

Lecture 12

6.2 Volumes

Definition 1. A **cross section** of a solid S is the plane region formed by intersection S with a plane P .

Definition 2. Let S be a solid that lies between planes $x = a$ and $x = b$. If the cross-sectional area of S in the plane P_x through x and perpendicular to the x -axis is $A(x)$, where A is continuous function, then the **volume** of S is

$$V = \lim_{n \rightarrow \infty} \sum_{i=1}^n A(x_i^*) \Delta x_i = \int_a^b A(x) dx$$

Solid of Revolution

Definition 3. The solid obtained by rotating (revolving) a plane region about a line is called a **solid of revolution**.