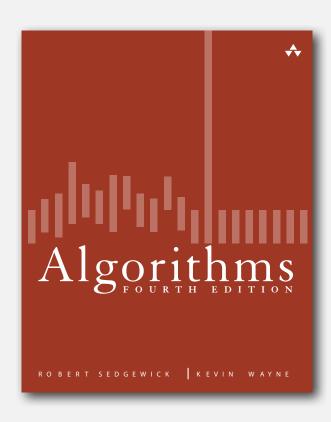
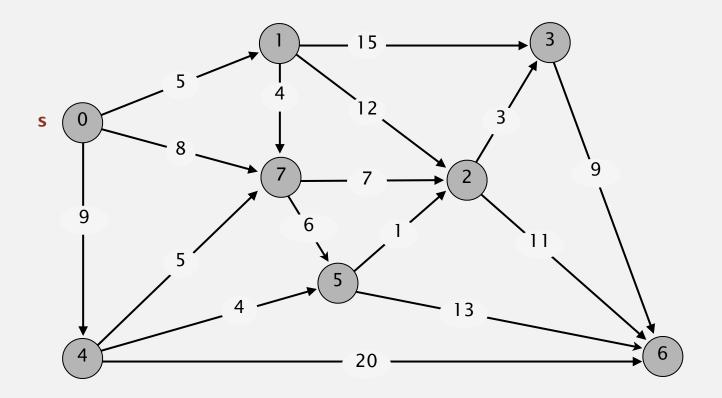
4.4 BELLMAN-FORD DEMO



Repeat V times: relax all E edges.



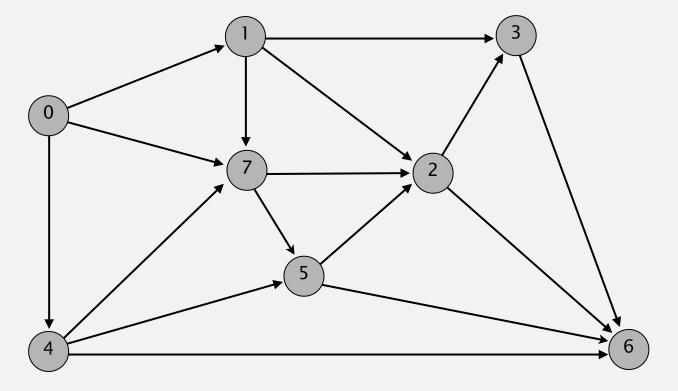
an edge-weighted digraph

0→1	5.0
0→4	9.0
0→7	8.0
1→2	12.0
1→3	15.0
1→7	4.0
2→3	3.0
2→6	11.0
3→6	9.0
4→5	4.0
4→6	20.0
4→7	5.0
5→2	1.0
5→6	13.0
7→5	6.0

7→2

7.0

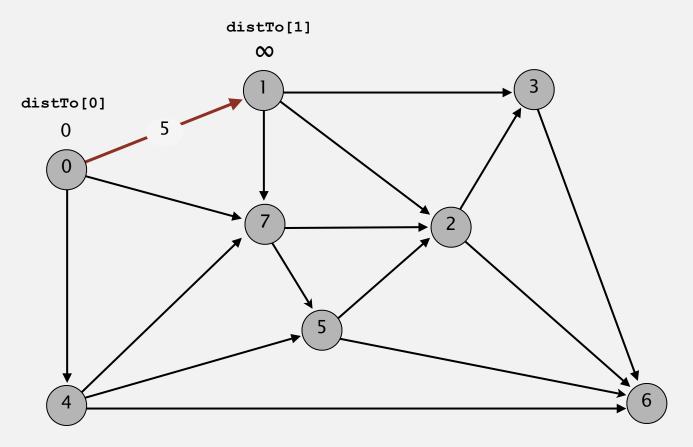
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1		
2		
3		
4		
5		
6		
7		

initialize

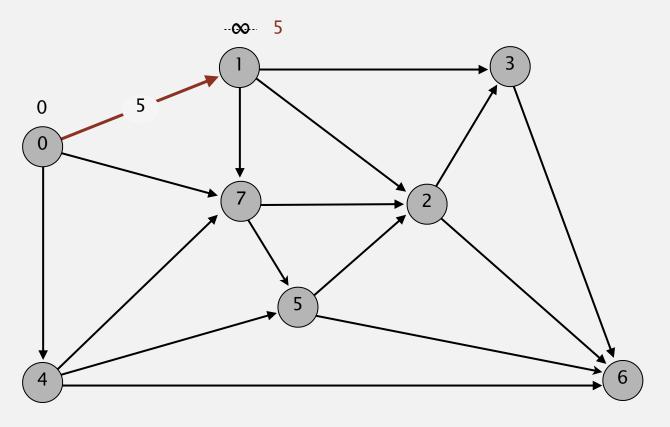
Repeat V times: relax all E edges.



V	distTo[]	edgeTo[]
0	0.0	_
1		
2		
3		
4		
5		
6		
7		

pass 0

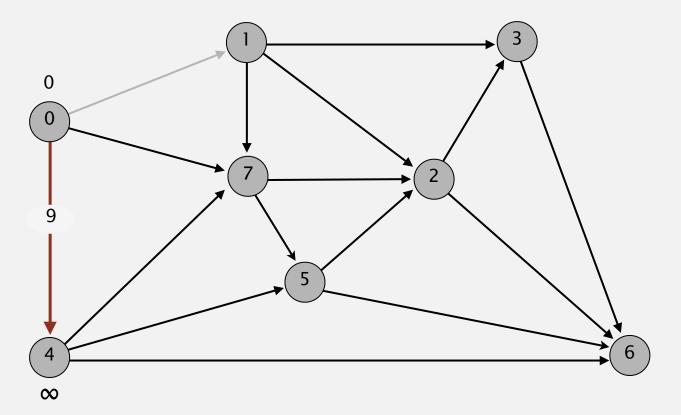
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	_
1	5.0	0→1
2		
3		
4		
5		
6		
7		

pass 0

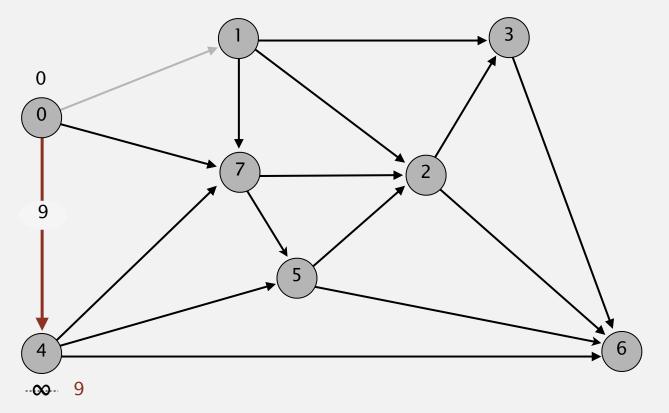
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	_
1	5.0	0→1
2		
3		
4		
5		
6		
7		

