# Identifying minimal failure-causing schemas in the presence of multiple failures

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Combinatorial testing (CT) has been proven effective in revealing the failures caused by the interaction of factors that affect the behavior of a system. The theory of Minimal Failure-Causing Schema (MFS) has been proposed to isolate the root cause of a failure after detected by CT. Most algorithms that aim to identify MFS focus on handling a single failure in the System Under Test (SUT). However, we argue that multiple failures are the more common testing scenario, under which masking effects may be triggered so that some failures cannot be observed. The traditional MFS theory, as well as the related identifying algorithms, lack a mechanism to handle such effects; hence, they may incorrectly isolate the MFS in the SUT. To address this problem, we propose a new MFS model that takes into account multiple failures. We first formally analyse the impact of the multiple failures on existing MFS identifying algorithms, especially in situations where masking effects are triggered by multiple failures. We then develop an approach that can assist traditional algorithms to better handle multiple failures testing scenario. Empirical studies were conducted using several kinds of open-source software, which showed that multiple failures with masking effects do negatively affect traditional MFS identifying approaches and that our approach can help to alleviate these effects.

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# 1. INTRODUCTION

With the increasing complexity and size of modern software, many factors, such as input parameters and configuration options, can affect the behaviour of the SUT. The unexpected failures caused by the interaction of these factors can make software test-

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Table I. MS word example

id	Highlight	$Status\ bar$	Bookmarks	Smart tags	Outcome
1	On	On	On	On	PASS
2	Off	Off	On	On	PASS
3	Off	On	Off	Off	Fail
4	On	Off	Off	On	PASS
5	On	Off	On	Off	PASS

ing challenging, especially when the interaction space is large. In the worst case, we need to examine every possible interaction of these factors as each interaction may cause unique failure [Song et al. 2012]. While exhaustive testing achieves maximal test coverage, it is impractical and uneconomical. One remedy for this problem is combinatorial testing, which systematically samples the interaction space and selects a relatively small set of test cases that cover all valid interactions, with the number of factors involved in each interaction no more than a prior fixed integer, i.e., the *strength* of the interaction. Many works in CT aim to construct the smallest set of test cases [Cohen et al. 1997; Bryce et al. 2005; Cohen et al. 2003; Lei et al. 2008], which is also called *covering array*.

Once failures are detected by a covering array, the failure-inducing interactions in the failing test cases should be isolated. This task is important as it can facilitate debugging efforts by reducing the code scope that needed for inspection [Ghandehari et al. 2012]. However, information from a covering array sometimes is not sufficient to identify the location and number of the failure-inducing interactions [Colbourn and McClary 2008]. Thus, additional information is needed. Consider the following example [Bach and Schroeder 2004], Table I presents a two-way covering array for testing an MS-Word application in which we want to examine various interactions of options for the MS-Word 'Highlight', 'Status Bar', 'Bookmarks' and 'Smart tags'. Assume the third test case failed. We can get five two-way suspicious interactions that may be responsible for this failure. They are respectively (Highlight: Off, Status Bar: On), (Highlight: Off, Bookmarks: Off), (Highlight: Off, Smart tags: Off), (Status Bar: On, Bookmarks: Off), (Status Bar: On, Smart tags: Off), and (Bookmarks: Off, Smart tags: Off). Without additional information, it is difficult to figure out the specific interactions in this suspicious set caused the failure. In fact, considering that the higher strength interactions could also be failure-inducing interactions, e.g., (Highlight: Off, Status Bar: On, Smart tags: Off), the problem becomes more complicated.

To address this problem, prior work [Nie and Leung 2011a] specifically studied the properties of the minimal failure-causing schemas in SUT, based on which additional test cases were generated to identify the MFS. Other approaches to identify the MFS in SUT include building a tree model [Yilmaz et al. 2006], adaptively generating additional test cases according to the outcome of the last test case [Zhang and Zhang 2011], ranking suspicious interactions based on some rules [Ghandehari et al. 2012], using graphic-based deduction [Martínez et al. 2008], among others.

Most existing approaches mainly focus on the ideal scenario in which SUT only contains one failure, under which the outcomes of test cases can be simply categorized into fail or pass. However, in this paper, we argue that SUT with multiple distinguished failures is the more common testing scenario in practice, and moreover, this affects the effectiveness of Failure-inducing Combinations Identifying(FCI) approaches. One main impact of multiple failures on FCI approaches is the masking effect. A masking effect [Dumlu et al. 2011; Yilmaz et al. 2014] occurs when some failures prevent test cases from checking interactions that are supposed to be tested. Take the Linux command *Grep* for example. We noticed that there are two different failures reported

in the bug tracker system. The first <sup>1</sup> claims that Grep incorrectly matches unicode patterns with '\<\>', while the second <sup>2</sup> claims an incompatibility between option '-c' and '-o'. When we put these two scenarios into one test case, only one failure will be observed, which means the other failure is masked by the observed failure. This effect will prevent test cases from executing normally, leading to incorrect judgment of the correlation between the interactions checked in the test case and the failure that has been masked. This effect was firstly noted by Dumlu and Yilmaz in [Dumlu et al. 2011], in which they found that the masking effects in CT can prevent traditional covering array fail in testing some interactions.

As masking effect can negatively affect the performance of FCI approaches, a natural question is how this effect biases the results of these approaches. In this paper, we formalize the process of identifying the MFS under the circumstances in which masking effects exist in the SUT and try to answer this question. One insight from the formal analysis is that we cannot completely get away from the impact of masking effects even if we do exhaustive testing. Even worse, either ignoring the masking effects or treating multiple failures as one failure is detrimental to the FCI process.

Based on this concern, we propose a strategy to alleviate this impact by adopting the divide and conquer framework, i.e., separately handles each failure in the SUT. For a particular failure under analysis, when applying traditional FCI approaches to identify the failure-inducing interactions, we pick the test cases generated by FCI approaches that trigger any failure other than the failure under analysis and replace them with some newly regenerated test cases. These new test cases should either pass or trigger the same failure under analysis.

The key to our approach is to search for a test case that does not trigger unexpected failures which may introduce the masking effect. To guide the search process, i.e., to reduce the possibility that the newly generated test case will trigger an unexpected failure, a natural idea is to take some characteristics from the existing test cases and make the characteristics of the newly searched test case as different from the test cases which triggered the unexpected failure as possible. To reach this target, we define the related strength between the factor and the failure. The higher the related strength between a factor and a particular failure, the greater the likelihood that the factor will trigger this failure. We then use the integer linear programming (ILP) technique to find a test case which has the least related strength with the unexpected failure.

To evaluate the effectiveness of our approach, we applied our strategy on the FCI approach FIC\_BS [Zhang and Zhang 2011]. The subjects used were two open-source software systems found in the developers' forum in the Source-Forge community. Through studying their bug reports in the bug tracker system as well as their user's manuals, we built a testing model which can reproduce the reported bugs with given test cases. We then compared the FCI approach augmented with our strategy to the original FCI approach. We further empirically studied the performance of the important component of our strategy – searching satisfied test cases. To conduct this study, we compared our approach with the augmented FCI approach by randomly searching satisfied test cases. We finally compared our approach with the only existing masking handling technique – FDA-CIT [Yilmaz et al. 2014]. Our studies showed that our replacing strategy as well as the searching test case component achieved a better performance than the traditional approaches when the subject suffered multiple failures, especially when these failures can import masking effects.

The main contributions of this paper are:

<sup>&</sup>lt;sup>1</sup>http://savannah.gnu.org/bugs/?29537

<sup>&</sup>lt;sup>2</sup>http://savannah.gnu.org/bugs/?33080

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```
public float foo(int a, int b, int c, int d){
   //step 1 will cause an exception when b == c
   float x = (float)a / (b - c);

   //step 2 will cause an exception when c < d
   float y = Math.sqrt(c - d);

