Identifying minimal failure-causing schemas in the presence of multiple faults

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Combinatorial testing (CT) has been proven effective in revealing the failures caused by the interaction of factors that affect the behavior of a system. The theory of Minimal Failure-Causing Schema (MFS) has been proposed to isolate the root cause of a failure after CT. Most algorithms that aim to identify MFS focus on handling a single fault in the System Under Test (SUT). However, we argue that multiple faults are more common in practice, under which masking effects may be triggered so that some failures cannot be observed. The traditional MFS theory lacks a mechanism to handle such effects; hence, they may incorrectly isolate the MFS. To address this problem, we propose a new MFS model that takes into account multiple faults. We first formally analyse the impact of the multiple faults on existing MFS identifying algorithms, especially in situations where masking effects are triggered by multiple faults. We then develop an approach that can assist traditional algorithms to better handle multiple faults. Empirical studies were conducted using several kinds of open-source software, which showed that multiple faults with masking effects do negatively affect traditional MFS identifying approaches and that our approach can help to alleviate these effects.

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1. INTRODUCTION

With the increasing complexity and size of modern software, many factors, such as input parameters and configuration options, can affect the behaviour of the SUT. The failures caused by the interaction of these factors can make software testing challenging, especially when the interaction space is large. In the worst case, we need to examine every possible interaction of these factors as each interaction may cause unique

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39:2 X. Niu et al.

Table I. MS word example

id	Highlight	$Status\ bar$	Bookmarks	$Smart\ tags$	Outcome
1	On	On	On	On	PASS
2	Off	Off	On	On	PASS
3	Off	On	Off	Off	Fail
4	On	Off	Off	On	PASS
5	On	Off	On	Off	PASS

failure [Song et al. 2012]. While exhaustive testing achieves maximal test coverage, it is impractical and uneconomical. One remedy for this problem is Combinatorial Testing (CT)¹, which systematically samples the interaction space and selects a relatively small set of test cases that cover all valid interactions, with the number of factors involved in each interaction no more than a prior fixed integer, i.e., the *strength* of the interaction. Many works in CT aim to construct the smallest set of test cases [Cohen et al. 1997; Bryce et al. 2005; Cohen et al. 2003; Lei et al. 2008], which is also called *covering array*.

Once failures are detected by a covering array, the failure-inducing interactions in the failing test cases should be isolated. This task is important as it can facilitate debugging efforts by reducing the code scope that needed for inspection [Ghandehari et al. 2012]. However, information from a covering array sometimes is not sufficient to identify the location and number of the failure-inducing interactions [Colbourn and McClary 2008]. Thus, additional information is needed. Consider the following example [Bach and Schroeder 2004], Table I presents a two-way covering array for testing an MS-Word application in which we want to examine various interactions of options for 'Highlight', 'Status Bar', 'Bookmarks' and 'Smart tags'. Assume the third test case failed. We can get six two-way suspicious interactions that may be responsible for this failure. They are respectively (Highlight: Off, Status Bar: On), (Highlight: Off, Bookmarks: Off), (Highlight: Off, Smart tags: Off), (Status Bar: On, Bookmarks: Off), (Status Bar: On, Smart tags: Off), and (Bookmarks: Off, Smart tags: Off). Without additional information, it is difficult to figure out the specific interactions in this suspicious set that caused the failure. In fact, considering that the higher strength interactions could also be failure-inducing interactions, e.g., (Highlight: Off, Status Bar: On, Smart tags: Off), the problem becomes more complicated.

To address this problem, prior work [Nie and Leung 2011a] specifically studied the properties of the failure-inducing interactions in the SUT, based on which additional test cases were generated to identify them. Other approaches to identify the failure-inducing interactions in the SUT include building a tree model [Yilmaz et al. 2006], adaptively generating additional test cases according to the outcome of the last test case [Zhang and Zhang 2011], ranking suspicious interactions based on some rules [Ghandehari et al. 2012], and using graphic-based deduction [Martínez et al. 2008], among others.

Most existing approaches mainly focus on the ideal scenario in which SUT only contains one fault, under which the outcomes of test cases can be simply categorized into failure or pass. However, in this paper, we argue that SUT with multiple faults is the more common testing scenario in practice, which will result in many distinguished failures as outcomes of test cases, and moreover, this affects the effectiveness of Failure-inducing Interactions Identifying (FII) approaches. One main impact of multiple faults on FII approaches is the masking effect. A masking effect [Dumlu et al. 2011; Yilmaz et al. 2014] occurs when some failures prevent test cases from checking interactions that are supposed to be tested. Take the Linux command *Grep* for example. We no-

¹Another term for CT is Combinatorial Interaction Testing, which is abbreviated as CIT. In this paper, they are uniformly cited as Combinatorial testing (CT).

ticed that there are two different failures reported in the bug tracker system. The first 2 claims that Grep incorrectly matches unicode patterns with '<<>>', while the second 3 claims an incompatibility between option '-c' and '-o'. When we put these two scenarios into one test case, only one failure will be observed, which means the other failure is masked by the observed failure. This effect will prevent test cases from executing normally, leading to incorrect judgment of the correlation between the interactions checked in the test case and the failure that has been masked. This effect was firstly noted by Dumlu and Yilmaz in [Dumlu et al. 2011], in which they found that the masking effects in CT can prevent traditional covering array in testing some interactions.

As masking effect can negatively affect the performance of FII approaches, a natural question is how this effect biases the results of these approaches. In this paper, we formalize the process of identifying the failure-inducing interactions under the circumstances in which masking effects exist in the SUT and try to answer this question. One insight from the formal analysis is that we cannot completely avoid the impact of masking effects even if we do exhaustive testing. Even worse, either ignoring the masking effects or treating different failures as the same failure is detrimental to the FII process.

To address this concern, we propose a strategy to alleviate this impact by adopting a divide and conquer framework. With this framework, FII approaches is scheduled to separately handle each failure in the SUT. Specifically, for a particular failure, FII approaches only focus on the test cases that either pass or trigger the same failure under analysis. Test cases that triggered other different failures will be replaced with some newly generated test cases. In this way, FII approaches can properly work with little interference from the negative masking effects.

The key to our strategy is to search for a test case that does not trigger *unexpected* failures, i.e., failures different from the one under analysis. To guide the search process, a natural idea is to take some characteristics from the existing test cases, and make the characteristics of the newly searched test case as disparate from the test cases which triggered unexpected failures as possible. To reach this target, we define the *suspiciousness* between a factor and the failure. The higher the *suspiciousness* a factor is related to a particular failure, the greater the likelihood that the factor will trigger this fault. We then use the integer linear programming (ILP) technique to find a test case which has the least *suspiciousness* with unexpected failures.

To evaluate the effectiveness of our approach, we applied our strategy on the FII approach FIC_BS [Zhang and Zhang 2011]. The subjects used were two open-source software systems found in the developers' forum in the Source-Forge community. Through studying their bug reports in the bug tracker system as well as their user's manuals, we built a testing model which can reproduce the reported bugs with given test cases. We then compared the FII approach augmented with our strategy to the original FII approach. We further empirically studied the performance of the important component of our strategy – searching satisfied test cases. To conduct this study, we compared our approach with the augmented FII approach by randomly searching satisfied test cases. We finally compared our approach with the only existing masking handling technique – FDA-CIT [Yilmaz et al. 2014]. Our studies showed that our replacing strategy as well as the searching test case component achieved a better performance than the traditional approaches when the subject encountered multiple faults, especially when these faults can induce masking effects.

The main contributions of this paper are:

²http://savannah.gnu.org/bugs/?29537

³http://savannah.gnu.org/bugs/?33080

39:4 X. Niu et al.

```
public float foo(int a, int b, int c, int d){
   //step 1 will cause an exception when b == c
   float x = (float)a / (b - c);

   //step 2 will cause an exception when c < d
   float y = Math.sqrt(c - d);

   return x+y;
}</pre>
```

Fig. 1. A simple program foo with four input parameters

- We formally analysed the relationships between failure-inducing interactions and test sets. (Section 3)
- We studied the impact of the masking effects caused by multiple faults on FII approaches. (Section 4)
- We proposed an efficient test case replacement strategy to alleviate the impact of these effects (Section 5)
- We conducted several empirical studies and showed that our strategy can assist FII approaches to achieve better performance in identifying failure-inducing interactions in the SUT with masking effects. (Section 8)

2. MOTIVATING EXAMPLE

We constructed a small example to illustrate the motivation of our approach. Assume a method *foo* has four input parameters: a, b, c, and d. The four parameter types are all integers and their values are: $v_a = \{7,11\}, v_b = \{2,4,5\}, v_c = \{4,6\}, v_d = \{3,5\}$. The code of *foo* is shown in Figure 1.

There are two potential failures of foo: first, in step 1 we can get an Arithmetic Exception when b is equal to c, i.e., b=4 and c=4, that causes a division by zero. Second, another Arithmetic Exception will be triggered in step 2 when c < d, i.e., c=4 and d=5, taking square root of a negative number. So the expected failure-inducing interactions in this example should be (-, 4, 4, -) and (-, -, 4, 5).

FII approaches do not consider the code detail; instead, they apply black-box testing, i.e., feed inputs to the programs and execute them to observe the result. The basic proposition of FII approaches is that the failure-inducing interactions for a particular failure can only appear in those test cases that trigger this fault. FII approaches often aim at using as few test cases as possible to get the same (or approximate) result as exhaustive testing, so the results derived from an exhaustive testing set are the best that FII approaches can achieve. Here, we will show how exhaustive testing works to identify the failure-inducing interactions for the program.

We first generate every possible test case listed in the column "test case" of Table II. The execution results are listed in the result column of Table II. In this column, PASS means that the program runs without any exception. $Ex\ 1$ indicates that the program triggered an exception corresponding to step 1 and $Ex\ 2$ indicates the program triggered an exception corresponding to step 2. From the data listed in Table II, we can determine that (-, 4, 4, -) must be the failure-inducing interaction of $Ex\ 1$ as all the test cases that triggered $Ex\ 1$ contain this interaction. Similarly, interactions (-, 2, 4, 5) and (-, 5, 4, 5) must be the failure-inducing interactions of $Ex\ 2$. We list these interactions and the corresponding exceptions in Table III.

Note that in this example we did not get the expected result with traditional FII approaches. The failure-inducing interactions for Ex 2 are (-,2,4,5) and (-,5,4,5), respectively, instead of the expected interaction (-,-,4,5). So why did we fail to get the

id test case result id test case result (7, 2, 4, 3)PASS 13 (11, 2, 4, 3)PASS (7, 2, 4, 5)Ex 2 (11, 2, 4, 5)Ex 2 14 (7, 2, 6, 3)PASS 15 (11, 2, 6, 3)PASS (7, 2, 6, 5)PASS (11, 2, 6, 5)16 PASS (7, 4, 4, 3)(11, 4, 4, 3)Ex 1 Ex 1 (7, 4, 4, 5)Ex 1 18 (11, 4, 4, 5)Ex 1 (7, 4, 6, 3)PASS 19 (11, 4, 6, 3)PASS (7, 4, 6, 5)PASS 20 (11, 4, 6, 5)PASS (7, 5, 4, 3)PASS 21 (11, 5, 4, 3)PASS 10 (7, 5, 4, 5)Ex 2 $\overline{22}$ (11, 5, 4, 5)Ex 2 23 (7, 5, 6, 3)PASS (11, 5, 6, 3)PASS PASS 24 (11, 5, 6, 5)12(7, 5, 6, 5)PASS

Table II. test cases and their corresponding result

Table III. Identified failure-inducing interactions and their corresponding Exception

Failure-inducing interaction	Exception
(-, 4, 4, -)	Ex 1
(-, 2, 4, 5)	Ex 2
(-, 5, 4, 5)	Ex 2

(-,-,4,5)? The reason lies in *test case* 6 (7,4,4,5) and *test case* 18 (11,4,4,5). These two test cases contain the interaction (-,-,4,5), but they did not trigger Ex 2; instead, Ex 1 was triggered.

Now consider the source code of *foo*. If Ex 1 is triggered, it will stop executing the remaining code and report the exception result. In other words, Ex 1 may mask Ex 2. Let us re-examine the interaction (-,-,4,5). If we suppose that *test case* 6 and *test case* 18 should trigger Ex 2 if they did not trigger Ex 1, then we can conclude that (-,-,4,5) should be the failure-inducing interaction of Ex 2, which is identical to the expected one. However, we cannot get this result, unless we fix the code that triggers Ex 1 and re-execute all the test cases.

So in practice, when we lack resources to execute all the test cases repeatedly or can only do black-box testing, a more economical and efficient approach to alleviate the masking effect on FII approaches is desired.

3. FORMAL MODEL OF MINIMAL FAILURE-CAUSING SCHEMA

This section presents some definitions and propositions for a formal description of failure-inducing interactions and test sets.

3.1. Minimal Failure-causing Schemas in CT

Assume that the behaviour of a SUT is influenced by k parameters, and each parameter p_i has a_i discrete values from the finite set V_i , i.e., $a_i = |V_i|$ (i = 1,2,...,k). In practice, these parameters can represent many factors, such as input variables, run-time options, building options, etc. Next we will give some formal definitions, some of them (Definitions 3.1, 3.3, 3.4) were originally defined in [Nie and Leung 2011b].

Definition 3.1. A *test case* of a SUT is an array of k values, one for each parameter of the SUT, which is denoted as a k-tuple $(v_1, v_2,...,v_k)$, where $v_1 \in V_1, v_2 \in V_2 ... v_k \in V_k$.

For the example in Section 2, (a = 7, b = 2, c = 4, d = 3) is a test case, which is actually a group of values being assigned to each input parameter.

Definition 3.2. A failure is an abnormal execution of a test case.

39:6 X. Niu et al.

In CT, such a *failure* can be a thrown exception, compilation error, assertion failure or constraint violation. In this paper, failures are classified according to the the specific *fault* information. For example, if failures have the same exception traces information, they are treated as the same failure. The main point in this paper is to study the impact of multiple different *failures* on failure-inducing interactions identification.

To facilitate our discussion, we introduce the following assumptions that will be used throughout this paper:

Assumption 1. The execution result of a test case is deterministic.

This assumption is the most common assumption of CT fault diagnosis. It indicates that the outcome of executing a test case is reproducible and will not be affected by some random events.

ASSUMPTION 2. Different failures in the SUT can be distinguished by various information such as exception traces, state conditions, or the like.

This assumption indicates that the testers can detect different failures during testing. As different failures will complicate fault diagnosis tasks, distinguishing them is the first step to resolve them.

Assumption 3. All the tests are valid in the SUT, i.e., there is no inter-option constraints in the SUT.

Here *option* indicates the parameter of a SUT. This assumption shows that we can always determine the outcome after executing a test case, i.e., either pass or fail with some exceptions.

In practice, these assumptions will not always be satisfied. Later we will discuss their impacts on the theories and approach proposed in this paper, as well as the measures to alleviate them. Particulary for the third assumption, we later will show that one type of inter-option constraint is essentially equal to a specific failure. Thus we can directly use the approach in this paper to solve it.

Now let us consider the condition that some failures are triggered by some test cases. It is then desirable to determine the cause of these failures and hence some parameter values of the failing test cases must be analysed.

Definition 3.3. For the SUT, the τ -tuple $(-,v_{b_1},...,v_{b_{\tau}},...)$ is called a τ -degree schema $(0 < \tau \le k)$ when some τ parameters have fixed values and the others can take on their respective allowable values, represented as "-".

When $\tau = k$, τ -degree *schema* is actually a test case. Furthermore, if every fixed value in a schema is in a test case, we say this test case *contains* the schema.

For example, (-, 4, 4, -) in Table III is a 2-degree schema. And the test case (7, 4, 4, 3) contains this schema.

Definition 3.4. Let c_1 be a m-degree schema, c_2 be an n-degree schema in the SUT, and m < n. If all the fixed parameter values in c_1 are also in c_2 , then c_2 subsumes c_1 . In this case, we can also say that c_1 is a sub-schema of c_2 , and c_2 is a super-schema of c_1 , denoted as $c_1 \prec c_2$.

For example, in the motivating example, the 2-degree schema (-, 4, 4, -) is a subschema of the 3-degree schema (-, 4, 4, 5), that is, $(-,4,4,-) \prec (-,4,4,5)$.

According to definition 3.4, it is obvious that the subsuming relationship ' \prec ' is transitive, i.e., if $c_1 \prec c_2, c_2 \prec c_3$, then $c_1 \prec c_3$.

Definition 3.5. If for any test case, as long as it contains the schema c, it will trigger a particular fault F. Then we call c the *failure-causing schema* of F. Additionally, if

none of the sub-schema of c is the failure-causing schema of F, we then call c the Minimal Failure-causing Schema (MFS) of F.

In fact, MFS is identical to the failure-inducing interactions discussed previously. Identifying MFS helps to focus on the root cause of a failure and thus facilitates the debugging efforts. Note that all the failures discussed in this paper are option-related [Yilmaz et al. 2006]. That is, all the failures are caused by the interactions of the parameter values in the SUT. Another noteworthy thing is that, in practice, the MFS definition (Section 3.5) may not be valid. This is because in some specific cases, e.g., the masking problems which we will discussed later, we may not determine whether some test cases will trigger the particular failure of F, or not.

Some notations used later are listed below for convenient reference:

- -k: The number of parameters that influence the SUT.
- $-V_i$: The set of discrete values that the *i*th parameter of the SUT can take.
- $-T^*$: The exhaustive set of test cases for the SUT. For a SUT with k parameters, and each parameter can take $|V_i|$ values, the number of test cases in T^* is $\prod_{i=1}^{i < -k} |V_i|$. Note that some test cases may be invalid if there exists constraints among the parameters.
- -T: A set of test cases. (Similarly for $T_i, T_j,$)
- $-\bar{T}$: The complementary test set of T, i.e., $\bar{T} \cup T = T^*$, $\bar{T} \cap T = \emptyset$.
- $-A \setminus B$: The set of elements that belong to set A but not to B. For example $T_i \setminus T_i$ indicates the set of test cases that belong to set T_i , but not to T_j .
- -L: The number of faults contained in the SUT.
- $-F_m$: The mth fault in the SUT ($1 \le m \le L$); A failure which is classified to fault fault F_m is called *failure* of F_m .
- $-T_{F_m}$: All the test cases that can trigger the failure of F_m in the SUT.
- $-\mathcal{T}(c)$: All the test cases that contain the schema c in the SUT. Based on the definition of MFS, we know that if schema c is an MFS of F_m , then $\mathcal{T}(c) \subseteq T_{F_m}$. Note that, there may be multiple MFS for F_m
- $-\mathcal{I}(t)$: All the schemas that are contained in the test case t, e.g., $\mathcal{I}((111)) = \{(1-t)\}$ $-)(-1-)(-1)(11-)(1-1)(-11)(111)\}.$ $-\mathcal{I}(T): \text{All the schemas that are contained in test set } T, \text{ i.e., } \mathcal{I}(T) = \bigcup_{t \in T} \mathcal{I}(t).$
- $-\mathcal{S}(T)$: All the schemas that are only contained in test set T (Referred to as Special schemas); $S(T) = I(T) \setminus I(T)$.
- $-\mathcal{C}(T)$: A set of the minimal schemas that are only contained in test set T (Referred to as Minimal schemas); $C(T) = \{c | c \in S(T) \text{ and } \exists c' \prec c, s.t., c' \in S(T)\}.$

3.2. Relations between schemas and test sets

PROPOSITION 3.6 (SMALLER SCHEMA c HAS A LARGER $\mathcal{T}(c)$). For schemas c_1 , c_2 , if $c_1 \prec c_2$, then all the test cases that contain c_2 must also contain c_1 , i.e., $\mathcal{T}(c_2) \subseteq \mathcal{T}(c_1)$.