pass 0

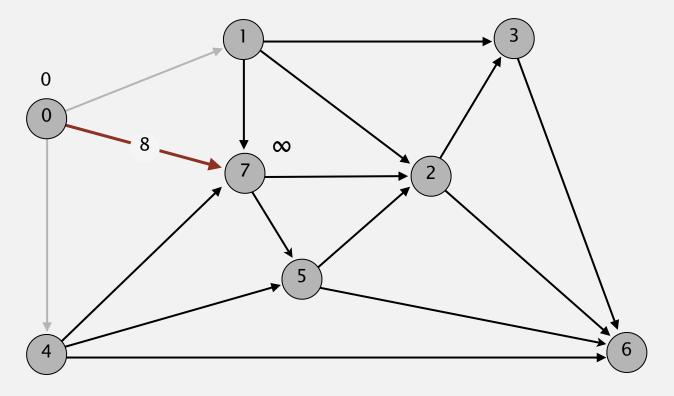
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[
0	0.0	-
1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7		

pass 0

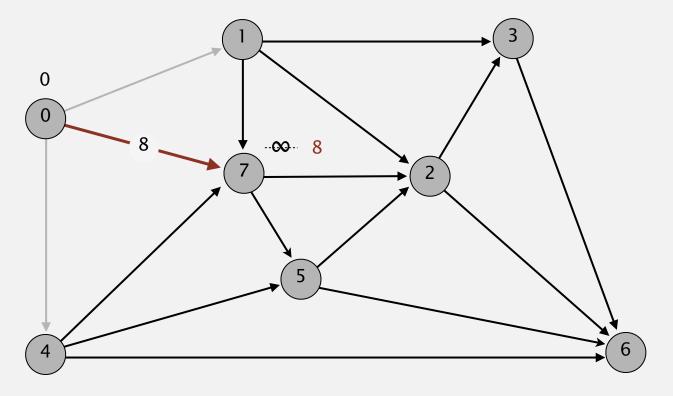
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[
0	0.0	-
1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7		

pass 0

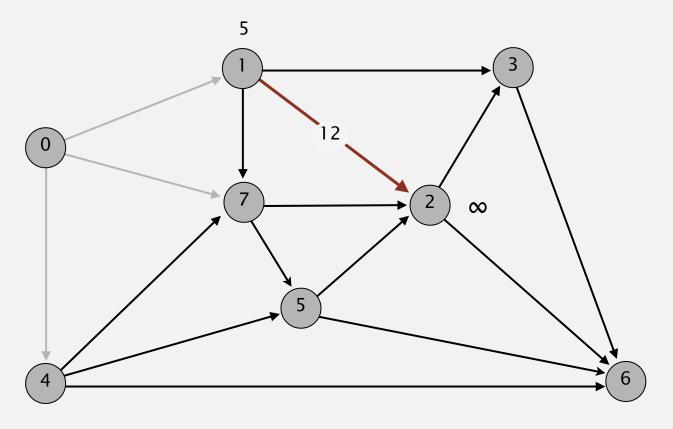
Repeat V times: relax all E edges.



v	<pre>distTo[]</pre>	edgeTo[
0	0.0	-
1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

pass 0

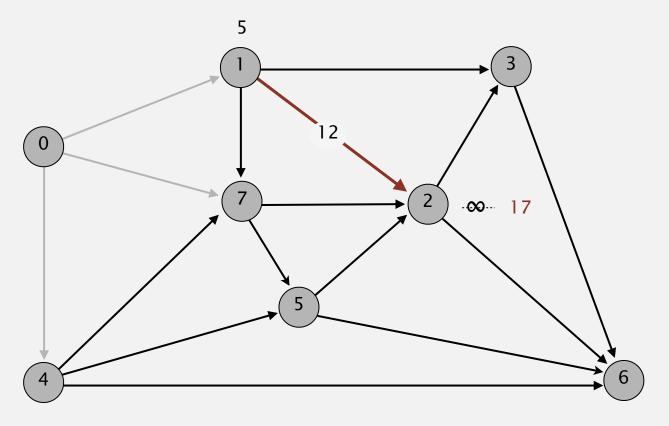
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2		
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

pass 0

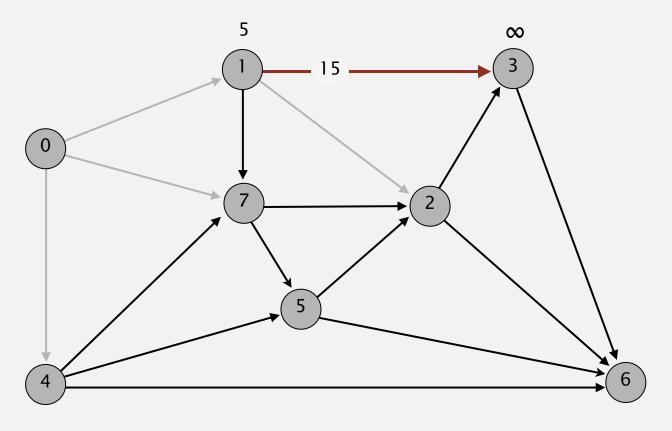
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

pass 0

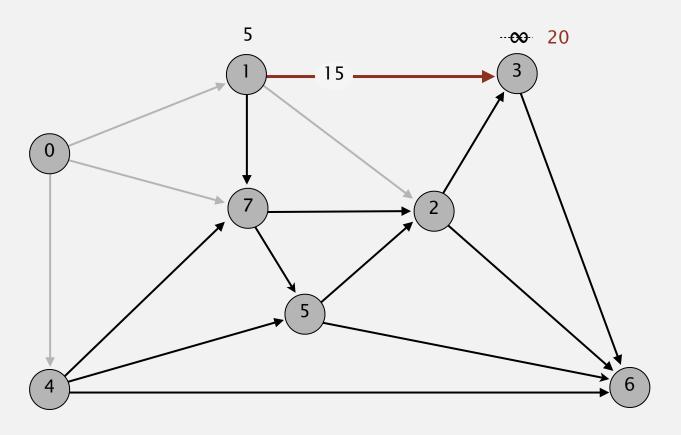
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3		
4	9.0	0→4
5		
6		
7	8.0	0→7

