

# Identifying minimal failure-causing schemas for multiple faults

XINTAO NIU and CHANGHAI NIE, State Key Laboratory for Novel Software Technology, Nanjing University

ALVIN CHAN, Hong Kong Polytechnic University

JEFF Y. LEI, Department of Computer Science and Engineering, The University of Texas at Arlington

Combinatorial testing\_(CT) has been proven to be effective to reveal the potential failures caused by the interaction of the inputs or options of the System Under Test\_(SUT). To extend and fullymake full use ef-CT, athe theory of Minimal Failure-Causing Schema\_(MFS) ishas been proposed. The use of MFS helps to isolate the root cause of athe failure after CT detection, which is desired after detecting them by CT. Most existed algorithms that have been based on MFS theory isofocus on identifying the MFS to identifyin SUT with the a single fault; however, we argue that multiple faults are is the more common testing scenario, and under which masking effects may be triggered so that some expected faults will not be observed\_normally. Traditional MFS theory, as well as theits related identifying algorithms, lack a mechanism to handle such effects; hence, they will maymake them incorrectly isolate the MFS in the SUT. To address this problem, we proposed a new MFS model that takes into account with considering multiple faults. We first formally analyse the impact of the multiple faults on the extantexisted MFS isolating algorithms, especially in situations wherewhen masking effects are were triggered by etween these multiple faults. Based on this, we then developgive an approach that can assist traditional algorithms to better handle the-multiple faults testing scenarios. Empirical studies were conducted using with several kinds of open-source software\_were conducted, which showed that multiple faults with masking effects do negatively affect on-traditional MFS identifying approaches and that our approach can help them to alleviate these effects.

Categories and Subject Descriptors: D.2.5 [Software Engineering]: Testing and debugging—Debugging aids,testing tools

General Terms: Reliability, Verification

Additional Key Words and Phrases: Software Testing, Combinatorial Testing, Failure-causing schemas, Masking effects

# ACM Reference Format:

Xintao Niu, Changhai Nie and Hareton Leung, 2014.ldentifying failure-causing schemas for multiple faults. ACM Trans. Embedd. Comput. Syst. 9, 4, Article 39 (March 2010), 39 pages. DOI:http://dx.doi.org/10.1145/0000000.0000000

### 1. INTRODUCTION

With the increasing complexity and size of modern software, many factors, such as input parameters and configuration options, can <u>affectinfluence</u> the behaviour of the SUT. The unexpected faults caused by the interaction <u>ofamong</u> these factors can make <u>software</u> testing <u>challengingsuch software a big challenge</u> if the interaction space is too large. In the worst case, we need to examine every possible combination of these factors as each <u>such combination</u> can contain unique faults [Song <u>et al.</u> 2012]. While conducting <u>such</u> exhaustive testing is ideal and necessary in theory, it is impractical and net uneconomical.-in-consideration

This work was supported by the National Natural Science Foundation of China (No. 61272079), the Research Fund for the Doctoral Program of Higher Education of China (No.20130091110032), the Science Fund for Creative Research Groups of the National Natural Science Foundation of China (No. 61321491), and the Major Program of National Natural Science Foundation of China (No. 91318301)

Program of National Natural Science Foundation of China (No. 91318301)

Permission to make digital or hard copies of part or all of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies show this notice on the first page or initial screen of a display along with the full citation. Copyrights for components of this work owned by others than ACM must be honored. Abstracting with credit is per-mitted. To copy otherwise, to republish, to post on servers, to redistribute to lists, or to use any component of this work in other works requires prior specific permission and/er a fee. Permissions may be requested from the Publications Dept., ACM, Inc., 2 Penn Plaza, Suite 701, New York, NY 10121-0701 USA, fax +1 (212) 869-0481, or permissions@acm.org.

0481, or permissions@acm.org. ©c 2010 ACM 1539-9087/2010/03-ART39 \$15.00 DOI:http://dx.doi.org/10.1145/0000000.0000000

Table I. MS word example

id	Highlight	Status bar	Bookmarks	Smart tags	Outcome
1	On	On	On	Off	PASS
2	On	Off	Off	On	PASS
3	Off	On	Off	Off	Fail
4	Off	Off	On	Off	PASS
5	Off	On	On	On	PASS

of the limited testing time and computing resource. One remedy for this problem is combinatorial testing, which systematically samples the interaction space and selects a relatively small set of test cases that cover all the valid iterations, with the number of factors involved in the interaction no more than a prior fixed integer, i.e., the **Strength** of the interaction. Many works in CT aims to construct the smallest set of such efficient testing objects [Cohen et al. 1997; Bryce et al. 2005; Cohen et al. 2003], which is also referred to ascalled a **Covering array**.

Once failures are detected by the covering array, it is desired to isolate the failure-inducing combinations in these faileding test cases must be isolated. This task is important in CT as it can facilitate the debugging efforts by reducing the code scope that needed for inspection to in spected. [Ghandehari et al. 2012]. However, Only with the information sturn from the covering array sometimes does not clearly is far from clear to identify the location and magnitude of the failure-inducing combinations [Colbourn and McClary 2008]. Thus, deeper analysis is needed to be conducted. Consider Take an the following example [Bach and Schroeder 2004]/2; Fig. 1 presents a 2two-way covering array for testing anthe MS\_wWord application; in which we want to examine vari-ous combinations of options for the MS\_word. 'Highlight', 'Status Bar', 'Bookmarks' and 'Smart tags' of MS word. Assume the third test case faileds, then wore thenean get that there are five 2two-way suspi-cious combinations that may be responsible for this failure: Highlight Off, Bookmarks: Off), (Highlight: Off, Smart tags: Off), (Status Bar: On, Bookmarks: Off), (Status Bar: On, Smart tags: Off) and (Bookmarks: Off, Smart tags: Off). (Note that (Highlight: Off, Status Bar: On) is excludeds in this set as it appeared in the fifth passing test case). Without any more information, we cannot figure out which one or more of the combinationssome in this suspicious set caused theis failure. In fact, taking into account of the higher\_strength combination, e.g., (Highlight: Off, Status Bar: On, Smart tags: Off), the problem becomes will grow more complicated.

To address this problem, prior work [Nie and Leung 2011a] specifically studied the properties of the minimal failure-causing schemas in SUT, based on which, a further diagnosis by the generating additional test cases was applied that and therefore can identify the MFS in the test case. Other works have been proposed ways to identify the MFS in SUT, which include approaches such as building a tree model [Yilmaz et al. 2006], ex-ploiting the methodology of minimal failure-causing schema [Nie and Leung 2011a], ranking suspicious classification ous combinations based on some rules [Ghandehari et al. 2012], using graphic-based deduction [Mart'unez et al. 2008], among others, and so on These ap-proaches can be classified partitioned into two categories [Colbourn and McClary 2008]: adap-tive—test cases that are thosen by sed on the outcomes of the executed tests [Nie and Leung 2011a; Ghandehari et al. 2012; Niu et al. 2013; Zhang and Zhang 2011 Shakya et al. 2012; Wang et al. 2010; Li et al. 2012] or nonadaptive—test cases that are chosen independently and can be executed parallel [Yilmaz et al. 2006; Colbourn and McClary 2008; Mart'unez et al. 2008; 2009; Fouche' et al. 2009].

The MFS methodology as well as other MFS\_identifying approaches mainly focus on the ideal scenario in whichthat SUT only contains one fault, i.e., the test case under testing can either fails or passes the testing. However, in this paper, we argue that SUT with multiple distinguished faults is the more common testing scenario in practice, and moreover, this do have impacts on the Failure-inducing Combinations Identifying(FCI) approaches. One main impact of multiple faults on FCI approaches is the masking ef-

effects. A masking effect [Dumlu et al. 2011; Yilmaz et al. 2013] is an effect in which that some failures prevents test cases from normally checking combinations that are supposed to be tested. Take the Linux command— Grep—for example\_¬ wwe noticed that there are two different faults reported in the bug tracker system. The first—one—1 claims that Grep incorrectly matches unicode patterns with '\<\>', while the second—one—2 claims an incompatibility between option '-c' and '-o'. When we put these two scenarios into one test case, only one fault information—will be observed, which means another fault is masked by the observed faultene. This effects will prevent test cases from executing normally executing consequently—make approaches make a in incorrectly judgements of the correlation be-tween the combinations checked in the test case and the fault that has been masked and therefore not observed been prevented to be observed.

As <u>we knowknown</u> that masking effects negatively affect the performance of FCI approaches, a natural question is how this effect biases the results of <u>theseFCI</u> approaches. In this paper, we formalized the process of identifying <u>the MFS</u> under the circumstances <u>in whichthat</u> masking effects exist in <u>the SUT</u> and try to answer this question. One insight from the formal analysis is that we cannot completely get away from the impact of <u>the masking effects</u> even if we do exhaustive testing. <u>ButFurthermore, and in proving the masking effects</u> and regarding multiple faults as one fault <u>are detrimental toare harmful thefor FCI process.</u>

Based on this concern e insight we proposed a strategy to alleviate this impact. This strategy adopts the divide and conquer framework, *i.e.*, separately handles each fault in the SUT. For a particular fault under analysis, when applying traditional FCl approaches to identify the failure-inducing combinations, we pick the test cases generated by FCl approaches that trigger unexpected faults and replace them with <a href="newly-regenerated-newly-test">newly-regenerated newly-test cases</a>. These newly test cases should either pass or trigger the same fault under analysis.

The key to our approach is to search <u>for</u> a test case that do<u>es</u> not trigger unexpected fault-s <u>whichthat</u> may import <u>athe</u> masking effect. To guide the searching process, <u>i.e.</u>, to reduce the possibility that the extra generated test case <u>will</u> triggering <u>an</u> unexpected fault, a nat-ural idea is to <u>takelearn</u> some characteristics from the existeding test cases and make the characteristics of the newly searched test case as <u>different</u> <u>as possiblemuch as different</u> from those existinged test cases which triggered <u>the</u> unexpected fault. To reach this target, we define the <u>related strength</u> between the factor and the faults, <u>for which tThe strongermore</u> the <u>related strength</u> is between a factor and a particular fault, the <u>greater the likelihoodmore that thatthe</u> factor <u>willis likely to</u> trigger this fault. We then us<u>eing the the</u> integer linear programming (ILP) technique to find a test case which has the <u>leastsmallest related strength withbetween the</u> unexpected fault.

To evaluate the performance of our approach, we applied our strategy on the FCI approach FIC BS [Zhang and Zhang 2011]. The subjects we used were several open-source software found inwith the developers' forum in the Source-Forge community. Through studying their bug reports in the bug tracker system as well as their user's manuals guide, we built athe testing model which can reproduce the reported bugs with specific test cases. We then respectively compare the FCI approach augmented with our strategy (AUGF-CI) towith the traditional FCI approach with these subjects. We further empirically studied the performance of the important component of our strategy—searching satisfied test cases to conduct this study, we compare our AUGFCI approach with the augmented FCI approach augment—by randomly searching satisfied test cases. We finally compared our approach with the existinged masking handling technique—FDA-CIT [Yilmaz et al. 2013]. All of these empirical studies showed that our replacing strategy as well as the searching test case component achievedget a better performance than these traditional approaches when

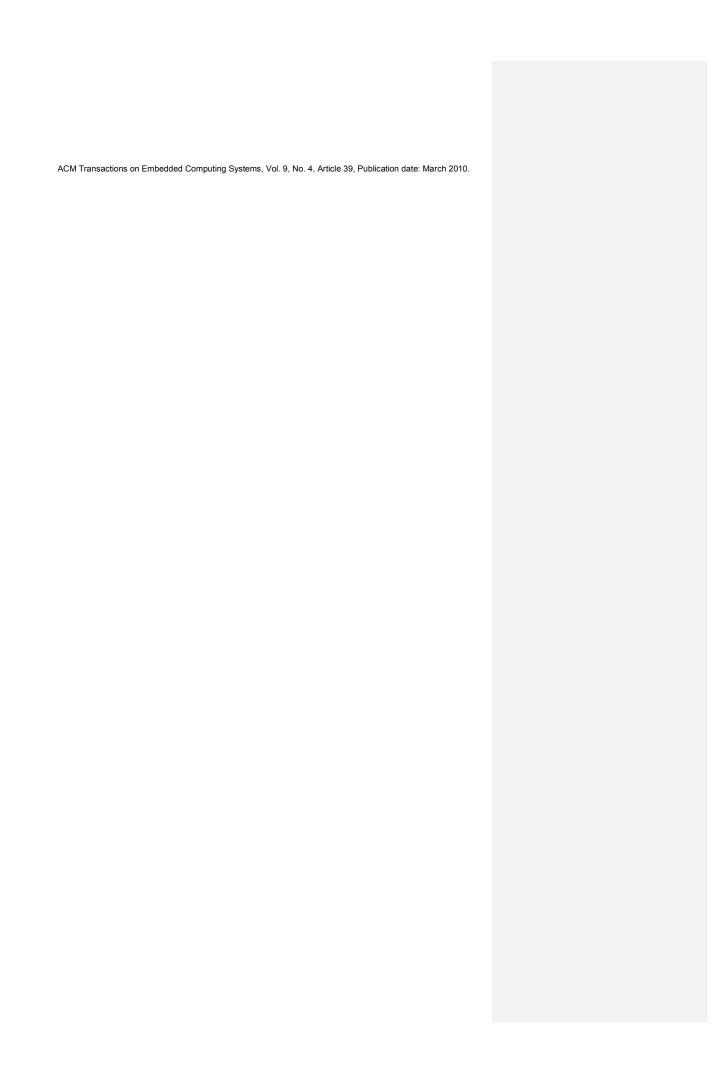
Formatted: Font: Italic
Formatted: Font: Italic

Formatted: Font: Italic

Formatted: Font: Italic

http://savannah.gnu.org/bugs/?29537

http://savannah.gnu.org/bugs/?33080



39:4 X. Niu et al.

```
public float foo(int a, int b, int c, int d){ //step 1 will
   cause an exception when b == c float x = (float)a /
   (b - c);

//step 2 will cause an exception when c < d float y
   = Math.sqrt(c - d);

return x+y;
}</pre>
```

Fig. 1. A toy program with four input parameters

the subject is suffereding multiple faults, especially when these faults can import masking effects.

The main contributions of this paper are:

- We studied the impact of the masking effects among multiple faults on the isolation of the failure-inducing combinations in SUT.
- We proposed a divide and conquer strategy of selecting test cases to alleviate the impact of these is effects.
- We designed an efficient test case searching method which can rapidly find a test case that does not trigger an unexpected fault.
- We conducted several empirical studies and showed that our strategy can assist FCI approaches to <u>achieveget</u> better performance <u>inon</u> identifying failure-inducing combinations in SUT with masking effects.

### 2. MOTIVATING EXAMPLE

For convenience, we This section constructed a small program example, for convenience to illustrate the benefitsment of our approach. Assume we have a method foo which has four input pa-rameters: a, b, c, and d. These types of these four parameters types are all integers and the values

that they can take are:  $v_a = \{7, 11\}$ ;  $v_b = \{2, 4, 5\}$ ;  $v_c = \{4, 6\}$ ;  $v_d = \{3, 5\}$ . The code detail code of the method is shown listed in Figure 1.

Considering Inspecting the simple code in Figure 1, we can find two potential faults: Efirst, in the step 1 we can get an *Arithmetic\_Exception* when b is equal to c, *i.e.*, b = 4 & and c = 4, that which makes division by zero. Second, another *Arithmetic\_Exception* will be triggered in step 2 when c < d, *i.e.*, c = 4 & and d = 5, which makes square roots of negative numbers. So the expected failure-inducing combinations in this example should be (-, 4, 4, -) and (-, -, 4, 5).

Traditional FCI algorithms do not consider the <u>code</u> detail of the <u>code</u>; instead, they apply black-box testing to test this program, i.e., they feed inputs to those programs and execute them to observe the result. The basic justification behind theose approaches is that the failure-inducing combinations for a particular fault <u>mustcan</u> only appear in those inputs that trigger this fault. As tTraditional FCI approaches aim at using as few inputs as possible to get the same (or <u>an</u> approximate) result as exhaustive testing, so the results derived from <u>an</u> exhaustive testing set <u>aremust be</u> the best that these FCI approaches can <u>achievereach</u>. Next, we will <u>showillustrate</u> how exhaustive testing works <u>toon</u> identifying the failure-inducing combinations in the program.

We first generate every possible inputs listed in the <u>Ccolumn "test inputs"</u> of Table II, and their execution results are listed in <u>the result Ccolumn "result"</u> of Table II. In this <u>Ccolumn, PASS</u> means that the program runs without any exception under the input in the same row. Ex 1 indicates that the program triggered an exception corresponding to the step 1 and Ex 2 indicates the program triggered an exception corresponding to the

Formatted: Font: Not Italic

Formatted: Font: Italic

Formatted: Font: Italic

Table II. test inputs and their corresponding result

id	test inputs	results	id	test inputs	result
1	(7, 2, 4, 3)	PASS	13	(11, 2, 4, 3)	PASS
2	(7, 2, 4, 5)	Ex 2	14	(11, 2, 4, 5)	Ex 2
3	(7, 2, 6, 3)	PASS	15	(11, 2, 6, 3)	PASS
4	(7, 2, 6, 5)	PASS	16	(11, 2, 6, 5)	PASS
5	(7, 4, 4, 3)	Ex 1	17	(11, 4, 4, 3)	Ex 1
6	(7, 4, 4, 5)	Ex 1	18	(11, 4, 4, 5)	Ex 1
7	(7, 4, 6, 3)	PASS	19	(11, 4, 6, 3)	PASS
8	(7, 4, 6, 5)	PASS	20	(11, 4, 6, 5)	PASS
9	(7, 5, 4, 3)	PASS	21	(11, 5, 4, 3)	PASS
10	(7, 5, 4, 5)	Ex 2	22	(11, 5, 4, 5)	Ex 2
11	(7, 5, 6, 3)	PASS	23	(11, 5, 6, 3)	PASS
12	(7, 5, 6, 5)	PASS	24	(11, 5, 6, 5)	PASS

Table III. Identified failure-inducing combinations and their corresponding  $\mathbf{E}\underline{\mathbf{e}}$ xception

Failure-inducing combinations	Exception
(-, 4, 4, -)	Ex 1
(-, 2, 4, 5)	Ex 2
(-, 3, 4, 5)	Ex 2

step 2. FromAccording to the data listed in Table II, we can determinefigure out that (-, 4, 4, -) must be the failure-inducing combination of Ex 1 as all the inputs that triggered Ex 1 contain this combination. Similarly, the combination (-, 2, 4, 5) and (-, 3, 4, 5) must be the failure-inducing combinations of the Ex 2. We listed these three combinations and their corresponding exceptions in Table III.

Note that in this case we did notn't get the expected result with traditional FCI approaches in this case. The failure-inducing combinations we geot for Ex 2 are (-,2,4,5) and (-,3,4,5) re-spectively instead of the expected combination (-,-,4,5). So why did we fail to getwe failed in getting the (-,-,4,5)? The reason lies in input 6: (7,4,4,5) and input 18: (11,4,4,5). These two in-puts contain the combination (-,-,4,5), but they didn't trigger the Ex 2, instead, Ex 1 was triggered.

Now let us get back to the source code of  $foo_{7}$  wWe can find that if Ex 1 is triggered, it will stop executing the remaining code and report the exception information. In another word, Ex 1 has a higher fault level than Ex 2, so that Ex 1 may mask Ex 2. Let us reexamine the combination (-,-,4,5) if we supposed that  $foundarder{input} 6$  and  $foundarder{input} 18$  should trigger Ex 2 if they didn't trigger Ex 1, then we can conclude that  $foundarder{input} 18$  should be the failure-inducing combination of the Ex 2, which is identical to the expected one.

