# Identify minimal failure-causing schemas for multiple faults

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Combinatorial testing(CT) is proven to be effective to reveal the potential failures caused by the interaction of the inputs or options of the System Under Test(SUT). To extend and make full use of CT, the theory of Minimal Failure-Causing Schema(MFS) has been proposed. The use of MFS helps to isolate the root cause of the failure, which is desired after detecting them by CT. Most existed algorithms based on MFS theory focus on identifying the MFS in SUT with the single fault, however, we argue that multiple faults is the more common testing scenario, and under which masking effects may be triggered so that some expect faults will not be observed normally. Traditional MFS theory as well as its identifying algorithms lack a mechanism to handle such effects, hence will make them incorrectly isolate the MFS in SUT. To address this problem, we proposed a new MFS model with considering multiple faults. We first formally analyse the impact of the multiple faults on existed MFS isolating algorithms, especially when masking effects were triggered between these multiple faults. Based on this, we then give an approach that can assist traditional algorithms to better handle the multiple faults testing scenarios. Empirical studies with several open-source software were conducted, which show that multiple faults with masking effects do negatively affect on traditional MFS identifying approach and our approach can help them to alleviate these effects.

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## 1. INTRODUCTION

With the increasing complexity and size of modern software, many factors, such as input parameters and configuration options, can influence the behaviour of the SUT. The unexpected faults caused by the interaction among these factors can make testing such software a big challenge if the interaction space is too large. In the worst case we need to examine every possible combination of these factors as each such combination can contain unique faults[Song et al. 2012]. While conducting such exhaustive testing is ideal and necessary in theory, it is impractical and not economical in consideration of the limited testing time and computing resource. One remedy for this problem is

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Table I. MS word example

id	Highlight	$Status\ bar$	Bookmarks	Smart tags	Outcome
1	On	On	On	Off	PASS
2	On	Off	Off	On	PASS
3	Off	On	Off	Off	Fail
4	Off	Off	On	Off	PASS
5	Off	On	On	On	PASS

combinatorial testing, which systematically sample the interaction space and select a relatively small set of test cases that cover all the valid iterations with the number of factors involved in the interaction no more than a prior fixed integer, i.e., the *strength* of the interaction. Many works in CT aims to construct the smallest set of such efficient testing object [Cohen et al. 1997; Bryce et al. 2005; Cohen et al. 2003], which also called *covering array*.

Once failures are detected by covering array, it is desired to isolate the failureinducing combinations in these failing test cases. This task is important in CT as it can facilitate the debugging efforts by reducing the code scope that needed to inspected[Ghandehari et al. 2012]. Only with the information stum from the covering array sometimes is far from clear to identify the location and magnitude of the failureinducing combinations [Colbourn and McClary 2008]. Thus, deeper analysis needed to be conducted. Take an example [Bach and Schroeder 2004], Fig I present a 2-way covering array for testing the MS word application, in which we want to examine various combination of options 'Highlight', 'Status Bar', 'Bookmarks' and 'Smart tags' of MS word. Assume the third test case failed, then we can get that there are five 2-way suspicious combinations may be responsible for this failure: (Highlight: Off, Bookmarks: Off),(Highlight: Off, Smart tags: Off), (Status Bar: On, Bookmarks: Off), (Status Bar: On, Smart tags: Off), (Bookmarks: Off, Smart tags: Off). (Note that (Highlight: Off, Status Bar: On) excludes in this set as it appeared in the fifth passing test case). Without any more information, we cannot figure out which one or some in this suspicious set caused this failure. In fact, taking account of the higher-strength combination, e.g., (Highlight: Off, Status Bar: On, Smart tags: Off), the problem will grow more complicated.

To address this problem, prior work [Nie and Leung 2011a] specifically studied the properties of the minimal failure-causing schemas in SUT, based on which, a further diagnosis with generating additional test cases was applied and therefore can identify the MFS in the test case. Other works have been proposed to identify the MFS in SUT, which include approaches such as building tree model [Yilmaz et al. 2006], exploiting the methodology of minimal failure-causing schema [Nie and Leung 2011a], ranking suspicious classification ous combinations based on some rules[Ghandehari et al. 2012], using graphic-based deduction [Martínez et al. 2008] and so on. These approaches can be partitioned into two categories [Colbourn and McClary 2008]: adaptive—test cases are chosen based on the outcomes of the executed tests [Nie and Leung 2011a; Ghandehari et al. 2012; Niu et al. 2013; Zhang and Zhang 2011; Shakya et al. 2012; Wang et al. 2010; Li et al. 2012]or nonadaptive—test cases are chosen independently and can be executed parallel [Yilmaz et al. 2006; Colbourn and McClary 2008; Martínez et al. 2009; Fouché et al. 2009].

The MFS methodology as well as other MFS identifying approaches mainly focus on the ideal scenario that SUT only contains one fault, i.e., the test case under testing can either fails or passes the testing. However, in this paper, we argue that SUT with multiple distinguished faults is the more common testing scenario in practice, and moreover, this do have impact on the Failure-inducing Combinations Identifying(FCI) approaches. One main impact of multiple faults on FCI approaches is the masking effects. A masking effect [Dumlu et al. 2011; Yilmaz et al. 2013] is an effect that some

failures prevents test cases from normally checking combinations that are supposed to be tested. Take the Linux command– Grep for example, we noticed that there are two different faults reported in the bug tracker system. The first one  $^1$  claims that Grep incorrectly match unicode patterns with '<', while the second one  $^2$  claims an incompatibility between option '-c' and '-o'. When we put this two scenarios into one test case, only one fault information will be observed, which means another fault is masked by the observed one. This effects will prevent test cases normally executing, consequently make approaches make a incorrectly judgements on the correlation between the combinations checked in the test case and the fault that been prevented to be observed.

As known that masking effects negatively affect the performance of FCI approaches, a natural question is how this effect bias the results of FCI approaches. In this paper, we formalized the process of identifying MFS under the circumstance that masking effects exist in SUT and try to answer this question. One insight from the formal analysis is that we cannot completely get away from the impact of the masking effect even if we do exhaustive testing. Furthermore, both ignoring the masking effects and regarding multiple faults as one fault are harmful for FCI process.

Based on the insight we proposed a strategy to alleviate this impact. This strategy adopts the divide and conquer framework, i.e., separately handles each fault in SUT. For a particular fault under analysis, when applying traditional FCI approaches to identify the failure-inducing combinations, we pick the test cases generated by FCI approaches that trigger unexpected faults and replace them with regenerated newly test cases. These newly test cases should either pass or trigger the same fault under analysis.

Our initial work demonstrated that the extent varies to what different FCI approaches suffered from the masking effects, as a result, follow-on work in this paper was proposed to construct an additional voting system, in which we take comprehensive account of various result from different algorithms. We rank the suspicious MFS according to the frequency it appeared in each algorithm's output, and recommend the MFS which has a high ranking.

To evaluate the performance of our strategy and the voting system, we applied our strategy on three FCI approaches, which are CTA [Yilmaz et al. 2006], OFOT [Nie and Leung 2011a], FIC\_BS [Zhang and Zhang 2011] respectively. The subjects we used are several open-source software with the developers' forum in Source-Forge community. Through studying their bug reports in the bug tracker system as well as their user's manual guide, we built the testing model which can reproduce the reported bugs with specific test cases. We then applied the traditional FCI approaches and their augmented versions to identify the failure-inducing combinations in the subjects respectively. The results of our empirical studies shows that the masking effects do impact on the FCI approaches, although to what the extent varies, and the approaches augmented with our strategy can identify failure-inducing combinations more accurately than traditional ones when facing masking effects, and moreover, this performance can get further improvement with using voting system.

The main contributions of this paper are:

- We studied the impact of the masking effects among multiple faults on the isolation of the failure-inducing combinations in SUT.
- We proposed a divide and conquer strategy of selecting test cases to alleviate the impact of this effects.

<sup>&</sup>lt;sup>1</sup>http://savannah.gnu.org/bugs/?29537

<sup>&</sup>lt;sup>2</sup>http://savannah.gnu.org/bugs/?33080

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```
public float foo(int a, int b, int c, int d){
   //step 1 will cause an exception when b == c
   float x = (float)a / (b - c);

   //step 2 will cause an exception when c < d
   float y = Math.sqrt(c - d);

