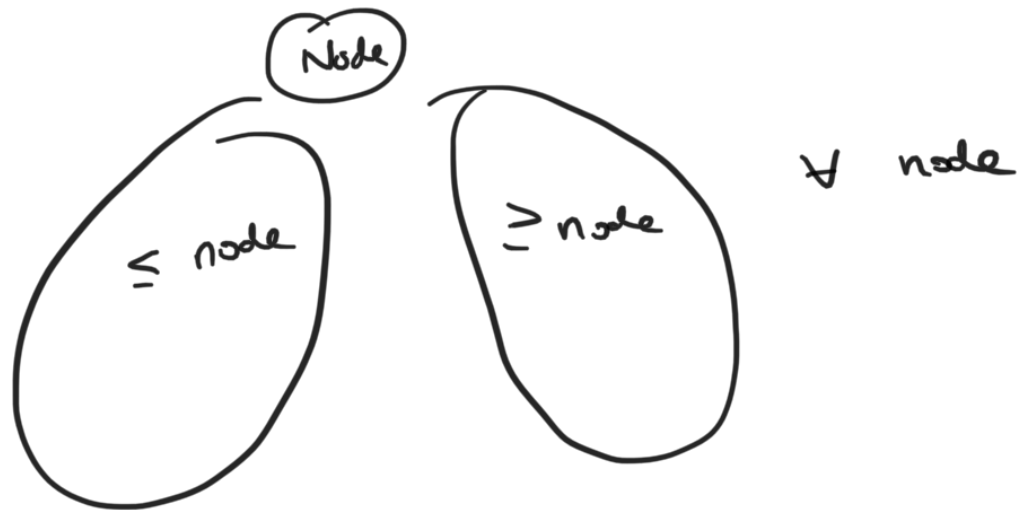


# Trees

Binary search tree (BST)

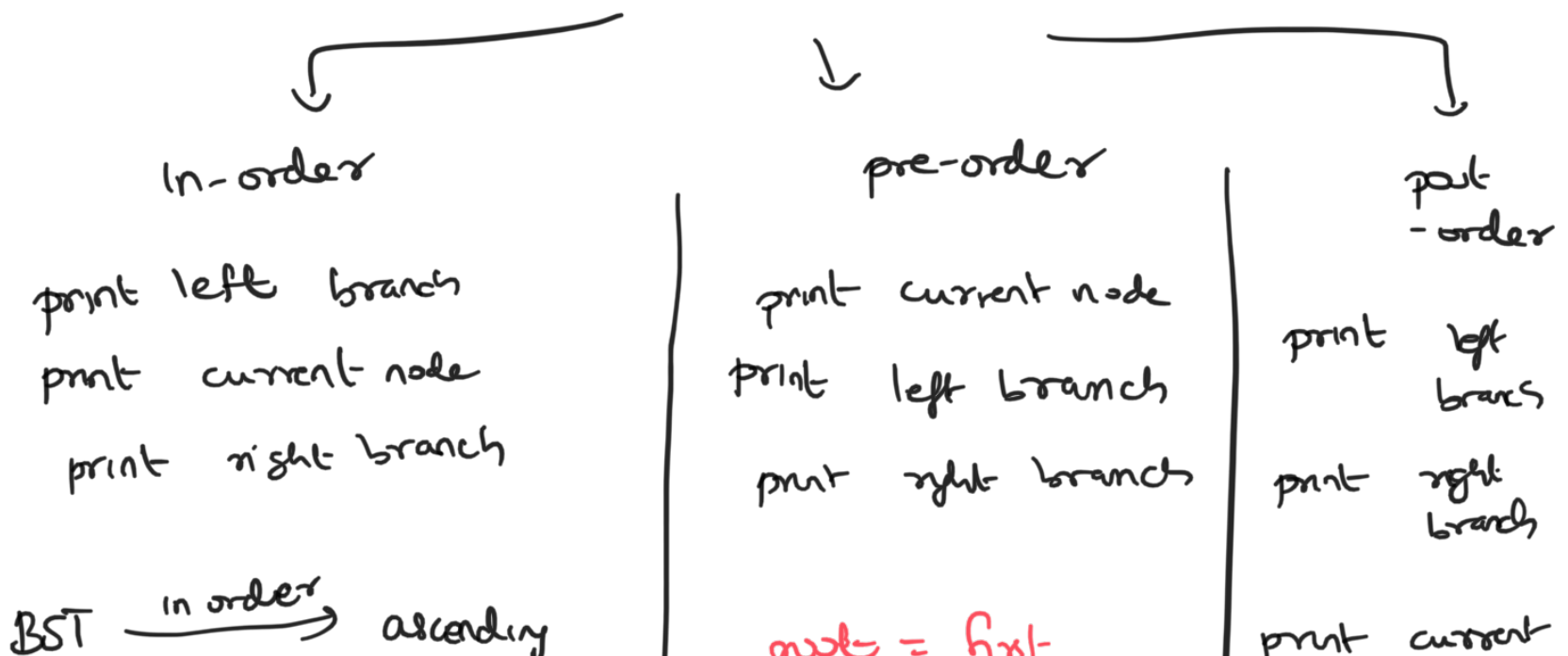


Balanced tree  $\rightarrow$  ensure  $O(\log n)$   
for insert, find

(eg) Red-Black trees,  
AVL trees

full binary tree - every node has 0/2 children

## Binary tree traversal



order

node  
visited

node

root = last  
node  
visited

## Bidirectional search

shortest path from  $s \rightarrow t$

→ Run 2 simultaneous bfs, one from

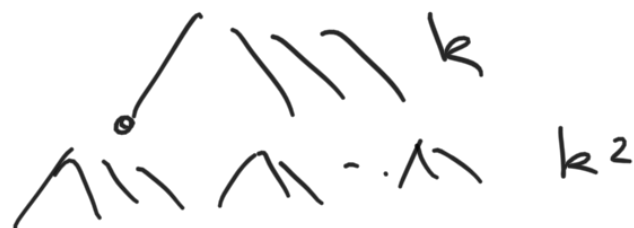
each node  $s, t$

→ searches collide,



If  $\deg(v) \leq k$

traditional bfs



$$k + k^2 + \dots + k^d$$

$$1 + k + \dots + k^d = \frac{k^{d+1} - 1}{k - 1} \sim O(k^{d+1})$$

in bidirectional

---

$$2 k^{d/2+1} \sim$$

$$O(k^{d/2+1})$$