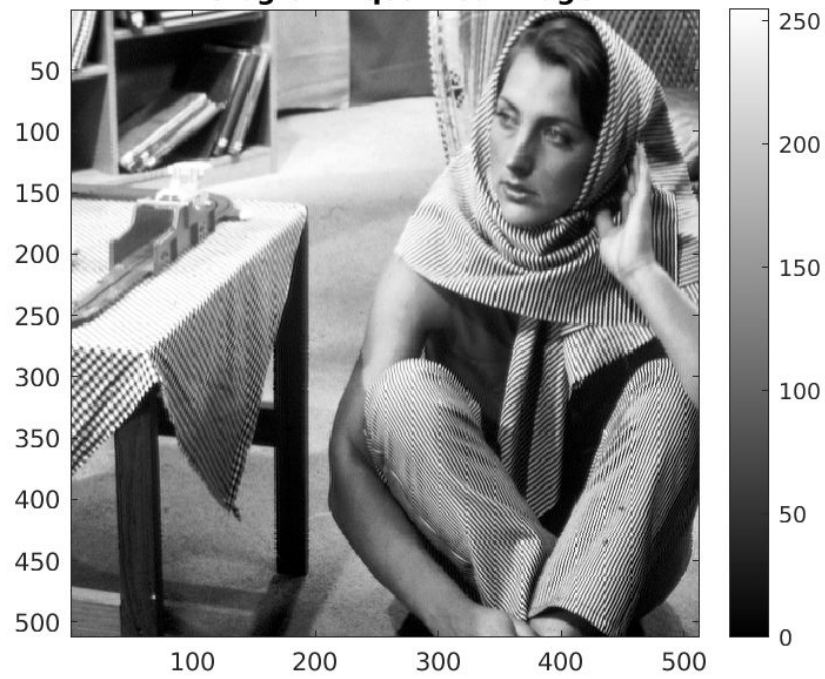
Contrast Stretching is not effective in (5) because the pixel values in the image already has a maximum of around 255 and a minimum of 0. In the case when the maximum and minimum are close to 255 and 0, we get no change in linear interpolation.

**Original Image**

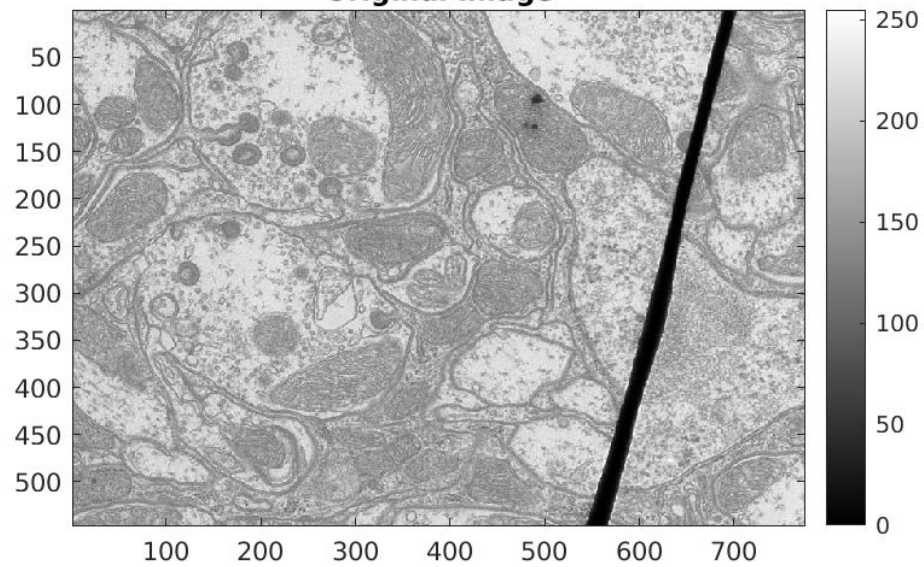


c)

