

**End-sem examination July-Dec 2020**

**Programme:** M.Tech. (CSE-CN)/Ph.D (CSE)    **Course:** MFCS    **Course code:** CS420102

**Full marks:** 40    **Time:** 2 hour.    **Session:** 2020-2021

**Answer any four questions**

1. Two teams A and B play a 5 match series. In each match A wins with probability  $p$  and loses with probability  $1-p$ . Compute the following: 10
  - The probability that the game ends after the third, the fourth or the fifth match.
  - The probability that A wins the series.
2. A gambler has Rs. 3/-. He bets Re. 1/- at a time and wins Re. 1/- with probability  $1/2$ . He stops playing if he loses Rs. 3/- or wins Rs. 4/-. 10
  - (a) Show that the process is Markov process.
  - (b) Is state 3 ergodic? Verify.
3. a) Prove the following transition probability matrix is irreducible: 5
$$\begin{matrix} & 0 & 1 \\ 1/2 & 1/2 \end{matrix}$$
  - b) If  $x$  is normally distributed with mean 18 and variance 3, and  $y$  is normally distributed with mean 24 and variance 2, and  $x$  and  $y$  are independent, what is  $P(12 \leq x < 14 \text{ and } 14 \leq y < 20)$ ? 5
4. a) Consider the function,  $f(X) = 5x_1^2x_2 + 4x_1x_2^3 - 8x_1x_2$ . Does the point (1,1) satisfy the FONC and SONC? 6
  - b) Compute the directional derivative of  $f(X) = 5x_1^2x_2 + 4x_1x_2^3 - 8x_1x_2$  at  $X = [1,0]$  in the direction  $S = [-1,-1]$ . 4
5. a) Apply gradient descent with a unit step size to  $f(X) = x_1^4x_2 + x_1x_2^4$  from a starting point of your choice. Compute four iterations. 6
  - b) In conjugate gradient descent, what is the normalized descent direction at the first iteration for the function  $f(x, y) = x^2 + xy + y^2 + 5$  when initialized at  $(x, y) = (1, 1)$ ? 4