

Segment Tree | Set 1 (Sum of given range)

Let us consider the following problem to understand Segment Trees.

We have an array $arr[0 \dots n-1]$. We should be able to

- 1 Find the sum of elements from index l to r where $0 \leq l \leq r \leq n-1$
- 2 Change value of a specified element of the array $arr[i] = x$ where $0 \leq i \leq n-1$.

A **simple solution** is to run a loop from l to r and calculate sum of elements in given range. To update a value, simply do $arr[i] = x$. The first operation takes $O(n)$ time and second operation takes $O(1)$ time.

Another solution is to create another array and store sum from start to i at the i th index in this array. Sum of a given range can now be calculated in $O(1)$ time, but update operation takes $O(n)$ time now. This works well if the number of query operations are large and very few updates.

What if the number of query and updates are equal? **Can we perform both the operations in $O(\log n)$ time once given the array?** We can use a Segment Tree to do both operations in $O(\log n)$ time.

Representation of Segment trees

1. Leaf Nodes are the elements of the input array.
2. Each internal node represents some merging of the leaf nodes. The merging may be different for different problems. For this problem, merging is sum of leaves under a node.

An array representation of tree is used to represent Segment Trees. For each node at index i , the left child is at index $2*i+1$, right child at $2*i+2$ and the parent is at $\lfloor (i-1)/2 \rfloor$.

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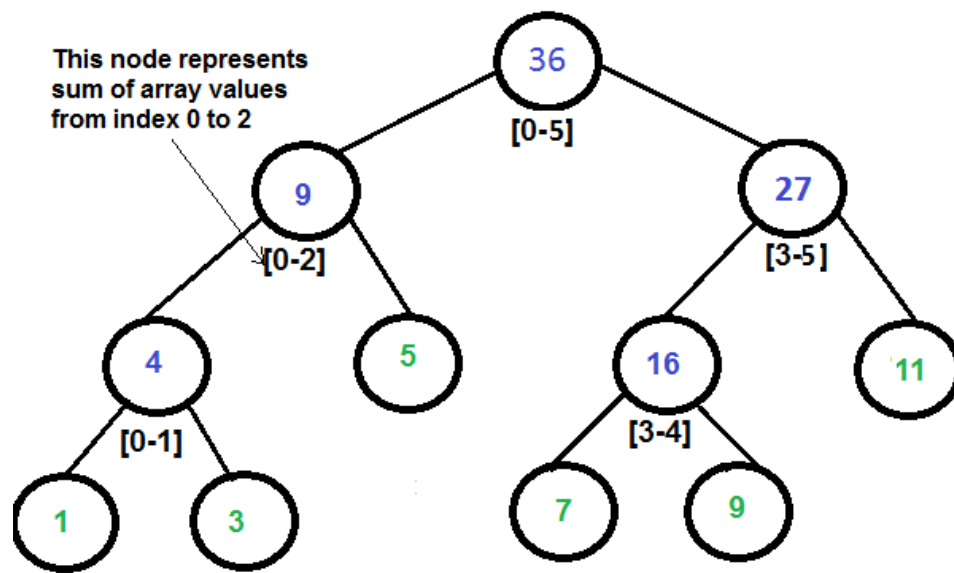


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Segment Tree for input array {1, 3, 5, 7, 9, 11}

Construction of Segment Tree from given array

We start with a segment $arr[0 \dots n-1]$. and every time we divide the current segment into two halves(if it has not yet become a segment of length 1), and then call the same procedure on both halves, and for each such segment we store the sum in corresponding node.

All levels of the constructed segment tree will be completely filled except the last level. Also, the tree will be a **Full Binary Tree** because we always divide segments in two halves at every level.

Since the constructed tree is always full binary tree with n leaves, there will be $n-1$ internal nodes. So total number of nodes will be $2*n - 1$.

Height of the segment tree will be $\lceil \log_2 n \rceil$. Since the tree is represented using array and relation between parent and child indexes must be maintained, size of memory allocated for segment tree will be $2 * 2^{\lceil \log_2 n \rceil} - 1$.