   return x+y;
}</pre>
```

Fig. 1. A toy program with four input parameters

Tabl	e II.	test	inputs	and	their	correspond	ling resu	lt
------	-------	------	--------	-----	-------	------------	-----------	----

id	test inputs	results	id	test inputs	result
1	(7, 2, 4, 3)	PASS	13	(11, 2, 4, 3)	PASS
2	(7, 2, 4, 5)	Ex 2	14	(11, 2, 4, 5)	Ex 2
3	(7, 2, 6, 3)	PASS	15	(11, 2, 6, 3)	PASS
4	(7, 2, 6, 5)	PASS	16	(11, 2, 6, 5)	PASS
5	(7, 4, 4, 3)	Ex 1	17	(11, 4, 4, 3)	Ex 1
6	(7, 4, 4, 5)	Ex 1	18	(11, 4, 4, 5)	Ex 1
7	(7, 4, 6, 3)	PASS	19	(11, 4, 6, 3)	PASS
8	(7, 4, 6, 5)	PASS	20	(11, 4, 6, 5)	PASS
9	(7, 5, 4, 3)	PASS	21	(11, 5, 4, 3)	PASS
10	(7, 5, 4, 5)	Ex 2	22	(11, 5, 4, 5)	Ex 2
11	(7, 5, 6, 3)	PASS	23	(11, 5, 6, 3)	PASS
12	(7, 5, 6, 5)	PASS	24	(11, 5, 6, 5)	PASS

- We designed a voting system for different FCI approaches which further improve the performance at finding MFS in SUT.
- We conducted several empirical studies and showed that our strategy can assist FCI approaches to get better performance on identifying failure-inducing combinations in SUT with masking effects.

## 2. MOTIVATING EXAMPLE

This section constructed a small program example, for convenience to illustrate the motivation of our approach. Assume we have a method *foo* which has four input parameters: a, b, c, d. The types of these four parameters are all integers and the values that they can take are:  $v_a = \{7,11\}, v_b = \{2,4,5\}, v_c = \{4,6\}, v_d = \{3,5\}$ . The detail code of the method is listed in Figure 1.

Inspecting the simple code in Figure 1, we can find two potential faults: First, in the step 1 we can get an ArithmeticException when b is equal to c, i.e., b = 4 & c = 4, that makes division by zero. Second, another ArithmeticException will be triggered in step 2 when c < d, i.e., c = 4 & d = 5, which makes square roots of negative numbers. So the expected failure-inducing combinations in this example should be (-, 4, 4, -) and (-, -, 4, 5).

Traditional FCI algorithms do not consider the detail of the code, instead, they apply black-box testing to test this program, i.e., feed inputs to those programs and execute them to observe the result. The basic justification behind those approaches is that the failure-inducing combinations for a particular fault must only appear in those inputs that trigger this fault. As traditional FCI approaches aim at using as few inputs as possible to get the same or approximate result as exhaustive testing, so the results derived from a exhaustive testing set must be the best that these FCI approaches can reach. Next we will illustrate how exhaustive testing works on identifying the failure-inducing combinations in the program.

Table III. Identified failure-inducing combinations and their corresponding Exception

Failure-inducing combinations	Exception
(-, 4, 4, -)	Ex 1
(-, 2, 4, 5)	Ex 2
(-, 3, 4, 5)	Ex 2

We first generate every possible inputs listed in the Column "test inputs" of Table II, and their execution results are listed in Column "result" of Table II. In this Column, PASS means that the program runs without any exception under the input in the same row.  $Ex\ 1$  indicates that the program triggered an exception corresponding to the step 1 and  $Ex\ 2$  indicates the program triggered an exception corresponding to the step 2. According to data listed in table II, we can figure out that  $(-,\ 4,\ 4,\ -)$  must be the failure-inducing combination of  $Ex\ 1$  as all the inputs triggered  $Ex\ 1$  contain this combination. Similarly, the combination  $(-,\ 2,\ 4,\ 5)$  and  $(-,\ 3,\ 4,\ 5)$  must be the failure-inducing combinations of the  $Ex\ 2$ . We listed this three combinations and their corresponding exception in Table III.

Note that we didn't get the expected result with traditional FCI approaches in this case. The failure-inducing combinations we get for Ex 2 are (-,2,4,5) and (-,3,4,5) respectively instead of the expected combination (-,-,4,5). So why we failed in getting the (-,-,4,5)? The reason lies in *input 6*: (7,4,4,5) and *input 18*: (11,4,4,5). This two inputs contain the combination (-,-,4,5), but didn't trigger the Ex 2, instead, Ex 1 was triggered.

Now let us get back to the source code of *foo*, we can find that if Ex 1 is triggered, it will stop executing the remaining code and report the exception information. In another word, Ex 1 has a higher fault level than Ex 2 so that Ex 1 may mask Ex 2. Let us re-examine the combination (-,-,4,5): if we supposed that *input 6* and *input 18* should trigger Ex 2 if they didn't trigger Ex 1, then we can conclude that (-,-,4,5) should be the failure-inducing combination of the Ex 2, which is identical to the expected one.

However, we cannot validate the supposition, i.e., *input 6* and *input 18* should trigger Ex 2 if they didn't trigger Ex 1, unless we have fixed the code that trigger Ex 1 and then re-executed all the test cases. So in practice, when we do not have enough resource to re-execute all the test cases again and again or can only take black-box testing, the more economic and efficient approach to alleviate the masking effect on FCI approaches is desired.

## 3. FORMAL MODEL

This section presents some definitions and propositions to give a formal model for the FCI problem.

## 3.1. Failure-causing Schemas in CT

Assume that the SUT is influenced by n parameters, and each parameter  $p_i$  has  $a_i$  discrete values from the finite set  $V_i$ , i.e.,  $a_i = |V_i|$  (i = 1,2,...n). Some of the definitions below are originally defined in [Nie and Leung 2011b].

*Definition* 3.1. A *test case* of the SUT is an array of n values, one for each parameter of the SUT, which is denoted as a n-tuple  $(v_1, v_2,...,v_n)$ , where  $v_1 \in V_1, v_2 \in V_2 ... v_n \in V_n$ .

In practice, these parameters in the test case can represent many factors, such as input variables, run-time options, building options or various combination of them. We need to execute the SUT with these test cases to ensure the correctness of the behaviour of the software.

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We consider the fact that the abnormally executing test cases as a *fault*. It can be a thrown exception, compilation error, assertion failure or constraint violation. When faults are triggered by some test cases, what is desired is to figure out the cause of these faults, and hence some subsets of this test case should be analysed.

Definition 3.2. For the SUT, the *n*-tuple  $(-,v_{n_1},...,v_{n_k},...)$  is called a *k*-value *schema*  $(0 < k \le n)$  when some k parameters have fixed values and the others can take on their respective allowable values, represented as "-".

In effect a test case itself is a k-value schema, when k = n. Furthermore, if a test case contain a schema, i.e., every fixed value in the combination is in this test case, we say this test case hits the schema.

Definition 3.3. let  $c_l$  be a l-value schema,  $c_m$  be an m-value schema in SUT and l < m. If all the fixed parameter values in  $c_l$  are also in  $c_m$ , then  $c_m$  subsumes  $c_l$ . In this case we can also say that  $c_l$  is a sub-schema of  $c_m$  and  $c_m$  is a parent-schema of  $c_l$ , which can be denoted as  $c_l \prec c_m$ .

For example, in the motivation example section, the 2-value schema (-, 4, 4, -) is a sub-schema of the 3-value schema (-, 4, 4, 5), that is,  $(-,4,4,-) \prec (-,4,4,5)$ .

Definition 3.4. If all test cases contain a schema, say c, trigger a particular fault, say F, then we call this schema c the failure-causing schema for F. Additionally, if none sub-schema of c is the faulty schema for F, we then call the combination c the Minimal Failure-causing Schema, i.e., (MFS) for F.

In fact, MFS is identical to the failure-inducing combinations we discussed previously. Figuring it out can eliminate all details that are irrelevant for causing the failure and hence facilitate the debugging efforts.

Let  $c_m$  be a m-value schema, we denote the set of all the test cases can hit the schema  $c_m$  as  $T(c_m)$ . Further, for the test case t, let  $\mathcal{I}(t)$  to denote the set of all the schemas that are hit by t, and for the set of test cases T, we let  $\mathcal{I}(T) = \bigcup_{t \in T} \mathcal{I}(t)$ . Then we have the following propositions.

PROPOSITION 3.5. if  $c_l \prec c_k$ , then  $T(c_k) \subset T(c_l)$ 

PROOF. Suppose  $\forall t \in T(c_k)$ , we have that t hits  $c_k$ . Then as  $c_l \prec c_k$ , so t must also hit  $c_l$ , as all the element in  $c_l$  must in  $c_k$ , which also in the test case t. Therefore we get  $t \in T(c_l)$ . Thus  $t \in T(c_k)$  implies  $t \in T(c_l)$ , so it follows that  $T(c_k) \subset T(c_l)$ .  $\square$ 

Table IV illustrates an example of SUT with four binary parameters (Unless otherwise specified, following examples also assume the SUT with binary parameters). The left column lists the schema (0,0,-,-) as well as all the test cases hit this schema, while the right column lists the test cases for schema(0,-,-,-). We can observe that (0,-,-,-) (0,0,-,-) and the the set of test cases which hit (0,-,-,-) contains the set that hits (0,0,-,-).

Proposition 3.6.

For any set T of test cases of a SUT, we can always get a set of minimal schemas  $C(T) = \{c \mid \exists c' \in C(T), s.t.c' \prec c\}$ , such that,

$$T = \bigcup_{c \in \mathcal{C}(T)} T(c)$$

PROOF. We prove by producing this set of schemas.

We denote the exhaustive test cases for SUT as  $T^*$ . And let  $T^* \setminus T$  be the test cases that in  $T^*$  but not in T. It is obviously  $\forall t \in T$ , we can always find at least one schema

Table IV. Example of the propo-

	c
	(0, -, - , -)
c	T(c)
(0, 0, -, -)	(0, 0, 0, 0)
T(c)	(0, 0, 0, 1)
(0, 0, 0, 0)	(0, 0, 1, 0)
(0, 0, 0, 1)	(0, 0, 1, 1)
(0, 0, 1, 0)	(0, 1, 0, 0)
(0, 0, 1, 1)	(0, 1, 0, 1)
	(0, 1, 1, 0)
	(0, 1, 1, 1)

Table V. Example of the minimal schemas

T	S(T)	C(T)
(0, 0, 0, 0)	(0, 0, 0, 0)	(0, 0, 0, -)
(0, 0, 0, 1)	(0, 0, 0, 1)	(0, 0, -, 0)
(0, 0, 1, 0)	(0, 0, 1, 0)	
	(0, 0, 0, -)	
	(0, 0, -, 0)	

 $c \in \mathcal{I}(t)$ , such that  $c \notin \mathcal{I}(T^* \setminus T)$ . Specifically, at least the test case t itself as schema

Then we collect all the satisfied schemas( $c \in \mathcal{I}(t)$  and  $c \notin \mathcal{I}(T^* \setminus T)$ ) in each test case

t of T, which can be denoted as:  $S(T) = \{\mathcal{I}(T) - \mathcal{I}(T^* \backslash T)\}$ . For the set S(T), we can have  $\bigcup_{c \in S(T)} T(c) = T$ . This is because first, for  $\forall t \in T$  $T(c), (T(c) \subset \bigcup_{c \in S(T)} T(c)).$  it must have  $t \in T$ , as if not so, then  $t \in T^* \backslash T$ , which contradict with the definition of S(T). So  $t \in T$ . Hence,  $\bigcup_{c \in S(T)} T(c) \subset T$ .