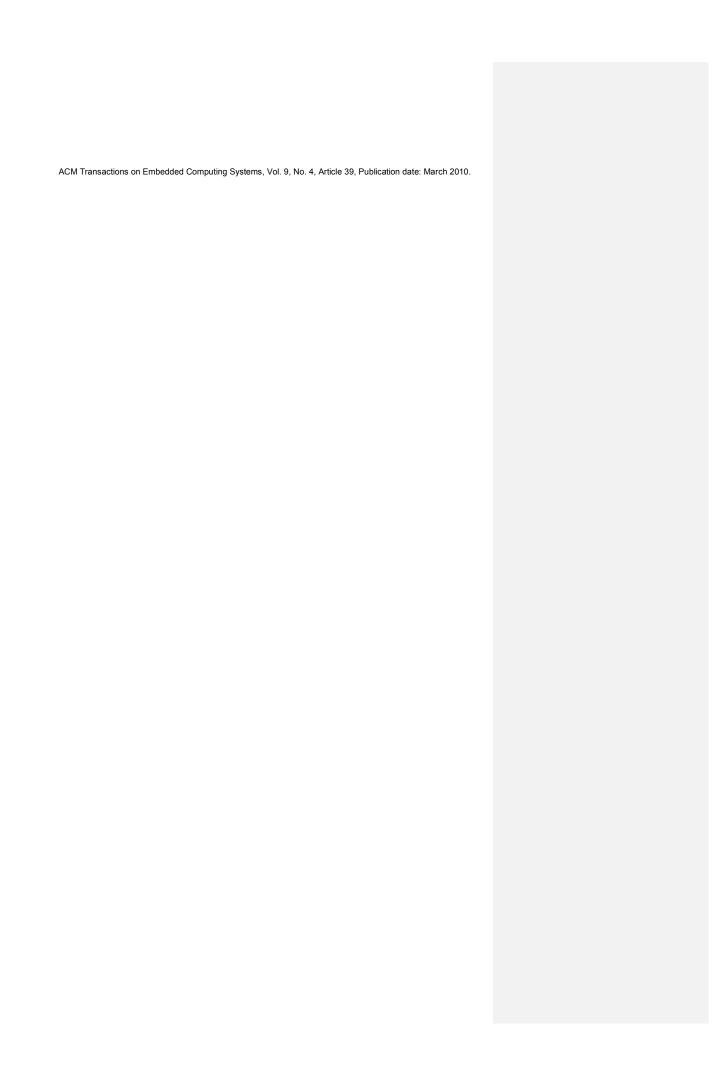
However, we cannot validate the supposition, i.e. that input 6 and input 18 should trigger Ex 2 if it they didn't trigger Ex 1, unless we have fixed the code that triggers Ex 1 and then re-executed all the test cases. So in practice, when we do not have enough resources to re-execute all the test cases again and again or can only dotake black-box testing, the more economical and efficient approach to alleviate the masking effect on FCI approaches is desired.

## 3. FORMAL MODEL

This section presents some definitions and propositions  $\underline{\text{forto-give}}$  a formal model  $\underline{\text{to}}$  solve the  $\underline{\text{for the-FCI}}$  problem.

## 3.1. Failure-causing Schemas in CT

Assume that the SUT is influenced by k parameters, and each parameter  $p_i$  has  $a_i$  discrete values from the finite set  $V_i$ , i.e.,  $a_i = |V_i|$  (i = 1,2,..k). Some of the definitions below were are originally defined in [Nie and Leung [2011b]].



39:6 X. Niu et al.

Definition 3.1. A test case of the SUT is an array of k values, one for each parameter of the SUT, which is denoted as a k-tuple  $(v_1, v_2,...,v_k)$ , where  $v_1 \in V_1, v_2 \in V_2 ... v_k \in V_k$ .

In practice, these parameters in the test case can represent many factors, such as input variables, run-time options, building options, or various combinations of them. We need to execute the SUT with these test cases to ensure the correctness of the software behaviour of the software.

We consider the fact that the abnormallyly executeding test cases to beas a fault. It can be a thrown exception, compilation error, assertion failure, or constraint violation. When faults are triggered by some test cases, we needwhat is desired is to determine figure out the cause of these faults;, and hence, some subsets of this test case mustshould be analysed.

Definition 3.2. For the SUT, the t-tuple  $(-,v_{k1},...,v_{kt},...)$  is called a t-value schema (0 < t $\leq k$ ) when some t parameters have fixed values and the others can take on their respective allowable values, represented as "-".

In effect a test case itself is a t-value schema, when t = k. Furthermore, if a test case contains a schema, i.e., every fixed value in the combination is in this test case, we say this test case hits the schema.

Definition 3.3. Let  $c_l$  be a l-value schema,  $c_m$  be an m-value schema in SUT, and l <  $\it m$ . If all the fixed parameter values in  $\it c_I$  are also in  $\it c_m$ , then  $\it c_m$  subsumes  $\it c_I$ . In this case, we can also say that  $c_l$  is a sub-schema of  $c_m$ , and  $c_m$  is a parent-schema of  $c_l$ , which can be denoted as  $c_l < c_m$ .

For example, in the motivation example section, the  $2\underline{two}$ -value schema (-, 4, 4, -) is a sub-schema of the 3three-value schema (-, 4, 4, 5), that is, (-,4,4,-) < (-,4,4,5).

Definition 3.4. If all test cases contain a schema, say c, and trigger a particular fault, say  $F_{-}$ , then we call this schema c the failure-causing schema for  $F_{-}$  Additionally, if none of the sub-schema of c is the failure-causing schema for F-, we then call the schema c the *Minimal Failure-causing Schema*, *i.e.*, the (MFS) for *F*-.

In fact, MFS is identical to the failure-inducing combinations we discussed previous-ly. Figuring itthis out can eliminate all details that are irrelevant to the cause of thefor causing the failure and, hence, facilitate the debugging efforts.

Some notions used later are listed below for convenient referencein the following for the convenience of reference:

- k: the number of parameters that influence the SUT.
- $V_i$ : the set of discrete values that the *i*th factor of the SUT can take.  $T^*$ : The exhaustive set of test cases for the SUT. For an SUT with k factors, and each factor can take  $|V^i|$  values, the number of this set of test cases  $T^*$  is  $\prod_{i < = k} |V^i|$ . factor can take |V| values, the number of this set of test cases  $T^*$  is
- L: the number of faults that contained in the SUT.
- $-F_m$ : the mth fault in the SUT: for different faults, we can differentiate them from their exception traces or other buggy information.
- $T_{F_m}$ : All the test cases that can trigger the fault  $F_m$ . T (c): All the test cases that can hit\_(contain) the schema c. Based on the definition of MFS, we know can learn that if schema c is MFS for  $F_m$ , then T(c) must be subsumed
- -I(T): All the schemas that are hit in a set of test cases T, i.e.,  $I(T) = t \in T^{I(t)}$ .

Formatted: Indent: Left: 0.18 cm, First line: 0.43 cm, Line spacing:

Formatted: Font: 10 pt

Formatted: Font: Italic

Formatted: Font: Italic

Formatted: Font: Italic

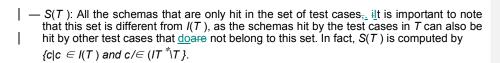


Table IV. Example of the proposition 3.5

	С
	(0, -, - , -)
С	T (c)
(0, 0, - , -)	(0, 0, 0, 0)
T (c)	(0, 0, 0, 1)
(0, 0, 0, 0)	(0, 0, 1,0)
(0, 0, 0, 1)	(0, 0, 1, 1)
(0, 0, 1,0)	(0, 1, 0, 0)
(0, 0, 1, 1)	(0, 1, 0, 1)
	(0, 1, 1,0)
	(0, 1, 1, 1)

—  $\mathcal{C}(T)$ : the minimal schemas only hit by the set of test cases T, this set is the sub-set of S(T), which is defined as  $\langle c/c \in S(T) \rangle$  and  $\langle c/c \in S(T) \rangle$ .

PROPOSITION 3.5. For evalue schema  $c_l$  and m-value schema  $c_m$ , if  $c_l < c_m$ , then we can have all the test cases his  $c_m$  that must also hit  $c_l$ , i.e.,  $T(c_m) \subset T(c_l)$ .

PROOF Suppose  $\forall t \in T(c_m)$ , we have that t hits  $c_m$ . Then as  $c_l \prec c_m$ , it must have t must also hitting  $c_l$ . This is because all the elements in  $c_l$  are also in  $c_m$ , which are contained in the test case t. Therefore, we get  $t \in T(c_l)$ . Thus  $t \in T(c_m)$  implies  $t \in T(c_l)$ , so it follows that  $T(c_m) \subset T(c_l)$ .  $\square$ 

Table IV illustrates an example of the SUT with four binary parameters ( $\frac{1}{2}$  unless otherwise specified, the following examples also assume the SUT with binary parameters). The left column lists the schema (0,0,-,-) as well as all the test cases that hit this schema, while the right column lists the test cases for schema (0,-,-,-). We can observe that (0,-,-,-) and the the set of test cases which hit (0,-,-,-) contains the set that hits (0,0,-,-).

Proposition 3.6.

For any set T of test cases of a SUT, we can always get a set of minimal schemas  $\mathcal{Q}(T) = \langle c \not/ c \vec{J} \in \mathcal{Q}(T); s:t:c \prec c \rangle$ , such that,

$$T = \bigcup_{\mathbf{c} \in \mathcal{A}T} T(\mathbf{c})$$

PROOF. We prove this by producing this set of schemas.

We have denoted the exhaustive test cases for SUT as  $T^*$  and let  $T^*|T$  be the test cases that  $\underline{are}$  in  $T^*$  but not in T. It is obviously  $\forall t \in T_{\underline{-}}, \underline{w} \ \underline{W} \underline{e}$  can always find at least one schema which hit by t, i.e.,  $\underline{e} \ l$ , such that  $\underline{e} \ l$ . Specifically, at least the test case t itself as schema holds.

Then we collect all the satisfied schemas which only hit by the test cases in the test cases of , which can be denoted as: S''  $(f \in T'')$   $C \in T'$   $C \in$ 

 $c; s:t:; c' \in S(T)$ . For this set, we can still have  $c \in M(S(T))$  T(c) = T. We also prove this

Table V. Example of the minimal schemas

Τ	S(T)	C(T)
(0, 0, 0, 0) (0, 0, 0, 1) (0, 0, 1, 0)	(0, 0, 0, 0) (0, 0, 0, 1) (0, 0, 1, 0) (0, 0, 0, -)	(0, 0, 0, -) (0, 0, -, 0)
	(0, 0, -, 0)	L
1.1		1.1

by two steps, first and obviously,  $\neg c \in M(S(T))$   $T(c) \subset T(C)$ .  $c \in S(T)$  T(c). Then, we just need to (T) M(C(T)), we can have some c $\forall \in S$ In fact Ü  $\cup$  SM(S(T)), such that  $c \prec c$ . According to the Proposition 3.5,  $T(c) \subset T(c)$ . So for any test case  $t \in _{c \in S(T)} T(c)$ , as we have either  $\exists c \in S(T) | M(S(T))$ ; s:t:;  $t \in T(c)$  or  $\exists c \in S(T) | M(S(T))$ M(S(T)); s:t:;  $t \in T(c)$ . Both cases can deduce  $t \in T(c)$  $c M((T)) T(c). So, c (T) T(c) \subset$  $c \in M(S(T))$ U ∈s U ∈ S  $c \in M(S(T))$  T(c), and M(S(T)) is the set of schemas that holds Hence,  $c \in S(T)$  T(c) =this proposition

For example,  $\frak{t}$  Table V lists the  $\frak{S}(T)$  and minimal schemas  $\frak{C}(T)$  for the set of test cases T. We can see that for any other schemae not in  $\frak{C}(T)$ , either  $\frak{we}$  can  $\frak{we}$  find a test case not in T hit the schema,  $\frak{e.g.}, (0,0,-,-)$  with the test case (0,0,1,1) not in T-, or that is the parent schema of one of the two minimal schemas,  $\frak{e.g.}, (0,0,0,0)$  the parent schema of both (0,0,0,-) and (0,0,-,0).

Let  $T_{F_m}$  denotes the set of all the test cases triggering fault  $F_{m^-}$ , then  $\mathcal{L}(T_{F_m})$  actually is the set of MFS of  $F_m$  by definition of MFS.

From the construction process of  $\mathcal{Q}T$ ), one observation is that the minimal schemas  $\mathcal{Q}(T)$  is the subset of the the-schemas set  $\mathcal{S}(T)$ , i.e.,  $\mathcal{Q}(T) \subset \mathcal{S}(T)$ , and for any schema in  $\mathcal{S}(T)$ , it either belongs to  $\mathcal{Q}(T)$ , or is the parent schema of one element of  $\mathcal{Q}(T)$ . Then, we can have the following proposition.

PROPOSITION 3.7. For any test cases set T and schema c, if any test case hit c is in the set T, i.e.,  $T(c) \subset T$ , then it must be that  $c \in S(T)$ .

PROOF. We first have  $c \in \mathcal{C}(T(c))$ , this is obviously and in fact the minimal schemas for the test cases set T(c) only contain one schema, which is exactly c itself. As discussed previously, we have  $\mathcal{C}(T(c)) \subset \mathcal{S}(T(c))$ , so it must be  $c \in \mathcal{S}(T(c))$ .

Then as  $T(c) \subset T$ , it follows  $S(T(c)) \subset S(T)$  by definition. In detail,  $S(T(c)) = \langle c/c \in I(T(c)) \rangle$  and  $C \in I(T^*|T(c))$ , so  $S(T(c)) \subset \langle c/c \in I(T) \rangle$  and  $C \in I(T^*|T(c))$ , which is exactly S(T).

So as  $c \in S(T(c))$  and hence  $c \in S(T)$ .

For two different sets of test cases, there exist some relationships between the minimal schemas of these two sets that, which varyies in the relevancy between with respect to thise two different sets of test cases. In fact, there are three possible associations between two different sets of test cases: inclusion, disjointed, and intersection, as listed in figure 2. We didn't not list the condition forthat two sets that are identical, because on that condition the minimal schemas must also be identical. To discuss the properties of the relationship of the minimal schemas between two different sets of test cases is important as we willcan learn later the masking effects between multiple faults that will make the MFS identifying pro-cess work incorrectly works, i.e., these FCI approaches may isolate the minimal schemas for the set of test cases which are biased from the expected failing set of test cases. And these properties can help us to figure out the

Formatted: Font: Italic

Formatted: Font: Italic

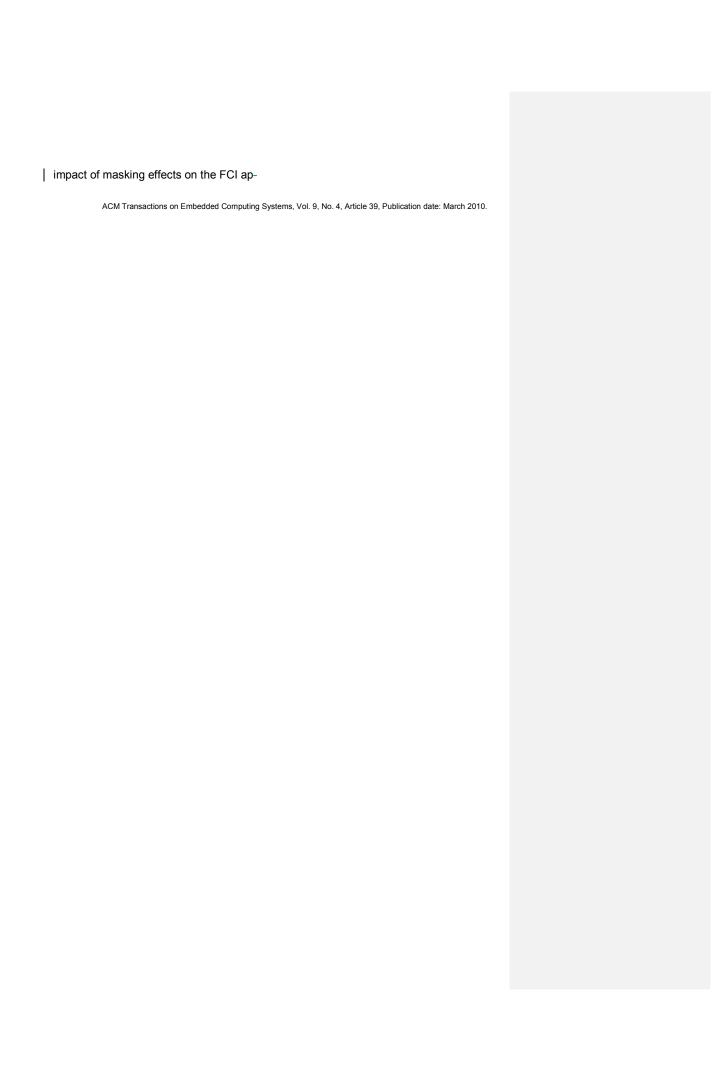


Table VI. Example of the scenarios

		Tį	$T_{k}$
$T_I$	$T_{k}$	(0, 0, 0)	(0, 0, 0)
(0, 0, 0)	(0, 0, 0)	(0, 0, 1)	(0, 0, 1)
(0, 0, 1)	(0, 0, 1)	(0, 1, 0)	(0, 1, 0)
(0, 1, 0)	(0, 1, 0)		(1, 1, 0)
	(0, 1, 1)		(1, 1, 1)
$C(T_I)$	$C(T_k)$	$C(T_I)$	$C(T_k)$
(0, 0, -)	(0, -, -)	(0, 0, -)	(0, 0, -)
(0, -, 0)		(0, -, 0)	(0, -, 0)
			(1, 1, -)

proaches. Next, we will separately discuss the relationship between minimal schemas under the three conditions.

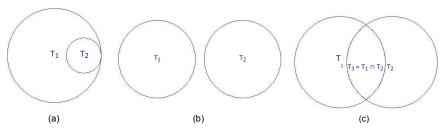


Fig. 2. Test sSuites relationships

### 3.2. Inclusion

It is the first relationship corresponding to Fig. 2(a). We can have the following proposition with two sets of test cases which have  $\frac{1}{2}$  inclusion relationship.

PROPOSITION 3.8. For two sets of test cases  $T_l$  and  $T_k$ , assume that  $T_l \subset T_k$ . Then, we have

$$\forall c_l \in \mathcal{C}(T_l)$$
 either we have  $c_l \in \mathcal{C}(T_k)$  or have  $\exists c_k \in \mathcal{C}(T_k)$ ; s:t:;  $c_k \prec c_l$ :

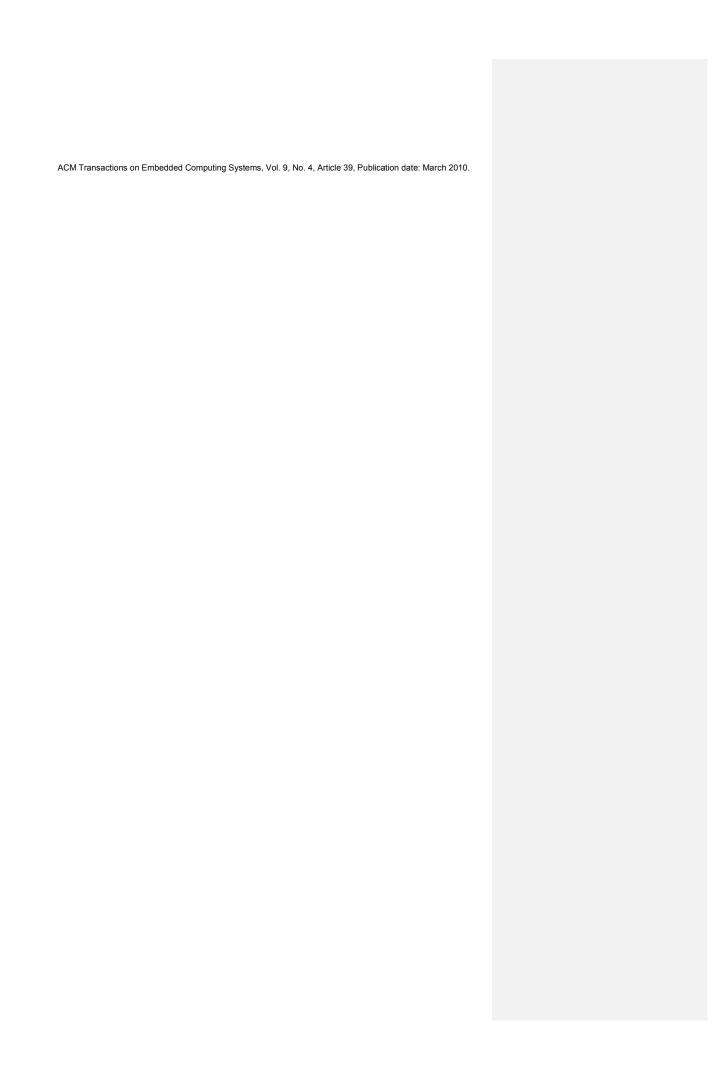
PROOF. Obviously for  $\forall c_l \in \mathcal{Q}(T_l)$  we can get  $T(c_l) \subset T_l \subset T_k$ . According to the proposition 3.7, we can have  $c_l \in S(T_k)$ . So this proposition holds as the schema in  $S(T_k)$  either is also in  $\mathcal{Q}(T_k)$ , or must be the parent of some schemas in  $\mathcal{Q}(T_k)$ .  $\square$ 

Based on this proposition, in fact, the schema  $c_k \in \mathcal{C}(T_k)$  remains with the following three possible relationships with  $\mathcal{C}(T_l): (1) \ c_k \in \mathcal{C}(T_l)$ , or  $(2) \ \exists c_l \in (T_l)$ ; s:t:;  $c_k \prec c_l$  or  $c_k = c_l$ ; or  $c_l \prec c_k$ . For the third case, we call  $c_k$  is intelevant to  $(T_l)$ 

We illustrate these scenarios in Table VI. There are two parts in this table, with each part showings two sets of test cases:  $T_l$  and  $T_k$ , which have  $T_l \subset T_k$ . For the left part we can see that in the schema in  $\mathcal{C}(T_l)$ : (0, 0, -) and (0, -, 0), both are the parent of the schema of the one in  $\mathcal{C}(T_k)$ : (0, -, -). While for the right part, the schemas in  $\mathcal{C}(T_l)$ : (0, 0, -) and (0, -, 0) are both also in  $\mathcal{C}(T_k)$ . Furthermore, one schema in  $\mathcal{C}(T_k)$ : (1, 1, -) is irrelevant to  $\mathcal{C}(T_l)$ .

