Top-down and Bottom-up Strategies for Generating Incremental Covering Arrays

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Abstract—**Combinatorial Testing (CT) is an effective technique for testing the interactions of factors in the Software Under Test (SUT). By designing an efficient set of test cases, i.e., a covering array, CT aims to check every possible valid interaction in SUT. Most existing covering array generation algorithms require a given *degree t* in prior, such that only the interactions with no more than *t* factors are to be checked. In practice, however, the value of *t* cannot be properly determined, especially for systems with complex interaction space. Hence, incremental covering arrays are preferred. In this paper, we propose two strategies (*Bottom-up* and *Top-down*) for generating incremental covering arrays which can increase the coverage strength when required. A comparative evaluation of these two strategies is performed on 55 software subjects (including 25 real-world software and 30 synthetic systems). The results mainly shows that strategy *Bottom-up* have an advantage over strategy *Top-down* at lower degrees with respect to the size of covering arrays, while strategy *Top-down* performs better at higher degrees. However, when concerning the fault detection rate, strategy *Top-down* gets higher scores at lower degrees, while *Bottom-up* is better at higher degrees.**

Index Terms—**Combinatorial Testing, Covering Array, Incremental Covering Array, Bottom-up and Top-down strategy**

I. INTRODUCTION

With the growing complexity and scale of modern software systems, various factors, such as input values and configure options, can affect the behaviour of a system. Even worse, some interactions between them can trigger unexpected negative effects on the software. To ensure the correctness and quality of the software system, it is desirable to detect and locate these *bad* interactions. The simplest way to solve this problem is to perform exhaustive testing for all the possible valid interactions of the system. It is, however, not practical due to the combinatorial explosion. Therefore, the selection of a group of representative test cases from the whole testing space is required.

Combinatorial testing has been proven to be effective in sampling an effective set of test cases[1]. It works by generating a relatively small set of test cases, i.e., a covering array, to test the interactions involving a given number of factors that may affect the behavior of a system. The number of factors involved in those selected interactions is limited in a moderate range, which is usually from 2 to 6 [2].

Many algorithms have been proposed to generate covering arrays. Despite many differences between them, those works all assume that the degree t is a given priori. The degree t indicates the largest number of factors involved in the interactions to be covered, and the corresponding covering arrays which can satisfy this coverage criteria is called t-way covering arrays. In practice, however, the value of t is difficult to determine due to two reasons as follows. First, many software systems suffer from complex interaction space which make it challenging to estimate t. In such case, even experienced testers can make mistakes and estimate a wrong value for t, which can significantly affect the effectiveness and efficiency of CT. Specifically, if t is estimated to be larger than required, many redundant test cases will be generated, which is a waste of computing resource. And if t is estimated to be smaller than required, then the generated covering array is not sufficient to obtain an effective test set. Second, even though t has been properly determined, there may not be enough time to completely execute all the test cases in the covering array.

This is because testing software only makes sense before the next version is released. This time interval between two release versions may sometimes be too short for a complete testing of a high-strength covering array, especially in the scenario of continuous integration [3].

To address these shortcomings of traditional covering arrays, the notion of incremental covering array [3] has been proposed. Such object can be deemed as adaptive covering array, which can increase the degree t when required. As it can generate higher strength covering array based on lower strength covering array, it can reduce the cost when comparing with generating multiple ways of covering arrays. Additionally, it can be better applied on testing the software of which the released time is frequently changed and cannot be predicted. Another advantage for generating incremental covering array is that, testers can detect most faults in the software as soon as possible. This is because according to [2], most faults (about 70% to 80%) are caused by 2-degree interactions, and almost all faults can be covered by 6-way covering arrays. As incremental covering arrays first cover those lower-degree interactions, the faults caused by them will be detected sooner.

In consideration of the size of the total number of test cases, we argue that this approach of generating incremental covering array may produce too many test cases. This is obvious, as generating higher-strength covering array based on the lower-strength covering array (called *bottom-up* strategy later) does not aim to optimize the size of the higher-strength covering array. As a result, it may generate more test cases than those approaches that focus on generating a particular higher-strength covering array.

Then, a natural question, and also the motivation of this paper is, **is it possible to generate an incremental covering array with the same number of the overall test cases as those by the particular high-way covering array generation algorithms?** Due to the obvious conclusion that any high way covering array must cover all the lower way interactions, the answer for this question is *yes*, as we can just apply a particular covering array generation algorithm to generate the high-strength covering array, and then generate the lower-strength covering arrays by extracting some subset of the test cases which can cover all the lower degree interactions. We refer to this strategy as the *top-down* strategy.

In this paper, we give two different implementations for each strategy. Specifically, for *bottom-up* strategy, we first gives an approach which is based on directly seeding test cases of lower-way covering array. Another approach comes from the existing incremental covering array algorithm [3], which uses multiple covering arrays instead of one for seeding test cases. For *top-down* strategy, the key of the first implementation is to select the test cases with as much un-covered interactions as possible from higher-way covering arrays, while the second implementation is to select test cases with maximal hamming distances at each iteration.

We evaluated these four approaches by comparing them at constructing several incremental covering arrays on 55 wildly used subjects (including 25 real-world software and 30 synthetic systems). There are three metrics that are used in the empirical studies, i.e., the size of the incremental covering arrays for each degrees, the time cost when generating these test cases, and the fault detection rate of these covering arrays. The results mainly show that strategy *Bottom-up* have an advantage over strategy *Top-down* at lower degrees with respect to the size of covering arrays, while strategy *Top-down* performs better at higher degrees. However, when concerning the fault detection rate, strategy *Top-down* gets higher scores at lower degrees, while *Bottom-up* is better at higher degrees. Besides these observations, we also found that different implementations of these generation strategies also have impacts on the performance, especially for strategy *Top-down*, of which the implementation with considering un-covered interactions had a significant advantage over the one based on hamming distance.

Our contributions include:

1) We propose a formal description of incremental covering array, and give a proof of the existence of it.
2) We propose two strategies for generating incremental covering arrays, and for each strategy we give two different implementations.
3) We conduct a series of empirical experiments to evaluate the characteristics (test size, time cost, and fault detection) of these four approaches.
4) We offer a guideline for selecting which strategy when generating incremental covering array in practice.

II. BACKGROUND

This section gives some formal definitions related to CT. Assume that the behaviour of SUT is influenced by k parameters, and each parameter p_i has a_i discrete values from the finite set V_i, i.e., $a_i = |V_i|$ ($i = 1,2,..k$). Then a *test case* of the SUT is a group of values that are assigned to each parameter, which can be denoted as $(v_1, v_2, ..., v_k)$. An t-degree interaction can be formally denoted as $(-, ..., v_{n_1}, -, ..., v_{n_2}, -, ..., v_{n_t}, -, ...)$, where some t parameters have fixed values and other irrelevant parameters are represented as "-". In fact, a test case can be regarded as a k-degree interaction.