Then second, for any test case t in T, as we have learned at least find one c in  $\mathcal{I}(t)$ , such that c in S(T). Then for  $T(c) \subset \bigcup_{c \in S(T)} T(c)$  and  $t \in T(c)$ , so  $t \in \bigcup_{c \in S(T)} T(c)$ , therefore,  $T \subset \bigcup_{c \in S(T)} T(c)$ .

Since  $\bigcup_{c \in S(T)} T(c) \subset T$  and  $T \subset \bigcup_{c \in S(T)} T(c)$ , so it follows  $\bigcup_{c \in S(T)} T(c) = T$ .

Then we denote the minimal schemas of S(T) as  $M(S(T)) = \{c | c \in S(T) \text{ and } \exists c' \prec T\}$  $c, s.t., c' \in S(T)$ }. For this set, we can still have  $\bigcup_{c \in M(S(T))} T(c) = T$ . We also prove this by two steps, first and obviously,  $\bigcup_{c \in M(S(T))} T(c) \subset \bigcup_{c \in S(T)} T(c)$ . Then we just need to prove that  $\bigcup_{c \in S(T)} T(c) \subset \bigcup_{c \in M(S(T))} T(c)$ .

In fact by definition of M(S(T)), for  $\forall c' \in S(T) \backslash M(S(T))$ , we can have some  $c \in$ M(S(T)), such that  $c \prec c'$ . According to the Proposition 1,  $T(c') \subset T(c)$ . So for any test case  $t \in \bigcup_{c \in S(T)} T(c)$ , as we have either  $\exists c' \in S(T) \setminus M(S(T)), s.t., t \in T(c')$  or  $\exists c \in S(T) \setminus M(S(T)), s.t., t \in T(C')$  $M(S(T)), s.t., t \in T(c)$ . Both cases can deduce  $t \in \bigcup_{c \in M(S(T))} T(c)$ . So,  $\bigcup_{c \in S(T)} T(c) \subset T(c)$  $\bigcup_{c \in M(S(T))} T(c).$ 

Hence,  $\bigcup_{c \in S(T)} T(c) = \bigcup_{c \in M(S(T))} T(c)$ , and M(S(T)) is the set of schemas that holds this proposition.  $\Box$ 

For example, table V lists the S(T) and minimal schemas C(T) for set of test cases T. We can see that for any other schemas not in  $\mathcal{C}(T)$ , either can we find a test case not in T hit the schema, e.g.,(0,0,-,-) with the test case (0,0,1,1) not in T, or is the parent schema of one of this two minimal schemas, e.g., (0,0,0,0) the parent schema of both (0,0,0,-) and (0,0,-,0).

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Let  $\mathcal{C}(T_{F_m})$  denotes the set of all the test cases triggering fault  $F_m$ , then  $\mathcal{C}(T_{F_m})$  actually is the set of MFS of  $F_m$  by definition of MFS. And obviously for  $\forall c_m$  we have  $\mathcal{C}(T(c_m)) = \{c_m\}$ .

From the construction process of  $\mathcal{C}(T)$ , one observation is that the schemas in S(T) either belongs to  $\mathcal{C}(T)$ , or be the parent schema of one element of  $\mathcal{C}(T)$ . Then we can have the following proposition.

**PROPOSITION** 3.7. For any  $T(c) \subset T$ , then it must be that  $c \in S(T)$ .

PROOF. We first have  $\mathcal{C}(T(c)) = \{c\}$ , and  $\mathcal{C}(T(c)) \subset S(T(c))$ . Then as  $T(c) \subset T$ , it follows  $S(T(c)) \subset S(T)$  by definition. So we can have  $\mathcal{C}(T(c)) \subset S(T)$  and hence  $c \in S(T)$ .  $\square$ 

For two different set of test cases, there exist some relationships between the minimal schemas of these two set, which varies in the relevancy between this two different set of test cases. In fact, there are three possible associations between two different set of test cases: *inclusion*, *disjoint*, and *intersection* as listed in figure 2. We didn't list the condition that two set that are identical, because on that condition the minimal schemas must also be identical. To discuss the properties of the relationship of the minimal schemas between two different set of test cases is important as we can learn later the masking effects between multiple faults will make the MFS identifying process incorrectly works, i.e., these FCI approaches may isolate the minimal schemas for the set of test cases which are biased from the expected failing set of test cases. And these properties can help us to figure out the impact of masking effects on the FCI approaches. Next we will separately discuss the relationship between minimal schemas under the three conditions.

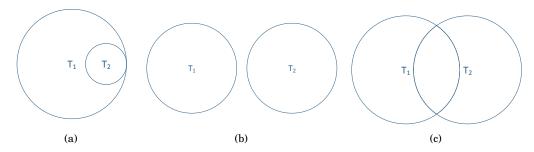


Fig. 2. Test Suites relationship

### 3.2. Inclusion

It is the first relationship corresponding to Fig. 2(a). We can have the following proposition with two set of test cases which have the inclusion relationship.

PROPOSITION 3.8. For two set of test cases  $T_l$  and  $T_k$ , assume that  $T_l \subset T_k$ . Then we have

$$\forall c_l \in \mathcal{C}(T_l) \ either \ c_l \in \mathcal{C}(T_k) \ or \exists c_k \in \mathcal{C}(T_k), s.t., c_k \prec c_l.$$

PROOF. Obviously for  $\forall c_l \in \mathcal{C}(T_l)$  we can get  $T(c_l) \subset T_l \subset T_k$ . According to the proposition 3, we can have  $c_l \in S(T_k)$ . So this proposition holds as the schema in  $S(T_k)$  either is also in  $\mathcal{C}(T_k)$ , or must be the parent of some schemas in  $\mathcal{C}(T_k)$ .  $\square$ 

Table VI. Example of the scenarios

			$T_l$	$T_k$
$T_l$	$T_k$	_	(0, 0, 0)	(0, 0, 0)
(0, 0, 0)	(0, 0, 0)		(0, 0, 1)	(0, 0, 1)
(0, 0, 1)	(0, 0, 1)		(0, 1, 0)	(0, 1, 0)
(0, 1, 0)	(0, 1, 0)			(1, 1, 0)
	(0, 1, 1)			(1, 1, 1)
$C(T_l)$	$C(T_k)$	_	$C(T_l)$	$C(T_k)$
(0, 0, -)	(0, -, -)	_	(0, 0, -)	(0, 0, -)
(0, -, 0)			(0, -, 0)	(0, -, 0)
		•		(1, 1, -)

Table VII. Example of disjoint examples

$T_l$	$T_k$
(0, 0, 0)	(1, 0, 0)
(0, 1, 0)	(1, 0, 1)
	(1, 1, 0)
$C(T_l)$	$C(T_k)$
(0, -, 0)	(1, 0, -)
	(1, -, 0)

Based on this proposition, in fact, the  $c_k \in \mathcal{C}(T_k)$  remains the following three possibilities: 1)  $c_k \in \mathcal{C}(T_l)$ , or 2)  $\exists c_l \in \mathcal{C}(T_l), s.t., \ c_k \prec c_l, \ \text{or 3}) \ \not\exists c_l \in \mathcal{C}(T_l), s.t., c_k \prec c_l \ \text{or } c_k = c_l, \ \text{or } c_l \prec c_k.$  For the third case, we call  $c_k$  is *irrelevant* to  $\mathcal{C}(T_l)$ 

We illustrate these scenarios in Table VI. There are two parts in this table, each part shows two set of test cases:  $T_l$  and  $T_k$ , which have  $T_l \subset T_k$ . For the left part, we can see that the schema in  $\mathcal{C}(T_l)$ : (0, 0, -) and (0, -, 0), both are the parent of the schema of the one in  $\mathcal{C}(T_k)$ : (0, -, -). While for the right part, the schemas in  $\mathcal{C}(T_l)$ : (0, 0, -) and (0, -, 0) are both also in  $\mathcal{C}(T_k)$ . Furthermore, one schema in  $\mathcal{C}(T_k)$ : (1, 1, -) is irrelevant to  $\mathcal{C}(T_l)$ .

## 3.3. Disjoint

This relationship is corresponding to the Fig.2(b), For two different set of test cases, one obvious properties is listed as follows:

**PROPOSITION 3.9.** For two set  $T_1, T_2$ , if  $T_1 \cap T_2 = \emptyset$ , we have,  $S(T_1) \cap S(T_2) = \emptyset$ .

PROOF. If  $S(T_1) \cap S(T_2) \neq \emptyset$ . Without loss of generality, we let  $c \in S(T_1) \cap S(T_2)$  we can learn that T(c) must both in  $T_1$  and  $T_2$ , which is contradiction.  $\Box$ 

This properties tells that the minimal schemas of two disjoint test cases should be irrelevant to each other, Table VII list the example of this scenario, we can learn in this table that for two different test cases set  $T_l, T_k$ , their minimal schemas, i.e., (0, -, 0) and (1, 0, -), (1, -, 0) respectively, are irrelevant to each other.

## 3.4. Intersect

This relationship is corresponding to the Fig.2(c). This scenario is the most common scenario for two set of test cases, but also the most complicated scenario for analysis. For convenience to illustrate the properties of the minimal schemas of this scenario, we assume without of loss of generality that  $T_1 \cap T_2 = T_3$  as depicted in Fig.2(c). Then we can have the following properties:

PROPOSITION 3.10. It must have  $\exists c_1 \in \mathcal{C}(T_1) \text{ and } c_2 \in \mathcal{C}(T_2)$ . s.t.  $c_1$  and  $c_2$  are irrelevant

PROOF. Firstly, we can learn that  $C(T_1 - T_3)$  are irrelevant to  $C(T_2 - T_3)$ , as  $(T_1 - T_3) \cap (T_2 - T_3) = \emptyset$ .

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Table VIII. Example of Intersect by irrelevant examples

$T_1$	$T_2$
(1, 0, 0)	(1, 0, 0)
(1, 0, 1)	(1, 1, 0)
$\mathcal{C}(T_1)$	$C(T_2)$
(1, 0, -)	(1, -, 0)

Table IX. Example of Intersect by identical examples

$T_1$	$T_2$	$T_3$
(0, 1, 0)	(0, 0, 0)	(1, 1, 0)
(1, 1, 0)	(0, 0, 1)	(1, 1, 1)
(1, 1, 1)	(1, 1, 0)	
	(1, 1, 1)	
$C(T_1)$	$C(T_2)$	$C(T_3)$
(-, 1, 0)	(0, 0, -)	(1, 1, -)
(1, 1, -)	(1, 1, -)	

As  $C(T_1 - T_3)$  is either identical to some schemas in  $C(T_1)$  or be parent schemas of them. If some of them are identical, then these identical ones must be irrelevant to  $C(T_2)$  as  $T_1 - T_3 \cap T_2 = \emptyset$ . This is also holds if  $C(T_2 - T_3)$  is identical to some schemas in  $C(T_2)$ .

Next, if both  $\mathcal{C}(T_1-T_3)$  and  $\mathcal{C}(T_2-T_3)$  are parent schemas of some of  $\mathcal{C}(T_1)$  and  $\mathcal{C}(T_2)$  respectively, without loss of generality, we make  $c_{1-3} \prec c_1$ ,  $(c_{1-3} \in \mathcal{C}(T_1-T_3) \ and \ c_1 \in \mathcal{C}(T_1))$  and  $c_{2-3} \prec c_2$ ,  $(c_{2-3} \in \mathcal{C}(T_2-T_3) \ and \ c_2 \in \mathcal{C}(T_2))$ . Then these corresponding subschemas in  $\mathcal{C}(T_1)$  and  $\mathcal{C}(T_2)$ , i.e.,  $c_1$  and  $c_2$  respectively, must also be irrelevant to each other. This is because  $T(c_1) \supset T(c_{1-3})$  and  $T(c_2) \supset T(c_{1-3})$ . And as  $T(c_{1-3}) \cap T(c_{2-3}) = \emptyset$  So  $T(c_1)$  and  $T(c_2)$  are neither identical nor subsuming each other.  $\square$ 

For example, Table VIII shows two test cases interact each other at test case (1,0,0), but their minimal schemas, (1,0,-) and (1,-,0) respectively, are irrelevant to each other.

PROPOSITION 3.11. If there we can find  $\exists c_1 \in \mathcal{C}(T_1) \text{ and } c_2 \in \mathcal{C}(T_2)$ , s.t.,  $c_1$  is identical to  $c_2$ , Then it must have  $c_1 = c_2 \in \mathcal{C}(T_3)$ 

PROOF. As we get that the identical schema must share the identical test cases, then the only identical test cases between  $T_1$  and  $T_2$  is  $T_1 \cap T_2 = T_3$ . So the only possible identical schemas between  $\mathcal{C}(T_1)$  and  $\mathcal{C}(T_2)$  is in  $\mathcal{C}(T_3)$ .  $\square$ 

We must know that this proposition holds when some schemas in  $C(T_3)$  is identical some schemas in  $C(T_1)$  and  $C(T_2)$ .

For example, Table IX shows two test cases interact each other at test cases (1,1,0) and (1,1,1), and they have identical minimal schemas, i.e., (1,1,-), which is also the minimal schema in  $\mathcal{C}(T_3)$ .

PROPOSITION 3.12. If there we can find  $\exists c_1 \in \mathcal{C}(T_1) \text{ and } c_2 \in \mathcal{C}(T_2)$ , s.t.,  $c_1$  is parent-schema of  $c_2$ , Then it must have  $c_1 \in \mathcal{C}(T_3)$ . (and vice versa).