### 3.3. Disjoint

This relationship is correspondsing to the Fig. 2(b), For two different sets of test cases, one obvious propertyies is listed as follows:



39:10 X. Niu et al.

 $\begin{array}{ccc} & & \text{VII.} \ \underline{\text{Disjoint}} \\ \text{Table} & & \underline{\textbf{Ee}} \text{xample} \underline{\textbf{s}} & \text{of} \\ \underline{\text{disjoint examples}} & & \end{array}$ 

$T_I$	$T_{k}$
(0, 0, 0) (0, 1, 0)	(1, 0, 0) (1, 0, 1)
(0, 1, 0)	(1, 0, 1)
C(T <sub>I</sub> )	$C(T_k)$
(0, -, 0)	(1, 0, -)
	(1, -, 0)

Proposition 3.9.

can learn that  $T \cap 1$ 

This propert<u>yies</u> tells that the minimal schemas of two disjointed test cases should be irrelevant to each other\_T Table VII list the shows an example of this scenario\_T www e can learn infrom this table that for two different test cases sets  $T_1, T_K$ , their minimal schemas, i.e., (0, -, 0) and (1, 0, -), (1, -, 0), respectively, are irrelevant to each other.

#### 3.4. Intersect

This relationship is correspondsing to the Fig. 2(c). This scenario is the most common scenario for two sets of test cases, but is also the most complicated scenario for analysis.

wWe assume that  $T_1$   $T_2$  3 is as depicted in Fig. 2(c). Then, we can have the following preperties:

PROPOSITION 3.10. For two intersecting sets of test cases  $T_1$  and  $T_2$  (this two\_set is neither identical nor do the members subsumeing each other), it must have  $\exists c_1 \in \mathcal{Q}(T_1)$  and  $c_2 \in \mathcal{Q}(T_2)$ . s.t.  $c_1$  and  $c_2$  are irrelevant.

PROOF. Firstly, -we -can -learn -that - $\mathcal{Q}(T_1 \mid T_3)$  are irrelevant to  $\mathcal{Q}(T_2 \mid T_3)$ , as  $(T_1 \mid T_3)$   $(T_2 \mid T_3) = \emptyset$ .

or bethe parent schemas  $As \ \mathcal{A}_{1} \ | \ 3$  is either identical to some schemas in  $\mathcal{C}$  of them, then if some of them are identical, i.e.,  $\exists c \ ; s:t:; c \in \mathcal{A}(T_1 \ | T_3)$  and  $c \in \mathcal{A}(T_1)$ , then these schemas c must be irrelevant to  $(T_2)$  as  $(T_1 \ | T_3)$  is identical to some schemas in  $\mathcal{A}(T_2)$ .

Next, if both  $(T_1|T_3)$  and  $(T_2|T_3)$  are parent schemas of some of  $(T_1)$  and  $(T_2)$ , respectively, without loss of generality, we let  $c_1 \prec c_{1-3}$ ,  $(c_{1-3} \in (T_1|T_3)$  and  $c_1 \in (T_1)$ ) and  $c_2 \prec c_{2-3}$ ,  $(c_{2-3} \in (T_2|T_3)$  and  $c_2 \in (T_2)$ ). Then, these corresponding sub-schemas in  $(T_1)$  and  $(T_2)$ , i.e.,  $(C_1)$  and  $(C_2)$  respectively, must also be irrelevant to each other.

This is because  $T(c_1) \supset T(c_1-s)$  and  $T(c_2) \supset T(c_1-s)$ . And as  $T(c_1-s) \supset T(c_2-s) = \emptyset$ , so  $T(c_1)$  and  $T(c_2) \supset T(c_2-s) = \emptyset$ , so  $T(c_1) \supset T(c_1-s) = \emptyset$ .

For example, Table VIII shows two test cases that interact with each other at test case (1,0,0), but their minimal schemas, (1,0,-) and (1,-0), respectively, are irrelevant to each other.

3.11. For two intersecting set of test cases  $T_1$  and  $T_2$ , and let  $T_3$  =

|  $T_1$   $T_2$ , if we can find  $\exists c_1 \in \mathcal{Q}(T_1)$  and  $c_2 \in \mathcal{Q}(T_2)$ , s.t.,  $c_1$  is identical to  $c_2$ ,  $\mp \underline{t}$ hen it must have  $c_1 = c_2 \in \mathcal{Q}(T_3)$ 

PROOF. As we getsee that the ijdentical schema must share the identical test cases, then the only identical test cases between T and  $T_2$  is  $T_1$  and  $T_2$  is  $T_1$ . So the only possible

identical schemas between  $\mathcal{L}(T_1)$  and  $\mathcal{L}(T_2)^1$  is in  $\mathcal{L}(T_3)$ .

Formatted: Font: Italic

Table VIII. Example of Intersection by irrelevantexamples

<i>T</i> <sub>1</sub>	<i>T</i> <sub>2</sub>
(1, 0, 0)	(1, 0, 0)
(1, 0, 1)	(1, 1, 0)
C(T <sub>1</sub> )	$C(T_2)$
(1, 0, -)	(1, -, 0)

Table IX. Example of Intersection by identical examples

<i>T</i> <sub>1</sub>	T <sub>2</sub>	$T_3 = T_1$ $T_2$
(0, 1, 0)	(0, 0, 1)	(1, 1, 1)
(1, 1, 1)	(1, 1, 0)	(., ., .,
	(1, 1, 1)	
$C(T_1)$	$C(T_2)$	C(T <sub>3</sub> )
(-, 1, 0)	(0, 0, -)	(1, 1, -)
(1, 1, -)	(1, 1, -)	

Table X. Example of Intersect<u>ion</u> by subsume<u>ing</u> examples

T <sub>1</sub>	T <sub>2</sub>	$T_3 = T_1$ $T_2$
(0, 1, 0) (1, 0, 0)	(0, 0, 0) (1, 0, 0)	(1, 0, 1)
(1, 0, 1)	(1, 0, 1)	(1, 1, 0)
(1, 1, 0)	(1, 1, 0) (1, 1, 1)	
C(T <sub>1</sub> )	$C(T_2)$	C(T <sub>3</sub> )
(-, 1, 0) (1, 0, -)	(-, 0, 0) (1, -, -)	(1, 0, -) (1, -, 0)
(1, -, 0)	(-, , ,	(1, , 1)

) isare

We must know that this proposition holds when some schemas in  $(T T identical to some schemas in <math>\mathcal{C}_{1} 1$  and  $\mathcal{C}_{2} 1$ .

For example, Table IX shows two test cases <u>that</u> interact <u>with</u> each other at test cases (1,1,0) and (1,1,1), and they have identical minimal schemas, <u>i.e.</u>, (1,1,-), which is al-so the minimal schema in  $\mathcal{C}(T_3)$ .

PROPOSITION 3.12. For two intersecting sets of test cases  $T_1$  and  $T_2$ , and let  $T_3 = T_1$ ,  $T_2$ , if there we can find  $\exists c_1 \in \mathcal{Q}(T_1)$  and  $c_2 \in \mathcal{Q}(T_2)$ , s.t.,  $c_1$  is the parent-schema of  $c_2$ , then it must have  $c_1$  ( $T_3$ ), (and vice versa).

 $\cap$ 

PROOF. We have proved previously if two schemas have <u>have a subsuminges</u> relationship, then their test cases must also have <u>an inclusion relationship</u>. And as the only inclusion relationship between  $T_1$  and  $T_2$  is that  $T_3 \subset T_1$  and  $T_3 \subset T_2$ . So the parent schemas must be in  $\mathcal{L}(T_3)$ .  $\square$ 

It is noted that this proposition holds when holds when some schema in  $\mathcal{C}(T_3)$  is identical in  $\mathcal{C}(T_1)$  (or  $\mathcal{C}(T_2)$ ), and simultaneously the same schemas in  $\mathcal{C}(T_3)$  must be the parent-schema of the minimal schemas of another set of test cases, *i.e.*,  $\mathcal{C}(T_2)$  (or  $\mathcal{C}(T_3)$ ).

Table X illustrates this scenario $_{\bar{\tau}}$  in which $_{\bar{\tau}}$  the minimal schemas of  $T_1$ : (1,0,-),(1,-,0),which isare also the schemas in  $\mathcal{C}(T_3)$ , is the parent schema of the minimal schema of  $T_2$ : (1 - -)

It is noted that theseis three conditions can simultaneously appears when two sets of

Formatted: Font: Italic



39:12 X. Niu et al.

### 3.5. Identifying the MFS

According to thisese analysis, we can determine  $C(T_{Fm})$  actually is the set of failure-causing schemas of  $F_m$ . Then in theory, if we want to accurately figure out the MFS in the SUT, we need to exhaustively execute each possible test case, and collect the failing test cases  $T_{\mbox{\it Fm}}$  . This is impossible in practice, especially when the testing space is verytoo large.

So for traditional FCI approaches, they need to select thea subset of the exhaustive test cases, and then either use antake some assumption to make prediction of the remaining test cases or just give a suspicious ranking. As giving a suspicious ranking can also be regard as a special case of making a prediction (with computing the possibility), so we next only formally describe the mechanism of FCI approaches belonging to the first type. We refer

 $\underline{to}$  the observed fail $\underline{eding}$  test case  $\underline{asto}$   $T_{failobserved}$ , and refer  $\underline{to}$  the remaining  $\underline{failed}$  test cases based on prediction as the approach predict to be failed as  $T_{failpredicted}$ . We also denote the actually entire failing test cases as  $T_{fail}$ . Then the MFS identified by FCI approaches can be depicted as:

For each FCI approach, the way it predicts the T according to observed faileding test cases varies; further-more, as the test cases it generates are different,

faileding test cases observed by different test cases, *i.e., Tfailobserved* also varies. We takeoffer an example using the OFOT approach to illustrate this formula.

Suppose that the SUT has 3 parameters, each of which can take 2 values. And assume the test case (1, 1, 1) failed. Then, we can describe the FCI process as shown in Table XI. In this table, test case *t* failed, and OFOT mutated one factor of the *t* one time to generate new test cases:  $t_1$ ;  $t_2$ ;  $t_3$ , It found the the  $t_1$  passed, which indicates that this test case breaks the MFS in the original test case t. So, the (1,-,-) should be one failure-causing factor, and as the other mutating processes all failed, this which means no other failure indusing factors are the other mutating processes. failure-inducing factors were broken, the MFS in t is (1,-,-).

Now let us explain this process with our formal model. Obviously the  $T_{failobserved}$  is  $\{(1,1,1),(1,0,1),(1,1,0)\}$ . And as having found, (0,-,-) broke the MFS, hence by theo-

ry\_[Nie and Leung 2011a], all the test cases that contain (0,-,-) should pass the test cases (This conclusion is built on the assumption that the SUT just contains one failure-causing schema). As a result, (0,1,1),(0,0,1),(0,1,0),(0,0,0) should pass the testing-ing. Further, as obviously the test case either passes or fails the testing (we label the skipping the testing as a special case of failing), so the remaining test case (1,0,0), will be predicted to failas failing,

j.e., Tfailpredicted is {(1,0,0)}. Takening together, the MFS using the OFOT strategy can be de-scribed as:  $C(T_{failobserved}, T_{failpredicted}) = C(\{(1, 1, 1), (1, 0, 1), (1, 1, 0), (1, 0, 0)\}) = (1, -, -)$ 

which is identical to the

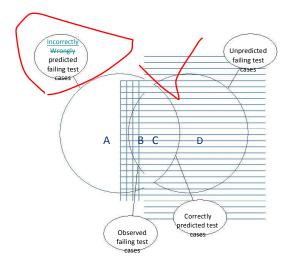
Table XI. OFOT with our strategy

	orig	ginal	test	case	Outcome
	t	1	1	1	Fail
•		0	bserv	red	
	1	0	1	1	Pass
	2	1	0	1	Fail
	tз	1	1	0	Fail
		р	redic	ted	
	<i>t</i> <sub>4</sub>	0	0	1	Pass
	$t_5$	0	1	0	Pass
	t <sub>4</sub> t <sub>5</sub> t <sub>6</sub>	1	0	0	Fail
	t7	0	0	0	Pass

Formatted: Font: Italic

Formatted: Justified, Indent: First line: 0.35 cm, Line spacing: Multiple 0.83 li, Don't allow hanging punctuation

Similarly, other FCI approaches can also be modeled into this formal description. We will not  $\underline{\text{discuss}}$  in detail  $\underline{\text{discuss}}$ -how to model each FCI approach as this is not the point of this paper. It is noted that the test cases FCI predicts to be failing  $\underline{\text{isare}}$  not always identical



**Formatted:** None, Space Before: 0 pt, Don't keep with next, Don't keep lines together

Fig. 3. gGenerally FCI model of FCI

to the actually failing test cases. In fact, we can generally depict the process of FCI approaches as shown inlike Fig. 3.

We can see in Fig.  $3_{\tau}$  that \_area A denotes the test cases that should <u>havebe</u> passed testing <u>but were cases while</u> it predicted to be failed <u>ones</u>, area B depicts the test cases that the approach observed to be failed test cases, area C refers to the failed test cases that <u>were not doesn't to be</u> observed <u>to be</u> but <u>werebe</u> predicted to be failed test cases and area D <u>showsillustrates</u> the failed test cases that <u>are</u> neither <u>to be</u> observed nor <u>to be</u> predicted. This figure is actually one sample of the condition <u>in whichthat</u> two sets of test cases intersect with each other, in specific,

areas 
$$B$$
  $C = T_1$  area  $D$   $B$   $C = T_2$  and area  $B$   $C = T_1$   $T_2 = T_3$ .

Tearned previously that this scenario makes the schemas identified in  $C = T_1$  biased from

the expected MFS in  $T_2$ ; specifically, they, in specific, their must be irrelevant schemas between  $C(T_1)$  and  $C(T_2)$ , which means that the FCI approach will identify some minimal schemas that areis irrelevant to the actual MFS, and must ignore some actual MFS. Moreover, under the appropriate conditions listed in propositions 3.11 and 3.12, FCI may identify the identical schemas or parent-schema or sub-schema of the actual MFS. So in order—to identify the schemas as accurately as possible, the FCI approach needs to make  $T_1$  as similar as possible to  $T_2$ ; specifically, it must makes area B and area C as large as possible, and make area A as small as possible.

However, even though each FCI approach tries its best to identify the MFS as accurate as possible, masking effects raised from the test cases will resultmake in their efforts being in vain. We next will discusses the masking problem and how it affects the FCI approaches.

# 4. MASKING EFFECT

Definition 4.1. A masking effect is thean effect that results when while a test case t hits an MFS for a particular fault, but the however, t does not didn't trigger the expected fault because another fault was triggered ahead of it that which prevents t from being to be normally checked.

Taking the masking effects into account, when identifying the MFS for a specific fault,

say,  $F_m$ , we should not ignore these test cases which should have triggered  $F_m$  if ACM Transactions on Embedded Computing Systems, Vol. 9, No. 4, Article 39, Publication date: March 2010.

Table XII. mMasking effects for exhaustive testing

<i>T</i> <sub>1</sub>	mask(1)	$T_*$
(1, 1, 1, 1)	(1, 1, 0, 0)	(0, 1, 0, 0)
(1, 1, 1, 0) (1, 1, 0, 1)	(0, 1, 1, 1)	(0, 0, 0, 0) (1, 0, 0, 0)
(1, 1, 0, 1)		(1, 0, 1, 1)
		(0, 0, 1, 1)
actual MFS for 1	regard as one fault	distinguish faults
1 mask(1)	1 mask(1) T*)	C(T <sub>1</sub> )
0	(-, -, 0, 0) U	(1, 1, -, 1)
(-, 1, 1, 1)	(1, 1, -, -)	(1, 1, 1, -)
	(-, -, 1, 1)	

they didn't trigger other faults. We call these test cases  $T_{mask(Fm)}$ . Hence, the MFS for fault  $F_m$  should be  $(T_{Fm} \dots Y_{mask(Fm)})'$ 

fault  $F_m$  should be  $(T_{Fm} | f_{mask(F_m)})$ . As an example, in the motivation example in (7,4,4,5),(11,4,4,5), So the MFS for Ex2 is  $C(T_{FEx \ 2} | f_{mask(FEx \ 2)})$ , which is (-,-,4,5). In practice with masking effects, however, it is

the MFS, unless we fix some bugs in the SUT and re-execute the test cases to figure  $\max_{mask(F_m)}$ 

In effect for traditional FCI approaches, without the knowledge of  $T_{mask(Fm)}$ , only two strategies can be adopted when facing the multiple faults problem. We will sepa-rately analyse the two strategies under exhaustive testing conditions and normal FCI testing conditions.

# 4.1. mMasking effects for exhaustive testing

4.1.1. Regarded as one fault. The first one is the most common strategy, <u>as it doesn't not</u> dis-tinguish the faults, <u>i.e.</u>, <u>it treatsregard</u> all <u>of the types of faults as one fault-failure</u>, <u>and</u> others as pass.

With this strategy,  $\mp$ the minimal schemas we identify are the set the number of all the faults in the SUT. Obviously,  $T_{Fm}$   $T_{mask(F_m)} \subset C$  this case, by Proposition 3.8. some schemas we get may the set C this case, by Proposition 3.8. some schemas we get may C

this case, by Proposition 3.8, some schemas we get may the actual MFS, or be irrelevant to the actual MFS.

As an example, consider the test cases in Table XII. In this example, assume we need to characterize the MFS for error  $1_{\underline{.}\underline{.}\underline{.}}$  aAll the test cases that triggered error 1 areis listed in the column  $T_{1\underline{.}\underline{.}}$  similarly, we list the test cases that triggered other faults in column  $T_{mask(1)}$  and  $T_{\underline{*}}$  respectively, in which the former masked the error 1, while the latter  $\underline{did}$  not. Actually the MFS for error 1 should be (1,1,-,-) and (-,1,1,1) as we listed them in the column actual MFS for 1. However, when we use thetake\_regard as one fault strategy, the minimal schemas we geter will be (-,-,0,0), (1,1,-,-), (-,-,1,1), in which the (-,-,0,0) is irrelevant to the actual MFS for error 1, and the (-,-,1,1) is the sub-schema of the actual MFS (-,1,1,1).

4.1.2. Distinguishing faults. Distinguishing the faults by the exception traces or error code can help make relate the MFS related to a particular fault. Yilmaz in [Yilmaz et al. 2013] proposed the multiple-class failure characterizing method instead of the ternary-class approach to make the characterizing process more accurately. Besides, other approaches can also be easily extended with this strategy forte be applied on SUT application with multiple faults. U

This strategy focuses on identifying the set of  $C(T_{F_m})$ , and as  $T_{F_m}T_{mask(F_m)}\supset T_{F_m}$ , con-sequently, some schemas that get through this strategy may be the parent-schema of some

MFS. Moreover, some MFS may be irrelevant to the schemas we get with this strategy, which means this strategy will ignore these MFS.