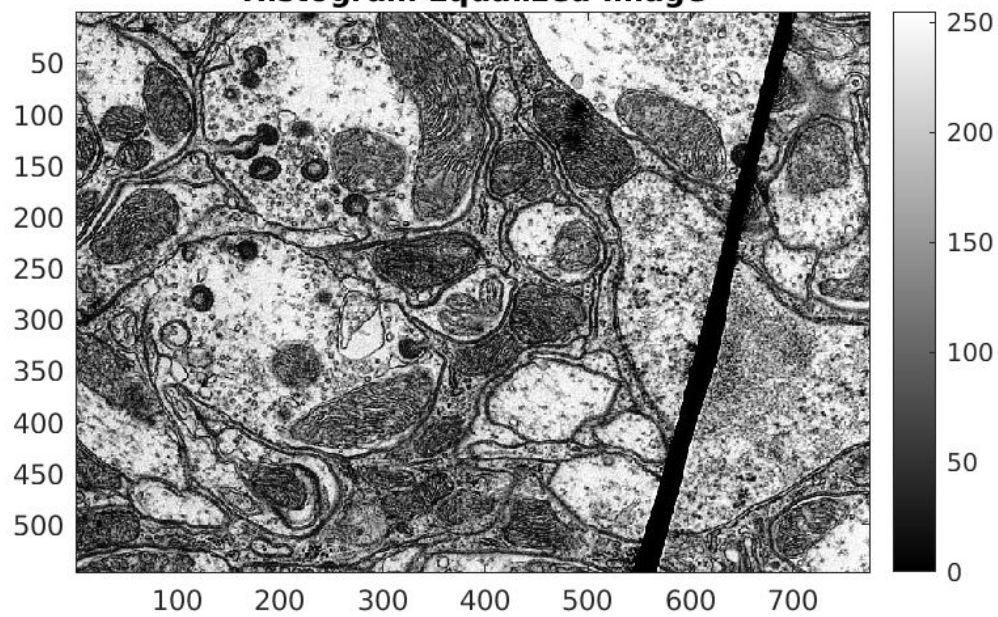
**Histogram Equalized Image**



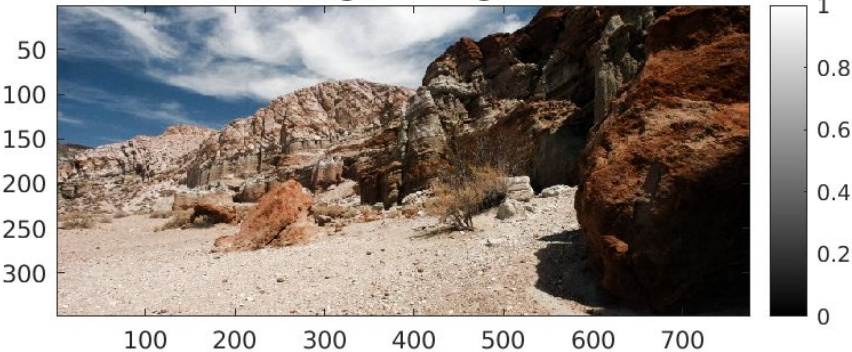
**Original Image**



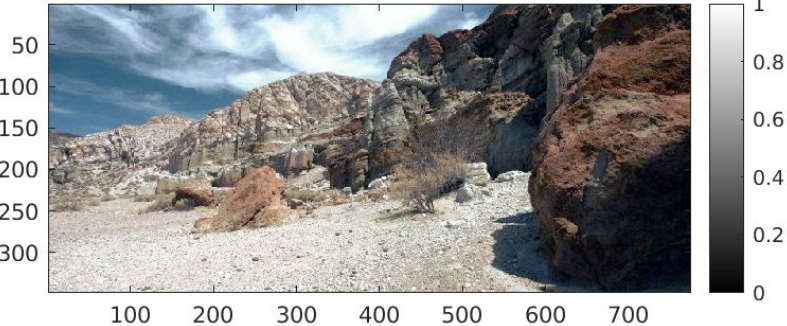
**Histogram Equalized Image**



**Original Image**

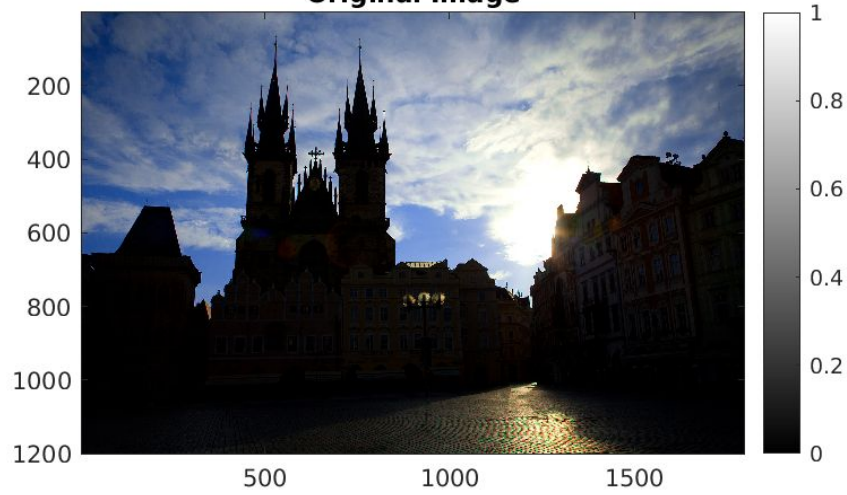


**Histogram Equalized Image**





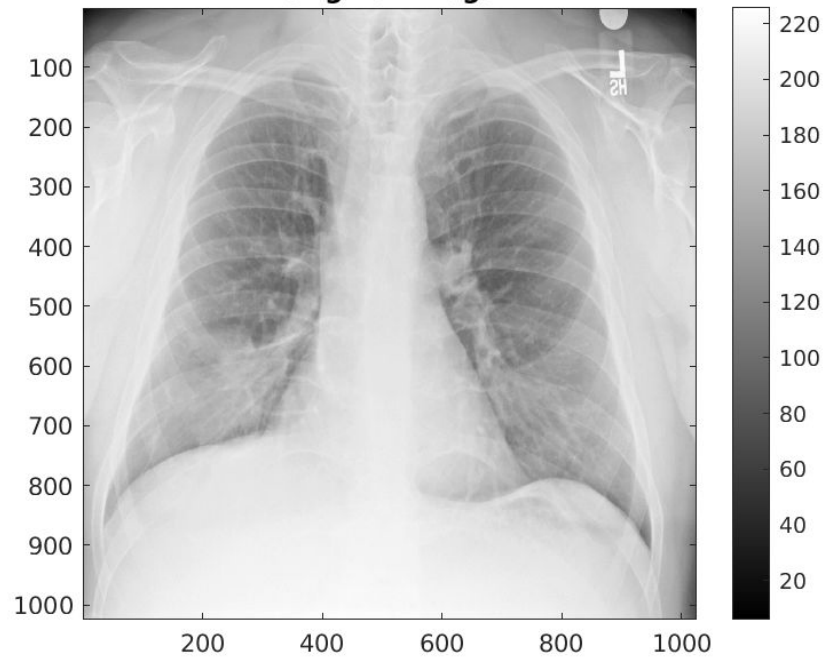
**Original Image**



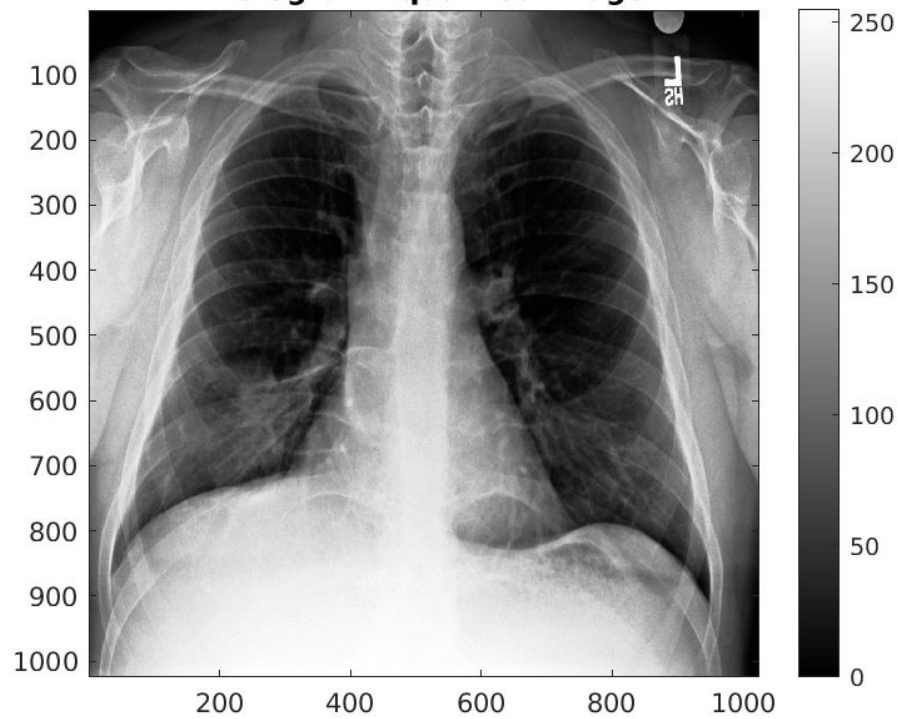
**Histogram Equalized Image**



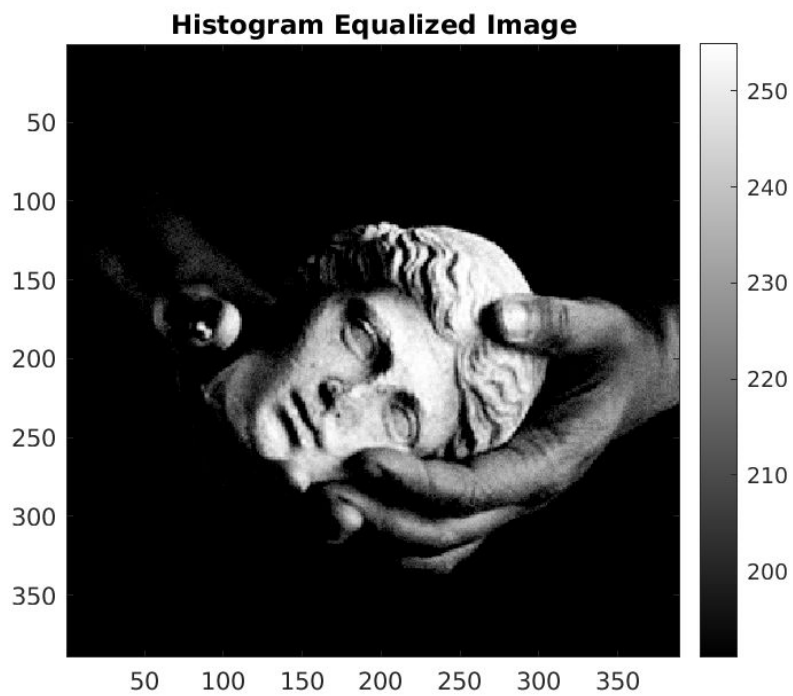
**Original Image**



**Histogram Equalized Image**

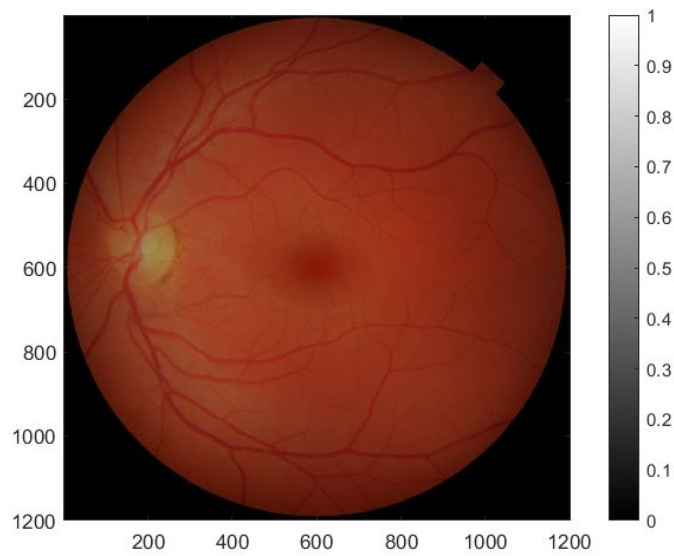




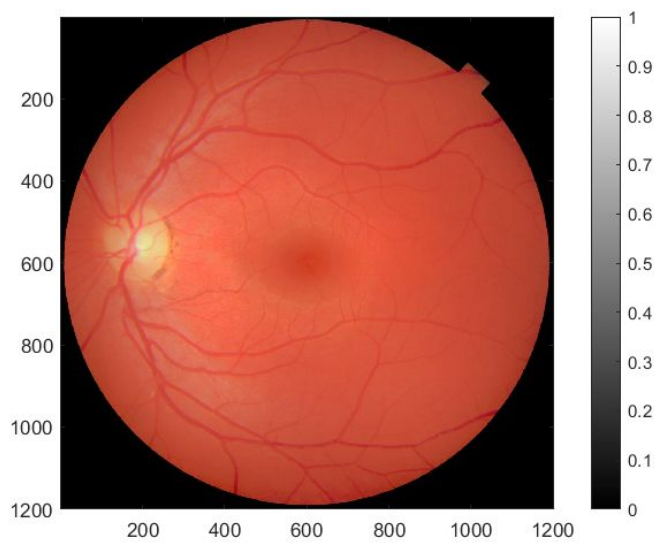


As we saw in the last part, there is no effect of Contrast Stretching on (5). However, we see a better result in HE. Hence HE is preferred in this case.