Query for Sum of given range

Once the tree is constructed, how to get the sum using the constructed segment tree. Following is algorithm to get the sum of elements.

```
int getSum(node, l, r)
{
    if range of node is within l and r
```

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```

        return value in node
    else if range of node is completely outside l and r
        return 0
    else
        return getSum(node's left child, l, r) +
               getSum(node's right child, l, r)
}

```

Update a value

Like tree construction and query operations, update can also be done recursively. We are given an index which needs to be updated. Let *diff* be the value to be added. We start from root of the segment tree, and add *diff* to all nodes which have given index in their range. If a node doesn't have given index in its range, we don't make any changes to that node.

Implementation:

Following is implementation of segment tree. The program implements construction of segment tree for any given array. It also implements query and update operations.

```

// Program to show segment tree operations like construction, query and
#include <stdio.h>
#include <math.h>

// A utility function to get the middle index from corner indexes.
int getMid(int s, int e) { return s + (e - s)/2; }

/* A recursive function to get the sum of values in given range of the array.
The following are parameters for this function.

st    --> Pointer to segment tree
index --> Index of current node in the segment tree. Initially 0 is
         passed as root is always at index 0
ss & se --> Starting and ending indexes of the segment represented by
         current node, i.e., st[index]
qs & qe --> Starting and ending indexes of query range */
int getSumUtil(int *st, int ss, int se, int qs, int qe, int index)
{
    // If segment of this node is a part of given range, then return the
    // sum of the segment
    if (qs <= ss && qe >= se)
        return st[index];

    // If segment of this node is outside the given range
    if (se < qs || ss > qe)
        return 0;
}

```

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```
// If a part of this segment overlaps with the given range
int mid = getMid(ss, se);
return getSumUtil(st, ss, mid, qs, qe, 2*index+1) +
       getSumUtil(st, mid+1, se, qs, qe, 2*index+2);
}

/* A recursive function to update the nodes which have the given index
their range. The following are parameters
st, index, ss and se are same as getSumUtil()
i    --> index of the element to be updated. This index is in input
diff --> Value to be added to all nodes which have i in range */
void updateValueUtil(int *st, int ss, int se, int i, int diff, int ind)
{
    // Base Case: If the input index lies outside the range of this segment
    if (i < ss || i > se)
        return;

    // If the input index is in range of this node, then update the value
    // of the node and its children
    st[index] = st[index] + diff;
    if (se != ss)
    {
        int mid = getMid(ss, se);
        updateValueUtil(st, ss, mid, i, diff, 2*index + 1);
        updateValueUtil(st, mid+1, se, i, diff, 2*index + 2);
    }
}

// The function to update a value in input array and segment tree.
// It uses updateValueUtil() to update the value in segment tree
void updateValue(int arr[], int *st, int n, int i, int new_val)
{
    // Check for erroneous input index
    if (i < 0 || i > n-1)
    {
        printf("Invalid Input");
        return;
    }

    // Get the difference between new value and old value
    int diff = new_val - arr[i];

    // Update the value in array
    arr[i] = new_val;

    // Update the values of nodes in segment tree
    updateValueUtil(st, 0, n-1, i, diff, 0);
}
```

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akshay what happens to our code when we put it here??

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Akshay kabra I have done this in O(n) with no extra...

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kanu i think recursion we can use for that....

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```

// Return sum of elements in range from index qs (query start) to
// qe (query end). It mainly uses getSumUtil()
int getSum(int *st, int n, int qs, int qe)
{
    // Check for erroneous input values
    if (qs < 0 || qe > n-1 || qs > qe)
    {
        printf("Invalid Input");
        return -1;
    }

    return getSumUtil(st, 0, n-1, qs, qe, 0);
}

// A recursive function that constructs Segment Tree for array[ss..se]
// si is index of current node in segment tree st
int constructSTUtil(int arr[], int ss, int se, int *st, int si)
{
    // If there is one element in array, store it in current node of
    // segment tree and return
    if (ss == se)
    {
        st[si] = arr[ss];
        return arr[ss];
    }