Formatted: Font: Italic

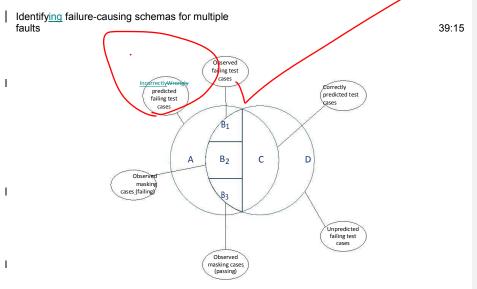


Fig. 4. FCI with masking effects

For the simple example in Table XII, when we useing this strategy, we will get the minimal schemas (1, 1, -, 1) and (1, 1, 1, -), which are both the parent schemas of the actual MFS (1,1,-,-), and we will observe that there is no schemas gotten by this strategy have any relationship with the actual MFS (-,1,1,1), which means they were ignored. it ignored the schema.

It is noted that, the motivation example in section 2 actually adopted this strategy, so we see that which made the schemas identified for Ex 2: (-,2,4,5), (-,3,4,5) are the parent-schemas of the correct MFS(-,-,4,5).

## 4.2. Mmasking effects for FCI approaches

With masking effects, the scenario of traditional FCI approaches is a bit more complicated than the previous two exhaustive testing scenarios, which can beand is depicted in the Figure 4. In this figure, areas A, C and D areis the same as in Figure 3, and area B is divided into three sub-areas, in which  $B_1$  is still represents the observed faileding test cases for the current analysed fault, area  $B_2$  represents the test cases that triggered other faults which masked the current fault, and area  $B_3$  is represents the test cases that triggered other faults which did not mask the current fault.

With this model, if we have known which test cases mask the expected fault, <u>i.e.</u>, <u>if we have fig-ured out the B2 and B3 areas</u>, then the schemas that <u>the FCI</u> approach will identify can be

described as  $C(A B_1 B_2 C)$ . We next denote this result as knowing masking effects. However, as

involvement. Correspondingly, when <u>using thetaking</u> regard as one fault strategy, the

ditional FCI identify is are  $C(A \ B_1 \ B_2 \ B_3 \ C)$ . And for the distinguishing faults strategy, the MFS is  $_{C}(A \ B \ C)$ . Next, we will respectively discuss the influence of masking

4.2.1. <u>Using the Taking</u> regard as one fault strategy. For the first strategy: regard as one fault, the impact of masking effects on FCI approaches can be described as <u>shown in</u> Figure 5. To under-stand the content of this figure, let us <u>goet</u> back to the relationship between the minimal schemas of two different sets of test cases. For the <u>knowing masking effects</u> condition, the result identified by <u>the FCI</u> approach, <u>i.e.</u>,

C(A

B<sub>1</sub>

B<sub>2</sub>
C), is one case of the <u>inter-terms</u>

B<sub>2</sub> C), is one case of the *inter-*

 $\ \ \cup$   $\ \cup$   $\ \cup$   $\ \cup$   $\$   $\$  | parent-schema, sub-schema, <u>is irrelevant to the actual MFS. And if we then apply the regard</u>

39:16 X. Niu et al.

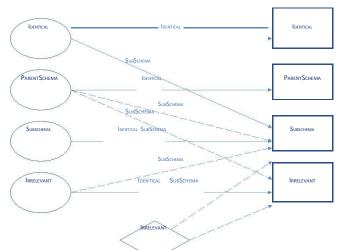


Fig. 5. mMasking effects influence on FCI <u>using</u>with regard as one

as one fault, the minimal schemas we getet are  $C(A \ B_1 \ B_2 \ B_3 \ C)$ . Obviously, we the minimal schema gottenet by this have  $A \ B_1 \ B_2 \ B_3 \ C \supset A \ B_1 \ B_2 \ C$ . So so is either the sub-schema or identical to some schemas from the ones gotten by this partial schema or identical to some schemas from the ones gotten by the sub-schema or identical to some schemas from the ones gotten by this partial schema or identical to some schemas from the ones gotten.

known masking effects, or exist some schemas irrelevant to all of them. Taking these two properties together, we will get what is shown in Figure 5.

The ellipses in the left column of this figure illustrated the relationship between the schemas identified under the *knowing masking effects* condition with the actual MFS, which includes the four possibilities: identical, sub-schema, parent-schema, and irrelevant. For each relationship in this part, without of loss of generality, we consider

 $c_{origin}$  and  $c_{m,\tau}$   $c_{origin}$  is the minima schema gotten by knowing masking effects, and  $c_m$  is the actual MFS. Then, when we apply the regard as one fault strategy, we may get some

schemas which are identical or sub-schema of  $c_{origin}$ , say  $c_{new}$  s.t.,  $c_{new} = c_{origin}$  or  $c_{new} < c_{origin}$ . In this figure, we use the directed line to represent these two transfor-mations with different labels in each line. As for the schemas  $c_{new}$  that are is irrelevant to

all the  $c_{origin}$ , we in the bottom of this figure use a rhombus labeled with ""Irrelevant" to representexpress them. Then, we must have some relationship between the  $c_{new}$  and actual MFS, which also has ve four possibilities represented as rectangles in the right column.

Note that there exists two types of directed line, solid line and dashed line, in which

the former indicates that this transformation is deterministic, e.g., if  $c_{origin} \le c_m$  and  $c_{new} \le c_{origin}$ , then we must have  $c_{new} < c_m$ . The latter type means the transformation is just one of all the possibilities in such condition-condition, e.g., if  $c_{origin}$  irrelevant  $c_m$  and  $c_{new} \le c_{origin}$  then we can have either  $\exists c_m$  is one actual MFS; s.t. $c_{new} < c_m$  or  $c_{new}$  irrelevant to all actual MFS. (We will later give illustrative examples to illustrate them).

In this figure, only two transformations can make  $\exists c_m$  is one actual MFS; s:t:  $c_{new} = c_m$  or  $c_m < c_{new}$ , which are when  $c_{origin} = c_m$ ,  $c_{new} = c_{origin}$  or  $c_m < c_{origin}$ ,  $c_{new} = c_{origin}$  respectively. This can be easily understood, as to make  $c_{new} = c_m$  or  $c_m < c_{new}$ , according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  according to the proposition 3.11 and 3.12, it must have  $(c_{new})$  accord

Formatted: Font: Italic

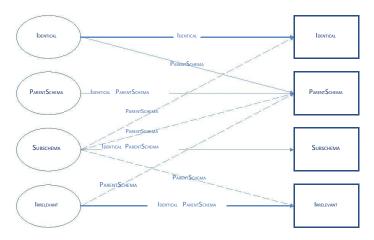


Fig. 6. mMasking effects influence on FCI with distinguishing faults

 $c_{new}$  that is the sub-schema of  $c_{origin}$ . Consequently,  $(c_{new}) < c_{(B1)} = c_{(B1)}$  if we have  $c_{new} < c_{origin} = c_{(D1)} = c_{(D1)}$ 

As the identical transformation is simple, so next-we will ignore itthem and just take examples to illustrate the other transformations. Table XIII presents all these possibilities except these identical transformations. This table consists comprises of three parts, withhich the upper part givings the test cases for each area in the abstract FCI model. It is noted that with interesting the merged the area B1, B2 and C areas into one column toles the way of compute ing the minimal schemas of the three approaches—actual MFS, knowing masking effects, regarded as one fault are all dependent on the merging the test cases of these is three areas, not on their specific distribution of them. The middle part of this table shows the min-imal schemas that using this particular method. Andt last, the lowrbellow part in specific depicts the sample of each possible result of the transformation in the Figure 5. In this part,

 $c_m = c_{origin} \rightarrow c_{new} \prec c_m$  indicates the scenario that the schema  $c_{origin}$  got by knowing masking effects is identical to one actual MFS  $c_{m,\overline{1}}$  Then, taking regard as one fault, we got  $c_{new} \prec c_{origin}$ , so and such that we can have  $\exists c_m$  is one actual MFS; s:t.;  $c_{new} \prec c_m$ . Other formulae in this column can be explained in this way, in which  $c_{new}$  irrele and  $c_{origin}$  irrele means that the schema  $c_{new}$  and  $c_{origin}$  is irrelevant to all the actual MFS, respectively. The mark \*in  $c_m$  and  $c_m$  respectively, represent these two conditions. The formulae in the last two rows,  $c_{newirrele} \prec c_m$  and  $c_{newirrele}$  indicate the schemas  $c_{newirrele}$  obtainedget by regard as one fault are is irrelevant to all the  $c_{origin}$  in which the former is the subschema of some actual MFS  $c_m$  while the latter is irrelevant to all of the actual

MFS. The \* in the  $c_{origin}$  column means that the  $c_{new}$  is irrelevant to all the  $c_{origin}$ .

4.2.2. using distinguish strategy. And for the second strategy  $\dot{x}$  distinguish faults, the influence can be described as in Figure 6.

This figure is organised the same way as <u>frigure</u> 5. As with <u>the</u> distinguish faults strategy, the minimal schemas identified are actually *C*(*A* 

B<sub>1</sub> *C*). Obviously *A* B<sub>1</sub>

A B B C. So under this transformation, the c<sub>new</sub> schema or identical to the c <sub>origin</sub>

Formatted: Font: Italic

Formatted: Font: Not Italic

should be either the

parent-

39:18 X. Niu et al.

Table XIII. Example of the influence of the regard as one fault for FCI approach

	· u —	U			
Α	B <sub>1</sub>	B <sub>2</sub> C	B <sub>3</sub>		ס
(0,0,0,1,0,0)	(1,1,1,0,0,0)		(1,0,1,0,0,0)	(1,1,0,0,0,0)	
(0,0,0,1,1,0)			(1,0,1,0,1,0) $(1,1,0,0,1,0)$		
(0,0,1,0,0,0)	(1,1,1,1,0,0)		(0,0,1,0,1,0)	(1,1,0,1,0,0)	
(0,0,1,1,0,0)	(1,1,1,1,1,0)		(0,0,1,1,1,0)	(1,1,0,1,1,0)	
	(1,0,1,		(0,1,0,0,0,0)		,1,0,1)
	(1,0,1,		(0,1,0,1,0,0)	(0,1,1,1,0,1)	
	(0,0,0,		(0,1,1,0,0,0)		
	(0,0,0,0,0,0)		(0,1,1,1,0,0)		
	(0,0,1,1,1,1)		(1,0,0,0,0,0)		
	(0,1,1,1,1,1)		(1,0,0,0,1,0)		
			(1,1,1,1,1,1)		
			(1,0,1,1,1,1)		
actual MFS		knowing masking	0 0		ault U
α <sub>B1</sub> B <sub>2</sub> C		<i>C</i> ( <i>A</i> ∪ <i>B</i> <sub>1</sub>			$B_2$ $B_3$ $C)$
(1,1,-,-,-,0)		(1,1,1,-,-,0)		(1,-,1,-,-,0)	
(1,-,1,1,-,0)		(1,-,1,1,-,0)		(0,0,-,-,0)	
(0,0,0,0,-,0)		(0,0,0,-,-,0)		(0,-,-,0,0)	
(0,-,1,1,-,1)		(0,0,-,-,0,0)		(-,0,1,-,-,0)	
		(-,0,1,1,0,0)		(-,-,1,-,0,0)	
		(0,-,1,1,1,1)		(-,0,-,0,-,0)	
				(-,-,1,1,1,1)	
				(1,-,1,1,-)	
				(-,0,1,1,1,-)	
transformatio		c <sub>m</sub> (1,-,1,1,-,0)	C <sub>origin</sub> (1,-,1,1,-,0)	c <sub>new</sub> (1,-,1,-,-,0)	<u>c<sub>m'</sub></u> (1,-,1,1,-,0)
$Cm = Corigin \rightarrow Cnew < Cm$		(1,-,1,1,-,0)	(1,1,1,-,-,0)	(1,-,1,-,-,0)	(1,-,1,1,-,0)
Cm < Corigin → Cnew < Cm Cm <		(0,-,1,1,-,1)	(0,-,1,1,1,1)	(-,-,1,1,1,1)	(1, ,1,1,,0)
Corigin → Cnew Irrele		(0,0,0,0,-,0)	(0,0,0,-,-,0)	(0,0,-,-,-,0)	(0,0,0,0,-,0)
Corigin < Cm → Cnew < Cm Corigin		(0,0,0,0, ,0)	(0,0,-,-,0,0)	(0,0,-,-,-,0)	(0,0,0,0,-,0)
irrele → cnew < cm c <sub>origin</sub> irrele		*	(-,0,1,1,0,0)	(-,0,1,-,-,0)	*
→ c <sub>new</sub> irrele <sub><c< sub=""></c<></sub>		*	( ,0, 1, 1,0,0)	(-,0,-,0,-,0)	(0,0,0,0,-,0)
newirrele m		*	*	(1,-,1,1,1,-)	*
Cnewirrele irrele				(1, -, 1, 1, 1, -)	

We take an example to illustrate this type of transformation, which is depicted in Table XIV. Similar to our with previous strategy, we omit the samples that is belong to the identical transformations.

We note!t is noted that <u>in addition todespite</u> the transformations <u>that</u> corresponding <u>to</u> each directed line <u>that is depicted in Figure 6</u>, there is one more transformation <u>that can appear in this strat-</u>

egy, which can make some  $c_{origin}$  removed from the newly minimal schemas, i.e./  $c \exists_{new}$ ; s:t:;  $c_{new} = c_{origin}$  or  $c_{origin} \prec c_{new}$ . For the example of the Table XIV example, in the last row we used a formula  $c_{origin}$  ignored to represent this condition, with the mark \* in the  $c_{new}$  indicatinge that the  $c_{origin}$  is irrelevant to all the  $c_{new}$ . In this row, we can find for the schema  $c_{origin} = -(1,1,0,0,1,-)$ , which is identical to the one in the actual MFS: there exists no  $c_{new}$  which is identical to or is the parent-schema of this schema. Consequently,

in this condition, this strategy may ignore some actual MFS compared with knowing masking effects.

In fact, besides this special case that may <u>result inmake</u> the FCI approach ignor<u>inge</u> some actual MFS, there exists some other cases  $\underline{\text{that}}$  can also achieve the same effect\_ $\bar{\tau}$  from example, when

the  $c_{new}$  is the only schema that is *related* to  $c_{origin}$ , (*related* means not irrelevant, and in this case it is either identical to or the parent-schema). And the corresponding parent-schema

 $c_{origin}$  is the only schema which is related to one actual MFS  $c_m$ . Then, if the  $c_{new}$  is irrelevant to all the actual MFS, we will ignore the actual MFS  $c_m$ . This *ignored* event

is caused byof the  $c_{new}$  growing into the irrelevant schemas, which can also be appeared in the strategy regard as one fault. However, the aforementoined and cause of ignored—the

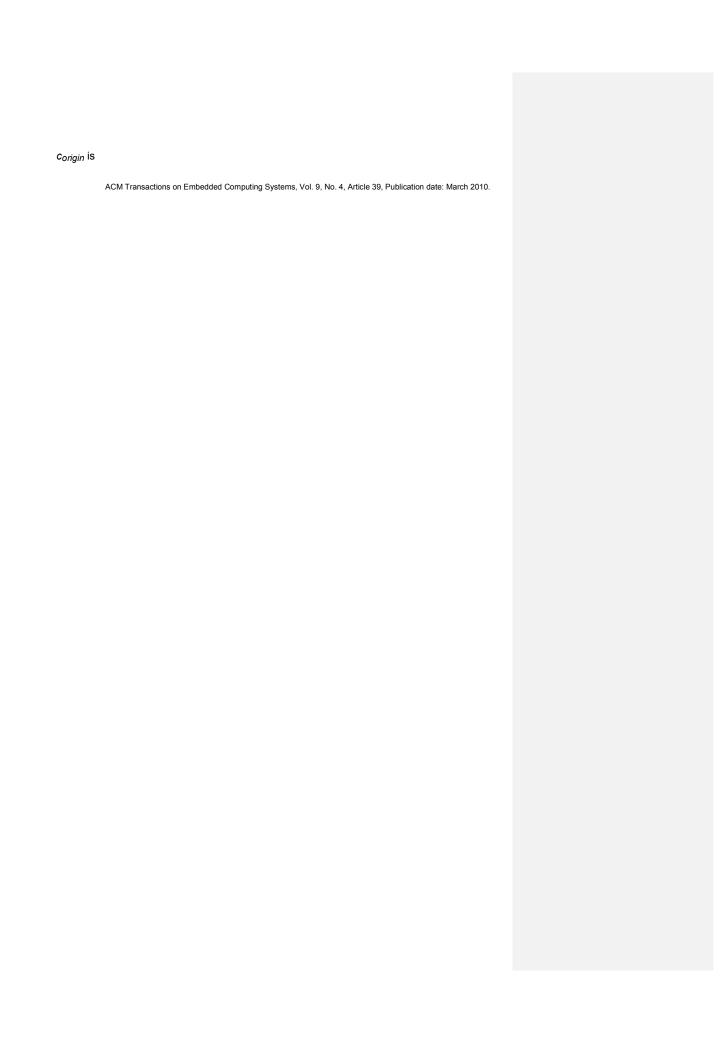


Table XIV. Example the influence of distinguish faults for FCI approach

Table XIV. Example the influence of distinguish faults for FCI approach								
Α	B <sub>1</sub> C	B <sub>2</sub>						
A (0,0,0,1,1,0,0) (0,0,1,1,0,0) (0,0,1,0,1,0) (0,0,1,0,0,0) (1,1,0,0,0) (0,0,1,1,0,1)	B1 C (0,0,0,0,1,0) (0,0,0,1,0,0) (1,1,1,1,1,0) (1,1,0,0,1,0) (1,1,0,1,1,0) (1,1,1,0,0,0) (1,1,1,1,0,1,0)	(0,0,1,1,1,0) (1,1,0,1,0,0) (1,0,1,1,0,1) (0,0,1,1,1,1) (1,1,0,0,1,1) (0,1,0,0,1,1) (1,0,1,0,1,1)	D (0,1,1,0,1,0) (0,1,1,0,1,0) (0,1,1,1,0,0) (0,1,1,1,1,0) (1,1,1,1,1) (0,1,1,1,1,1) (1,1,1,1,0,1) (1,0,0,1,1,1)					
actual MFS C(B1 B2 C D)	(1,0,1,1,1,1) (0,0,0,0,1,1) (1,0,0,0,1,1) knowin	g masking effects B <sub>1</sub> B <sub>2</sub> C)	distinguishfaults $\alpha$ A B1 C)					
(1,1,-,1,-,0) (-,-,0,0,1,1) (0,0,0,-,0,0) (0,0,0,-,0) (1,0,-,-1,1) (1,1,0,0,1,-) (-,1,1,-,-1,0) (-,-,1,1,1,1) (1,1,-,-1,0) (-,1,1,1,1,-) (1,1,1,1,-) (1,1,1,1,-) (1,-,1,1,1,-) (1,-,1,1,-1) (0,0,0,0,1,-)	(-, (0, (0, (1, (1, (1,	(0,0,-,-,-,0) (-,0,1,1,-,1) (0,0,1,1,-,-) (0,0,0,0,1,-) (1,1,0,0,1,-) (1,0,1,-,1,1) (1,0,-0,1,1) (-,-,0,0,1,1)		(0,0,-,-,0,0) (0,0,-,0,-,0) (1,1,1,-,-,0) (1,1,-,-,1,0) (1,1,-,0,-,0) (0,0,1,1,0,-) (1,0,1,1,1,1) (-0,0,0,1,1) (0,0,0,0,1,-)				
transformation	Cm	<b>C</b> origin	Cnew	c <sub>m'</sub> (-,-,0,0,1,1)				
$cm = corigin \longrightarrow cm < cnew$ $cm < corigin \longrightarrow cm < cnew$ $corigin < cm \longrightarrow cnew$ $irrele$ $corigin < cm \longrightarrow cnew < cm$ $corigin < cm \longrightarrow cm < cnew$ $corigin < cm \longrightarrow cm$ $corigin < cm$ $corigin < cm$ $corigin < cm$ $corigin < cm$ $corigin$	(-,-,0,0,1,1 (1,0,-,-1,1 (1,1,-1,-,0) (0,0,0,0,-,0 (1,1,-,1,-,0) (1,1,-,1,-,0) *	(1,0,1,-,1,1) (1,1,-,-,0) (0,0,-,-,0) (1,1,-,-,0) (1,1,-,-,0) (-0,1,1,-,1) (0,0,1,1,-,-)	(-,0,0,0,1,1) ((1,0,1,1,1,1)) (1,1,-,0,-,0) (0,0,0,-,-,0) (1,1,1,-,-,1,0) (1,0,1,1,1,1) (0,0,1,1,0,-)	(-,-,0,0,1,1) ((1,0,-,-,1,1)) ((0,0,0,0,-,0) (-,1,1,-,-,0) (1,1,-,-,1,0) (1,-,1,1,-,1)				

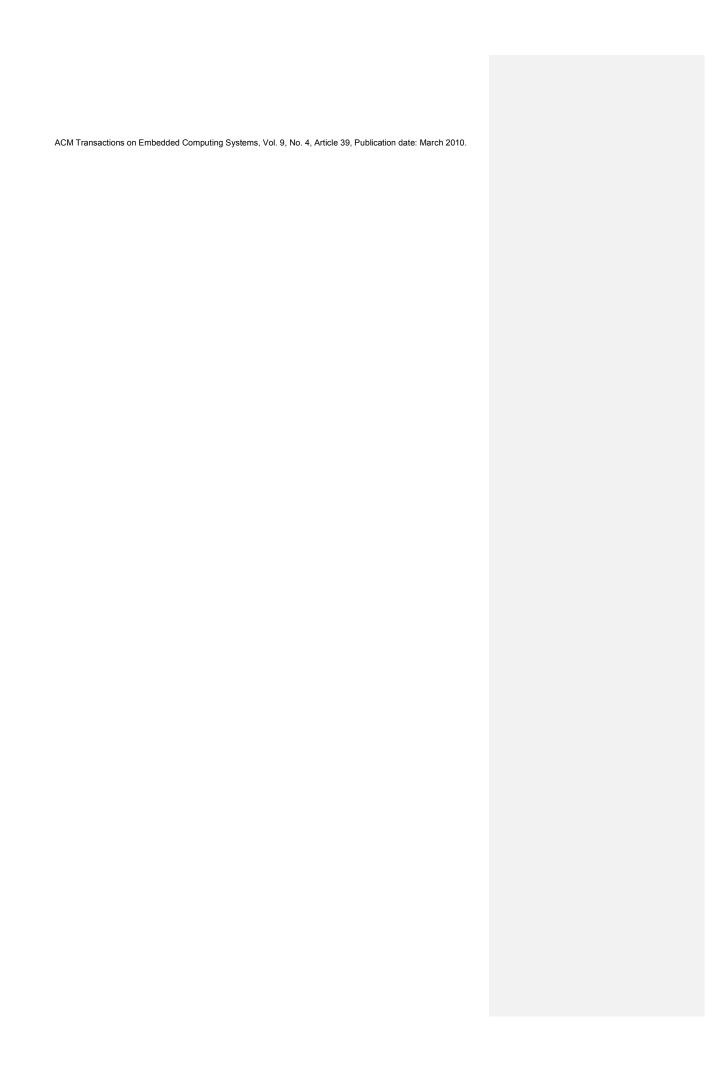
removed from the newly minimal schemas can only happens in the strategy distinguish faults.