PROOF. We have proved previously if two schemas have have subsumes relationship, then their test cases must also have inclusion relationship. And as the only inclusion relationship between  $T_1$  and  $T_2$  is that  $T_1 \subset T_3$  and  $T_2 \subset T_3$ . So the parent schemas must be in  $\mathcal{C}(T_3)$ .  $\square$ 

It is noted that this proposition holds when holds when some schema in  $C(T_3)$  is identical in  $C(T_1)$  (or  $C(T_2)$ ), and simultaneously the same schemas in  $C(T_3)$  must be

Table X. Example of Intersect by subsume examples

$T_1$	$T_2$	$T_3$
(0, 1, 0)	(0, 0, 0)	(1, 0, 0)
(1, 0, 0)	(1, 0, 0)	(1, 0, 1)
(1, 0, 1)	(1, 0, 1)	(1, 1, 0)
(1, 1, 0)	(1, 1, 0)	
	(1, 1, 1)	
$C(T_1)$	$C(T_2)$	$C(T_3)$
(-, 1, 0)	(-, 0, 0)	(1, 0, -)
(1, 0, -)	(1, -, -)	(1, -, 0)
(1, -, 0)		

the parent-schema of the minimal schemas of another set of test cases, i.e.,  $\mathcal{C}(T_2)$  (or  $\mathcal{C}(T_1)$ ).

Table X illustrates this scenario, in which, the minimal schemas of  $T_1$ : (1,0,-),(1,-,0), which is also the schemas in  $\mathcal{C}(T_3)$ , is the parent schema of the minimal schema of

It is noted that this three condition can simultaneously appears when two set of test cases interest with each other.

## 3.5. Identify the MFS

According to these analysis, we can get that  $\mathcal{C}(T_{F_m})$  actually is the set of failure-causing schemas of  $F_m$ . Then in theory, if we want to accurately figure out the MFS in SUT, we need to exhaustively execute each possible test case, and collect the failing test cases  $T_{F_m}$ . This is impossible in practice especially when the testing space is too large.

So for traditional FCI approaches, they need to select the subset of the exhaustive test cases, and then either take some assumption to make prediction of the remaining test cases or just give a suspicious rank. As giving a suspicious rank can also be regard as a special case of making prediction(with computing the possibility), so we next only formally describe the mechanism of FCI approaches belong to the first type. We refer the observed failing test case to  $T_{fail_{observed}}$ , and refer the remaining test cases the approach predict to be failed as  $T_{fail_{predicted}}$ . We also denote the actually entire failing test cases as  $T_{fail}$ . Then the MFS identified by FCI approaches can be depicted as:

MFS =  $\mathcal{C}(T_{fail_{observed}} \bigcup T_{fail_{predicted}})$ . For each FCI approach, the way it predict the  $T_{fail_{predicted}}$  according to observed failing test cases varies, further more, as the test cases it generates is different, the failing test cases observed by different test cases, i.e.,  $T_{fail_{observed}}$  also varies. We take an example using OFOT approach to illustrate this formula.

Suppose SUT has 3 parameters, each can take 2 values. And assume the test case (1, 1, 1) failed. Then we can describe the FCI process as Table XI. In this table, test case t failed, and OFOT mutated one factor of the t one time to generate new test cases:  $t_1 - t_3$ , It found the the  $t_1$  passed, which indicates that this test case break the MFS in the original test case t. So the (1,-,-) should be one failure-causing factor, and as other mutating process all failed, which means no other failure-inducing factors were broken, therefore, the MFS in t is (1,-,-).

Now let us explain this process with our formal model. Obviously the  $T_{fail_{obs}}$ is  $\{(1,1,1),(1,0,1),(1,1,0)\}$ . And as having found (0,-,-) broke the MFS, hence by OFOT theory, all the test cases contain (0,-,-) should pass the test cases (This conclusion is built on the assumption that SUT just contain one failure-causing schema). As a result, (0,1,1), (0,0,1), (0,1,0), (0,0,0) should pass the testing. Further, as obviously the test case either passes or fails the testing (we label the skip the testing as a special case of failing), so the remaining test case(1,0,0), will be predicted as failing, i.e., 39:12 X. Niu et al.



Fig. 3. generally modeling of FCI

 $T_{fail_{predicted}}$  is  $\{(1,0,0)\}$ . Taking together, the MFS using OFOT strategy can be described as:  $\mathcal{C}(T_{fail_{observed}}\bigcup T_{fail_{predicted}}) = \mathcal{C}(\{(1,1,1),(1,0,1),(1,1,0),(1,0,0)\}) = (1,-,-),$  which is identical to the one it got previously.

Table XI. OFOT with our strategy

ori	gina	l te	Outcome				
t	1	1	1	Fail			
	observed						
$t_1$	0	1	1	Pass			
$t_2$	1	0	1	Fail			
$t_3$	1	1	0	Fail			
	pre	dict	ed				
$t_4$	0	0	1	Pass			
$t_5$	0	1	0	Pass			
$t_6$	1	0	0	Fail			
$t_7$	0	0	0	Pass			

Similarly, other FCI approaches can also be modeled into this formal description. We will not in detail discuss how to model each FCI approach as this is not the point of this paper. It is noted that the test cases FCI predict to be failing is not always identical to the actually failing test cases. In fact, we can generally depict the process of FCI approaches like Fig. 3.

We can see in this figure, area A denotes the test cases that should be passing ones while it predicted to be failing, area B depicts the test cases that the approach observed to be failing test cases, area C refers to the failing test cases that doesn't to be observed but be predicted to be failing test cases and area D illustrates the failing test cases that neither to be observed nor to be predicted. This figure is actually one sample of the condition that two set of test cases interest with each other, in specific, area  $A \cup B \cup C = T_1$ , area  $D \cup B \cup C = T_2$  and area  $B \cup C = T_3$ .

We learned previously this scenario makes the schemas identified in  $T_1$  biased from the expected MFS in  $T_2$ , in specific, their must be irrelevant schemas between  $\mathcal{C}(T_1)$  and  $\mathcal{C}(T_2)$ , which means that FCI approach will identify some minimal schemas that is irrelevant to actual MFS, and must ignore some actual MFS. Moreover, under the appropriate condition list in proposition 3.11 and 3.12, FCI may identify the identical schemas or parent-schema or sub-schema of the actual MFS. So in order to identify the schemas as accurate as possible, the FCI approach needs to make  $T_1$  as similar as possible to  $T_2$ , specifically, makes area B and area C as large as possible, and make area A as small as possible.

However, even though each FCI approach tries its best to identify the MFS as accurate as possible, masking effects raised from test cases will make their efforts in vain. We next will discusses the masking problem and how it affect the FCI approaches.

## 4. MASKING EFFECT

Definition 4.1. A masking effect is the effect that while a test case t hit a MFS for a particular fault, however, t didn't trigger the expected fault because other fault was triggered ahead which prevents t to be normally checked.

Taking the masking effects into account, when identifying the MFS for a specific fault, say,  $F_m$ , we should not ignore these test cases which should have triggered  $F_m$  if they didn't trigger other faults. We call these test cases  $T_{mask(F_m)}$ . Hence, the MFS for fault  $F_m$  should be  $\mathcal{C}(T_{F_m} \bigcup T_{mask(F_m)})$ 

As an example, in the motivation example in section 2, the  $F_{mask(F_{Ex~2})}$  is  $\{(7,4,4,5),(11,4,4,5)\}$ , So the MFS for Ex2 is  $\mathcal{C}(T_{F_{Ex~2}} \bigcup T_{mask(F_{Ex~2})})$ , which is (-,-,4,5). In practice with masking effects, however, it is not possible to correctly identifying

In practice with masking effects, however, it is not possible to correctly identifying the MFS, unless we fix some bugs in the SUT and re-execute the test cases to figure out  $T_{mask(F_m)}$ .

out  $T_{mask(F_m)}$ . In effect for traditional FCI approaches, without the knowledge of  $T_{mask(F_m)}$ , only two strategies can be adopted when facing the multiple faults problem. We will separately analyse the two strategies under exhaustive testing condition and normal FCI testing condition.

## 4.1. masking effects for exhaustive testing

4.1.1. Regard as one fault. The first one is the most common strategy, it doesn't distinguish the faults, i.e., regard all the types of faults as one fault-failure, others as pass.

With this strategy, The minimal schemas we identify are the set  $\mathcal{C}(\bigcup_{i=1}^L T_{F_i})$ , L is the number of all the faults in the SUT. Obviously,  $T_{F_m} \bigcup T_{mask(F_m)} \subset \bigcup_{i=1}^L T_{F_i}$ . So in this case, by Proposition 3.8, some schemas we get may be the sub-schemas of some of the actual MFS, or irrelevant to the actual MFS.

As an example, consider the test cases in Table XII. In this example, assume we need to characterize the MFS for error 1, all the test cases that triggered error 1 is listed in the column  $T_1$ , similarly, we list the test cases that triggered other fault in column  $T_{mask(1)}$  and  $T_*$  respectively, in which the former masked the error 1 while the latter not. Actually the MFS for error 1 should be (1,1,-,-) and (-,1,1,1) as we listed them in the column actual MFS for 1. However, when we take regard as one fault strategy, the minimal schemas we got will be (-,-,0,0), (1,1,-,-), (-,-,1,1), in which the (-,-,0,0) is irrelevant to the actual MFS for error 1 and the (-,-,1,1) is the sub-schema of the actual MFS (-,1,1,1).

4.1.2. Distinguish faults. Distinguishing the faults by the exception traces or error code can help make the MFS related to particular fault. Yilmaz in [Yilmaz et al. 2013]

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	•	J
$T_1$	$T_{mask(1)}$	$T_*$
(1, 1, 1, 1)	(1, 1, 0, 0)	(0, 1, 0, 0)
(1, 1, 1, 0)	(0, 1, 1, 1)	(0, 0, 0, 0)
(1, 1, 0, 1)		(1, 0, 0, 0)
		(1, 0, 1, 1)
		(0, 0, 1, 1)
actual MFS for 1	regard as one fault	distinguish faults
$C(T_1 \bigcup T_{mask(1)})$	$\mathcal{C}(T_1 \bigcup T_{mask(1)} \bigcup T_*)$	$\mathcal{C}(T_1)$
(1, 1, -, -)	(-, -, 0, 0)	(1, 1, -, 1)
(-, 1, 1, 1)	(1, 1, -, -)	(1, 1, 1, -)
	(-, -, 1, 1)	

Table XII. masking effects for exhaustive testing

proposed the *multiple-class* failure characterizing method instead of *ternary-class* approach to make the characterizing process more accurately. Besides, other approaches can also be easily extended with this strategy to be applied on SUT with multiple faults.

This strategy focus identifying the set of  $\mathcal{C}(T_{F_m})$ , and as  $T_{F_m} \bigcup T_{mask(F_m)} \supset T_{F_m}$ , consequently, some schemas get through this strategy may be the parent-schema of some MFS. Moreover, some MFS may be irrelevant to the schemas get with this strategy, which means this strategy will ignore these MFS.

