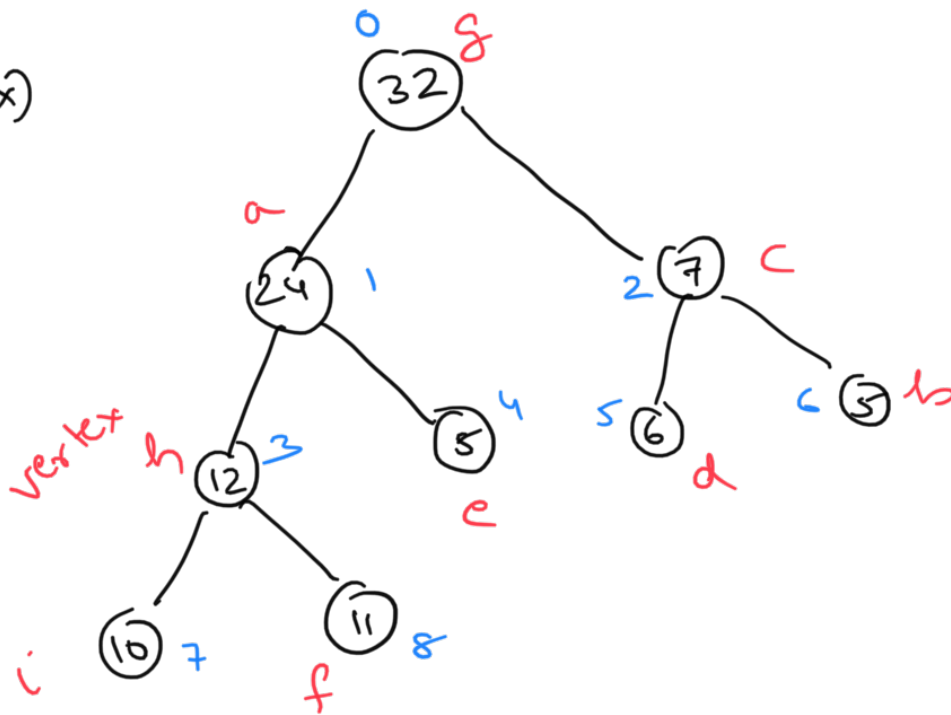


Heaps again

Sometimes you want to update values in a heap

(ex)