## 4.3. Summary of the masking effects on the FCI approach

From the analysis of the formal model, we can learn that masking effects do influence the FCI approaches, and even worse more, both the strategies regard as one fault and distinguish faults strategy are harmful. Specifically, which specifically the former comparesing the knowning masking effects have a large possibility of gettingthat get more sub-schemas of the actual MFS and getting more schemas which are irrelevant to the MFS, while the latter may get more paren-t schemas of the MFS and can also get more irrelevant MFS. Further, Bboth the two-strategies can ignored the actual MFS and the distinguish faults stragegy is more likely to ignore the MFS than the regard as one faultformer strategy.

Note that our discussion is based on <u>anthat SUT using a deterministic software</u>, <u>i.e.</u>, the random failing information of <u>a</u> test case will be ignored. The non-deterministic problem <u>results in a more will</u> complex <u>our</u> test scenario, which will not be discussed in this paper.

Formatted: Font: Italic
Formatted: Font: Italic



39:20 X. Niu et al.

#### 5. TEST CASE REPLACING STRATEGY

The main reason why the FCI approach fails to properly work is that we cannot determine the areas  $B_2$  and  $B_3$ , i.e., if the test case under test triggers other faults which are different from the current one, we cannot figure out whether this test case will trigger the current expected fault as the masking effects may prevent that. So in order to limit the impact of this effect on the FCI approach, we need to reduce the number of test cases that trigger other faults as much as possible.

In the exhaustive testing, as all the test cases will be used to identify the MFS, there is no room left to improve the performance without fixing the other faults and re-executing all the test cases. However, when <u>you</u> just needing to select part of <u>all the whole</u> test cases to identify <u>the MFS</u>, which is <u>howas the traditional FCI approach works</u>, we can adjust the test cases we need to use by selecting <u>the proper ones, thereby limiting so that we can limit</u> the size of  $T(mask_{Fm})$  so that it isto by

### 5.1. Replacinge test cases that triggering an unexpected fault

The basic idea is to pick the test cases that trigger other faults and generate newly test cases to replace them. These regenerated test cases should either pass in the execution or trigger  $F_m$ . The replacement must satisfy the condition that the newly generated ones will not negatively influence the original identifying process.

Commonly, when we replace the test case that triggers <u>an</u> unexpected fault with a new test case, we should keep some part in the original test case. we call this part <u>theas</u> fixed part, and mutate <u>the</u> other part with different values from the original one. For example, if a test case (1,1,1,1) triggered an unexpected fault, and the fixed part is (-,-,1,1), <u>whichthen</u> we can replace <u>it</u>—with a test case (0,0,1,1) which may either pass or trigger an expected fault.

The *fixed part* can varyies for different FCI approaches, <u>e.g.</u>, for the OFOT algorithm, the <u>factors are the fixed part is the factors except</u> for the one that needs to be validated, <u>even if whether</u> it is the component of the MFS, while for <u>the FIC BS</u>, we will fix the factors that should not be mutated <u>for</u>of the test case in the next iteration of <u>the FIC BS</u> process.

We note!t is noted that this replacement may need to be executed multiple times for one fixed part as we could not always find a test case that by coincidence satisfiedy our require-ments. Our previous work just randomly choese test cases until one was found thatfind one satisfied the test case. That brute method may be simple and really works, but also it may require tryingneed to try too many times to get the satisfied one. So to handle this problem and reduce the cost, we augmented our previous approach by with computing the strength of the test case with the other faults, and then we will-selected the one test case from a group of candidate test cases that has the least strength that is related to the other faults.

To explain the *strength* notation, we need first to introduce the *strength* with which that a factor is related to a particular fault. We use all(o) to represent the number of executed test cases that contain this factor, and m(o) to indicate the number of test cases that trigger the fault  $F_m$  and contain this factor. Then, a the *strength* that a factor is related to

particular fault,  $\underline{i.e.}$ ,  $\underline{S(o; F_m)}$ , is  $\underline{\frac{m(o)}{all(o)+1}}$ . This heuristic formula is based on the idea that if a factor frequently appears in the test cases that trigger the particular fault then it is more likely to be the inducing factor that triggers this type of fault. We present in the denominator for two facts: 1. avoid the division by zero when the factor  $\underline{b-1}$  as hever

Formatted: Font: Not Italic

Formatted: Font: Italic

Formatted: Font: Italic

appeareds before, and 2. reduce the bias when a factor rarely appears in the test set but by coincidence appears in a failing test case with a particular fault.

With this <u>factor</u> strength of the factor, we then define that the strength of a test case f is related to a particular fault  $F_m$  as:

$$S(f; F_m) = \frac{1}{2} S(o; F_m)$$

In this formula, k is the number of factors in the test case f, o is the specific factor in f. This formula computes the average strength of all the factors in the test case as the strength for this test case that is related to a particular fault. For a test case that is selected to be tested, we want that the ability of that case to trigger another fault to beneed to make it as small as possible ility to trigger other faults. In practice, one test case can have different related strength to different faults, so we can not always find a test case that hasve the least relating strength to all the faults when compareding to other test cases. With this fact in mind, our target changes to find a test case for whichthat the maximal strength it is of the related fault among other faults is should be the least compared tominimal comparing other test cases. Formally, we should choose a test case f, s.t.,

$$\min_{f \in R} \max_{m \leq L \& m \neq n} S(f; F_m) \tag{EQ1}$$

In this formula, *L* is the number of all the faults, and *n* is the current analysed fault. *R* is ехсер

have been tested. Obviously  $|R| = \frac{1}{t} \int_{t=1}^{t} \int_{t=1}^{t$ We can further resolve this problem. Consider the test case we get—\_\_f satisfied the EQ1. Without loss of generality, we assume that the fault  $F_k$ ;  $k \neq n$  is the fault with which that the test case f has the maximal related strength compared to the than other faults. Then, a natural property for f is that any other test case f which satisfies that fault  $F_k$  is the maximal related fault for this test case and must have  $S(f; F_k) \le S(f; F_k)$ Formally, to get such a test case is to solve the following formula:

$$\min S(f; F_k)$$
 (EQ2) s.t.  $f \in R$ 

$$S(f; F_k) > S(f; F_i); 1 \le i \le L \& i = /k; n$$

With this formula, to solve the EQ1, we just need to find the particular fault  $F_k$ , such that the related *strength* between the test case f satisfies the EQ2, and this fault is the smallerst than all other faults. Formally, we need to find-:

min 
$$S(f; F_k)$$
 (EQ3) s.t.  $1 \le k \le L \& k \ne n$ 

## f; F<sub>k</sub> satisfies EQ2

According to the EQ3, the problem that to get such a test case lies in solvingen to solve the EQ2, because if EQ2that is solved, we just need to rank the one that has the minimal value from the solutions to EQ2. As to EQ2, it can be formulated as an 0-1 integer linear programming (ILP) problem. Assume the SUT we test hasve K factors, in which the *i*th factor has  $V_i$  values can it can take from. And the SUT has L faults. We then define the variable  $x_{ij}$  as:

 $x_{ij} = 1$  the ith factor of the test case take the jth value for that factor 0 otherwise

We then take  $o_{mij}$  to be the related *strength* between the *j*th value of the *i*th fac-tor of the SUT and the fault  $F_{m}$ . And we use a set R of factors with its val-ues to define the fixed part in the test case we should not change, *i.e.*, R =

Formatted: Font: Italic

Formatted: Font: Italic

 $\{(i;j)|i$  is the fixed factor in the test case; j is the corresponding value $\}$ . As we can generate redundant test cases, so we keep a set of test cases  $T_{executed}$  to guide to generate different test cases. Then the EQ2 can be detailed as  $\underline{in}$  the following ILP:

In this formula, the constraints (1) and (2) indicate that the variable  $x_{ij}$  is a 0-1 in-teger. Constraint (3) indicates that a factor in one test case can only take one value. Constraint (4) indicates the test case should not change values ofto the fixed part. Con-straint (5) indicates that the related strength between Fault  $F_m$  and the test case is greater maximal than the others. Constraint (6) indicates the test cases generated should not be the same as the test cases in  $T_{existed}$ 

As we have formulated the problem into a 0-1 integer programming problem, we just need to utilize an ILP solver to solve this formula. In this paper, we use a the solver introduced in [Berkelaar et al. 2004], which is a mixed Integer Linear Programming (MILP) solver that can handle satisfaction and optimization problems.

The complete process of replacing a test case with a new one  $\underline{\text{while}}$  keeping some fixed part is depicted in Algorithm 1:

The inputs for this algorithm consists of the fault type, www eurrently-focus on  $-F_m$ , the fixed part of which we want to keep from the original test case  $-s_{fixed}$ , the values sets that each factor can take from respectively -Param and the set of matrix  $o_1; :::o_L$ , for any element in which, say  $o_m$ , is recorded the related strength between each specific factor with each value and the fault  $F_m$ , i.e.,  $o_m = \{o_{mij} \mid 0 \le i \le K - 1; 0 \le j \le V_i\}$ . The output of this algorithm is a test case  $t_{new}$  which either triggers the expected  $F_m$  or

This algorithm is an outer loop (lines 1 - 19) containing two parts:

The first part\_(lines 2 - 9) generates a new test case which is supposed to be least likely to trigger faults different from  $F_m$ . The basic idea for this part is to search each fault different from  $F_m$  (line 3) and find the best test case that has the least related strength with other faults. In detail, for each fault we set\_up an ILP solver (line 4) and use it to get an optimal test case for that fault according to EQ4 (line 5). We compare the optimal value for each fault, and choose the one has an less strength related to other faults (lines 6 - 9).

The Second part is to check whether the newly generated test case is as expected

Formatted: Font: Italic

(lines 10 - 16). We first execute the SUT under the newly generated test case\_(line 10) and update the related strength matrix (o<sub>1</sub>:::o<sub>L</sub>) for each factor that is involved in this

18 return null

### ALGORITHM 1: FReplacinge test cases triggering unexpected faults

```
Input: fault type F_m, fixed part s_{fixed}, values set that each option can take Param, the related
             strength matrix o1:::oL
   Output: tnew the regenerate test case, I the frequency number
  1 while not MeetEndCriteria() do
       optimal MAX; t_{new} null;

forall the F_k 2 F_1, ...F_m, F_{m+1}...F_L do

solver setup(s_{fixed}; Param_i F_m; o_1...o_L);
 4
             (optimal; t<sub>new</sub>) solver:getOptimalTest();
 5
             if optimal < optimal then
 6
              tnew
                           tnew;
            end
 8
 9
        end
        result
                    execute(t_{new});
 10
        updatetRelatedStrengthMatrix(tnew);
11
        if result == PASS or result == F_m then
12
            return tnew;
13
            continue;
15
16
        end
17 end
```

newly generated test case (line 11). We then check the executed result\_ $\div$  if either the test case passes or triggers the same fault –  $F_m$ , we will get an satisfied test case (line 12), and we will directly form this test case (line 13). Otherwise, we will repeat the process, i.e., generate a newly test case and check again (line 14 - 15).

we noted is noted that this algorithm has another exit, besides we find an expected test case (line 12), which is when the function <code>MeetEndCriteria()</code> returns <code>true(line 1)</code>. We didn't explicitly show what the function <code>MeetEndCriteria()</code> is like because this is dependent ing on the computing resource and how accurate you want to the identifying result to be. In detail, if you want to get a high quality result and you have enough computing resource, you can try <code>manyueh</code> times to get the expected test <code>case\_i</code> otherwise, a relatively small number of attempts is recommended.

In this paper, we just set 3 as the <u>greatest number ofbiggest</u> repeat<u>sed times</u> for this function. When it end<u>sed</u> with *MeetEndCriteria()* is true, we will return null\_(line 18), which means we cannot find an expected test case.

#### 5.2. A case study usingwith the replacementing strategy

Suppose we have to test a system with eight parameters, each of which has three options. And when we execute the test case  $T_0$  – (0 0 0 0 0 0 0 0), a failure—e1 is triggered. Next, we will use the FCl approach – FIC BS [Zhang and Zhang 2011] with replacementing strategy to identify the MFS for the e1. Furthermore, there are two more potential faults, e2 and e3, that may be triggered during the testing, which will mask the desired fault e1. The process is shownlisted in Figure 7. In this figure, there are two main columns\_in this figure, tThe left main column indicates the executed test cases during testing as well as their executed results, and each executed test case corresponds to a specific label,  $T_1 - T_8$ , atim the left. The right main column lists the related strength matrix when we comes with a test case triggersed e2 or e3. In detail, the matrix records the related strength between each factor (columns O1 – O8) for each value it can take (column v) with the unexpected fault (column F). The executed test case, which is in bold, indicates the one that triggers theother faults and should be replaced in the next iteration.

ACM Transactions on Embedded Computing Systems, Vol. 9, No. 4, Article 39, Publication date: March 2010.

Formatted: Font: Italic

39:24 X. Niu et al.

Table XV. The number of test cases each FCI approach needed to identify the MFS

Method	number of test cases to identify MFS
Charles ELA	depends on the covering array
Martinez with safe value [Mart-inez et al. 2008; 2009]	O(dlogk + d )
Martinez without safe values [Mart´ınez et al. 2008; 2009]	O(d + dlogk + log k) O(ds logk)
Martinez' ELA [Mart'-nez et al. 2008; 2009]	O(ds <sup>v</sup> logk)
Shi SOFOT [Shi et al. 2005]	O(k)
Nie OFOT [Nie and Leung 2011a]	$O(k \times d)$
Ylimaz classification tree	depends on the covering array
FIC [Zhang and Zhang 2011]	O(k)
_ FIC BS [Zhang and Zhang 2011]	O(t(logk + 1) + 1)
Ghandehari's suspicious based [Ghandehari et al. 2012]	depends on the number and size of MFS
TRT [Niu et al. 2013]	$O(d \times t \times logk + t^{u})$

From Figure 7, for the test case that triggered e2 – (2 1 1 1 0 0 0 0) (in this case, the fixed part of the test case is (- - - - 0 0 0 0), in which the last four factors are is the same as the original test case  $T_0$ ), we generates the related matrix atin the left. Each element in

this matrix is computed as the  $\frac{m(o)}{all(o)+1}$  , for example, for the O7 factor with value 0, we can find two test cases that contain this element,  $\underline{i.e.}$ ,  $\underline{T_0}$  and  $\underline{T_1}$ , so the all(o) is 2. And only one test case triggers the fault e2, which means m(o) = 1. So the final related strength between this factor with e2 is 2+1 = 0.33. All the related strength with e3 is labeled with a short slash as there is no test case triggering this fault in this iteration. After this matrix has been determined, we can obtained an optimal test case with the ILP solver, which is  $\underline{T_1}$ –(1 2 2 2 0 0 0 0), with its related strength 0.167, which is smaller than that of the others.

This replace process trigged each time <u>a newthe newly</u> test case <u>that</u> trigger<u>ed</u> <u>another</u> fault, <u>and</u> until we finally get the MFS. Some-times we could not find a satisfied replacing test case in just one trial like  $T_1$  to  $T_1$ . When <u>thisit</u> happened, we <u>will needed to repeat searching</u> the proper test case, we desired, <u>e.g.</u>, <u>Ffor example, for  $T_4$ , which triggered e3, we tried three times—  $T_4$ ;  $T_4$ ;  $T_4$  to finally get a satisfied one  $T_4$  which passes the testing. It is noted that the matrix continues to change with the test case generated and executed so that we can adaptively find an optimal one in the current process.</u>

#### 5.3. Complexity analysis

This complexity <u>relieslay</u> on two facts: the number of test cases <u>that triggered</u> other faults which need to be replaced, and the number of test cases that need to be tried to generate a non-masking-effects test case. The complexity is the product of th<u>eseis</u> two facts.

The first fact is comparable to the extra test cases that <u>are</u> needed to identify the MFS, and this number varies in different FCI approaches. Table XV lists the number of test cases that each algorithms that needed to get the MFS. In this table, *d* indicates the number of MFS in the SUT. *k* means the number of the parameters of the SUT. *t* is the number of MFS factors of the MFS in the SUT. *c* is an upper bond, and satisfies,  $d \le 2^{C} \log \log k$ . *v* is the number of values one parameter can take.

It must be noted that each algorithm may be limited to some restrictions to identify the result, details of which are shown incan be saw in [Zhang and Zhang 2011].