We omit the proof of this proposition as it is quite obvious. Suppose a SUT with four binary parameters, which can be denoted as SUT(24). Table IV illustrates an example of the Proposition 3.6. The left column lists the schema $c_2 = (0,0,-,-)$ as well as all the test cases in $\mathcal{T}(c_2)$, while the right column lists the schema $c_1 = (0, -, -, -)$ and $\mathcal{T}(c_1)$. We can see that when $c_1 \prec c_2$, $\mathcal{T}(c_2) \subseteq \mathcal{T}(c_1)$.

PROPOSITION 3.7 (SPECIAL SCHEMA SET OF TEST SET T). For any test set T of the SUT, $\bigcup_{c \in S(T)} \mathcal{T}(c) = T$.

PROOF. As $\mathcal{S}(T) = \mathcal{I}(T) \setminus \mathcal{I}(\bar{T})$, $\forall c \in \mathcal{S}(T), \ c \in \mathcal{I}(T) \ and \ c \notin \mathcal{I}(\bar{T})$. Then $\forall t \in \mathcal{T}(c), t \ contains \ c$, indicating that $t \in T$. Hence, $\mathcal{T}(c) \subseteq T$. Then $\bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c) \subseteq T$.

Table IV. Example of Proposition 3.6

	c_1
	(0, -, -, -)
c_2	$\mathcal{T}(c_1)$
(0, 0, -, -)	(0, 0, 0, 0)
$\mathcal{T}(c_2)$	(0, 0, 0, 1)
(0, 0, 0, 0)	(0, 0, 1, 0)
(0 , 0 , 0, 1)	(0, 0, 1, 1)
(0 , 0 , 1, 0)	(0, 1, 0, 0)
(0, 0, 1, 1)	(0, 1, 0, 1)
	(0, 1, 1, 0)
	(0, 1, 1, 1)

On the other hand, $\forall t \in T$, $\exists c' \in \mathcal{I}(t)$, such that $c' \notin \mathcal{I}(\bar{T})$ (at least it holds when c' = t). Hence, $c' \in \mathcal{S}(T)$. Obviously $t \in \mathcal{T}(c') \subseteq \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c)$. Therefore, $T \subseteq \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c)$. \square

PROPOSITION 3.8 (MINIMAL SCHEMA SET OF TEST SET T). For any test set T of the SUT, $\bigcup_{c \in C(T)} \mathcal{T}(c) = T$.

PROOF. As $\mathcal{C}(T) = \{c | c \in \mathcal{S}(T) \ and \ \not\exists c' \prec c, s.t., c' \in \mathcal{S}(T)\}$, indicating that $\mathcal{C}(T) \subseteq \mathcal{S}(T)$. It is then obviously $\bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c) \subseteq \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c)$. Hence, we just need to prove that $\bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c) \subseteq \bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c)$.

 $\forall t \in \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c), \ \exists c \in \mathcal{S}(T), \ s.t., t \in \mathcal{T}(c).$ According to the definition of $\mathcal{C}(T), \ \exists c' \in \mathcal{C}(T), s.t., \ c' = c \ or \ c' \prec c.$ Correspondingly $\mathcal{T}(c') = \mathcal{T}(c), \ or \ \mathcal{T}(c) \subseteq \mathcal{T}(c')$ by Proposition 3.6. Hence, $t \in \mathcal{T}(c') \subseteq \bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c).$

Therefore, $\bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c) = \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c) = T$. \square

Table V gives an example of T^* , T, \bar{T} , $\mathcal{S}(T)$ and $\mathcal{C}(T)$ in SUT(2³). We can find that all the schemas in $\mathcal{S}(T)$ and $\mathcal{C}(T)$ are only contained in test set T, and for any $t \in T$, it contains at least one schema in $\mathcal{S}(T)$ and $\mathcal{C}(T)$. Additionally, $\mathcal{C}(T)$ is a minimal schema set which filters those super schemas in $\mathcal{S}(T)$.

Table V. Example of the special and minimal schemas

T^*	T	\bar{T}	$\mathcal{S}(T)$	C(T)
(0, 0, 0)	(0, 0, 0)		(0, 0, -)	(0, 0, -)
(0, 0, 1)	(0, 0, 1)		(0, -, 0)	(0, -, 0)
(0, 1, 0)	(0, 1, 0)		(0, 0, 0)	
(0, 1, 1)		(0, 1, 1)	(0, 0, 1)	
(1, 0, 0)		(1, 0, 0)	(0, 1, 0)	
(1, 0, 1)		(1, 0, 1)		
(1, 1, 0)		(1, 1, 0)		
(1, 1, 1)		(1, 1, 1)		

Let T_{F_m} denotes the set of all the test cases triggering failure of F_m , then $\mathcal{C}(T_{F_m})$ actually is the MFS set of F_m .

According to the definition of $\mathcal{C}(T)$, one observation is $\mathcal{C}(T) \subseteq \mathcal{S}(T)$, and for any schema in $\mathcal{S}(T)$, it either belongs to $\mathcal{C}(T)$, or is the super schema of one element of $\mathcal{C}(T)$, i.e., $\forall c \in \mathcal{S}(T), \exists c' \in \mathcal{C}(T), s.t., c' = c, \ or \ c' \prec c.$

PROPOSITION 3.9 (MINIMAL SCHEMA OF THE SUBSET OF TEST SET T). For any test set T and schema c of the SUT, if $T(c) \subseteq T$, $c \in S(T)$.

PROOF. Assume $c \notin \mathcal{S}(T)$, i.e., $c \notin \mathcal{I}(T) \setminus \mathcal{I}(\bar{T})$, then $c \in \mathcal{I}(\bar{T})$. It indicates that $\exists t \in \bar{T}, t \in \mathcal{T}(c)$, which contradicts that $\mathcal{T}(c) \subseteq T$. Therefore, $c \in \mathcal{S}(T)$. \square

Table VI shows an example of this proposition for $SUT(2^3)$. In this table, the test set $\mathcal{T}(c)$ of schema c is the subset of test set T. As a result, the special schema set $\mathcal{S}(T)$ of T contains this schema c = (0, 0, -).

Table VI. Example of a minimal schema of the subset of a test set

c	$\mathcal{T}(c)$	T	$\mathcal{S}(T)$
(0, 0, -)	(0, 0, 0)	(0, 0, 0)	(0, -, -)
	(0, 0, 1)	(0, 0, 1)	(0, -, 0)
		(0, 1, 0)	(0, -, 1)
		(0, 1, 1)	(0, 0, -)
			(0, 1, -)
			(0, 0, 0)
			(0, 0, 1)
			(0, 1, 0)
			(0, 1, 1)

Based on Proposition 3.9, as long as $\mathcal{T}(c)\subseteq T$ for any schema c and any test set T in the SUT, c either belongs to C(T) or is the super-schema of some schema in C(T). Considering a more general scenario, i.e., two test sets T_1 , T_2 with $T_2\subseteq T_1$, we then can easily obtain the relationships between $\mathcal{C}(T_1)$ and $\mathcal{C}(T_2)$ according to Proposition 3.9.

PROPOSITION 3.10 (MINIMAL SCHEMAS IN THE SMALLER TEST SET). For T_1 and T_2 of the SUT with $T_2 \subseteq T_1$, $\forall c_2 \in \mathcal{C}(T_2)$, $\exists c_1 \in \mathcal{C}(T_1)$, s.t., either $c_1 = c_2$ or $c_1 \prec c_2$.

PROOF. $\forall c_2 \in \mathcal{C}(T_2), \mathcal{T}(c_2) \subseteq T_2 \subseteq T_1$. According to Proposition 3.9, $c_2 \in \mathcal{S}(T_1)$. By definitions of $\mathcal{S}(T)$ and $\mathcal{C}(T)$, $\exists c_1 \in \mathcal{C}(T_1), s.t., c_1 = c_2, \ or \ c_1 \prec c_2$. \Box

PROPOSITION 3.11 (MINIMAL SCHEMAS IN THE LARGER TEST SET). For T_1 and T_2 of the SUT, $T_2 \subseteq T_1$. Then $\forall c_1 \in \mathcal{C}(T_1)$, $\exists c_2 \in \mathcal{C}(T_2), s.t.$, (1) $c_1 = c_2$, or (2) $c_1 \prec c_2$, or (3) $\not\exists c_2 \in \mathcal{C}(T_2), s.t.$, $c_2 \prec c_1$ or $c_2 = c_1$, or $c_1 \prec c_2$.

PROOF. Assume that $\exists c_1 \in \mathcal{C}(T_1)$, s.t., $\exists c_2 \in \mathcal{C}(T_2), c_2 \prec c_1$. According to Proposition 3.11, as $T_2 \subseteq T_1$, so $\forall c_2 \in \mathcal{C}(T_2), \exists c_1' \in \mathcal{C}(T_1), s.t.$, either $c_1' = c_2$ or $c_1' \prec c_2$. Combining them, we can get that $c_1' \prec c_1$. This is a obvious contradiction, as c_1 and c_1' are both minimal schemas in $\mathcal{C}(T_1)$.

Hence, apart from the impossible relationship $c_2 \prec c_1$, then $\forall c_1 \in \mathcal{C}(T_1)$, $\exists c_2 \in \mathcal{C}(T_2), s.t.$, (1) $c_1 = c_2$, or (2) $c_1 \prec c_2$, or (3) $\not\exists c_2 \in \mathcal{C}(T_2), s.t.$, $c_2 \prec c_1$ or $c_2 = c_1$, or $c_1 \prec c_2$. \Box

We need to note the third case, i.e., $\not\exists c_2 \in \mathcal{C}(T_2), s.t., c_1 \prec c_2 \ or \ c_1 = c_2, \ or \ c_2 \prec c_1$. We refer to this case as c_1 is irrelevant to $\mathcal{C}(T_2)$. Furthermore, we can also say a schema is irrelevant to another schema if these two schemas are neither identical nor subsuming each other.

We illustrate these scenarios with examples in Table VII for $SUT(2^3)$. There are two parts in this table, with each part showing two test sets: T_1 and T_2 , which have $T_2 \subseteq T_1$. In the left part, the schemas in $\mathcal{C}(T_2)$: (0, 0, -) and (0, -, 0), both are the super-schemas of the one in $\mathcal{C}(T_1)$:(0, -, -). While in the right part, the schemas in $\mathcal{C}(T_2)$: (0, 0, -) and (0, -, 0) are both also in $\mathcal{C}(T_1)$. Furthermore, one schema in $\mathcal{C}(T_1)$: (1, 1, -) is irrelevant to $\mathcal{C}(T_2)$.

In summary, these propositions provide the foundation of MFS identification (Propositions 3.7 and 3.8), and more meaningful, they clarify the relationships between the minimal schemas of two different test sets (Propositions 3.11 and 3.10), which is the key to explain the impact of masking effects later.

Table VII.	Minimal schemas of two subsuming tes	st
set		

		T_2	T_1
T_2	T_1	(0, 0, 0)	(0, 0, 0)
(0, 0, 0)	(0, 0, 0)	(0, 0, 1)	(0, 0, 1)
(0, 0, 1)	(0, 0, 1)	(0, 1, 0)	(0, 1, 0)
(0, 1, 0)	(0, 1, 0)		(1, 1, 0)
	(0, 1, 1)		(1, 1, 1)
$C(T_2)$	$C(T_1)$	$C(T_2)$	$C(T_1)$
(0, 0, -)	(0, -, -)	(0, 0, -)	(0, 0, -)
(0, -, 0)		(0, -, 0)	(0, -, 0)
			(1, 1, -)

3.3. Identify the MFS

In this section, we will study how traditional MFS identification approaches, i.e., FII approaches, identify the MFS. Let T_F indicates all the failing test cases and T_P all the passing test cases (Note that $T_F \cap T_P = \emptyset$ and $T_F \cup T_P = T^*$). Then the MFS for the SUT is $\mathcal{C}(T_F)$. Theoretically, to accurately figure out the MFS in the SUT, we need to exhaustively execute each possible test case, and collect the failing test cases T_F . This is impossible in practice, especially when the testing space is very large.

As it is impractical to get all the MFS, the appropriate is to determine some MFS of them. With the following proposition, we can learn that with knowing subset of the test cases, we can also determine some of them are MFS.

PROPOSITION 3.12 (EQUAL MINIMAL SCHEMAS). For T_1 and T_2 , $T_1 \subset T_2$. If $\exists c \in \mathcal{C}(T_1)$, such that $c \in \mathcal{C}(T_2)$. Then, for any test set T_3 , such that $T_1 \subset T_3 \subset T_2$, we have $c \in \mathcal{C}(T_3)$.

PROOF. According to Proposition 3.11, $\forall c \in \mathcal{C}(T_1)$, exists $c' \in \mathcal{C}(T_3)$, such that either $c' \prec c$ or c' = c. Let us assume that $c' \prec c$. As there exists $c'' \in \mathcal{C}(T_2)$, such that c = c'', then $c' \prec c''$. This is contradiction as $T_3 \subset T_2$, so $\forall c' \in \mathcal{C}(T_3)$, exists $c'' \in \mathcal{C}(T_2)$, such that either $c'' \prec c'$ or c'' = c'. Hence, we have the assumption $c' \prec c$ does not hold, indicating that c' = c. \square

For example, Table VIII shows the minimal schemas for T_1 , T_2 , T_3 and T_3' , where $T_1 \subset T_3 \subset T_2$ and $T_1 \subset T_3' \subset T_2$. We can find that $\mathcal{C}(T_1)$, i.e., (0, 0, -) is identical to that one in $\mathcal{C}(T_2)$, which also in $\mathcal{C}(T_3)$ and $\mathcal{C}(T_3')$.

Table VIII. Identical minimal schemas of subsuming test sets

T_1	$ T_2 $	T_3	T_3'
0 0 0	0 0 0	0 0 0	0 0 0
$0 \ 0 \ 1$	0 0 1	0 0 1	0 0 1
	1 1 1	1 1 1	1 1 0
	1 1 0		
$C(T_1)$	$C(T_2)$	$C(T_3)$	$\mathcal{C}(T_3)$ '
0 0 -	0 0 -	0 0 -	0 0 -
	1 1 -	1 1 1	1 1 0

Based on this proposition, let $T_{F-known}$ be the given test cases which are known to be failing, and $T_{P-known}$ be the known passing test cases. $T_{unknown} = T^* \setminus (T_{F-known} \bigcup T_{P-known})$ be the test cases that are not known to be failing or not. Based on Proposition 3.12, we have the following lemma:

LEMMA 3.13 (DETERMINE SOME MFS). $\forall c \in C(T_{F-known}), if \exists c' \in C(T_{F-known}), if \exists c' \in C(T_{F-known}), such that <math>c = c'$, then c must be MFS.

The proof of this lemma is obvious. With this lemma, we can determine some MFS in the SUT without executing all the test cases. However, to identify a MFS c, there still needs many test cases to execute; at least, we should execute all the test cases in $\mathcal{T}(c)$. For example, for SUT(2^8), to identify the MFS (1, 1, -, -, -, -, -), we should make sure all the test cases contain this schema must fail, of which the number is $|T_{F-known}| = 2^{8-2} = 64$. This number grows exponentially with number of parameters in the SUT. Hence, traditional FII approaches will take some assumptions to further reduce the number of needed test cases to identify the MFS.

Generally, with proper assumptions, apart from the test cases which have been executed, we can infer some of the remaining test cases to be passing or failing. Formally, let $T_{F-infer}$ refer to the test cases that can be inferred to be failing and $T_{P-infer}$ the inferred passing test cases. With the test cases of which the outcomes can be inferred, the test cases which are known to failing is increased to be $T_{F-known} \bigcup T_{F-infer}$, and the unknown test cases decreased to be $T_{unknown} \setminus (T_{F-infer} \bigcup T_{P-infer})$. Based on Lemma 3.13, $\forall c \in \mathcal{C}(T_{F-known} \bigcup T_{F-infer})$, if it is identical to some schema in $\mathcal{C}((T_{F-known} \bigcup T_{F-infer}) \bigcup (T_{unknown} \setminus (T_{F-infer} \bigcup T_{P-infer})))$, then c must be MFS. The assumptions and corresponding inferring process vary with different FII ap-

The assumptions and corresponding inferring process vary with different FII approaches. To specifically describe the inferring processes of different FII approaches is far beyond this paper. Next, we will only focus on describing the FIC BS appraoch[Zhang and Zhang 2011]—an efficient adaptive MFS identification approach.

The algorithm of FIC_BS is listed in the appendix, as well as the corresponding interpretation. We will give a simple example to illustrate how FIC_BS works. For SUT(2^4), assume the test case (1, 1, 1, 1) failed, then the FIC_BS approach can be illustrated in Table IX. In this table, to identify the MFS in t_0 , FIC_BS generated 4 more test cases, i.e., t_1, t_2, t_3 and t_4 . Each of these test cases consists of two parts: the same part in the original failing test case, we called the *fixed* part against t_0 ; and the part with values different from the original failing one, we called them the *mutated* part against t_0 . For example, for test case t_1 , the *fixed* part (against t_0) is (-, -, 1, 1) and the *mutated* part is (0, 0, -, -). Note that these mutated parts do not necessary be value (0, 0, -, -). We just need make them different from what are in t_0 (This is important to the latter proposed approach). The MFS obtained by FIC_BS is (-, 1, -, 1). This conclusion is based on the following assumption.