A. Covering array

Definition 1. A t-way *covering array* $MCA(N; t, k, (a_1, a_2, ..., a_k))$ is a test set in the form of $N \times k$ table, where each row represents a *test case* and each column represents a parameter. For any t columns, each possible t-degree interaction of the t parameters must appear at least once. When $a_1 = a_2 = ... = a_k = v$, a t-way covering array can be denoted as $CA(N; t, k, v)$.

For example, Table I (a) shows a 2-way covering array $CA(5; 2, 4, 2)$ for the SUT with 4 boolean parameters. For any two columns, any 2-degree interaction is covered. Covering array has proven to be effective in detecting the failures caused by interactions of parameters of the SUT. Many existing algorithms focus on constructing covering arrays such that the number of test cases, i.e., N, can be as small as possible.

B. Incremental covering array

Definition 2. An incremental covering array $ICA([N_{t_1}, N_{t_1+1}, ..., N_{t_2}]; [t_1, t_2], k, (a_1, a_2, ..., a_k))$ is a test set in the form of $N_{t_2} \times k$ table, where $t_1 < t_2$ and $N_{t_1} < N_{t_1+1} < , ..., < N_{t_2}$. In this table, the first N_{t_i} lines ($t_1 \leq t_i \leq t_2$) is a covering array $MCA(N_{t_i}; t_1 + i, k, (a_1, a_2, ..., a_k))$.

When $a_1 = a_2 = ... = a_k = v$, an incremental covering array can be denoted as $ICA([N_{t_1}, N_{t_1+1}, ..., N_{t_2}]; [t_1, t_2], k, v)$.

Table I shows an example of incremental covering array, in which the two-way covering array $CA(5; 2, 4, 2)$ is a subset of the three-way covering array $CA(9; 3, 4, 2)$, which is also an incremental covering array $ICA([5, 9]; [2, 3], 4, 2)$.

TABLE I: Experiment of Incremental covering array

(a) CA(5;2,4,2)

0	0	1	0
1	0	0	0
1	1	1	0
0	1	0	1
1	0	1	1

(b) CA(9;3,4,2) && ICA([5,9];[2,3],4,2)

0	0	1	0
1	0	0	0
1	1	1	0
0	1	0	1
1	0	1	1
0	1	0	0
0	0	0	1
0	1	1	1
1	1	0	1

Theorem. For each covering array $MCA(N_{t_2}; t_2, k, (a_1, a_2, ..., a_k))$, we can find an $ICA([N_{t_1}, N_{t_1+1}, ..., N_{t_2}]; [t_1, t_2], k, (a_1, a_2, ..., a_k))$, s.t., their test cases are the same.

Proof. We just need to prove that for any covering array, $MCA(N_t; t, k, (a_1, a_2, ..., a_k))$, we can find a $MCA(N_{t-1}; t - 1, k, (a_1, a_2, ..., a_k))$, such that, $N_{t-1} < N_t$ and for any test case $f \in MCA(N_{t-1}; t - 1, k, (a_1, a_2, ..., a_k))$, it has $f \in MCA(N_t; t, k, (a_1, a_2, ..., a_k))$.

First, $MCA(N_t; t, k, (a_1, a_2, ..., a_k))$ itself must be an $MCA(N_t; t - 1, k, (a_1, a_2, ..., a_k))$, as it must cover all the $(t - 1)$-degree interactions.

Then, assume to obtain a $(t - 1)$-way covering array, any one test case in $MCA(N_t; t, k, (a_1, a_2, ..., a_k))$ can not be reduced. With this assumption, any test case will cover at least one $(t - 1)$-degree interaction that only appears in this test case. Without loss of generality, let test case $(v_1, v_2, ..., v_k)$ cover the $(t - 1)$-degree interaction $(-, ..., v_{p_1}, ...-, ...v_{p_2}, ..., -, ..., v_{p_{t-1}}, ... - ..., v_{p_t}, ..., -, ...)$ which only appears in the test case. Then obviously the t-degree interaction $(v'_1, ..., v_{p_1}, ...-, ...v_{p_2}, ..., -, ..., v_{p_{t-1}}, ... - ..., v_{p_t}, ..., -, ...)$ $(v'_1 \neq v_1)$ will never be covered by any test case in $MCA(N_t; t, k, (a_1, a_2, ..., a_k))$, and hence $MCA(N_t; t, k, (a_1, a_2, ..., a_k))$ is not a t-way covering array (Note this is based on that the parameter can take on more than one value).

This is a contradiction, and means that we can reduce at least one test case in $MCA(N_t; t, k, (a_1, a_2, ..., a_k))$, so that

it is still a $(t - 1)$-way covering array. $\square$

This theorem shows the existence of the incremental covering arrays. As discussed before, generating the incremental covering arrays is of importance, as it supports adaptively increasing the coverage strength. According to this theorem, when testing a SUT, testers can firstly execute the lowest-strength covering array in the incremental covering arrays, and then execute additional test cases from those higher-strength covering arrays as required. The reuse of previously executed test cases will reduce the cost for generating multiple different-ways covering arrays.

III. GENERATING INCREMENTAL COVERING ARRAYS

This section presents two strategies to generate the incremental covering arrays. The first strategy, i.e., the *bottom-up* strategy starts from generating the lowest-strength covering array and then the higher-strength ones. The second strategy, i.e., the *top-down* strategy firstly generated the highest-strength covering array, then the lower-strength covering array.

A. Bottom-up strategy

This strategy is listed as Strategy 1. The inputs for this

Strategy 1 Bottom-up strategy

Input: $Params$ ▷ Parameters (and their values)
      t_1 ▷ the lowest strength
      t_2 ▷ the highest strength
Output: ICA ▷ the incremental covering arrays
1: $ICA \leftarrow EmptySet$
2: **for** $t_i = t_1; \; t_i \leq t_2; \; t_i \; ++$ **do**
3:    $CA_i \leftarrow EmptySet$
4:    **if** $t_i == t_1$ **then**
5:       $CA_i \leftarrow CA\_Gen(Params, t_i)$
6:    **else**
7:       $CA_i \leftarrow extend(Params, t_i, CA_{i-1})$
8:    **end if**
9:    $ICA.append(CA_i)$
10: **end for**
11: **return** ICA

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strategy consists of the values for each parameter of the SUT $-Params$, the lowest strength t_1 of the covering array in the incremental covering array, and the highest strength t_2 of the covering array . The output of this strategy is an incremental covering array – ICA.

This strategy generates the covering array from lower-strength to higher-strength (line 2). If the current coverage strength t_i is equal to t_1, it just utilizes a covering array generation algorithm to generate the particular covering array (line 4 - 5). Otherwise, it will first take the previous generated covering array CA_{i-1} as seeds, and then utilize covering array generation algorithm to append additional test cases to satisfy higher coverage criteria (line 6 - 7).