To get the magnitude of the second fact, we need to figure out the possibility of that a test case that could triggering other fault. The first thing we need to considereare is the fixed part, as the additional generated test case should somehow contain this part. As we have mentioned before, we can in fact generate  $(v-1)^{k-p}$  (p is the number of factors in the fixed part) possible test cases that contain the fixed part. Apart from the one that

Formatted: Font: Italic

Formatted: Font: Italic

needs to be replaced, there remain  $(v-1)^{k-p}-1$ , which indicates the complexity is  $O((v-1)^{k-p}-1)$ . However, to avoid the exponential computational complexity, we in this algorithm we use the method *MeetEndCriteria()* (line 1) function to end the algorithm

1

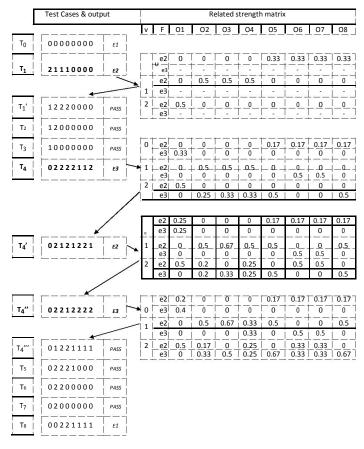
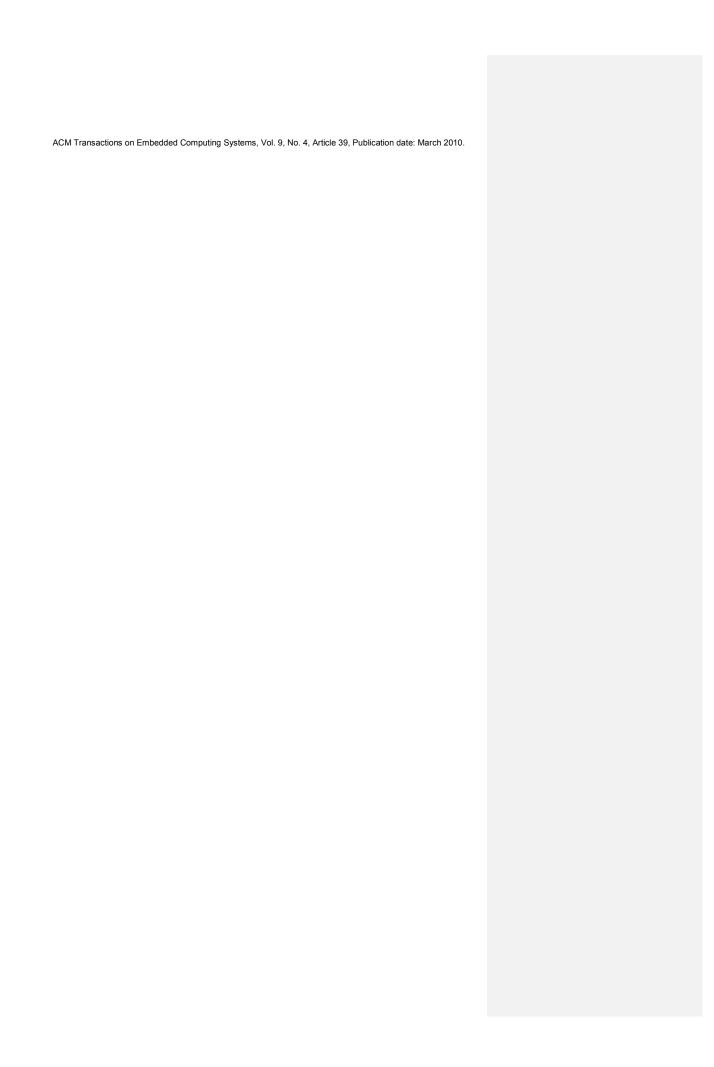


Fig. 7. A case study using of our approach

when the trying times is over a prior given constant, say N, so the final complexity for the second part is  $O(min(N; (v-1)^{k-p}-1))$ .

We notelt is noted that exponential factor k-p directly affects the complexity of the second factor,  $\frac{1}{2}$  The greatermore p is, the less test cases that canould be generated. For a different approach, p is different. As for OFOT, p is a fixed number, which is k-1. This it is the minimal number of the test cases we need to usegive. While for FIC BS, the p varies in the test cases it generates, ranginges from k-1 to 1. While for the non-adaptive, as the fixed part is the coverage, we list them as t. We have listed all of them all in Table XVI. It is noted that the Martinezwithoutsafevalues has veno such complexity, this is because this approach works when v=2, and this will results in that we will not havinge other test cases to be replaced if we test a fixed part when triggering other faults.



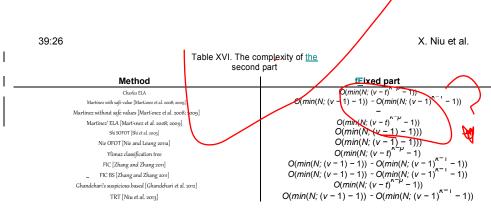


Table XVII. Software under survey

software	versions	LOC	classes	bug pairs
HSQLDB	2.orc8	139425	495	#981 & #1005
	2.2.5	156066	508	#1173 & #1179
	2.2.9	162784	525	#1286 & #1280
JFlex	1.4.1	10040	58	#87 & #80
	1.4.2	10745	61	#98 & #93

#### 6. EMPIRICAL STUDIES

To investigate the impact of masking effects for FCI approaches in real software test-ing scenarios and to evaluate the performance that how well our approach handles this effect, we conducted several empirical studies which we discuss in this section. Each one-of the studies focuses on addressing one particular issueproblem, as follows: which are listed as following:

Q1: Do masking effects exist in real software that when it contains multiple faults?

**Q2**: How well does much do our approach performs compared  $\underline{to}$  with traditional approaches?

**Q3**: Is the ILP\_based test case searching technique efficient compared to random selection? with randomly selecting?

**Q4**: Compareding towith another existed masking effects handling approaches work – the FDA-CIT [Yilmaz et al. 2013], does our new approach have any advantages?

### 6.1. The existence and characteristics of masking effects

In the first study, we surveyed two open-source kinds of software to gain an insight intoen the existence of multiple faults and their effects. The software under study wereare: HSQLDB and JFlex\_, tThe first is a database management software written in pure jJava, and the second is a lexical analyser generator. Each of them contains different versions. Each isAll the two subjects are highly configurable so that the options and their combinations can influence their behaviour. Additionally, they all have a developers' community so that we can easily obtainget the real bugs reported in the bug tracker forum. Table XVII lists the program, the number of versions we surveyed, number of lines of uncommented code, number of classes in the project, and the bug's id of the software we studied.

6.1.1. Study setup. We first looked through the bug tracker forum of each software and focused on the bugs which are caused by the options combination. For each such bug, we will derive its MFS by analysing the bug description report and theits attached test file which can reproduce the bug. For example, through analysing the source code of the test file of bug

Formatted: Font: Italic

# #981 for HSQLDB, we found the failure-inducing combinations for

 $<sup>\</sup>overline{3_{\mbox{http://sourceforge.net/p/hsqldb/bugs http://sourceforge.net/p/jjlex/bugs}}$ 

this bug <u>areis</u>: (preparestatement, placeHolder, Long string)... <u>Thesethis</u> three factors together form the condition <u>that triggers the bug on which the bug will be triggered.</u>
These analysed results will be later regarded as the "prior MFS". <u>later.</u>

We further built the testing scenario for each version of the software listed in Table XVII.\_The testing scenario is properly constructed so that we can reproduce different faults bythrough controlling the inputs to theat test file. For each particular version of the software, the source code of the testing file as well as other detailed experiment information is available at—<a href="https://code.google.com/p/merging-bug-file">https://code.google.com/p/merging-bug-file</a>.

Table XVIII. Input model of HSQLDB

	mon options	values
	erver Type	server, webserver, inprocess
ex	kisted form	mem, file
res	ultSetTypes	forwad, insensitive, sensitive
resultS	etConcurrencys	read_only, updatable
result	SetHoldabilitys	hold, close
Sta	tementType	statement, prepared
	common bBo	olean options
sql.enfo		orce names, sql.enforce refs
versions	specific options	values
2.0rc8	more	true, false
	placeHolder	true, false
	cursorAction	next,previous,first,last
2.2.5	multiple	one, multi, default
	placeHolder	true, false
2.2.9	duplicate	dup, single, default
	default-commit	true, false
versions	Config space	
2.0rc8	2°× <sub>3</sub> 3 <sup>*</sup> × <sub>4</sub> 4'	
2.2.5	2° × 3° × 4' 2° × 3° 2° × 3°	
2.2.9	$2^{8} \times 3^{3}$	

We then generated the exhaustive test suite consisting of all the possible combinations of these options, and under each of them, we executed the prepared testing file. We recorded the output of each test case to observe whether there were test cases containing prior MFS that did but do not produce the corresponding bug.

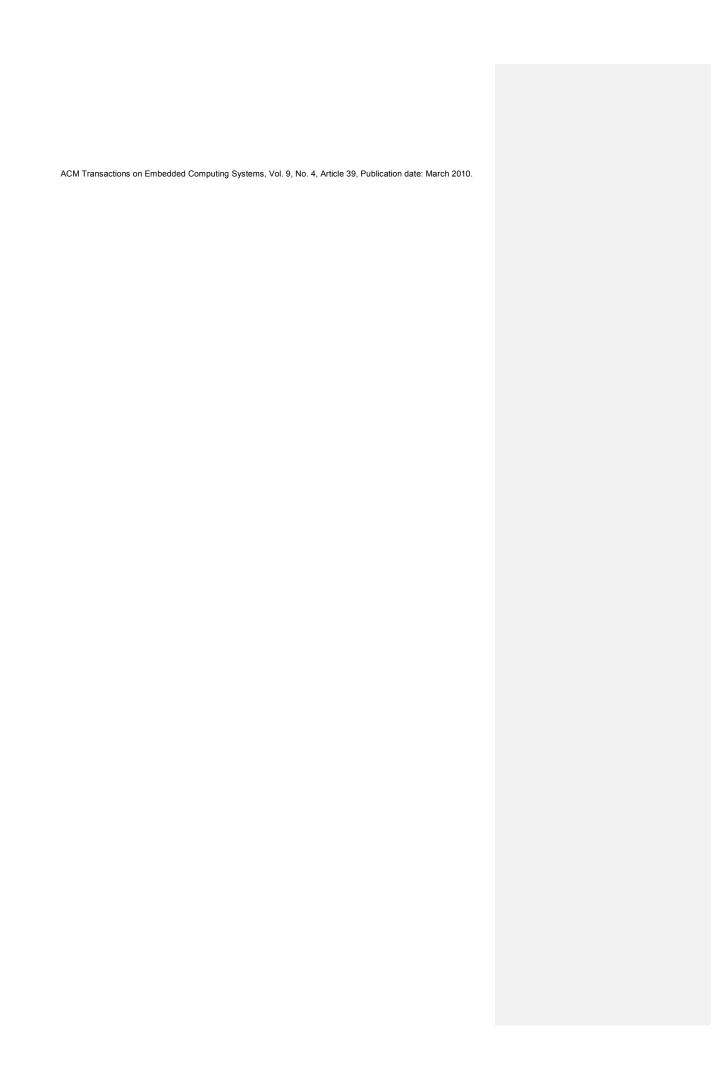
6.1.2. Results and discussion. Table XX lists the results of our survey. Column "all tests" give the total number of test cases we executed.— Column "failure" indicate the number of test cases that failed during testing, and Golumn "masking" indicates the number of test cases which triggered the masking effect.

We observed that for each version of the software under analysis that we listed in the Table XX, the test cases with masking effects do exist, i.e., test cases containing MFS did not trigger the corresponding bug. In effect, there are about 768 out of 4608 test

**Formatted:** Default Paragraph Font, Font: (Default) Calibri, 11 pt

**Formatted:** Font: Italic, No underline, Font color: Auto

**Formatted:** Font: Italic, No underline, Font color: Auto



39:28 X. Niu et al.

Table XIX. Input model of JFlex

con	nmon options	values
	generation	switch, table, pack
	charset	default, 7bit, 8bit, 16bit
	common boole	ean options
		ar,line,column,notunix, yyeof
versions	specific options	values
1.4.1	hasReturn	has, non, default
	normal	true, false
1.4.2	lookAhead	one, multi, default
	type	true, false
	standalone	true, false
versions	Config space	
1.4.1	11 × 32 × 41	
1.4.2	2 ×3 ×4	

Table XX. Number of faults and their masking effects

software	versions	all tests	failure	masking
HSQLDB	2cr8	18432	4608	768
	2.2.5	6912	3456	576
	2.2.9	6912	3456	1728
JFlex	1.4.1	36864	24576	6144
	1.4.2	73728	36864	6144

cases (16.7%) in hsqldb with 2rc8 version. This rate is about 16.7%, 50%, 25%, and 16.7%, respectively, for the remaining software versions, which is not trivial.

So the answer to **Q1** is that in practice, when SUT have multiple faults, the masking effects do exist widely in the test cases.

## 6.2. Comparinge our approach towith traditional algorithms

In the second study, our aim wasis to compare the performance of our approach to traditional approaches inef identifying the MFS under the impact of masking effects. between our approach with traditional ones. To conduct this study, we needed to respectively apply the our approach and traditional algorithms toen identifying MFS in a group of software and evaluate their identifying results. The five prepared versions of software in Table XVII used as test objects as testing subjects is far from a general evaluation of such objects. subjects, hHowever, to construct such real testing scenarios is time-consuming as we mustneed to carefully study the tutorial of that software as well as the bug tracker report. So in order to give a desirable result based on more testing objects subjects, we then synthesize a number bunch of such testing scenarios of which the character-izations, such as the number of factors, the number of faults, and the possible masking effects, are similar to that of the real software. In detail, we set the number of parameters k of the SUT to a ranged from 8 to 30. We limited the scale of the SUT to a relatively small size because we needed to exhaustively execute each possible test case of the SUT to select the failing test cases which we and then fed intothem to the FCI approach. We then randomly choose 10 such SUTs, and for each SUT we injected 2-to 5 different MFS-into it, which that can mask each other. The degree of the MFS we injected are ranged from 1 to 6.

Above all, Table XXI lists the testing model <u>foref</u> both the real and synthesizing testing scenario. In this table, the column 'software' indicates the SUT under test., <u>fF</u>or the real SUT, we label it with the form 'name + version', while for the synthesizing ones, we label them as 'synthez+ id'. The column 'Model' presents the model of the input space for that software. <u>The Llast column shows the MFS as well as their masking sequence for each testing <u>objectsubject</u>. The MFS is presented in an abbreviated form {#index<sub>#value</sub>}, <u>e.g.</u>, (5<sub>1</sub>; 6<sub>0</sub>; 7<sub>0</sub>) actually means (-----1, 0, 0, -, -, -, -) for HSQLDB of version '2cr8'. It</u>

**Formatted:** Font: Italic, No underline, Font color: Auto

Table XXI. The testing models used inof the case study

software	Model	MFS& masking sequence
HSQLDB 2cr8	29 × 32 × 4	$(5_1; 6_0; 7_0) \rightarrow (5_1; 8_2; 9_2) = (5_1; 8_2; 9_1) \rightarrow (5_1; 8_3; 9_2) = (5_1; 8_3; 9_1)$
HSQLDB 2.2.5	2° × 3°	$(6_1; 7_0) \rightarrow (5_2)$
HSQLDB 2.2.9	2° × 3°	$(6_0) \rightarrow (0_1; 5_1; 7_0) = (0_0; 5_1; 7_0) \rightarrow (5_1; 7_0)$
JFlex 1.4.1	2 10 × 3 × 4 1	$(0_0) \to (1_0)$
JFlex 1.4.2	2 × 3 × 4	$(1_0; 2_1) \rightarrow (0_1)$
synthez 1	2°×3°×4'	$(2_1; 3_0) \rightarrow (1_1; 2_1) = (1_0; 3_0)$
synthez 2	$2^{\circ} \times 3^{2} \times 4^{1}$	$(4_1; 6_0; 7_1; 8_0) \rightarrow (1_1; 3_1; 5_1) \rightarrow (2_0; 3_1; 6_0)$
synthez 3	2° × 3°	$(2_1; 3_0) \rightarrow (1_0) = (4_1) \rightarrow (6_0; 7_0)$
synthez 4	$2^{\prime} \times 3^{2} \times 4^{1}$	$(0_1; 2_1; 5_0; 6_1) \rightarrow (2_1; 4_0) = (6_1; 7_0) \rightarrow (3_0; 4_0; 5_0)$
synthez 5	$2^{4} \times 3^{3} \times 4^{2}$	$(0_0; 1_1; 3_0; 6_1; 8_0) \rightarrow (2_0; 3_0; 4_1)$
synthez 6	29 × 3 <sup>2</sup>	$(20; 71; 81) \rightarrow (31; 51) = (40) \rightarrow (31; 60; 71) \rightarrow (31; 71; 80)$
synthez 7	2 10 × 3 1 × 4 1	$(3_1; 4_0; 5_0) \rightarrow (2_0; 4_0; 7_1; 9_0) \rightarrow (6_1; 10_0; 11_1)$
synthez 8	2 × 3 × 4	$(10; 31; 40; 71; 90; 121) \rightarrow (00; 21; 31; 71; 100; 111)$
synthez 9	2 <sup>4</sup> × 4 <sup>3</sup>	$(3_1; 5_0) \rightarrow (5_0; 6_1)$
synthez 10	2' × 3 <sup>3</sup> × 4 <sup>1</sup>	$(0_1; 3_0; 4_1; 7_0) \rightarrow (2_0; 3_0; 5_1) = (2_0; 3_0; 5_0)$

is noted that we using '¿' and '=' to describe the masking sequence of each MFS, in which '¿' means the left MFS in this operator can mask the right MFS of this operator, le a

 $(5_1; 6_0; 7_0) \rightarrow (5_1; 8_2; 9_2)$  means if  $(5_1; 6_0; 7_0)$  appears in the test case, then  $(5_1; 8_2; 9_2)$  will not be triggered. Operator '=' means that these is two MFS will not mask each other.

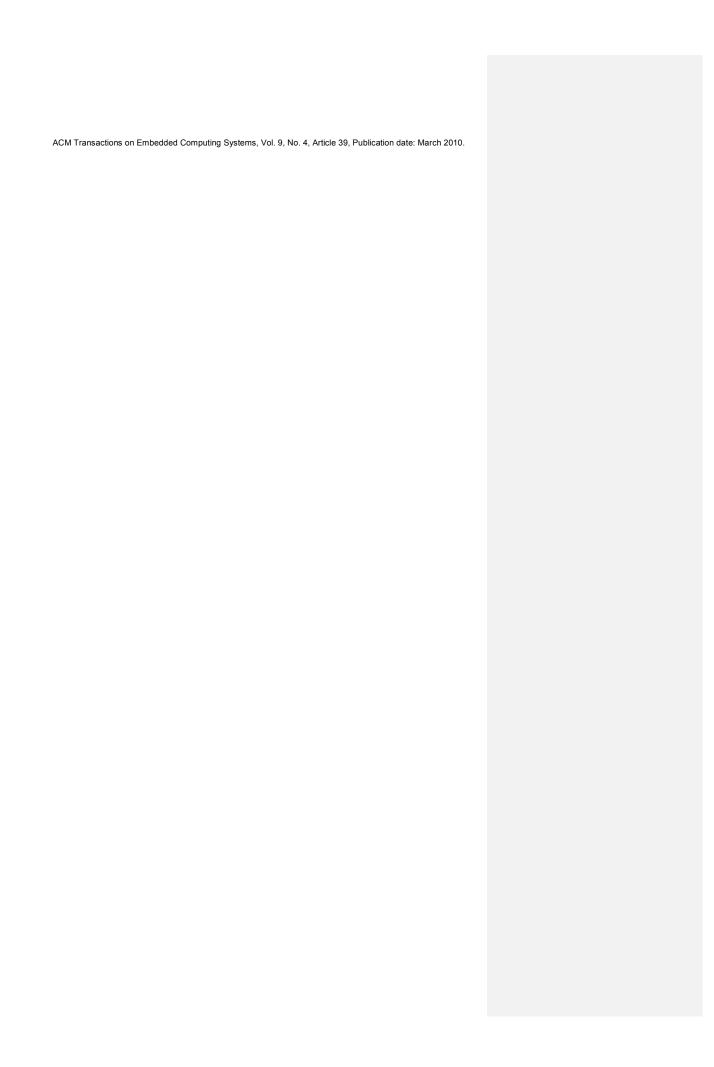
6.2.1. Study setup. After preparing the subjects under testing, we then apply our ap-proach (augment the FIC BS with replacing strategy) to en identifying the MFS of each SUT listed in Table XXI. Specifically!n specific, for each SUT we select each test case that faileding during testing and feed these into them to our FCI approach as the input\_, t\_Then\_ after the identifying process is over, we record the MFS eachit got (referred to as identified MFS, for convenience) and the extra test cases it needed. For the traditional FIC BS approach, we designed the same experiment as that used for our approach, but as the objectsubject being tested under test hads multiple faults for which the traditional FIC BS can—not be applied directly applied-on, we adopted two traditional strategies on the FIC BS algorithm, j.e., regard as one fault and distinguish faults de-scribed in Section 3.2. The purpose of recording the generated additional test cases is to later quantify the additive cost of our approach.

We next compared the identified MFS of each approach with the prior MFS to quantify the degree that each suffers from masking effects, such that we can figure out how much better our approaches performs better than traditional ones when the SUT contains potential masking effects. There are five metrics we need to <a href="calculatecare">calculatecare</a> in this study, which are <a href="listed-as">listed-as</a> follows:

- (1) The number of the common combinations that appeared in both identified MFS and prior MFS. We denote this metric as accurate number later.
- (2) The number of the identified combinations which <u>areis</u> the parent combinations of some prior failure-inducing combinations. We refer <u>it—this metric asto the parent</u> number.
- (3) The number of the identified combinations that <u>are</u> is the sub combinations of some prior failure-inducing combinations, which <u>are</u> is referred to <u>as the sub number</u>.
- (4) The number of ignored failure-inducing combinations. This metric counts these combinations in prior failure-inducing combinations, which are irrelevant to the identified combinations. We label the metric it as ignored number.

**Formatted:** Font: Italic, No underline, Font color: Auto

**Formatted:** Font: Italic, No underline, Font color: Auto



39:30 X. Niu et al.