   return x+y;
}</pre>
```

Fig. 1. A simple program foo with four input parameters

- We studied the impact of the masking effects caused by multiple failures on the isolation of the failure-inducing interactions in SUT.
- We proposed a divide and conquer strategy for selecting test cases to alleviate the impact of these effects.
- We designed an efficient test case searching method which can find a test case that does not trigger an unexpected failure.
- We conducted several empirical studies and showed that our strategy can assist FCI approaches to achieve better performance in identifying failure-inducing interactions in SUT with masking effects.

#### 2. MOTIVATING EXAMPLE

We constructed a small example to illustrate the motivation of our approach. Assume a method *foo* has four input parameters: a, b, c, and d. The four parameter types are all integers and their values are:  $v_a = \{7,11\}, v_b = \{2,4,5\}, v_c = \{4,6\}, v_d = \{3,5\}$ . The code of *foo* is shown in Figure 1.

There are two potential failures of foo: first, in step 1 we can get an Arithmetic Exception when b is equal to c, i.e., b=4 and c=4, that causes a division by zero. Second, another Arithmetic Exception will be triggered in step 2 when c < d, i.e., c=4 and d=5, taking square root of a negative number. So the expected failure-inducing interactions in this example should be (-, 4, 4, -) and (-, -, 4, 5).

Traditional FCI algorithms do not consider the code detail; instead, they apply black-box testing, i.e., feed inputs to the programs and execute them to observe the result. The basic justification behind those approaches is that the failure-inducing interactions for a particular failure can only appear in those test cases that trigger this failure. Traditional FCI approaches aim at using as few test cases as possible to get the same (or approximate) result as exhaustive testing, so the results derived from an exhaustive testing set are the best that these FCI approaches can achieve. Next, we will show how exhaustive testing works to identify the failure-inducing interactions for the program.

We first generate every possible test case listed in the column "test case" of Table II. The execution results are listed in the result column of Table II. In this column, PASS means that the program runs without any exception.  $Ex\ 1$  indicates that the program triggered an exception corresponding to step 1 and  $Ex\ 2$  indicates the program triggered an exception corresponding to step 2. From the data listed in Table II, we can determine that (-,4,4,-) must be the failure-inducing interaction of  $Ex\ 1$  as all the test cases that triggered  $Ex\ 1$  contain this interaction. Similarly, interactions (-,2,4,5) and (-,5,4,5) must be the failure-inducing interactions of  $Ex\ 2$ . We list these interactions and the corresponding exceptions in Table III.

Note that in this example we did not get the expected result with traditional FCI approaches. The failure-inducing interactions for Ex 2 are (-,2,4,5) and (-,5,4,5), re-

id	test case	result	id	test case	result
1	(7, 2, 4, 3)	PASS	13	(11, 2, 4, 3)	PASS
2	(7, 2, 4, 5)	Ex 2	14	(11, 2, 4, 5)	Ex 2
3	(7, 2, 6, 3)	PASS	15	(11, 2, 6, 3)	PASS
$\overline{4}$	(7, 2, 6, 5)	PASS	16	(11, 2, 6, 5)	PASS
5	(7, 4, 4, 3)	Ex 1	17	(11, 4, 4, 3)	Ex 1
6	(7, 4, 4, 5)	Ex 1	18	(11, 4, 4, 5)	Ex 1
7	(7, 4, 6, 3)	PASS	19	(11, 4, 6, 3)	PASS
8	(7, 4, 6, 5)	PASS	20	(11, 4, 6, 5)	PASS
9	(7, 5, 4, 3)	PASS	21	(11, 5, 4, 3)	PASS
10	(7, 5, 4, 5)	Ex 2	22	(11, 5, 4, 5)	Ex 2
11	(7, 5, 6, 3)	PASS	23	(11, 5, 6, 3)	PASS
12	(7, 5, 6, 5)	PASS	24	(11, 5, 6, 5)	PASS

Table II. test cases and their corresponding result

Table III. Identified failure-inducing interactions and their corresponding Exception

Failure-inducing interaction	Exception
(-, 4, 4, -)	Ex 1
(-, 2, 4, 5)	Ex 2
(-, 5, 4, 5)	Ex 2

spectively, instead of the expected interaction (-,-,4,5). So why did we fail to get the (-,-,4,5)? The reason lies in *test case* 6 (7,4,4,5) and *test case* 18 (11,4,4,5). These two test cases contain the interaction (-,-,4,5), but they did not trigger Ex 2; instead, Ex 1 was triggered.

Now consider the source code of *foo*. We can find that if Ex 1 is triggered, it will stop executing the remaining code and report the exception result. In other word, Ex 1 may mask Ex 2. Let us re-examine the interaction (-,-,4,5). If we suppose that *test case 6* and *test case 18* should trigger Ex 2 if they did not trigger Ex 1, then we can conclude that (-,-,4,5) should be the failure-inducing interaction of Ex 2, which is identical to the expected one.

Unless we fix the code that triggers Ex 1 and re-execute all the test cases, we cannot validate the supposition that *test case 6* and *test case 18* should trigger Ex 2 in case they did not trigger Ex 1. So in practice, when we lack resources to execute all the test cases repeatedly or can only do black-box testing, a more economical and efficient approach to alleviate the masking effect on FCI approaches is desired.

#### 3. FORMAL MODEL OF MINIMAL FAILURE-CAUSING SCHEMA

This section presents some definitions and propositions for a formal model to solve the FCI problem.

# 3.1. Minimal Failure-causing Schemas in CT

Assume that the behaviour of SUT is influenced by k parameters, and each parameter  $p_i$  has  $a_i$  discrete values from the finite set  $V_i$ , i.e.,  $a_i = |V_i|$  (i = 1,2,...,k). In practice, these parameters can represent many factors, such as input variables, run-time options, building options, etc. Next we will give some formal definitions, some of them (Definitions 3.1, 3.3, 3.4) were originally defined in [Nie and Leung 2011b].

*Definition* 3.1. A *test case* of SUT is an array of k values, one for each parameter of the SUT, which is denoted as a k-tuple  $(v_1, v_2, ..., v_k)$ , where  $v_1 \in V_1, v_2 \in V_2 ... v_k \in V_k$ .

For example in Section 2, (a = 7, b = 2, c = 4, d = 3) is a test case, which is actually a group of values being assigned to each input parameter.

*Definition* 3.2. A *failure* is the abnormal execution of a test case.

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In CT, such a *failure* can be a thrown exception, compilation error, assertion failure or constraint violation. In this paper, we focus on studying the impact of multiple *failures* on failure-inducing interactions identification. To facilitate our discussion, we introduce the following assumptions that will be used throughout this paper:

Assumption 1. The execution result of a test case is deterministic.

This assumption is the most common assumption of CT fault diagnosis. It indicates that the outcome of executing a test case is reproducible and will not be affected by some unexpected random events.

ASSUMPTION 2. Different failures in the SUT can be distinguished by various information such as exception traces, state conditions, or the like.

This assumption indicates that the testers can detect different failures during testing. As different failures will complicate fault diagnosis tasks, distinguishing them is the first step to resolve them.

Now let us consider the condition that some failures are triggered by some test cases. It is then desirable to determine the cause of these failures and hence some parameter values of these failing test cases must be analysed.

Definition 3.3. For the SUT, the  $\tau$ -tuple  $(-,v_{k_1},...,v_{k_t},...)$  is called a  $\tau$ -degree *schema*  $(0 < \tau \le k)$  when some  $\tau$  parameters have fixed values and the others can take on their respective allowable values, represented as "-".

When  $\tau = k$ ,  $\tau$ -degree *schema* is actually a test case. Furthermore, if every fixed value in a schema is in a test case, we say this test case *contains* the schema.

For example, (-, 4, 4, -) in Table III is a 2-degree schema. And the test case (7, 4, 4, 3) contains this schema.

Definition 3.4. Let  $c_1$  be a m-degree schema,  $c_2$  be an n-degree schema in SUT, and m < n. If all the fixed parameter values in  $c_1$  are also in  $c_2$ , then  $c_2$  subsumes  $c_1$ . In this case, we can also say that  $c_1$  is a sub-schema of  $c_2$ , and  $c_2$  is a super-schema of  $c_1$ , denoted as  $c_1 \prec c_2$ .

For example, in the motivating example, the 2-degree schema (-, 4, 4, -) is a subschema of the 3-degree schema (-, 4, 4, 5), that is,  $(-,4,4,-) \prec (-,4,4,5)$ .

According to definition 3.4, it is obviously that the subsuming relationship ' $\prec$ ' is transitive, i.e., if  $c_1 \prec c_2, c_2 \prec c_3$ , then  $c_1 \prec c_3$ .

Definition 3.5. If all test cases contain a schema c, and trigger a particular failure F, then we call c the failure-causing schema of F. Additionally, if none of the subschema of c is the failure-causing schema of F, we then call C the Minimal Failure-causing Schema (MFS) of F.

In fact, MFS is identical to the failure-inducing interactions discussed previously. Identifying MFS helps to focus on the root cause of a failure and thus facilitate the debugging efforts.

Some notations used later are listed below for convenient reference:

- -k: The number of parameters that influence the SUT.
- $-V_i$ : The set of discrete values that the *i*th parameter of SUT can take.
- $-T^*$ : The exhaustive set of test cases for the SUT. For a SUT with k parameters, and each parameter can take  $|V_i|$  values, the number of test cases in  $T^*$  is  $\prod_{i=1}^{i<=k} |V_i|$ . Note that some test cases may be invalid if there exists constraints among the parameters.
- T: A set of test cases. (Similarly for  $T_i, T_j, ....$ )
- $-\bar{T}$ : the complementary test set of T, i.e.,  $\bar{T} \cup T = T^*$ ,  $\bar{T} \cap T = \varnothing$ .

- $-A \setminus B$ : the set of elements that belong to set A but not to B. For example  $T_i \setminus T_j$  indicates the set of test cases that belong to set  $T_i$ , but not to  $T_j$ .
- L : The number of failures contained in the SUT.
- $-F_m$ : The *m*th failure in the SUT ( $1 \le m \le L$ ); for different failures, we can differentiate them based on their exception traces or other information.
- $-T_{F_m}$ : All the test cases that can trigger the failure  $F_m$  in the SUT.
- $-\mathcal{T}(c)$ : All the test cases that contain the schema c in the SUT. Based on the definition of MFS, we know that if schema c is an MFS of  $F_m$ , then  $\mathcal{T}(c) \subseteq T_{F_m}$ .
- $-\mathcal{I}(t)$ : All the schemas that are contained in the test case t, e.g.,  $\mathcal{I}((111)) = \{(1--1)(-1)(-1)(11-)(1-1)(-11)(111)\}.$
- $-\mathcal{I}(T)$ : All the schemas that are contained in test set T, i.e.,  $\mathcal{I}(T) = \bigcup_{t \in T} \mathcal{I}(t)$ .
- $-\mathcal{S}(T)$ : All the schemas that are only contained in test set T (Referred to as *Special schemas*);  $\mathcal{S}(T) = \mathcal{I}(T) \setminus \mathcal{I}(\bar{T})$ .
- $-\mathcal{C}(T)$ : A set of the minimal schemas that are only contained in test set T (Referred to as *Minimal schemas*);  $\mathcal{C}(T) = \{c | c \in \mathcal{S}(T) \text{ and } \exists c' \prec c, s.t., c' \in \mathcal{S}(T)\}.$

#### 3.2. Relations between schemas and test sets

PROPOSITION 3.6 (SMALLER SCHEMA c HAS A LARGER  $\mathcal{T}(c)$ ). For schemas  $c_1$ ,  $c_2$ , if  $c_1 \prec c_2$ , then all the test cases that contain  $c_2$  must also contain  $c_1$ , i.e.,  $\mathcal{T}(c_2) \subset \mathcal{T}(c_1)$ .

PROOF.  $\forall t \in \mathcal{T}(c_2)$ , t contains  $c_2$ . As t is a k-degree schema, then it has  $c_2 \prec t$ . As  $c_1 \prec c_2$ , then  $c_1 \prec t$ , indicating that t contains  $c_1$ . Therefore,  $t \in \mathcal{T}(c_1)$ . So it follows that  $\mathcal{T}(c_2) \subset \mathcal{T}(c_1)$ .  $\square$ 

Suppose a SUT with four binary parameters, which can be denoted as SUT( $2^4$ ). Table IV illustrates an example of the Proposition 3.6. The left column lists the schema  $c_2$  = (0,0,-,-) as well as all the test cases in  $\mathcal{T}(c_2)$ , while the right column lists the schema  $c_1$  = (0,-,-,-) and  $\mathcal{T}(c_1)$ . We can see that when  $c_1 \prec c_2$ ,  $\mathcal{T}(c_2) \subset \mathcal{T}(c_1)$ .

Table IV. Example of Proposition 3.6

	$c_1$
	(0, -, - , -)
$c_2$	$\mathcal{T}(c_1)$
(0, 0, -, -)	(0, 0, 0, 0)
$\mathcal{T}(c_2)$	(0, 0, 0, 1)
(0, 0, 0, 0)	(0, 0, 1, 0)
(0, 0, 0, 1)	(0, 0, 1, 1)
(0, 0, 1, 0)	(0, 1, 0, 0)
(0, 0, 1, 1)	(0, 1, 0, 1)
	(0, 1, 1, 0)
	(0, 1, 1, 1)

Proposition 3.7 (Special schema set of test Set T). For any test set T of the SUT,  $\bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c) = T$ .

PROOF. As  $S(T) = \mathcal{I}(T) \setminus \mathcal{I}(\bar{T})$ ,  $\forall c \in S(T)$ ,  $c \in \mathcal{I}(T)$  and  $c \notin \mathcal{I}(\bar{T})$ . Then  $\forall t \in \mathcal{T}(c)$ , t contains c, indicating that  $t \in T$ . Hence,  $\mathcal{T}(c) \subseteq T$ . Then  $\bigcup_{c \in S(T)} \mathcal{T}(c) \subseteq T$ .