red colour:
vertex label
corresponding
to datum
in original
problem

blue colour:
node location in
heap

maintain

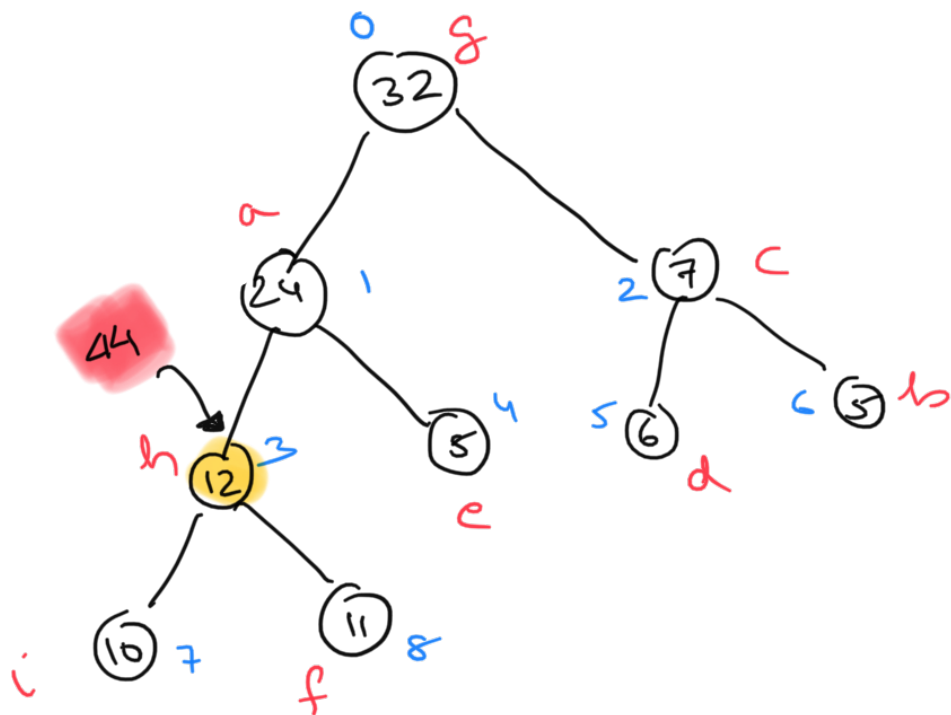
(I) vertex to heap node

a: 1, b: 6, c: 2, d: 5, e: 4, f: 8, g: 0, h: 3, i: 7

(II) heap node to vertex

0: g, 1: a, 2: c, 3: h, 4: e, 5: d, 6: b, 7: i, 8: f

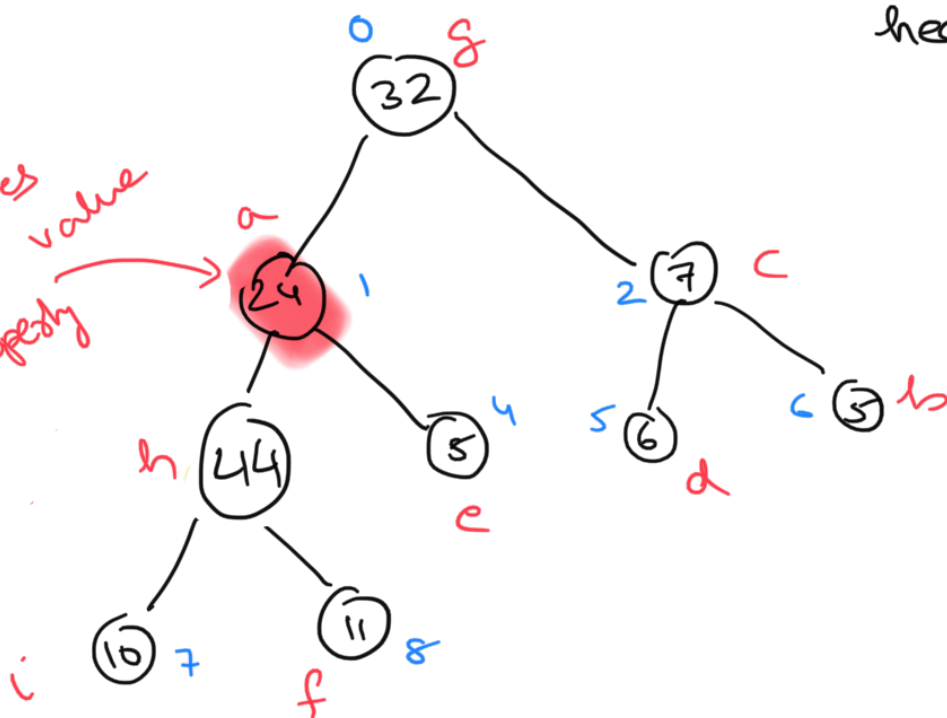
Say you want to update vertex h's value
from 12 to 44 in original problem.



$44 > 12$, so

heap property
if at all
will be
violated
upwards.