(5) The number of irrelevant combinations. This metric counts these combinations in these identified combinations that, which are irrelevant to the prior failure-inducing combinations. It is referred to <u>as</u> the *irrelevant number*.

Among these five metrics, <u>the</u> high accurate number value indicates FCI approaches <u>that</u> performs effectively, while <u>the</u> ignored number and irrelevant number indicate the degree of deviation for the FCI approaches. <u>The For parent number and sub number, they</u> indicate <u>the FCI approaches that, although with additional noisy information, can determine part parameter values <u>for about</u> the failure-inducing combinations, <u>although</u> with additional noisy information.</u>

Besides these specific metrics, we <u>alsoin addition</u> give <u>an</u>-composite criteria to measure the overall performance of each approach. The computing formula for theis composite criteria is as follows:

In this formula, accurate, parent, sub, irrelevant, and ignored respectively represents the value of each specific metric. related function gives the similarity between the schemas (either parent or sub) and the real MFS. The similarity between two schemas  $S_A$  and  $S_B$  is computed as:

$$Similarity(S_A; S_B) \stackrel{\underline{the \ same \ elements \ in \ S_A \ and \ S_B}}{\max(Degree(S_A); Degree(S_B))}$$

For example, the similarity of (- 1 2 - 3) and (- 2 2 - 3) is  $\frac{2}{3}$ , as the same elements of this two schemas, are the third and last elements, and both of these two schemas are third-degree and the same elements.

So the *related* function is the summation of similarity of all the parent or sub schemas with their corresponding MFS.

6.2.2. Results and discussion. Table\_XXII depicts the results of the second case study. There are eight main columns in this table, (too\_wide\_so\_we break it into two part-s), which respectively indicates: the object to whichsubject we apply the FCI approach, the number of accurate MFS each approach identified, the number of identified schemas which areis the sub-schema parent-schema of some prior MFS, \text{\text{th}} the number of identified schemas which areis irrelevant to all the prior MFS, the metric which gives the overall evaluation of each approach, and the extra test cases each algorithm needed. For each main column, there are four sub-columns which respectively-depicteticts the results for the FCI with regard as one fault strategy, FCI with distinguish faults strategy, FCI with replacing strategy based on ILP test case searching, and FCI with replacing strategy based on randomly searching. The last one iswill be discussed in the next case study.

We first observed that, the results of two traditional strategies—regard as one fault and distinguish faults—are-coincide with the formal analysis in section 4. Specifically, In specific, the former has more sub-schemas of MFS than the latter for all the 15 subjects, and the latter has more parent-schemas of MFS than the former. For the 'ignored MFS' metric, as we have executed all the failing test cases, we get 0 ignored MFS for all the approaches. So in order to evaluate this metric offor the approaches, we record ithis metric for each FCI one test case one at a time and take the average value as the result, which is listed in the parentheses. We also found in most cases (except synthez 5 and synthez 6) that the approach with distinguish strategy get more ignored MFS than the othersanother one, which is—also coincides with the formal analysis. And for the 'irrelevant MFS', we found regard as one fault strategy in most cases geot more 'irrelevant MFS' than the othersanother, which wasis also as expected.

**Formatted:** Font: Not Italic, No underline, Font color: Auto

Table XXII. Result of the evaluation of each appraoch

Subject	accura	ate			sub				parent				ignore			
	One	Distin	ILP	Rand	One	Distin	ILP	Rand	One	Distin	ILP	Rand	One	Distin	ILP	Rand
HSQL2cr8	2	3	5	5	3	2	0	2	0	2	4	5	0(2.04)	0(3.91)	0(4.0)	0(4.1)
HSQL2.2.5	2	2	2	2	1	0	0	0	0	1	1	1	0(0.83)	0(1.0)	0(1.0)	0(1.0)
HSQL2.2.9	2	3	2	2	3	1	1	1	0	4	1	1	0(1.33)	0(2.83)	0(2.56)	0(2.56)
JFlex1.4.1	2	2	2	2	0	0	0	0	0	1	0	0	0(0.75)	0(1.0)	0(1.0)	0(1.0)
JFlex 1.4.2	2	2	2	2	1	0	0	0	0	1	1	1	0(0.67)	0(1.0)	0(1.0)	0(1.0)
synthez 1	2	1	1	1	2	0	0	0	0	2	2	2	0(1.0)	0(2.0)	0(2.0)	0(2.0)
synthez 2	3	3	3	3	10	0	0	0	0	10	6	6	0(1.96)	0(2.0)	0(2.0)	0(2.0)
synthez 3	4	3	3	3	4	2	2	2	0	5	5	5	0(2.08)	0(2.84)	0(2.84)	0(2.84)
synthez 4	3	3	3	3	10	3	2	3	0	6	5	5	0(2.6)	0(2.8)	0(2.9)	0(2.85)
synthez 5	2	2	2	2	4	0	0	0	0	2	1	1	0(1.02)	0(1.0)	0(1.0)	0(1.0)
synthez 6	2	3	3	3	15	4	4	4	0	8	8	8	0(1.99)	0(3.72)	0(3.72)	0(3.72)
synthez 7	3	3	3	3	10	0	0	0	0	6	6	6	0(2.04)	0(2.0)	0(2.0)	0(2.0)
synthez 8	2	2	2	2	4	0	0	9	0	4	3	3	0(1.05)	0(1.0)	0(1.0)	0(1.0)
synthez 9	2	1	1	1	1	0	0	0	0	1	1	1	0(0.8)	0(1.0)	0(1.0)	0(1.0)
synthez 10	0	1	1	1	3	1	1	1	0	0	0	0	0(1.0)	0(1.46)	0(1.31)	0(1.31)

irrelev	ant			overal	I			test cas	test cases			
One	Distin	ILP	Rando	One	Distin	ILP	Rand	One	Distin	ILP	Rand	
0	2	0	34	0.57	0.65	0.88	0.23	8.125	11.92	17	17.72	
7	0	0	0	0.25	0.83	0.83	0.83	8.67	7.67	10.17	11.3	
4	0	0	0	0.4	0.74	8.0	8.0	9.167	8.61	11.72	13.14	
25	0	0	0	0.07	0.83	1	1	23.5	6.5	8	9.68	
25	0	0	0	0.09	0.83	0.83	0.83	20.5	9	11.67	13.12	
15	17	17	17	0.19	0.11	0.11	0.11	16.5	18	41.75	41.75	
1	0	0	0	0.54	0.76	8.0	8.0	11.19	14.12	16.96	17.08	
13	9	9	9	0.28	0.34	0.34	0.34	12.73	9.46	14.18	14.44	
9	9	9	9	0.35	0.4	0.39	0.39	9.91	13.02	18.55	18.45	
1	0	0	0	0.65	0.88	0.92	0.92	13.04	13.7	14.77	14.84	
8	10	10	10	0.38	0.36	0.36	0.36	14.91	11.75	15.37	15.71	
5	0	0	0	0.39	0.83	0.83	0.83	12.77	14.59	16.44	16.53	
3	0	0	0	0.56	0.9	0.91	0.91	24.45	25.25	26.27	26.37	
0	0	0	0	0.75	0.83	0.83	0.83	6.8	8	9	9	
0	2	1	1	0.5	0.47	0.58	0.58	9.08	11	15.38	15.53	

We then observed that our approach can perreform better than theis two traditional strategies... The advantages are shown byin the more accurate MFS and less irrelevant schemas. Our approach also identified the least number of sub-schemas. As for the 'parent-schema' metric, our approach performeds better than 'distinguish faults' but not as wellgood as 'regard as one fault'. This is because our strategy is actually-based on the 'distinguish faults' strategy (the main difference is that our strategy filters these unsatisfied test cases). However, our approach is not as good separat the 'ignored MFS' metric... The possible reason for this may be that the unsatisfied test cases we discard may contain some useful information about the MFS. Above all, our approach achievesget the best perfor-mance compareding with the otheranother two strategies, which can be shown in the 'overall' met-ric. Theis overall metric indicates that our approach performs better than 'distinguish faults' strategy, and—which is better than the 'regard as one fault' strategy.

**Formatted:** Font: Italic, No underline, Font color: Auto

Therefore, the answer we got for **Q2** is <u>that</u>: Qour approach <u>achievesget a</u> better performance than <u>the</u> two traditional strategies when handling masking effects <u>at anin a</u> acceptable extra cost.

#### 6.3. Evaluating the ILP-based test case searching method

The third empirical study aims to evaluate the efficiency of the ILP-based test case searching component in our approach. To conduct this study, we implemented an FCI approach which is also augmented by the with replacing test cases strategy, but the test case replacing process is by random.

6.3.1. Study setup. The setup of this case study is based on the second case study, and uses in fact, we use the same SUT model as in Table XXI. Then, we apply the newly randomly searching based FCI approach to identifyen identifying the MFS in these prepared SUTs. In order tTo avoid the bias that comes from the randomness, we repeat the newly approach 30 times to identify the MFS in each faileding test case. We will compute the average additional test cases as well as other metrics listed in the precise section of the random-based approach.

6.3.2. Result and discussion. The evaluation of this random-based approach is also shownlist-ed in Table XXII. Compareding with to our ILP-based approach, we observed that there is little distinction between them in terms of the metrics: accurate schemas, parent-schemas, sub-schemas, ignored schemas, irrelevant schemas\_(the ILP-based approach performs a-slightly better, e.g., for subject HSQL2cr8, the ILP-based approach identified less sub-parents \_\_npar-ent and irrelevant schemas than the random-based \_procedure). This is because the two approaches is both use the test case replacing strategy, so when examininge a schema, both of this two ap-proaches may obtainget the same result, although the test cases generated will be different. However, when considering the cost of each approach will take, we can find the ILP-based approach performs better, which can reduces in the average to 1 or - 2 test cases less than random-based procedureone.

In summary, the answer for Q3 is that: How to searching for a satisfied test case does have in-fluence on the performance offer our approach, especially regardingat the number of needed extra test cases needed, and the ILP\_based test cases can handle the masking effects at a relatively smaller cost than then the random-based approach can.

## 6.4. Comparisoncompare with Feedback\_-driven combinatorial testing

The FDA-CIT [Yilmaz et al. 2013] approach can handles masking effects so that the covering array it generates can cover all the t-way schemas without being masked by the MFS. There is an integrated FCI approach in of the FDA-CIT, of which this FCI approach has two versions, i.e., ternary-class and multiple-class. In this paper, we use the multiple-class version foras our comparativeed approach, as Yilmaz it is claimsed that the multiple-class version performs better than the former in [Yilmaz et al. 2013].

6.4.1. Study setup. As the FCI approach of FDA-CIT <u>uses</u> a post-analysis\_(classified tree) technique on given test cases, in this paper the same as [Yilmaz et al. 2013] we fed the FDA-CIT the covering array as the input just as was done in the Yilmaz study [Yilmaz et al. 2013].

**Formatted:** Font: Italic, No underline, Font color: Auto

The covering arrays we generated are ranged from 2-4 ways. The covering array generating method we used is that contained in [Cohen et al. 2003].

**Formatted:** Font: Italic, No underline, Font color: Auto

as it can be easily extended with constraints dealing and seeds injecting [Cohen *et al.* 2007b], which is needed in the FDA-CIT process. As different test cases will influence the results of the characterization process, so-we repeated generating 30 different 2-4 way covering arrays and fed them into the FDA-CIT. Then, we recorded the results of this approach, which consists of the metrics mentioned in the second case study.

Besides the FDA-CIT, we also applied our ILP-based approach to the en-generated the covering array. SpecificallyIn specific, for each failing test case in the covering array, we separately appliedy our approach to identify the MFS in that case. In fact, we can reduce the number of extra test cases if we utilize the other test cases in the covering array [Li et al. 2012]), but we didn't utilize the information tofer simplify the experiment. We then merged all the test cases that our approach needed for each failing test case in the covering array, and we also merged other metrics listed in the second case study for each failing test cases.

As our approach generated different test cases from the FDA-CIT, we also letused the multiple-class FCI approach of FDA-CIT to characterize the MFS using the test cases generated by our approach, so that we couldean get obtain a fairermore fair result with which to evaluate when evaluating the FCI approach.

6.4.2. Result and discussion. We ist the average result of the 30\_-times experiment for the FDA-CIT, ILP-based approach, and FDA-CIT using our test cases (FDAs), respectively, in Table XXII. The result is organised almost the same way as in Table XXII, except that we have added a t column which indicates the strength of the covering array we generated for this experiment.

Table XXIII: Comparison with FDA-CIT

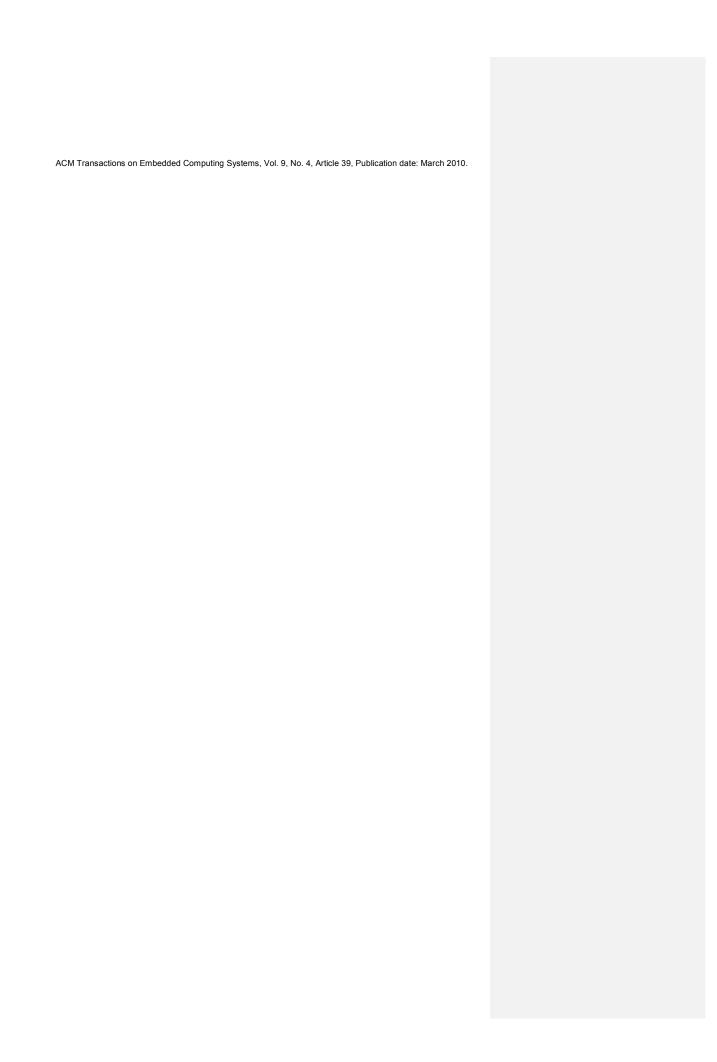
Subject		accurate			sub			parent			ignore		
	t	FDA	ILP	FDA-s	FDA	ILP	FDA-s	FDA	ILP	FDA-s	FDA	ILP	FDA-s
HSQL2cr8	2	0.17	2.27	1.57	0.57	0	0	0.17	0.4	2.17	3.87	2.3	2
	3	1.47	3.67	1	0	0	0	4.67	2	6.07	0.63	0.3	0.17
	4	0.83	4.8	1	0	0	0	9.03	3.37	8	0	0	0
HSQL2.2.5	2	1	1.97	0.37	0	0	0	2.4	0.73	3.8	0.4	0	0
	3	0	2	0.4	0	0	0	5	1	3.8	0	0	0
	4	0	2	0.33	0	0	0	5	1	4	0	0	0
HSQL2.2.9	2	0.9	1.77	0.9	0	0.77	9	1.47	0.47	6.8	1.93	0.53	0
	3	1	2	0.83	0	1	0	5.13	0.93	7.1	0.2	0	0
	4	1	2	1	0	1	0	5.87	1	6.7	0	0	0
JFlex 1.4.1	2	0	2	0	0	0	0	4.03	0	4	0	0	0
	3	0	2	0	0	0	0	4	0	0	0	0	4
	4	0	2	0	0	0	0	4	0	0	0	0	0
JFlex 1.4.2	2	0.3	1.97	0.93	0	0	0	3.6	1	2.16	0.03	0	0
	3	0	2	0.97	0	0	0	5	1	2.1	0	0	0
	4	0	2	1	0	0	0	5	1	2	0	0	0
synthez 1	2	0.97	1	1	0	0	0	1.7	1.93	2	0	0.07	0
	3	1	1	1	0	0	0	2	2	2	0	0	0
	4	1	1	1	0	0	0	2	2	2	0	0	0
synthez 2	2	0.17	1.3	0.73	0.37	0	0	0	0.4	2.37	2.27	1.2	1.03
	3	0.73	2.23	0.5	0	0	0	1.9	1.3	7.1	1.2	0.43	0.53
	4	0.63	2.97	0.1	0	0	0	5.3	2.33	16.1	0.53	0	0
synthez 3	2	0.43	2.97	0.73	0	0.93	0	4.3	1.73	5.3	0.47	0.17	0.5

Continued on next page

**Formatted:** Font: Italic, No underline, Font color: Auto

**Formatted:** Font: Italic, No underline, Font color: Auto

**Formatted:** Font: Not Italic, No underline, Font color: Auto



**Formatted:** Font: Italic, No underline, Font color: Auto

1	3	0.2	3	0.87	О	1.57	0	7.2	3.67	6.57	0.07	0	0
		0.03	3	1	0	1.97	0	10.4	3	6	0	0	0
synthez 4	2	0.3	2.3	0.33	0.07	0.63	0	2.63	1.97	7.7	1.93	0.63	0.4
	3	0.37	2.97	0.07	0	1.26	0	6.5	3.53	10.97	0.83	0.07	0
	4	0.07	3	0	0	1.77	0	11.7	4.67	11.4	0	0	0
synthez 5	2	0.2	1.2	8.0	0.3	0	0	0.1	0.03	0.83	1.4	0.77	0.97
	3	0.87	1.4	0.53	0	0	0	0.5	0.23	3.03	1	0.6	0.77
	4	0.7	1.9	0.37	0	0	0	1.77	0.33	6.5	0.9	0.1	0.03
synthez 6	2	0.23	2.63	0.17	0.2	2	0	2.93	1.63	9.63	2.6	0.5	0.4
	3	0.1	3	0.1	0	2.83	0	7.4	3.83	12.5	1.2	0.17	0.03
	4	0	3	0	0	3.8	0	10.2	6.03	14.5	0.47	0	0
synthez 7	2	0.13	1.43	0.83	0.23	0	0	0.1	0.63	1.4	2.53	1.03	0.93
	3	0.87	2.17	0.93	0	0	0	0.43	1.23	2.97	1.77	0.17	0.13
	4	1	2.87	1	0	0	0	3.23	2.53	4.6	0.27	0	0
synthez 8	2	0	0.2	0.17	0.03	0	0	0	0	0.03	0.3	0.13	0.13
	3	0	0.6	0.5	0.1	0	0	0	0	0.03	0.97	0.47	0.53
	4	0	1.33	8.0	0.1	0	0	0	0.07	0.67	1.53	0.4	0.5
synthez 9	2	1	1	1	0	0	0	0.46	0.6	0.77	0.53	0	0.23
	3	1	1	1	0	0	0	1	1	1	0	0	0
	4	1	1	1	0	0	0	1	1	1	0	0	0
synthez10	2	0	0.63	0	0.6	1	0.2	0	0	0.83	1.8	0.37	1.9
	3	0.07	0.97	0	0.23	1	0.03	0.36	0	1.9	2.23	0.03	1.97
	4	0	1	0	0.07	1	0	1.7	0	2	1.87	0	2

	irrelevant			overall			test cases		
t	FDA	ILP	FDA-s	FDA	ILP	FDA-s	FDA	ILP	FDA-s
2	2.53	0	1.97	0.12	0.51	0.39	23.6	70.1	70.1
3	3	0	1.47	0.51	0.87	0.6	76.6	241.8	241.8
4	0.97	0	0	0.65	0.9	0.71	183.5	606.6	606.6
2	1.4	0	0.1	0.38	0.87	0.56	26.7	68.8	68.8
3	0	0	0	0.52	0.83	0.56	67	202.4	202.4
4	0	0	0	0.53	0.83	0.56	130.1	503.3	503.3
2	2.37	0	0.2	0.28	0.72	0.58	29.2	78.3	78.3
3	0.1	0	0	0.61	8.0	0.61	72.8	221.7	221.7
4	0	0	0	0.64	8.0	0.62	129.8	560.3	560.3
2	0	0	0	0.49	1	0.5	30.5	87.3	87.3
3	0	0	0	0.5	1	0.5	73.4	269.2	269.2
4	0	0	0	0.5	1	0.5	190.6	724.7	724.7
2	0.63	0	0	0.5	0.83	0.62	34.3	106.9	106.9
3	0.03	0	0	0.52	0.83	0.61	72.3	305.7	305.7
4	0	0	0	0.53	0.83	0.61	186.8	836.9	836.9
2	0.33	14.3	0	0.66	0.13	0.78	40.3	342.87	342.87
3	0	16.73	0	0.78	0.12	0.78	93.4	809.1	809.1
4	0	17	0	0.78	0.12	0.78	218.8	1532.8	1532.8
2	1.37	0	1.2	0.11	0.52	0.4	19.77	54.4	54.4
3	2.2	0	1.33	0.36	0.82	0.52	59.5	171.5	171.5
4	2.6	0	1	0.44	0.89	0.54	152.7	415.1	415.1