Test Case outcome 1 fail t_0 pass t_1 0 0 1 1 t_2 1 1 1 fail 0 0 1 0 pass

Table IX. FIC_BS running example

ASSUMPTION 4. The mutated part of each additional test cases consists of safe values, i.e., none of the parameter value in mutate part is the part of any MFS.

Based on this assumption, we have the following two lemmas:

LEMMA 3.14. $\forall t \in T_{unknown}$, if $\exists t' \in T_{P-known}$, such that the parameter values of the mutated part of t (against t') are all safe values, then t must be a passing test case.

PROOF. Assume that t is a failing test case. As $\{t\} \subset T_F$, $\exists c \in \mathcal{C}(T_F)$, such that $c \prec t$ or c = t (Based on Proposition 3.9). In other words, $\forall e \in c$, it has $e \in t$. As c has no parameter value that is safe value (Assumption 4), so $\forall e \in c$, it has $e \in (t \setminus mutate)$, where mutate indicates the mutated part of t against t'. However, as t' also contain

39:12 X. Niu et al.

 $(t \setminus mutate)$, so t' should be a failing test case, which is contradiction. Hence, t must be a passing test case. \Box

For example, if (0, 0, 0, 0) is known to be passing test case, and (-, -, -, 1) is safe value, then test case (0, 0, 0, 1) must be a passing test case.

LEMMA 3.15. $\forall t \in T_{unknown}$, if $\exists t' \in T_{F_known}$, such that the mutated part of t' (against t) consists of safe values, then t must be a failing test case.

This lemma can be proved according to Lemma 3.14. As a example, assume (0, 0, 0, 0) is known to be a failing test case, and (-, -, -, 0) is safe value, then test case (0, 0, 0, 1) must be a failing test case.

Based on these two lemmas, we can easily infer some unknown test cases to be failing or not. In table IX, FIC_BS assume assumption that (0, -, -, -), (-, 0, -, -), (-, -, 0, -) and (-, -, -, 0) are *safe values*. Then those inferred test cases are listed in Table X with column 'State' *infer*. For example, the mutated part of t_2 against the known passing test case t_4 is the (-, -, 0, -), which is safe value, so t_2 should be inferred to be passing; the mutated part of the known failing test case t_{16} against the unknown test case t_{14} is still the safe value (-, -, 0, -), so t_{14} should be inferred to be failing.

ID	Te	st Ca	ıse		Outcome	State
t_1	0	0	0	0	pass	infer
$\mathbf{t_2}$	0	0	0	1	pass	infer
$\mathbf{t_3}$	0	0	1	0	pass	infer
t_4	0	0	1	1	pass	known
t_5	0	1	0	0	pass	known
t_6	0	1	0	1	fail	known
t_7	0	1	1	0	-	unkonwn
t_8	0	1	1	1	fail	known
t_9	1	0	0	0	-	unkonwn
t_{10}	1	0	0	1	-	unkonwn
t_{11}	1	0	1	0	-	unkonwn
t_{12}	1	0	1	1	-	unkonwn
t_{13}	1	1	0	0	-	unkonwn
$\mathbf{t_{14}}$	1	1	0	1	fail	infer
t_{15}	1	1	1	0	-	unkonwn
t_{16}	1	1	1	1	fail	known

Table X. Test outcomes for MFS(- 1 - 1)

After these test cases having been inferred, we can find that $\mathcal{C}(T_{F-known} \bigcup T_{F-infer}) = \mathcal{C}(\{t_6, t_8, t_{14}, t_{16}\}) = (-, 1, -, 1), \text{ and } \mathcal{C}((T_{F-known} \bigcup T_{F-infer}) \bigcup (T_{unknown} \setminus (T_{F-infer} \bigcup T_{P-infer}))) = \mathcal{C}(\{t_6, t_8, t_{14}, t_{16}, t_7, t_9, t_{10}, t_{11}, t_{12}, t_{13}, t_{13}, t_{15}\}) = (1, -, -, -), (-, 1, -), (-, 1, -, 1).$ Hence, we can learn that (-, 1, -, 1) must be MFS.

This example illustrate that the FII approach cannot execute all the test cases, but with proper assumptions, the schemas identified by FII can be approximate to or even equal to the exactly correct MFS in the SUT. Other FII approaches can also be built into our formal model for MFS identification, but this will not be discussed here as it is not the point of this paper. Even though each FII approach tries to identify the MFS as accurately as possible, however, masking effects will negatively affect the observed outcomes and the inferred results. We next discuss the masking problem.

4. MASKING EFFECT

As discussed before, $C(T_{F_m})$ is the MFS set of fault F_m in theory. When considering the masking effects between multiple faults, however, this formula is not correct.

Definition 4.1. A masking effect occurs when a test case t contains an MFS of a particular fault, but it does not trigger the expected fault because other unexpected event, such another fault or unaccounted control dependency, was triggered ahead of it that prevents *t* from being normally checked.

Taking the masking effects into account, when identifying the MFS of a specific fault F_m , we should not ignore those test cases which did not trigger F_m but should have triggered it. We call these test cases $T_{mask(F_m)}$. Hence, the MFS of fault F_m should be

 $\mathcal{C}(T_{F_m} \bigcup T_{mask(F_m)})$. Going back to the motivating example in Section 2, as test case 6 and test case 18 should trigger Ex 2 in case they did not trigger Ex 1, $T_{mask(F_2)}$ is $\{(7,4,4,5),(11,4,4,5)\}$. Hence, the MFS of Ex2 is $C(T_{F_2} \bigcup T_{mask(F_2)})$, which is (-,-,4,5) instead of the incorrect schema set $\{(-,2,4,5),(-,5,4,5)\}$.

In practice with masking effects, however, it is not possible to correctly identifying the MFS, unless we fix some bugs in the SUT and re-execute the test cases to figure out $T_{mask(F_m)}$.

For traditional FII approaches, without the knowledge of $T_{mask(F_m)}$, two common strategies can be adopted to deal with the multiple faults problem, i.e., regarded as same failure and distinguishing failures. The former strategy treats all types of faults as one fault, and hence all the failures are considered the same, while the latter distinguishes the failures but with no special consideration of the masking effects, i.e., if a test case fails with a particular type of fault, this strategy presumes it does not contain other types of faults.

4.1. Regarded as same failure strategy

This is the most common strategy. With this strategy, the minimal schemas are the set $\mathcal{C}(\bigcup_{i=1}^L T_{F_i})$, where L is the number of all the faults in the SUT. Obviously, $T_{F_m} \bigcup T_{mask(F_m)} \subseteq \bigcup_{i=1}^L T_{F_i}$. By Proposition 3.11, some schemas obtained by this strategy may be the sub-schemas of some of the actual MFS, or be irrelevant to the actual MFS.

As an example, consider the test cases in Table XI. Assume we need to characterize the MFS of fault 1. All the test cases that triggered fault 1 are listed in column T_{F_1} ; similarly, we list the test cases that triggered failures of other faults in column $T_{mask(F_1)}$ and T_{non_mask} , respectively, in which the former masked fault 1, while the latter did not. Actually the MFS of fault 1 should be (1,1,-,-) and (-,1,1,1) as we listed them in the column 'actual MFS of fault 1'. However, when we use the regarded as same failure strategy, the minimal schemas obtained will be (-,-,0,0), (1,1,-,-), (-,-,1,1), in which (-,-,0,0) is irrelevant to the actual MFS of fault 1, and (-,-,1,1) is a sub-schema of the actual MFS (-,1,1,1).

 $\frac{T_{mask(F_1)}}{(1, 1, 0, 0)}$ $\frac{T_{non_mask}}{(0, 1, 0, 0)}$ (1, 1, 1, 1)(1, 1, 1, 0)(0, 1, 1, 1)(0, 0, 0, 0)(1, 1, 0, 1)(1, 0, 0, 0)(1, 0, 1, 1)(0, 0, 1, 1)actual MFS of Fault 1 regarded as same failure distinguishing failures $C(T_{F_1} \bigcup T_{mask(F_1)})$ $\frac{\mathcal{C}(T_{F_1} \bigcup T_{mask(F_1)} \bigcup T_{non_mask})}{(\text{-},\text{-},\text{0},\text{0})}$ $C(T_{F_1})$ (1, 1, -, -)(1, 1, -, 1)(-, 1, 1, 1)(1, 1, -, -)(1, 1, 1, -)(-, -, 1, 1)

Table XI. masking effects for exhaustive testing

39:14 X. Niu et al.

4.2. Distinguishing failures strategy

Distinguishing the failures by the exception traces or error code can help identify the MFS related to a particular failure. Yilmaz [Yilmaz et al. 2014] proposed the *multiple-class* failure characterizing method instead of the *ternary-class* approach to make the characterizing process more accurate. Besides, other approaches can also be easily extended using this strategy for testing the SUT with multiple faults.

This strategy focuses on identifying the set of $C(T_{F_m})$. As $T_{F_m} \bigcup T_{mask(F_m)} \supseteq T_{F_m}$, by Proposition 3.11, some schemas obtained by this strategy may be the super-schema of some actual MFS. Moreover, some MFS may be irrelevant to the schemas obtained by this strategy, which means that this strategy will *ignore* these actual MFS.

For the simple example shown in Table XI, when using this strategy, we will get the minimal schemas (1, 1, -, 1) and (1, 1, 1, -), which are both super schemas of the actual MFS (1,1,-,-). Furthermore, no schemas obtained by this strategy have any relationship with the actual MFS (-,1,1,1), which means it was ignored.

It is noted that the motivating example in section 2 actually adopted this strategy. As a result, the schemas identified for Ex 2: (-,2,4,5), (-,3,4,5) are the super-schemas of the correct MFS(-,-,4,5).

4.3. Masking effects for FII approaches

Based on previous analysis, even though exhaustive testing is conducted to obtain T_{F_m} , we cannot determine the MFS set because of the masking effects. For traditional MFS identification approaches, i.e., FII approaches, masking effects can make problems worse. This is because FII approaches, with masking effects, not only unable determine $T_{mask(F_m)}$ as discussed before, but also make wrong inferring outcomes of some test cases without executing, i.e., wrong $T_{F-infer}$ and $T_{P-infer}$ as mentioned in Section 3.3.

Consider a FII example that still use the FIC_BS method [Zhang and Zhang 2011]. Similar to the example listed in Table IX, assume the test case (1, 1, 1, 1) failed with F_1 (The MFS is still assumed to be (-, 1, -, 1) as Table IX). Then assume that an known MFS (-, 1, 0, -) that trigger F_2 , where fault F_2 can mask F_1 . Next we will illustrate how FIC_BS works using strategies the *regarded as one strategy* and *distinguishing failures strategy*, respectively.

First, for the first strategy, i.e., regarded as one strategy, we list how it works in Fig. 2, as well as the masking effects it suffers. With this strategy, it just needs three additional test cases to determine the MFS in the original failing test case t, i.e., t_1 , t_2 , and t_3 (listed in the left part of Fig. 2). The right part of Fig. 2 shows the MFS it obtained is (-, 1, -, -), which is obviously wrong (See the correct result in Table X, which should be (-, 1, -, 1), but this strategy treat the sub-schema (-, 1, -, -) of it to be MFS). The middle part of Fig. 2 explains why this strategy can get this result. Specifically, it treats all failures as the same failure, i.e., failure of F_1 . Hence, test case t_5 in the middle of Fig. 2 (Marked Strategy in the column 'State') is determined to trigger F_1 . Here, the test case t_5 corresponds to the test case t_3 in the left part of Fig.2 (The ID we refer to one test case next are all in the middle part). According to the Assumption 3.14 and 3.15, test cases t_1 , t_2 , t_3 , t_6 , t_7 , t_{13} , t_{14} , and t_{15} are determined to be pass or fail with F_1 , respectively. After then, we can determine that (-, 1, -, -) should be the MFS. This is because, $\mathcal{C}(T_{F_1}) = \mathcal{C}(\{t_5, t_6, t_7, t_8, t_{13}, t_{14}, t_{15}, t_{16}\}) = (-, 1, -, -)$, which has been included in $\mathcal{C}(T_{F_1} \cup T_{unknown}) = \mathcal{C}(\{t_5, t_6, t_7, t_8, t_9, t_{10}, t_{11}, t_{12}, t_{13}, t_{14}, t_{15}, t_{16}\}) = (1, -, -, -)$, (-, 1, -, -)

For the second strategy, i.e., distinguishing failures, we list the result in Fig. 3. Different from the first strategy, it treat the different failure other than failure of F_1 as pass. As a result, test case t_5 and t_6 in the middle part of Fig. 3 are determined to be

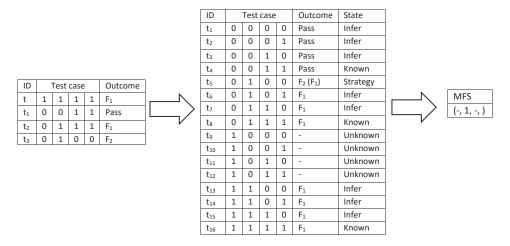


Fig. 2. Masking effects of strategy Regarded as same failure

pass. Then combining the inferred test cases, it finally get the MFS (-, 1, 1, 1), which is also not correct (This schema is the super-schema of the original MFS (-, 1, -, 1)).

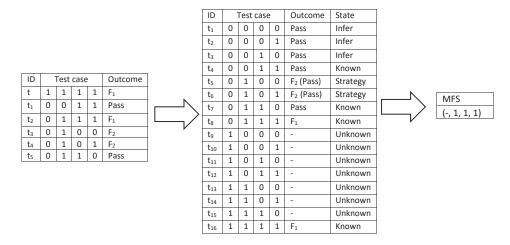


Fig. 3. Masking effects of strategy Distinguishing failures

Such deviations for these two strategies are caused by the reduction of the test cases which are known to be failing with specific fault. Here, test cases (0, 1, 0, 0) and (0, 1, 0, 1) both triggered other faults, among which the second test case (0, 1, 0, 1) should trigger F_1 if fault F_2 was not triggered first, while the first test case not. Hence, neither strategy Regarded as same failure nor Distinguishing failures can make a perfect determination of the result of these two test cases. Besides this, the incorrect determination of these test cases negatively affect the the inference of FII approach—FIC_BS. For example, with strategy Regarded as same failure, it wrongly infer the test case t_{15} (1, 1, 1, 0) to be fail with F_1 (See the middle part of Fig. 2), which should be marked as 'Unknown' in Table X. With strategy Distinguishing failures, however, it marked

39:16 X. Niu et al.

test case t_{14} (1, 1, 0, 1) as 'Unknown' (See the middle part of Fig. 3), which should be inferred to be fail with F_1 in Table X.

As masking effect has significant impact on the FII approaches, alleviating this negative effect is desired to improve the quality of the identified MFS.

5. TEST CASE REPLACING STRATEGY

The main reason that the FII approach fails to work properly is that it cannot determine $T_{mask(F_m)}$. In other words, if the test case triggers other unexpected failures which are different from the currently analysed F_m , it cannot figure out whether this test case will trigger F_m because of the masking effects. So to limit the impact of this effect on the FII approach, it is important to reduce the number of test cases that trigger other different failures, as it can reduce the probability that the expected failure may be masked by other different failures.

For the exhaustive testing model, i.e., $\mathcal{C}(T_{F_m})$, as all the test cases will be used to identify the MFS, there is no room left to improve the performance unless we fix other different failures and re-execute all the test cases. However, if only a subset of all test cases is used to identify the MFS (which is how the traditional FII approach works), it is important to make the right selection to limit the size of $T_{mask(F_m)}$ to be as small as possible.

5.1. Replacing test cases that trigger unexpected failures

The basic idea is to pick the test cases that trigger other faults and generate new test cases to replace them. The regenerated test cases should either pass in the execution or trigger F_m .

Normally, when we replace the test case that triggers an unexpected failure with a new test case, we should keep some part of the original test case. We call this part the *fixed part*, and mutate the other part with different values from the original one. For example, if a test case (1,1,1,1) triggered an unexpected failure, and the fixed part is (-,-,1,1). Then, we can replace it with a test case (0,0,1,1) which may either pass or trigger the same failure as currently analysed.

The fixed part can vary for different FII approaches. For example, for the OFOT [Nie and Leung 2011a] algorithm, the parameter values are the fixed part except for the one that needs to be validated, while for the FIC_BS [Zhang and Zhang 2011] approach, the fixed parts are dynamically changed, depending on the outcome of the execution of last generated test case.

This replacement process may need to be executed multiple times for one fixed part as it may not always be possible to find a test case that coincidentally satisfied our requirement. One replacement method is randomly choosing test cases until the satisfied test case is found. While this method may be simple and straightforward, however, it also may require tries. So to handle this problem and reduce the cost, we propose a replacement approach by computing the *suspiciousness* of the test case with the other faults, and then selecting the test case from a group of candidate test cases that has the least *suspiciousness* with other faults.

To explain the *suspiciousness* notion, we first introduce the *suspiciousness* between a parameter value o and a particular fault. We use all(o) to represent the number of executed test cases that contain this parameter value, and $f_i(o)$ to indicate the number of test cases that trigger the failure of $F_i, 1 \le i \le L$ and contain this parameter value. Then, the *suspiciousness* between a parameter value and a particular fault, i.e., $Sp(o, F_i)$, is $\frac{f_i(o)}{all(o)+1}$. This heuristic formula is based on the idea that if a parameter value frequently appears in the test cases that trigger a particular failure, then it is more likely to be the inducing factor that triggers this fault. We add 1 in the denominator for

two reasons: (1) avoid division by zero when the parameter value has never appeared before, (2) reduce the bias when a parameter value rarely appears in the test set but coincidentally appears in a failing test case with a particular fault.

Table XII gives an example to compute the suspiciousness between parameter values and particular faults. The left part of this table gives 4 executed test cases with their outcomes, in which faults F_1 and F_2 are triggered. The right part shows the suspiciousness between each parameter value and these two faults. Specifically, consider the parameter P_1 taking value 0. There are three test cases t_1 , t_2 , and t_4 that contain this parameter value, and only t_2 triggered F_1 . Hence, $Sp(P_1=0,F_1)=\frac{f_1(o)}{all(o)+1}=\frac{1}{3+1}=\frac{1}{4}$

Table XII. Suspiciousness example

ID	Test cases executed	Outcomes
$\overline{t_1}$	(0, 0, 0)	Pass
t_2	(0, 1, 1)	F_1
t_3	(1, 1, 0)	F_2
t_4	(0, 1, 1)	F_2

Suspiciousness for $F1$				
	P_1	P_2	P_3	
0	1/4	0	0	
1	0	1/4	1/3	
Suspiciousness for $F2$				
	P_1	P_2	P_3	
0	1/4	0	1/3	
_1	1/2	1/2	1/3	

With the *suspiciousness* associated with a parameter value, we then define the *suspiciousness* between a test case t and a particular fault F_i as:

$$Sp(t, F_i) = \frac{1}{k} \sum_{o \in t} Sp(o, F_i)$$
 (EQ1)

where k is the number of parameters in t, and o is the specific parameter value in t. The *suspiciousness* between a test case and a fault is actually the average *suspiciousness* between each parameter value in the test case and this fault. For example, considering an unexecuted test case (1, 0, 0). With the suspiciousness of all the parameter values listed Table XII, $Sp((1,0,0), F_1) = 1/3 \times (0+0+0) = 0$ and $Sp((1,0,0), F_2) = 1/3 \times (1/2+0+1/3) = 5/18$.