On the other hand,  $\forall t \in T$ ,  $\exists c' \in \mathcal{I}(t)$ , such that  $c' \notin \mathcal{I}(\overline{T})$  (at least it holds when c' = t). Hence,  $c' \in \mathcal{S}(T)$ . Obviously  $t \in \mathcal{T}(c') \subseteq \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c)$ . Therefore,  $T \subseteq \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c)$ .  $\square$ 

Proposition 3.8 (Minimal schema set of test Set T). For any test set T of the SUT,  $\bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c) = T$ .

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PROOF. As  $\mathcal{C}(T) = \{c | c \in \mathcal{S}(T) \ and \ \not\exists c' \prec c, s.t., c' \in \mathcal{S}(T)\}$ , indicating that  $\mathcal{C}(T) \subseteq \mathcal{S}(T)$ . It is then obviously  $\bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c) \subseteq \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c)$ . Hence, we just need to prove that  $\bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c) \subseteq \bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c)$ .

 $\forall t \in \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c), \ \exists c \in \mathcal{S}(T), \ s.t., t \in \mathcal{T}(c).$  According to the definition of  $\mathcal{C}(T), \ \exists c' \in \mathcal{C}(T), s.t., \ c' = c \ or \ c' \prec c.$  Correspondingly  $\mathcal{T}(c') = \mathcal{T}(c), \ or \ \mathcal{T}(c) \subset \mathcal{T}(c')$  by Proposition 3.6. Hence,  $t \in \mathcal{T}(c') \subseteq \bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c).$ 

Therefore,  $\bigcup_{c \in \mathcal{C}(T)} \mathcal{T}(c) = \bigcup_{c \in \mathcal{S}(T)} \mathcal{T}(c) = T$ .  $\square$ 

Table V gives an example of  $T^*$ , T,  $\bar{T}$ ,  $\mathcal{S}(T)$  and  $\mathcal{C}(T)$  in SUT(2<sup>3</sup>). We can find that all the schemas in  $\mathcal{S}(T)$  and  $\mathcal{C}(T)$  are only contained in test set T, and for any  $t \in T$ , it contains at least one schema in  $\mathcal{S}(T)$  and  $\mathcal{C}(T)$ . Additionally,  $\mathcal{C}(T)$  is a minimal schema set which filters those super schemas in  $\mathcal{S}(T)$ .

Table V. Example of the special and minimal schemas

$T^*$	T	$ar{T}$	$\mathcal{S}(T)$	C(T)
(0, 0, 0)	(0, 0, 0)		(0, 0, -)	(0, 0, -)
(0, 0, 1)	(0, 0, 1)		(0, -, 0)	(0, -, 0)
(0, 1, 0)	(0, 1, 0)		(0, 0, 0)	
(0, 1, 1)		(0, 1, 1)	(0, 0, 1)	
(1, 0, 0)		(1, 0, 0)	(0, 1, 0)	
(1, 0, 1)		(1, 0, 1)		
(1, 1, 0)		(1, 1, 0)		
(1, 1, 1)		(1, 1, 1)		

Let  $T_{F_m}$  denotes the set of all the test cases triggering failure  $F_m$ , then  $\mathcal{C}(T_{F_m})$  actually is the MFS set of  $F_m$ .

According to the definition of  $\mathcal{C}(T)$ , one observation is  $\mathcal{C}(T) \subseteq \mathcal{S}(T)$ , and for any schema in  $\mathcal{S}(T)$ , it either belongs to  $\mathcal{C}(T)$ , or is the super schema of one element of  $\mathcal{C}(T)$ , i.e.,  $\forall c \in \mathcal{S}(T), \exists c' \in \mathcal{C}(T), s.t., c' = c, \ or \ c' \prec c.$ 

PROPOSITION 3.9 (MINIMAL SCHEMA OF THE SUBSET OF TEST SET T). For any test set T and schema c of the SUT, if  $\mathcal{T}(c) \subseteq T$ ,  $c \in \mathcal{S}(T)$ .

PROOF. Assume  $c \notin \mathcal{S}(T)$ , i.e.,  $c \notin \mathcal{I}(T) \setminus \mathcal{I}(\bar{T})$ , then  $c \in \mathcal{I}(\bar{T})$ . It indicates that  $\exists t \in \bar{T}, t \ contains \ c$ , hence  $t \in \mathcal{T}(c)$ , which is contradicts that  $\mathcal{T}(c) \subseteq T$ . Therefore,  $c \in \mathcal{S}(T)$ .  $\square$ 

Table VI shows an example of this proposition for  $SUT(2^3)$ . In this table, the test set  $\mathcal{T}(c)$  of schema c is the subset of test set T. As a result, the special schema set  $\mathcal{S}(T)$  of T contains this schema c = (0, 0, -).

Table VI. Example of a minimal schema of the subset of a test set

c	$\mathcal{T}(c)$	T	$\mathcal{S}(T)$
(0, 0, -)	(0, 0, 0)	(0, 0, 0)	(0, -, -)
	(0, 0, 1)	(0, 0, 1)	(0, -, 0)
		(0, 1, 0)	(0, -, 1)
		(0, 1, 1)	(0, 0, -)
			(0, 1, -)
			(0, 0, 0)
			(0, 0, 1)
			(0, 1, 0)
			(0, 1, 1)

Based on Proposition 3.9, as long as  $\mathcal{T}(c) \subseteq T$  for any schema c and any test set T in the SUT, c either belongs to C(T) or is the super-schema of some schema in C(T). Considering a more general scenario, i.e., two test sets  $T_1$ ,  $T_2$  with  $T_2 \subset T_1$ , it must exist some relationships between their minimal schemas  $\mathcal{C}(T_1)$  and  $\mathcal{C}(T_2)$ .

PROPOSITION 3.10 (MINIMAL SCHEMAS IN THE SMALLER TEST SET). For  $T_1$  and  $T_2$  of the SUT with  $T_2 \subset T_1$ , it has  $\forall c_2 \in \mathcal{C}(T_2)$ ,  $\exists c_1 \in \mathcal{C}(T_1)$ , s.t., either  $c_1 = c_2$  or  $c_1 \prec c_2$ .

PROOF.  $\forall c_2 \in \mathcal{C}(T_2), \ \mathcal{T}(c_2) \subseteq T_2 \subset T_1$ . According to Proposition 3.9,  $c_2 \in \mathcal{S}(T_1)$ . According to the definitions of  $\mathcal{S}(T)$  and  $\mathcal{C}(T)$ ,  $\exists c_1 \in \mathcal{C}(T_1), s.t., c_1 = c_2, \ or \ c_1 \prec c_2$ .  $\Box$ 

PROPOSITION 3.11 (MINIMAL SCHEMAS IN THE LARGER TEST SET). For  $T_1$  and  $T_2$  of the SUT,  $T_2 \subset T_1$ . Then  $\forall c_1 \in \mathcal{C}(T_1)$ ,  $\exists c_2 \in \mathcal{C}(T_2), s.t.$ , (1)  $c_1 = c_2$ , or (2)  $c_1 \prec c_2$ , or (3)  $\not\exists c_2 \in \mathcal{C}(T_2), s.t.$ ,  $c_2 \prec c_1$  or  $c_2 = c_1$ , or  $c_1 \prec c_2$ .

Proposition 3.11 is exactly the antithesis of Proposition 3.10. We need to note the third case, i.e.,  $\exists c_2 \in \mathcal{C}(T_2), s.t., c_1 \prec c_2 \ or \ c_1 = c_2, \ or \ c_2 \prec c_1$ . We refer to this case as  $c_1$  is *irrelevant* to  $\mathcal{C}(T_2)$ . Furthermore, we can also say a schema is *irrelevant* to another schema if these two schemas are neither identical nor subsuming each other.

We illustrate these scenarios with examples in Table VII for  $SUT(2^3)$ . There are two parts in this table, with each part showing two test sets:  $T_1$  and  $T_2$ , which have  $T_2 \subset T_1$ . In the left part, the schemas in  $\mathcal{C}(T_2)$ : (0, 0, -) and (0, -, 0), both are the super-schemas of the one in  $\mathcal{C}(T_1)$ :(0, -, -). While in the right part, the schemas in  $\mathcal{C}(T_2)$ : (0, 0, -) and (0, -, 0) are both also in  $\mathcal{C}(T_1)$ . Furthermore, one schema in  $\mathcal{C}(T_1)$ : (1, 1, -) is irrelevant to  $\mathcal{C}(T_2)$ .

Table VII. Minimal schemas of two subsuming test set

			$T_2$	$T_1$
$T_2$	$T_1$		(0, 0, 0)	(0, 0, 0)
(0, 0, 0)	(0, 0, 0)		(0, 0, 1)	(0, 0, 1)
(0, 0, 1)	(0, 0, 1)		(0, 1, 0)	(0, 1, 0)
(0, 1, 0)	(0, 1, 0)			(1, 1, 0)
	(0, 1, 1)			(1, 1, 1)
$C(T_2)$	$C(T_1)$	-	$C(T_2)$	$C(T_1)$
(0, 0, -)	(0, -, -)		(0, 0, -)	(0, 0, -)
(0, -, 0)			(0, -, 0)	(0, -, 0)
		-		(1, 1, -)

# 4. MASKING EFFECT

As discussed before,  $C(T_{F_m})$  is the MFS set of failure  $F_m$  in theory. When considering the masking effects between multiple failures, however, this formula is not correct.

*Definition* 4.1. A *masking effect* occurs when a test case t contains an MFS of a particular failure, but it does not trigger the expected failure because another failure was triggered ahead of it that prevents t from being normally checked.

Taking the masking effects into account, when identifying the MFS of a specific failure  $F_m$ , we should not ignore those test cases which did not trigger  $F_m$  but should have triggered it. We call these test cases  $T_{mask(F_m)}$ . Hence, the MFS of failure  $F_m$  should be  $\mathcal{C}(T_{F_m} \bigcup T_{mask(F_m)})$ .

Going back to the motivating example, as test case 6 and test case 18 should trigger

Going back to the motivating example, as *test case* 6 and *test case* 18 should trigger Ex 2 in case they did not trigger Ex 1, then  $F_{mask(F_2)}$  is  $\{(7,4,4,5),(11,4,4,5)\}$ . Hence, the MFS of Ex2 is  $C(T_{F_2} \bigcup T_{mask(F_2)})$ , which is (-,-,4,5) instead of the incorrect schema set  $\{(-,2,4,5),(-,5,4,5)\}$ .

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In practice with masking effects, however, it is not possible to correctly identifying the MFS, unless we fix some bugs in the SUT and re-execute the test cases to figure out  $T_{mask(F_m)}$ .

out  $T_{mask(F_m)}$ . For traditional FCI approaches, without the knowledge of  $T_{mask(F_m)}$ , two common strategies can be adopted when facing the multiple failures problem, i.e.,  $regarded\ as$  one failure and  $distinguishing\ failures$ . The former strategy treats all types of failures as one failure–failure, and others as pass, while the latter distinguishes the failures but with no special consideration of the masking effects, i.e., if a test case fails with a particular type of fault, this strategy presumes it does not contain other type of faults. We will separately discuss the two strategies under exhaustive testing condition and normal FCI testing condition.

## 4.1. Regarded as one failure strategy

This is the most common strategy. With this strategy, the minimal schemas are the set  $\mathcal{C}(\bigcup_{i=1}^L T_{F_i})$ , L is the number of all the failures in the SUT. Obviously,  $T_{F_m} \bigcup T_{mask(F_m)} \subset \bigcup_{i=1}^L T_{F_i}$ . By Proposition 3.11, some schemas obtained by this strategy may be the sub-schemas of some of the actual MFS, or be irrelevant to the actual MFS.

As an example, consider the test cases in Table VIII. Assume we need to characterize the MFS of failure 1. All the test cases that triggered failure 1 are listed in column  $T_{F_1}$ ; similarly, we list the test cases that triggered other failures in column  $T_{mask(F_1)}$  and  $T_{non\_mask}$ , respectively, in which the former masked failure 1, while the latter did not. Actually the MFS of failure 1 should be (1,1,-,-) and (-,1,1,1) as we listed them in the column 'actual MFS of failure 1'. However, when we use the regarded as one failure strategy, the minimal schemas obtained will be (-,-,0,0), (1,1,-,-), (-,-,1,1), in which (-,0,0) is irrelevant to the actual MFS of failure 1, and (-,-,1,1) is a sub-schema of the actual MFS (-,1,1,1).

$T_{F_1}$	$T_{mask(F_1)}$	$T_{non\_mask}$
$\frac{1}{(1,1,1,1)}$	$\frac{mask(F_1)}{(1, 1, 0, 0)}$	(0, 1, 0, 0)
(1, 1, 1, 0)	(0, 1, 1, 1)	(0, 0, 0, 0)
(1, 1, 0, 1)		(1, 0, 0, 0)
		(1, 0, 1, 1)
		(0, 0, 1, 1)
actual MFS of <i>failure 1</i>	regarded as one failure	distinguishing failures
$\mathcal{C}(T_{F_1} \bigcup T_{mask(F_1)})$	$C(T_{F_1} \bigcup T_{mask(F_1)} \bigcup T_{non\_mask})$	$\mathcal{C}(T_{F_1})$
(1, 1, -, -)	(-, -, 0, 0)	(1, 1, -, 1)
(-, 1, 1, 1)	(1, 1, -, -)	(1, 1, 1, -)
	(-, -, 1, 1)	

Table VIII. masking effects for exhaustive testing

# 4.2. Distinguishing failures strategy

Distinguishing the failures by the exception traces or error code can help identify the MFS related to particular failure. Yilmaz [Yilmaz et al. 2014] proposed the *multiple-class* failure characterizing method instead of the *ternary-class* approach to make the characterizing process more accurate. Besides, other approaches can also be easily extended with this strategy for testing SUT with multiple failures.

This strategy focuses on identifying the set of  $\mathcal{C}(T_{F_m})$ . As  $T_{F_m} \bigcup T_{mask(F_m)} \supset T_{F_m}$ , some schemas obtained by this strategy may be the super-schema of some actual MFS. Moreover, some MFS may be irrelevant to the schemas obtained by this strategy, which means this strategy will *ignore* these actual MFS.

For the simple example shown in Table VIII, when using this strategy, we will get the minimal schemas (1, 1, -, 1) and (1, 1, 1, -), which are both super schemas of the actual MFS (1,1,-,-). Furthermore, no schemas obtained by this strategy have any relationship with the actual MFS (-,1,1,1), which means it was ignored.

It is noted that the motivating example in section 2 actually adopted this strategy. As a result, the schemas identified for Ex 2: (-,2,4,5), (-,3,4,5) are the super-schemas of the correct MFS(-,-,4,5).

# 4.3. Masking effects for FCI approaches

The masking effects may be worse. This is because, for most approaches, it may not get all the test cases, and so the masking effects between a test case may be more harmful than discussed before.

For example, for OFOT approach, it

In this section, we focus on the SUT with single fault. Let  $T_f$  indicates all the failing test cases and  $T_p$  all the passing test cases. In fact,  $T_f \cap T_p = \emptyset$  and  $T_f \cup T_p = T^*$ . Then the MFS for the SUT is  $\mathcal{C}(T_f)$ . Theoretically, to accurately figure out the MFS in the SUT, we need to exhaustively execute each possible test case, and collect the failing test cases  $T_f$ . This is impossible in practice, especially when the testing space is very large.