Violates
local
property



So swap 24 and 44

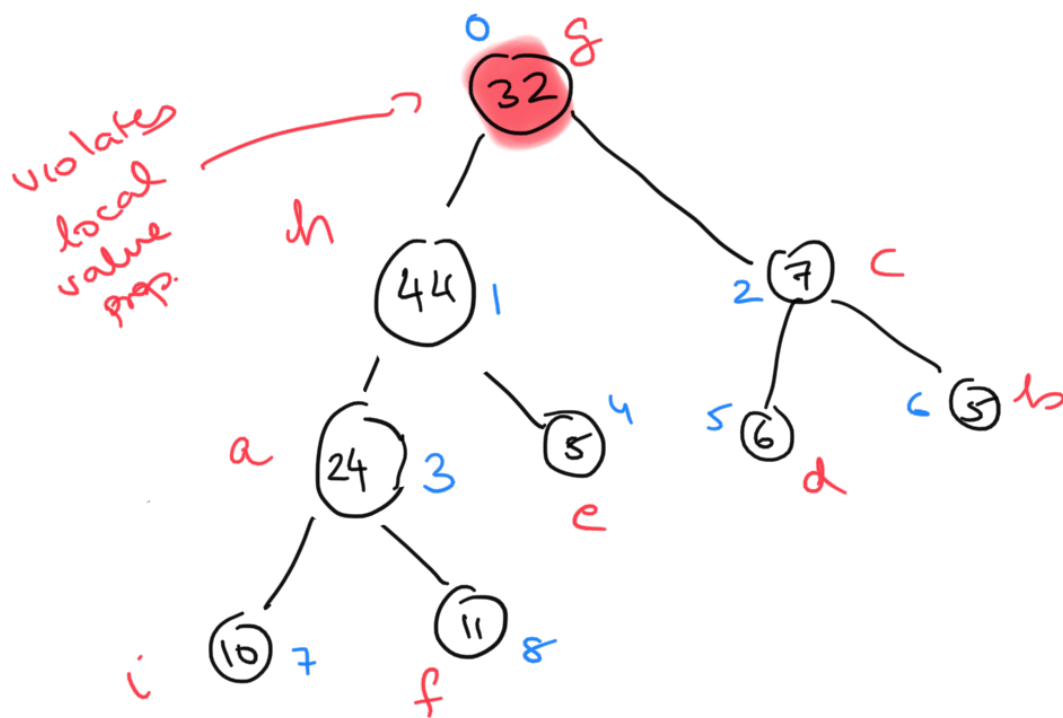
Update

→ (I) vertex to heap node

$a: \overset{3}{\cancel{x}}$, $b: 6$, $c: 2$, $d: 5$, $e: 4$, $f: 8$, $g: 0$, $h: \overset{1}{\cancel{x}}$, $i: 7$

→ (II) heap node to vertex

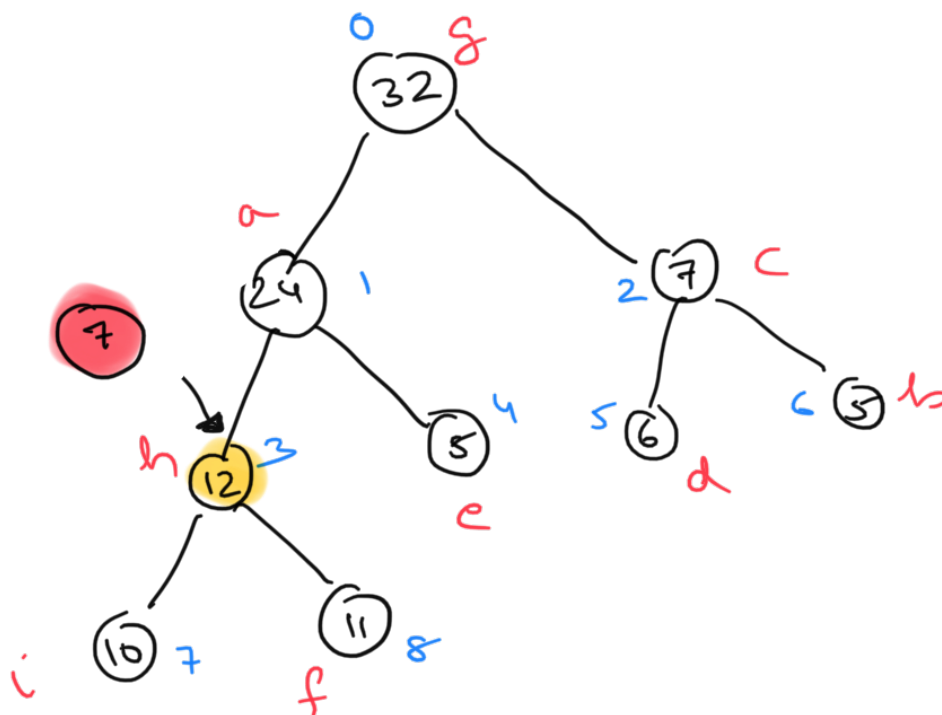
$0: g$, $1: \overset{a}{\cancel{x}}$, $2: c$, $3: \overset{h}{\cancel{x}}$, $4: e$, $5: d$, $6: b$, $7: i$, $8: f$