Fig.1 presents an example for constructing $ICA([6, 13, 24]; [2, 4], 5, 2)$ by this strategy. In this example, the covering array

c1	0	0	0	0	0
c2	1	1	1	1	0
c3	0	0	1	1	1
c4	1	1	0	0	1
c5	0	1	0	1	0
c6	1	0	1	0	0

2-way

c7	1	0	0	1	1
c8	0	1	1	0	1
c9	0	1	1	0	0
c10	0	0	0	0	1
c11	1	0	0	1	0
c12	0	1	0	1	1
c13	1	0	1	0	1

3-way

c14	1	1	0	0	0
c15	0	0	1	1	0
c16	1	1	1	1	1
c17	0	0	1	0	0
c18	1	0	0	0	0
c19	0	1	0	0	0
c20	0	0	0	1	0
c21	1	1	1	0	0
c22	0	1	1	1	0
c23	1	1	0	1	0
c24	1	0	1	1	0

4-way

Fig. 1: Bottom-up strategy example

generation algorithm used is AETG [4]. The two-way covering array (test cases c_1 to c_6) is directly generated, and the three-way covering array (test cases c_1 to c_{13}) is generated by adding additional test cases (test cases c_7 to c_{13}) based on the previous two-way covering array. The four-way covering array (test cases c_1 to c_{24}) is constructed on the previous three-way covering array. In total, to reach the 4-way covering array, 24 test cases are needed for this strategy.

B. Top-down strategy

This strategy is listed as Strategy 2, which generates covering arrays in the opposite order (line 2) of the bottom-up strategy. Similarly, if the current coverage strength t_i is equal to t_2, it directly generates the particular covering array (line 4 - 5). Otherwise, it will extract the covering array from a higher covering array (CA_{i+1}) (line 6 - 7).

An example for this strategy is given in Fig.2. In this example, we first generated the 4-way covering array $CA(16; 4, 5, 2)$. Then we selected 14 test cases to form a three-covering array $CA(14; 3, 5, 2)$. Next the two-way covering array $CA(8; 2, 5, 2)$ is extracted from $CA(14; 3, 5, 2)$. The rows with dark background from the higher-strength covering arrays represent those selected test cases.

From the two examples, an obvious observation is that for the *top-down* strategy, it has a significant advantage over the *bottom-up* strategy with respect to the size of the 4-way covering array (16 test cases generated by *top-down*, while 24 by *bottom-up*). But when considering the lower-strength covering arrays, the *bottom-up* strategy performs slightly better

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Strategy 2 Top-down strategy

Input: $Params$ ▷ Parameters (and their values)
     t_1 ▷ the lowest strength
     t_2 ▷ the highest strength
Output: ICA ▷ the incremental covering arrays
1:   $ICA \leftarrow EmptySet$
2: **for** $t_i = t_2;\ t_i \geq t_1;\ t_i\ --$ **do**
3:     $CA_i \leftarrow EmptySet$
4:     **if** $t_i == t_2$ **then**
5:       $CA_i \leftarrow CA\_Gen(Params, t_i)$
6:     **else**
7:       $CA_i \leftarrow extract(Params, t_i, CA_{i+1})$
8:     **end if**
9:     $ICA.append(CA_i)$
10: **end for**
11: **return** ICA

4-way

c1	0	0	0	0	0
c2	1	1	0	0	0
c3	0	1	1	0	0
c4	0	0	0	1	1
c5	1	0	0	1	0
c6	0	0	1	0	1
c7	1	0	0	0	1
c8	0	1	0	0	1
c9	1	0	1	0	0
c10	0	1	0	1	0
c11	0	0	1	1	0
c12	1	1	1	0	1
c13	1	1	1	1	0
c14	1	0	1	1	1
c15	0	1	1	1	1
c16	1	1	0	1	1

3-way: c1, c2, c3, c4, c5, c6, c7, c8, c9, c10, c12, c13, c14, c15
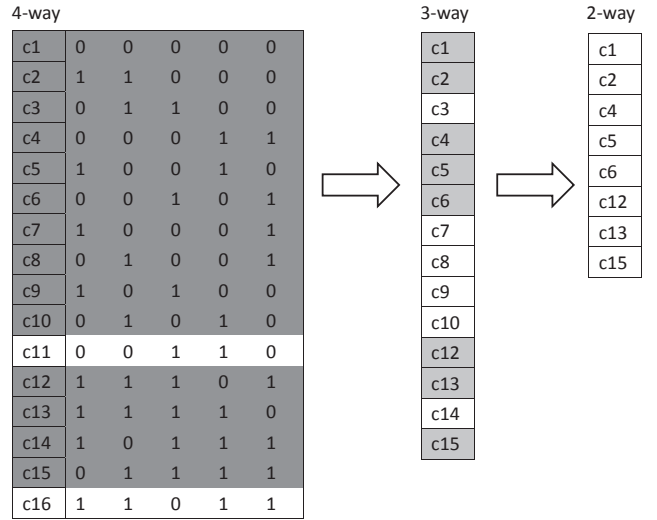
2-way: c1, c2, c4, c5, c6, c12, c13, c15

Fig. 2: Top-down strategy example

(13 and 6 by *bottom-up* for degree 3 and 2, respectively; while 14 and 8 by *top-down*).

IV. IMPLEMENTATION OF THE TWO STRATEGIES

In this section, we will describe a specific implementation of the two strategies proposed in the previous section.

A. Common parts of two strategies

1) Covering array generation method: Our covering array generation approach is IPOG [5], [6], [7], which firstly builds a *t*-way test set for the first *t* parameters, then extends the test set to build a t-way test set for the first *t+1* parameters, and then continues to extend the test set until it builds a t-way test set for all the parameters. We select this algorithm mainly because it is very efficient, that is, it can quickly generate a t-way covering array even though *t* is a relatively large number (up to 6). This is important, as in our experiments, some subjects contain an extremely large input space, which

is unfavorable to apply some time-consuming covering array generation approaches.

2) Constraints handling: Our constraints handling technique is based on Minimum Forbidden Tuples (MFTs) [8], [9], which is well supported by IPOG generation algorithm. A forbidden tuple is a tuple as the value assignment of some parameters that violates constraints. A minimum forbidden tuple is a forbidden tuple of minimum size that covers no other forbidden tuples. Given some constraints for one SUT, we should compute all the MFTs of the SUT, and then limit the test cases to the ones that do not contain any tuple in the MFTs.

B. Implementation of strategy Bottom-up

The key part of strategy *Bottom-up* is seeding existing test cases for higher-way covering array. Specifically, when given a lower-way covering array as seed, we need to eliminated those higher-degree tuples that have already been covered by this covering array. After this, we need to generate additional test cases to cover the un-covered higher-degree tuples until all the higher-degree tuples are covered.