pass 0

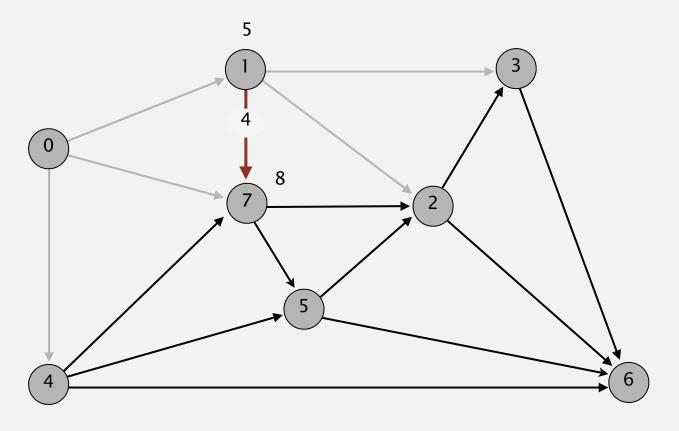
Repeat V times: relax all E edges.



v distTo[] edgeTo 0 0.0 - 1 5.0 0→1	[]
1 5 0 0→1	
1 3.0 0-1	
2 17.0 1→2	
3 20.0 1→3	
4 9.0 0→4	
5	
6	
7 8.0 0→7	

pass 0

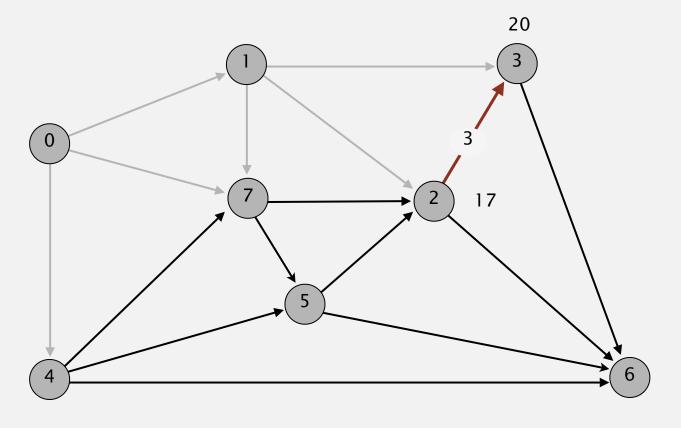
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	_
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5		
6		
7	8.0	0→7

pass 0

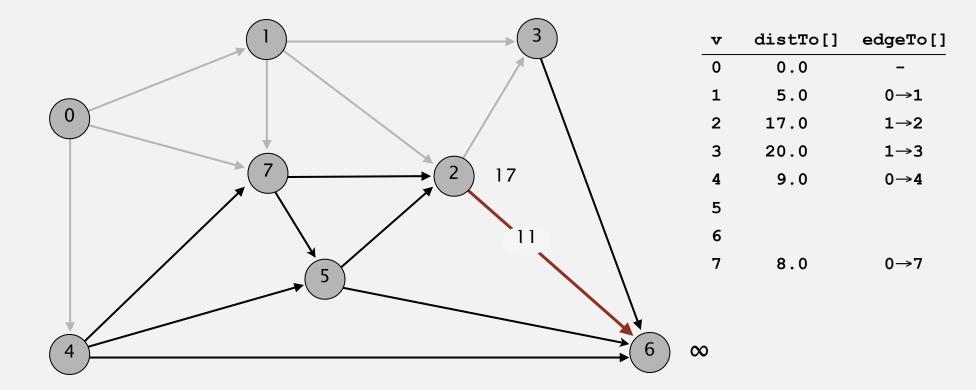
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	_
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5		
6		
7	8.0	0→7

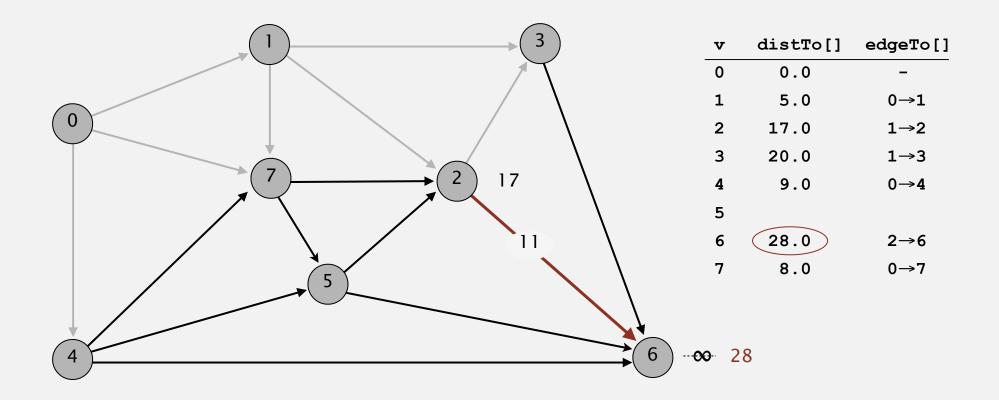
pass 0

Repeat V times: relax all E edges.



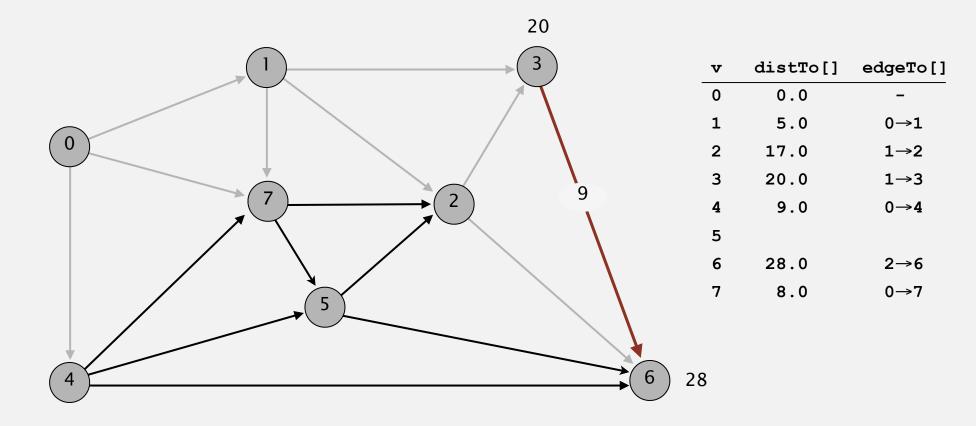
pass 0

Repeat V times: relax all E edges.