Traditional FCI approaches select a subset of the exhaustive test cases to execute. Hence, we can only observe the outcomes of a part of the whole test cases. Formally, let  $T_{f-obs}$  denote the observed failing test cases, and  $T_{p-obs}$  the observed passing test cases. To obtain the MFS, the outcomes of the remaining test cases should be inferred by the FCI approaches. Correspondingly, let  $T_{f-inf}$  refer to the inferred failing test cases and  $T_{p-inf}$  the inferred passing test cases. Obviously,  $T_{f-obs} \bigcup T_{p-obs} \bigcup T_{f-inf} \bigcup T_{p-inf} = T^*$ , and they are mutually disjoint. Then the MFS identified by FCI approaches can be depicted as: MFS =  $\mathcal{C}(T_{f-obs} \bigcup T_{f-infer})$ .

We offer an FCI example using the OFOT method [Nie and Leung 2011a]. For  $T_{f-infer}$  are the standard of the offer and  $T_{f-infer}$  are the standard of the offer and  $T_{f-infer}$  and  $T_{f-infer}$  are  $T_{f-infer}$ .

We offer an FCI example using the OFOT method [Nie and Leung 2011a]. For SUT( $2^3$ ), assume the test case (1, 1, 1) failed, then the OFOT approach can be illustrated in Table IX. In this table, test case t failed, and OFOT mutated one parameter value of test case t at a time to generate new test cases:  $t_1; t_2; t_3$ . The pass of  $t_1$  indicates that this test case breaks the MFS in the original test case t. So, (1,-,-) should be one failure-causing factor, and as the other test cases ( $t_2, t_3$ ) all failed, this means no other failure-inducing factors were broken (note that this conclusion is based on the assumption that t only contains one MFS); therefore, the MFS in t is (1,-,-).

In this example, only 4 test cases are observed

Table IX. OFOT with our strategy

ori	gina	l te	st case	Outcome			
$\overline{t}$	1	1	1	Fail			
	observed						
$t_1$	0	1	1	Pass			
$t_2$	1	0	1	Fail			
$t_3$	1	1	0	Fail			
	predicted						
$t_4$	0	0	1	Pass			
$t_5$	0	1	0	Pass			
$t_6$	1	0	0	Fail			
$t_7$	0	0	0	Pass			

To solve it is meaningful.

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#### 5. TEST CASE REPLACING STRATEGY

The main reason that the FCI approach fails to work properly is that it cannot determine  $B_2$  and  $B_3$ , i.e., if the test case triggers other failures which are different from the currently analysed one, it cannot figure out whether this test case will trigger the current expected failure because of the masking effects. So to limit the impact of this effect on the FCI approach, it is important to reduce the number of test cases that trigger other different failures, as it can reduce the probability that expected failure may be masked by other failures.

In the exhaustive testing, as all the test cases will be used to identify the MFS, there is no room left to improve the performance unless we fix other failures and re-execute all the test cases. However, if only a subset of all test cases is used to identify the MFS (which is how the traditional FCI approach works), it is important to make the right selection to limit the size of  $\mathcal{T}(mask_{F_m})$  to be as small as possible.

#### 5.1. Replacing test cases that trigger unexpected failures

The basic idea is to pick the test cases that trigger other failures and generate new test cases to replace them. The regenerated test cases should either pass in the execution or trigger  $F_m$ . The replacement must satisfy the condition that the newly generated ones will not negatively influence the original identifying process.

Normally, when we replace the test case that triggers an unexpected failure with a new test case, we should keep some part of the original test case. We call this part the *fixed part*, and mutate the other part with different values from the original one. For example, if a test case (1,1,1,1) triggered an unexpected failure, and the fixed part is (-,-,1,1). Then, we can replace it with a test case (0,0,1,1) which may either pass or trigger the expected failure.

The fixed part can vary for different FCI approaches, e.g, for the OFOT [Nie and Leung 2011a] algorithm, the parameter values are the fixed part except for the one that needs to be validated, while for the FIC\_BS [Zhang and Zhang 2011] approach, the fixed parts are dynamically changed, depending on the outcome of the execution of last generated test case.

This replacement may need to be executed multiple times for one fixed part as it may not always possible to find a test case that coincidentally satisfied our requirement. One replacement method is randomly choosing test cases until the satisfied test case is found. While this method may be simple and straightforward, however, it also may require trying many times. So to handle this problem and reduce the cost, we propose a replacement approach by computing the *strength* of the test case with the other failures, and then we select the test case from a group of candidate test cases that has the least *strength* related to the other failures.

To explain the strength notion, we first introduce the strength that a parameter value is related to a particular failure. We use all(o) to represent the number of executed test cases that contain this parameter value, and m(o) to indicate the number of test cases that trigger the failure  $F_m$  and contain this parameter value. Then, the strength that a parameter value is related to a particular failure, i.e.,  $S(o,F_m)$ , is  $\frac{m(o)}{all(o)+1}$ . This heuristic formula is based on the idea that if a parameter value frequently appears in the test cases that trigger a particular failure, then it is more likely to be the inducing factor that triggers this failure. We add 1 in the denominator for two reasons: (1) avoid division by zero when the parameter value has never appeared before, (2) reduce the bias when a parameter value rarely appears in the test set but coincidentally appears in a failing test case with a particular failure.

With the *strength* associated with a parameter value, we then define the *strength* of a test case f is related to a particular failure  $F_m$  as:

$$S(f, F_m) = \frac{1}{k} \sum_{o \in f} S(o, F_m)$$
 (EQ1)

where k is the number of parameters in f, and o is the specific parameter value in f. The *strength* that a test case is related to a failure is defined as the average *strength* of the relevance between each parameter value in the test case and this failure. For a selected test case, we want its ability to trigger another failure to be as small as possible, such that the masking effects can be alleviated. In practice, the relevance *strength* varies between test case with different failures. As a result, we cannot always find a test case that, for any failure, the *strength* that this test case is related to that failure is the least. With this in mind, we have to settle for a test case, such that the maximal possible failure (except for the one that is currently analysed) it can trigger should be the least likely to be triggered when compared with that of other test cases. In other word, we need to find a test case, so that the maximal *strength* that it is related to another failure is minimal. Formally, we should choose a test case f, s.t.,

$$\min_{f \in R} \max_{m \le L\&m \ne n} S(f, F_m)$$
 (EQ2)

where L is the number of failures, and n is the current analysed failure. R is the set of all possible test cases that contain the fixed part except those that have been tested. The test case is from the set R because the FCI approach needs to keep the fixed part when generating additional test cases and the test case should not have been executed. Obviously  $|R| = \prod_{i \not\in fixed} (v_i) - |\{t \mid t \ contains \ the \ fixed \ part \ \& \ t \ is \ executed\}|.$ 

We can further resolve this problem. Consider the test case f satisfies EQ2. Without loss of generality, we assume that the failure  $F_k, k \neq n$  is the failure with which the test case f has the maximal related strength compared to the other failures. Then, a natural property for f is that any other test case f' which satisfies that failure  $F_k$  is the maximal related failure for this test case and must have  $S(f, F_k) <= S(f', F_k)$ . Formally, to obtain such a test case is to solve the following formula:

$$\begin{array}{ll} \min & S(f,F_k) \\ \text{s.t.} & f \in R \\ & S(f,F_k) > S(f,F_i), \quad 1 \leq i \leq L \ \& \ i \neq k,n \end{array}$$

To solve EQ2, we just need to find a particular failure  $F_k$ , and the corresponding test case  $f_k$  that satisfies EQ3, such that the related *strength* between  $f_k$  and  $F_k$  is smaller than the related *strength* between any other failures and their corresponding test cases that satisfy EQ3. Formally, we need to find:

$$\begin{array}{ll} \min & S(f,F_k) \\ \text{s.t.} & 1 \leq k \leq L \ \& \ k \neq n \\ & f,F_k \ satisfies \ EQ3 \end{array} \tag{EQ4}$$

According to EQ4, to determine such a test case lies in solving EQ3 because if it is solved we just need to rank the one that has the minimal value from the solutions to EQ3. As to EQ3, it can be formulated as an 0-1 integer linear programming (ILP) problem. Assume the SUT has K parameters in which the ith parameter has  $V_i$  values. And the SUT has L failures. We then define the variable  $x_{ij}$  as:

$$x_{ij} = \begin{cases} 1 & the \ ith \ parameter \ of \ the \ test \ case \ take \ the \ jth \ value \ for \ that \ parameter \\ 0 & otherwise \end{cases}$$

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We then take  $o_{m_{ij}}$  to be the related *strength* between the jth value of the ith parameter of the SUT and the failure  $F_m$ . And we use a set R of parameter values to define the fixed part in the test case we should not change, i.e., R = $\{(i,j)|i \text{ is the fixed parameter in the test case}, j \text{ is the corresponding value}\}$ . As we can generate redundant test cases, so we keep a test set  $T_{executed}$  to guide the generation of different test cases. Then EQ3 can be transformed into following ILP formula:

min 
$$\frac{1}{|K|} \sum_{i=0}^{K} \sum_{j=0}^{V_i} o_{m_{ij}} \times x_{ij}$$
 (EQ5)

s.t. 
$$0 \le x_{ij} \le 1$$
  $i = 0..K - 1, j = 0, ..V_i - 1$  (1)

$$x_{ij} \in \mathbb{Z}$$
  $i = 0..K - 1, j = 0, ..V_i - 1$  (2)

$$\sum_{i=0}^{V_j} x_{ij} = 1 i = 0...K - 1 (3)$$

$$x_{ij} = 1 (i, j) \in R (4)$$

$$\sum_{(i,j)\in t} x_{ij} < K \qquad \qquad t \in T_{existed} \tag{6}$$

In EQ5, constraints (1) and (2) indicate that the variable  $x_{ij}$  is a 0-1 integer. Constraint (3) indicates that a parameter in one test case can only take on one value. Constraint (4) indicates that the test case should not change values of the fixed part. Constraint (5) indicates that the related strength between the test case and failure  $F_m$ is higher than that of the other failures. Constraint (6) indicates that the test cases generated should not be the same as the test cases in  $T_{existed}$ .

As we have formulated the problem into a 0-1 integer programming problem, we just need to utilize an ILP solver to solve this formula. In this paper, we use the solver introduced in [Berkelaar et al. 2004], which is a mixed Integer Linear Programming (MILP) solver that can handle satisfaction and optimization problems.

The complete process of replacing a test case with a new one while keeping some fixed part is depicted in Algorithm 1.

The inputs to this algorithm consist of the failure  $F_m$ , the fixed part of which we want to keep from the original test case  $s_{fixed}$ , the set of values that each parameter can take Param and the set of matrix  $o_1, o_2, ... o_m, ..., o_L$ , where  $o_m$  (  $1 \leq m \leq L$  ) is recorded the related strength between each specific parameter with each value and the failure  $F_m$ , i.e.,  $o_m = \{o_{m_{ij}} | 0 \le i \le K - 1, 0 \le j \le V_i\}$ . The output of this algorithm is a test case  $t_{new}$  which either triggers the expected  $F_m$  or passes.

The outer loop of this algorithm (lines 1 - 19) contains two parts:

The first part (lines 2 - 9) generates a new test case which is supposed to be least likely to trigger failures different from  $F_m$ . The basic idea for this part is to search each failure different from  $F_m$  (line 3) and find the best test case that has the least related strength with other failures. In detail, for each failure we set up an ILP solver (line 4) and use it to get an optimal test case for that failure according to EQ5 (line 5). We compare the optimal value for each failure, and choose the one with less strength related to other failures (lines 6 - 9).

#### **ALGORITHM 1:** Replacing test cases triggering unexpected failures