For the simple example in Table XII, when we using this strategy, we will get the minimal schemas (1, 1, -, 1) and (1, 1, 1, -), which are both the parent schemas of actual MFS (1,1,-,-), and we will observe that there is no schemas got by this strategy have any relationship with the actual MFS (-,1,1,1), which means it ignored the schema.

It is noted that, motivation example in section 2 actually adopted this strategy, which made the schemas identified for Ex 2: (-,2,4,5), (-,3,4,5) are the parent-schemas of the correct MFS(-,-,4,5).

## 4.2. masking effects for FCI approaches

With masking effects, the scenario of traditional FCI approaches is a bit complicated than previous two exhaustive testing scenario, which can be depicted in the Figure 4. In this figure, area A, C and D is the same as Figure 3, area B is divided into three subareas, in which  $B_1$  is still the observed failing test cases for the current analysed fault, area  $B_2$  is the test cases triggered other fault which masked the current fault and area  $B_3$  is the test cases triggered other fault which did not mask the current fault.

With this model, if we have known which test cases mask the expect fault, i.e., figured out the B2 and B3, then the schemas FCI approach will identify can be described as  $\mathcal{C}(A \bigcup B_1 \bigcup B_2 \bigcup C)$ . We next denote this result as *knowing masking effects*. However, as we discussed before, to get this result is not possible without human involvement. Correspondingly, when taking *regard as one fault* strategy, the MFS traditional FCI identify are  $\mathcal{C}(A \bigcup B_1 \bigcup B_2 \bigcup B_3 \bigcup C)$ . And for *distinguish faults* strategy, the MFS is  $\mathcal{C}(A \bigcup B_1 \bigcup C)$ . Next, we will respectively discuss the influence of masking effects on the two strategies.

4.2.1. Taking regard as one fault strategy. For the first strategy: regard as one fault, the impact of masking effects on FCI approaches can be described as Figure 5. To understand the content of this figure, let us get back to the relationship between the minimal schemas of two different set of test cases. For the knowing masking effects condition, the result identified by FCI approach, i.e.,  $C(A \bigcup B_1 \bigcup B_2 \bigcup C)$ , is one case of the intersect scenario. It means that the minimal schemas get in this condition can be identical, parent-schema, sub-schema, irrelevant to the actual MFS. And then apply the regard as one fault, the minimal schemas we got are  $C(A \bigcup B_1 \bigcup B_2 \bigcup B_3 \bigcup C)$ . Obviously we have  $A \bigcup B_1 \bigcup B_2 \bigcup B_3 \bigcup C \supset A \bigcup B_1 \bigcup B_2 \bigcup C$ . So the minimal schema get by this s-

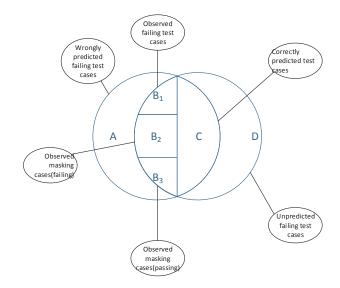


Fig. 4. FCI with masking effects

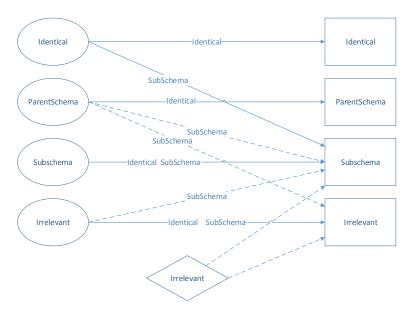


Fig. 5. masking effects influence on FCI with regard as one fault

trategy is either the sub-schema or identical to some schemas from the ones got by *known masking effects*, or exist some schemas irrelevant to all of them. Taking this two properties together, we will get Figure 5.

The ellipses in the left column of this figure illustrated the relation between the schemas identified under the *knowing masking effects* condition with the actual MFS, which includes the four possibilities: identical, sub-schema, parent-schema and irrelevant. For each relationship in this part, without of loss of generality, we consider  $c_{origin}$  and  $c_m$ ,  $c_{origin}$  is the minima schema got by *knowing masking effects*, and  $c_m$  is

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the actual MFS. Then when we apply regard as one fault strategy, we may get some schemas which are identical or sub-schema of  $c_{origin}$ , say  $c_{new}$  s.t.,  $c_{new} = c_{origin}$  or  $c_{new} \prec c_{origin}$ . In this figure, we use the directed line to represent this two transformations with different labels in each line. As for the schemas  $c_{new}$  that is irrelevant to all the  $c_{origin}$ , we in the bottom of this figure use a rhombus labeled with "Irrelevant" to express them. Then we must have some relationship between the  $c_{new}$  and actual MFS, which also have four possibilities represented as rectangles in the right column.

Note that there exists two types of directed line, solid line and dashed line, in which the former indicates that this transformation is deterministic, e.g., if  $c_{origin} \prec c_m$  and  $c_{new} \prec c_{origin}$ , then we must have  $c_{new} \prec c_m$ . The latter type means the transformation is just one of all the possibilities in such condition, e.g., if  $c_{origin}$  irrelevant  $c_m$  and  $c_{new} \prec c_{origin}$ , then we can have either  $\exists c_{m'}$  is one actual MFS, s.t. $c_{new} \prec c_m$  or  $c_{new}$  irrelevant to all actual MFS. (We will later give examples to illustrate them).

In this figure, only two transformation can make  $\exists c_{m'}$  is one actual MFS, s.t.  $c_{new} = c_{m'}$  or  $c_{m'} \prec c_{new}$ , which are when  $c_{origin} = c_m$ ,  $c_{new} = c_{origin}$  or  $c_m \prec c_{origin}$ ,  $c_{new} = c_{origin}$  respectively. This can be easily understood, as to make  $c_{new} = c_{m'}$  or  $c_{m'} \prec c_{new}$ , according to the proposition 3.11 and 3.12, it must have  $T(c_{new}) \subset (B_1 \bigcup B_2)$ . If after transformation, we got  $c_{new} \prec c_{origin}$ , then we must have  $\exists t \in B_3, s.t., t \in T(c_{new})$ , otherwise, there should have no changing to the  $c_{origin}$ , and must have no newly schema  $c_{new}$  that is the sub-schema of  $c_{origin}$ . Consequently,  $T(c_{new}) \not\subset (B_1 \bigcup B_2)$  if we have  $c_{new} \prec c_{origin}$ . So in order to make e  $c_{new} = c_{m'}$  or  $c_{m'} \prec c_{new}$ , the transformation can only be identical, i.e.,  $c_{new} = c_{origin}$  and must have  $c_{origin} = c_m$  or  $c_m \prec c_{origin}$  correspondingly.

As the identical transformation is simple, so next we will ignore them and just take examples to illustrate the other transformations. Table XIII presents all these possibilities except these identical transformation. This table comprises of three parts, which the upper part give the test cases for each area in the abstract FCI model. It is noted that we merged the area  $B_1$ ,  $B_2$  and C into one column as the way of computing the minimal schemas of three approaches - actual MFS, knowing masking effects, regard as one fault are all dependent on the merging test cases of this three area, not on the specific distribution of them. The middle part of this table shows the minimal schemas that using particular method. At last the bellow part in specific depicts the sample of each possible result of the transformation in the Figure 5. In this part,  $c_m = c_{origin} \rightarrow c_{new} \prec c_{m'}$  indicates the scenario that the schema  $c_{origin}$  got by knowing masking effects is identical to one actual MFS  $c_m$ , then taking regard as one fault, we got  $c_{new} \prec c_{origin}$ , and such that we can have  $\exists c_{m'}$  is one actual MFS, s.t.,  $c_{new} \prec c_m$ . Other formula in this column can be explained in this way, in which  $c_{new}$  irrele and  $c_{origin}\ irrele$  means the schema  $c_{new}$  and  $c_{origin}$  is irrelevant to all the actual MFS respectively. The mark \* in  $c_m$  and  $c_{m'}$  respectively represent this two condition. The formula in the last two rows,  $c_{new_{irrele}} \prec c_{m'}$  and  $c_{new_{irrele}irrele}$  indicate the schemas  $c_{new_{irrele}}$  got by regard as one fault is irrelevant to all the  $c_{origin}$ , in which the former is the subschema of some actual MFS  $c_{m'}$  while the latter is irrelevant to all the actual MFS. The \* in the  $c_{origin}$  column means that the  $c_{new}$  is irrelevant to all the  $c_{origin}$ .

4.2.2. using distinguish strategy. And for the second strategy: distinguish faults, the influence can be described as Figure 6.

This figure is organised the same way as figure 5. As with distinguish faults strategy, the minimal schemas identified are actually  $\mathcal{C}(A \bigcup B_1 \bigcup C)$ . Obviously  $A \bigcup B_1 \bigcup C \subset A \bigcup B_1 \bigcup B_2 \bigcup C$ . So under this transformation, the  $c_{new}$  should be either parent-schema or identical to the  $c_{origin}$ .

 $B_1 \bigcup B_2 \bigcup C$ (1,0,1,0,0,0)(0,0,0,1,0,0)(1,1,1,0,0,0)(1,1,0,0,0,0)(0,0,0,1,1,0)(1,1,1,0,1,0)(1,0,1,0,1,0)(1,1,0,0,1,0)(0,0,1,0,0,0)(1,1,1,1,0,0)(0,0,1,0,1,0)(1,1,0,1,0,0)(0,0,1,1,0,0)(1,1,1,1,1,0)(0,0,1,1,1,0)(1,1,0,1,1,0)(1,0,1,1,0,0)(0,1,0,0,0,0)(0,0,1,1,0,1)(1,0,1,1,1,0)(0,1,0,1,0,0)(0,1,1,1,0,1)(0,0,0,0,1,0)(0,1,1,0,0,0)(0,0,0,0,0,0)(0,1,1,1,0,0)(0,0,1,1,1,1)(1,0,0,0,0,0)(1,0,0,0,1,0)(0,1,1,1,1,1)(1,1,1,1,1,1)(1,0,1,1,1,1)actual MFS  $knowing\ masking\ effects$ one fault  $\mathcal{C}(B_1 \bigcup B_2 \bigcup C \bigcup D)$  $\mathcal{C}(A\bigcup B_1 \bigcup B_2 \bigcup C)$  $C(A \bigcup B_1 \bigcup B_2 \bigcup B_3 \bigcup C)$ (1,1,1,-,-,0)(1,1,-,-,0)(1,-,1,-,-,0)(1,-,1,1,-,0)(0,0,-,-,0) (1,-,1,1,-,0)(0,0,0,-,-,0)(0,0,0,0,-,0)(0,-,-,-,0,0)(0,-,1,1,-,1)(0,0,-,-,0,0)(-,0,1,-,-,0)(-,0,1,1,0,0)(-,-,1,-,0,0)(0, -, 1, 1, 1, 1)(-,0,-,0,-,0)(-,-,1,1,1,1)(1,-,1,1,1,-)(-,0,1,1,1,-)transformation  $c_m$  (1,-,1,1,-,0)  $c_{origin} \ (1,-,1,1,-,0)$  $c_{new}$  $\frac{c_{m'}}{(1,-,1,1,-,0)}$  $\begin{array}{c} c_m = c_{origin} \rightarrow c_{new} \prec c_{m'} \\ c_m \prec c_{origin} \rightarrow c_{new} \prec c_{m'} \end{array}$ (1,-,1,-,-,0) (1,1,1,-,-,0)(1,1,-,-,0)(1,-,1,-,-,0)(1,-,1,1,-,0) $c_m \prec c_{origin} \rightarrow c_{new} \ irrele$ (0,-,1,1,-,1)(0,-,1,1,1,1)(-,-,1,1,1,1)(0,0,-,-,0)(0,0,0,0,-,0)(0,0,0,-,-,0)(0,0,0,0,-,0) $c_{origin} \prec c_m \rightarrow c_{new} \prec c_{m'}$ (0,0,-,-,0,0)  $c_{origin} \ irrele \rightarrow c_{new} \prec c_{m'}$ (0,0,-,-,0)(0,0,0,0,-,0) $c_{origin} \ irrele \rightarrow c_{new} \ irrele$ (-,0,1,1,0,0)(-,0,1,-,-,0)(-,0,-,0,-,0)  $\begin{array}{c} c_{new_{irrele}} \prec c_{m'} \\ c_{new_{irrele}} \ irrele \end{array}$ (0,0,0,0,-,0)

Table XIII. Example the influence of regard as one fault for FCI approach



(1,-,1,1,1,-)

Fig. 6. masking effects influence on FCI with distinguish faults

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We take an example to illustrate this type of transformation, which is depicted in Table XIV. Similar with previous strategy, we omit the samples that is belong to the identical transformation.