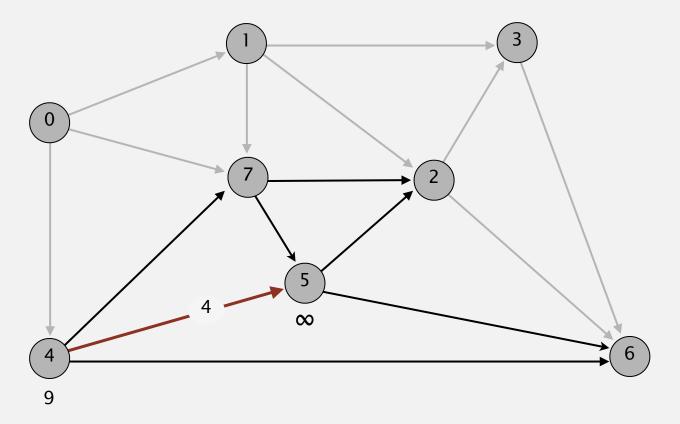
pass 0

Repeat V times: relax all E edges.



pass 0

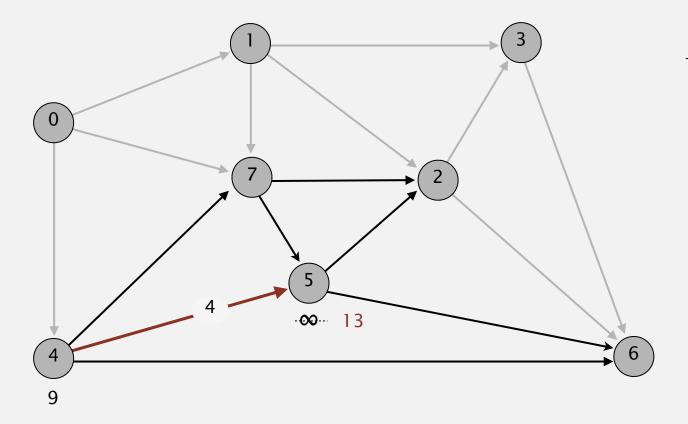
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5		
6	28.0	2→6
7	8.0	0→7

pass 0

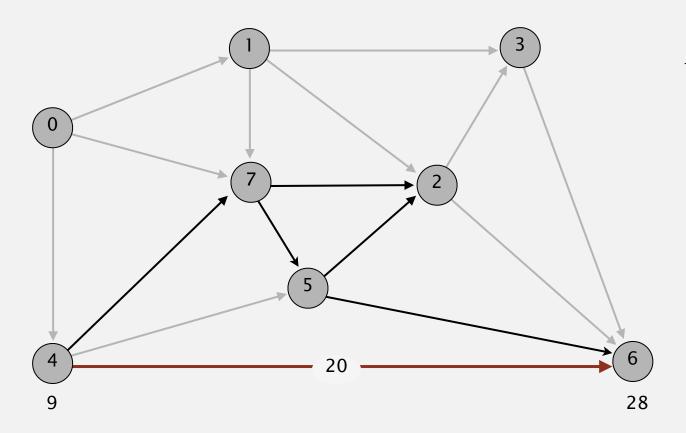
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	28.0	2→6
7	8.0	0→7

pass 0

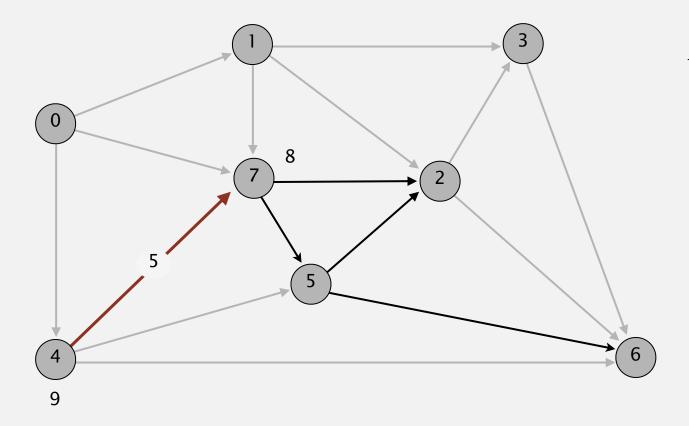
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	28.0	2→6
7	8.0	0→7

pass 0

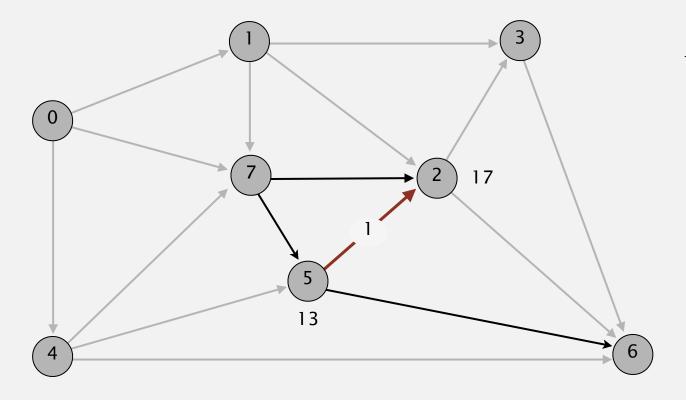
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	28.0	2→6
7	8.0	0→7

pass 0

Repeat V times: relax all E edges.

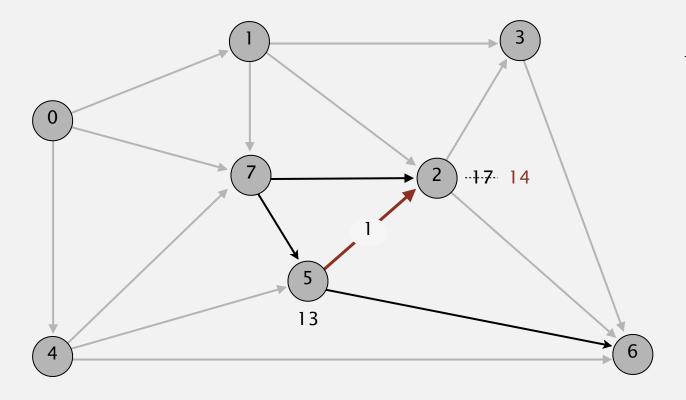


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	17.0	1→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	28.0	2→6
7	8.0	0→7