In this paper, we offer two approaches with different seeding process. The first one is simple: We directly take all the test cases in the lower covering array as the initial test set of higher covering array. We later call them the *Bottom-up* approach. The second approach comes from an existing study [3], of which the seeding test cases are consist of two parts: one part is partial test cases (instead of the whole covering array) from the lower-way covering array, the other part comes from an existing incremental covering array which is generated along with this covering array. We later call this approach the *Collaborative bottom-up* approach. The main reason that *collaborative bottom-up* generates distinct incremental covering arrays for one SUT is for handling un-determined failures and fault localization issues.

More specifically, Figure 3 depicts the differences between these two approaches. In this figure, the left side simply shows how do approach *bottom-up* generate incremental covering arrays, while the right side shows the *collaborative bottom-up* approach. From this figure, we can easily learn that the bottom-up is very simple and straightforward, it only needs to build the t-way covering array based on the seed of $t-1$-way covering array. While for *collaborative bottom-up* approach, the process is slightly more complicated. First of all, its target is to generate several incremental covering arrays. For the first one in these incremental covering arrays, it follows the *bottom-up* approach, i.e., take $t-1$-way covering array as the seed to build t-way covering array. For the remaining incremental covering arrays, the t-way covering arrays needs seeding test cases from their own $t-1$-way covering arrays and some test cases from the initially generated $t+1$ covering array (the first incremental covering array). For example, in the second incremental covering array (at the middle) generated by "collaborative bottom-up" approach in Figure 3, we can find some part (E) of the 3-way covering array comes from
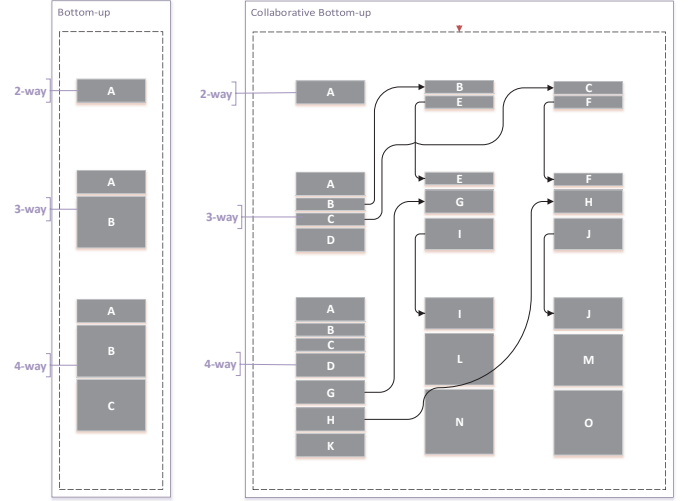

Fig. 3: Bottom-up strategy and Collaborative bottom-up strategy

the 2-way covering array at the middle, while the other part(G) comes from the 4-way covering array at the left.

C. Implementation of strategy Top-down

The key part of the top-down strategy is extracting test cases from higher-way covering array. It is desirable to obtain a minimal t-way covering array CA_t from a $t+1$-way covering array CA_{t+1}. However, this is impractical if CA_{t+1} is too large, because to get the minimal CA_t, we need to exhaustively check every possible subset of the CA_{t+1}. Hence, in this paper, we offer two pragmatic approaches to resolve this issue.

The first approach selects the test cases from CA_{t+1} with the maximal un-covered t-degree interactions at each interaction until the CA_t is constructed. Note that after one test case is selected, the un-covered interactions of each of the remaining test cases should be re-computed. One simple method is to completely search each t-degree interactions of each test case and then judge whether it is already covered. However, it is very time consuming, especially considering the fact that there are more than 60 million 5-degree interactions of one test case for some subjects in our empirical studies. In fact, we do not need to re-compute all the interactions for all the remaining test cases when one test case is selected. Instead, we only need to record the newly covered interactions of the last selected test case, and then check each of the remaining test cases whether it contains some of these newly covered interactions; if so, the number of un-covered interactions should be updated by subtracting the number of these contained interactions. We later call this approach the *top-down* approach.

The second approach selects the test case from CA_{t+1} which has the longest hamming distance from the test cases that have already been selected. The hamming distance between two test cases, say, c_1 and c_2, is computed in the following formula:

$$\frac{\#the\ num\ of\ different\ elements\ between\ c_1\ and\ c_2}{\#the\ num\ of\ all\ the\ elements\ in\ c_1\ and\ c_2}$$

The selection process repeats until we obtain a complete t-way covering array. Note that computing the hamming distance of one test case is much easier than computing the uncovered interactions for the first approach, because the number of elements in one test case is normally much fewer than the number of interactions in one test case. The second approach is referred to as *top-down hamming* approach in the remaining of the paper.

V. RESEARCH QUESTIONS

We set up the following three research questions to investigate the effectiveness and the efficiency of the four approaches which belong to two strategies.

RQ1.What about the size of the incremental covering array generated by the four approaches?

To evaluate these approaches, the size of the covering array is one important metric. In CT, the main goal is to make the size of the covering array as small as possible. With respect to the incremental covering array, instead of focusing on covering array with one specified strength, we should evaluate all the covering arrays with different strengths in it. How to apply the two strategies in practice depends on what strength of the covering arrays they are good at generating. For example, if one strategy can generate smaller size of lower-way covering array, it is a better choice at generating incremental covering array within a short testing time (current software under testing will be soon expired for the releasing of the next version). On the contrary, if one strategy can generate smaller size of higher-way covering array, it is better to be applied on testing the software within a long testing time.

RQ2.How efficient are these approaches in terms of computation time cost?

The computation time that is needed to generate covering array is also a very important metric to evaluate the four approaches. Many approaches in CT is limited to a given time budgeted for searching the optimal covering arrays. But when apply covering array in practice, it is normally not possible to obtain a proper time budgeted in prior. Hence, it is necessary to optimize the covering array generation process to reduce the time cost. Similar to our first research question, we will investigate the time to generate the covering arrays with different test strengths in the incremental covering array.

RQ3.How efficient are these approaches with respect to fault detection?

A τ-way covering array guarantees all the τ-degree (or less than τ-degree) faulty interactions can be detected after execution. However, for different τ-way covering arrays, the rate of faults detection varies. This reason is obvious: The test cases and test sequences are different for those τ-way covering arrays, and hence, the number of tests that must be run varies for detecting specific τ-degree faulty interactions. In this paper, we firstly use the metric "Rate of Fault Detection"(RFD)

[10] to evaluate the efficiency of covering arrays with respect to fault detection.

More formally [10], let T=$\{t_1, t_2, ..., t_m\}$ be a test suite for SUT, with test cases in T to be run in the order: $t_1 \rightarrow t_2 \rightarrow ... \rightarrow t_m$. Let $T_i = \{t_1, t_2, ..., t_i\}$ for $1 \leq i \leq m$, and let $T_i(\tau - degree)$ be the set of t-degree interactions that are covered by test set T_i. Then, the τ way RFD of test suite T is:

τ-RFD$(T) = \sum_{i=1}^{m} \mid T_i(\tau - degree) \mid$.

