

1. (1 point) You are given the four points in the plane $A = (4, 8)$, $B = (8, -5)$, $C = (10, 1)$, and $D = (13, -3)$. The graph of the function $f(x)$ consists of the three line segments AB , BC and CD . Find the integral $\int_4^{13} f(x) dx$ by interpreting the integral in terms of sums and/or differences of areas of elementary figures.

$$\int_4^{13} f(x) dx = \underline{\hspace{2cm}}$$

2. (1 point) Use the Midpoint Rule to approximate

$$\int_{-1.5}^{4.5} x^3 dx$$

with $n = 6$.

3. (1 point) Use the Midpoint Rule to approximate the integral

$$\int_2^{10} (5x + 7x^2) dx$$

with $n=3$.

4. (1 point) Consider the function $f(x) = \frac{x^2}{4} + 8$.

In this problem you will calculate $\int_0^4 \left(\frac{x^2}{4} + 8 \right) dx$ by using the definition

$$\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \left[\sum_{i=1}^n f(x_i) \Delta x \right]$$

The summation inside the brackets is R_n which is the Riemann sum where the sample points are chosen to be the right-hand endpoints of each sub-interval.

Calculate R_n for $f(x) = \frac{x^2}{4} + 8$ on the interval $[0, 4]$ and write your answer as a function of n without any summation signs. You will need the summation formulas on page 383 of your textbook (page 364 in older texts).

$$R_n = \underline{\hspace{2cm}}$$

$$\lim_{n \rightarrow \infty} R_n = \underline{\hspace{2cm}}$$

5. (1 point) Let $\int_5^{14} f(x) dx = 10$, $\int_5^8 f(x) dx = 7$, $\int_{11}^{14} f(x) dx = 3$.
Find $\int_8^{11} f(x) dx = \underline{\hspace{2cm}}$
and $\int_{11}^8 (10f(x) - 7) dx = \underline{\hspace{2cm}}$

6. (1 point) Use the Midpoint Rule to approximate

$$\int_{-1.5}^{4.5} x^3 dx$$

with $n = 6$.

7. (1 point) Use the Midpoint Rule to approximate the integral

$$\int_6^{13} (-10x - 8x^2) dx$$

with $n=3$.

8. (1 point)

(a) By reading values from the given graph of f , use five rectangles to find a lower estimate and an upper estimate for the area under the given graph of f from $x = 0$ to $x = 10$.

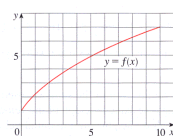
Lower estimate $\approx \underline{\hspace{2cm}}$

Upper estimate $\approx \underline{\hspace{2cm}}$

(b) Repeat part (a) with 10 rectangles in each case.

Lower estimate $\approx \underline{\hspace{2cm}}$

Upper estimate $\approx \underline{\hspace{2cm}}$



9. (1 point)

The speed of a runner increased steadily during the first three seconds of a race. Her speed at half-second intervals is given in the following table:

t (s)	0	0.5	1.0	1.5	2.0	2.5	3.0
v (ft/s)	0	6.2	10.8	14.9	18.1	19.4	20.2

Find lower and upper estimates for the distance (in feet) that she traveled during these three seconds.

Lower estimate = $\underline{\hspace{2cm}}$ feet

Upper estimate = $\underline{\hspace{2cm}}$ feet

10. (1 point)

Definition: The AREA A of the region S that lies under the graph of the continuous function f is the limit of the sum of the areas of approximating rectangles

$$A = \lim_{n \rightarrow \infty} R_n = \lim_{n \rightarrow \infty} [f(x_1)\Delta x + f(x_2)\Delta x + \dots + f(x_n)\Delta x]$$

Consider the function $f(x) = \frac{\ln(x)}{x}$, $3 \leq x \leq 10$. Using the above definition, determine which of the following expressions represents the area under the graph of f as a limit.

- A. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\ln(3 + \frac{7i}{n})}{3 + \frac{7i}{n}}$
- B. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{7 \ln(\frac{7i}{n})}{n \cdot \frac{7i}{n}}$
- C. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{7 \ln(3 + \frac{7i}{n})}{n \cdot 3 + \frac{7i}{n}}$
- D. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{10 \ln(\frac{10i}{n})}{n \cdot \frac{10i}{n}}$
- E. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{10 \ln(3 + \frac{10i}{n})}{n \cdot 3 + \frac{10i}{n}}$

11. (1 point)

Definition: The AREA A of the region S that lies under the graph of the continuous function f is the limit of the sum of the areas of approximating rectangles

$$A = \lim_{n \rightarrow \infty} R_n = \lim_{n \rightarrow \infty} [f(x_1)\Delta x + f(x_2)\Delta x + \dots + f(x_n)\Delta x]$$

Consider the function $f(x) = x \cos(x)$, $0 \leq x \leq \pi/2$. Using the above definition, determine which of the following expressions represents the area under the graph of f as a limit.

- A. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{\pi i}{2n} \cos \left(\frac{\pi i}{2n} \right) \right)$
- B. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi}{2n} \left(\frac{\pi i}{2n} \cos \left(\frac{\pi i}{2n} \right) \right)$
- C. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi}{2n} \left(\frac{\pi}{2n} \cos \left(\frac{\pi}{2n} \right) \right)$
- D. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi i}{2n} \left(\frac{\pi i}{2n} \cos \left(\frac{\pi i}{2n} \right) \right)$
- E. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi}{2n} \left(\cos \left(\frac{\pi i}{2n} \right) \right)$

12. (1 point)

Determine which of the following regions has an area equal to the given limit without evaluating the limit:

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{2}{n} \left(5 + \frac{2i}{n} \right)^{10}$$

- A. The area of the region under the graph of $y = x^5$ on the interval $[5, 7]$.
- B. The area of the region under the graph of $y = x^{10}$ on the interval $[2, 5]$.

- C. The area of the region under the graph of $y = x^5$ on the interval $[2, 5]$.
- D. The area of the region under the graph of $y = x^{10}$ on the interval $[5, 7]$.

13. (1 point)

Definition: The AREA A of the region S that lies under the graph of the continuous function f is the limit of the sum of the areas of approximating rectangles

$$A = \lim_{n \rightarrow \infty} R_n = \lim_{n \rightarrow \infty} [f(x_1)\Delta x + f(x_2)\Delta x + \dots + f(x_n)\Delta x]$$

(a) Use the above Definition to determine which of the following expressions represents the area under the graph of $f(x) = x^3$ from $x = 0$ to $x = 1$.