```
Input: failure F_m, fixed part s_{fixed}, set of values that each option can take Param, the related
            strength matrix o_1...o_L
   Output: t_{new} the regenerate test case, The frequency number
   while not MeetEndCriteria() do
       optimal \leftarrow MAX \; ; \; t_{new} \leftarrow null \; ;
       forall the F_k \in F_1, ... F_m, F_{m+1} ... F_L do
3
            solver \leftarrow setup(s_{fixed}, Param, F_m, o_1...o_L);
            (optimal', t'_{new}) \leftarrow solver.getOptimalTest();
5
            if optimal' < optimal then
 6
7
               t_{new} \leftarrow t'_{new};
 8
       end
10
       result \leftarrow execute(t_{new});
       updatetRelatedStrengthMatrix(t_{new});
11
       if result == PASS or result == F_m then
12
            return t_{new};
13
14
15
           continue;
       end
16
17 end
18 return null
```

The second part is to check whether the newly generated test case is as expected (lines 10 - 16). We first execute the SUT under the newly generated test case (line 10) and update the related strength matrix  $(o_1...o_L)$  for each parameter value that is involved in this newly generated test case (line 11). We then check the execution result. If the test case passes or triggers the same failure  $-F_m$ , a satisfied test case is obtained (line 12) and returned (line 13). Otherwise, we will repeat the process, i.e., generate a new test case and check again (lines 14 - 15).

Note that this algorithm has another exit, besides finding an expected test case (line 12), which is when the function MeetEndCriteria() returns true (line 1). We did not explicitly show function MeetEndCriteria(), because this is dependent on the computing resource and the desired accuracy. In detail, if we want to get a high quality result and have enough computing resource, it is desirable to try many times to get the expected test case; otherwise, a relatively small number of attempts is recommended.

In this paper, we just set 3 as the greatest number of iterations for this function. When it ends with *MeetEndCriteria()* returning true, it will return null (line 18), which means we cannot find an expected test case.

# 5.2. A case study using the replacement strategy

Suppose we have to test a system with eight parameters, each of which has three options. And when we execute the test case  $T_0$  – (0, 0, 0, 0, 0, 0, 0, 0, 0), a failure—e1 is triggered. Furthermore, there are two more potential failures, e2 and e3, that may be triggered during the testing; and they will mask the desired failure e1. Next, we will use FIC\_BS [Zhang and Zhang 2011] with replacement strategy to identify the MFS of e1. The process is shown in Figure 2. In this figure, there are two main columns. The left main column indicates the executed test cases during testing as well as the executed results, and each executed test case corresponds to a specific label,  $T_1 - T_8$ , at the left. The right main column lists the related strength matrix when a test case triggers e2 or e3. In detail, the matrix records the related strength between each parameter (Columns e1) for each value it can take (Column v) with the unexpected failure

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(Column F). The executed test case, shown in bold, indicates the one that triggers the other failure and should be replaced in the next iteration.

The completed MFS identifying process listed in Figure 2 works as follows: firstly the original FCI approach determines which fixed part needed to be test in each iteration. Then the extra test case will be generated to fill in the remaining part. After executing the extra test case, if the result of the execution is normal, i.e., did not trigger unexpected failure  $(e_2, e_3)$ , then the original FCI process will continue until the MFS is identified. Otherwise, the replacement strategy starts when an unexpected failure is triggered. The replacement process will mutate the parameter values that is not in the fixed part according to Algorithm 1. After the replacement process, the control for the MFS identifying process will be passed back to the original FCI approach. Next we will specifically explain how the replacement works with an example in this figure.

From Figure 2, for the test case that triggered e2-(2,1,1,1,0,0,0,0) (in this case, the fixed part of the test case is (-,-,-,0,0,0,0), in which the last four parameter values are the same as the original test case  $T_0$ ), we generate the related matrix at left. Each element in this matrix is computed as  $\frac{m(o)}{all(o)+1}$ ; for example, for the P7 parameter with value 0, we can find two test cases that contain this element, i.e.,  $T_0$  and  $T_1$ , so all(o) is 2. And only one test case triggers the failure e2, which means m(o)=1. So the final related strength between this parameter value with e2 is  $\frac{1}{2+1}=0.33$ . All the related strength with e3 is labeled with a short slash as there is no test case triggering this failure in this iteration. After this matrix has been determined, we can obtain the optimal test case with the ILP solver, which is  $T_1'-(1,2,2,2,0,0,0,0)$ , with its related strength 0.167, which is smaller than that all.

This replacement process is started each time a new test case that triggered another failure until we finally get the MFS. Sometimes we could not find a satisfied replacing test case in just one trial like  $T_1$  to  $T_1'$ . When this happened, we needed to repeat searching the proper test case. For example, for  $T_4$  which triggered e3, we tried three times— $T_4', T_4'', T_4'''$  to finally get a satisfied  $T_4'''$  which passes the testing. Note that the related strength matrix continues to change as the test case is generated and executed so that we can adaptively find an optimal one.

#### 6. EMPIRICAL STUDIES

To investigate the impact of masking effects on FCI approaches in real software testing scenarios and to evaluate the performance of our approach in handling this effect, we conducted several empirical studies. Each of the studies focuses on addressing one particular issue, as follows:

- **Q1**: Do masking effects exist in real software that contains multiple failures?
- **Q2**: How well does our approach perform compared to traditional approaches?
- **Q3**: Is the ILP-based test case searching technique efficient compared to the random selection?
- **Q4**: Compared to another masking effects handling approach FDA-CIT [Yilmaz et al. 2014], does our approach have any advantages?

# 6.1. The existence and characteristics of masking effects

In the first study, we surveyed two kinds of open-source software systems to gain an insight into the existence of multiple failures and their effects. The software under study were HSQLDB and JFlex. The first is a database management software written in pure Java and the second is a lexical analyser generator. The reason that we chose these two systems is because they both contain different versions and are all highly configurable so that the options and their interactions can affect their behaviour. Additionally, they all have a developer community so that we can easily obtain the real

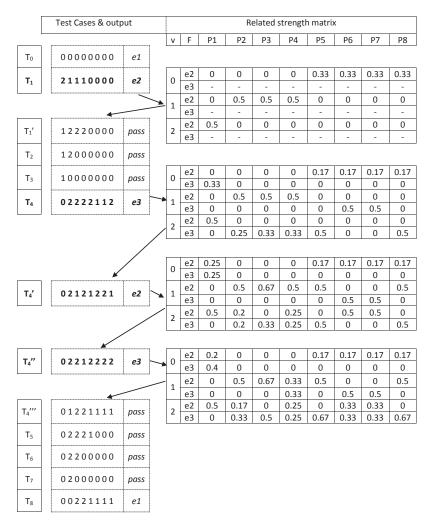


Fig. 2. A case study using our approach

bugs reported in the bug tracker forum. Table X lists the program, the versions surveyed, number of lines of uncommented code, number of classes in the project, and the bug's id  $^3$ for each of the software.

6.1.1. Study setup. We first looked through the bug tracker forum and focused on the bugs which are caused by the options interactions. For each such bug, we derived its MFS by analysing the bug description report and the associated test file which can reproduce the bug. For example, through analysing the source code of the test file of bug#981 for HSQLDB, we found the failure-inducing interaction for this bug is (preparestatement, placeHolder, Long string). These three parameter values together form the condition that triggers the bug. The analysed result was later regarded as the "prior MFS".

<sup>&</sup>lt;sup>3</sup>http://sourceforge.net/p/hsqldb/bugs http://sourceforge.net/p/jflex/bugs

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Table X.	Software	under	survey
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software	versions	LOC	classes	bug pairs
HSQLDB	2.0rc8	139425	495	#981 & #1005
	2.2.5	156066	508	#1173 & #1179
	2.2.9	162784	525	#1286 & #1280
JFlex	1.4.1	10040	58	#87 & #80
	1.4.2	10745	61	#98 & #93

We further built the testing scenario for each version of the software listed in Table X. The testing scenario is constructed so that we can reproduce different failures by controlling the inputs to the test file. For each version, the source code of the testing file as well as other detailed information is available at https://code.google.com/p/merging-bug-file.

Next, we built the input model which consists of the options related to the failure-inducing interactions and additional options that are commonly used. The detailed model information is shown in Tables XI and XII for HSQLDB and JFLex, respectively. Each table is organised into three groups: (1) common options, which lists the options as well as their values under which every version of this software can be tested; (2) specific options, under which only the specific version can be tested; and (3) configure space, which depicts the input model for each version of the software, presented in the abbreviated form  $\#values^{\#number\ of\ parameters} \times ...$ , e.g.,  $2^9 \times 3^2 \times 4^1$  indicates the software has 9 parameters that can take 2 values, 2 parameters 3 values, and only one parameter 4 values.

Table XI. Input model of HSQLDB

comi	non options	values
Server Type		server, webserver, inprocess
ex	isted form	mem, file
rest	ıltSetTypes	forwad, insensitive, sensitive
resultS	etConcurrencys	read_only, updatable
resultS	SetHoldabilitys	hold, close
	tementType	statement, prepared
sql.enf	orce_strict_size	true, false
sql.ei	nforce_names	true, false
sql.	enforce_refs	true, false
versions	specific options	values
2.0rc8	more	true, false
	placeHolder	true, false
	cursorAction	next,previous,first,last
2.2.5	multiple	one, multi, defailure
	placeHolder	true, false
2.2.9	duplicate	dup, single, defailure
	defailure_commit	true, false
versions	Config space	
2.0rc8	$2^9 \times 3^2 \times 4^1$	
2.2.5	$2^{8} \times 3^{3}$	
2.2.9	$2^{8} \times 3^{3}$	

We then generated the exhaustive test set consisting of all possible interactions of these options. For each of them, we executed the prepared testing file. We recorded the output of each test case to observe whether there were test cases containing prior MFS that did not produce the corresponding bug. Later we refer to those test cases that contain the MFS but did not trigger the expected failure as the *masked* test cases.

Table XII. Input model of JFlex

com	mon options	values							
g	generation	switch, table, pack							
	charset	default, 7bit, 8bit, 16bit							
	public	true, false							
8	apiprivate	true, false							
	cup	true, false							
	caseless	true, false							
	char	true, false							
	line	true, false							
	column	true, false							
	notunix	true, false							
	yyeof	true, false							
versions	specific options	values							
1.4.1	hasReturn	has, non, default							
	normal	true, false							
1.4.2	lookAhead	one, multi, default							
	type	true, false							
	standalone	true, false							
versions	Config space								
1.4.1	$2^{10} \times 3^2 \times 4^1$								
1.4.2	$2^{11} \times 3^2 \times 4^1$								

Table XIII. Number of failures and their masking effects

software	versions	all tests	failure	masking
HSQLDB	2cr8	18432	4608	768 (16.7%)
-	2.2.5	6912	3456	576 (16.7%)
-	2.2.9	6912	3456	1728 (50%)
JFlex	1.4.1	36864	24576	6144 (25%)
-	1.4.2	73728	36864	6144 (16.7%)

6.1.2. Results and discussion. Table XIII lists the results of our survey. Column "all tests" gives the total number of test cases executed. Column "failure" indicates the number of test cases that failed during testing, and column "masking" indicates the number of masked test cases. The percentage in the parentheses indicates the proportion of masked test cases and the failing test cases.

We observed that for each version of the software under analysis listed in Table XIII, test cases with masking effects do exist, i.e., test cases containing MFS did not trigger the corresponding bug. In fact, there are about 768 out of 4608 test cases (16.7%) in hsqldb with 2rc8 version. This rate is about 16.7%, 50%, 25%, and 16.7%, respectively, for the remaining software versions.

So the answer to  $\mathbf{Q1}$  is that in practice, when SUT have multiple failures, masking effects do exist widely in the test cases.

It is notable that in Yilmaz's [Yilmaz et al. 2014] paper, a similar study about the existence of the masking effects has been conducted. The main difference between that work and ours is that Yilmaz's work quantify impact of the masking effects as the number of  $\tau$ -degree schemas that only appear in the test cases that triggered other failures. Here, the  $\tau$ -degree schemas can be either MFS or not. Our work, however, quantify the masking effects as the number of test cases that are masked by unexpected failures. These test cases should contain some MFS, i.e., they should have triggered the expected failure if they did not trigger any other failure. The reason that we quantify the masking effects in such way is because our work seeks to handle the masking effects in the MFS identifying process. As the test cases which contain the MFS but do not produce the corresponding failure will significantly affect the MFS identifying

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results, their number can better reflect the impact of the masking effects on the FCI approach.

#### 6.2. Comparing our approach with traditional algorithms

The second study aims to compare the performance of our approach with traditional approaches in identifying MFS under the impact of masking effects. To conduct this study, we need to apply our approach and traditional algorithms to identify MFS in a variety of software and evaluate their results. The five versions of software in Table X used as test objects are far from the requirement for a general evaluation. However, to construct many real testing objects is time-consuming as we must carefully study the detail of that software as well as the bug tracker report. To compromise, we synthesized 10 more testing objects. These synthesized objects are ten small programs which can directly return outputs when executed with given inputs. To make the synthetic objects as similar as possible to the real software, we firstly analysed the characterizations, such as the number of parameters, the number of failures, and the possible masking effects, of the real software. We observed that the number of parameters of the SUT ranged from 8 to 30, the number of different failures in the SUT ranged from 2 to 4, and the number of MFS of a failure ranged from 1 to 2, in which the degree of the MFS ranged from 1 to 6. Then for each characterization, we randomly selected one value in the corresponding range and assigned it to the input model by adjusting the relationships between the inputs and outputs of these programs.