For a selected test case, we want its ability to trigger failures of other faults to be as small as possible, such that the masking effects can be alleviated. In practice, the *suspiciousness* varies between test cases and different faults. As a result, we cannot always find a test case that, for any fault, the *suspiciousness* between this test case and that fault is the least.

Table XIII illustrates such a scenario for SUT(2^4). Suppose the FII approach is analysing MFS for fault F_1 , and needs to replace test case (0,0,0,0) with fixed part (0, -, -, -) that triggers failures of other faults, i.e., F_2 or F_3 . This table lists five candidate test cases, with their suspiciousness with F_2 and F_3 given in the corresponding columns. It is obvious that t_1 has the least suspiciousness with fault F_3 and F_4 and the least suspiciousness with F_4 . These two test cases, however, should not be selected for their suspiciousness with another fault is too high. Instead, F_4 is a good choice as both its suspiciousness with F_4 and F_4 is not high (The higher one is just 0.4).

With this in mind, we have to settle for a test case, such that the most likely fault (except for the one that is currently analysed) it can trigger should be the least likely to be triggered when compared with that of other test cases. In other words, we need to find a test case, so that the maximal suspiciousness between this test case and the most likely fault it can trigger is minimal. Formally, we should choose a test case t, s.t.,

39:18 X. Niu et al.

Table XIII. Select minimal ma	aximal suspiciousness
-------------------------------	-----------------------

ID	Candidate test cases	$Sp(t, F_2)$	$Sp(t,F_3)$	$Max Sp(t, F_m), m = 2, 3$
t_1	(0, 0, 0, 1)	0.7	0.2	$Sp(t_1, F_2) : 0.7$
t_2	(0, 0, 1, 0)	0.2	0.6	$Sp(t_2, F_3) : 0.6$
$\mathbf{t_3}$	(0, 0, 1, 1)	0.4	0.3	$Sp(t_3, F_2) : 0.4$
t_4	(0, 1, 0, 0)	0.3	0.5	$Sp(t_4, F_3) : 0.5$
t_5	(0, 1, 0, 1)	0.5	0.3	$Sp(t_5, F_2) : 0.5$

$$\min_{t \in R} \max_{1 \le i \le L \& i \ne m} Sp(t, F_i)$$
 (EQ2)

where L is the number of faults, and m is the current analysed fault. R is the set of all possible test cases that contain the fixed part except those that have been tested. As fixed part is a set of parameter values which can be deemed as a schema, then obviously $R = \mathcal{T}(fixed) \setminus T_{executed}$, where $\mathcal{T}(fixed)$ is all the test cases that contain this fixed part and $T_{executed}$ represents those executed test cases. Additional test cases need to be selected in set R, so that FII approaches can work properly.

The complete process of replacing a test case with a new one while keeping some fixed part is depicted in Algorithm 1.

ALGORITHM 1: Replacing test cases triggering unexpected failures

```
Input: fault F_m, all the candidate test cases R, the suspiciousness matrix Sp
   Output: t_{new} the regenerate test case
   while not MeetEndCriteria() do
       t_{new} \leftarrow \min_{t \in R} \max_{1 \leq i \leq L \& i \neq m} Sp(t, F_i);
       result \leftarrow execute(t_{new});
3
       update\_SP(t_{new});
       if result = PASS or result = F_m then
           return t_{new};
 6
       else
 7
 8
        continue;
       end
10 end
11 return null
```

The inputs to this algorithm consist of the fault F_m under analysis, the candidate test cases $R = \mathcal{T}(fixed) \backslash T_{executed}$ and the suspiciousness matrix Sp, which records the suspiciousness between each factor o and each fault F_i , i.e., $Sp(o,F_i)$ ($1 \le i \le L$). The output of this algorithm is a test case t_{new} which either triggers the expected F_m or passes.

The outer loop of this algorithm (lines 1 - 10) contains three parts:

The first part (lines 2 - 3) generates and executes a new test case which is supposed to be least likely to trigger faults different from F_m . The new test case is generated according to EQ2. In our implementation, we use the solver introduced in [Berkelaar et al. 2004], which is a mixed Integer Linear Programming (MILP) solver suitable for satisfaction and optimization problems. (Note that a simpler linear search algorithm can also be applied in our approach to find a proper test case. However, as this problem to search a proper test case is related to Integers (a test case consists of discrete parameters with discrete values), so we use Integer Linear Programming (ILP) technique instead.)

The second part (line 4) updates the suspiciousness matrix (Sp) for each parameter value that is involved in this newly generated test case (line 4). Specifically, for a particular parameter value o, the number of executed test cases that contain o, i.e., all(o), increases by 1. Additionally, if this test case triggers failure of F_i ($1 \le i \le L$), then the number of test cases that contain o and trigger failure of F_i , i.e., $f_i(o)$, increases by 1. At last, the suspiciousness value will be re-computed according to formula $Sp(o,F_i) = \frac{f_i(o)}{all(o)+1}$ ($1 \le i \le L$).

The last part (lines 5 - 9) checks whether the newly generated test case is as expected. Specifically, if the test case passes or triggers the same failure of fault $-F_m$, a satisfied test case is obtained (line 5) and returned (line 6). Otherwise, we will repeat the process, i.e., generate a new test case and check again (lines 7 - 8).

Note that this algorithm has another exit, besides finding an expected test case (line 6), which is when the function MeetEndCriteria() returns true (line 1). We did not explicitly show function MeetEndCriteria(), because this is dependent on the computing resource and the desired accuracy. In detail, if we want to get a high quality result and have enough computing resource, it is desirable to try many times to get the expected test case; otherwise, a relatively small number of attempts to find a proper test case is recommended.

6. ILLUSTRATION OF THE APPROACH

This section will completely illustrate the MFS identification approach that combines the traditional MFS identification procedure with test cases replacement strategy.

6.1. MFS identification with replacement strategy

Algorithm 2 shows the procedure of the approach. The inputs to this algorithm are the fault F_m that is currently focused on and an original failing test case t. The output of this algorithm is to give the MFS for fault F_m in the test case t. Variable SP is to record the suspicious value between each parameter value with each fault. $T_{Unknown}$ is the set of test cases that is not yet determined to be fail with fault F_m or not, and $T_{F-Known}$ is the set of test cases that are deemed to trigger the fault F_m . This algorithm loops until some MFS are determined (line 25 27). This is based on Lemma 3.13 in Section 3.3. Specifically, by computing the minimal schemas of $T_{F-Known}$, i.e., $\mathcal{C}(T_{F-Known})$, and minimal schemas of $T_{F-Known} \cup T_{Unknown}$, respectively, we can determine $\mathcal{C}(T_{F-Known})$ are MFS if they are contained in $\mathcal{C}(T_{F-Known} \cup T_{Unknown})$.

In each iteration of this algorithm, it will generate one additional test case (line 7) to execute. This test case is randomly selected from a candidate set R which has the same fixed part (line 6). The fixed part is different in each iteration (See Algorithm 3 in the Appendix for detail). Then the approach will execute this test case (line 8) and update the suspicious matrix (line 9) according to the execution result. If the result is pass or fail with the same fault F_m , then the generated test case is a proper test case for MFS identification; otherwise, we should run the replacement strategy (line 10 - 15) based on Algorithm 1. Note that if we cannot find a proper test case by Algorithm 1, we need to randomly select one test case in R (line 13), and regard it as fail with F_m (line 14). Next we will infer the result of some unknown test cases according to the result of the generated test case t_{next} (line 17 - 24). This inferring procedure is exactly based on Lemma 3.15 and 3.14. After that, we should updated the $T_{F-known}$ and $T_{Unknown}$ (line 19 - 20, line 23), and re-check if the ending condition is satisfied (line 27).

39:20 X. Niu et al.

ALGORITHM 2: MFS identification with Replacing test cases strategy

```
Input: fault F_m, original failing test case t
    Output: MFS return the determined MFS
   Sp \leftarrow init\_Suspicious\_Matrix(t);
2 T_{Unknown} \leftarrow T_{ALL} \setminus t;
3 T_{F-Known} \leftarrow \{t\};
4 MFS \leftarrow empty;
5 while true do
         R \leftarrow \mathcal{T}(current\_fixed\_part);
 6
        t_{next} \leftarrow random\_pick(R);
7
        result \leftarrow execute(t_{next});
8
         update\_SP(t_{next});
        if result \neq PASS and result \neq F_m then
10
              t_{next} \leftarrow Replacing(F_m, Sp, R);
11
              if t_{next} == null then
12
                   t_{next} \leftarrow random\_pick(R);
13
                   result \leftarrow F_m
14
             end
15
        end
16
        if result == F_m then
17
              T_{infer-F} \leftarrow InferringFailing(t_{next}, SV);
18
              T_{F-Known} \leftarrow T_{F-Known} \bigcup t_{next} \bigcup T_{infer-F};
19
              T_{Unknown} \leftarrow T_{Unknown} \setminus (t_{next} \bigcup T_{infer-F});
20
21
              T_{infer-P} \leftarrow InferringPassing(t_{next}, SV);
22
23
              T_{Unknown} \leftarrow T_{Unknown} \setminus (t_{next} \bigcup T_{infer-P});
24
         MFS \leftarrow \mathcal{C}(T_{F-Known});
25
         M_{Possible} \leftarrow \mathcal{C}(T_{F-Known} \bigcup T_{Unknown});
26
        if MFS \subseteq M_{Possible} then
27
             break;
28
        end
29
30 end
31 return M_{Candidate}
```

6.2. A case study using the replacement strategy

In this section, we will give a case study to illustrate the approach. Suppose we have to test a system with eight parameters, each of which has three options, i.e., SUT(3^8). When we execute the test case t_0 – (0, 0, 0, 0, 0, 0, 0, 0, 0, a failure of fault–e1 is triggered. Furthermore, there are two more potential faults, e2 and e3, that may be triggered during the testing and they will mask the desired fault e1. Next, we will use FIC_BS [Zhang and Zhang 2011] with replacement strategy to identify the MFS of e1. The process is shown in Figure 4. In this figure, there are two main columns. The left main column indicates the executed test cases during testing as well as the executed results, with each executed test case corresponding to a specific label, t_1 – t_8 , at the left. The underline part for each test case is the fixed part according to FIC_BS [Zhang and Zhang 2011]. The right main column lists the suspiciousness matrix when a test case triggers e2 or e3. The executed test case, shown in bold, indicates the one that triggers the failure of other faults and should be replaced in the next iteration.

The completed MFS identifying process listed in Figure 4 works as follows: firstly the original FII approach determines which fixed part needed to be tested in each iteration. Then an extra test case will be generated to fill in the remaining part. After executing the extra test case, if the result of the execution is normal, i.e., did not

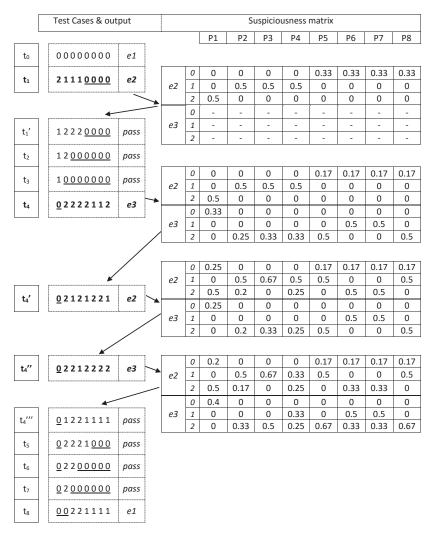


Fig. 4. A case study using our approach

trigger any unexpected faults (e_2,e_3) , then the original FII process will continue until the MFS is identified. Otherwise, the replacement strategy starts when an unexpected failure of other faults is triggered. The replacement process will mutate the parameter values that are not in the fixed part according to EQ2. After the replacement process, the control for the MFS identifying process will be passed back to the original FII approach. Next we will specifically explain how the replacement works with an example in Figure 4.

From Figure 4, for the test case that triggered $e^2 - (2, 1, 1, 1, 0, 0, 0, 0)$ (in this case, the fixed part of the test case is (-, -, -, -, 0, 0, 0, 0), in which the last four parameter values are the same as the original test case t_0), we generate the related matrix at left. Each element in this matrix is computed according to EQ1. All the suspiciousness with e^3 is labeled with a short slash as there is no test case triggering this fault in this iteration. After this matrix has been determined, we can obtain the optimal test case

39:22 X. Niu et al.

with the ILP solver, which is t'_1 –(1, 2, 2, 2, 0, 0, 0, 0), with its suspiciousness 0.167, which is smaller than all other test cases.

This replacement process is started each time a new test case that triggered another fault until we finally get one proper test case. Sometimes we could not find a satisfied replacing test case in just one trial like t_1 to t_1' . When this happened, we needed to repeat searching the proper test case. For example, for t_4 which triggered e3, we tried three times— t_4' , t_4'' , t_4'' to finally get a satisfied t_4'' which passes the testing. Note that the suspiciousness matrix continues to change as the test case is generated and executed so that we can adaptively find an optimal one.

With the replacement test cases, the FII approach can properly work. At last, the MFS identified for fault e1 is (0,0, -, -, -, -, -, -) (Test cases passed when we mutated the first two parameter values of the original failing cases). Note that, we did not show the theoretic process to obtain the MFS (0,0,-,-,-,-,-). This is because we need to list all the possible test cases $(3^8=6561$ test cases in total) to illustrate this process, which is not applicable in this paper.

Another notable point is that, in this example, test cases that trigger e2 and e3 do not contribute to the MFS identification. In real-world scenario, however, it is appealing to iteratively start MFS identification for e2 and e3 based on these test cases.

7. DISCUSSION ABOUT THE INFLUENCE OF THE ASSUMPTIONS

(1, 1, 1)

In section 3.1, we introduced three assumptions that can simplify our formal modeling and proposed approach, and in section 3.3, we introduced the safe value assumption which can reduce the number of test cases to identify MFS. In this section, we will discuss the influence of them on our propositions and approach, as well as some measures to alleviate their impacts.

7.1. Deal with non-deterministic problem

The first assumption is that the outcomes of all the tests are deterministic. In practice, re-executing the same test case may result in different outcomes. For example, if the program using some random variables, different runs of the test case will assign different values to these random variables. As a result, the control follow of the program may be changed and hence the outcome will be different. We called this type of failure the non-deterministic failure [Yilmaz et al. 2006; Fouché et al. 2009]. Non-deterministic failure will complicate the MFS identification, and even worse, it may lead to an unreliable result of the MFS identification. Consider the the following example in Table XIV, the only difference between the left with the right test set is the outcome of test case (0, 1, 1). This subtle difference result in the different results of the MFS identification. Hence, if there is one or more test cases which have non-deterministic executing results, the MFS identification is not reliable.

 $\frac{T_{fail}}{(0,0,0)}$ $\frac{T_{fail}}{(0,0,0)}$ MFS $T_{\underline{pass}}$ MFS(0, -, -)(0, 0, -)(0, 0, 1)(0, -, 0)(0, 0, 1)(0, 1, 0)(0, 1, 0)(0, 1, 1)(0, 1, 1)(1, 0, 0)(1, 0, 0)(1, 0, 1)(1, 0, 1)(1, 1, 0)(1, 1, 0)

Table XIV. MFS of two similar test sets

Inspiring the idea that using multiple same-way covering arrays to identify the MFS [Fouché et al. 2009], one potential solution to alleviate this non-deterministic failure is

(1, 1, 1)

by adding redundancy, i.e., through re-executing one test case to obtain the relatively stable outcome. However, this measure will increase the overall cost of the MFS identification, so the tradeoff between cost and the quality of MFS identification should be further studied.

7.2. Deal with failures distinguishing problem

The second assumption is that that different errors in the software can be easily distinguished by information such as exception traces, state conditions, or the like. If we cannot directly distinguish them, our approach does not work. This is because we cannot determine which test case should be replaced and should be replaced with what. In such case, one potential solution is to use the clustering techniques to classify the failures according to available information [Zheng et al. 2006; Jones et al. 2007; Podgurski et al. 2003]. If we cannot classify them because we do not have enough information (e.g., the black box testing) or it is too costly, we believe the only approach is to take the regarded as same failure strategy. With this strategy, we must aware that the MFS identified are likely to be sub-schemas or irrelevant schemas of the actual MFS.

7.3. Deal with inter-option constraints

The third assumption is that all the test cases are valid, i.e., SUT does not has any inter-option constraint. This is a very strong assumption. In this section, we will try to remove this assumption. In fact, with constraints has been known in prior, many studies in CT has proposed approaches to avoid them when generating test cases [Cohen et al. 2007a; 2007b; 2008; Calvagna and Gargantini 2008; Yu et al. 2013; Petke et al. 2013; Yu et al. 2015]. Generally, with constraints known in prior, not all all test cases in the SUT are valid. We set those valid test cases, i.e., do not contain any of the constraints as T_{valid} . Hence, the test cases we generated for MFS identification or replacement are limited to those in T_{valid} . Note that this can also make MFS identification unavailable. For example, in Table XV, assume test case(0, 1, 1) is invalid. Then without any more information, we can determine the MFS (See two different results in Table XIV).

Table XV. MFS identification with constraints

T_{fail}	T_{pass}	$T_{invalid}$
(0, 0, 0)		
(0, 0, 1)		
(0, 1, 0)		
		(0, 1, 1)
	(1, 0, 0)	
	(1, 0, 1)	
	(1, 1, 0)	
	(1, 1, 1)	

Another type of constraint is those that do not be found at first, but triggered later in testing[Yilmaz et al. 2014]. The same as the approach proposed in [Yilmaz et al. 2014], we can just treat them as one type of failure, and then use MFS identification approach to identify them when encounter those invalid test cases.

7.4. Deal with safe values

The last assumption is the safe value, i.e., each parameter has one value that is not the part of any MFS. With this assumption, based on Lemma 3.15 and 3.14, we can infer the result of many test cases without executing them. On the contrary, if this

39:24 X. Niu et al.

assumption does not hold, those test cases may be inferred to the wrong results. As a result, the MFS that identified by FII approaches are not accurate.