Note that, the τ-RFD value of one test suite is influenced by the number of tests in this suite. In order to remove the influence of the number of tests, we compute the τ-RFD of each approach by using the same number of tests (for each subject, we will take the minimal size of the covering array generated by the four approaches as the number of tests).

VI. EXPERIMENT SET-UPS

A. Benchmarks

We used 55 SUT as the subjects of our experiments, which are shown in Table II. These subjects are wildly used to evaluate the performance of the covering array generation approach. Among these subjects, the first 20 subjects (from *Banking1* to *Telecom*), are obtained from a recent benchmark created by Segall et al [11], which have already been used in several works [12], [13]. These 20 subjects cover a wide range of applications, including telecommunications, health care, storage and banking systems. The following five subjects (from *SPIN-S* to *Bugzilla*) were firstly introduced by Cohen et al. [14], [15]. Among them, SPIN-S and SPIN-V are two components for model simulation and verification, GCC is a compiler system, Apache is a web server application, and Bugzilla is a web-based bug tracking system. These five subjects have been wildly used in literatures [16], [14], [15], [17], [18], [19], [13]. The last 30 (from Syn1 to Syn30) are synthetic subject models that are generated by Cohen et al. [15]. These synthetic subject models are designed with similar characterization (input space, constraints, etc.) of those real subjects and have been used in following studies[17], [18], [19], [13].

In Table II, the model is presented in the abbreviated form $\#values^{\#number\ of\ parameters}$, e.g., $7^3 6^2$ indicates the software has 3 parameters that can take 7 values and 2 parameters take 6 values. The constraint is presented in the form $\#degree^{\#number\ of\ constraints}$, e.g., $2^3 3^{18}$ means that the SUT contains 3 constraints with 2-degree and 18 constraints with 3-degree.

B. Set-up and procedure

For each SUT listed in Table II, we adopted four approaches i.e., *bottom-up*, *Collaborative bottom-up*, *top-down*, and *top-down hamming*, to generate an incremental covering array from 2-way to 6-way. We recorded the size of each covering array contained in this incremental covering array, the generation time (seconds) that is consumed to generate these covering arrays. After that, we computed the RFD for each covering array.

TABLE II: The models of the SUT

Name	Model	Constraint
Banking1	$3^4 4^1$	5^{112}
Banking2	$2^{14} 4^1$	2^3
CommonProtocal	$2^{10} 7^1$	$2^{10} 3^{10} 4^{12} 5^{96}$
Concurrency	2^5	$2^4 3^1 5^2$
Healthcare1	$2^6 3^2 5^1 6^1$	$2^3 3^{18}$
Healthcare2	$2^5 3^6 4^1$	$2^1 3^6 5^{18}$
Helathcare3	$2^{16} 3^6 4^5 5^1 6^1$	2^{31}
Helathcare4	$2^{13} 3^{12} 4^6 5^2 6^1 7^1$	2^{22}
Insurance	$2^6 3^1 5^1 6^2 11^1 13^1 17^1 31^1$	-
NetworkMgmt	$2^2 4^1 5^3 10^2 11^1$	2^{20}
ProcessorComm1	$2^3 3^6 4^6$	2^{13}
ProcessorComm2	$2^3 3^{12} 4^8 5^2$	$1^4 2^{121}$
Services	$2^3 3^4 5^2 8^2 10^2$	$3^{386} 4^2$
Storage1	$2^1 3^1 4^1 5^1$	4^{95}
Storage2	$3^4 6^1$	-
Storage3	$2^9 3^1 5^3 6^1 8^1$	$2^{38} 3^{10}$
Storage4	$2^5 3^7 4^1 5^2 6^2 7^1 9^1 13^1$	2^{24}
Storage5	$2^5 3^8 5^3 6^2 8^1 9^1 10^2 11^1$	2^{151}
SystemMgmt	$2^5 3^4 5^1$	$2^{13} 3^4$
Telecom	$2^5 3^1 4^2 5^1 6^1$	$2^{11} 3^1 4^9$
SPIN-S	$2^{13} 4^5$	2^{13}
SPIN-V	$2^{42} 3^2 4^{11}$	$2^{47} 3^2$
GCC	$2^{189} 3^{10}$	$2^{37} 3^3$
Apache	$2^{158} 3^8 4^4 5^1 6^1$	$2^3 3^1 4^2 5^1$
Bugzilla	$2^{49} 3^1 4^2$	$2^4 3^1$
Syn1	$2^{86} 3^3 4^1 5^5 6^2$	$2^{20} 3^4 1$
Syn2	$2^{86} 3^3 4^3 5^1 6^1$	$2^{19} 3^3$
Syn3	$2^{27} 4^2$	$2^9 3^1$
Syn4	$2^{51} 3^4 4^2 5^1$	$2^{15} 3^2$
Syn5	$2^{155} 3^7 4^3 5^5 6^4$	$2^{32} 3^6 4^1$
Syn6	$2^{73} 4^3 6^1$	$2^{26} 3^4$
Syn7	$2^{29} 3^1$	$2^{13} 3^2$
Syn8	$2^{109} 3^2 4^2 5^3 6^3$	$2^{32} 3^4 4^1$
Syn9	$2^{57} 3^1 4^1 5^1 6^1$	$2^{30} 3^7$
Syn10	$2^{130} 3^6 4^5 5^2 6^4$	$2^{40} 3^7$
Syn11	$2^{84} 3^4 4^2 5^2 6^4$	$2^{28} 3^7$
Syn12	$2^{136} 3^4 4^3 5^1 6^3$	$2^{23} 3^4$
Syn13	$2^{124} 3^4 4^1 5^2 6^2$	$2^{22} 3^4$
Syn14	$2^{81} 3^5 4^3 6^3$	$2^{13} 3^2$
Syn15	$2^{50} 3^4 4^1 5^2 6^1$	$2^{20} 3^2$
Syn16	$2^{81} 3^3 4^2 6^1$	$2^{30} 3^4$
Syn17	$2^{128} 3^3 4^2 5^1 6^3$	$2^{25} 3^4$
Syn18	$2^{127} 3^2 4^4 5^6 6^2$	$2^{23} 3^4 4^1$
Syn19	$2^{172} 3^9 4^9 5^3 6^4$	$2^{38} 3^5$
Syn20	$2^{138} 3^4 4^5 5^4 6^7$	$2^{42} 3^6$
Syn21	$2^{76} 3^3 4^2 5^1 6^3$	$2^{40} 3^6$
Syn22	$2^{72} 3^4 4^1 6^2$	$2^{31} 3^4$
Syn23	$2^{25} 3^1 6^1$	$2^{13} 3^2$
Syn24	$2^{110} 3^2 5^1 6^4$	$2^{25} 3^4$
Syn25	$2^{118} 3^6 4^2 5^1 6^4$	$2^{23} 3^3 4^1$
Syn26	$2^{87} 3^1 4^3 5^4$	$2^{28} 3^4$
Syn27	$2^{55} 3^2 4^2 5^1 6^4$	$2^{17} 3^3$
Syn28	$2^{167} 3^{16} 4^2 5^3 6^6$	$2^{31} 3^6$
Syn29	$2^{134} 3^7 5^3$	$2^{19} 3^3$
Syn30	$2^{73} 3^3 4^3$	$2^{20} 3^2$

Note that, as we mentioned before, *collaborative bottom-up* generates multiple incremental covering arrays for one SUT to increase their abilities to handle the random or non-determined failures. Hence, to make a fair comparison, we recorded the average data of these covering arrays, which includes the average size, corresponding time cost and RFD, and then compared them with those of other approaches.