It is noted that despite the transformations corresponding each directed line that is depicted in Figure 6, there is one more transformation can appear in this strategy, which can make some  $c_{origin}$  removed from the newly minimal schemas, i.e.,  $\exists c_{new}, s.t., c_{new} = c_{origin}$  or  $c_{origin} \prec c_{new}$ . For the example of the Table XIV, in the last row we used a formula  $c_{origin}$  ignored to represent this condition, the mark \* in the  $c_{new}$  indicate that the  $c_{origin}$  is irrelevant to all the  $c_{new}$ . In this row, we can find for the schema  $c_{origin} - -(1,1,0,0,1,-)$ , which is identical to the one in actual MFS, there exists no  $c_{new}$  which is identical or is the parent-schema of this schema. Consequently, in this condition, this strategy may ignore some actual MFS comparing with knowing masking effects.

In fact, besides this special case that may make the FCI approach ignore some actual MFS, there exists some other cases can also achieve the same effect, for example, when the  $c_{new}$  is only schema that is related to  $c_{origin}$ , (related) means not irrelevant, in this case it is either identical or parent-schema). And the corresponding parent-schema  $c_{origin}$  is the only schema which is related to one actual MFS  $c_m$ . Then if the  $c_{new}$  is irrelevant to all the actual MFS, we will ignore the actual MFS  $c_m$ . This ignored event is caused of the  $c_{new}$  grow into the irrelevant schemas, which can also be appeared in the strategy regard as regard from the newly minimal schemas can only happens in the strategy regard regard

## 4.3. Summary of the masking effects on FCI approach

From the analysis of formal model, we can learn that masking effects do influence the FCI approaches, worse more, both strategies *regard as one fault* and *distinguish faults* are harmful, which specifically the former comparing the knowing masking effects have a large possibility that get more sub-schemas of the actual MFS and get more schemas which are irrelevant to the MFS, while the latter may get more parent schemas of the MFS and can also get more irrelevant MFS. Further, Both the two strategies can ignored the actual MFS and the *distinguish* is more likely ignore the MFS than the former strategy.

Note that our discussion is based on that SUT is a deterministic software, i.e., the random failing information of test case will be ignored. The non-deterministic problem will complex our test scenario, which will not be discussed in this paper.

## 5. TEST CASE REPLACING STRATEGY

The main reason why FCI approach fails to properly work is that we cannot determine the area  $B_2$  and  $B_3$ , i.e., if the test case under test trigger other faults which is different from the current one, we cannot figure out whether this test case will trigger the current expected fault as the masking effects may prevent that. So in order to limit the impact of this effect on FCI approach, we need to reduce the number of test cases that trigger other faults as much as possible.

In the exhaustive testing, as all the test cases will be used to identify the MFS, there is no room left to improve the performance without fixing the other faults and re-executing all the test cases. However, when just needing to select part of the whole test cases to identify MFS, which is as traditional FCI approach works, we can adjust the test cases we need to use by selecting proper ones so that we can limit the size of  $T(mask_{F_m})$  to be as small as possible.

 $B_1 \bigcup C$ (0,0,0,1,1,0)(0,0,0,0,0,0)(0,0,1,1,1,0)(0,1,1,0,0,0)(0,0,0,0,1,0)(0,1,1,0,1,0)(0,0,1,1,0,0)(1,1,0,1,0,0)(0,0,1,0,1,0)(0,0,0,1,0,0)(1,0,1,1,0,1)(0,1,1,1,0,0)(0,0,1,0,0,0)(1,1,1,1,1,0)(0,0,1,1,1,1)(0,1,1,1,1,0)(1,1,0,0,0,0)(1,1,0,0,1,0)(1,1,0,0,1,1)(1,1,1,1,1,1)(1,1,0,1,1,0)(0,1,0,0,1,1)(0,0,1,1,0,1)(0,1,1,1,1,1)(1,1,1,0,0,0)(1,0,1,0,1,1)(1,1,1,1,0,1)(1,1,1,1,0,0)(1,0,0,1,1,1)(1,1,1,0,1,0)(1,0,1,1,1,1)(0,0,0,0,1,1)(1,0,0,0,1,1)actual MFS  $knowing\ masking\ effects$ distinguish faults $C(B_1 \bigcup B_2 \bigcup C \bigcup D)$  $C(A \bigcup B_1 \bigcup B_2 \bigcup C)$  $\mathcal{C}(A \bigcup B_1 \bigcup C)$ (0,-,1,1,1,-)(1,1,-,-,0)(0,0,0,-,-,0)(1,1,-,1,-,0)(0,0,-,-,-,0)(0,0,-,-,0,0)(-,0,1,1,-,1)(0,0,-,0,-,0)(-,-,0,0,1,1)(0,0,0,-,0,0)(0,0,1,1,-,-)(1,1,1,-,-,0)(0,0,0,0,-,0)(0,0,0,0,1,-)(1,1,-,-,1,0)(1,0,-,-,1,1)(1,1,0,0,1,-)(1,1,-,0,-,0)(1,1,0,0,1,-)(1,0,1,-,1,1)(0,0,1,1,0,-)(1,0,-,0,1,1)(1,0,1,1,1,1)(-,1,1,-,-,0)(-,-,1,1,1,1)(-,-,0,0,1,1)(-,0,0,0,1,1)(1,1,-,-,1,0)(0,0,0,0,1,-)(-,1,1,1,1,-)(1,1,1,1,-,-)(1,-,1,1,-,1)(0,0,0,0,1,-)transformation  $\frac{c_{origin}}{(-,-,0,0,1,1)}$  $\frac{c_{m'}}{(-,-,0,0,1,1)}$ (-,-,0,0,1,1) (-,0,0,0,1,1) $c_m = c_{origin} \rightarrow c_{m'} \prec c_{new}$ ((1,0,-,-,1,1)) $c_m \prec c_{origin} \rightarrow c_{m'} \prec c_{new}$ (1,0,-,-,1,1)(1,0,1,-,1,1)((1,0,1,1,1,1)) $c_{origin} \prec c_m \rightarrow c_{new} \ irrele$ (1,1,-,1,-,0)(1,1,-,-,-,0)(1,1,-,0,-,0)(0,0,0,-,-,0)(0,0,0,0,-,0) $c_{origin} \prec c_m \rightarrow c_{new} \prec c_{m'}$ (0,0,0,0,-,0)(0,0,-,-,0)(1,1,-,1,-,0)(1,1,1,-,-,0) $c_{origin} \prec c_m \rightarrow c_{m'} \prec c_{new}$ (1,1,-,-,-,0)(-,1,1,-,-,0)(1,1,-,-,-,0) (-,0,1,1,-,1)  $c_{origin} \prec c_m \rightarrow c_{m'} = c_{new}$ (1,1,-,-,1,0)(1,1,-,-,1,0)(1,1,-,-,1,0) $c_{origin} \ irrele \rightarrow c_{m'} \prec c_{new}$ (1,0,1,1,1,1)(1,-,1,1,-,1)

Table XIV. Example the influence of distinguish faults for FCI approach

## 5.1. Replace test case triggering unexpected fault

 $c_{origin} irrele \rightarrow c_{new} irrele$ 

 $c_{origin}$  ignored

The basic idea is to pick the test cases that trigger other faults and generate newly test cases to replace them. These regenerated test cases should either pass in the execution or trigger  $F_m$ . The replacement must satisfy that the newly generated ones will not negatively influence the original identifying process.

(1,1,0,0,1,-)

(0,0,1,1,-,-)

(1,1,0,0,1,-)

(0,0,1,1,0,-)

Commonly, when we replace the test case that triggers unexpected fault with a new test case, we should keep some part in the original test case, we call this part as *fixed* part, and mutate other part with different values from the original one. For example, if a test case (1,1,1,1) triggered an unexpected fault, and the fixed part is (-,-,1,1), then we can replace it with a test case (0,0,1,1) which may either pass or trigger expected fault.

The fixed part can varies for different FCI approaches, e.g, for OFOT algorithm, the fixed part is the factors except for the one that need to be validated whether it is the component of the MFS, while for FIC\_BS, we will fix the factors that should not be mutated of the test case in the next iteration of FIC\_BS process.

It is noted that this replacement may need to execute multiple times for one fixed part as we could not always find a test case that by coincidence satisfy our require-

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ment. Our previous work just randomly choose test cases until find one satisfied test case. That brute method may be simple and really works, but also may need to try too many times to get the satisfied one. So to handle this problem and reduce the cost, we augment our previous approach with computing the *strength* of the test case with the other faults, and then we will select one test case from a group of candidate test cases that has the least *strength* that is related to other faults.

To explain the *strength* notation, we need first introduce the *strength* that a factor is related to a particular fault. We use all(o) to represent the number of executed test cases that contain this factor, and m(o) to indicate the number of test cases that trigger the fault  $F_m$  and contain this factor. Then a the *strength* that a factor is related to a particular fault, i.e.,  $S(o, F_m)$ , is  $\frac{m(o)}{all(o)+1}$ . This heuristic formula is based on the idea that if a factor frequently appears in the test cases that trigger the particular fault, then it is more likely to be the inducing factor that trigger this type of fault. We plus 1 in the denominator for two facts: 1. avoid the division by zero when the factor is never appears before, 2. reduce the bias when a factor rarely appears in the test set but by coincidence appears in a failing test case with a particular fault.

With this *strength* of the factor, we then define the *strength* a test case f is related to a particular fault  $F_m$  as:

$$S(f, F_m) = \frac{1}{|f|} \sum_{o \in f} S(o, F_m)$$

This formula computes the average *strength* of all the factors in the test case as the *strength* for this test case that is related to a particular fault. For a test case that is selected to be tested, we need to make it as small possibility to trigger other faults, so we need to choose the test case that make the following formula as small as possible.

$$\max_{m < L \& m \neq n} S(f, F_m)$$

In this formula, L is the number of all the faults, n is the current analysed fault. Then the process of replacing a test case with a new one keeping some fixed part is depicted in Algorithm 1:

The inputs for this algorithm consists of a test case which trigger an unexpected fault  $-t_{original}$ , the fixed part which we want to keep from the original test case  $-s_{fixed}$ , the fault type which we currently focus on  $-F_m$ , the values sets that each option can take from respectively and the size of the candidate test cases in which we will select one best test case to execute -N. The output of this algorithm is a test case  $t_{new}$  which either trigger the expected  $F_m$  or passes.

This algorithm is a outer loop(line 1 - 19) containing two parts:

The first part(line 2 - 12) generates a new test case which is different from the original one. Different from the original algorithm, we generate a set of candidate test cases (line 3 - 11) instead of only one, and then choose the one that has the least possibility that is related to other faults(line 12) according to our previous formula. Our candidate set of test cases is initialed as size N, the specific number it is assigned is a tradeoff between how quickly this algorithm ended in getting a candidate test case and how many times you'd like to try to find a really satisfied test case. It is noted that when N = 1, it grows into our previous algorithm. Each test cases in the candidate set is generated by random(line 4 - 11), they must be different from existed test cases(we don't show in this pseudo code) and each one of them should keep the fixed part (line 9), and just mutate the factors which are not in that part(line 2). The mutation for each factor works by selecting one legal value which is different from the original one(line 5 - 8).

## ALGORITHM 1: replace test cases triggering unexpected faults