    // If there are more than one elements, then recur for left and
    // right subtrees and store the sum of values in this node
    int mid = getMid(ss, se);
    st[si] = constructSTUtil(arr, ss, mid, st, si*2+1) +
              constructSTUtil(arr, mid+1, se, st, si*2+2);
    return st[si];
}

/* Function to construct segment tree from given array. This function
allocates memory for segment tree and calls constructSTUtil() to
fill the allocated memory */
int *constructST(int arr[], int n)
{
    // Allocate memory for segment tree
    int x = (int)(ceil(log2(n))); //Height of segment tree
    int max_size = 2*(int)pow(2, x) - 1; //Maximum size of segment tree
    int *st = new int[max_size];

    // Fill the allocated memory st
    constructSTUtil(arr, 0, n-1, st, 0);

    // Return the constructed segment tree

```

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```

    return st;
}

// Driver program to test above functions
int main()
{
    int arr[] = {1, 3, 5, 7, 9, 11};
    int n = sizeof(arr)/sizeof(arr[0]);

    // Build segment tree from given array
    int *st = constructST(arr, n);

    // Print sum of values in array from index 1 to 3
    printf("Sum of values in given range = %d\n", getSum(st, n, 1, 3))

    // Update: set arr[1] = 10 and update corresponding segment
    // tree nodes
    updateValue(arr, st, n, 1, 10);

    // Find sum after the value is updated
    printf("Updated sum of values in given range = %d\n",
        getSum(st, n, 1, 3))

    return 0;
}

```

Output:

```

Sum of values in given range = 15
Updated sum of values in given range = 22

```

Time Complexity:

Time Complexity for tree construction is $O(n)$. There are total $2n-1$ nodes, and value of every node is calculated only once in tree construction.

Time complexity to query is $O(\log n)$. To query a sum, we process at most four nodes at every level and number of levels is $O(\log n)$.

The time complexity of update is also $O(\log n)$. To update a leaf value, we process one node at every level and number of levels is $O(\log n)$.

Segment Tree | Set 2 (Range Minimum Query)

References:

<http://www.cse.iitk.ac.in/users/aca/lop12/slides/06.pdf>

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

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**Guest** · 2 months ago

sdf

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**srihari** · 2 months ago

In getSumUtil function,
the first condition
why $qs \leq ss$ is taken instead of $qs == ss$

^ | ▼ · Reply · Share ›

**anubis** · 2 months ago

to construct size of segment tree, $2^{2^{\lceil \log_2(n) \rceil}} - 1$: this will result a size
 $n=6$

$\log_2(n) = 2.58$, ceiling of $(2.58) = 3$, i.e. $2^{2^3} - 1 = 15$. How come it gives 1?

^ | ▼ · Reply · Share ›

**helper** · 3 months ago

this is quite interesting. we were taught this in class but i never knew impleme
implementation. thanks for sharing.

^ | ▼ · Reply · Share ›

**sree_ec** · 3 months ago

while constructing the segement tree, size of segment tree can be calculated

In this example it is complicated by using $2^{(2^{\lceil \log_2(n) \rceil})} - 1$

in this example, it is complicated by doing $2 \cdot (2^{\lceil \log_2(n) \rceil} - 1)$
where $2^{\lceil \log_2(n) \rceil} = n$

3 ^ | v • Reply • Share ›



Ratan Roy → sree_ec • 3 months ago

The formula is not $2 \cdot 2^{\lceil \log_2(n) \rceil} - 1$. It is $2 \cdot 2^{\lceil \log_2(n) \rceil} - 1$. The reason is the same level. If they were, then the formula $2 \cdot 2^{\lceil \log_2(n) \rceil} - 1$ will give the representation.

1 ^ | v • Reply • Share ›



DS+Algo=Placement • 6 months ago

How is the complexity become $O(n)$ for updation if we use array storing the sum? 'Another Solution'?

^ | v • Reply • Share ›



Boris Marchenko → DS+Algo=Placement • 6 months ago

If you have array of 10 elements, you should store sum array of 10 elements. If you have 5, in the sum array you should update 5 elements. If we will update element number of elements to update in the sum array is $N/2$ (10 for element 1, 5 for element 2, etc.). Complexity is linear - $O(N/2) = O(N)$.