In theory, to solve this problem, we should exhaustively execute all the test cases of which the results could be inferred. This is a costly process, and hence, some approaches have been proposed to handle such problem. Martinez [Martínez et al. 2008; 2009] proposed two approaches without the safe value assumption, but both of them either needs to know the number of the MFS or the degrees of them in prior. Then either through generating higher-way covering array or adaptively generating additional test case, they can determine the MFS. We [Niu et al. 2013] have also proposed one approach to alleviate this problem. In that work, we repeatedly check the same schema to reduce the impacts of non-safe values problem.

8. EMPIRICAL STUDIES

To investigate the impact of masking effects on FII approaches in real software testing scenarios and to evaluate the performance of our approach in handling this effect, we conducted several empirical studies. Each of the studies focuses on addressing one particular issue, as follows:

- **Q1**: Do masking effects exist in real software that contains multiple faults?
- **Q2**: How well does our approach perform compared to traditional approaches?
- **Q3**: Is the ILP-based test case searching technique efficient compared to the random selection?
- **Q4**: Compared to another masking effects handling approach FDA-CIT [Yilmaz et al. 2014], does our approach have any advantages?

8.1. The existence and characteristics of masking effects

In the first study, we surveyed three kinds of open-source software systems to gain an insight into the existence of multiple faults and their effects. The software under study were HSQLDB, JFlex and Grep. The first is a database management software written in pure Java, the second is a lexical analyser generator, and the last one is a command-line utility for searching plain-text data sets for lines matching a regular expression. The reason that we chose these these systems is because they contain different versions and are all highly configurable so that the options and their interactions can affect their behaviour. Additionally, they all have a developer community so that we can easily obtain the real bugs reported in the bug tracker forum. Table XVI lists the program, the versions surveyed, number of lines of uncommented code, number of classes in the project, and the bug's id ⁴ for each of the software.

software	versions	LOC	classes	bugs' id
HSQLDB	2.0rc8	139425	495	#981 & #1005
	2.2.5	156066	508	#1173 & #1179
	2.2.9	162784	525	#1286 & #1280
JFlex	1.4.1	10040	58	#87 & #80
	1.4.2	10745	61	#98 & #93
Grep	2.6.3	27046	156	#7600 & #29537
	2.22	48101	297	#33080 & #28588

Table XVI. Software under survey

⁴http://sourceforge.net/p/hsqldb/bugs http://sourceforge.net/p/jflex/bugs http://savannah.gnu.org/bugs/

values

2

2

3

 $\overline{2}$

2

2

2

3

4

2

-count

 $2^5 \times 3^1 \times 4^1$

 $2^4\times 3^2\times 4^1$

versions Config space

8.1.1. Study setup. We first looked through the bug tracker forum and focused on the bugs which are caused by the options interactions. For each of them, we derived its MFS by analysing the bug description report and the associated test file which can reproduce the bug. For example, through analysing the source code of the test file of bug#981 for HSQLDB, we found the failure-inducing interaction for this bug is (preparestatement, placeHolder, Long string). These three parameter values together form the condition that triggers the bug. The analysed result was later regarded as the "prior MFS".

We further built the testing scenario for each version of the software listed in Table XVI. The testing scenario is constructed so that we can reproduce different failures by controlling the inputs to the test file. For each version, the source code of the testing file as well as other detailed information is available at http://gist.nju.edu.cn/doc/multi/.

Next, we built the input model which consists of the options related to the failureinducing interactions and additional options that are commonly used. The detailed models information is shown in Table XVII for HSQLDB, JFLex and Grep, respectively. Each table is organised into three groups: (1) common options, which lists the options as well as their values under which every version of this software can be tested; (2) specific options, under which only the specific version can be tested; and (3) configure space, which depicts the input model for each version of the software, presented in the abbreviated form $\#values^{\#number\ of\ parameters} \times ...$, e.g., $2^9 \times 3^2 \times 4^1$ indicates the software has 9 parameters that can take 2 values, 2 parameters 3 values, and only one parameter 4 values.

JFlexcommon options values values common options Server Type 3 generation 3 2 existed form Grep4 charset resultSetTypes 3 common options public 2 2 resultSetConcurrencys -E 2 apiprivate 2 resultSetHoldabilitys 2 cup StatementType 2 -V or -color caseless 2 2 versions specific options values sql.enforce_strict_size 2 char sql.enforce_names 2 2.6.3ascii 2 line $sql.enforce_refs$ command 2 column versions specific options values word 2 notunix 2.0rc82 more charset yyeof placeHolder 2 2.22 -A or -B or -C versions specific options values cursorAction 4 value hasReturn 2.2.5 3 multiple only-matching

HSQLDB

placeHolder

duplicate

defailure_commit

 $2^9 \times 3^2 \times 4^1$

 $2^8\times 3^3$

 $2^8 \times 3^3$

versions Config space

229

2.0rc8

2.2.5

2.2.9

2

3

1.4.2

1.4.1

1.4.2

Table XVII. Input models of HSQLDB, JFlex and Grep

We then generated the exhaustive test set consisting of all possible interactions of these options. For each of them, we executed the prepared testing file. We recorded the output of each test case to observe whether there were test cases containing prior MFS that did not produce the corresponding bug. Later we refer to those test cases that contain the MFS but did not trigger the expected failure as the *masked* test cases.

normal

lookAhead

type

standalone

 $2^{10} \times 3^2 \times 4^1$

 $2^{11} \times 3^2 \times 4^1$

versions Config space

2

3

2

2.6.3

2.22

39:26 X. Niu et al.

software	versions	all tests		failure		masking	total
HSQLDB	2cr8	18432	#1(2304)	#2(1152)	#3(1152)	#1>#2#3(768)	768 (16.7%)
-	2.2.5	6912	#1(1728)	#2(1728)	-	#1>#2(576)	576 (16.7%)
-	2.2.9	6912	#1(2304)	#2(768)	#3(384)	#1>#2#3(960) #2>#3(768)	1728 (50%)
JFlex	1.4.1	36864	#1(12288)	#2(12288)	-	#1>#2(6144)	6144 (25%)
-	1.4.2	73728	#1(18432)	#2(18432)	-	#1>#2(6144)	6144 (16.7%)
Grep	2.6.3	384	#1(128)	#2(64)	#3(72)	#1>#2#3(80) #2>#3(16)	96 (36.4%)
-	2.22	576	#1(192)	#2(64)	#3(80)	#1>#2#3(80) #2>#3(16)	6144 (28.6%)

Table XVIII. Number of failures and their masking effects

8.1.2. Results and discussion. Table XVIII lists the results of our survey. Column "all tests" gives the total number of test cases executed. Column "failure" indicates the number of test cases that failed during testing. Specifically, we give the specific number of failing test cases of each fault (labeled in the form #n). Note that the faults we listed here include some uncontrolled dependencies, so there are more faults than Table XVI. Column "masking" indicates the specific number of test cases that are masked by each fault. In this column, we use the form (#m > #n#n"...) to indicate that fault #m masks faults (#n#n"...). The last column "total" shows the number of masked test cases in total (for all the faults). The percentage in the parentheses in this column indicates the proportion of masked test cases and the failing test cases.

We observed that for each version of the software under analysis listed in Table XVIII, test cases with masking effects do exist, i.e., test cases containing MFS did not trigger the corresponding bug. In fact, there are 768 out of 4608 test cases (about 16.7%) in hsqldb with 2rc8 version. This rate is about 16.7%, 50%, 25%, 16.7%, 36.4%, and 28.6% respectively, for the remaining software versions.

So the answer to **Q1** is that in practice, when SUTs have multiple faults, masking effects do exist widely.

It is notable that in Yilmaz's [Yilmaz et al. 2014] paper, a similar study about the existence of the masking effects has been conducted. The main difference between that work and ours is that their work quantifies the impact of the masking effects as the number of τ -degree schemas that only appear in the test cases that triggered failures of other faults. Here, the τ -degree schemas can be either MFS or not. Our work, however, quantifies the masking effects as the number of test cases that are masked by different failures. These test cases should contain some MFS, i.e., they should have triggered the expected failure if they did not trigger any other different failure. The reason that we quantify the masking effects in such way is because our work seeks to overcome the masking effects in the MFS identifying process. As the test cases which contain the MFS but do not produce the corresponding failure will significantly affect the MFS identifying results, their number can better reflect the impact of the masking effects on the FII approach.

8.2. Comparing our approach with traditional approaches

The second study aims to compare the performance of our approach with traditional approaches in identifying MFS under the impact of masking effects. To conduct this study, we need to apply our approach and traditional algorithms to identify MFS in a variety of software and evaluate their results. The seven versions of software in Table XVI used as test objects are far from the requirement for a general evaluation. However, to construct real testing objects for evaluations is time-consuming. This is because we must carefully study the detail of that software as well as the bug tracker reports. To compromise, we synthesized 5 more testing objects. These synthesized objects

Object	Model	Faults	MFS of each fault
H2cr8	$2^9 \times 3^2 \times 4^1$	$e_1 > e_2 > e_3$	$(5_1, 6_0, 7_0)_{e_1}, (5_1, 8_2, 9_2)_{e_2}, (5_1, 8_2, 9_1)_{e_2}, (5_1, 8_3, 9_2)_{e_3}, (5_1, 8_3, 9_1)_{e_3}$
H2.2.5	$2^{8} \times 3^{3}$	$e_1 > e_2$	$(6_1,7_0)_{e_1},(5_2)_{e_2}$
H2.2.9	$2^{8} \times 3^{3}$	$e_1 > e_2 > e_3$	$(6_0)_{e_1}, (0_1, 5_1, 7_0)_{e_2}, (0_0, 5_1, 7_0)_{e_2}, (5_1, 7_0)_{e_3}$
J1.4.1	$2^{10} \times 3^2 \times 4^1$	$e_1 > e_2$	$(0_0)_{e_1}, (1_0)_{e_2}$
J1.4.2	$2^{11} \times 3^2 \times 4^1$	$e_1 > e_2$	$(1_0, 2_1)_{e_1}, (0_1)_{e_2}$
G2.6.3	$2^5 \times 3^1 \times 4^1$	$e_1 > e_2 > e_3$	$(0_0)_{e_1}, (1_1, 2_1)_{e_2}, (3_0, 4_1)_{e_3}, (3_1, 4_1)_{e_3}, (3_2, 4_1)_{e_3}$
G2.22	$2^4 \times 3^2 \times 4^1$	$e_1 > e_2 > e_3$	$(0_0)_{e_1}, (1_0, 2_3)_{e_2}, (1_1, 2_3)_{e_2}, (3_0, 4_0)_{e_3}$
syn1	$2^7 \times 3^2 \times 4^1$	$e_4 > e_3 > e_2 > e_1$	$(2_0,7_0)_{e_1},(3_1,5_1)_{e_2},(4_0)_{e_2},(6_0,7_2)_{e_3},(6_1,8_2)_{e_4}$
	$2^4\times 3^2\times 4^1$		$(2_0, 3_0)_{e_1}, (2_0, 5_1)_{e_1}, (4_0, 6_1)_{e_2}, (3_1, 6_0)_{e_2}, (2_2, 4_3)_{e_3}$
syn3	$2^4 \times 3^3 \times 4^1$	$e_4 > e_3 > e_2 > e_1$	$(0_0, 1_0)_{e_1}, (1_1, 2_1)_{e_2}, (2_1, 3_1)_{e_2}, (4_1, 7_1)_{e_3}, (5_2, 6_2)_{e_4}$
syn4	$2^7 \times 3^2 \times 4^1$	$e_5 > e_4 > e_3 > e_2 > e_1$	$(0_0)_{e_1}, (1_1, 3_0)_{e_2}, (2_1)_{e_3}, (4_0, 5_0)_{e_4}, (6_0)_{e_5}$
syn5	37	$e_4 > e_3 > e_2 > e_1$	$(0_0)_{e_1}, (2_0, 3_0)_{e_2}, (2_1, 4_1)_{e_2}, (1_2, 2_2)_{e_3}, (0_2, 6_0)_{e_4}$

Table XIX. The testing models used in the case study

are five small programs which can directly return outputs when executed with given inputs (details of them are also available at http://gist.nju.edu.cn/doc/multi/.).

Table XIX lists the testing model for both the real and synthetic testing objects. In this table, column 'Object' indicates the SUT under test. For the real SUT listed in Table XVI, we label the seven software as H2cr8, H2.2.5, H2.2.9, J1.4.1, J1.4.2, G2.6.3and G2.22 respectively. While for the synthesized ones, we label them in the form of 'syn+ id'. Column 'Model' presents the input space for each testing object. Column 'Faults' shows the different faults in the software and their masking relationships. In this column, '>' means the left fault will mask the right fault, i.e., if the a failure of the left fault is triggered, then the failure of the right fault will not be triggered. Furthermore, '>' is transitive so that the left fault can mask all the faults in the right. For example, for the H2cr8 object, we can find three faults: e_1 , e_2 , and e_3 . By using the formula $e_1 > e_2 > e_3$, we indicate that fault e_2 will mask e_3 ; and e_1 will mask both e_2 and e_3 . Here for the simplicity of the experiment, we did not build more complex testing scenarios such as the masking effects can be in the form $e_1 > e_2$, $e_2 > e_3$, $e_3 > e_1$ or even $e_1 > e_2$, $e_2 > e_1$. The last column shows the MFS of each fault. The MFS is presented in an abbreviated form $\{\#index_{\#value}\}_{fault}$, e.g., for the object H2cr8, $(5_1, 6_0, 7_0)_{e_1}$ actually means (-, -, -, -, -, 1, 0, 0, -, -, -, -, -) is the MFS of fault e_1 .

8.2.1. Study setup. After preparing the objects under testing, we then applied our approach (FIC BS with replacement strategy) to identify the MFS. Specifically, for each SUT we selected each test case that failed during testing and fed it into our FII approach as the input. Then, after the identifying process was completed, we recorded the identified MFS and the extra test cases needed. For the traditional FIC BS approach, we designed the same experiment. But as the objects being tested have multiple faults for which the traditional FIC BS can not be applied directly, we adopted two traditional strategies on the FIC BS algorithm, i.e., regarded as same failure and distinguishing failures as described in Section 4.3. The purpose of recording the generated additional test cases is to quantify the additive cost of our approach.

We next compared the identified MFS of each approach with the prior MFS to quantify the degree that each suffers from masking effects. There are five metrics used in this study, listed as follows:

- (1) Accurate number: the number of identified MFS which are actual prior MFS.
- (2) Super number: the number of identified MFS that are the super schemas of some prior MFS.

39:28 X. Niu et al.

(3) Sub number: the number of identified MFS that are the sub schemas of some prior MFS.

- (4) *Ignored number*: the number of schemas that are in the prior MFS, but irrelevant to the identified MFS.
- (5) *Irrelevant number*: the number of schemas in the identified MFS that are irrelevant to the prior MFS.

Among these five metrics, the accurate number directly indicates the effectiveness of the FII approaches, since to identify as many actual MFS as possible is the target for every FII approach. Metrics ignored number and irrelevant number indicate the extent of deviation for the FII approaches; specifically, the former indicates how much information about the MFS will miss, while the latter indicates how serious the distraction would be due to the "useless" schemas identified by the FII approach. Super number and sub number are the metrics in between, i.e., to identify some schemas that is super or sub schemas of the actual MFS is better than identifying irrelevant ones or ignoring some MFS, but it is worse than identifying the schema that is identical to some actual MFS. This is intuitive, as given the super / sub schemas, we just need to remove / add some elements of the original schemas to get the actual MFS. While for the irrelevant or ignore schemas, however, more efforts will be needed (e.g., both adding and removing operations will be needed to revise the irrelevant schemas to the actual MFS).

Besides these specific metrics, we also define a composite metric to measure the overall performance of each approach. The composite metric *aggregate* is defined as follows:

$$Aggregate = \frac{accurate + related(super) + related(sub)}{accurate + super + sub + irrelevant + ignored}$$

In this formula, accurate, super, sub, irrelevant, and ignored represent the value of specific metric. To refine the evaluation of different super / sub schemas, we design a related function which gives the similarity between the schemas (either super or sub) and the real MFS, so that we can quantify the specific effort for changing a super / sub schema to the real MFS. The similarity between two schemas c_1 and c_2 is computed as:

$$Similarity(c_1, c_2) = \frac{number\ of\ same\ elements\ in\ c_1\ and\ c_2}{\max(Degree(c_1), Degree(c_2))}$$

For example, the similarity of (- 1 2 - 3) and (- 2 2 - 3) is $\frac{2}{3}$. This is because (- 1 2 - 3) and (- 2 2 - 3) have the same third and last elements, and both of them are 3-degree.

The *related* function is the summation of similarity of all the super or sub schemas with their corresponding MFS.

8.2.2. Results and discussion. Figure 5 depicts the results of the second case study. There are seven sub-figures in this figure, i.e., Figure 5(a) to Figure 5(g). They indicate the results of the number of accurate MFS each approach identified, the number of identified schemas which are the sub-schema / super-schema of some prior MFS, the number of ignored prior MFS, the number of identified schemas which are irrelevant to all the prior MFS, the aggregate value, and the extra test cases each algorithm needed, respectively.

For each sub-figure, there are four polygonal lines, each of which shows the results for one of the four strategies: regarded as same failure, distinguishing failures, replacement strategy based on ILP searching, replacement strategy based on random searching



Fig. 5. Result of the evaluation for second case study

ACM Transactions on Embedded Computing Systems, Vol. 9, No. 4, Article 39, Publication date: March 2010.

39:30 X. Niu et al.

(The last one will be discussed in the next case study). Specifically, each point in the polygonal line indicates the specific result of a particular strategy for the corresponding testing object. For example in Figure 5(a), the point marked with '■' at (1,0.25) indicates that the approach using *regarded as same failure* strategy identified 0.25 accurate MFS on average for one failing test case of the testing object—HSQLDB 2cr8. The raw data for this experiment can be found in Table XXI of the Appendix. Note that all these data are average values, i.e., the average performance of these approaches when identifying the MFS in each failing test case.

Accurate number: Figure 5(a) shows the average number of accurate schemas that each approach achieved. It appears that *ILP* performed the best among the three approaches. In fact, for most testing objects (testing objects 1, 4, 5, 6, 7, 9, 10, 11 and 12), *ILP* either obtained the most number of accurate MFS, or tie with the most number of accurate MFS. The second best approach is *distinguishing failures*, which obtained better results than *regarded as same failure* for testing objects 1, 6, 8, 9, 10, 11, and 12.