We ran all the experiments on a server which has a 6-core CPU of 2.0GHz (Intel Xeon E5-2640 v2), and a 16 GB memory. It took us four weeks in total to obtain all the results. Note that not all the covering arrays can run up to 6 way because of the memory limitation and computing time.

VII. RESULTS AND DISCUSSION

A. RQ1. The size of the incremental covering array

B. RQ2. The time cost of the incremental covering array

C. RQ3. The RFD of the incremental covering array

The results are listed in Fig. 4 and Fig. 5 for covering array size and consuming time, respectively. There are 55 sub figures in these two main figures, one for each subject. In each subject, the x axis lists the covering array strength, which is ranged from 2-way to 6-way. The y axis shows the size of each covering array, which is normalized to between 0 to 1. There are three polygonal lines in each sub-figure, each of which shows the results for one of the three strategies: *Bottom-up*, *Top-down*, and *Collaborative Bottom-up* [3].

One important observation in this figure is that there is a significant advantage of strategy *Bottom-up* over *Top-down* at the size of covering arrays. Specifically, among the 55 subjects, there are 55 subjects (all the subjects) on which *Bottom-up* generates smaller size of 2-way covering array than *Top-down*, 50 subjects on 3-way covering array, 28 subjects on 4-way covering array, and 12 subjects on 5-way covering array. In contrast, *Top-down* only generates smaller size of test cases for 3 subjects on 3-way covering array, 20 subjects on 4-way, 10 subjects on 5-way, and 11 subjects on 6-way.

We list these comparative data in Table III. Column "Bottom-up" shows the number of subjects that strategy *Bottom-up* performs better. We attached the number of test cases that is decreased on average in the parentheses. Column "Top-down" shows the better results for strategy *Top-down*, and Column "Equal" shows the number of subjects that these two strategies generate the same size of covering array.

TABLE III: Comparative data between two strategies (Size)

Degree	Bottom-up #subjects (#test cases)	Top-down #subjects (#test cases)	Equal
2	55 (270.04)	0 (-)	0
3	50 (624.4)	3 (39.0)	2
4	28 (657.71)	20 (36.95)	3
5	12 (638.42)	10 (39.0)	3
6	0 (-)	11 (38.55)	0

Based on Table III, we can learn that, besides the number of subjects, *Bottom-up* strategy also has a significant advantage on the extent to which it has decreased the size of test cases. In fact, *Bottom-up* strategy has decreased the number of test cases ranged from 270 to 657 on average, while *Top-down* strategy just decreased the number of test cases no more than 40.

Above all, the answer to research question 1 is:

Except for the highest-way (6-way) covering array on which *Top-down* strategy has a slight advantage, it falls
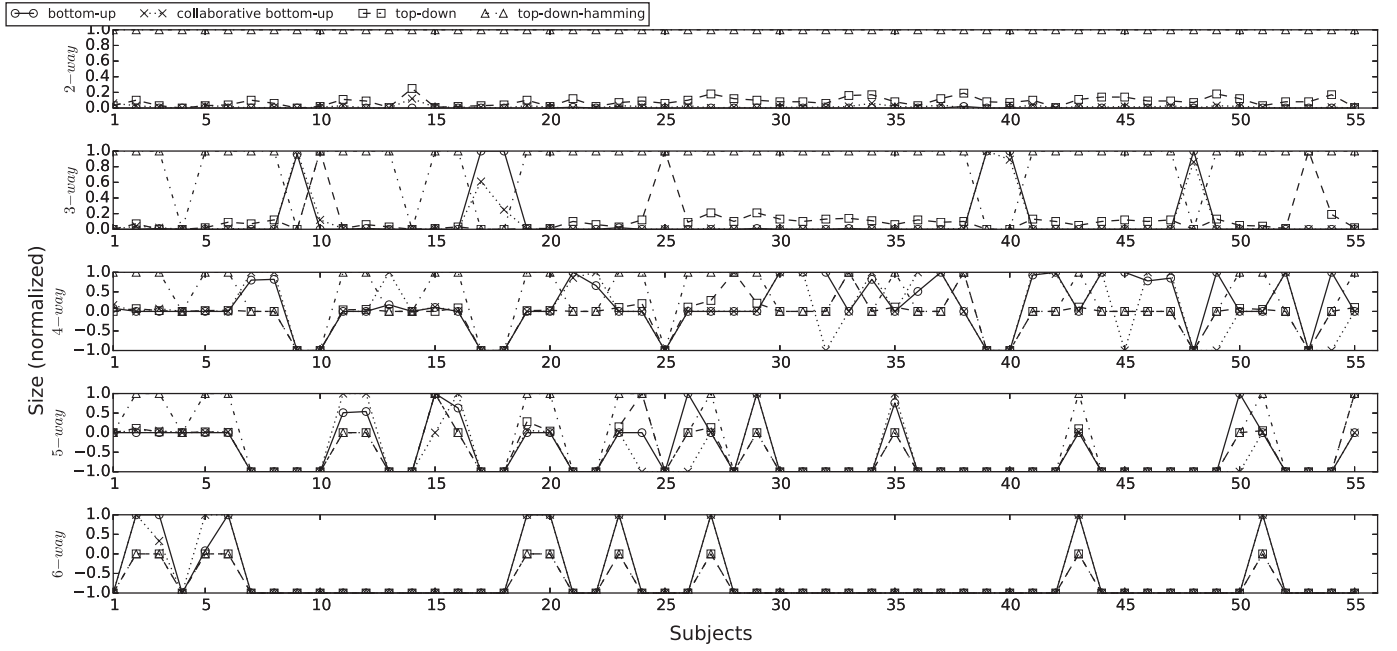
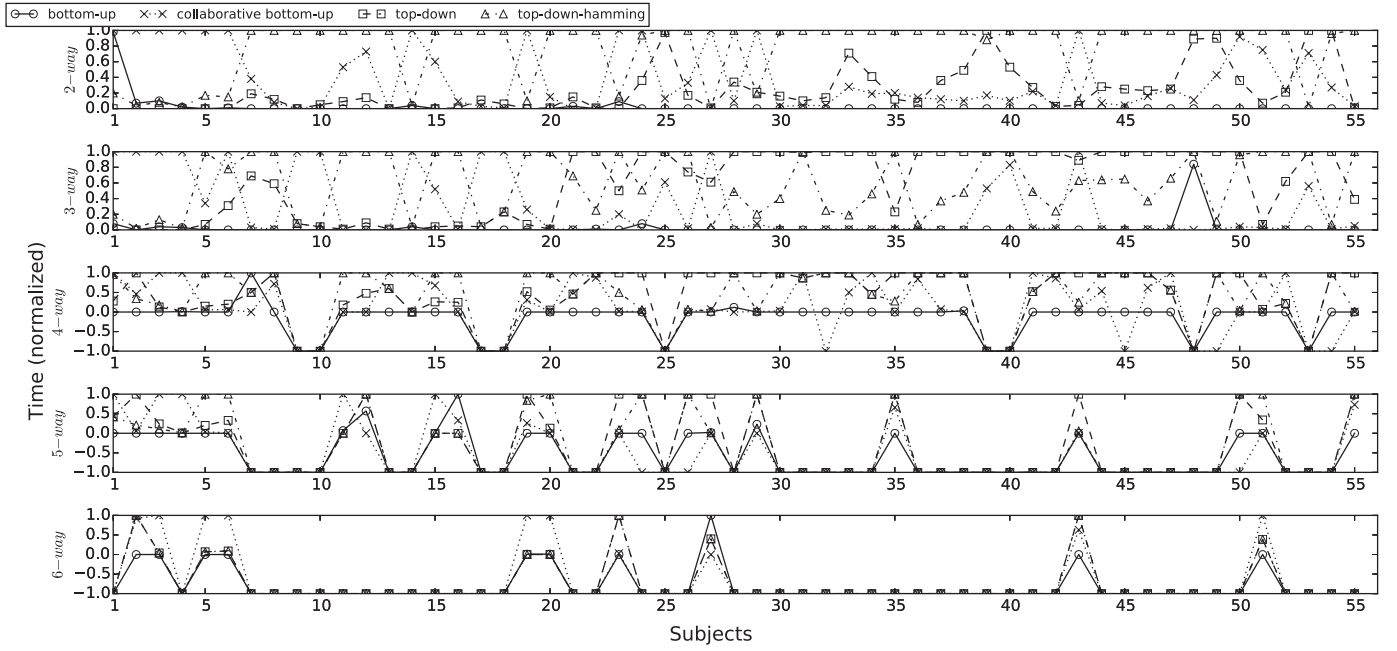Fig. 4: The comparison of the three strategies with respect to the size of covering arrays