^ | v • Reply • Share ›



DS+Algo=Placement → Boris Marchenko • 6 months ago

Thanx

^ | v • Reply • Share ›



vipinkaushal • 6 months ago

i think the size allocated should be $2^h - 1$ where $h = \lceil \log_2(n) \rceil$
because for last we have not to mark null child
please clear my doubt
thanks

^ | v • Reply • Share ›



Ratan Roy → vipinkaushal · 3 months ago

it is $\text{pow}(2, h) - 1$ if root is considered to have height of 1.

it is $2 * \text{pow}(2, h) - 1$ if root is considered to have height of 0.

Note: $\text{ceil}(\log_2(n))$, where n is number of leaves, gives a height that coi

^ | v · Reply · Share ›



ryan → vipinkaushal · 5 months ago

no it should be $2 * \text{pow}(2, h) - 1$, because $(n-1)$ space is required to store
oru can say $n-1$ will be non leaf node and n will be leaf node

^ | v · Reply · Share ›



matheus · 7 months ago

I think that the function `constructSTUtil` has a little problem, when we get on the
this operation: $i * 2 + 2$ we get outside of the array on the next function call.

^ | v · Reply · Share ›



ryan → matheus · 5 months ago

no "st" array is sufficient enough

^ | v · Reply · Share ›



anonymous · 7 months ago

// Update the values of nodes in segment tree

`updateValueUtil(st, 0, n-1, i, diff, 0);` i think is wrong

it should be `updateValueUtil(st, 0, n-1, i, diff, i);` since we update child nodes of

^ | v · Reply · Share ›



gaurav · 8 months ago

Shouldn't 'if ($qs \leq ss \ \&\& \ qe \geq se$)' in `getSumUtil()` function be 'if ($qs \geq ss \ \&$

^ | v · Reply · Share ›



prashant · 9 months ago

`void update(tnode* root, int arr[], int low, int high, int ind, int val)`

void update(node *root, int arr[], int low, int high, int ind, int val)

{

if(low==high)

{

root->data=val;

return;

}

int mid=(low+high)/2;

if(ind>mid)

update(root->rchild,arr,mid+1,high,ind,val);

if(ind<=mid)

[see more](#)

^ | v • Reply • Share ›



prashant • 9 months ago

note the crucial points

1-segment tree is not complete binary tree

2-the left and right subtree are divided based on middle values

3-the sum and update code are similar to binary search code so its implementation for update process

construction is simple ...just recursively go down dividing the index into 2 halves

node data and during unwinding phase adjust root->data

for range sum

if ind1>mid then just move to right subtree

if ind2<=mid move to left

else split the range index into 2 halves

```
int sum(tnode* root,int low,int high,int l,int h)

{

if((low==l)&&(high==h))

return root->data;
```

see more

^ | v · Reply · Share ›



dmr · 9 months ago

We can use segment trees for finding sum in a given range. But how can this in a given range in $O(\log n)$ time? This is a question in References link (<http://www.cse.iitk.ac.in/user...> given above.

^ | v · Reply · Share ›



prshant jha · 10 months ago

here is my update version in $O(\log n)$ complexity with much simpler implementation: <http://ideone.com/SppdWT>

3 ^ | v · Reply · Share ›



The_Geek → prshant jha · 5 days ago

IMO, It is not a proper implementation also. Because while creating tree of elements. But while fetching sum you are again computing sum. The So the implementation does not seem correct to me. If anybody can clarify here?

^ | v · Reply · Share ›



The_Geek → prshant jha · 5 days ago

How (arr+i) can work, while computing range query, because memory So it is not guaranteed that (arr+i) will move root pointer to i-th node from

^ | v · Reply · Share ›



GOPI GOPINATH → prshant jha · 9 months ago

will the complexity in your implementation be $O(\log n)$???? but to find tl runtime ryt ????