- A. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i}{n} \right)^3 \frac{5}{n}$
- B. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i}{n} \right) \frac{1}{n}$
- C. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i}{n} \right) \frac{5}{n}$
- D. $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i}{n} \right)^3 \frac{1}{n}$

(b) Evaluate the limit that is the correct answer to part (a). You may find the following formula for the sum of cubes helpful:

$$1^3 + 2^3 + 3^3 + \dots + n^3 = \sum_{i=1}^n i^3 = \left(\frac{n(n+1)}{2} \right)^2.$$

Value of limit = _____

14. (1 point) Estimate $\int_{-2}^2 4 - x^2 dx$ using left endpoints for $n = 4$ approximating rectangles.

$$\int_{-2}^2 4 - x^2 dx \text{ is approximately } \underline{\hspace{2cm}}$$

15. (1 point) Estimate $\int_{-2}^2 4 - x^2 dx$ using midpoints for $n = 4$ approximating rectangles.

$$\int_{-2}^2 4 - x^2 dx \text{ is approximately } \underline{\hspace{2cm}}$$

16. (1 point) Estimate $\int_0^4 x^2 dx$ using left endpoints for $n = 4$ approximating rectangles.

$$\int_0^4 x^2 dx \text{ is approximately } \underline{\hspace{2cm}}$$

17. (1 point) Find the numerical value of the sum below.

$$\sum_{j=2}^7 (3j - 2) = \underline{\hspace{2cm}}$$

18. (1 point) Find the numerical value of the sum below.

$$\sum_{i=3}^5 (i^2 - i) = \underline{\hspace{2cm}}$$

19. (1 point) Express the following sum in closed form.

$$\sum_{k=1}^n (2 + 2k)^2 = \underline{\hspace{2cm}}$$

Hint: Start by multiplying out $(2 + 2k)^2$.

Note: Your answer should be in terms of n .

20. (1 point) Evaluate the definite integral:

$$\int_1^{3.5} 2x^{-1} dx = \underline{\hspace{2cm}}$$

21. (1 point) Evaluate the definite integral:

$$\int_1^6 (5 - 3x^{-3}) dx = \underline{\hspace{2cm}}$$

22. (1 point) If $f(x) = \int_x^{x^2} t^2 dt$

then

$$f'(x) = \underline{\hspace{2cm}}$$

$$f'(-2) = \underline{\hspace{2cm}}$$

23. (1 point) Given

$$f(x) = \int_0^x \frac{t^2 - 36}{1 + \cos^2(t)} dt$$

At what value of x does the local max of $f(x)$ occur?

$$x = \underline{\hspace{2cm}}$$

24. (1 point) Use the Fundamental Theorem of Calculus to evaluate the definite integral.

$$\int_{-4}^4 x^2 - 2x - 5 dx = \underline{\hspace{2cm}}$$

25. (1 point) Use the Fundamental Theorem of Calculus to find the derivative of

$$F(x) = \int_1^x \frac{1}{1+t^2} dt.$$

$$F'(x) = \underline{\hspace{2cm}}$$

26. (1 point) Use the Fundamental Theorem of Calculus to carry out the following differentiation:

$$\frac{d}{dx} \int_1^{\sqrt{x}} t^t dt = \underline{\hspace{2cm}}.$$

27. (1 point) Calculate the following antiderivatives:

(a) $\int (9t - 6t^9 - 8) dt = \underline{\hspace{2cm}} + C.$

(b) $\int \left(\frac{1}{u^{9/4}} + 5\sqrt{u} \right) du = \underline{\hspace{2cm}} + C.$

(c) $\int \left(\frac{1}{7x^3} \right) dx = \underline{\hspace{2cm}} + C.$

28. (1 point)

Evaluate the integral

$$\int_0^9 \sqrt{4t} dt$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

29. (1 point)

Evaluate the integral

$$\int_1^9 \frac{-6x - 4}{\sqrt{x}} dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

30. (1 point)

Evaluate the integral

$$\int_0^{\pi/4} \frac{-7 - 7\cos^2(x)}{\cos^2(x)} dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

31. (1 point)

Evaluate the integral

$$\int_4^9 \left(2\sqrt{x} + \frac{1}{\sqrt{x}} \right)^2 dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

32. (1 point) Calculate the following antiderivatives:

(a) $\int x^3 dx = \underline{\hspace{2cm}} + C.$

(b) $\int x^{4/7} dx = \underline{\hspace{2cm}} + C.$

(c) $\int x^{-6} \sqrt{x} dx = \underline{\hspace{2cm}} + C.$

33. (1 point) Calculate the following antiderivatives:

(a) $\int \frac{9}{x} dx = \underline{\hspace{2cm}} + C.$

(b) $\int -6\sin x + 6\cos x dx = \underline{\hspace{2cm}} + C.$

(c) $\int -10e^x dx = \underline{\hspace{2cm}} + C.$

34. (1 point) Evaluate the indefinite integral.

$$\int \frac{5}{5x^8} + \frac{5x^8}{5} dx = \underline{\hspace{2cm}} + C.$$

35. (1 point) Evaluate the indefinite integral.

$$\int 6\sec^2 x - 5e^x dx = \underline{\hspace{2cm}} + C.$$

36. (1 point) Use the Fundamental Theorem of Calculus to evaluate the definite integral.

$$\int_{-1}^1 x^2 - x + 1 \, dx = \underline{\hspace{2cm}}$$

37. (1 point) Use the Fundamental Theorem of Calculus to evaluate the definite integral.

$$\int_1^4 -x(x^5 + 3) \, dx = \underline{\hspace{2cm}}$$

38. (1 point) Use the Fundamental Theorem of Calculus to evaluate the definite integral.

$$\int_2^3 \frac{3}{x^4} \, dx = \underline{\hspace{2cm}}$$

39. (1 point) Use the Fundamental Theorem of Calculus to find the derivative of

$$F(x) = \int_4^x t^4 \, dt.$$

Then evaluate the derivative at $x = -5$.

1. $F'(x) = \underline{\hspace{2cm}}$
2. $F'(-5) = \underline{\hspace{2cm}}$

40. (1 point) Use the Fundamental Theorem of Calculus to find the derivative of

$$F(x) = \int_1^x \frac{1}{1+t^5} \, dt.$$

$$F'(x) = \underline{\hspace{2cm}}$$

41. (1 point) Use the Fundamental Theorem of Calculus to find the derivative of

$$F(x) = \int_x^2 \sin(t^4) \, dt.$$

$$F'(x) = \underline{\hspace{2cm}}$$

42. (1 point) Use the Fundamental Theorem of Calculus to find the derivative of

$$F(x) = \int_{-2}^{\sin x} \cos(t^2) + t \, dt.$$

$$F'(x) = \underline{\hspace{2cm}}$$

43. (1 point)

Find the derivative of $f(x) = x \sin(x) + \cos(x) + C$ to complete the following integration formula:

$$\int \underline{\hspace{2cm}} \, dx = x \sin(x) + \cos(x) + C$$

44. (1 point)

Find the derivative of $f(x) = -\frac{\sqrt{x^2+a^2}}{a^2x} + C$ to complete the following integration formula:

$$\int \underline{\hspace{2cm}} \, dx = -\frac{\sqrt{x^2+a^2}}{a^2x} + C$$

45. (1 point)

Using an upper-case "C" for any arbitrary constants, find the general indefinite integral

$$\int 10x^{-3/4} \, dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

46. (1 point)

Using an upper-case "C" for any arbitrary constants, find the general indefinite integral

$$\int (-9x^3 + 9x - 2) \, dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