Fig. 5: The comparison of the three strategies with respect to the time cost
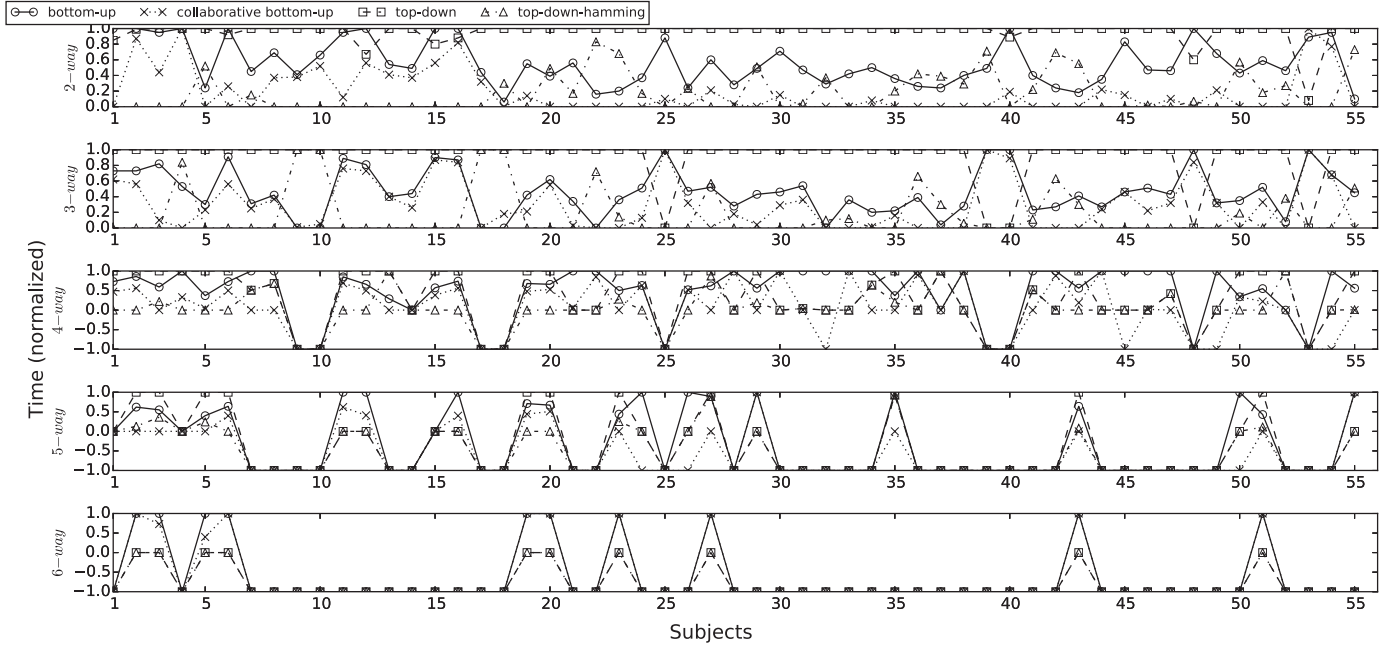
Fig. 6: The comparison of the three strategies with respect to the RFD

far behind strategy *Bottom-up* at the size of generated covering array.

One reason for this result is because the method to extract lower-way covering arrays from higher coverings is not optimal. As mentioned before, considering of the efficiency, we use a greedy method to select test cases from higher covering arrays. This may result in that, for strategy *Top-down*, the number of test cases of the lower-way covering array may be larger than needed. We believe another reason for this result is the covering array generation approach IPOG. This is because that even though for higher-way covering array (6-way), strategy *Top-down* did not have any significant advantages over *Bottom-up*, which indicates that IPOG is not good at generating higher-way covering array.

With respect to the second research question, we can also find that *Bottom-up* performs better than *Top-down*. Similar to the first question, we list the comparative data of time cost in Table IV. Column "Bottom-up" shows the number of subjects that strategy *Bottom-up* performs better. We also attached the seconds that are decreased on average to generate the covering array in the parentheses. Column "Top-down" shows the better results for strategy *Top-down*.