Sub number & super number: Figure 5(b) and 5(c) depicts the results for *sub number* and *super number*, respectively. These two figures firstly showed a clear trend for strategies *regarded as same failure* and *distinguishing failures*, i.e., the former identified more sub schemas of actual MFS than the latter, while the latter identified more super schemas of actual MFS than the former. This is consistent with our formal analysis in Section 4.1 and Section 4.2.

The performance of our strategy *ILP* for these two metrics are in between. Specifically, *ILP* identify more sub schemas than strategy *distinguishing failures* but fewer than *regarded as same failure*; and *ILP* identify more super schemas than *regarded as same failure*, but fewer than *distinguishing failures*.

Ignore number & irrelevant number: The results of the two negative performance metrics are given in Figure 5(d) and 5(e), respectively. One observation is that, comparing with strategy *regarded as same failure*, *distinguishing failures* obtained fewer irrelevant schemas, but ignored more actual MFS. This is also consistent with formal analysis in Section 4. Note that for metric *irrelevant number*, strategy *regarded as same failure* obtained significantly much more irrelevant schemas than the remaining strategies, which make it hard to distinguish each other if we post them together into one figure. Hence, we draw this figure with only three polygonal lines (for *distinguishing failures*, *ILP*, and *random* respectively). Besides this, we offer a smaller figure in Figure 5(e), which includes the strategy *regarded as same failure*, to depicts the comparison of all these approaches.

The second observation is that *ILP* did a good job at reducing the scores for these two negative metrics. Specifically, for *ignored number*, our approach performed better than strategy *distinguishing failures* at the most testing objects (1, 3, 7, 10, 11, 12) in Figure 5(d), but is not as good as strategy *regarded as same failure*. In fact, strategy *regarded as same failure* has a significant advantage at reducing the number of ignored MFS as it tends to associate the failures with all the failing test cases. However, when we consider the *irrelevant number*, we can find that our approach is the best among all three strategies (better than *distinguishing failures* at testing objects 1, 3, 6, 7, 11, 12 in Figure 5(e), and better than strategy *regarded as same failure* for almost all the testing objects). We believe this improvement is caused by our test cases replacing strategy, as it can increase the test cases that are useful for identifying the MFS and decrease those useless test cases.

Aggregative for the five metrics: The composite results are given in Figure 5(f). This metric gives an overall evaluation of the quality of the identified schemas. From this figure, we can find that *ILP* performed the best, next the *distinguishing failures*,

the last is the *regarded as same failure* (See the testing objects 1, 3, 4, 6, 7, 10, 11, and 12 in Figure 5(f)).

It is as expected that *ILP* performed better than *distinguishing failures* as it is actually the refinement version of latter. In fact, *ILP* also make the failures distinguished from each other. The main difference between ILP and distinguishing failures is that the former has to replace the test cases that triggered any failure other than the currently analysed one while the latter will not change the generated test cases.

It is a bit of surprise to find, however, that strategy distinguishing failures performed better than regarded as same failure at almost all the testing objects. This result cannot be derived from the formal analysis. We believe the reason is that the masking effects are monotonic in these testing objects we constructed for evaluation. That is, it can only appear that bug A always mask bug B, but cannot have the circumstances that bug A can mask bug B and bug B can also mask bug A. This condition is favorable for the distinguishing failures strategy. For example, assume bug A masks bug B; then when we identify the MFS of bug A, the distinguishing failures is the correct strategy, as if there is a test case trigger the bug B, then it must not trigger the bug A (otherwise, bug B will not be triggered). Hence, there is a probability that is up to 50 that distinguishing failures strategy makes the correct operation.

Test cases: The number of test cases generated for identifying the MFS indicates the cost of FII approach. The result is shown in Figure 5(g). We can find that strategy *ILP* generated more test cases than the other strategies. In specific, the gap between the *ILP* and other two strategies ranged from about 2 to 5. This is acceptable when comparing to all the test cases that each approach needed. The increase in test cases for our approach is necessary, as additional test cases must be generated when some test cases cannot help to identify the MFS of the currently analysed failure. As for strategies distinguishing failures and regarded as same failure, there is no significant difference between the number of test cases generated.

Above all, we draw three conclusions, which help to answer **Q2**:

- 1) Distinguishing failures strategy obtained more super number and ignored number than regard one failure strategy, while the latter identified more sub number and irrelevant number than the former. This result is consistent with the previous formal analysis in Section 4.
- 2) Considering the quality of the MFS each approach identified, we can find that our *ILP* approach achieves the best performance, followed by the strategy *distinguishing failures*.
- 3) Although our approach need more test cases than the other two strategies, it is acceptable.

8.3. Evaluating the ILP-based test case searching method

The third empirical study aims to evaluate the efficiency of the ILP-based test case searching component of our approach. To conduct this study, we implemented an FII approach which is also augmented by the *replacing test cases* strategy, with test case randomly replaced.

- 8.3.1. Study setup. The setup of this case study is based on the second case study, and uses the same SUT model as shown in Table XIX. We apply the new random searching based FII approach to identify the MFS in the prepared SUTs. To avoid the bias coming from the randomness, we repeat the new approach 30 times to identify the MFS in each failing test case. We then compute the average additional test cases as well as other metrics listed in section 8.2.1 for the random-based approach.
- 8.3.2. Results and discussion. The evaluation of this random-based approach is also shown in Figure 5, in which the polygonal line marked with ' \star ' in each sub-figure

39:32 X. Niu et al.

indicates the results. The raw data can also be found in the Row 'R' of Table XXI in the appendix. In addition, as the approach is based on random, we offer the t-test to test whether. The p-value is also given in the Row 'P(I,R)' Table XXI.

Compared to the ILP-based approach, we can firstly observe that there is little distinction between them in terms of the metrics: accurate schemas, super-schemas, subschemas, ignored schemas, irrelevant schemas (for some particular cases the ILP-based approach performs slightly better, e.g., in Figure 5(b) for the first testing object, the ILP-based approach identified fewer sub schemas than that of the Random-based approach and in Figure 5(c) still for the first object the ILP-based approach identified fewer super schemas than that of the random-based approach). The similar quality of the identified MFS between these two approaches is conceivable as they both use the test case replacement strategy, although the test cases generated may be different.

Secondly, when considering the cost, we find that the ILP-based approach performs better, which can reduce on average 1 to 2 test cases compared to the random-based procedure.

At last, considering the p-value.

To be precise, we next compared the test cases only used for replacement of the two approaches. By this we can eliminate the interference of other test cases for identifying MFS, and focus on the performance of the key part of these two approaches — replacement strategy.

Figure 6 shows the result. The data is normalized so that the results of the 15 objects can be shown together. For all subjects ILP reduce the test cases for replacement by about 5 to 40 percent when compared with the random-based approach. On average, for each call of the replacement algorithm, it can save about 0.44 test cases (labeled in each dot of the line). This may be trivial. But considering the masking status in Table XVIII, this cost reduction is significant for MFS identifying in practice.

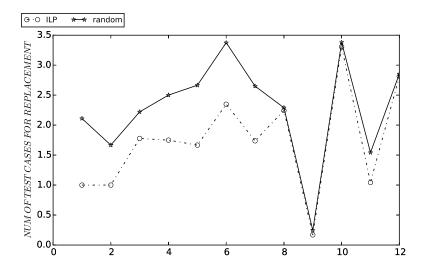


Fig. 6. The comparison of the number of replacement test cases

In summary, the answer for **Q3** is that searching for a satisfied test case affects the performance of our approach, especially regarding the number of extra test cases, and the ILP-based test cases can handle the masking effects at a relatively smaller cost than the random-based approach.

Table XX. The average test cases needed for one replacement

	H2cr8	H2.2.5	H2.2.9	J1.4.1	J1.4.2	G2.6.3	G2.22	syn1	syn2	syn3	syn4	syn5
ILP	1	1	1.77	1.75	1.66	2.34	1.73	2.24	0.16	3.3	1.04	2.81
Rand	2.11	1.66	2.22	2.5	2.66	3.37	2.64	2.29	0.24	3.38	1.54	2.85
\mathcal{P}	1.6E-60	1.1E-51	1.3E-51	2.5E-67	3.9E-70	8.0E-37	1.5E-42	2.5E-28	2.1E-28	1.1E-28	4.3E-45	3.2E-16

8.4. Comparison with Feedback driven combinatorial testing

The FDA-CIT [Yilmaz et al. 2014] approach can handle masking effects so that the generated covering array can cover all the τ -degree schemas without being masked by the MFS. There is an integrated FII approach in the FDA-CIT, which has two versions, i.e., ternary-class and multiple-class. In this paper, we use the multiple-class version for our comparative approach, as Yilmaz claims that it performs better than the former [Yilmaz et al. 2014].

The FDA-CIT process starts with generating a *t*-way covering array (In [Yilmaz et al. 2014], this is a test case-aware covering array [Yilmaz 2013]). After executing the test cases in this covering array, it records the outcome of each test case and then applies the classification tree method (Wekas implementation of C4.5 algorithm(J48) [Hall et al. 2009]) on the test cases to characterize the MFS of each fault. It then labels these MFS as the schemas that can trigger masking effects. Later, if the interaction coverage is not satisfied (here the interaction coverage criteria is different from the traditional covering array [Yilmaz et al. 2014]), it will re-generate a covering array that aims to cover these schemas that were masked by these MFS and then repeat the previous steps.

The main target of FDA-CIT is to guarantee that the generated test cases should cover all the τ -degree schemas. To achieve this goal, FDA-CIT needs to repeatedly identify the schemas that can trigger the masking effects. So to make the two approaches (FDA-CIT and ILP) comparable, we need to collect all the MFS that FDA-CIT characterized in each iteration and then compare them with the MFS identified by our approach.

8.4.1. Study setup. As FDA-CIT used a post-analysis (classification tree) technique on covering arrays, we first generated 2 to 4 ways covering arrays. The covering array generating method is based on augmented simulated annealing [Cohen et al. 2003], as it can be easily extended with constraint dealing and seed injection [Cohen et al. 2007b], which is needed by the FDA-CIT process. As different test cases will influence the results of the characterization process, we generated 30 different 2 to 4 way covering arrays and fed them to the FDA-CIT. Then after running FDA-CIT, we recorded the MFS identified, and by comparing them with prior actual MFS, we can evaluate the quality of the identified schemas according to the metrics mentioned in the previous case study.

Besides the FDA-CIT, we also applied our ILP-based approach to the generated covering array. Specifically, for each failing test case in the covering array, we separately applied our approach to identify the MFS of that case. In fact, we can reduce the number of extra test cases if we utilize the other test cases in the covering array [Li et al. 2012]), but we did not utilize the information to simplify the experiment. Similarly, we then recorded the MFS that are identified by our approach, and evaluate them according to the corresponding metrics. In addition, we recorded the overall test cases (including the initially generated covering array) that this approach needed and compared the magnitude of these test cases with that of FDA-CIT.

As mentioned before, the FII approach in FDA-CIT, i.e., classification tree algorithm, is a post-analysis technique. Given different test sets, the results identified by the classification tree algorithm are also different. Then a natural question is, what the

39:34 X. Niu et al.

schemas identified by FDA-CIT will be if the classification tree method is applied on the test cases generated by our ILP approach? This question is of importance as first, we can learn whether the test cases generated by ILP can help FDA-CIT approach to improve the quality of the identified schemas; second, the comparison between ILP and FDA-CIT will be more fair as they share the same test cases. For this, a new approach that is based on FDA-CIT is introduced, which is augmented by replacing the original test cases in FDA-CIT with those generated by ILP approach. Then the schemas identified by the classification tree algorithm in FDA-CIT are recorded and evaluated. This new approach is referred to as *FDA-CITs* later.

8.4.2. Result and discussion. The result is shown in Figure 7. We conducted three groups of experiments. The first one generated 30 different 2-way cover arrays for each testing object, and then for each covering array we applied the three approaches to identify the MFS. The average evaluation results for the experiments based on 30 covering arrays are listed in the Sub-figure 7(a). The other two groups of experiments starts with 3-way covering arrays and 4-way covering arrays, of which their results are depicted in Sub-figure 7(b) and 7(c) respectively.

In each sub-figure, there are 7 columns, showing the outcomes for the previous mentioned 6 metrics and one more metric (Column *Testcase*), which indicates the overall test cases that each approach needed. Each column has three bars (Except for the Column *Testcase*, as the overall test cases for ILP and FDA-CITs are the same), which indicate the results for approach FDA-CIT, ILP and FDA-CITs, respectively.

Note that in Figure 7, the results for each metric is the average evaluation for all the results of the experiments on the 15 testing objects in Table XIX. The raw results for each testing object are listed in Table XXII in the appendix. The raw data is organised the same way as Table XXI, except that we added a column t which indicates the strength of the covering array generated for this experiment.

With respect to the relationships between the results and the degree t of the covering arrays, we have the following observations:

First, for every metric in our study, the order of the performance of each approach is stable against the change of degree t. Take for example the metric accurate number. No matter what t is (2, 3 or 4), ILP always obtained the most schemas that are identical to the actual MFS, then is FDA-CITs, and the last is FDA-CIT. This observation indicates that the difference between the performance of these approaches is not dependent on the characteristics of the covering array, but instead on the approaches themselves.

Second, with increasing t, the overall performance of each approach is improved. For example, the score of the aggregative metric of ILP is 0.55, 0.66 and 0.69, respectively, for t equals to 2, 3 and 4. The improvement is mainly because with increasing t, the number of test cases also increased. Accordingly, the approach will observe more failing test cases, so that we can get the schemas more close to the actual MFS.

Third, for different approaches in our study, the effect of the change of t on the scores of other metrics varies. Specifically, for ILP, with increasing t, metrics accurate number, sub number, super number, irrelevant number also increase, while metric ignore number decreases. This is mainly because ILP is based on FIC_BS [Zhang and Zhang 2011], which works on single failing test case. When t increases, the number of test cases also increases. Then when applying our approach, more schemas may be identified from those additional failing test cases, so the number of accurate MFS, subschemas of the actual MFS, super-schemas of the actual MFS, and schemas that are irrelevant to the actual MFS will increase. Furthermore, some actual MFS that had been ignored before may be obtained. For FDA-CIT and FDA-CITs, however, we find that $sub\ number\ and\ irrelevant\ number\ decrease\ with increasing <math>t$. We believe this result is due to the use of the classification tree method. A typical classification tree

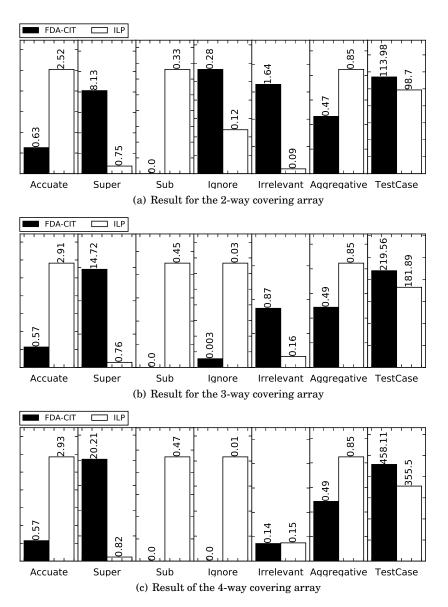


Fig. 7. Three approaches augmented with the replacing strategy

works by partitioning the test cases according to some aspects. Here, the aspect is the parameter value of the SUT. And one path (conjunction of nodes from the root to one leaf in the tree) in this tree is deemed as an MFS. So when test cases increase, the classification may need more nodes to classify the test cases. This induces the so-called 'over fitting' problem. As a result, the schemas identified by *FDA-CIT* and *FDA-CITs* tend to be the super schemas of the actual MFS, leading to a decrease of *sub number* and *irrelevant number*.

Other observations include:

First, compared with the original approach *FDA-CIT*, *FDA-CIT*s has obvious advantages at almost all the metrics except for *super number*. In detail, *FDA-CITs* obtained

39:36 X. Niu et al.

more schemas that are identical to the actual MFS (accurate number), fewer schemas that are the sub schemas of actual MFS (sub number), and lower scores for the two negative metrics (ignored number and irrelevant number). At last, the schemas identified by FDA-CITs showed an overall higher quality than that of the original FDA-CIT (aggregative metric). We have discussed previously that FDA-CIT tends to identify super-schemas of actual MFS when the test cases increase. So for metric super number, it is no surprise that FDA-CITs identified more super schemas of actual MFS than FDA-CIT, because it used the test cases generated by ILP, which were more than that of the original FDA-CIT. The difference between the overall performance of FDA-CIT and FDA-CITs is also expected. In fact, this result is consistent with our previous observation that when t increases, the overall performance for each approach also increases.

Second, in terms of the quality of the MFS identified, we can clearly find that our approach performed better than the other approaches. This is manifested in that our approach obtained more accurate schemas and identified fewer irrelevant ones. We believe this gap is mainly caused by the FII approach. Because for *ILP* and *FDA-CITs*, the test cases used to identify the MFS are the same. The only difference is how they utilize them to identify MFS. However, this result does not mean that FIC_BS is better than the classification tree method under all conditions. The classification tree method has its own advantage, i.e., it does not need to generate additional test cases, and as a result, *FDA-CIT* generated fewer test cases than that of *ILP*.

In fact, another reason that our approach generated more test cases is that the FII approach, i.e., FIC BS, works on single test case, so when there are many failing test cases in the covering array, we need to repeatedly use our approach to identify the MFS for each failing test case. This process may produce many redundant test cases, because many failing test cases contain the same MFS, and when we have already identified the MFS in one test case, there is no need to identify it again in other failing test cases. Jieli [Li et al. 2012] introduced a method that utilizes the previous generated test cases to reduce such redundance. Here we did not use this technique to simplify our experiment. We believe if we utilize the MFS that has been already identified in previous iteration, the overall number of test cases will decrease.

Above all, we can conclude three points in this experiment, which provide answer to $\mathbf{Q4}$:

1)The degree t of the covering array does not affect the order of the performance of different approaches, but for each approach, the bigger the t is, the better its performance.

2) When taking the test cases generated by our *ILP* approach, *FDA-CITs* performed better than the original *FDA-CIT* approach.

3)Considering the quality of the MFS each approach identified, *ILP* performed better than the other two approaches, although it needed more test cases.

Based on these observations, a recommendation for selecting masking handling techniques in practice is that to get a more precise identification of the MFS in the SUT, *ILP* is preferred, and for lower number of test cases, *FDA-CIT* may be a better choice.