pass 0

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

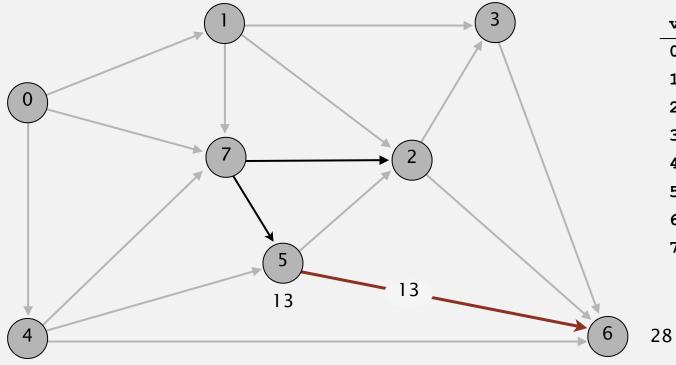


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	28.0	2→6
7	8.0	0→7

pass 0

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

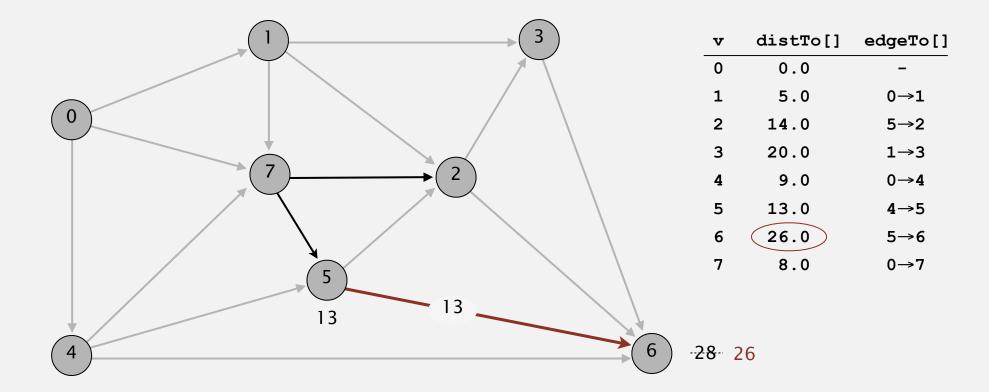


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	28.0	2→6
7	8.0	0→7

pass 0

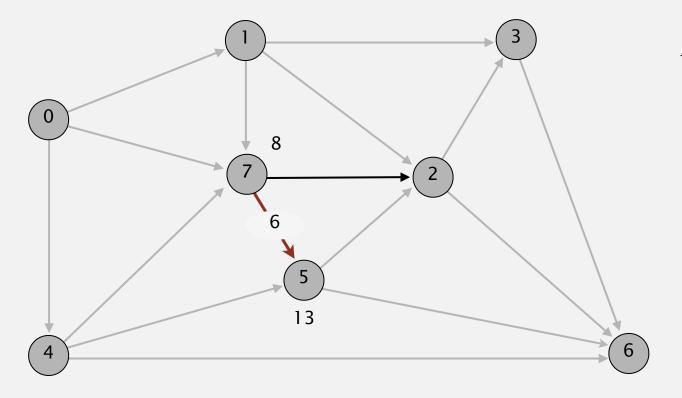
 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.



pass 0

Repeat V times: relax all E edges.

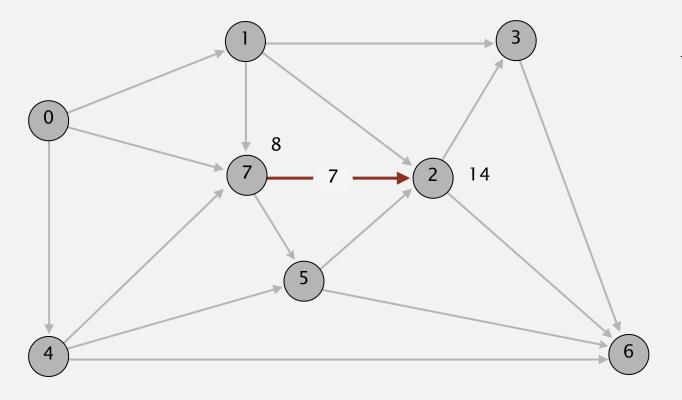


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 0

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

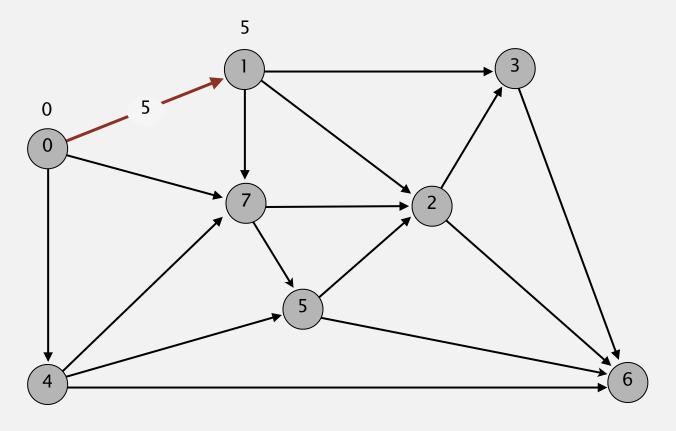


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 0

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

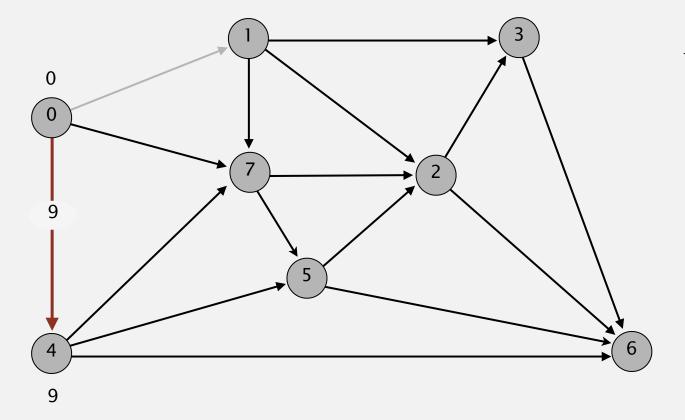
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

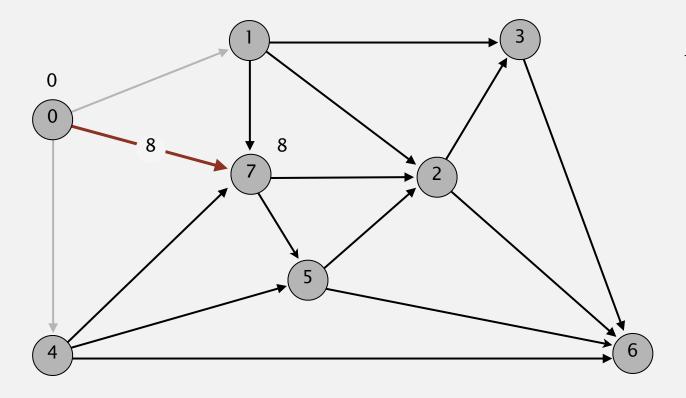
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