Table XIV lists the testing model for both the real and synthesizing testing objects. In this table, column 'Object' indicates the SUT under test. For the real SUT listed in Table X, we label the five software as H2cr8, H2.2.5, H2.2.9, J1.4.1, J1.4.2, respectively. While for the synthesized ones, we label them in the form of 'syn+id'. Column 'Model' presents the input space for each testing object. Column 'Failures' shows the different failures in the software and their masking relationships. In this column, '>' means the left failure will mask the right failure, i.e., if the left failure is triggered, then the right failure will not be triggered. Furthermore, '>' is transitive so that the left failure can mask all the failures in the right. For example, for the H2cr8 object, we can find three failures:  $e_1$ ,  $e_2$ , and  $e_3$ . By using the formula  $e_1 > e_2 > e_3$ , we indicate that the failure  $e_2$  will mask  $e_3$  and  $e_1$  will mask both  $e_2$  and  $e_3$ . Here for the simplicity of the experiment, we did not build more complex testing scenarios such as the masking effects can happened in the form  $e_1 > e_2$ ,  $e_2 > e_3$ ,  $e_3 > e_1$  or even  $e_1 > e_2$ ,  $e_2 > e_1$ . The last column shows the MFS of each failure. The MFS is presented in an abbreviated form  $\{\#index_{\#value}\}_{failure}$ , e.g., for the object H2cr8,  $(5_1, 6_0, 7_0)_{e_1}$  actually means (-, -, -, -, -, 1, 0, 0, -, -, -, -, -) is the MFS of the failure  $e_1$ .

6.2.1. Study setup. After preparing the objects under testing, we then applied our approach (FIC BS with replacement strategy) to identify the MFS. Specifically, for each SUT we selected each test case that failed during testing and fed it into our FCI approach as the input. Then, after the identifying process was completed, we recorded the identified MFS and the extra test cases needed. For the traditional FIC BS approach, we designed the same experiment. But as the objects being tested have multiple failures for which the traditional FIC BS can not be applied directly, we adopted two traditional strategies on the FIC BS algorithm, i.e., regarded as one failure and distinguishing failures as described in Section 3.2. The purpose of recording the generated additional test cases is to quantify the additive cost of our approach.

We next compared the identified MFS of each approach with the prior MFS to quantify the degree that each suffers from masking effects. There are five metrics used in this study, listed as follows:

(1) Accurate number: the number of identified MFS which are actual prior MFS.

Object	Model	Failures	MFS of each failure
H2cr8	$2^9 \times 3^2 \times 4^1$	$e_1 > e_2 > e_3$	$(5_1, 6_0, 7_0)_{e_1}, (5_1, 8_2, 9_2)_{e_2}, (5_1, 8_2, 9_1)_{e_2}, (5_1, 8_3, 9_2)_{e_3}, (5_1, 8_3, 9_1)_{e_3}$
H2.2.5	$2^{8} \times 3^{3}$	$e_1 > e_2$	$(6_1, 7_0)_{e_1}, (5_2)_{e_2}$
H2.2.9	$2^{8} \times 3^{3}$	$e_1 > e_2 > e_3$	$(6_0)_{e_1}, (0_1, 5_1, 7_0)_{e_2}, (0_0, 5_1, 7_0)_{e_2}, (5_1, 7_0)_{e_3}$
J1.4.1	$2^{10}\times 3^2\times 4^1$	$e_1 > e_2$	$(0_0)_{e_1}, (1_0)_{e_2}$
J1.4.2	$2^{11}\times 3^2\times 4^1$	$e_1 > e_2$	$(1_0, 2_1)_{e_1}, (0_1)_{e_2}$
syn1	$2^5 \times 3^3 \times 4^1$	$e_1 > e_2$	$(2_1,3_0)_{e_1},(1_1,2_1)_{e_2},(1_0,3_0)_{e_2}$
syn2	$2^6 \times 3^2 \times 4^1$	$e_1 > e_2 > e_3$	$(4_1, 6_0, 7_1, 8_0)e_1, (1_1, 3_1, 5_1)e_2, (2_0, 3_1, 6_0)e_3$
syn3	$2^{5} \times 3^{3}$	$e_1 > e_2 > e_3$	$(2_1,3_0)_{e_1},(1_0)_{e_2},(4_1)_{e_2},(6_0,7_0)_{e_3}$
syn4	$2^7 \times 3^2 \times 4^1$	$e_1 > e_2 > e_3$	$(0_1, 2_1, 5_0, 6_1)_{e_1}, (2_1, 4_0)_{e_2}, (6_1, 7_0)_{e_2}, (3_0, 4_0, 5_0)_{e_3}$
syn5	$2^4 \times 3^3 \times 4^2$	$e_1 > e_2$	$(0_0, 1_1, 3_0, 6_1, 8_0)_{e_1}, (2_0, 3_0, 4_1)_{e_2}$
syn6	$2^{9} \times 3^{2}$	$e_1 > e_2 > e_3 > e_4$	$(2_0,7_1,8_1)_{e_1},(3_1,5_1)_{e_2},(4_0)_{e_2},(3_1,6_0,7_1)_{e_3},(3_1,7_1,8_0)_{e_4}$
	$2^{10}\times 3^1\times 4^1$		$(3_1, 4_0, 5_0)_{e_1}, (2_0, 4_0, 7_1, 9_0)_{e_2}, (6_1, 10_0, 11_1)_{e_3}$
syn8	$2^{11} \times 3^1 \times 4^1$	$e_1 > e_2$	$(1_0, 3_1, 4_0, 7_1, 9_0, 12_1)_{e_1}, (0_0, 2_1, 3_1, 7_1, 10_0, 11_1)_{e_2}$
syn9		$e_1 > e_2$	$(3_1, 5_0)_{e_1}, (5_0, 6_1)_{e_2}$
syn10	$2^7 \times 3^3 \times 4^1$	$e_1 > e_2$	$(0_1, 3_0, 4_1, 7_0)_{e_1}, (2_0, 3_0, 5_1)_{e_2}, (2_0, 3_0, 5_0)_{e_2}$

Table XIV. The testing models used in the case study

- (2) *Super number*: the number of identified MFS that are the super schemas of some prior MFS.
- (3) Sub number: the number of identified MFS that are the sub schemas of some prior MFS.
- (4) *Ignored number*: the number of schemas that are in the prior MFS, but irrelevant to the identified MFS.
- (5) *Irrelevant number*: the number of schemas in the identified MFS that are irrelevant to the prior MFS.

Among these five metrics, the accurate number directly indicates how effectively the FCI approaches performed, since to identify as many actual MFS as possible is the target for every FCI approach. Metrics ignored number and irrelevant number indicate the extent of deviation for the FCI approaches, specifically, the former indicates how much information about the MFS will miss, while the latter indicates how serious the distraction would be due to the useless schemas identified by the FCI approach. Super number and sub number are the metrics in between, i.e., to identify some schemas that is super or sub schemas of the actual MFS is better than identifying irrelevant ones or ignoring some MFS, but it is worse than identifying the schema that is identical to some actual MFS. This is intuitive, as given the super / sub schemas, we just need to remove / add some elements of the original schemas to get the actual MFS. While for the irrelevant or ignore ones, however, more efforts will be needed (e.g., both adding and removing operations will be needed to revise the irrelevant schemas to the actual MFS).

Besides these specific metrics, we also give a composite metric to measure the overall performance of each approach. The composite metric *aggregate* is defined as follows:

$$Aggregate = \frac{accurate + related(super) + related(sub)}{accurate + super + sub + irrelevant + ignored}$$

In this formula, *accurate*, *super*, *sub*, *irrelevant*, and *ignored* represent the value of each specific metric. To refine the evaluation of different *super* / *sub* schemas, we design a *related* function which gives the similarity between the schemas (either super or sub) and the real MFS, so that we can quantify the specific effort for changing a

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super / sub schema to the real MFS. The similarity between two schemas  $S_A$  and  $S_B$  is computed as:

$$Similarity(S_A, S_B) = \frac{number\ of\ same\ elements\ in\ S_A\ and\ S_B}{\max(Degree(S_A), Degree(S_B))}$$

For example, the similarity of (-1 2 - 3) and (-2 2 - 3) is  $\frac{2}{3}$ . This is because  $S_A$  and  $S_B$  have the same third and last elements, and both of them are 3-degree.

So the *related* function is the summation of similarity of all the super or sub schemas with their corresponding MFS.

6.2.2. Results and discussion. Figure 3 depicts the results of the second case study. There are seven sub-figures in this figure, i.e., Figure 3(a) to Figure 3(g). They indicate the results of the number of accurate MFS each approach identified, the number of identified schemas which are the sub-schema / super-schema of some prior MFS, the number of ignored prior MFS, the number of identified schemas which are irrelevant to all the prior MFS, the aggregate value, and the extra test cases each algorithm needed, respectively. For each sub-figure, there are four polygonal lines, each of which shows the results for one of the four strategies: regarded as one failure, distinguishing failures, replacement strategy based on ILP searching, replacement strategy based on random searching (The last one will be discussed in the next case study). Specifically, each point in the polygonal line indicates the specific result of a particular strategy for the corresponding testing object. For example in Figure 3(a), the point marked with '\rightarrow' at (1,2) indicates that the approach using regarded as one failure strategy identified 2 accurate MFS in the testing object-HSQLDB 2cr8. The raw data for this experiment can be found in Table XV of the Appendix. Note that all the data except for the metric ignored number are based on all failing test cases for each testing object, i.e., we got the data by comparing the union of the schemas identified in each the failing test cases to the prior actual MFS. As for metric ignored number, however, we found that if we merged all the schemas identified in each failing test case, there is no MFS ignored. We therefore use the average score of *ignored number* for each failing test case, which can be seen in the parentheses in Column ignore of Table XV. Next we will discuss the results for each metric.

**Accurate number:** Figure 3(a) shows the number of accurate schemas that each approach achieved. It appears that there is no outstanding strategy, i.e., there does not exist a strategy that can always perform better or worse than others. For example, for the testing object 1, *ILP* performed the best in obtaining the accurate MFS, while for the testing object 2, distinguishing failures identified the most accurate MFS and for testing object 3, regarded as one failure did the best. However, upon closer inspection, we can find that strategy distinguishing failures performed a little better than strategy regarded as one failure. This can be reflected in that there are four testing objects (1, 3, 11, and 15) on which strategy distinguishing failures performed better, while for strategy regarded as one failure there are only three superior testing objects (6, 8, and 14). This subtle difference can be explained by our formal analysis in Section 4. Specifically, for the strategy regarded as one failure, only scenario 1 in Table ?? can result in the FCI approaches identifying the schemas that are identical to some actual MFS, while for distinguishing failures, there are two scenarios (scenarios 1 and 7 in Table ??). As a result, distinguishing failures strategy has a slighter larger chance than regard as one failure to identify the schemas that are identical to the actual MFS.

We can further find that strategies *replacement strategy based on ILP searching* (short for *ILP* later) and *distinguishing failures* have similar results. This can be easily understood, as strategy *ILP* is actually a refinement version of the strategy *dis-*

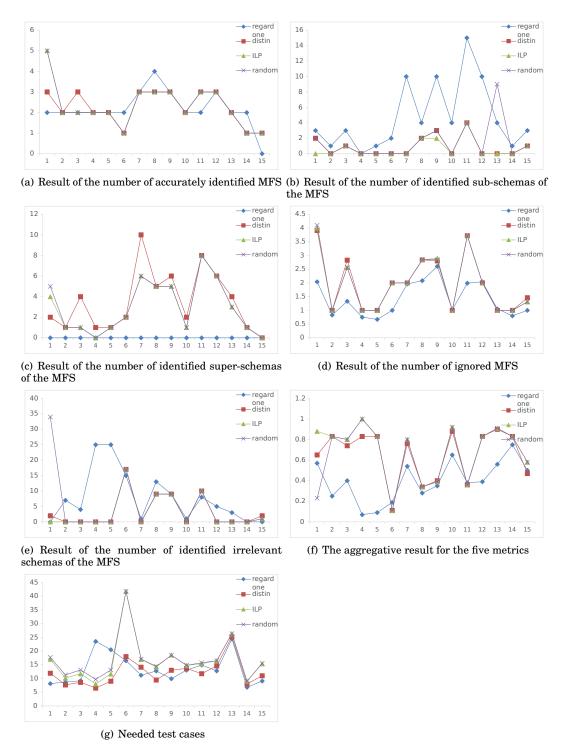


Fig. 3. Result of the evaluation of each approach

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tinguishing failures, which also make the failures distinguished with each other. The main difference between *ILP* and *distinguishing failures* is that the former has to replace the test cases that triggered any failure other than the currently analysed one while the latter will not change the generated test cases. As a result, the comparison of other metrics (sub, super, ignore, irrelevant numbers) also showed the similarity between strategy *ILP* and *distinguishing failures*.

**Sub number & super number:** Figure 3(b) and 3(c) depicts the results for *sub number* and *super number*, respectively. These two figures firstly showed a clear trend for strategies *regarded as one failure* and *distinguishing failures*, i.e., the former identified more sub schemas of actual MFS than the latter, while the latter identified more super schemas of actual MFS than the former. This is consistent with our formal analysis. Specifically, there are 6 scenarios (scenarios 3, 5, 6, 7, 8, 9 listed in Table ??) for strategy *regarded as one fault* that can lead to the identified schemas being sub schemas of actual MFS, while *distinguishing failures* strategy has 2 such scenarios (scenarios 3, 7 in Table ??). But for the scenarios that can result in the schemas being super schemas of actual MFS, strategy *regarded as one failure* only has one (scenario 2 in Table ??), while *distinguishing failure* has 5 such scenarios (scenarios 2, 5, 6, 7, 8 in Table ??).

Although offering similar result as *distinguishing failures* strategy, our strategy *ILP* tend to identify fewer sub schemas and super schemas of actual MFS than strategy *distinguishing failures* (testing objects 1, 9 in Figure 3(b) and testing objects 3, 4,7,9,10 13 in Figure 3(c)). We believe this is an improvement, as too many sub schemas and super schemas will make it harder to identify the actual MFS. One issue is the redundancy problem, as many sub or super schemas in fact point to the same actual MFS.

**Ignore number & irrelevant number:** The results of the two negative performance metrics are given in Figure 3(d) and 3(e), respectively.

There are two main observations: first, for strategies regarded as one failure and distinguishing failures, we can find that the former identified more irrelevant schemas of the actual MFS, while the latter ignored more actual MFS. This observation is as expected, because in our formal analysis the strategy regarded as one failure has more scenarios than distinguishing failures that can lead to the schemas being irrelevant to the actual MFS, in detail, the former has 4 such scenarios (scenarios 4, 6, 8, 9 in Table ??) while the latter has three (scenarios 4, 7,8 in Table ??). And for strategy distinguishing failures, five scenarios (scenarios 3,6,8,9,10) in Table ?? increases the chance to ignore the actual MFS than the strategy regarded as one failure (scenarios 5, 7 in Table ??).

The second observation is that *ILP* did a good job at reducing the scores for these two negative metrics. Specifically, for *ignored number*, our approach performed better than strategy *distinguishing failures* at testing object 3 and 15 in Figure 3(d), but is not as good as strategy *regarded as one failure*. In fact, strategy *regarded as one failure* has a significant advantage at reducing the number of ignored MFS as it tends to associate the failures with all the failing test cases. However, when we consider the *irrelevant number*, we can find that our approach is the best among all three strategies (better than *distinguishing failures* at testing object 1 in Figure 3(e), and better than strategy *regarded as one failure* for most testing objects). We believe this improvement is caused by our test cases replacing strategy, as it can increase the test cases that are useful for identifying the MFS and decrease those useless test cases.

**Aggregative for the five metrics:** The composite results are given in Figure 3(f). This metric gives an overall evaluation of the quality of the identified schemas. From this figure, we can find that *ILP* performed the best, next the *distinguishing failures*, the last is the *regarded as one failure* (See the testing object 1, 3 and 4 in Figure 3(f)).

It is as expected that *ILP* performed better than *distinguishing failures* as it is actually the refinement version of latter. It is a bit of surprise to find, however, that strategy *distinguishing failures* performed better than *regarded as one failure* at almost all the testing objects. This result cannot be derived from the formal analysis. A possible explanation is that in these testing objects constructed, the possibility of triggering a masking effect is relatively small. Consequently if we take the strategy *regarded as one failure*, we are more likely to misjudge a test case which triggered other failures to be the failing test case for the failure we currently focus on.

**Test cases:** The number of test cases generated for identifying the MFS indicates the cost of FCI approach. The result is listed in Figure 3(g). We can obviously find that strategy *ILP* generated more test cases than the other strategies. In specific, the gap between the *ILP* and other two strategies ranged from about 2 to 5 (except for the 6th testing object, which exceeds 20), this is acceptable when comparing to all the test cases that each approach needed. The increase in test cases for our approach is necessary, as additional test cases must be generated when some test cases are not satisfied for identifying the MFS of the currently analysed failure. As for strategies distinguishing failures and regarded as one failure, there is no significant difference between the number of test cases generated.

Above all, we draw three conclusions, which help to answer **Q2**:

- 1) The results of strategy distinguishing failures and regard one failure are consistent with the previous formal analysis.
- 2) Considering the quality of the MFS each approach identified, we can find that our *ILP* approach achieves the best performance, followed by the strategy *distinguishing failures*.
- 3) Although our approach need more test cases than the other two strategies, it is an acceptable number.

## 6.3. Evaluating the ILP-based test case searching method

The third empirical study aims to evaluate the efficiency of the ILP-based test case searching component of our approach. To conduct this study, we implemented an FCI approach which is also augmented by the *replacing test cases* strategy, but the test case is randomly replaced.

- 6.3.1. Study setup. The setup of this case study is based on the second case study, and uses the same SUT model as shown in Table XIV. We apply the new random searching based FCI approach to identify the MFS in the prepared SUTs. To avoid the bias coming from the randomness, we repeat the new approach 30 times to identify the MFS in each failing test case. We then compute the average additional test cases as well as other metrics listed in section 6.2.1 for the random-based approach.
- *6.3.2. Results and discussion.* The evaluation of this random-based approach is also shown in Figure 3, in which the polygonal line marked with '×' in each sub-figure indicates the results. The raw data can also be found in the column 'R' of Table XV in the appendix.

Compared to the ILP-based approach, we can firstly observe that there is little distinction between them in terms of the metrics: accurate schemas, super-schemas, subschemas, ignored schemas, irrelevant schemas (for some particular cases the ILP-based approach performs slightly better, e.g., in Figure 3(b) for the first testing object, the ILP-based approach identified less subschemas than that of the Random-based approach and in Figure 3(c) still for the first object the ILP-based approach identified less super schemas than that of the random-based approach). The similar quality of the identified MFS between these two approaches is conceivable as they both use the test case replacement strategy, although the test cases generated may be different.

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Secondly, when considering the cost, we find that the ILP-based approach performs better, which can reduce on average 1 to 2 test cases compared to the random-based procedure. It shows that our integer programming based searching technique can find a satisfied test case more rapidly than the random approach.

In summary, the answer for **Q3** is that searching for a satisfied test case affects the performance of our approach, especially regarding the number of extra test cases, and the ILP-based test cases can handle the masking effects at a relatively smaller cost than the random-based approach.

# 6.4. Comparison with Feedback driven combinatorial testing

The FDA-CIT [Yilmaz et al. 2014] approach can handle masking effects so that the generated covering array can cover all the  $\tau$ -degree schemas without being masked by the MFS. There is an integrated FCI approach in the FDA-CIT, of which this FCI approach has two versions, i.e., ternary-class and multiple-class. In this paper, we use the multiple-class version for our comparative approach, as Yilmaz claims that it performs better than the former [Yilmaz et al. 2014].

The FDA-CIT process starts with generating a t-way covering array (In [Yilmaz et al. 2014], this is a test case-aware covering array [Yilmaz 2013]). After executing the test cases in this covering array, it records the outcome of each test case and then applies the classification tree method (Wekas implementation of C4.5 algorithm(J48) [Hall et al. 2009]) on the test cases to characterize the MFS of each failure. It then labels these MFS as the schemas that can trigger masking effects. And later if the interaction coverage is not satisfied (here the interaction coverage criteria is different from the traditional covering array, details see [Yilmaz et al. 2014]), it will re-generate a covering array that aims to cover these schemas that were masked by these MFS labeled as masking effects and then repeat the previous steps.

The main target of FDA-CIT is to make the generated test cases to cover all the  $\tau$ -degree schemas. In order to achieve this goal, FDA-CIT needs to repeatedly identify the schemas that can trigger the masking effects. So to make the two approaches (FDA-CIT and ILP) comparable, we need to collect all the MFS that FDA-CIT characterized in each iteration and then compare them with the MFS identified by our approach.

6.4.1. Study setup. As FDA-CIT used a post-analysis (classification tree) technique on covering arrays, we first generated 2 to 4 ways covering arrays. The covering array generating method is based on augmented simulated annealing [Cohen et al. 2003], as it can be easily extended with constraint dealing and seed injecting [Cohen et al. 2007b], which is needed by the FDA-CIT process. As different test cases will influence the results of the characterization process, we generated 30 different 2 to 4 way covering arrays and fed them to the FDA-CIT. Then after running the FDA-CIT, we recorded the MFS identified, and by comparing them with prior actual MFS, we can evaluate the quality of the identified schemas according to the metrics mentioned in the previous case study.

Besides the FDA-CIT, we also applied our ILP-based approach to the generated covering array. Specifically, for each failing test case in the covering array, we separately applied our approach to identify the MFS of that case. In fact, we can reduce the number of extra test cases if we utilize the other test cases in the covering array [Li et al. 2012]), but we did not utilize the information to simplify the experiment. Similarly, we then recorded the MFS that are identified by our approach, and evaluate them according to the corresponding metrics. In addition, we recorded the overall test cases (including the initially generated covering array) that this approach needed and compared the magnitude of these test cases with that of FDA-CIT.

As mentioned before, the FCI approach in FDA-CIT, i.e., classification tree algorithm, is a post-analysis technique. Given different test sets, the results identified by the classification tree algorithm are also different. Then a nature question is, what the schemas identified by FDA-CIT will be if the classification tree method is applied on the test cases generated by our approach ILP? To figure this question out is of importance as first, we can learn that whether the test cases generated by ILP can help FDA-CIT approach to improve its quality of the identified schemas; second, the comparison between ILP and FDA-CIT will be more fair as they share the same test cases. For this, a new approach that based on FDA-CIT is introduced, which is augmented by replacing the original test cases in FDA-CIT with those generated by ILP approach. Then the schemas identified by the classification tree algorithm in FDA-CIT are recorded and evaluated. This new approach is referred to as *FDA-CITs* later.

6.4.2. Result and discussion. The result is listed in Figure 4. We conducted three groups of experiments. The first one generated 30 different 2-way cover arrays for each testing object, and then for each covering array we applied the three approaches to identify the MFS. The average evaluation results for the experiments based on 30 covering arrays are listed in the Sub-figure 4(a). The other two groups of experiments starts with 3-way covering arrays and 4-way covering arrays, of which their results are depicted in Sub-figure 4(b) and 4(c) respectively.

In each sub-figure, there are 7 columns, showing the outcomes for the previous mentioned 6 metrics and one more metric (Column *Testcase*), which indicates the overall test cases that each approach needed. Each column has three bars (Except for the Column *Testcase*, as the overall test cases for ILP and FDA-CITs are the same), which indicate the results for approach FDA-CIT, ILP and FDA-CITs, respectively.

Note that in Figure 4, the results for each metric is the average evaluation for all the results of the experiments on the 15 testing objects in Table XIV. The raw results for each testing object are listed in Table XVI in the appendix. The raw data is organised the same way as Table XV, except that we added a column t which indicates the strength of the covering array generated for this experiment.

With respect to the relationships between the results and the degree *t* of the covering arrays, we have the following observations:

First, for every metric in our study, the order of the performance of each approach is stable against the change of degree t. Take for example the metric accurate number. No matter what t is (2, 3 or 4), ILP always obtained the most schemas that are identical to the actual MFS, and then is FDA-CITs, and the last is FDA-CIT. This observation indicates that the difference between the performance of these approaches is not dependent on the characteristics of the covering array, but instead on the approaches themselves.

Second, with increasing t, the overall performance of each approach is improved. For example, the score of the aggregative metric of ILP is 0.55, 0.66 and 0.69, respectively, for t equals to 2, 3 and 4. The improvement is mainly because with increasing t, the number of test cases also increased. Based on this, the approach will observe more failing test cases (See area B in Figure  $\ref{eq:total_property}$ ), so that we can get the schemas more close to the actual MFS.

Third, for different approaches in our study, the effect of the change of t on the scores of other metrics varies. Specifically, for ILP, with increasing t, metrics accurate number, sub number, super number, irrelevant number also increase, while metric ignore number decreases. This is mainly because ILP is based on  $FIC\_BS$  [Zhang and Zhang 2011], which works on single failing test case. As we all know, when t increases, the number of test cases also increases. Then when applying our approach, more different schemas may be identified from those additional failing test cases, so the number of

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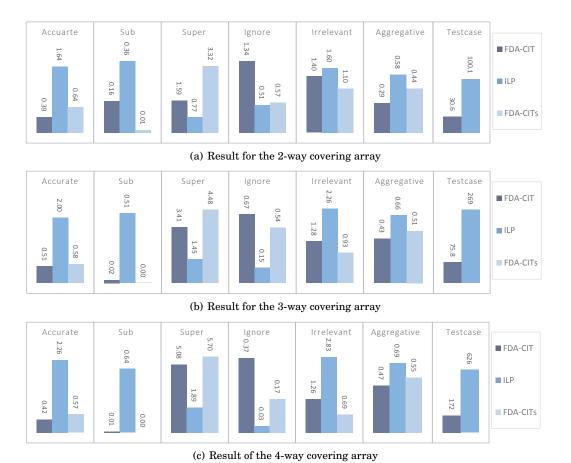


Fig. 4. Three approaches augmented with the replacing strategy

accurate MFS, sub-schemas of the actual MFS, super-schemas of the actual MFS, and schemas that are irrelevant to the actual MFS will increase. Furthermore, some actual MFS that had been ignored before may be obtained. For FDA-CIT and FDA-CITs, however, we find that sub number, irrelevant number decrease with increasing t. We believe this result is due to the use of the classification tree method. A typical classification tree works by partitioning the test cases according to some aspects. Here, the aspect is the parameter value of the SUT. And one path (conjunction of nodes from the root to one leaf in the tree) in this tree is deemed as an MFS. So when test cases increase, the classification may need more nodes to classify the test cases. This induces the so-called 'over fitting' problem. As a result, the schemas identified by FDA-CIT and FDA-CITs tend to be the super schemas of the actual MFS, leading to a decrease of sub number and irrelevant number.

Other observations include:

First, when compared with the original approach FDA-CIT, FDA-CITs has obvious advantages at almost all the metrics except for super number. In detail, FDA-CITs obtained more schemas that are identical to the actual MFS (accurate number), less schemas that are the sub schemas of actual MFS (sub number), and lower scores for the two negative metrics (ignored number and irrelevant number). At last, the schemas identified by FDA-CITs showed an overall higher quality than that of the original

FDA-CIT (aggregative metric). We have discussed previously that FDA-CIT tends to identify super-schemas of actual MFS when the test cases increase. So for metric super number, it is no surprise that FDA-CITs identified more super schemas of actual MFS than FDA-CIT, because it used the test cases generated by ILP, which were more than that of the original FDA-CIT. The difference between the overall performance of FDA-CIT and FDA-CITs is also expected. In fact, this result is consistent with our previous observation that when t increases, the overall performance for each approach also increases.

Second, in terms of the quality of the MFS identified, we can clearly find that our approach performed better than the other approaches. This is mainly manifested in that our approach obtained more accurate schemas and identified less irrelevant ones. We believe this gap is mainly caused by the FCI approach. Because for *ILP* and *FDA-CITs*, the test cases used to identify the MFS are the same. The only difference is how they utilize them to identify MFS. However, this result does not mean that FIC\_BS is better than the classification tree method under all conditions. The classification tree method has its own advantage, i.e., it does not need to generate additional test cases, and as a result, *FDA-CIT* generated less test cases than that of *ILP*.

In fact, another reason why our approach generated more test cases is that the F-CI approach, i.e., FIC\_BS, works on single test case, so when there are many failing test cases in the covering array, we need to repeatedly use our approach to identify the MFS for each failing test case. This process may produce many redundant test cases, because many failing test cases contain the same MFS, and when we have already identified the MFS in one test case, there is no need to identify it again in other failing test cases. Jieli [Li et al. 2012] introduced a method that utilizes the previous generated test cases to reduce such redundance. Here we did not use this technique to simplify our experiment. We believe if we utilize the MFS that are already identified in previous iteration, the overall number of test cases will decrease.

Above all, we can conclude three points in this experiment, which provide answer to **Q4**:

1)The degree t of the covering array does not determine the order of the performance of different approaches, but for each approach, the bigger the t is, the better its performance will be.

2)When taking the test cases generated by our approach *ILP*, *FDA-CITs* performed better than the original *FDA-CIT* approach.

3)Considering the quality of the MFS each approach identified, *ILP* performed better than the other two approaches, although it needed more test cases.

Based on these observations, a recommendation for selecting masking handling techniques in practice is that to get a more precise identification of the MFS in the SUT, *ILP* is preferred, and for a small size of test cases, *FDA-CIT* may be a better choice.

# 6.5. Threats to validity

6.5.1. internal threats. There are two threats to internal validity. First, the characteristics of the actual MFS in the SUT can affect the FCI results. This is because the magnitude and location of the MFS can make the FCI approaches generate different test cases. And as a result, it can make the observed failing test cases and predicted failing test cases different (See Figure ??). In the worst case, the FCI approach happens to identify the exact actual MFS, and in that condition our test case replacing strategy is of no use. In this paper, we used 15 testing objects, in which 5 are real software systems with real faults and 10 synthetic ones with injected faults. To reduce the influence caused by different characteristics of the MFS, we need to build more testing objects and injected more different types of faults for a more comprehensive study of our approach.