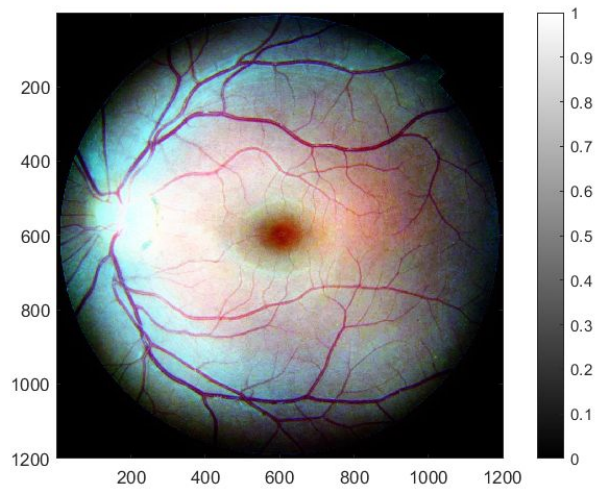
d)



Original Image



HM image



HE image

It is evident from the three images that Histogram Matching more resembles the reference image. This is helpful when we want the image to have a particular appearance. HE image has a very low orange tint and looks unrealistic. Hence this is not recommended.

e)

Part e results and best parameters are written in the mainScript.m. They are not added in this document due to a large number of photos.

Please refer to the code (mainscript)

### Question 3:

a)

The CDF of a histogram equalized image is a ramp, that is, its histogram is uniform in the region. As mentioned in the question, after the transformation  $h_1$  and  $h_2$  should be equalized individually in the intervals  $[0, a]$  and  $[a, 1]$ . Let the transformed histogram be  $g$  and  $g_1$  and  $g_2$  respectively in the intervals  $[0, a]$  and  $[a, 1]$ .

Therefore, keeping mass preservation:

$$g = \frac{\alpha}{a} ; I \in [0, a]$$

$$g = \frac{1 - \alpha}{1 - a} ; I \in [a, 1]$$

Where,

$$\alpha = \int_0^a h(I) dI$$

The mean intensity of this new transformed histogram would be its expectation:

$$\begin{aligned} E[g] &= \int_0^1 g(I) I dI \\ E[g] &= \left( \int_0^a \frac{\alpha}{a} I dI \right) + \left( \int_a^1 \frac{1 - \alpha}{1 - a} I dI \right) \\ E[g] &= \frac{(1 - \alpha)(1 + a)}{2} + \frac{\alpha a}{2} \\ E[g] &= \frac{1 - \alpha + a}{2} \end{aligned}$$

Therefore the mean of g is  $(1 - \alpha + a)/2$ .

b)

Since 'a' is the median intensity therefore,  $\alpha = 1/2$ .

Therefore mean intensity of the resulting histogram is  $(1 + a)/2$ .

c)

Histogram equalization can cause the gray-scale stretching which changes the average luminescence of the picture which is undesirable in some cases. This method of dividing the picture into two parts based on their gray levels and contrast stretching them individually thus restricts big changes of luminescence level of the picture. Therefore, for those pictures which need to be contrast stretched with minimal change in luminescence levels we should apply this new method.

d)

In the below three images, we can clearly see that the Modified HE image as discussed in the previous parts outperforms the Histogram Equalization Output. Hence this is a better approach in such images.