```
Input: the original test case t_{original}, fault type F_m, fixed part s_{fixed}, values set that each
             option can take Param, the size of candidate test cases N
   Output: t_{new} the regenerate test case, The frequency number
   while not MeetEndCriteria() do
        s_{mutant} \leftarrow t_{original} - s_{fixed};
        Candi \leftarrow inital \ set \ of \ size \ N;
 3
        while Candi is not full do
            for all the opt \in s_{mutant} do
 5
                 i = getIndex(Param, opt);
 6
                 opt \leftarrow opt' \ s.t. \ opt' \in Param[i] \ and \ opt'! = opt;
 7
            end
            t' \leftarrow s_{fixed} \bigcup s_{mutant};
            Candi.append(t');
10
        end
11
        t_{new} \leftarrow \arg\min_{t' \in Candi} \max_{i < L \& i \neq m} S(t', F_i);
12
        result \leftarrow execute(t_{new});
13
        if result == PASS \ or \ result == F_m then
14
            return t_{new};
15
16
        else
            continue;
17
18
        end
19 end
   return null
```

Second part is to check whether the newly generated test case is as expected(line 13 - 18). We first execute the SUT under the newly generated test case(line 13) and then check the executed result. Either the test case passes or triggers the same fault –  $F_m$  meets the requirement(line 14), and if so we will directly return this test case(line 15). Otherwise, we will repeat the process, i.e., generate newly test case and check again(line 16 - 17).

Similar as our previous work, this algorithm has another exit besides we find an expected test case(line 10), which is when the function MeetEndCriteria() returns true(line 1). We didn't explicitly show what the function MeetEndCriteria() is like, because this is depending on the computing resource and how accurate you want to the identifying result to be. In detail, if you want to get a high quality result and you have enough computing resource, you can try much times to get the expected test case, otherwise, a relatively small number of attempts is recommended.

In this paper, we just set 3 as the biggest repeated times for this function. When it ended with MeetEndCriteria() is true, we will return null(line 15), which means we cannot find an expected test case.

# 5.2. A case study with the replacing strategy

Suppose we have to test a system with eight parameters, each has three options. And when we execute the test case  $T_0$  – (0 0 0 0 0 0 0 0), a failure–Err1 is triggered. Next we will use the FCI approach – FIC\_BS [Zhang and Zhang 2011] with replacing strategy to identify the MFS for the Err1. Furthermore, there are two more potential faults Err2 and Err3 may be triggered during the testing, which will mask the desired fault Err1. The process is listed in Figure 7. In this figure, there is two main columns in this figure, the left column indicate the executed test ases during testing, while the right column represents the candidate test cases that are used to select one to replace the test case that trigger other faults. Each executed test case corresponds to a specific label  $T_1$  –

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 $T_9$  in the left. The executed test case which is in bold indicate the one that trigger other faults, and at the right column the test case that is selected to be replaced the undesired test case is marked by a shaded background to be distinguished from other candidate test cases.

From Figure 7, for the test case that triggered other faults - (1 1 0 0 0 0 0 0 0) (in this case, the fixed part of the test case is (- - 0 0 0 0 0 0), which the last four factors is the same as the original test case  $T_0$ ), we randomly generate three test cases as the candidate test cases, which are (2 1 0 0 0 0 0), (2 2 0 0 0 0 0), (1 2 0 0 0 0 0 0) respectively. For one candidate test case in the set–(2 1 0 0 0 0 0 0), the *strength* it is related to the Err2 can be computed as

$$\frac{1}{8}\left(\frac{0}{1+1} + \frac{1}{1+1} + \frac{1}{2+1} + \frac{1}{2+1} + \frac{1}{2+1} + \frac{1}{3+1} + \frac{1}{3+1} + \frac{1}{3+1} + \frac{1}{3+1}\right) = 0.27083$$

In this formula, each sub item in the right parentheses shows the *strength* for each factor that is related to Err~2. For example, for the first factor which has value 2, we can only find one test case  $T_1$  – (2 2 1 2 0 0 0 0) contain this factor. This test case passed during testing and no other test case contain this factor. So the M(o) and ALl(o) for this factor is 0 and 1 respectively, and the *strength* it is related to the Err2 is is  $\frac{0}{1+1}$ . For the second factor of candidate test case (2 1 0 0 0 0 0 0), we can only find the test case (1 1 0 0 0 0 0 0) contain it and trigger the fault – Err2. So M(o) and ALl(o) for this factor are both 1, and the corresponding strength is  $\frac{1}{1+1}$ . The strength of remaining factors in this test case is computed in the same way and finally the average strength of all these factors is regard as the strength of the candidate test case (2 1 0 0 0 0 0 0) that is related to the fault Err2. We also follow the same way to compute the strength that these test cases that is related to Err3, as this type fault is never triggered currently, so these strength are all 0.

After computed the *strength* for all these candidate test cases, we then choose the one that is least likely to be related to other faults. In this case, we choose the candidate test case (2 2 0 0 0 0 0 0), its maximal *strength* related to the other fault is against Err 2, which is 0.2083. It is smaller that other two candidate test cases, which both 0.27083. So we choose it as the replaced the test case in the next iteration, i.e.,  $T_2'$ .

This replace process trigged each time the newly test case trigger other fault, and until we finally get the MFS. Some times we could not find a satisfied replacing test case in just one trial. When it happened, we will need repeat searching the proper test case we desired, e.g., for the  $T_8$  which triggered Err3 in Figure 7, we have tried two times  $-T_8'$  and  $T_8''$  to get the satisfied test case  $T_8''$ .

There is a point need to be noted here, i.e., this approach is actually an augmented random approach, to be exactly choose the one that has the smallest strength, we in theory need to rank the  $(\prod_{i\in \neg fixed}|v_i-1|-1)$  (every combination of the value options except the ones in the fixed part) possible candidate test cases. For example, when we find (0 0 1 2 1 2 2 1 ) triggered other fault, we need to select one candidate test case from the set  $\{(0\ 0\ 1\ 1\ 1\ 1\ 1\ 1),(0\ 0\ 1\ 1\ 1\ 1\ 2\ 1),(0\ 0\ 1\ 1\ 1\ 1\ 2\ 2)...(0\ 0\ 2\ 2\ 2\ 2\ 2)\},$  of which the size is  $2^6-1$  (the 1 that is subtracted is the originally test case (0 0 1 2 1 2 2 1) triggered other fault). We should note that in the algorithm when we replace the factor value, we do not assign it with the value that appears in the original failing test case, e.g., for (0 0 1 2 1 2 2 1), we will not replace them with test case such as (0 0 0 2 1 0 0 1), this is because we do not want the fixed part we try to test may be interfered with other factors in the original failing test case. So the possible number of test cases we can generate is  $(\prod_{i\in \neg fixed}|v_i-1|-1)$  instead of  $(\prod_{i\in \neg fixed}|v_i|-1)$ .

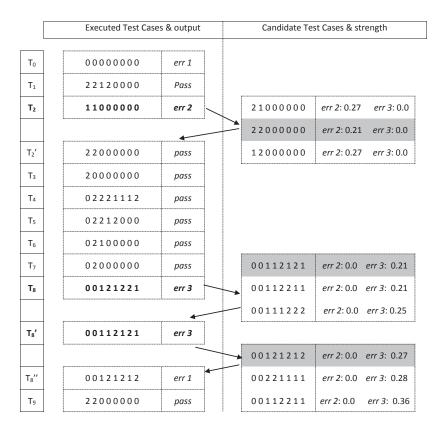


Fig. 7. A case study of our approach

It could cause an exponential explosion in the searching space when k is large and fixed part is small. So in this paper we just give this augmented random approach just choose the one "best" test case in a prior given number of randomly generated candidate test cases set. Nevertheless, we believe there may exists other better approaches, e.g., the heuristic approach or greedy approach, may do better at searching a test case with less *strength* related to other faults, which however, will not be discussed in this paper.

# 5.3. Complexity analysis

This complexity lay on two facts: the number of test cases triggered other faults which need to be replaced, and the number of test cases that need to be tried to generate a non-masking-effects test case. The complexity is the product of this two facts.

The first fact is comparable to the extra test cases that needed to identify the MFS, and this number varies in different FCI approaches. Table XV list the number of test cases that each algorithms that needed to get the MFS. In this table, d indicates the number of MFS in the SUT. k means the number of the parameters of the SUT. t is the degree of the MFS in the SUT. t is an upper bond, satisfies, t is the number of values one parameter can take.

It must be noted that each algorithm may be limited to some restrictions to identify the result, details can be saw in [Zhang and Zhang 2011].

To get the magnitude of the second fact, we need to figure out the possibility that a test case that could trigger other fault. The first thing we need to care is the *fixed* 

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Table XV. The number of test cases each FCI approach needed to identify MFS

#### Method number of test cases to identify MFS Charles ELA $O(\hat{d}logk + \hat{d}^2)$ Martinez with safe value [Martínez et al. 2008; 2009] Martinez without safe values [Martínez et al. 2008; 2009] $O(d^2 + dlogk + log^c k)$ Martinez' ELA [Martínez et al. 2008; 2009] $ds^v log k$ Shi SOFOT [Shi et al. 2005] Nie OFOT [Nie and Leung 2011a] kdYlimaz classification tree FIC [Zhang and Zhang 2011] t(logk+1)+1FIC\_BS [Zhang and Zhang 2011] Ghandehari's suspicous based [Ghandehari et al. 2012] TRT [Niu et al. 2013]

Table XVI. The complexity of second part

Method	fixed part
Charles ELA	$O(\min(N, (v-t)^{k-p} - 1))$
Martinez with safe value [Martínez et al. 2008; 2009]	$O(min(N, (v-1)-1)) O(min(N, (v-1)^{k-1}-1))$
Martinez without safe values [Martínez et al. 2008; 2009]	_
Martinez' ELA [Martínez et al. 2008; 2009]	$O(\min(N, (v-t)^{k-p} - 1))$
Shi SOFOT [Shi et al. 2005]	O(min(N,(v-1)-1)))
Nie OFOT [Nie and Leung 2011a]	O(min(N,(v-1)-1)))
Ylimaz classification tree	$O(\min(N, (v-t)^{k-p} - 1)$
FIC [Zhang and Zhang 2011]	$O(min(N, (v-1)-1)) O(min(N, (v-1)^{k-1}-1))$
FIC_BS [Zhang and Zhang 2011]	$O(min(N, (v-1)-1)) O(min(N, (v-1)^{k-1}-1))$
Ghandehari's suspicous based [Ghandehari et al. 2012]	$O(min(N,(v-t)^{k-p}-1))$
TRT [Niu et al. 2013]	$O(min(N, (v-1)-1)) O(min(N, (v-1)^{k-1}-1))$

part, as the additional generated test case should somehow contain this part. As we have mentioned before we can in fact generate  $(v-1)^{k-p}$  (p is the number of factors in the *fixed* part)possible test cases that contain the *fixed* part. Apart from the one that need to be replaced, there remain  $(v-1)^{k-p}-1$ , which indicates the complexity is  $O((v-1)^{k-p}-1)$ . However, to avoid the exponential computational complexity, we in this algorithm use a method MeetEndCriteria() (line 1) function to end the algorithm when the trying times is over a prior given constant, say N, so the final complexity for the second part is  $O(min(N, (v-1)^{k-p}-1))$ .

It is noted that exponential factor k-p directly affects the complexity of the second factor, the more p is, the less test cases could be generated. For different approach, p is different. As for OFOT, p is a fixed number, which is k-1, it is the minimal number of the test cases we need to give. While for FIC\_BS, the p varies in the test cases it generates, ranges from k-1 to 1. While for non-adaptive, as the fixed part is the coverage, we list them as t. We list them all in Table XVI. It is noted that the Martinezwithoutsafevalues have no such complexity, this is because this approach works when v=2, and this will result in that we will not have other test cases to be replaced if we test a fixed part when trigger other faults.

## 6. EMPIRICAL STUDIES

We conducted several empirical studies to address the following questions:

- **Q1**: Do masking effects exist in real software when it contain multiple faults?
- Q2: How much do traditional approaches suffer from these real masking effects?
- **Q3**: Can our approach do better than traditional approaches when facing these masking effects?

**Q4**: Comparing with previous work, do our new approach get improvement in handling effects and limiting the costs(reducing extra test cases).

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software	versions	LOC	classes	bug pairs <sup>3</sup>
HSQLDB	2.0rc8	139425	495	#981 & #1005
	2.2.5	156066	508	#1173 & #1179
	2.2.9	162784	525	#1286 & #1280
JFlex	1.4.1	10040	58	#87 & #80
	1.4.2	10745	61	#98 & #93

Table XVII. Software under survey

**Q5**: Does voting system that consists of different approaches can make improvements?

## 6.1. The existence of masking effects

In the first study, we surveyed two open-source software to gain an insight on the existence of multiple faults and their effects. The software under study are: HSQLDB and JFlex, the first is a database management software written in pure java and the second is a lexical analyser generator. Each of them contain different versions. All the two subjects are highly configurable so that the options and their combination can influence their behaviour. Additionally, they all have developers' community so that we can easily get the real bugs reported in the bug tracker forum. Table XVII lists the program, the number of versions we surveyed, number of lines of uncommented code, number of classes in the project and the bug's id of each software we studied.

6.1.1. Study setup. We first looked through the bug tracker forum of each software and picked some bugs which are caused by the options combination. For each bug, we will derive its failure-inducing combinations by analysing the bug description report and its attached test file which can reproduce the bug. For example, through analysing the source code of the test file of bug#981 for HSQLDB, we found the failure-inducing combinations for this bug is: (preparestatement, placeHolder, Long string), this three factors together form the condition on which the bug will be triggered. These analysed results will be regarded as the "prior failure-inducing combinations" later.

We further selected pairs of bugs belong to the same version and merged their test file, so that we can reproduce different faults through controlling the inputs to that merged test file. This merging manipulation varies with the pair of bugs we selected, and for each pair of bugs, the source code of the merging file as well as other detailed experiment information is available at—https://code.google.com/p/merging-bug-file.

Next we built the input model which consist of the options related to the failure-inducing combinations and additional noise options. The detailed model information is in Table XVIII and XIX for HSQLDB and JFLex respectively. Each table is organised into four groups: 1)"common options", which lists the options as well as their values under which every version of this software can be tested. 2)"common boolean options", which lists additional common options whose values type is boolean. 3) "specific options", under which only the specific version of that software can be tested. 4) "configure space", which depicts the input model for each version of the software.

We then generated the exhaustive test suite consist of all the possible combinations of these options and under each of them we executed the merged test file. We recorded the output of each test case to observe whether there are test cases contain prior failure-inducing combination but do not produce the corresponding bug.

6.1.2. Result and discussion. Table XX lists the results of our survey. Column "all tests" give the total number of test cases we executed , Column "failure" indicate the number of test cases that failed during testing and Column "masking" indicate the number of test cases which trigger the masking effect.

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Table XVIII. Input model of HSQLDB

comi	mon options	values	
Se	erver Type	server, webserver, inprocess	
ex	isted form	mem, file	
res	ultSetTypes	forwad, insensitive, sensitive	
resultS	etConcurrencys	read_only, updatable	
resultS	SetHoldabilitys	hold, close	
Sta	tementType	statement, prepared	
common boolean options			
sql.enfor	sql.enforce_strict_size, sql.enforce_names, sql.enforce_refs		
versions	specific options	values	
2.0rc8	more	true, false	
	placeHolder	true, false	
	cursorAction	next,previous,first,last	
2.2.5	multiple	one, multi, default	
	placeHolder	true, false	
2.2.9	duplicate	dup, single, default	
	default_commit	true, false	
versions	Config space		
2.0rc8	$2^9 \times 3^2 \times 4^1$		
2.2.5	$2^{8} \times 3^{3}$		
2.2.9	$2^{8} \times 3^{3}$		

Table XIX. Input model of JFlex

com	mon options	values		
g	eneration	switch, table, pack		
	charset	default, 7bit, 8bit, 16bit		
	common boolean options			
public, apij		ar,line,column,notunix, yyeof		
versions	specific options	values		
1.4.1	hasReturn	true, false, default		
	normal	true, false		
1.4.2	lookAhead	one, multi, default		
	type	true, false		
	standalone	true, false		
versions	Config space			
1.4.1	$2^{10} \times 3^2 \times 4^1$			
1.4.2	$2^{11} \times 3^2 \times 4^1$			

Table XX. Number of faults and their masking effects

software	versions	all tests	failure	masking
HSQLDB	2cr8	18432	4608	768
-	2.2.5	6912	3456	576
-	2.2.9	6912	3456	1728
JFlex	1.4.1	36864	24576	6144
-	1.4.2	73728	36864	6144

We observed that for each version of the software under analysis we listed in the Table XX, the test cases with masking effects do exist, i.e., test cases containing failure inducing combinations did not trigger the corresponding bug. In effect, there is about 768 out of 4608 test cases (16.7%) in hsqldb with 2rc8 version. This rate is about 16.7%, 50%, 25%, 16.7% respectively for the remaining software versions, which is not trivial.

So the answer to  $\mathbf{Q1}$  is that in practice, when SUT have multiple faults, the masking effects do exist widely in the test cases.

### 6.2. Performance of the traditional algorithms

In the second study, our aim is to learn the degree that the masking effect impact on the traditional approaches. To conduct this study, we need to apply the traditional algorithms to identify the failure-inducing combinations for the prepared software in Table XVII and compare them with the prior failure-inducing combinations.

