

$$E[\log L(\vec{x}, \vec{z} | \theta)] = \sum_{i=1}^n (\log \tau - \frac{1}{2} \log(2\pi\sigma^2) - \sum_{j=1}^n E[z_{ij}] \frac{(x_i - \mu_j)^2}{2\sigma^2})$$

$$\frac{d}{d\theta} E[\log L(\vec{x}, \vec{z} | \theta)] = \frac{d}{d\theta} (\sum_{i=1}^n \log \tau - \frac{1}{2} \log(2\pi\sigma^2) - \sum_{j=1}^n E[z_{ij}] \frac{(x_i - \mu_j)^2}{2\sigma^2})$$

$$= \sum_{j=1}^n \frac{E[z_{ij}] (x_i - \mu_j)}{2} \quad (\sigma^2 = 1)$$

$$= \frac{1}{2} (\sum_{j=1}^n E[z_{ij}] x_i - \sum_{j=1}^n E[z_{ij}] \mu_j) = 0$$

$$\Rightarrow \sum_{j=1}^n E[z_{ij}] x_i = \sum_{j=1}^n E[z_{ij}] \mu_j$$

$$\mu_j = \frac{\sum_{i=1}^n E[z_{ij}] x_i}{\sum_{i=1}^n E[z_{ij}]}$$