8.5. Threats to validity

8.5.1. internal threats. There are two threats to internal validity. First, the characteristics of the actual MFS in the SUT can affect the FII results. This is because the magnitude and location of the MFS can make the FII approaches generate different test cases. As a result, it can make the observed failing test cases and inferred failing test cases different. In the worst case, the FII approach happens to identify the exact actual MFS, then our test case replacing strategy is of no use. In this paper, we used 15 testing objects, in which 5 are real software systems with real faults and 10 synthetic

ones with injected faults. To reduce the influence caused by different characteristics of the MFS, we need to build more testing objects and injected additional types of faults for a more comprehensive study of our approach.

The second threat is that we just applied our test case replacing strategy on one FII approach – FIC_BS [Zhang and Zhang 2011]. Although we believe the test case replacing strategy can also improve the quality of the identified MFS for other FII approaches when the testing object is suffering from masking effects, the extent to which their results can be refined may vary for different FII approaches. For example, for FIC_BS [Zhang and Zhang 2011] used in this paper, there are about (v-1) to $(v-1)^{k-1}$ (k is the number of parameters in a test case, v is the number of values each parameter can take) candidate test cases that can be replaced when one test case triggered failure of other fault, while for OFOT [Nie and Leung 2011a], there are (v-1) candidates. As a result, FIC_BS can have a higher chance than OFOT to find a satisfied test case. To learn the difference between the improvement of different FII approaches when applying our test case replacing strategy, we need to try more FII approaches in the future.

8.5.2. external threats. One threat to external validity comes from the real software we used. In this paper we have only surveyed two types of open-source software with five different versions, of which the program scale is medium-sized. This may impact the generality of our results.

The second threat comes from the possible masking relationships between multiple faults in the real software. In this paper, we just focus on the condition that the masking effects are transitive, i.e., if fault A masks B, and fault B masks C, then fault A must mask fault C. In practice, the relationships between multiple faults may be more complicated. One possible scenario is that two faults are in a loop, for which they can even mask each other in a particular condition. Such a case will make our formal analysis invalid and will significantly complicate the relationships between schemas and their corresponding test cases. A new formal model should be proposed to handle that type of masking effects.

The third threat is that all the failures in the experiments are option-related. In practice, some failures may not related to the parameters you modeled in the SUT. For example, consider the Internet Explorer option-compliant testing problem [Nie et al. 2013]. Initially we may not properly model the options we should test, as a result, it can happen the explorer will always crash no matter we change which option in the initial model. This will cause the MFS identification non-sense, as all the test cases fail during testing. To solve this problem, one potential solution is to re-model the options we should test, as the error may be related to other options in the SUT (For example, those options which are set to default value). Or alternately, we should try other testing techniques to assist original CT. For example, if the error is related to the internal code instead of those configuration options, we may try programming slicing technique [Weiser 1981] or spectrum-based approaches [Naish et al. 2011]. In such case, the parameters that we model for the SUT should not only limited to be configuration options or simple inputs, but also those variables, predicates, or other logical structures and data in the software we test.

9. RELATED WORKS

Shi and Nie presented an approach for failure revealing and failure diagnosis in CT [Shi et al. 2005], which first tests the SUT with a covering array, then reduces the value schemas contained in the failing test case by eliminating those appearing in the passing test cases. If the failure-causing schema is found in the reduced schema set, failure diagnosis is completed with the identification of the specific input values

39:38 X. Niu et al.

which caused the failure; otherwise, a further test suite based on SOFOT is developed for each failing test case, and the schema set is then further reduced, until no more faults are found or the fault is located. Based on this work, Wang proposed an AIFL approach which extended the SOFOT process by adaptively mutating factors in the original failing test cases in each iteration to characterize failure-inducing interactions [Wang et al. 2010].

Nie et al. introduced the notion of Minimal Failure-causing Schema(MFS) and proposed the OFOT approach which is an extension of SOFOT that can isolate the MFS in the SUT [Nie and Leung 2011a]. This approach mutates one value for that parameter, hence generating a group of additional test cases each time to be executed. Compared with SOFOT, this approach strengthens the validation of the factor under analysis and can also detect the newly imported faulty interactions.

Delta debugging [Zeller and Hildebrandt 2002] is an adaptive divide-and-conquer approach to locate interaction failure. It is very efficient and has been applied to real software environment. Zhang et al. also proposed a similar approach that can efficiently identify the failure-inducing interactions that has no overlapped part [Zhang and Zhang 2011]. Later, Li improved the delta-debugging based approach by exploiting useful information in the executed covering array [Li et al. 2012].

Colbourn and McClary proposed a non-adaptive method [Colbourn and McClary 2008]. Their approach extends a covering array to the locating array to detect and locate interaction failures. Martinez proposed two adaptive algorithms. The first one requires safe value as the assumption and the second one removes this assumption when the number of values of each parameter is equal to 2 [Martínez et al. 2008; 2009]. Their algorithms focus on identifying faulty tuples that have no more than 2 parameters.

Ghandehari et al. defined the suspiciousness of tuple and suspiciousness of the environment of a tuple [Ghandehari et al. 2012]. Based on this, they ranked the possible tuples and generated the test configurations. They further utilized the test cases generated from the inducing interaction to locate the fault [Ghandehari et al. 2013].

Yilmaz proposed a machine learning method to identify inducing interactions from a combinatorial testing set [Yilmaz et al. 2006]. They constructed a classification tree to analyze the covering arrays and detect potential faulty interactions. Beside this, Fouché [Fouché et al. 2009] and Shakya [Shakya et al. 2012] made some improvements in identifying failure-inducing interactions based on Yilmaz's work.

Our previous work [Niu et al. 2013] proposed an approach that utilizes the tuple relationship tree to isolate the failure-inducing interactions in a failing test case. One novelty of this approach is that it can identify the overlapped faulty interaction. This work also alleviates the problem of introducing new failure-inducing interactions in additional test cases.

In addition to the studies that aim at identifying the failure-inducing interactions in test cases, there are others that focus on working around the masking effects.

Constraints handling become more and more popular in CT these years. A constraint is an invalid interaction that should not appear in the test case. It can be deemed as the masking effect which are known in prior [Yilmaz et al. 2014]. Cohen [Cohen et al. 2007a; 2007b; 2008] studied the impact of the constraints that render some generated test cases invalid in CT. They also proposed an approach that integrates the incremental SAT solver with the covering arrays generating algorithm to avoid those invalid interactions. Further study was conducted [Petke et al. 2013] to show that with consideration of constraints, higher-strength covering arrays with early failure detection are practical.

Besides, there are additional works that aim to study the impact of constraints for CT [Garvin et al. 2011; Bryce and Colbourn 2006; Calvagna and Gargantini 2008;

Grindal et al. 2006; Yilmaz 2013]. Among them, [Bryce and Colbourn 2006] distinguished the constraints into two types: hard and soft, which the former cannot be included in the test case, while the latter can be permitted, but not desirable. [Grindal et al. 2006] comprehensively compared the performance of four strategies at handling the constraints in the covering array. [Calvagna and Gargantini 2008] proposed an heuristic strategy to handle the constraints. It can support an ad-hoc inclusion or exclusion of interactions such that the user can customize output of the covering array. [Garvin et al. 2011] refined the simulated annealing algorithm to efficiently construct the covering array while considering the constraints. [Yilmaz 2013] introduced the test case-specific constraints; differing from the system-wide constraints, these constraints can only be triggered in some specific test cases.

Chen et al. addressed the issues of shielding parameters in combinatorial testing and proposed the Mixed Covering Array with Shielding Parameters (MCAS) to solve the problem caused by shielding parameters [Chen et al. 2010]. The shielding parameters can disable some parameter values to expose additional interaction errors, which can be regarded as a special case of masking effects.

Dumlu and Yilmaz proposed a feedback-driven approach to work around the masking effects [Dumlu et al. 2011]. Specifically, they first used classification tree to classify the possible failure-inducing interactions and eliminate them. Then they generate new test cases to detect possible masked interaction in the next iteration. They further extended their work [Yilmaz et al. 2014] by proposing a multiple-class CTA approach to distinguish failures in the SUT. In addition, they empirically studied the impact of masking effects on both ternary-class and multiple-class CTA approaches.

These works can be categorized into 3 groups according to their relationships with our work. First, we discuss the works that aim to identifying the MFS in the SUT. Our work also focuses on identifying the MFS, but instead of single fault, our work considers the impact of multiple faults on the FII approaches, and based on this, a test case replacement strategy is proposed that can assist these FII approaches in reducing the negative effects. Second, the works that aim to deal with the constraints. As discussed before the constraints can be deemed as a special masking effect. Our work differs from them in that the masking effects handled in this paper are those that can be dynamically triggered; that is, we did not know them in prior. Another difference between our work with these constraints handling works is that their target is to avoid the constraints when generating covering array. However, our work aims to remove the masking effects of the FII approaches. Last, the work that is most similar to our work [Yilmaz et al. 2014], which also considered the masking effects that are dynamically appeared in test cases. But different from our work, it mainly focused on reducing the masking effects in the covering array, so that the covering array can support a comprehensive validation of all the τ -degree schemas. The approach used to reduce this negative effect is to use the FII approach to identify the schemas that can trigger this effect in each iteration. Our approach, however, addresses the masking effects that happened in these FII approaches themselves, and our approach alleviates the masking effects by augmenting the FII approaches with a test case replacement strategy.

10. CONCLUSIONS

Masking effects of multiple faults in the SUT can bias the results of traditional failure-inducing interactions identifying approaches. In this paper, we formally analysed the impact of masking effects on FII approaches and showed that the two traditional strategies, i.e., regarded as same failure and distinguishing failures, are both inefficient in handling such impact. We further presented a test case replacement strategy for FII approaches to alleviate such impact.

39:40 X. Niu et al.

In our empirical studies, we extended FIC_BS [Zhang and Zhang 2011] with our strategy. The comparison between our approach and traditional approaches was performed on several open-source software. The results indicated our strategy assists the traditional FII approach in achieving better performance when facing masking effects in the SUT. We also empirically evaluated the efficiency of the test case searching component by comparing it with the random searching based FII approach. The results showed that the ILP-based test case searching method can perform more efficiently. Last, we compared our approach with existing technique for handling masking effects – FDA-CIT [Yilmaz et al. 2014], and observed that our approach achieved a more precise result which can better support debugging, though our approach required more test cases than FDA-CIT.

As for the future work, we need to do more empirical studies to make our conclusions more general. Our current experiments focus on medium-sized software. We would like to extend our approach to more complicated, large-scaled testing scenarios. Another promising work in the future is to integrate the white-box testing technique into the FII approaches. We believe gaining insight into source code can help figure out the relationships between multiple faults, and hence facilitate the FII approaches obtaining more accurate results. And last, because the extent to which the FII suffers from masking effects varies with different algorithms, combining these different FII approaches would be desired in the future to further improve identifying MFS of multiple faults.

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39:42 X. Niu et al.

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Online Appendix to: Identifying minimal failure-causing schemas in the presence of multiple faults

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A. THE DETAIL ALGORITHMS OF FIC_BS

ALGORITHM 3: The algorithm of FIC_BS

```
Input: Failing test case t_{original}, Safe values of parameter SV
   Output: The MFS in the t_{original}
1 C_{free} \leftarrow NULL;
2 MFS \leftarrow NULL;
   while true do
         C_{cand} \leftarrow t_{original} \setminus C_{free} \setminus MFS;
         while |C_{cand}| > 1 && ContainMFS\_factor(C_{cand}) do
5
             (C_{low}, C_{high}) \leftarrow BinaryPartition(C_{cand});
6
             testCase \leftarrow Mutate(t_{original}, SV, C_{low} \bigcup C_{free});
7
             if Run(testCase) == PASS then
8
                  C_{cand} \leftarrow C_{low};
             else
10
11
                  C_{cand} \leftarrow C_{high};
                  C_{free} \leftarrow C_{low} \bigcup C_{free};
12
             end
13
14
        end
        if C_{cand} == NULL then
15
          break;
16
17
        end
        MFS \leftarrow MFS \cup C_{cand};
18
19 end
20 return MFS;
```

Here, C_{free} indicates the parameter values in $t_{original}$ that is not related to the failure. C_{cand} are the set of parameter values in $t_{original}$ that is needed to check in one iteration (Note that C_{cand} must contain at least one factor of MFS (line 5)). This algorithm consists of two loops. The outer loop (line 3 - 19) is to repeatedly search failure-inducing parameter values in $t_{original}$ and append them in MFS (line 18), until none of failure-inducing parameter value is found (line 15). The inter loop (line 5 - 14) focus on finding one failure-inducing parameter value in C_{cand} (Those parameters which have been determined to be part of MFS or in C_{free} is omitted (line 4)). To reach this target, the inter loop repeatedly use binary search technique to reduce the scope of parameter values (C_{cand}) that need to check (line 5 - 14). In each iteration, C_{cand} is split into two equally size part, i.e., C_{low} and C_{high} (line 6). Then a new test case is generated by

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App-2 X. Niu et al.

mutating the C_{free} part and C_{low} part of the original failing test case $t_{original}$ (line 7). For example, assume the original failing test case is (1, 1, 1, 1). The C_{free} is the second parameter value, i.e., (-, 1, -, -) and C_{low} part is the third parameter value (-, -, 1, -). Then a new test case may be generated like (1, 0, 0, 1). Note that the mutated values should be one of safe values set (SV), and the parameter values that is not mutated in this iteration is called fixed part. If the newly generated test case passed (This indicates that MFS was broken. As C_{free} is not related to the failure, hence, at least one element in C_{low} is failure-inducing), then the scope of failure-inducing elements will be reduced to C_{low} (line 8 - 9). Otherwise, it will be reduced to C_{high} part (line 11) (This is because MFS was not broken, indicating that MFS is in C_{high}). In this case, C_{low} will be appended to the C_{free} part (line 12), as it does not related to the MFS. The inter loop ends when C_{cand} has just one element (one failure-inducing parameter value is found, and should appended to MFS (line 18)), or is empty (no more failure-inducing parameter value can be found, the algorithm ends (line 15- 17)).

B. THE DETAIL OF THE EXPERIMENTS

Table XXI. Result of the evaluation

		HSQL1	HSQL2	HSQL3	JFlex1	Jflex2	Grep1	Grep2	syn1	syn2	syn3	syn4	syn5
accurate	R^{1}	0.25	0.83	0.72	1	0.83	0.59	0.7	0.39	0.88	0.55	0.54	0.28
	D^2	0.66	0.83	0.72	0.75	0.83	0.62	0.7	0.55	0.96	0.76	0.71	0.65
	I^3	0.83	0.83	0.66	1	0.83	0.78	0.92	0.48	0.98	0.93	0.78	0.76
	R 4	0.54	0.83	0.66	1	0.83	0.76	0.85	0.55	0.98	0.93	0.64	0.76
	p(I,R)5	2.34E-57	NaN	NaN	NaN	NaN	3.29E-15	2.61E-27	1.87E-38	NaN	NaN	8.04E-42	NaN
super	R	0	0	0	0	0	0	0	0	0	0	0	0
	D	0.08	0.16	0.16	0.25	0.16	0.19	0.2	0.32	0.03	0.23	0.08	0.19
	I	0.16	0.16	0.11	0	0.16	0.06	0.02	0.32	0.01	0.06	0	0.07
	R	0.02	0.16	0.11	0	0.16	0.04	0.02	0.32	0.01	0.06	0	0.07
	p(I,R)	2.32E-56	NaN	NaN	NaN	NaN	2.92E-10	NaN	NaN	NaN	NaN	NaN	NaN
sub	R	0.58	0.16	0.27	0	0.16	0.45	0.32	0.41	0.03	0.61	0.44	0.91
	D	0.16	0	0.05	0	0	0.06	0.04	0.11	0	0.02	0.13	0.12
	I	0	0	0.22	0	0	0.06	0.04	0.18	0	0.06	0.21	0.15
	R	0.16	0	0.22	0	0	0.07	0.07	0.11	0	0.06	0.22	0.15
	p(I,R)	7.84E-47	NaN	NaN	NaN	NaN	1.25E-06	5.15E-12	1.87E-38	NaN	NaN	1.15E-19	NaN
ignore	R	0.16	0	0	0	0	0	0	0.25	0.07	0.02	0.05	0.08
	D	0.08	0	0.05	0	0	0.12	0.04	0.06	0	0.07	0.13	0.19
	I	0	0	0	0	0	0.09	0	0.06	0	0.03	0.07	0.15
	R	0.27	0	0	0	0	0.12	0.04	0.06	0	0.03	0.2	0.15
	p(I,R)	7.23E-56	NaN	NaN	NaN	NaN	2.15E-12	1.25E-22	NaN	NaN	NaN	5.90E-40	NaN
irrelevant	R	0.16	0.66	0.66	5.75	3.83	1.84	1.42	0.58	0.07	2.22	0.95	2.2
	D	0.08	0	0.05	0	0	0.12	0.04	0.27	0	0.29	0.12	0.03
	I	0	0	0	0	0	0.09	0	0.27	0	0.29	0.08	0
	R	0.27	0	0	0	0	0.12	0.04	0.27	0	0.29	0.2	0
	p(I,R)	7.23E-56	NaN	NaN	NaN	NaN	2.15E-12	1.25E-22	NaN	NaN	NaN	1.16E-36	NaN
aggregate	R	0.49	0.77	0.58	0.41	0.52	0.39	0.5	0.45	0.91	0.35	0.52	0.3
	D	0.84	0.91	0.86	0.87	0.91	0.78	0.85	0.72	0.99	0.75	0.77	0.76
	I	0.95	0.91	0.88	1	0.91	0.85	0.96	0.69	0.99	0.82	0.81	0.81
	R	0.66	0.91	0.88	1	0.91	0.82	0.9	0.73	0.99	0.82	0.67	0.81
	p(I,R)	2.00E-60	NaN	NaN	NaN	NaN	1.65E-17	1.59E-28	1.87E-38	NaN	NaN	2.64E-40	NaN
testNum	R	8.12	8.66	9.16	23.5	20.5	10.24	9.5	9.9	13.03	14.51	10.4	12.75
	D	11.91	7.66	8.61	6.5	9	7.09	6.47	13.02	13.69	9.96	8.49	8.33
	I	17	10.16	12	8	11.66	11.13	12.04	18.03	14.69	17.18	11.39	21.1
	R	17.72	11.29	13.13	9.67	13.11	13.56	14.26	18.45	14.83	17.66	12.49	20.47
	p(I,R)	7.19E-47	5.07E-50	8.32E-54	1.26E-71	8.87E-73	6.97E-40	2.75 E-37	5.28E-39	1.74E-26	6.31E-42	5.79E-38	3.86E-44

 $^{^1}$ O denotes the strategy regarded as same failure. 2 D denotes the strategy distinguishing failures. 3 I denotes the replacement strategy based on ILP searching. 4 R denotes the replacement strategy based on randomly searching. 4 p(I,R) denotes the p-value of a test of significance is the probability that the results of ILP and Random are equal