47. (1 point)

Using an upper-case "C" for any arbitrary constants, find the general indefinite integral

$$\int (3 - \sqrt{x})^2 \, dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

48. (1 point)

Using an upper-case "C" for any arbitrary constants, find the general indefinite integral

$$\int -8x\sqrt{x} \, dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

49. (1 point)

Using an upper-case "C" for any arbitrary constants, find the general indefinite integral

$$\int (-7\cos(x) - 9\sin(x)) \, dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

50. (1 point)

Evaluate the integral

$$\int_{-1}^0 (10x + 6e^x) \, dx$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

51. (1 point)

Evaluate the integral

$$\int_1^4 \sqrt{t}(-10+t) \, dt$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

52. (1 point)

Evaluate the integral

$$\int_1^2 \frac{-3y - 7y^7}{y^3} \, dy$$

$$\text{Integral} = \underline{\hspace{2cm}}$$

53. (1 point)

Evaluate the following integral by making the given substitution:

$$\int x^2 \sqrt{x^3 + 6} dx, \quad u = x^3 + 6$$

Note: Any arbitrary constants used must be an upper-case "C".

54. (1 point)

Evaluate the following integral by making the given substitution:

$$\int \frac{-3 \sin(\sqrt{x})}{\sqrt{x}} dx, \quad u = \sqrt{x}$$

Note: Any arbitrary constants used must be an upper-case "C".

55. (1 point)

Evaluate the indefinite integral

$$\int 5x(x^2 + 3)^4 dx$$

Note: Any arbitrary constants used must be an upper-case "C".

56. (1 point)

Evaluate the indefinite integral

$$\int -5(2 - x)^6 dx$$

Note: Any arbitrary constants used must be an upper-case "C".

57. (1 point)

Evaluate the indefinite integral

$$\int \frac{10x}{(x^2 + 1)^2} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

58. (1 point)

Evaluate the indefinite integral

$$\int 4 \sec(2x) \tan(2x) dx$$

Note: Any arbitrary constants used must be an upper-case "C".

59. (1 point)

Evaluate the indefinite integral

$$\int \frac{-7(\ln(x))^2}{x} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

60. (1 point)

Evaluate the indefinite integral

$$\int \frac{-9 \cos(\sqrt{t})}{\sqrt{t}} dt$$

Note: Any arbitrary constants used must be an upper-case "C".

61. (1 point)

Evaluate the indefinite integral

$$\int 5 \cos(x) \sin^6(x) dx$$

Note: Any arbitrary constants used must be an upper-case "C".

62. (1 point)

Evaluate the indefinite integral

$$\int e^x \sqrt{5 + e^x} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

63. (1 point)

Evaluate the indefinite integral

$$\int \frac{8}{x \ln(x)} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

64. (1 point)

Evaluate the indefinite integral

$$\int \frac{-8e^x}{e^x + 1} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

65. (1 point)

Evaluate the indefinite integral

$$\int \frac{5 \cos(\pi/x)}{x^2} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

66. (1 point)

Evaluate the indefinite integral

$$\int 8 \sqrt[3]{x^3 + 1} x^5 dx$$

Note: Any arbitrary constants used must be an upper-case "C".

67. (1 point)

Evaluate the indefinite integral

$$\int \frac{2x}{1+x^4} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

68. (1 point)

Evaluate the indefinite integral

$$\int \frac{-6x^2}{\sqrt{1-x}} dx$$

Note: Any arbitrary constants used must be an upper-case "C".

69. (1 point)

Evaluate the definite integral (if it exists)

$$\int_0^4 \frac{3x}{\sqrt{1+2x}} dx$$

If the integral does not exist, type "DNE".

70. (1 point) Sketch the region enclosed by $y = e^{2x}$, $y = e^{4x}$ and $x = 1$.

Decide whether to integrate with respect to x or y , and then find the area of the region.

The area is _____.

71. (1 point) Sketch the region enclosed by $x + y^2 = 30$ and $x + y = 0$.

Decide whether to integrate with respect to x or y , and then find the area of the region.

The area is _____.

72. (1 point) Evaluate the indefinite integral.

$$\int e^{6x} \sin(7x) dx = \text{_____} + C.$$

73. (1 point) Evaluate the definite integral.

$$\int_0^1 x^2 \sqrt[4]{e^x} dx = \text{_____}$$

74. (1 point) Evaluate the definite integral.

$$\int_1^6 \sqrt{t} \ln(t) dt = \text{_____}$$

75. (1 point) **Integration by Parts:** This is the most important integration technique we've discussed in this class. It has a wide range of applications beyond increasing our list of integration rules.

$$\int z^3 \ln z dz = \text{_____}.$$

$$\int e^t \cos t dt = \text{_____}.$$

$$\int_0^{2\pi} \sin(x) \sin(x+1) dx = \text{_____}.$$

76. (1 point) Sketch the region enclosed by the given curves and decide whether to integrate with respect to x or y . Find the area of the region bounded by $2y = 4\sqrt{x}$, $y = 5$ and $2y + 2x = 6$.

Answer: _____

77. (1 point) Sketch the region enclosed by the given curves and decide whether to integrate with respect to x or y . Find the area of the region bounded by $y = 4x^2$ and $y = x^2 + 3$

Answer: _____

78. (1 point) Find total area enclosed by the graphs of $y = 9x^2 - x^3 + x$ and $y = x^2 + 16x$.

Answer: _____

79. (1 point) Use integration by parts to evaluate the integral.

$$\int x e^{2x} dx$$

Answer: _____ + C

80. (1 point) Use integration by parts to evaluate the integral.

$$\int 2x \cos(4x) dx$$

Answer: _____ + C

81. (1 point) Use integration by parts to evaluate the definite integral.

$$\int_1^7 \sqrt{t} \ln t dt$$

Answer: _____

82. (1 point) Evaluate the definite integral.

$$\int_2^7 \ln x^{33} dx$$

Answer: _____

83. (1 point) Evaluate the indefinite integral.

$$\int x \sin^2(8x) dx$$

84. (1 point) Evaluate the indefinite integral.

$$\int \ln(x^2 + 17x + 70) dx$$

85. (1 point)
Evaluate the integral

$$\int_{\pi/2}^{3\pi/4} 4 \sin^5(x) \cos^3(x) dx$$

86. (1 point)
Evaluate the integral

$$\int 1 \sin^3(mx) dx$$

Note: Use an upper-case "C" for the constant of integration.

87. (1 point)
Evaluate the integral

$$\int_0^{\pi/2} -3 \cos^2(x) dx$$

88. (1 point)
Evaluate the integral

$$\int_0^{\pi} -9 \cos^6(x) dx$$

89. (1 point)
Evaluate the integral

$$\int_0^{\pi/2} 9 \sin^2(x) \cos^2(x) dx$$

90. (1 point)
Evaluate the integral

$$\int_0^{\pi/2} -4 \sec^4(t/2) dt$$

91. (1 point)
Evaluate the integral

$$\int -1 \tan^4(x) dx$$

Note: Use an upper-case "C" for the constant of integration.