6.2.1. Study setup. The traditional approaches we selected are: OFOT[Nie and Leung 2011a], FIC\_BS [Zhang and Zhang 2011] and CTA[Yilmaz et al. 2006], in which CTA is a integrated failure characterization part of FDA-CIT[Yilmaz et al. 2013]. As CTA is a post-analysis technique applied on given test cases, different test cases will influence the result of characterization process. So to avoid randomness and to be fair, we fed the CTA with the same test cases generated by OFOT to get deterministic results. Additionally, the classified tree algorithms for CTA we chose is J48 implemented in Weka [Hall et al. 2009].

For each test case in the exhaustive set for a particular software, we applied O-FOT, FIC\_BS and CTA respectively to isolate the failure-inducing combinations in this test case. As the subject under test has multiple faults, there are two strategies we adopted in this case study, i.e., *regard as one fault* and *distinguish faults* described in Section 3.2. We then collected all the failure-inducing combinations identified by each algorithm for each strategy respectively and refer them as *identified combinations* for convenience.

We next compared the result with the prior failure-inducing combinations to quantify the degree that traditional approaches suffers from masking effect. There are five metrics we need to care in this study, which are listed as follows:

- (1) The number of the common combinations appeared in both identified combinations and prior failure-inducing combinations. We denote it as *accurate number* later.
- (2) The number of the identified combinations which is the parent combinations of some prior failure-inducing combinations. We refer it to *parent number*.
- (3) The number of the identified combinations that is the sub combinations of some prior failure-inducing combinations, which is referred to *sub number*.
- (4) The number of ignored failure-inducing combinations. This metric counts these combinations in prior failure-inducing combinations, which are irrelevant to the identified combinations. We label it as *ignored number*.
- (5) The number of irrelevant combinations. This metric counts these combinations in these identified combinations, which are irrelevant to the prior failure-inducing combinations. It is referred to the *irrelevant number*.

Among these five metrics, high accurate number value indicates FCI approaches performs effectively, while *ignored number* and *irrelevant number* indicate the degree of deviation for the FCI approaches. For parent number and sub number, they indicate FCI approaches that, although with additional noisy information, can determine part parameter values about the failure-inducing combinations.

This case study was conducted on the five subjects: HSQLDB with version 2rc8, 2.2.5 and 2.2.9, JFlex with versions 1.4.1 and 1.4.2. We summed up these metrics for each subject and illustrated them together in Figure 8 for analysis.

6.2.2. Result and discussion. Figure 8 depicts the result of the second case study. There are three sub-figures, respectively, corresponding to the result of three approaches: FIC\_BS, OFOT and CTA. In each sub-figure, the five columns "accurate", "parent", "sub", "ignore" and "irrelevant" respectively presents the five metrics mentioned above. Two bars in each column respectively illustrate the result of strategy for regard as one fault and distinguish faults.

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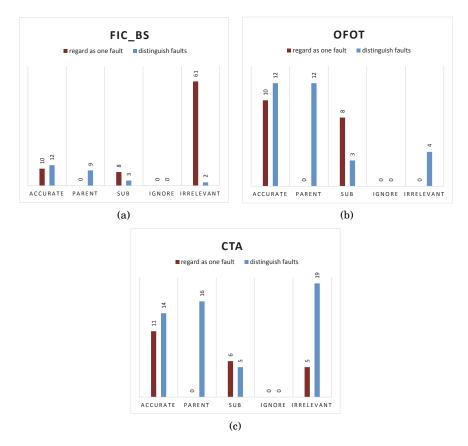


Fig. 8. Results of two strategies for traditional approaches: FIC\_BS, OFOT and CTA

We first observed that, traditional approaches do suffer from the masking effect to some extent. Specifically, in the Figure 8(a), FIC\_BS approach only correctly identified 12 and 10 accurate combinations for the two traditional strategies respectively, while wrongly identified 14 and 69 combinations, among which *parent number*, *sub number*, *irrelevant number* are 9,3,2 and 0,8,61 respectively. Similar results can be observed in Figure 8(b) and 8(c) for approach OFOT and CTA .

Another interesting observations is that for the regard as one fault and distinguish faults strategy, the former get more sub combinations than latter, while distinguish faults strategy get more parent combinations than regard as one strategy. This result accorded with our formal analysis in section 3.2. With respect to the metrics irrelevant combinations, however, we didn't get as expected as the formal analysis. In fact, both the case that regard as one fault has more irrelevant combinations (see Figure 8(a)) and the case that distinguish faults obtained more irrelevant combinations (see Figure 8(b) and 8(c)) exist. With checking the executing process and the combinations they got, we believed one possible main reason for this result is that the algorithm encountered the problem of importing newly faults which bias their identifying process.

We further observed that, for different algorithms, the extent to what they suffered from masking effects varied. For instance, for FIC\_BS approach, under the masking effects, they identified the 61 and 2 irrelevant combinations for two strategies, while for OFOT and CTA, this value is 0 and 4, 5 and 19 respectively. There are two factors

caused this difference: the chosen test cases and the analysis method. For FIC\_BS and OFOT, the test cases they chosen for isolating failure-inducing combinations is different, which consequently changed the masking effects they may encountered. For OFOT an CTA, while the test cases they chose are the same, the difference lies at the way they characterizing the failure-inducing combinations in the test cases: OFOT directly identify the parameter according to the passed test cases while CTA used classified tree analysis.

Therefore, the answer we got for **Q2** is: traditional algorithms do suffer from the multiple faults and their masking effect, although the extent varies in different algorithms.

## 6.3. Performance of our approach

The third empirical study aims to observe the performance of our approach and compare it with the result got by the traditional approaches. Our approach augments the three traditional FCI approaches with replacing test cases strategy described in Section 4.

*6.3.1. Study setup.* The setup of this case study is almost the same as the second case study. The difference is that the algorithms we choose are three augmented ones.

6.3.2. Result and discussion. Figure 9 presents the result of the last case study. The organization of this figure is similar to the second study. The bar in each column depicts the results of the augmented approaches, which is labelled as "replacing strategy". We marked two additional points in each column which represent the result of *regard* as one fault and distinguish faults strategy to get a comparison with the augmented approaches.

Comparing our approach with two traditional strategies in Figure 9, we observed that there is significant improvement for augmented approaches in reducing the wrongly identified combinations. For instance, CTA approach in Figure 9(c) only got 2 irrelevant combinations with replacing strategy, while the traditional two strategy got 5 and 19 irrelevant combinations respectively. And for FIC\_BS in Figure 9(a) this comparison is 2 for replacing strategy, and 2, 61 for two traditional strategies.

Besides, the augmented approaches also get a good performance at limiting the number of sub combinations and parent combination. In effect, compared with *distinguish* faults which is good at limiting sub combinations while producing more parent combinations and regard as one fault which is the other way around, the augmented ones get a more balanced result. Specifically, for instance, in Figure 9(a) for approach FIC\_BS, distinguish faults strategy obtained 9 parent combinations while got 3 sub combinations. And for regard as one fault strategy, it got none parent combination but attained 8 sub combinations. For the replacing strategy, it only identified 4 parent combinations, which smaller than distinguish faults strategy, and obtained 3 sub combinations which is smaller than regard as one fault strategy and equal to distinguish faults strategy.

Apart from these improvement, there is some slight decline for the augmented approaches in some specific situation. For example, we noted that for replacing strategy, it nearly got 2 less accurate combinations on average than traditional strategies, and ignored 1 more failure-inducing combinations on average than traditional ones.

In summary, the answer for **Q3** is: our approach do make the FCI approaches, to some extent, get better better performance at identifying failure-inducing combinations when facing masking effect between multiple faults.

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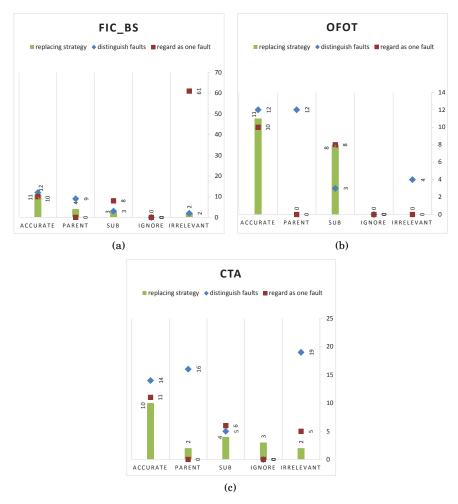


Fig. 9. Three approaches augmented with the replacing strategy

## 6.4. Voting System

The last empirical study aims to observe the performance of our approach and compare it with the result got by the traditional approaches. Our approach augments the three traditional FCI approaches with replacing test cases strategy described in Section 4.

*6.4.1. Study setup.* The setup of this case study is almost the same as the second case study. The difference is that the algorithms we choose are three augmented ones.

6.4.2. Result and discussion.

## 6.5. Threats to validity

There are several threats to validity for these empirical studies. First, we have only surveyed five open-source software, four of which are medium-sized and one is large-sized. This may impact the generality of our observations. Although we believe it is quite possible a common phenomenon in most software that contain multiple faults which can mask each other, we need to investigate more software to support our conjecture.

The second threat comes from the input model we built. As we focused on the options related to the perfect combinations and only augmented it with some noise options, there is a chance we will get different result if we choose other noise options. More different options needed to be opted to see whether our result is common or just appeared in some particular input model.

The third threats is that we just observed three failure-inducing combinations identifying algorithms, further works needed to examine more algorithms in this filed to get a more general result.

## 7. RELATED WORKS

Shi and Nie presented a further testing strategy for fault revealing and failure diagnosis[Shi et al. 2005], which first tests SUT with a covering array, then reduces the value schemas contained in the failed test case by eliminating those appearing in the passed test cases. If the failure-causing schema is found in the reduced schema set, failure diagnosis is completed with the identification of the specific input values which caused the failure; otherwise, a further test suite based on SOFOT is developed for each failed test cases, testing is repeated, and the schema set is then further reduced, until no more failure is found or the fault has been located. Based on this work, Wang proposed an AIFL approach which extended the SOFOT process by mutating the changing strength in each iteration of characterizing failure-inducing combinations [Wang et al. 2010].

Nie et al. introduced the notion of Minimal Failure-causing Schema(MFS) and proposed the OFOT approach which extended from SOFOT that can isolate the MFS in SUT[Nie and Leung 2011a]. The approach mutates one value with different values for that parameter, hence generating a group of additional test cases each time to be executed. Compared with SOFOT, this approach strengthen the validation of the factor under analysis and also can detect the newly imported faulty combinations.

Delta debugging [Zeller and Hildebrandt 2002] proposed by Zeller is an adaptive divide-and-conquer approach to locate interaction fault. It is very efficient and has been applied to real software environment. Zhang et al. also proposed a similar approach that can identify the failure-inducing combinations that has no overlapped part efficiently [Zhang and Zhang 2011]. Later Li improved the delta-debugging based failure-inducing combination by exploiting the useful information in the executed covering array[Li et al. 2012].

Colbourn and McClary proposed a non-adaptive method [Colbourn and McClary 2008]. Their approach extends the covering array to the locating array to detect and locate interaction faults. C. Martinez proposed two adaptive algorithms. The first one needs safe value as their assumption and the second one remove the assumption when the number of values of each parameter is equal to 2[Martínez et al. 2008; 2009]. Their algorithms focus on identifying the faulty tuples that have no more than 2 parameters.

Ghandehari et al. defined the suspiciousness of tuple and suspiciousness of the environment of a tuple[Ghandehari et al. 2012]. Based on this, they rank the possible tuples and generate the test configurations. They further utilized the test cases generated from the inducing combination to locate the faults inside the source code[Ghandehari et al. 2013].

Yilmaz proposed a machine learning method to identify inducing combinations from a combinatorial testing set [Yilmaz et al. 2006]. They construct a classified tree to analyze the covering arrays and detect potential faulty combinations. Beside this, Fouché [Fouché et al. 2009] and Shakya [Shakya et al. 2012] made some improvements in identifying failure-inducing combinations based on Yilmaz's work.

Our previous work [Niu et al. 2013] have proposed an approach that utilize the tuple relationship tree to isolate the failure-inducing combinations in a failing test case. One

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novelty of this approach is that it can identify the overlapped faulty combinations. This work also alleviates the problem of introducing newly failure-inducing combinations in additional test cases.

In addition to the works that aims at identifying the failure-inducing combinations in test cases, there are some studies focus on working around the masking effects:

With having known masking effects in prior, Cohen [Cohen et al. 2007a; 2007b; 2008] studied the impacts that the masking effects render some generated test cases invalid in CT, and they proposed the approach that integrate the incremental SAT solver with covering array generating algorithms to avoid these masking effects in test cases generating process. Further study was conducted [Petke et al. 2013]to show the fact that with considering constrains, the higher-strength covering arrays with early fault detection is practical. Besides, additional constraints impacts in CT were studied in works like [Garvin et al. 2011; Bryce and Colbourn 2006; Calvagna and Gargantini 2008; Grindal et al. 2006; Yilmaz 2013].

Chen et al. addressed the issues of shielding parameters in combinatorial testing and proposed the Mixed Covering Array with Shielding Parameters (MCAS) to solve the problem caused by shielding parameters[Chen et al. 2010]. The shielding parameters can disable some parameter values to expose additional interaction errors, which can be regarded as a special case of masking effects.

Dumlu and Yilmaz proposed a feedback-driven approach to work around the masking effects[Dumlu et al. 2011]. In specific, it first use CTA classify the possible failure-inducing combinations and then eliminate them and generate new test cases to detect possible masked interaction in the next iteration. They further extended their work [Yilmaz et al. 2013], in which they proposed a multiple-class CTA approach to distinguish faults in SUT. In addition, they empirically studied the impacts on both ternary-class and multiple-class CTA approaches.

Our work differs from these ones mainly in the fact that we formally studied the masking effects on FCI approaches and further proposed a divide-and-conquer strategy to alleviate this impact.

## 8. CONCLUSIONS

Masking effects of multiple faults in SUT can bias the result of traditional failure-inducing combinations identifying approaches. In this paper, we formally analysed the impact of masking effects on FCI approaches and showed that both two traditional strategies are inefficient in handling such impact. We further presented a divide and conquer strategy for FCI approaches to alleviate this impact.

In the empirical studies, we extended three FCI approaches with our strategy. The comparison between this three traditional approaches and their improved variations was conducted on several open-source software. The results indicated that our strategy do assist traditional FCI approaches in getting a better performance when facing masking effects in SUT.

As a future work, we need to do more empirical studies to make our conclusion more general. Our current experimental subjects are several middle-sized software, we would like to extend our approach into more complicated and large-scaled testing scenarios. Another promising work in the future is to combine white-box testing technique to make the FCI approaches get more accurate results when handling masking effects. We believe that figuring out the fault levels of different bugs through white-box testing technique is helpful to reduce misjudgement in the failure-inducing combinations identifying process. At last, as the extent to what the FCI suffers from masking effects varies in different algorithms, the combination of different FCI approaches is desired in the future to further improve the performance for identifying failure-inducing combinations for multiple faults.

# 9. TYPICAL REFERENCES IN NEW ACM REFERENCE FORMAT APPENDIX

#### **ELECTRONIC APPENDIX**

The electronic appendix for this article can be accessed in the ACM Digital Library.

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# Online Appendix to: Identify minimal failure-causing schemas for multiple faults

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## A. THIS IS AN EXAMPLE OF APPENDIX SECTION HEAD

## **B. APPENDIX SECTION HEAD**

The primary consumer of energy in WSNs is idle listening. The key to reduce idle listening is executing low duty-cycle on nodes. Two primary approaches are considered in controlling duty-cycles in the MAC layer.