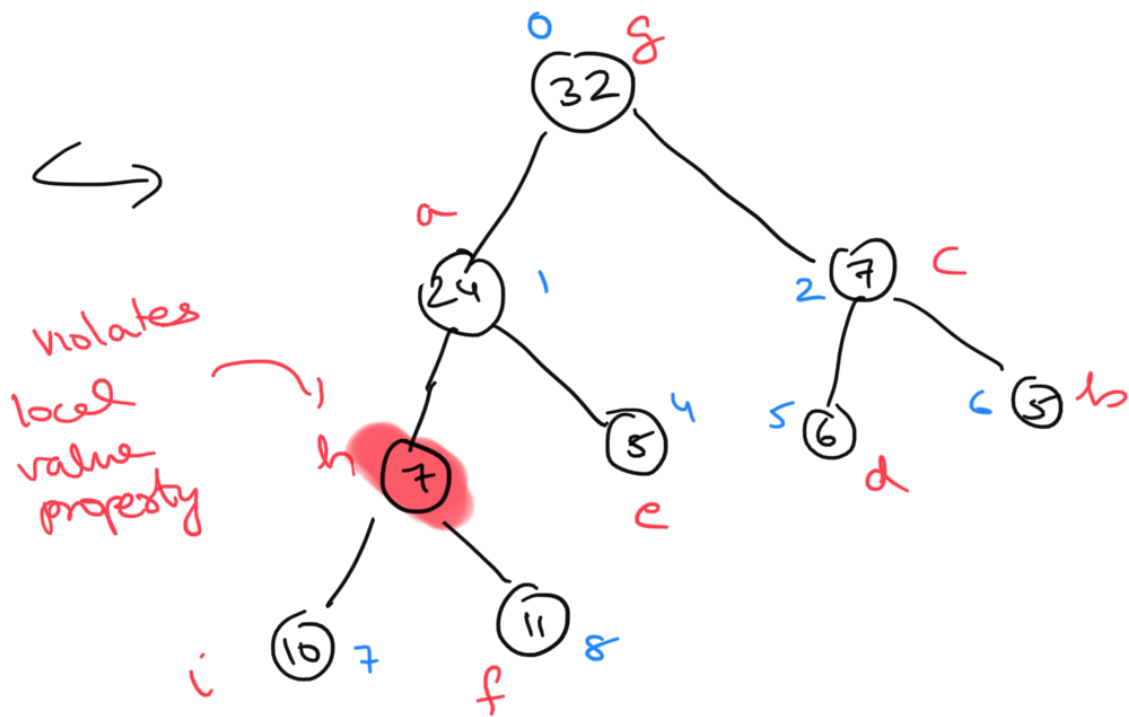
so swap 32 and 44 ...

so you end up walking up heap to repair it

Note if instead you wanted to replace 12 with 7, ...



you'll
walk
down the
tree
repairing
heap...



→ so swap 7 with max of its children
 $\max(10, 11) = 11$

→ so swap 7 and 11

⋮

so you end up walking down the heap

So updating one value → $\log n$

→ updating all values in heap

$O(n \log n)$