

PHYS UN1601 Recitation Worksheet 3

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Problem 1

Consider a particle subject to an acceleration of the form

$$\begin{aligned}a(t) &= 0, \quad t < 0 \\a(t) &= a_0 e^{-t/\tau}, \quad t > 0\end{aligned}$$

with $x(0) = x_0$ and $v(0) = v_0$.

- a) Evaluate $v(t)$ for $t > 0$.
- b) Evaluate $x(t)$ for $t > 0$.

Problem 2

A particle has an acceleration given by

$$\ddot{x} = -\omega^2(x - \lambda)$$

- a) What are the dimensions of ω and λ ?
- b) Suppose $x(0) = 0$ and $v(0) = \dot{x}(0) = v_0$. Find expressions for $x(t)$ and $v(t)$ for $t > 0$.

Problem 3

A tire rolls in a straight line without slipping. Its center moves with constant speed v . A small pebble lodged in the tread of the tire touches the road at time $t = 0$. Find the pebble's position, velocity and acceleration as functions of time.

Problem 4

A particle moves in the $x - y$ plane. Starting from $\vec{r} = r\hat{r}$ (the position vector is described entirely radially), do the following, showing all the steps in your evaluation of the derivatives.

- a) Obtain the most general expression for the velocity using the polar unit vectors \hat{r} and $\hat{\theta}$.
- b) Obtain the most general expression for the acceleration assuming $\theta = \omega t$ and that r has an arbitrary time dependence. Express your results using the polar unit vectors.
- c) Apply your results from parts a) and b) to calculate the velocity and acceleration, $\vec{v}(t)$ and $\vec{a}(t)$, for a particle moving with $\theta = \omega t$ and $r = r_0 e^{-t/\tau}$.