TABLE IV: Comparative data between two strategies (Time)

Degree	Bottom-up	Top-down
	#subjects (#seconds)	#subjects (#seconds)
2	49 (27.17)	6 (0.05)
3	53 (98.82)	2 (0.01)
4	48 (456.41)	3 (0.01)
5	21 (589.39)	4 (0.44)
6	8 (205.44)	3 (2.18)

From this table, it is easy to conclude that for most subjects,

strategy *Bottom-up* performs more efficiently with respect to the time cost. In fact, the time reduction of *Bottom-up* is ranged from 27 seconds to 289 seconds, while *Top-down* reduced less than 1 second for most subjects.

Besides this, another important observation is that strategy *Bottom-up* can run more higher-way covering arrays. Specifically, there are 4 subjects ('Insurance', 'NetworkMgmt', 'Storage4', and 'Storage5') on which *Bottom-up* can run more 4-way covering arrays than *Top-down*, 14 subjects ('Healthcare3', 'Healthcare4', 'Insurance', 'NetworkMgmt', etc.) that can run more 5-way covering arrays, and 10 subjects ('Healthcare3', 'Healthcare4', 'Insurance', 'NetworkMgmt', 'ProcessorComm1', etc.) that can run more 6-way covering arrays. For these subjects, strategy *Top-down* can not completely obtain the corresponding higher-way covering arrays within a proper time limitation.

Hence, the answer to the second question is :

Strategy *Bottom-up* is the better approach when considering the time cost for generating incremental covering array.

For the third question, we have the following observations:
First,
Second.
In summary, the answer to the research question 3 is :
For the last research question, there are several observations:

At first sight of Fig 4, we can hardly distinguish the traditional approach and *Bottom-up* strategy, which indicates that the two strategies has a similar performance at the size of generated covering array. This is easy to understand, as we mentioned before, the approach [3] is also a special version of *Bottom-up* strategy. But on closer inspection, these still exists

differences between them.

TABLE V: Compare Bottom-up strategy with Collaborative bottom-up strategy(Size)

Degree	Bottom-up	Collaborative bottom-up	Equal
	#subjects (#test cases)	#subjects (#test cases)	
2	45 (2.33)	6 (0.83)	4
3	24 (1.82)	21 (2.33)	10
4	24 (11.53)	7 (2.24)	17
5	18 (69.33)	2 (1.0)	14
6	1 (48.67)	1 (2.0)	16

We list the comparative data in Table V, which is similar to Table III. We can learn that there is a slight advantage (around 1 to 69 test case) of our approach *Bottom-up* over the traditional approach.

With respect to the time cost, it is easy to figure out that our approach *Bottom-up* performs better than the traditional approach. Similar to the size, we list the comparative data in Table VI for a clear view. In this table, we can learn that almost for all the subjects (54 for degree 2, 54 for degree 3, 46 for degree 4, 28 for degree 5, and 14 for degree 6), our approach *Bottom-up* costs less time than the traditional approach. The reason why our approach performs more efficiently is mainly because our approach does not need to generate a higher-way covering array in prior. This task is very time-consuming if the input space is too large.

TABLE VI: Compare Bottom-up strategy with Collaborative bottom-up strategy (Time)

Degree	Collaborative bottom-up	Top-down
	#subjects (#seconds)	#subjects (#seconds)
2	54 (0.18)	1 (0.08)
3	54 (0.82)	1 (5.9)
4	46 (80.19)	2 (30.4)
5	28 (716.38)	6 (181.64)
6	14 (2.31)	4 (431.43)

We do not give a closer inspection for comparing the traditional approach with *Top-down* strategy. This is because based on Fig. 4 and Fig. 5, we can easily find that the traditional approach also has a significant advantage over *Top-down* strategy at the covering array size and time cost.

Above all, the answer to the 4th question is:

With respect to the size of incremental covering array, strategy *Bottom-up* is slightly better than the traditional approach. Strategy *Bottom-up* also needs less time than the traditional approach to generate the covering arrays.

VIII. THREATS TO VALIDITY

There are several threats to validity in our studies.

First, our incremental covering array generation approach is implemented by using IPOG. Although IPOG can efficiently generate higher-way covering array for the SUT with large input space, it may generate too many test cases (due to the greedy strategy). It is necessary to try more covering array generation approaches to make the conclusion more general.

Second, the method to extract lower-way covering arrays from higher coverings is a greedy algorithm in this paper. This may result in that the size of the lower-way covering arrays generated by *Top-down* strategy may be larger than needed. If adopted some other methods, e.g., the post-optimal approach [20], [21], the number of test cases generated by *Top-down* strategy may be significantly decreased.

At last, our results are based on the 55 wildly used input models. That is, with other input models, the results may be different from this paper. It is appealing to further study the influence of the characteristics of the input models, e.g., the number of parameters, and the constraints, on the results of incremental covering array generation approach.

IX. RELATED WORK

Combinatorial testing has been proven to a effective testing technique in practice [22], especially on domains like configuration testing [23], [24], [25] and software inputs testing [4], [26], [27]. The most important task in CT is to generate covering arrays, which support the checking of various valid interactions of factors that influence the system under testing.

Nie et al. [1] gave a survey for combinatorial testing, in which the methods for generating covering arrays are classified. However, traditional static covering arrays can be hardly directly applied in practice, hence many adaptive methods are proposed.

Cohen et al. [28], [15] studied the constraints that can render some test cases in the covering array invalid. They proposed a SAT-based approach to avoid the impact. Nie et al.[29] proposed a model for adaptive CT, in which both the failure-inducing interactions and constraints can be dynamically detected and removed in the early test cases generation iteration. Further, the coverage strength of covering array can be adaptively changed as required.

S.Fouché et al. [3] proposed the incremental covering array, and gave a method to generate it. The method can be deemed as a special case of *bottom-up* strategy, with the only difference being that it used multiple lower-strength covering arrays instead only one in this paper to construct the higher-strength covering array. This is because their work needs to characterize the failure-inducing interactions in the covering array, in which multiple covering arrays can support a better diagnosis.

Calvagna et al. [30] proposed another work to generate higher-way in an iterative way. Different than our work, its main task to generate a covering array with a specific given degree. It builds a relationship between higher-way covering array with lower-covering array. Based on this, it can reduce the higher-way covering array generation problem to multiple lower covering array generation problem.

X. CONCLUSIONS AND FUTURE WORKS

Incremental covering array is an important object to make CT used in practice, because it makes CT more adaptive, such that we do not need to give the specific test strength in prior. This paper formally defined the incremental covering array and gave a proof to its existence. Furthermore, this paper

proposed two strategies for generating incremental covering arrays. Experimental results show that strategy *bottom-up* have a significant advantage over *top-down* at the size of the covering arrays and time cost. It is also performs more efficient than traditional approach with respect to the time cost.

As a future work, we will apply more covering array generation algorithms, to compare their performance at generating incremental covering arrays. Another interesting work is to combine the two strategies, so that we can first select a median coverage strength t and generate incremental covering arrays by *top-down* strategy. Then if the maximal-way covering array is generated, we can use *bottom-up* strategy to generate further higher-strength covering arrays. We believe such a combination strategy may offer a better performance.

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