^ | v · Reply · Share ›



prashant jha · 10 months ago

```
#include<iostream>
```

```
using namespace std;
```

```
struct node
```

```
{
```

```
node* lchild;
```

```
int data;
```

```
node* rchild;
```

```
node()
```

```
{
```

```
lchild=NULL;
```

```
rchild=NULL;
```

see more

^ | v · Reply · Share ›



prashant jha · 10 months ago

here is the implementation of the segment tree

<http://ideone.com/JPDzqz>

^ | v · Reply · Share ›



nwoebcke · 10 months ago

Although this puts an additional $O(\log(n))$ of memory on the heap, I think it makes recursion a little easier to follow. Also it is C++. To preserve the C language, you can use classes and rename the methods to functions with a struct pointer parameter

```
class Range {
public:
    int start;
    int end;
    Range(s, e) : start(s), end(e) {}
    void init(s, e) {
        start = s;
        end = e;
    }
    inline bool isInside(Range *other) {
        return start >= other->start && end <= other->end;
    }
    inline bool isOutside(Range *other) {
        return start > other->end || end < other->start;
    }
}
```

[see more](#)

^ | v · [Reply](#) · [Share](#) ›



Puneet Jaiswal · a year ago

Would this work as tree implementation

```
public class SegmentTree {
public static class STNode {
    int leftIndex;
    int rightIndex;
    int sum;
    STNode leftNode;
```

```

        STNode rightNode;
    }

    static STNode constructSegmentTree(int[] A, int l, int r) {
        if (l == r) {
            STNode node = new STNode();
            node.leftIndex = l;
            node.rightIndex = r;
            node.sum = A[l];
        }
    }
}

```

[see more](#)

^ | v • Reply • Share ›



mallard • a year ago

sorry but i think the language of implementation of above code is C and i think getting error when i am trying to run this code.I am using codeblock.

^ | v • Reply • Share ›



Pranjal Ranjan → mallard • 3 months ago

You can use malloc instead of new

^ | v • Reply • Share ›



Newbie90 • a year ago

What is the difference between the constructST and constructSTUtil functions constructSTUtil function.

^ | v • Reply • Share ›



Ankur Sao → Newbie90 • 9 months ago

ConstructST only allocates memory for the segment tree array and actually fills up the segment tree array. ConstructST then returns this array.

^ | v • Reply • Share ›



Vu Duc Minh • a year ago



Vaibhav Mittal · a year ago

I do not think the procedure "updateValueUtil" is a good one (even it is correct) should update from a leaf to the root; like the "constructSTUtil" procedure. In fact, "constructSTUtil". We only need one procedure for all two tasks.

^ | v · Reply · Share ›



Adrian Carballo · a year ago

Hey, great tutorial, I wrote a python implementation here <https://github.com/adrian-carballo/segment-tree>

^ | v · Reply · Share ›



Avinash Ks · a year ago

Just one doubt, in SumUtil, isn't qs supposed to be greater than ss and qe less than or equal to ss - se

^ | v · Reply · Share ›



Denis · a year ago

Hi, you wrote : "size of memory allocated for segment tree will be $2 * 2^{\lceil \log_2 n \rceil} - 1$ " where I assume n is a number of leafs in the tree. This seems not to be true using your example of a segment tree : "{1,3,5,7,9,11}", where n=6. Thus using $2 * 2^{\lceil \log_2 n \rceil} - 1$ size of memory allocated is 7, which is not 11 nodes. Suppose n should be replaced on the $(2 * n - 1)$ in your expression.

^ | v · Reply · Share ›



Denis → Denis · a year ago

Sorry, I've got it. You are using ceil() function in this case. So $2 * 2^{\lceil \log_2 n \rceil} - 1$ is the tree size. I was thinking about floor() instead of ceil().

^ | v · Reply · Share ›



Vishnu Kamavaram → Denis · 9 days ago

if for suppose n=30

$\text{ceil}(\log(30)) = 2.0$

size = $2 * 2^2 - 1 = 7$ (i think its wrong)

if I wrong do correct me !!!