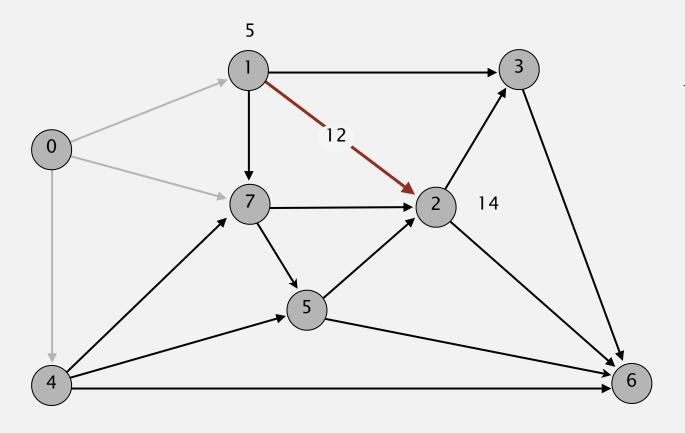
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

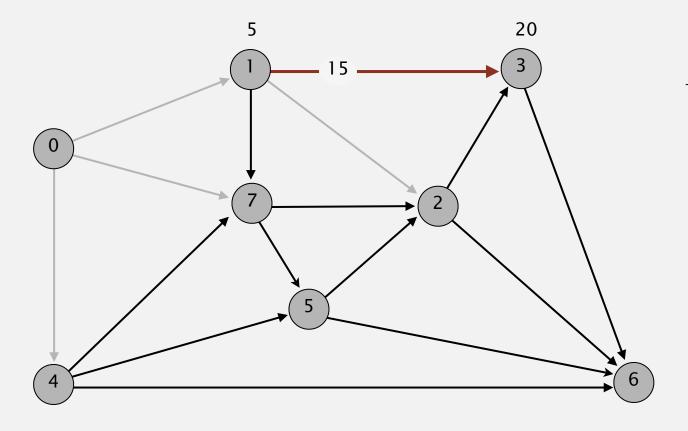
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

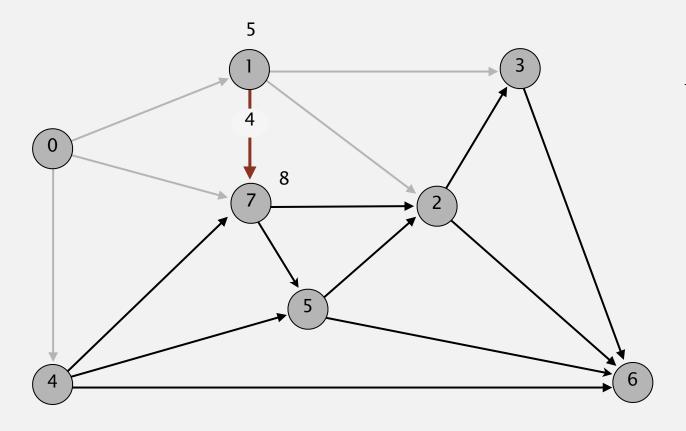
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

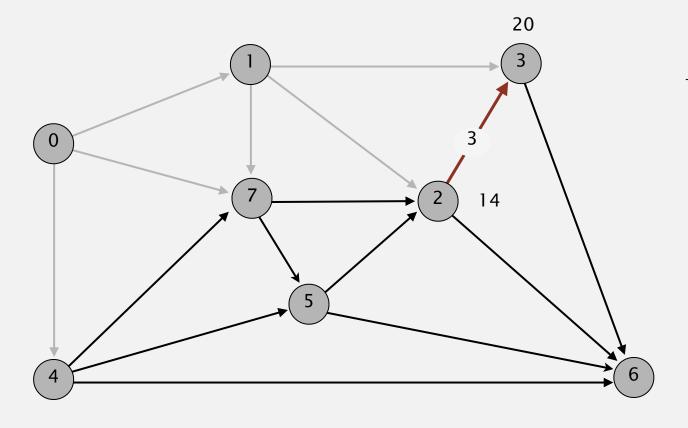
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

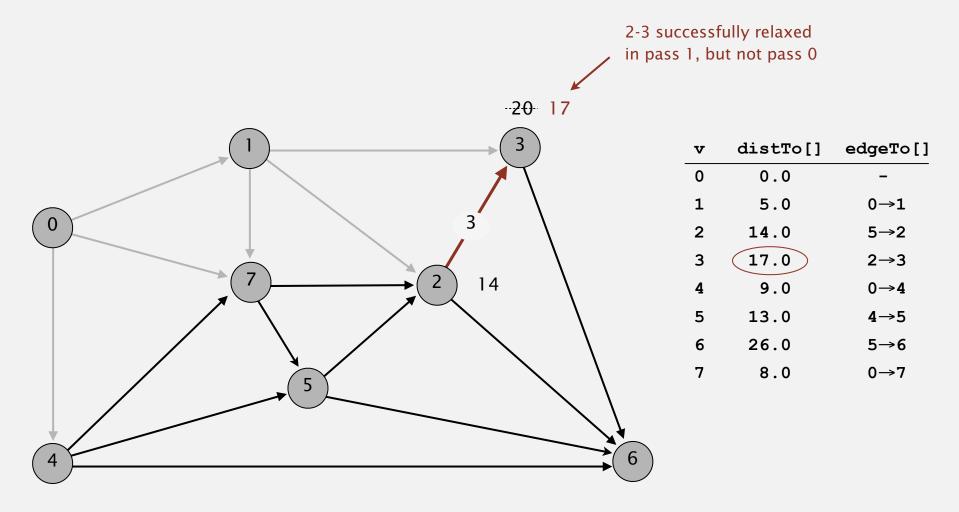
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	20.0	1→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

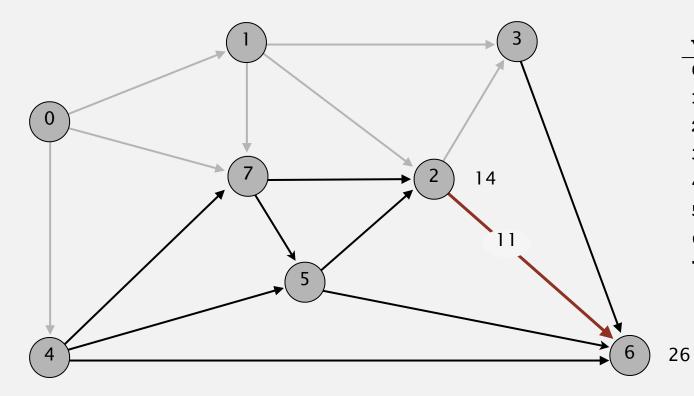
pass 1

Repeat V times: relax all E edges.



pass 1

Repeat V times: relax all E edges.