Table XXII. Comparison with FDA-CIT

									DA-CII					
			HSQL1	HSQL2	HSQL3	JFlex1	Jflex2	Grep1	Grep2	syn1	syn2	syn3	syn4	syn5
	accurate	Fda-cit	1.63	0	1	0	0	0.7	1	0.3	0.83	0.13	0.96	1
		ILP	3.66	2	2	2	2	2.2	3.93	1.23	1.56	4.03	1	4.63
		n-value	4.41E-12			NaN				5.95E-05				
	super	Fda-cit		5.16		4		9.26	8.6	6.5	0.53	19.16	12.06	19.2
	super	ILP				0		0.8	0.03	1.6	0	0.53	3.63	0
			2.95E-05							4.53E-12				
	sub	Fda-cit				0		0	0	0	0	0	0	0
	sub			0			-	-	-	0.9	0	-	0	-
		ILP				0 N. N.		0.66	0.03			0.63		0.73
١.		p-value				NaN	NaN			1.31E-07		8.72E-08		8.05E-10
2-way	ignore	Fda-cit				0		0.09	0.06	0.93	0.63	0.06	0.2	0
		ILP				0		0.46	0	0.23	0	0.03	0.4	0
2			1.78E-04		8.31E-02			2.02E-02					1.20E-01	
	irrelevant			0		0		2	1.93	3.1	0.7	4.63	1.56	3.1
		ILP			0	0	0	0.46	0	0.56	0	0	0	0.03
		p-value	1.48E-13	NaN	8.31E-02	NaN	NaN	2.05E-07	2.22E-07	1.59E-09	4.89E-07	2.32E-10	1.02E-09	1.61E-07
	aggregate	Fda-cit	0.46			0.5		0.47	0.48	0.36	0.58	0.36	0.31	0.41
l		ILP	0.88	0.93	0.82	1	0.93	0.63	0.98	0.59	1	0.86	0.6	0.92
		p-value	1.29E-16	6.32E-26	1.14E-13	NaN	8.79E-23	2.42E-09	4.88E-35	1.04E-07	1.04E-07	2.14E-30	1.13E-25	3.06E-43
	testNum	Fda-cit	72.33	62.13	61.76	73	72	106.36	162.53	83.76	77.76	204.53	120.16	271.4
		ILP	132.86	57.13	63.7	61.93	73.53	74.06	92.43	103.56	92.06	161.53	153.8	117.73
										5.75E-03				
H	accurate	-		0		0	0	0.96	1	0	1	0	1	1
	accurate	ILP		$\overset{\circ}{2}$		2	$\overset{\circ}{2}$	2.3	3.73		3.43	4.03	1	4.66
			4.14E-35			NaN				2.93E-21				1.7E-27
	Supor	Fda-cit		5		4	5	12.53	13.66	19.66	23.6	38.9	21.43	18.1
	super	ILP				0		0.83	0.1	1.2	0	0.43	3.96	0
		I	2.01E-14				7.79E-30		3.5E-22	5.22E-25				
	l-									0				
	sub	Fda-cit		0		0		0	0		0	0	0	0
		ILP p-value				0 NaN	0 NaN	0.9	0.13		1.2	0.66	0	0.6
											× /17 H:= 1 1	2 1/1H:_HX		3.15E-07
Ι.									4.34E-02					
ay	ignore	Fda-cit	0	0	0	0	0	0	0	0	0	0	0.03	0
-way		Fda-cit ILP	0	0	0	0	0	0 0.1	0	0 0.2	0	0	0.03 0.09	0 0
3-way	ignore	Fda-cit ILP p-value	0 0 NaN	0 0 NaN	0 0 NaN	0 0 NaN	0 0 NaN	0 0.1 8.31E-02	0 0 NaN	0 0.2 3.14E-02	0 0 NaN	0 0 NaN	0.03 0.09 3.10E-01	0 0 NaN
3-way		Fda-cit ILP p-value Fda-cit	0 0 NaN 0.8	0 0 NaN 0	0 0 NaN 0	0 0 NaN 0	0 0 NaN 0	0 0.1 8.31E-02 1.2	0 0 NaN 0.96	0 0.2 3.14E-02 1.23	0 0 NaN 2.16	0 0 NaN 2.53	0.03 0.09 3.10E-01 1.13	0 0 NaN 0.43
3-way	ignore irrelevant	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8	0 0 NaN 0 0	0 0 NaN 0 0	0 0 NaN 0 0	0 0 NaN 0 0	0 0.1 8.31E-02 1.2 0.46	0 0 NaN 0.96	0 0.2 3.14E-02 1.23 1.06	0 0 NaN 2.16 0.36	0 0 NaN 2.53	0.03 0.09 3.10E-01 1.13 0	0 0 NaN 0.43 0.03
3-way	ignore	Fda-cit ILP p-value Fda-cit ILP p-value	0 0 NaN 0.8 0 7.43E-06	0 0 NaN 0 0 NaN	0 0 NaN 0 0 NaN	0 0 NaN 0 0 NaN	0 0 NaN 0 0 NaN	0 0.1 8.31E-02 1.2 0.46 1.05E-04	0 0 NaN 0.96 0 8.56E-07	0 0.2 3.14E-02 1.23 1.06 5.51E-01	0 0 NaN 2.16 0.36 2.42E-11	0 0 NaN 2.53 0 5.4E-10	0.03 0.09 3.10E-01 1.13 0 1.78E-06	0 0 NaN 0.43 0.03 0.066167
3-way	ignore irrelevant	Fda-cit ILP p-value Fda-cit ILP p-value	0 0 NaN 0.8 0 7.43E-06	0 0 NaN 0 0 NaN 0.52	0 0 NaN 0 0 NaN 0.63	0 0 NaN 0 0	0 0 NaN 0 0 NaN 0.52	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48	0 0 NaN 0.96 0 8.56E-07	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38	0 0 NaN 2.16 0.36 2.42E-11 0.49	0 0 NaN 2.53 0 5.4E-10	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27	0 0 NaN 0.43 0.03 0.066167
3-way	ignore irrelevant aggregate	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94	0 0 NaN 0 0 NaN 0.52 0.93	0 0 NaN 0 0 NaN 0.63 0.81	0 0 NaN 0 0 NaN 0.5	0 0 NaN 0 0 NaN 0.52	0 0.1 8.31E-02 1.2 0.46 1.05E-04	0 0 NaN 0.96 0 8.56E-07	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38	0 0 NaN 2.16 0.36 2.42E-11	0 0 NaN 2.53 0 5.4E-10	0.03 0.09 3.10E-01 1.13 0 1.78E-06	0 0 NaN 0.43 0.03 0.066167
3-way	ignore irrelevant aggregate	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06	0 0 NaN 0 0 NaN 0.52 0.93	0 0 NaN 0 0 NaN 0.63 0.81	0 0 NaN 0 0 NaN 0.5	0 0 NaN 0 0 NaN 0.52 0.93	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66	0 0 NaN 0.96 0 8.56E-07 0.48 0.96	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77	0 0 NaN 2.53 0 5.4E-10 0.38 0.86	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64	0 0 NaN 0.43 0.03 0.066167 0.48 0.93
3-way	ignore irrelevant aggregate	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35	0 0 NaN 0 0 NaN 0.5	0 0 NaN 0 0 NaN 0.52 0.93	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66	0 0 NaN 0.96 0 8.56E-07 0.48 0.96	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77	0 0 NaN 2.53 0 5.4E-10 0.38 0.86	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64	0 0 NaN 0.43 0.03 0.066167 0.48 0.93
3-way	ignore irrelevant aggregate	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35	0 0 NaN 0 0 NaN 0.5 1 NaN	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38
3-way	ignore irrelevant aggregate testNum	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23
3-way	ignore irrelevant aggregate testNum	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23
3-way	ignore irrelevant aggregate testNum	Fda-cit ILP p-value	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10
3-way	ignore irrelevant aggregate testNum	Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP p-value Fda-cit ILP	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5	0 0 NaN 0 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 12.31E-21 0 2	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10
3-way	ignore irrelevant aggregate testNum accurate	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34	0 0 NaN 0 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN	0 0 NaN 0 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27
3-way	ignore irrelevant aggregate testNum	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27
3-way	ignore irrelevant aggregate testNum accurate super	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3	0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18
3-way	ignore irrelevant aggregate testNum accurate super	Fda-cit ILP p-value	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN
3-way	ignore irrelevant aggregate testNum accurate super	Fda-cit ILP p-value Fda-cit	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16	0 0 NaN 0 0 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN	0 0 NaN 0 0 0,52 0,93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28	0 0 0 NaN 0.43 0.03 0.066167 0.48 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0
3-way	ignore irrelevant aggregate testNum accurate super	Fda-cit ILP p-value Fda-cit ILP	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0	0 0 0 NaN 0 0 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN	0 0 NaN 0 0 0NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73
	ignore irrelevant aggregate testNum accurate super	Fda-cit ILP p-value	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN	0 0 0 NaN 0 0 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 NaN	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN	0 0 NaN 0 0 0NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 0 NaN	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08
	ignore irrelevant aggregate testNum accurate super	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 NaN	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 NaN	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0,7 4.54E-09	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08
	ignore irrelevant aggregate testNum accurate super sub	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN 0	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 0 NaN	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN	0 0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 NaN	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09 0	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0
4-way 3-way	ignore irrelevant aggregate testNum accurate super sub	Fda-cit ILP p-value	0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 0 NaN	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN	0 0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 NaN 0	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 NaN	0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 0 NaN	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 0 NaN	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09 0 0 NaN	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 0 NaN
	ignore irrelevant aggregate testNum accurate super sub ignore	Fda-cit ILP p-value Fda-cit	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN 0	0 0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 0 NaN	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN	0 0 0 NaN 0 0 0,52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 0 NaN	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 NaN	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 0 NaN 0	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 0 NaN	0 0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09 0 NaN 1.03	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0 0 NaN	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 NaN
	ignore irrelevant aggregate testNum accurate super sub ignore irrelevant	Fda-cit ILP p-value Fda-cit ILP	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN 0 0 NaN	0 0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 0 NaN 0	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN	0 0 0 NaN 0 0 0,52 0,93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 0 NaN 0 0	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 NaN 0	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 NaN 0	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01 0.5 1.1	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 NaN 0 0.13	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09 0 NaN 1.03 0	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0 0 NaN 0.2	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 NaN
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	ignore irrelevant aggregate testNum accurate super sub ignore irrelevant	Fda-cit ILP p-value Fda-cit ILP	0 0 0 NaN 0.8 0 7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN 0 0 NaN 0 0 0 NaN	0 0 0 NaN 0 0 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 0 NaN 0 0 NaN	0 0 NaN 0 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0 NaN	0 0 0 NaN 0 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN	0 0 0 NaN 0 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 NaN 0 0 NaN 0	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 0.56 1.03E-06 0.44	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 0 NaN 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01 0.5 1.1 1.42E-02	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 0 NaN 0 0.13 4.34E-02	0 0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0 NaN 1.03 0 0 2.28E-06	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0 0 NaN 0.2 0 3.14E-02	0 0 0 NaN 0.43 0.03 0.066167 0.48 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 NaN 0 0 NaN
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	ignore irrelevant aggregate testNum accurate super sub ignore irrelevant aggregate	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0.7 1.59E-34 8.9 1.5 5.78E-16 0 NaN 0 0 NaN 0 0 NaN 0 0 0 NaN 0 0 0 4.17E-40 421.8	0 0 NaN 0 0 NaN 0 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 NaN 0 0 NaN 0 0 NaN 0 0 NaN 0 0 0 0	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0 NaN 0 0 NaN 0 0 0 NaN 0 0 0.63 0.82 2.29E-32 295.73	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 0 0 NaN 0 0 NaN 0 0 NaN 143.13 143.1	0 0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 0 NaN 0 0 NaN 0 0 0 NaN 0 4 4 5 6 6 1 6 1 7 8 9 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 NaN 0 0.56 1.03E-06 0.44 0.44 0.44 0.44 0.44 0.44 0.44 0.	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 0 NaN 0.90 NaN 0.90 0.90 0.90 0.90 0.90 0.90 0.90 0.9	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01 0.5 1.1 1.42E-02 0.37 0.67 3.47E-11	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 0 NaN 0 0.13 4.34E-02 0.81 1.54E-15 975.93	0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09 0 0 NaN 1.03 0 2.28E-06 0.85 3.86E-24	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0 0 NaN 0.2 0 3.14E-02 0.26 0.26 0.26 0.26 0.26 0.27	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 0 NaN 0 0 NaN 0 0.49 0.73 1.67E-08 0 0 NaN 0 0.73 1.67E-08 0 0 0.73 0.73 0.73 0.73 0.73 0.73 0.73
	ignore irrelevant aggregate testNum accurate super sub ignore irrelevant aggregate testNum	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0.7.43E-06 0.66 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN 0 0 NaN 0 0 NaN 0 0 0 NaN 0.7 0.94 4.17E-40 421.8 403.93	0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 130 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 0 NaN 0 0 NaN 0 0 NaN 0 0.52 0.93 2.36E-22 295.13 237.6	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0 NaN 0 0 NaN 0 0.63 0.82 2.29E-32 244.16	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN 0 0 NaN 0 143.13 7.77E-54 1 0 NaN 143.13	0 0 0 NaN 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 0 NaN 0 0 NaN 0 0 NaN 0 0 0 NaN 0 4 4 5 6 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 NaN 0 0.56 1.03E-06 0.44 0.64 1.59E-18 241.16 1.59E-18	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 0 NaN 0 0 NaN 0.96 1.37 1.37 1.37 1.37 1.37 1.37 1.37 1.37	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01 0.5 1.1 1.42E-02 0.37 0.67 3.47E-11 490.2 378.33	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 0 NaN 0 0.13 4.34E-02 0.5 0.81 1.54E-15 975.93 662.9	0 0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0 0 NaN 1.03 0 2.28E-06 0.85 3.86 5.52E-24 4.54E-09 0 0 0.36 0.86 0.86 0.86 0.86 0.86 0.86 0.86 0.8	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0 0 NaN 0.2 0 3.14E-02 0.26 0.64 2.02E-39 298.7 304.3	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 NaN 0 0 NaN 0 0 0.83 0.93 0.93 0.93 0.93 0.93 0.93 0.93 0.9
	ignore irrelevant aggregate testNum accurate super sub ignore irrelevant aggregate testNum	Fda-cit ILP p-value Fda-cit ILP	0 0 NaN 0.8 0.7.43E-06 0.94 5.71E-30 182.36 219.3 2.69E-08 0.9 5 1.59E-34 8.9 1.5 5.78E-16 0 0 NaN 0 0 NaN 0 0 NaN 0 0 0 NaN 0.7 0.94 4.17E-40 421.8 403.93 4.32E-03	0 0 NaN 0 0 114.2 1.32E-11 0 2 NaN 5 0.36 3.95E-30 0 NaN 0 0 NaN 0 0 NaN 0 0 NaN 0 0 10.52 0.93 2.36E-22 295.13 237.6 2.33E-36	0 0 NaN 0 0 NaN 0.63 0.81 1.68E-35 129.13 122.53 8.66E-04 1 2 NaN 6 0.36 1.43E-32 0 1 NaN 0 0 NaN 0 0 NaN 0 0.63 0.82 2.29E-32 295.73 244.16 4.39E-27	0 0 NaN 0 0 NaN 0.5 1 NaN 190.03 143.13 7.77E-54 0 2 NaN 4 0 NaN 0 0 NaN 0 0 NaN 0 143.13 143	0 0 0 NaN 0 0 0 NaN 0.52 0.93 5.47E-22 186.96 156.13 2.31E-21 0 2 NaN 5 0.33 1.71E-30 0 0 NaN 0 0 NaN 0 0 NaN 0 0 1.71E-30 0 0 0 NaN 0 0 0 1.71E-30 0 0 0 1.71E-30 0 0 0 1.71E-30 0 0 0 1.71E-30 0 0 0 1.71E-30 0 0 0 1.71E-30 0 0 0 1.71E-30 0 0 0 0 1.71E-30 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0.1 8.31E-02 1.2 0.46 1.05E-04 0.48 0.66 3.63E-17 185.73 113.66 4.26E-04 1 2.16 1.59E-16 22 0.76 1.71E-43 0 1 NaN 0 0 NaN 0 0.56 1.03E-06 0.44 0.64 1.59E-18 2.41.16 1.59E-18	0 0 0 NaN 0.96 0 8.56E-07 0.48 0.96 5.37E-29 228.8 142.93 2.10E-03 1 3.76 8.79E-21 19.26 0.16 6.47E-37 0 0.13 4.34E-02 0 0 NaN 0 0 NaN 0.47 0.95 4.52E-25 358.56 243.86 2.41E-03	0 0.2 3.14E-02 1.23 1.06 5.51E-01 0.38 0.67 2.67E-10 243.8 217.73 1.59E-04 0 3.2 7.47E-23 25.7 1.5 8.4E-28 0 0.93 1.35E-07 0 0.09 1.84E-01 0.5 1.1 1.42E-02 0.37 0.67 3.47E-11	0 0 NaN 2.16 0.36 2.42E-11 0.49 0.77 6.57E-16 359.8 267.83 9.18E-35 1 3.5 1.56E-12 29.23 0 9.14E-25 0 1.13 8.04E-09 0 0 NaN 0 0.13 4.34E-02 0.81 1.54E-15 975.93 662.9 2.46E-04	0 0 0 NaN 2.53 0 5.4E-10 0.38 0.86 2.42E-24 310.16 235.5 1.21E-02 0 3.86 5.52E-21 66.96 0.5 4.1E-36 0 0.7 4.54E-09 0 0 NaN 1.03 0 2.28E-06 0.85 3.86 5.22-21 4.54E-09 4.54E-09 0 0 0.85 3.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0 0.86 4.54E-09 0 0.86 0.86 0.86 0.86 0.86 0.86 0.86 0.	0.03 0.09 3.10E-01 1.13 0 1.78E-06 0.27 0.64 2.53E-35 171.8 205.43 2.55E-03 1 1 NaN 32.46 4.3 3.6E-28 0 0 NaN 0 0 NaN 0.2 0 3.14E-02 0.26 0.64 2.02E-39 298.7 304.3 7.41E-01	0 0 0 NaN 0.43 0.03 0.066167 0.48 0.93 9.19E-38 316.13 244.23 6.07E-10 1 4.63 4.14E-27 18 0 NaN 0 0.73 1.67E-08 0 NaN 0 0 NaN 0 0 0.83 0.93 0.93 0.93 0.93 0.93 0.93 0.93 0.9