92. (1 point)
Evaluate the integral

$$\int 7 \csc(x) dx$$

Note: Use an upper-case "C" for the constant of integration. Also, use $1/\tan(x)$ for $\cot(x)$, and use $1/\sin(x)$ for $\csc(x)$.

93. (1 point)
Evaluate the integral

$$\int -9 \sin(5x) \sin(2x) dx$$

Note: Use an upper-case "C" for the constant of integration.

94. (1 point)
Evaluate the integral

$$\int 9 \sin(3x) \cos(x) dx$$

Note: Use an upper-case "C" for the constant of integration.

95. (1 point)
Evaluate the integral

$$\int 9 \cos(7x) \cos(5x) dx$$

Note: Use an upper-case "C" for the constant of integration.

96. (1 point)
Evaluate the integral

$$\int \frac{-7(1 - \tan^2(x))}{\sec^2(x)} dx$$

Note: Use an upper-case "C" for the constant of integration.

97. (1 point)
Evaluate the integral

$$\int 10 \sin^5(x) dx$$

Note: Use an upper-case "C" for the constant of integration.

98. (1 point)
Evaluate the integral

$$\int 1 \sin^4(x) \cos^4(x) dx$$

Note: Use an upper-case "C" for the constant of integration.

99. (1 point)
Evaluate the integral using the indicated trigonometric substitution.

$$\int -7x^3 \sqrt{9 - x^2} dx, \quad x = 3 \sin(\theta)$$

Note: Use an upper-case "C" for the constant of integration.

100. (1 point)

Evaluate the integral

$$\int_0^{2\sqrt{3}} \frac{3x^3}{\sqrt{16-x^2}} dx$$

101. (1 point)

Evaluate the integral

$$\int \frac{-3}{x^2\sqrt{25-x^2}} dx$$

Note: Use an upper-case "C" for the constant of integration.

102. (1 point)

Evaluate the integral

$$\int 7\sqrt{1-4x^2} dx$$

Note: Use an upper-case "C" for the constant of integration.

103. (1 point)

Evaluate the integral

$$\int \frac{-4}{x^2\sqrt{16x^2-9}} dx$$

Note: Use an upper-case "C" for the constant of integration.

104. (1 point)

Evaluate the integral

$$\int_0^1 9\sqrt{x^2+1} dx$$

105. (1 point)

Evaluate the integral

$$\int -7\sqrt{5+4x-x^2} dx$$

Note: Use an upper-case "C" for the constant of integration.

106. (1 point)

Evaluate the integral

$$\int \frac{-3}{(5-4x-x^2)^{5/2}} dx$$

Note: Use an upper-case "C" for the constant of integration.

107. (1 point)

Evaluate the integral

$$\int_0^{\pi/2} \frac{9\cos t}{\sqrt{1+\sin^2(t)}} dt$$

108. (1 point) Find the average value of $f(x) = \frac{3}{x^3} + 2x$ on the interval $[1, 2]$.

Average value = _____

109. (1 point) Find the mean value of the function $f(x) = |8-x|$ on the closed interval $[5, 11]$.
mean value = _____

110. (1 point) A solid lies between two parallel planes 4 feet apart and has a volume of 43 cubic feet. What is the average area of cross-sections of the solid by planes that lie between the given ones?

111. (1 point) Find the average value of : $f(x) = 7\sin x + 3\cos x$ on the interval $[0, 17\pi/6]$

Average value = _____

112. (1 point) One fine day in Rochester the low temperature occurs at 5 a.m.
and the high temperature at 5 p.m. The temperature varies sinusoidally all day.

The temperature t hours after midnight is

$$T(t) = A + B\sin\left(\frac{\pi(t-C)}{12}\right)$$

where A , B , and C are certain constants.

The low temperature is 28 and the high temperature is 36.
Find the average temperature during the first 8 hours after noon.
Hint: The high and low temperatures can be used together to find A and B . Determine C from the fact that it is hottest at 5 p.m.

113. (1 point)

(a) Find the average value of the function $f(x) = 1(x-3)^2$ on the interval $[2, 5]$.

$f_{ave} =$ _____

(b) Find two values of c such that $f_{ave} = f(c)$. List these values in increasing order.

Smaller value of $c =$ _____

Larger value of $c =$ _____

114. (1 point)

(a) Find the average value of the function $f(x) = 2\sin(x) - \sin(2x)$ on the interval $[0, \pi]$.

$f_{ave} =$ _____

(b) Use a calculator, computer, or the graph of f to find two values of c such that $f_{ave} = f(c)$. List these values in increasing order. Make sure your answers are correct to three decimal places.

Smaller value of $c =$ _____

Larger value of $c =$ _____

115. (1 point)

(a) Find the average value of the function $f(x) = \frac{2x}{(1+x^2)^2}$ on the interval $[0, 2]$.

$f_{ave} =$ _____

(b) Use a calculator, computer, or the graph of f to find two values of c such that $f_{ave} = f(c)$. List these values in increasing order. Make sure your answers are correct to three decimal places.

Smaller value of $c =$ _____

Larger value of $c =$ _____

116. (1 point)

Find the average value of the function $f(x) = 10x^2$ on the interval $[-1, 1]$.

$f_{ave} =$ _____

117. (1 point)

Find the average value of the function $f(x) = -10/x$ on the interval $[1, 4]$.

$f_{ave} =$ _____

118. (1 point)

Find the average value of the function $g(x) = 9\cos(x)$ on the interval $[0, \pi/2]$.

$g_{ave} =$ _____

119. (1 point)

Find the average value of the function $g(x) = -1x^2\sqrt{1+x^3}$ on the interval $[0, 2]$.

$g_{ave} =$ _____

120. (1 point)

Find the average value of the function $f(t) = 1te^{-t^2}$ on the interval $[0, 5]$.

$f_{ave} =$ _____

121. (1 point)

Find the average value of the function $f(t) = 4\sec(t)\tan(t)$ on the interval $[0, \pi/4]$.

$f_{ave} =$ _____

122. (1 point)

Find the average value of the function $h(r) = -6/(1+r)^2$ on the interval $[1, 6]$.

$h_{ave} =$ _____

123. (1 point)

Which of the following is the correct form of the partial fraction decomposition of $\frac{x-1}{x^3+x}$?

- A. $\frac{A}{x} + \frac{B}{x^2+1}$
- B. $\frac{Ax+B}{x} + \frac{C}{x^2+1}$
- C. $\frac{Ax+B}{x} + \frac{Cx+D}{x^2+1}$
- D. $\frac{A}{x} + \frac{Bx+C}{x^2+1}$

124. (1 point)

Which of the following is the correct form of the partial fraction decomposition of $\frac{x^4}{x^4-1}$?