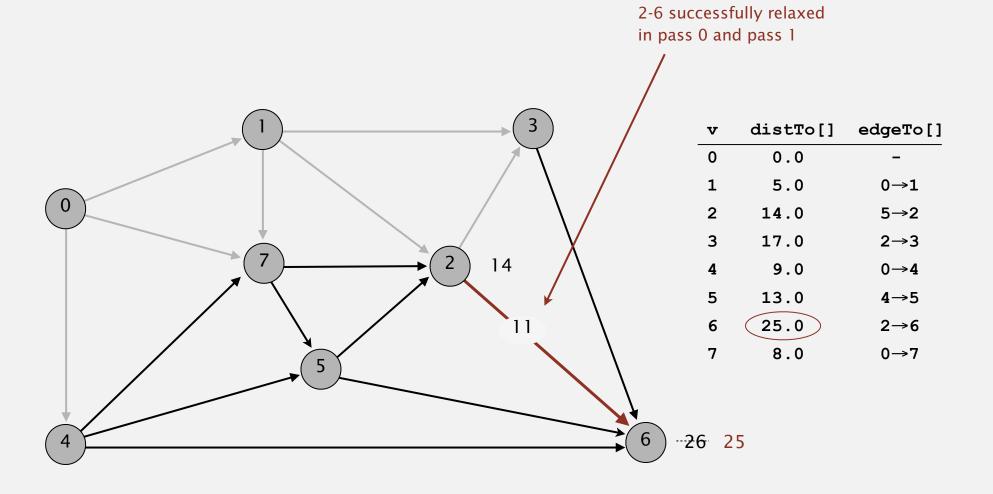


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	26.0	5→6
7	8.0	0→7

pass 1

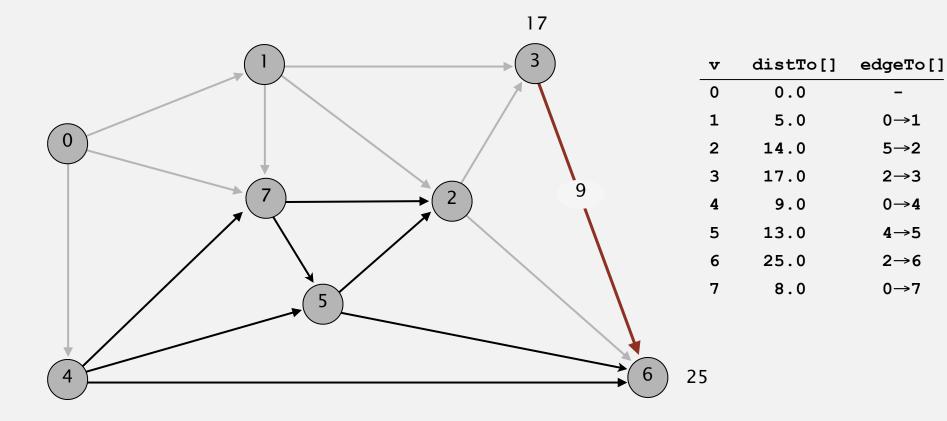
 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.



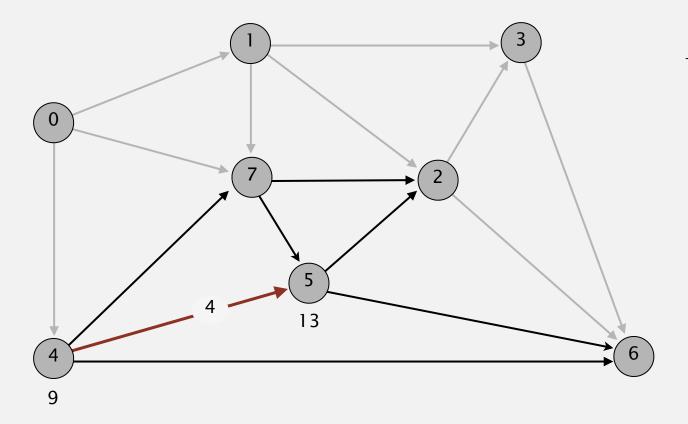
pass 1

Repeat V times: relax all E edges.



pass 1

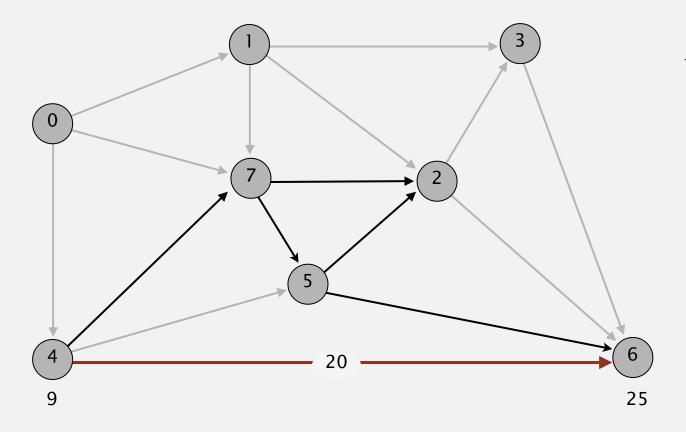
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

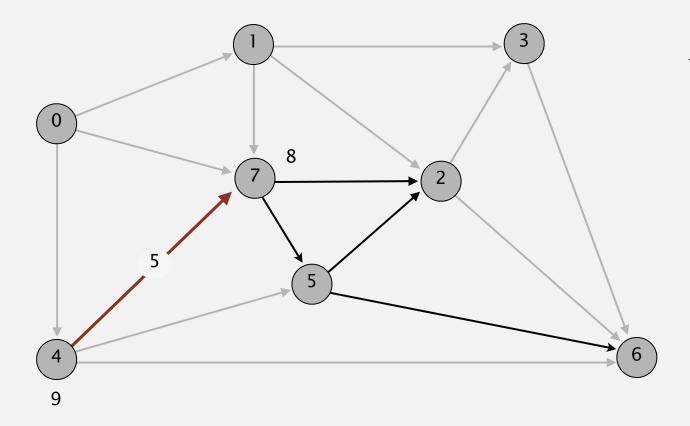
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

Repeat V times: relax all E edges.