^ | v • Reply • Share ›



Denis • a year ago

Hi, you wrote : "size of memory allocated for segment tree will be ", where I as tree. This is seems not to be true using your example of a segment tree : "{1,3 where n=6. Thus using size of memory allocated is 7, which is not true becau Suppose n should be replaced on the $(2*n-1)$ in your expression.

^ | v • Reply • Share ›



denial • a year ago

@geeksforgeeks:

Change suggestion in the paragraph "Query for Sum of given range". It should

```
int getSum(node, l, r)
{
    if range of node is within l and r
        return value in node

    if range of node is completely outside l and r
        return 0

    return getSum(node's left child, l, r) +
           getSum(node's right child, l, r)
}
```

let me know if I'm wrong. :)

^ | v • Reply • Share ›



denial • a year ago

@geeksforgeeks

Change suggestion in the paragraph "Query for Sum of given range" above :

You written it as :

```
int getSum(node, l, r)
{
    if range of node is within l and r
        return value in node
    else if range of node is completely outside l and r
        return 0
    else
        return getSum(node's left child, l, r) +
               getSum(node's right child, l, r)
}
```

should be changed to this:

[see more](#)

^ | v • Reply • Share ›



Prakhar Jain • 2 years ago

Time Complexity of query is $O(\log n)$ because we process at most "4 nodes" ; "nodes" which is wrong. For example take range [1-3] in your example and mal function, you will see there are at most 4 nodes at each level. Even it is also given in the iitk link you have given at the end.

```
/* Paste your code here (You may delete these lines if not writing code)
```

1 ^ | v • Reply • Share ›



GeeksforGeeks → Prakhar Jain • 2 years ago

@Prakhar Jain: Thanks for pointing this out. we have updated the post

^ | v · Reply · Share ›



Prakhar Jain → GeeksforGeeks · 2 years ago

Also, to update a leaf we process "two nodes" at each level, no

```
/* Paste your code here (You may delete these lines if r
```

^ | v · Reply · Share ›



kartik · 2 years ago

How do we do the updation if we have to update more than 2 values

like we have to increase all number in range a to b by 2

how our update function do this in $O(\log(n))$

can any body plz help

```
/* Paste your code here (You may delete these lines if not writing coo
```

^ | v · Reply · Share ›



Sumanth Bandi · 2 years ago

''Since the tree is represented using array and relation between parent and child is maintained, size of memory allocated for segment tree will be $2 * (2^{\lceil \log_2 n \rceil})$ line.

Why not just $2 * n - 1$? What are the bad sequences of just allotting $2 * n - 1$ nodes? Anybody pls help..

^ | v · Reply · Share ›



sumanth232 · 2 years ago

Since the tree is represented using array and relation between parent and child

memory allocated for segment tree will be $2 \cdot (2^{\lceil \log_2 n \rceil}) - 1$.

Why not just $2 \cdot n - 1$? What are the bad sequences of just allotting $2 \cdot n - 1$ nodes?
Anybody pls help..

^ | v • Reply • Share ›



alveko → sumanth232 • 2 years ago

The array must have enough elements to include a possible right-most leaf. The size of the array must increase with a step of power of 2. The size of $(2 \cdot n - 1)$ might not be enough.

```
// segment tree size (n is the number of elements in the input)
// (log2ceil(n)) is the level that can hold all distinct elements
// 2^(log2ceil(n)) is the number of elements at that level
// 2*2^(log2ceil(n))-1 is the total number of elements in the tree
```

/ Alexander K.

^ | v • Reply • Share ›



sumanth232 → alveko • 2 years ago

Thanks.. that made it clear..

```
/* Paste your code here (You may delete these lines if required) */
```

^ | v • Reply • Share ›



abhishek08aug • 2 years ago

Intelligent :D

^ | v • Reply • Share ›



Ouditchya Sinha • 2 years ago

Very nicely explained! Thank You GeeksforGeeks :). Just one question, where



very nicely explained. Thank you [Gerson Gerson](#)! ;) Just one question, when
the value in array & construct another segment tree? It seems to be working [h](#)
won't need update functions, would it be computationally costly? Will this

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