- A. $-1 + \frac{A}{x+1} + \frac{B}{x-1} + \frac{Cx+D}{x^2+1}$
- B. $1 + \frac{A}{x+1} + \frac{B}{x-1} + \frac{C}{x^2+1}$
- C. $-1 + \frac{A}{x+1} + \frac{B}{x-1} + \frac{C}{x^2+1}$
- D. $1 + \frac{A}{x+1} + \frac{B}{x-1} + \frac{Cx+D}{x^2+1}$

125. (1 point)

Evaluate the integral

$$\int \frac{2r^2}{r+4} dr$$

Note: Use an upper-case "C" for the constant of integration.

126. (1 point)

Evaluate the integral

$$\int \frac{-8}{(t+4)(t-1)} dt$$

Note: Use an upper-case "C" for the constant of integration.

127. (1 point)

Evaluate the integral

$$\int_0^1 \frac{5x-5}{x^2+3x+2} dx$$

128. (1 point)

Evaluate the integral

$$\int \frac{9x^2}{(x-3)(x+2)^2} dx$$

Note: Use an upper-case "C" for the constant of integration.

129. (1 point)

Evaluate the integral

$$\int \frac{-3x^2}{(x+1)^3} dx$$

Note: Use an upper-case "C" for the constant of integration.

130. (1 point)

Evaluate the integral

$$\int \frac{5}{(x-1)(x^2+9)} dx$$

Note: Use an upper-case "C" for the constant of integration.

131. (1 point)

Evaluate the integral

$$\int \frac{-5x-20}{x^2+2x+5} dx$$

Note: Use an upper-case "C" for the constant of integration.

132. (1 point)

Evaluate the integral

$$\int \frac{8}{x^4 - x^2} dx$$

Note: Use an upper-case "C" for the constant of integration.

133. (1 point)

Make a substitution to express the integrand as a rational function and then evaluate the integral

$$\int \frac{-1 \cos(x)}{\sin^2(x) + \sin(x)} dx$$

Note: Use an upper-case "C" for the constant of integration.

134. (1 point)

Use integration by parts and the technique of partial fractions to evaluate the integral

$$\int 7x \arctan(x) dx$$

Note: Use an upper-case "C" for the constant of integration.

135. (1 point)

Let S be the solid obtained by rotating the region bounded by the curves $y = x(x-1)^2$ and $y = 0$ about the y-axis. If you sketch the given region, you'll see that it can be awkward to find the volume V of S by slicing (the disk/washer method). Use cylindrical shells to find V.

Volume = _____

136. (1 point)

Use the method of cylindrical shells to find the volume of the solid obtained by rotating the region bounded by the curves $y = x^3$, $y = 8$, and $x = 0$ about the x-axis.

Volume = _____

137. (1 point)

Use the method of cylindrical shells to find the volume of the solid obtained by rotating the region bounded by the curves $y = 4x^2$ and $2x + y = 6$ about the x-axis.

Volume = _____

138. (1 point)

The region bounded by $x = 1 - y^4$ and $x = 0$ is rotated about the line $x = 2$. Find the volume of the resulting solid by any method.

Volume = _____

139. (1 point)

Using disks or washers, find the volume of the solid obtained by rotating the region bounded by the curves $y = x$ and $y = \sqrt{x}$ about the line $y = 1$.

Volume = _____

140. (1 point)

Using disks or washers, find the volume of the solid obtained by rotating the region bounded by the curves $y = x$ and $y = \sqrt{x}$ about the line $x = 2$.

Volume = _____

141. (1 point)

Which of the following integrals represents the volume of the solid obtained by rotating the region bounded by the curves $y = \tan^3(x)$, $y = 1$, and $x = 0$ about the line $y = 1$?

- A. $\pi \int_0^1 (\tan^3(x))^2 dx$
- B. $\pi \int_0^1 \tan^5(x) dx$
- C. $\pi \int_0^{\pi/4} (\tan^3(x))^2 dx$
- D. $\pi \int_0^{\pi/4} \tan^5(x) dx$
- E. $\pi \int_0^1 (1 - \tan^3(x))^2 dx$
- F. $\pi \int_0^{\pi/4} (1 - \tan^3(x))^2 dx$

142. (1 point)

Which of the following integrals represents the volume of the solid obtained by rotating the region bounded by the curves $y = \sin(x)$ and $y = 0$, with $0 \leq x \leq \pi$ about the line $y = -2$?

- A. $\pi \int_0^\pi [\sin(x) - 2]^2 dx$
- B. $\pi \int_{-2}^0 [\sin(x) - 2]^2 dx$
- C. $\pi \int_{-2}^0 [(\sin(x) + 2)^2 - (2)^2] dx$
- D. $\pi \int_{-2}^0 [\sin^2(x) + 2^2 - 2^2] dx$
- E. $\pi \int_0^\pi [(\sin(x) + 2)^2 - (2)^2] dx$
- F. $\pi \int_0^\pi [\sin^2(x) + 2^2 - 2^2] dx$

143. (1 point)

Use the method of cylindrical shells to find the volume of the solid obtained by rotating the region bounded by the curves $y = 4x - x^2$ and $y = 8x - 2x^2$ about the line $x = -2$.

Volume = _____

144. (1 point)

Call an improper definite integral type 1 if it is improper because the interval of integration is infinite.

Call it type 2 if it is improper because the function takes on an infinite value within the interval of integration.

Classify the type(s) for each of the following improper integrals.

- ☐ 1. $\int_0^1 \frac{1}{2x-1} dx$
- ☐ 2. $\int_{-\infty}^\infty \frac{\sin(x)}{1+x^2} dx$
- ☐ 3. $\int_1^2 \ln(x-1) dx$
- ☐ 4. $\int_1^2 \frac{1}{2x-1} dx$

145. (1 point)

Consider the integral

$$\int_1^\infty \frac{-8}{(3x+1)^2} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

146. (1 point)

Consider the integral

$$\int_{-\infty}^0 \frac{3}{2x-5} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

147. (1 point)

Consider the integral

$$\int_{-\infty}^{-1} \frac{-10}{\sqrt{2-w}} dw$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

148. (1 point)

Consider the integral

$$\int_4^\infty 1e^{-y/2} dy$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

149. (1 point)

Consider the integral

$$\int_{-\infty}^\infty -4xe^{-x^2} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

150. (1 point)

Consider the integral

$$\int_{-\infty}^\infty 4x^2 e^{-x^3} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

151. (1 point)

Consider the integral

$$\int_{2\pi}^\infty 3 \sin(\theta) d\theta$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

152. (1 point)

Consider the integral

$$\int_1^\infty \frac{-3x-3}{x^2+2x} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

153. (1 point)

Consider the integral

$$\int_0^\infty -1se^{-5s} ds$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

154. (1 point)

Consider the integral

$$\int_1^{\infty} \frac{10 \ln(x)}{x} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

155. (1 point)

Consider the integral

$$\int_1^{\infty} \frac{-10 \ln(x)}{x^3} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

156. (1 point)

Consider the integral

$$\int_0^3 \frac{3}{x\sqrt{x}} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

157. (1 point)

Consider the integral

$$\int_{-2}^3 \frac{-4}{x^4} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

158. (1 point)

Consider the integral

$$\int_0^{33} 7(x-1)^{-1/5} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

159. (1 point)

Consider the integral

$$\int_{-1}^1 \frac{6e^x}{e^x - 1} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

160. (1 point)

Consider the integral

$$\int_0^2 10z^2 \ln(z) dz$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

161. (1 point)

Determine whether the sequence $a_n = \frac{13n+6}{7n+11}$ converges or diverges. If it converges, find the limit.