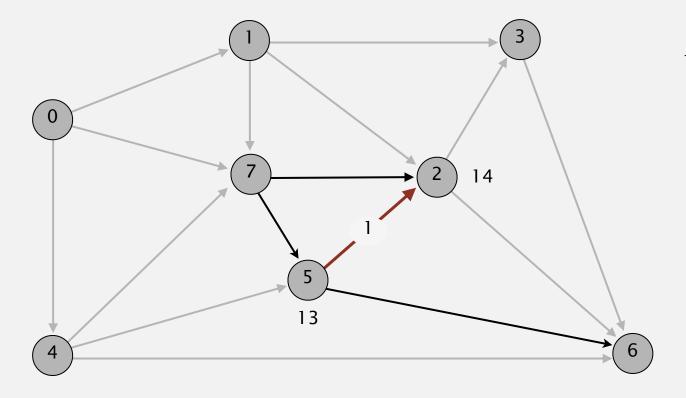


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

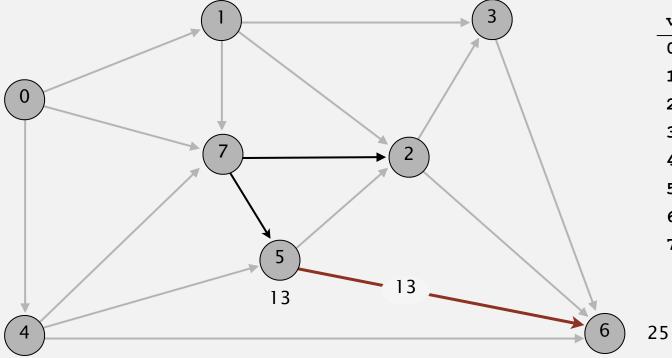


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

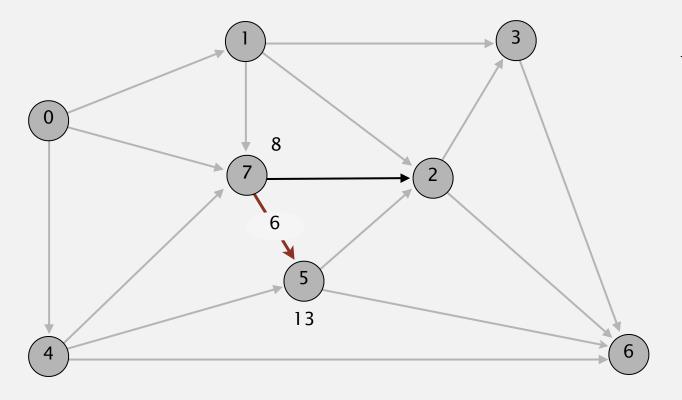


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

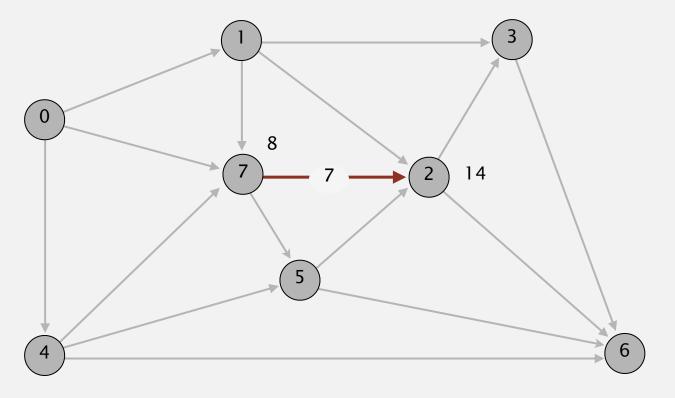


v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

Repeat V times: relax all E edges.

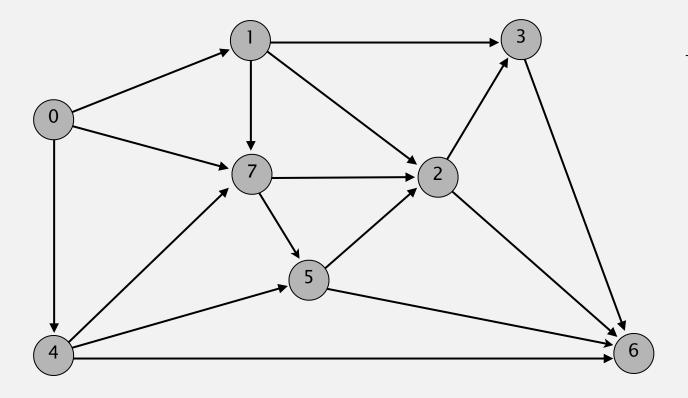


v	distTo[]	edgeTo[
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 1

 $0 \rightarrow 1 \quad 0 \rightarrow 4 \quad 0 \rightarrow 7 \quad 1 \rightarrow 2 \quad 1 \rightarrow 3 \quad 1 \rightarrow 7 \quad 2 \rightarrow 3 \quad 2 \rightarrow 6 \quad 3 \rightarrow 6 \quad 4 \rightarrow 5 \quad 4 \rightarrow 6 \quad 4 \rightarrow 7 \quad 5 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 5 \rightarrow 6 \quad 7 \rightarrow 5 \quad 7 \rightarrow 2 \quad 7 \rightarrow$

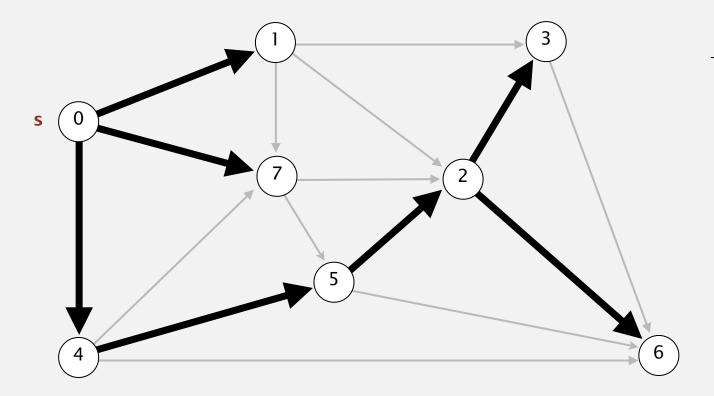
Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

pass 2, 3, 4, ... (no further changes)

Repeat V times: relax all E edges.



v	distTo[]	edgeTo[]
0	0.0	-
1	5.0	0→1
2	14.0	5→2
3	17.0	2→3
4	9.0	0→4
5	13.0	4→5
6	25.0	2→6
7	8.0	0→7

shortest-paths tree from vertex s