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The second threat is that we just applied our test case replacing strategy on one FCI approach – FIC\_BS [Zhang and Zhang 2011]. Although we believe the test case replacing strategy can also improve the quality of the identified MFS for other FCI approaches when the testing object is suffering from masking effects, the extent to which their results can be refined may vary for different FCI approaches. For example, for FIC\_BS [Zhang and Zhang 2011] used in this paper, there are about (v-1) to  $(v-1)^{k-1}$  candidate test cases that can be replaced when one test case triggered other failures, while for OFOT [Nie and Leung 2011a], we only have (v-1) candidates. As a result, FIC\_BS can have a higher chance than OFOT to find a satisfied test case. So to learn the difference between the improvement of different FCI approaches when applying our test case replacing strategy, we need to try more FCI approaches in the future.

6.5.2. external threats. One threat to external validity comes from the real software we used. In this paper we have only surveyed two types of open-source software with five different versions, of which the program scale is medium-sized. This may impact the generality of our results.

Another important threat is that our approach is based on the assumption that different errors in the software can be easily distinguished by information such as exception traces, state conditions, or the like. If we cannot directly distinguish them, our approach does not work. In such case, one potential solution is to use the clustering techniques to classify the failures according to available information [Zheng et al. 2006; Jones et al. 2007; Podgurski et al. 2003]. If we cannot classify them because we do not have enough information (e.g., the black box testing) or it is too costly, we believe the only approach is to take the *regarded as one failure* strategy. With this strategy, we must aware that the MFS identified are likely to be sub-schemas or irrelevant schemas of the actual MFS.

The third threat comes from the possible masking relationships between multiple failures in the real software. In this paper, we just focus on the condition that the masking effects are transitive, i.e., if failure A masks B, failure B masks C, then failure A must mask the failure C. In practice, the relationships between multiple failures may be more complicated. One possible scenario is that two failures are in a loop, for which the two failures can even mask each other in a particular condition. Such a case will make our formal analysis invalid and will significantly complicate the relationships between schemas and their corresponding test cases. A new formal model should be proposed to handle that type of masking effects.

# 7. RELATED WORKS

Shi and Nie presented an approach for failure revealing and failure diagnosis in CT [Shi et al. 2005], which first tests the SUT with a covering array, then reduces the value schemas contained in the failing test case by eliminating those appearing in the passing test cases. If the failure-causing schema is found in the reduced schema set, failure diagnosis is completed with the identification of the specific input values which caused the failure; otherwise, a further test suite based on SOFOT is developed for each failing test cases, and the schema set is then further reduced, until no more faults are found or the fault is located. Based on this work, Wang proposed an AIFL approach which extended the SOFOT process by adaptively mutating factors in the original failing test cases in each iteration to characterize failure-inducing interactions [Wang et al. 2010].

Nie et al. introduced the notion of Minimal Failure-causing Schema(MFS) and proposed the OFOT approach which is an extension of SOFOT that can isolate the MFS in SUT [Nie and Leung 2011a]. This approach mutates one value with different val-

ues for that parameter, hence generating a group of additional test cases each time to be executed. Compared with SOFOT, this approach strengthens the validation of the factor under analysis and can also detect the newly imported faulty interactions.

Delta debugging [Zeller and Hildebrandt 2002] is an adaptive divide-and-conquer approach to locate interaction failure. It is very efficient and has been applied to real software environment. Zhang et al. also proposed a similar approach that can efficiently identify the failure-inducing interactions that has no overlapped part [Zhang and Zhang 2011]. Later, Li improved the delta-debugging based approach by exploiting useful information in the executed covering array [Li et al. 2012].

Colbourn and McClary proposed a non-adaptive method [Colbourn and McClary 2008]. Their approach extends a covering array to the locating array to detect and locate interaction failures. C. Martinez proposed two adaptive algorithms. The first one requires safe value as the assumption and the second one removes this assumption when the number of values of each parameter is equal to 2 [Martínez et al. 2008; 2009]. Their algorithms focus on identifying faulty tuples that have no more than 2 parameters.

Ghandehari et al. defined the suspiciousness of tuple and suspiciousness of the environment of a tuple [Ghandehari et al. 2012]. Based on this, they ranked the possible tuples and generated the test configurations. They further utilized the test cases generated from the inducing interaction to locate the fault [Ghandehari et al. 2013].

Yilmaz proposed a machine learning method to identify inducing interactions from a combinatorial testing set [Yilmaz et al. 2006]. They constructed a classification tree to analyze the covering arrays and detect potential faulty interactions. Beside this, Fouché [Fouché et al. 2009] and Shakya [Shakya et al. 2012] made some improvements in identifying failure-inducing interactions based on Yilmaz's work.

Our previous work [Niu et al. 2013] proposed an approach that utilizes the tuple relationship tree to isolate the failure-inducing interactions in a failing test case. One novelty of this approach is that it can identify the overlapped faulty interaction. This work also alleviates the problem of introducing new failure-inducing interactions in additional test cases.

In addition to the studies that aim at identifying the failure-inducing interactions in test cases, there are others that focus on working around the masking effects.

Constraints handling become more and more popular in CT these years. A constraint is an invalid interaction that should not appear in the test case. It can be deemed as the masking effect which are known in prior [Yilmaz et al. 2014]. Cohen [Cohen et al. 2007a; 2007b; 2008] studied the impact of the constraints that render some generated test cases invalid in CT. They also proposed an approach that integrates the incremental SAT solver with the covering arrays generating algorithm to avoid those invalid interactions. Further study was conducted [Petke et al. 2013] to show that with consideration of constrains, higher-strength covering arrays with early failure detection are practical.

Besides, there are additional works that aim to study the impacts of constraints for CT [Garvin et al. 2011; Bryce and Colbourn 2006; Calvagna and Gargantini 2008; Grindal et al. 2006; Yilmaz 2013]. Among them, [Bryce and Colbourn 2006] distinguished the constraints into two types: hard and soft, which the former cannot be included in the test case, while the latter can be permitted, but not desirable. [Grindal et al. 2006] comprehensively compared the performance of four strategies at handling the constraints in the covering array. [Calvagna and Gargantini 2008] proposed an heuristic strategy to handle the constraints. It can support an ad-hoc inclusion or exclusion of interactions such that the user can customize output of the covering array. [Garvin et al. 2011] refined the simulated annealing algorithm to efficiently construct the covering array with considering the constraints. [Yilmaz 2013] introduced the test

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case-specific constraints; differing from the system-wide constraints, this constraint can only be triggered in some specific test cases.

Chen et al. addressed the issues of shielding parameters in combinatorial testing and proposed the Mixed Covering Array with Shielding Parameters (MCAS) to solve the problem caused by shielding parameters [Chen et al. 2010]. The shielding parameters can disable some parameter values to expose additional interaction errors, which can be regarded as a special case of masking effects.

Dumlu and Yilmaz proposed a feedback-driven approach to work around the masking effects [Dumlu et al. 2011]. Specifically, they first used classification tree to classify the possible failure-inducing interactions and eliminate them. Then they generate new test cases to detect possible masked interaction in the next iteration. They further extended their work [Yilmaz et al. 2014] by proposing a multiple-class CTA approach to distinguish failures in SUT. In addition, they empirically studied the impacts of masking effects on both ternary-class and multiple-class CTA approaches.

These works can be categorized into 3 groups according to their relationships with our work. First, the works that aim to identifying the MFS in the SUT. Our work also focuses on identifying the MFS, but instead of single failure, our work considers the impacts of multiple failures on the FCI approaches, and based on this, a test case replacement strategy is proposed that can assist these FCI approaches in reducing the negative effects. Second, the works that aim to handling the constraints. As discussed before the constraints can be deemed as a special masking effects. Our work differs from them in that the masking effects handled in this paper are those that can be dynamically triggered; that is, we did not know them in prior. Another difference between our work with these constraints handling works is that their target is to avoid the constraints when generating covering array. However, our work aims to removing the masking effects of the FCI approaches. Last, the work that is most similar to our work [Yilmaz et al. 2014], which also considered the masking effects that are dynamically appeared in test cases. But different from our work, it mainly focused on reducing the masking effects in the covering array, so that the covering array can support a comprehensive validation of all the  $\tau$ -degree schemas. The approach used to reduce this negative effect is to use the FCI approach to identify the schemas that can trigger this effect in each iteration. Our approach, however, aims to handling the masking effects that happened in these FCI approaches themselves, and our approach alleviates the masking effects by augmenting the FCI approaches with a test case replacement strategy.

#### 8. CONCLUSIONS

Masking effects of multiple failures in SUT can bias the results of traditional failure-inducing interactions identifying approaches. In this paper, we formally analysed the impact of masking effects on FCI approaches and showed that the two traditional strategies, i.e., *regarded as one fault* and *distinguishing failures*, are both inefficient in handling such impact. We further presented a test case replacement strategy for FCI approaches to alleviate such impact.

In our empirical studies, we extended FIC BS [Zhang and Zhang 2011] with our strategy. The comparison between our approach and traditional approaches was performed on several open-source software. The results indicated our strategy assists the traditional FCI approach in achieving better performance when facing masking effects in SUT. We also empirically evaluated the efficiency of the test case searching component by comparing it with the random searching based FCI approach. The results showed that the ILP-based test case searching method can perform more efficiently. Last, we compared our approach with existing technique for handling masking effects – FDA-CIT [Yilmaz et al. 2014], and observed that our approach achieved a more pre-

cise result which can better support debugging, though our approach required more test cases than FDA-CIT.

As for the future work, we need to do more empirical studies to make our conclusions more general. Our current experiments focus on medium-sized software. We would like to extend our approach to more complicated, large-scaled testing scenarios. Another promising work in the future is to integrate the white-box testing technique into the FCI approaches. We believe gaining insight into source code can help figure out the relationships between multiple failures, and hence facilitate the FCI approaches obtaining more accurate results. And last, because the extent to which the FCI suffers from masking effects varies with different algorithms, combining these different FCI approaches would be desired in the future to further improve identifying MFS of multiple failures.

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# Online Appendix to: Identifying minimal failure-causing schemas in the presence of multiple failures

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# A. THE DETAIL OF THE EXPERIMENTS

Table XV. Result of the evaluation of each appraoch

Subject	ac	cur	at	e	su	b			su	peı	•	ignore					irrelevant				all			test cases			
	0	$^{1}D$	$^2$ I $^3$	$^{3}R$	O	D	Ι	R	o	D	I R	0	D	I	R	0	D	Ι	R	0	D	I	R	0	D	I	R
HSQLDB 2cr8	2	3	5	5	3	2	0	2	0	2	4 5	0(2.04)	0(3.91)	0(4.0)	0(4.1)	0	2	0	34	0.57	0.65	0.88	0.23	8.125	11.92	17	17.72
HSQLDB 2.2.5	2	<b>2</b>	$^{2}$	$^{2}$	1	0	0	0	0	1	1 1	0(0.83)	0(1.0)	0(1.0)	0(1.0)	7	0	0	0	0.25	0.83	0.83	0.83	8.67	7.67	10.17	11.3
HSQLDB 2.2.9	2	3	2	2	3	1	1	1	0	4	1 1	0(1.33)	0(2.83)	0(2.56)	0(2.56)	4	0	0	0	0.4	0.74	0.8	0.8	9.167	8.61	11.72	13.14
JFlex 1.4.1	2	<b>2</b>	<b>2</b>	<b>2</b>	0	0	0	0	0	1	0 0	0(0.75)	0(1.0)	0(1.0)	0(1.0)	25	0	0	0	0.07	0.83	1	1	23.5	6.5	8	9.68
JFlex 1.4.2	2	<b>2</b>	<b>2</b>	<b>2</b>	1	0	0	0	0	1	1 1	0(0.67)	0(1.0)	0(1.0)	0(1.0)	25	0	0	0	0.09	0.83	0.83	0.83	20.5	9	11.67	13.12
synthez 1	2	1	1	1	2	0	0	0	0	$^{2}$	2 2	0(1.0)	0(2.0)	0(2.0)	0(2.0)	15	17	17	17	0.19	0.11	0.11	0.11	16.5	18	41.75	41.75
synthez 2	3	3	3	3	10	0	0	0	0	10	6 6	0(1.96)	0(2.0)	0(2.0)	0(2.0)	1	0	0	0	0.54	0.76	0.8	0.8	11.19	14.12	16.96	17.08
synthez 3	4	3	3	3	4	<b>2</b>	<b>2</b>	$^{2}$	0	5	5 5	0(2.08)	0(2.84)	0(2.84)	0(2.84)	13	9	9	9	0.28	0.34	0.34	0.34	12.73	9.46	14.18	14.44
synthez 4	3	3	3	3	10	3	<b>2</b>	3	0	6	5 5	0(2.6)	0(2.8)	0(2.9)	0(2.85)	9	9	9	9	0.35	0.4	0.39	0.39	9.91	13.02	18.55	18.45
synthez 5	2	<b>2</b>	<b>2</b>	<b>2</b>	4	0	0	0	0	$^{2}$	1 1	0(1.02)	0(1.0)	0(1.0)	0(1.0)	1	0	0	0	0.65	0.88	0.92	0.92	13.04	13.7	14.77	14.84
synthez 6	2	3	3	3	15	4	4	4	0	8	8 8	0(1.99)	0(3.72)	0(3.72)	0(3.72)	8	10	10	10	0.38	0.36	0.36	0.36	14.91	11.75	15.37	15.71
synthez 7	3	3	3	3	10	0	0	0	0	6	6 6	0(2.04)	0(2.0)	0(2.0)	0(2.0)	5	0	0	0	0.39	0.83	0.83	0.83	12.77	14.59	16.44	16.53
synthez 8	2	<b>2</b>	<b>2</b>	<b>2</b>	4	0	0	9	0	4	3 3	0(1.05)	0(1.0)	0(1.0)	0(1.0)	3	0	0	0	0.56	0.9	0.91	0.91	24.45	25.25	26.27	26.37
synthez 9	2	1	1	1	1	0	0	0	0	1	1 1	0(0.8)	0(1.0)	0(1.0)	0(1.0)	0	0	0	0	0.75	0.83	0.83	0.83	6.8	8	9	9
synthez 10	0	1	1	1	3	1	1	1	0	0	0 0	0(1.0)	0(1.46)	0(1.31)	0(1.31)	0	$^{2}$	1	1	0.5	0.47	0.58	0.58	9.08	11	15.38	15.53

 $<sup>^{1}</sup>$  O denotes the strategy regarded as one failure.  $^{2}$  D denotes the strategy distinguishing failures.

 $<sup>^3</sup>$  I denotes the replacement strategy based on ILP searching.

<sup>&</sup>lt;sup>4</sup> R denotes the replacement strategy based on randomly searching.

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Table XVI. Comparison with FDA-CIT

 $<sup>^1</sup>$  F is for the FDA-CIT approach.  $^2$  I is for the our approach with replacement strategy based on ILP searching.  $^3$  Fs is for the FDA-CITs approach.