Converges (y/n): _____

Limit (if it exists, blank otherwise): _____

162. (1 point) Find the first six terms of the recursively defined sequence

$$s_n = 5s_{n-1} + 1 \quad \text{for } n > 1, \quad \text{and } s_1 = 1.$$

first six terms = _____

(Enter your answer as a comma-separated list.)

163. (1 point) Determine whether the sequence is divergent or convergent. If it is convergent, evaluate its limit. If it diverges to infinity, state your answer as INF. If it diverges to negative infinity, state your answer as MINF. If it diverges without being infinity or negative infinity, state your answer as DIV.

$$\lim_{n \rightarrow \infty} \frac{6(n!)}{(6)^n}$$

164. (1 point) Find the limit of the sequence whose terms are given by

$$a_n = (n^2)(1 - \cos(\frac{5.1}{n})).$$

165. (1 point)

Compute the sum

$$\sum_{i=1}^{75} (2i-1) = \underline{\hspace{2cm}}.$$

166. (1 point) Consider the sequence

$$a_n = \frac{\ln(1/n)}{\sqrt{2n}}.$$

Write the first five terms of a_n , and find $\lim_{n \rightarrow \infty} a_n$. If the sequence diverges, enter "divergent" in the answer box for its limit.

a) First five terms: _____, _____, _____, _____, _____.

b) $\lim_{n \rightarrow \infty} a_n = \underline{\hspace{2cm}}.$

167. (1 point) Suppose

$$a_1 = 2, a_{n+1} = \frac{1}{2} \left(a_n + \frac{2}{a_n} \right).$$

Find $\lim_{n \rightarrow \infty} a_n =$ _____.

Hint: Let $a = \lim_{n \rightarrow \infty}$. Then, since $a_{n+1} = \frac{1}{2} \left(a_n + \frac{2}{a_n} \right)$, we have $a = \frac{1}{2} \left(a + \frac{2}{a} \right)$. Now solve for a .

168. (1 point) Consider the series:

$$\sum_{k=10}^{\infty} \left(\frac{3}{(k-1)^2} - \frac{3}{k^2} \right)$$

a) Determine whether the series is convergent or divergent:

_____.
(Enter "convergent" or "divergent" as appropriate.)

b) If it converges, find its sum: _____.

If the series diverges, enter here "divergent" again.

169. (1 point) For each sequence, find a formula for the general term, a_n . For example, answer n^2 if given the sequence $\{1, 4, 9, 16, 25, 36, \dots\}$

- ____1. $\frac{1}{2}, \frac{1}{4}, \frac{1}{6}, \frac{1}{8}, \dots$
____2. $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \dots$

170. (1 point) Determine whether the sequence is divergent or convergent. If it is convergent, evaluate its limit.

(If it diverges to infinity, state your answer as inf . If it diverges to negative infinity, state your answer as $-inf$. If it diverges without being infinity or negative infinity, state your answer as div .)

$$\lim_{n \rightarrow \infty} \frac{12(5^n) + 12}{13(5^n)}$$

Answer: _____

171. (1 point) Determine whether the sequence is divergent or convergent. If it is convergent, evaluate its limit.

(If it diverges to infinity, state your answer as inf . If it diverges to negative infinity, state your answer as $-inf$. If it diverges without being infinity or negative infinity, state your answer as div .)

$$\lim_{n \rightarrow \infty} (-1)^n \sin(12/n)$$

Answer: _____

172. (1 point) Determine the sum of the following series.

$$\sum_{n=1}^{\infty} \frac{(-2)^{n-1}}{7^n}$$

Answer: _____

173. (1 point) Determine whether the series is convergent or divergent. If convergent, find the sum; if divergent, enter div .

$$\sum_{n=1}^{\infty} \ln \frac{n}{n+1}$$

Answer: _____

174. (1 point) Find the values of x for which the series below converges.

$$\sum_{n=1}^{\infty} x^n 3^n$$

Answer: $|x| < \underline{\hspace{1cm}}$

175. (1 point) If a sequence c_1, c_2, c_3, \dots has limit K then the sequence $e^{c_1}, e^{c_2}, e^{c_3}, \dots$ has limit e^K . Use this fact together with l'Hopital's rule to compute the limit of the sequence given by $b_n = (1 + \frac{5.2}{n})^n$.

176. (1 point) Determine whether the sequence is divergent or convergent. If it is convergent, evaluate its limit. If it diverges to infinity, state your answer as "INF" (without the quotation marks). If it diverges to negative infinity, state your answer as "MINF". If it diverges without being infinity or negative infinity, state your answer as "DIV".

$$\lim_{n \rightarrow \infty} \frac{n^n}{e^{-4n}}$$

177. (1 point) For the following series, if it converges, enter the limit of convergence. If not, enter "DIV" (unquoted).

$$\sum_{n=1}^{\infty} \ln(2(n+1)) - \ln(2n)$$

178. (1 point)

Use the Comparison Theorem to determine whether the following integral is convergent or divergent.

$$\boxed{?} 1. \int_1^{\infty} \frac{7 \cos^2(x)}{1+x^2} dx$$

179. (1 point)

Use the Comparison Theorem to determine whether the following integral is convergent or divergent.

☐ 1. $\int_1^{\infty} \frac{8x}{\sqrt{1+x^6}} dx$

180. (1 point) (a) Compute s_5 (the 5th partial sum) of

$$s = \sum_{n=1}^{\infty} \frac{3}{3n^5}$$

(b) Estimate the error in using s_5 as an approximation of the sum of the series. (i.e. use $\int_5^{\infty} f(x) dx \geq R_5$)

(c) Use $n = 5$ and

$$s_n + \int_{n+1}^{\infty} f(x) dx \leq s \leq s_n + \int_n^{\infty} f(x) dx$$

to find a better estimate of the sum.

$$\leq s \leq$$

181. (1 point) Find the value of

$$\int_2^{\infty} \frac{dx}{(3x-2)^2}$$

Determine whether

$$\sum_{n=2}^{\infty} \left(\frac{1}{(3n-2)^2} \right)$$

Enter A if series is convergent, B if series is divergent. ____

182. (1 point) Determine the convergence or divergence of the following series.

$$\sum_{n=1}^{\infty} \frac{3^k + k}{k!}$$

- A. convergent
- B. divergent

183. (1 point) Determine the sum of the following series.

$$\sum_{n=1}^{\infty} \frac{(-4)^{n-1}}{5^n}$$

Answer: _____

184. (1 point) Determine whether the series is convergent or divergent. If convergent, find the sum; if divergent, enter *div*.

$$\sum_{n=1}^{\infty} \ln \frac{n}{n+1}$$

Answer: _____

185. (1 point) Find the values of x for which the series below converges.

$$\sum_{n=1}^{\infty} x^n 8^n$$

Answer: $|x| < \underline{\hspace{1cm}}$

186. (1 point) Compute the value of the following improper integral. If it converges, enter its value. Enter **infinity** if it diverges to ∞ , and **-infinity** if it diverges to $-\infty$. Otherwise, enter **diverges**.

$$\int_2^{\infty} \frac{dx}{3x(\ln(7x))^2} = \underline{\hspace{2cm}}$$

Does the series $\sum_{n=2}^{\infty} \frac{1}{3n(\ln(7n))^2}$ converge or diverge?