Continued on next page

2	1.03	3.77	1.13	0.37	0.46	0.37	48.6	138.7	138.7
3	0.83	6.77	0.07	0.38	0.38	0.44	106.3	315.3	315.3
4	0.43	8.56	0	0.38	0.34	0.45	147.9	565.7	565.7
2	3.4	1.4	1.97	0.24	0.6	0.44	42.7	142.2	142.2
3	2.5	3.43	1.03	0.39	0.54	0.51	86.5	373.2	373.2
4	1.33	6.73	0.03	0.48	0.44	0.55	202.2	899.7	899.7
2	0.7	0	1	0.2	0.59	0.4	21.9	46.9	46.9
3	0.37	0	1.63	0.46	0.71	0.43	76.9	150.3	150.3
4	1.87	0	2.03	0.34	0.92	0.54	232.9	433.2	433.2
2	3.03	3.7	2	0.19	0.42	0.37	45.7	132.6	132.6
3	2.3	6.5	0.67	0.31	0.38	0.43	99.5	338.9	338.9
4	1.8	9.1	0.03	0.37	0.36	0.44	152.6	781.9	781.9
2	1.93	0	1.97	0.09	0.61	0.38	20.3	58.8	58.8
3	3.2	0	2.87	0.2	88.0	0.44	52.6	164.7	164.7
4	4.5	0	2.27	0.35	0.9	0.51	145.3	413.1	413.1
2	0.17	0	0.3	0.01	0.1	0.05	16.1	45.2	45.2
3	0.63	0	0.87	0.02	0.3	0.17	43.1	64.3	64.3
4	1.4	0	0.93	0.04	0.67	0.41	109.3	145.6	145.6
2	0.63	0.6	0.67	0.54	0.7	0.6	36.2	43.4	43.4
3	0	0	0	0.83	0.83	0.83	84.3	145	145
4	0	0	0	0.83	0.83	0.83	188	291.6	291.6
2	1.5	0.3	3.97	0.23	0.61	0.17	23.4	84.9	84.9
3	4.03	0.53	3.97	0.13	0.66	0.2	73.4	263.2	263.2
4	4.03	1	4	0.21	0.58	0.2	202.2	685.9	685.9

From this result, we can first observe that in all the cases our ILP-based approach can identify more accurately identify the MFS and ignores less ignored MFS than the FDA-CIT approach. For the metric 'parent-schema', 'sub-schema', and 'irrelevant schemas', there are is ups and downs on both sides. With respect to the 'overall metric', we can find our approach hasve a significant advantage over the FDA-CIT, but it also requires needed much many more test cases than FDA-CIT.

We note!t is noted that, when applying the multiple-class FCI toon the test cases generated using our approach, their 'overall' metricire is still not as good as our ILP-based approach, but may showget some improvement overthan the original FDA-CIT.

Another interesting observation is that overall performance in most cases is increasing with the t, whichit can be easily understood: mMore test cases will contain more information about the MFS, so that we can utilize them to identifyied the MFS more precisely.

So the answer for the Q4 is: that Oour approach can achieveget a more precise result for about the MFS, and the FDA-CIT can performmake the identifying process using a small amount of extra test cases. Both of these two approaches have their ups and downs, choosing which approach in practice will depend on the specific scenario you test.

## 6.5. Threats to validity

There are several threats to <u>the</u> validity <u>offer</u> these empirical studies. First, we have only surveyed two <u>types of</u> open-source software with five different versions, of which the program scale is medium-sized. This may impact the generality of our observations. Although we believe it is quite possibly a common phenomenon in most software that

 $\hbox{contain$\underline{s}$ multiple faults which can mask each other, we need to investigate more software to support our $\underbrace{\hbox{belief}_{\hbox{conjecture}}}.$ 

**Formatted:** Font: Italic, No underline, Font color: Auto

The second threat comes from the input model we built. As we focused on the option-s related to the perfect combinations and only augmented it with some noise options, there is a chance we will get different results if we choose other noise options. More options need to be testeddifferent options needed to be opted to see whether our result is common or just appearsed in some particular input models.

The third threat is that we just evaluated one FCI approach – FIC BS [Zhang and Zhang 2011], so further works needsed to examine more algorithms in this fieldfiled to obtained a more general result.

### 7. RELATED WORKS

Shi and Nie presented a further testing strategy for fault revealing and failure diag-nosis[Shi et al. 2005], which first tests the SUT with a covering array, then reduces the value schemas contained in the failed test case by eliminating those appearing in the passed test cases. If the failure-causing schema is found in the reduced schema set, failure diagnosis is completed with the identification of the specific input values which caused the failure; otherwise, a further test suite based on SOFOT is developed for each failed test cases, testing is repeated, and the schema set is then further reduced, until no more failures is are found or the fault ishas-been located—. Based on this work, Wang pro-posed an AIFL approach which extended the SOFOT process by mutating the changeding strength in each iteration that of characterizeding failure-inducing combinations[Wang et al. 2010].

Nie et al. introduced the notion of Minimal Failure-causing Schema(MFS) and pro-posed the OFOT approach which is an extension of extended from SOFOT that can isolate the MFS in SUT\_[Nie and Leung 2011a]. The approach mutates one value with different values for that parameter, hence generating a group of additional test cases each time to be ex-ecuted. Compared with SOFOT, this approach strengthens the validation of the factor under analysis and also can detect the newly imported faulty combinations.

Delta debugging proposed by Zeller [Zeller and Hildebrandt 2002] proposed by Zeller is an adaptive divide-and-conquer approach to locate interaction faults. It is very efficient and has been applied in ato real software environment. Zhang et al. also proposed a similar ap-proach that can efficiently identify the failure-inducing combinations that haves no overlapped part efficiently [Zhang and Zhang 2011]. Later, Li improved the delta-debugging based failure-inducing combination by exploiting the useful information in the executed cov-ering array[Li et al. 2012].

Colbourn and McClary proposed a non-adaptive method [Colbourn and McClary 2008]. Their approach extends the covering array to the locating array to detect and locate interaction faults. C. Martinez proposed two adaptive algorithms. The first one requires aneeds safe value as their assumption, and the second one removes the assumption when the number of values of each parameter is equal to 2 [Mart'+nez et al. 2008; 2009]. Their algorithms focus on identifying the faulty tuples that have no more than 2 parameters.

Ghandehari et al. defined the suspiciousness of tuple and suspiciousness of the environment of a tuple\_[Ghandehari et al. 2012]. Based on this, they rank the pos-sible tuples and generate the test configurations. They further utilized the test cas-es generated from the inducing combination to locate the faults inside the source code\_[Ghandehari et al. 2013].

Yilmaz proposed a machine learning method to identify inducing combinations from a combinatorial testing set [Yilmaz et al. 2006]. They constructed a classified tree to ana-lyze the covering arrays and detect potential faulty combinations. Beside this, Fouche' [Fouche' et al. 2009] and Shakya [Shakya et al. 2012] made some improvements in identifying failure-inducing combinations based on Yilmaz's work.

Our previous work [Niu et al. 2013] have proposed an approach that utilizes the tuple relationship tree to isolate the failure-inducing combinations in a failing test case.

One

novelty of this approach is that it can identify the overlapped faulty combinations. This work also alleviates the problem of introducing newly failure-inducing combinations in additional test cases.

In addition to the <u>studiesworks</u> that aims at identifying the failure-inducing combinations in test cases, there are <u>others that</u>some studies focus on working around the masking effects.

With having known masking effects in prior. Cohen Cohen et al. 2007a; 2007b; 2008] studied the impacts of that the masking effects that render some generated test cases invalid in CT\_, and they He proposed anthe approach that integrates the incremental SAT solver with a covering array that generateding algorithms to avoid these masking effects in the process of generating test cases, generating process. Further study was conducted [Petke et al. 2013] to show the fact that with considering constrains, the higher—strength covering arrays with early fault detection are is practical. Besides, additional constraints impactings in CT were studied in the following works:works like [Garvin et al. 2011; Bryce and Colbeum 2006; Calvagna and Gargantini 2008; Grindal et al. 2006; Yilmaz 2013].

Chen et al. addressed the issues of shielding parameters in combinatorial testing and proposed the Mixed Covering Array with Shielding Parameters (MCAS) to solve the problem caused by shielding parameters [Chen et al. 2010]. The shielding parameters can disable some parameter values to expose additional interaction errors, which can be regarded as a special case of masking effects.

Dumlu and Yilmaz proposed a feedback-driven approach to work around the mask-ing effects [Dumlu et al. 2011]. Specifically, theyIn-specific, it first used CTA to classify the possible failure-inducing combinations and then eliminate them and generate new test cases to detect possible masked interaction in the next iteration. They further extended their work [Y-ilmaz et al. 2013], by proposingin which they proposed a multiple-class CTA approach to distinguish faults in SUT. In addition, they empirically studied the impacts on both ternary-class and multiple-class CTA approaches.

Our work differs from these ones mainly in the fact that we formally studied the masking effects on FCI approaches and further proposed a divide-and-conquer strate-gy to alleviate this impact.

#### 8. CONCLUSIONS

Masking effects of multiple faults in SUT can bias the results of traditional failure-inducing combinations identifying approaches. In this paper, we formally analysed the impact of masking effects on FCI approaches and showed that <a href="mailto:theboth">theboth</a> two traditional strategies are <a href="mailto:both">both</a> inefficient in handling such impact. We further presented a divide-and-conquer strategy for FCI approaches to alleviate <a href="mailto:suchthis">suchthis</a> impact.

In <u>ourthe</u> empirical studies, we extended FCI approach—FIC BS\_[Zhang and Zhang 2011] with our strategy. The comparison between our approach <u>andwith</u> its\_traditional <u>approachesones</u> wasere <u>performed</u> on several <u>kinds</u> of open-source software. The results indicated that our strategy do—assists <u>the</u> traditional FCI approach in <u>achievinggetting</u> a better performance when fac-ing masking effects in SUT. <u>In our approach</u>, <u>Ww</u>e also empirically evaluated the <u>the</u> efficiency of the test case searching component in our approach—by comparing it with <u>the</u> randomly searching based FCI approach, <u>of which</u> the results shows that the ILP—based test case searching method can perform much more efficiently. At ILast, we compared our approach with ex-istinged techniqs for handling masking effects handling technique—FDA-CIT[ Yilmaz <u>et al.</u> 2013], and observed that our approach achevedean get a more precise result which can

**Formatted:** Font: Italic, No underline, Font color: Auto

support better debugging aids, though our approach  $\frac{\text{need-generat}\underline{\text{es}}\text{ing}}{\text{more test cases}}$  than FDA-CIT.

As <u>fora</u> future work, we need to do more empirical studies to make our conclusions more general. Our current experiments focus onal subjects are several middle-sized software, www e would like to extend our approach into more complicated, and large-scaled testing scenarios. Another promising work in the future is to combine the white-box testing tech-nique to <u>facilitate obtaining more accurate results from FCI approaches when handling masking effects.</u> make the FCI approaches get more accurate results when handling masking

39:38 X. Niu et al.

effects.—We believe that figuring out the fault levels of different bugs through the white-box testing technique is helpful to reduce misjudgements in the failure-inducing combinations identifying process. Andt last, because the extent to whichat the FCI suffers from masking effects varies within different algorithms, athe combination of different FCI approaches would be desirable desired in the future to further improve the performance for identifying MFS for mul-tiple faults.

#### REFERENCES

- James Bach and Patrick Schroeder. 2004. Pairwise testing: A best practice that isnt. In *Proceedings of 22nd Pacific Northwest Software Quality Conference*. Citeseer, 180–196.
- Michel Berkelaar, Kjell Eikland, and Peter Notebaert. 2004. lp solve 5.5, Open source (Mixed-Integer) Lin-ear Programming system. Software. (May 1 2004). http://lpsolve.sourceforge.net/5.5/ Last accessed Dec, 18 2009.
- Renee' C Bryce and Charles J Colbourn. 2006. Prioritized interaction testing for pair-wise coverage with seeding and constraints. *Information and Software Technology* 48, 10 (2006), 960–970.
- Renee' C Bryce, Charles J Colbourn, and Myra B Cohen. 2005. A framework of greedy methods for constructing interaction test suites. In *Proceedings of the 27th international conference on Software engineering*. ACM, 146–155.
- Andrea Calvagna and Angelo Gargantini. 2008. A logic-based approach to combinatorial testing with constraints. In *Tests and proofs*. Springer, 66–83.
- Baiqiang Chen, Jun Yan, and Jian Zhang. 2010. Combinatorial testing with shielding parameters. In Soft-ware Engineering Conference (APSEC), 2010 17th Asia Pacific. IEEE, 280–289.
- David M. Cohen, Siddhartha R. Dalal, Michael L Fredman, and Gardner C. Patton. 1997. The AETG system: An approach to testing based on combinatorial design. Software Engineering, IEEE Transactions on 23, 7 (1997), 437–444.
- Myra B Cohen, Charles J Colbourn, and Alan CH Ling. 2003. Augmenting simulated annealing to build interaction test suites. In Software Reliability Engineering, 2003. ISSRE 2003. 14th International Symposium on. IEEE, 394–405.
- Myra B Cohen, Matthew B Dwyer, and Jiangfan Shi. 2007a. Exploiting constraint solving history to con-struct interaction test suites. In Testing: Academic and Industrial Conference Practice and Research Techniques-MUTATION, 2007. IEEE, 121–132.
- Myra B Cohen, Matthew B Dwyer, and Jiangfan Shi. 2007b. Interaction testing of highly-configurable sys-tems in the presence of constraints. In *Proceedings of the 2007 international symposium on Software testing and analysis*. ACM, 129–139.
- Myra B Cohen, Matthew B Dwyer, and Jiangfan Shi. 2008. Constructing interaction test suites for highly-configurable systems in the presence of constraints: A greedy approach. Software Engineering, IEEE Transactions on 34, 5 (2008), 633–650.
- Myra B Cohen, Peter B Gibbons, Warwick B Mugridge, and Charles J Colbourn. 2003. Constructing test suites for interaction testing. In Software Engineering, 2003. Proceedings. 25th International Conference on. IEEE, 38–48.
- Charles J Colbourn and Daniel W McClary. 2008. Locating and detecting arrays for interaction faults. *Jour-nal of combinatorial optimization* 15, 1 (2008), 17–48.
- Emine Dumlu, Cemal Yilmaz, Myra B Cohen, and Adam Porter. 2011. Feedback driven adaptive combina-torial testing. In Proceedings of the 2011 International Symposium on Software Testing and Analysis. ACM, 243–253.
- Sandro Fouche, Myra B Cohen, and Adam Porter. 2009. Incremental covering array failure characterization in large configuration spaces. In *Proceedings of the eighteenth international symposium on Software testing and analysis*. ACM, 177–188.
- Brady J Garvin, Myra B Cohen, and Matthew B Dwyer. 2011. Evaluating improvements to a meta-heuristic search for constrained interaction testing. *Empirical Software Engineering* 16, 1 (2011), 61–102.
- Laleh Sh Ghandehari, Yu Lei, David Kung, Raghu Kacker, and Richard Kuhn. 2013. Fault localization based on failure-inducing combinations. In *Software Reliability Engineering (ISSRE)*, 2013 IEEE 24th International Symposium on. IEEE, 168–177.
- Lalen Shikh Gholamhossein Ghandehari, Yu Lei, Tao Xie, Richard Kuhn, and Raghu Kacker. 2012. Iden-tifying failure-inducing combinations in a combinatorial test set. In Software Testing, Verification and Validation (ICST), 2012 IEEE Fifth International Conference on. IEEE, 370–379.

 $Mats\ Grindal, Jeff\ Offutt, and\ Jonas\ Mellin.\ 2006.\ Handling\ constraints\ in\ the\ input\ space\ when\ using\ combination\ strategies\ for\ software\ testing.\ (2006).$ 

Mark Hall, Eibe Frank, Geoffrey Holmes, Bernhard Pfahringer, Peter Reutemann, and Ian H Witten. 2009. The WEKA Data Mining Software: An Update; SIGKDD Explorations, Volume 11, Issue 1.

Jie Li, Changhai Nie, and Yu Lei. 2012. Improved Delta Debugging Based on Combinatorial Testing. In Quality Software (QSIC), 2012 12th International Conference on. IEEE, 102-105.

Conrado Mart'mez, Lucia Moura, Daniel Panario, and Brett Stevens. 2008. Algorithms to locate errors using covering arrays. In LATIN 2008: Theoretical Informatics. Springer, 504–519.

Conrado Mart'ınez, Lucia Moura, Daniel Panario, and Brett Stevens. 2009. Locating errors using ELAs, covering arrays, and adaptive testing algorithms. SIAM Journal on Discrete Mathematics 23, 4 (2009), 1776–1799.

Changhai Nie and Hareton Leung. 2011a. The minimal failure-causing schema of combinatorial testing.

ACM Transactions on Software Engineering and Methodology (TOSEM) 20, 4 (2011), 15.

Changhai Nie and Hareton Leung. 2011b. A survey of combinatorial testing. ACM Computing Surveys (C-SUR) 43, 2 (2011), 11.

Xintao Niu, Changhai Nie, Yu Lei, and Alvin TS Chan. 2013. Identifying Failure-Inducing Combinations Using Tuple Relationship. In Software Testing, Verification and Validation Workshops (ICSTW), 2013 IEEE Sixth International Conference on. IEEE, 271–280.

Justyna Petke, Shin Yoo, Myra B Cohen, and Mark Harman. 2013. Efficiency and early fault detection with lower and higher strength combinatorial interaction testing. In Proceedings of the 2013 9th Joint Meeting on Foundations of Software Engineering. ACM, 26–36.

Kiran Shakya, Tao Xie, Nuo Li, Yu Lei, Raghu Kacker, and Richard Kuhn. 2012. Isolating Failure-Inducing Combinations in Combinatorial Testing using Test Augmentation and Classification. In Software Test-ing, Verification and Validation (ICST), 2012 IEEE Fifth International Conference on. IEEE, 620–623.

Liang Shi, Changhai Nie, and Baowen Xu. 2005. A software debugging method based on pairwise testing. In Computational Science—ICCS 2005. Springer, 1088—1091.

Charles Song, Adam Porter, and Jeffrey S Foster. 2012. (Tree: Efficiently discovering high-coverage con-figurations using interaction trees. In Proceedings of the 2012 International Conference on Software Engineering. IEEE Press, 903–913.

Ziyuan Wang, Baowen Xu, Lin Chen, and Lei Xu. 2010. Adaptive interaction fault location based on combi-natorial testing. In Quality Software (QSIC), 2010 10th International Conference on. IEEE, 495–502.

Cemal Yilmaz. 2013. Test case-aware combinatorial interaction testing. Software Engineering, IEEE Trans-actions on 39, 5 (2013), 684-706.

Cemal Yilmaz, Myra B Cohen, and Adam A Porter. 2006. Covering arrays for efficient fault characterization in complex configuration spaces. Software Engineering, IEEE Transactions on 32,1 (2006), 20–34.

Cemal Yilmaz, Emine Dumlu, M Cohen, and Adam Porter. 2013. Reducing Masking Effects in Combinatorial Interaction Testing: A Feedback Driven Adaptive Approach. (2013).

Andreas Zeller and Ralf Hildebrandt. 2002. Simplifying and isolating failure-inducing input. Software En-gineering, IEEE Transactions on 28, 2 (2002), 183-200.

Zhiqiang Zhang and Jian Zhang. 2011. Characterizing failure-causing parameter interactions by adaptive testing. In Proceedings of the 2011 International Symposium on Software Testing and Analysis. ACM, 331–341.