- ?
- converges
- diverges to +infinity
- diverges to -infinity
- diverges

187. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{7}{3+7^n}$$

Input C for convergence and D for divergence: ____

Note: You have only one chance to enter your answer.

188. (1 point) Determine whether the following series converges or diverges:

$$\sum_{n=1}^{\infty} \frac{6}{\sqrt{n(n+4)(n+5)}}$$

Input C for convergence and D for divergence: ____

Note: You have only one chance to enter your answer.

189. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{n^9 + 6}{n^{10} + 8}$$

Input C for convergence and D for divergence: ____

Note: You have only one chance to enter your answer.

190. (1 point) Determine whether the following series converges or diverges:

$$\sum_{n=1}^{\infty} \frac{n}{\sqrt{n^5 + 4}}$$

Input C for convergence and D for divergence: ____

Note: You have only one chance to enter your answer.

191. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{4^n}{2+5^n}$$

Input C for convergence and D for divergence: ____

Note: You have only one chance to enter your answer.

192. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{5}{\sqrt{n}+6}$$

Input C for convergence and D for divergence: ____

Note: You have only one chance to enter your answer.

193. (1 point) Use the ratio test to determine whether $\sum_{n=18}^{\infty} \frac{n+9}{n!}$ converges or diverges.

(a) Find the ratio of successive terms. Write your answer as a fully simplified fraction. For $n \geq 18$,

$$\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = \lim_{n \rightarrow \infty} \underline{\hspace{2cm}}$$

(b) Evaluate the limit in the previous part. Enter ∞ as *infinity* and $-\infty$ as *-infinity*. If the limit does not exist, enter *DNE*.

$$\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = \underline{\hspace{2cm}}$$

(c) By the ratio test, does the series converge, diverge, or is the test inconclusive?

- Choose
- Converges
- Diverges
- Inconclusive

194. (1 point) (a) Use the comparison test to carefully determine if $\sum_{n=1}^{\infty} \frac{n+3^n}{n3^n-n}$ converges or diverges: this series

- A. converges
- B. diverges

(b) Use the ratio test to carefully determine if $\sum_{n=0}^{\infty} \frac{n^2+3}{3^n}$ converges or diverges: this series

- A. converges
- B. diverges

(c) Use the limit comparison test to carefully determine if $\sum_{n=1}^{\infty} \frac{3^n}{n3^n+n}$ converges or diverges: this series

- A. converges
- B. diverges

195. (1 point) For the following alternating series,

$$\sum_{n=1}^{\infty} a_n = 1 - \frac{(0.5)^2}{2!} + \frac{(0.5)^4}{4!} - \frac{(0.5)^6}{6!} + \frac{(0.5)^8}{8!} - \dots$$

how many terms do you have to go for your approximation (your partial sum) to be within 0.0000001 from the convergent value of that series?

196. (1 point) The three series $\sum A_n$, $\sum B_n$, and $\sum C_n$ have terms

$$A_n = \frac{1}{n^9}, \quad B_n = \frac{1}{n^2}, \quad C_n = \frac{1}{n}.$$

Use the Limit Comparison Test to compare the following series to any of the above series. For each of the series below, you must enter two letters. The first is the letter (A,B, or C) of the series above that it can be legally compared to with the Limit Comparison Test. The second is C if the given series converges, or D if it diverges. So for instance, if you believe the series converges and can be compared with series C above, you would enter CC; or if you believe it diverges and can be compared with series A, you would enter AD.

—1. $\sum_{n=1}^{\infty} \frac{6n^3 + n^2 - 6n}{8n^{12} - 7n^{11} + 7}$

—2. $\sum_{n=1}^{\infty} \frac{7n^2 + 6n^8}{2n^9 + 8n^3 - 2}$

—3. $\sum_{n=1}^{\infty} \frac{2n^2 + n^9}{1309n^{11} + 8n^2 + 7}$

197. (1 point) Consider the series $\sum_{n=1}^{\infty} a_n$ where

$$a_n = \frac{(n+4)!}{e^{n+1}\sqrt{n+6}}$$

In this problem you must attempt to use the Ratio Test to decide whether the series converges.

Compute

$$L = \lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right|$$

Enter the numerical value of the limit L if it converges, INF if it diverges to infinity, MINF if it diverges to negative infinity, or DIV if it diverges but not to infinity or negative infinity.

$L = \underline{\hspace{2cm}}$

Which of the following statements is true?

- A. The Ratio Test says that the series converges absolutely.
 - B. The Ratio Test says that the series diverges.
 - C. The Ratio Test says that the series converges conditionally.
 - D. The Ratio Test is inconclusive, but the series converges absolutely by another test or tests.
 - E. The Ratio Test is inconclusive, but the series diverges by another test or tests.
 - F. The Ratio Test is inconclusive, but the series converges conditionally by another test or tests.
- Enter the letter for your choice here: _____

198. (1 point) Determine the convergence or divergence of the following series.

$$\sum_{n=1}^{\infty} \frac{3^k + k}{k!}$$

- A. convergent
- B. divergent

199. (1 point) Determine whether the following series is

$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{1}{5n^{1.1}}$$

- A. conditionally convergent
- B. absolutely convergent
- C. divergent

200. (1 point) Determine whether the following series is

$$\sum_{n=2}^{\infty} (-1)^n \frac{1}{\sqrt{n^2 - 1}}$$

- A. conditionally convergent
- B. absolutely convergent
- C. divergent

201. (1 point) Match each of the following with the correct statement.

- A. The series is absolutely convergent.
- C. The series converges, but is not absolutely convergent.
- D. The series diverges.

- 1. $\sum_{n=1}^{\infty} \frac{(-1)^n 7^{n-1}}{(7)^{n+1} n^{\frac{1}{4}}}$
- 2. $\sum_{n=1}^{\infty} \frac{n^7}{4^n}$
- 3. $\sum_{n=1}^{\infty} \frac{(n+2)!}{9^n n!}$
- 4. $\sum_{n=1}^{\infty} (-1)^n \frac{n!}{5^n}$
- 5. $\sum_{n=1}^{\infty} \frac{(-1)^n}{4^n n!}$

202. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{2n^5 + 2}$$

Input C for convergence and D for divergence: _____

Note: You have only one chance to enter your answer.

203. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{\sqrt{n}}{n+6}$$

Input C for convergence and D for divergence: _____

Note: You have only one chance to enter your answer.

204. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} (-1)^n \frac{n}{8 + \ln n}$$

Input C for convergence and D for divergence: _____

Note: You have only one chance to enter your answer.

205. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} \frac{\cos(n\pi)}{n^{2/5}}$$

Input C for convergence and D for divergence: _____

Note: You have only one chance to enter your answer!

206. (1 point) Determine whether the following series converges or diverges.

$$\sum_{n=1}^{\infty} (-1)^n \sin\left(\frac{9}{n}\right)$$

Input C for convergence and D for divergence: _____

Note: You have only one chance to enter your answer.

207. (1 point) Determine whether the series is absolutely convergent, conditionally convergent, or divergent:

$$\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{n\sqrt{n}}$$

Input A for absolutely convergent, C for conditionally convergent, and D for divergent: _____

Note: You have only one chance to enter your answer.

208. (1 point) Determine whether the series is absolutely convergent, conditionally convergent, or divergent:

$$\sum_{n=1}^{\infty} \frac{(-9)^n}{n^9}$$

Input *A* for absolutely convergent, *C* for conditionally convergent, and *D* for divergent: ____

Note: You have only one chance to enter your answer.

209. (1 point) Test each of the following series for convergence by either the Comparison Test or the Limit Comparison Test. If at least one test can be applied to the series, enter CONV if it converges or DIV if it diverges. If neither test can be applied to the series, enter NA. (Note: this means that even if you know a given series converges by some other test, but the comparison tests cannot be applied to it, then you must enter NA rather than CONV.)

- ____ 1. $\sum_{n=1}^{\infty} \frac{(-1)^n}{4n}$
- ____ 2. $\sum_{n=1}^{\infty} \frac{(\ln(n))^2}{n+8}$
- ____ 3. $\sum_{n=1}^{\infty} \frac{4n^7 - n^4 + 5\sqrt{n}}{4n^9 - n^3 + 2}$
- ____ 4. $\sum_{n=1}^{\infty} \frac{\cos(n)\sqrt{n}}{5n+3}$
- ____ 5. $\sum_{n=1}^{\infty} \frac{5n^3}{n^7+3}$

210. (1 point) Select the FIRST correct reason why the given series converges.

- A. Convergent geometric series
- B. Convergent p series
- C. Comparison (or Limit Comparison) with a geometric or p series
- D. Cannot apply any test done so far in class

- ____ 1. $\sum_{n=1}^{\infty} \frac{\cos(n\pi)}{\ln(6n)}$
- ____ 2. $\sum_{n=1}^{\infty} \frac{(-1)^n \ln(e^n)}{n^4 \cos(n\pi)}$
- ____ 3. $\sum_{n=1}^{\infty} \frac{(n+1)(35)^n}{6^{2n}}$
- ____ 4. $\sum_{n=1}^{\infty} \frac{(-1)^n}{6n+5}$
- ____ 5. $\sum_{n=1}^{\infty} \frac{n^2 + \sqrt{n}}{n^4 - 9}$
- ____ 6. $\sum_{n=1}^{\infty} \frac{\sin^2(5n)}{n^2}$

211. (1 point) Select the FIRST correct reason why the given series converges.

- A. Convergent geometric series
- B. Convergent p series
- C. Comparison (or Limit Comparison) with a geometric or p series
- D. Alternating Series Test
- E. Cannot apply any test done so far in class

- ____ 1. $\sum_{n=1}^{\infty} (-1)^n \frac{\sqrt{n}}{n+6}$
- ____ 2. $\sum_{n=1}^{\infty} \frac{\sin^2(7n)}{n^2}$
- ____ 3. $\sum_{n=1}^{\infty} \frac{n^2 + \sqrt{n}}{n^4 - 6}$
- ____ 4. $\sum_{n=1}^{\infty} \frac{2(5)^n}{8^{2n}}$
- ____ 5. $\sum_{n=1}^{\infty} \frac{\cos(n\pi)}{\ln(5n)}$
- ____ 6. $\sum_{n=1}^{\infty} \frac{(-1)^n}{2n+5}$

212. (1 point) Match each of the following with the correct statement.

- A. The series is absolutely convergent.
- C. The series converges, but is not absolutely convergent.
- D. The series diverges.

- ____ 1. $\sum_{n=1}^{\infty} \frac{(-4)^n}{n^2}$
- ____ 2. $\sum_{n=1}^{\infty} \frac{(n+1)(5^2 - 1)^n}{5^{2n}}$
- ____ 3. $\sum_{n=1}^{\infty} (-1)^n \frac{\sqrt{n}}{n+8}$
- ____ 4. $\sum_{n=1}^{\infty} \frac{\sin(6n)}{n^2}$
- ____ 5. $\sum_{n=1}^{\infty} \frac{(-1)^n}{3n+7}$

213. (1 point)
Find the radius of convergence of the power series

$$\sum_{n=1}^{\infty} 10^n x^n n!$$

Your answer should be a nonnegative real number or the phrase "plus.infinity".

Radius of convergence is _____

214. (1 point)

Consider the function

$$\frac{1}{1-x^4}$$

Write a partial sum for the power series which represents this function consisting of the first 5 nonzero terms. For example, if the series were $\sum_{n=0}^{\infty} 3^n x^{2n}$, you would write $1 + 3x^2 + 3^2x^4 + 3^3x^6 + 3^4x^8$. Also indicate the radius of convergence.

Partial Sum: _____

Radius of Convergence: _____

215. (1 point)

Consider the function

$$\frac{1}{1+10^2x^2}$$

Write a partial sum for the power series which represents this function consisting of the first 5 nonzero terms. For example, if the series were $\sum_{n=0}^{\infty} 3^n x^{2n}$, you would write $1 + 3x^2 + 3^2x^4 + 3^3x^6 + 3^4x^8$. Also indicate the radius of convergence.

Partial Sum: _____

Radius of Convergence: _____

216. (1 point) Find the interval of convergence for the given power series.

$$\sum_{n=1}^{\infty} \frac{(x-5)^n}{n(-9)^n}$$

The series is convergent

from $x = \underline{\hspace{1cm}}$, left end included (Y,N): $\underline{\hspace{1cm}}$

to $x = \underline{\hspace{1cm}}$, right end included (Y,N): $\underline{\hspace{1cm}}$

217. (1 point) Match each of the Maclaurin series with right function.

—1. $\sum_{n=0}^{\infty} \frac{x^n}{n!}$

—2. $\sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!}$

—3. $\sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{(2n)!}$

—4. $\sum_{n=0}^{\infty} \frac{(-1)^n x^{2n+1}}{2n+1}$

A. $\arctan(x)$

B. $\cos(x)$

C. $\sin(x)$

D. e^x

218. (1 point) Find the interval of convergence for the given power series.

$$\sum_{n=1}^{\infty} \frac{n^6 (x+3)^n}{(8^n)(n^{\frac{20}{3}})}$$

The series is convergent:

from $x = \underline{\hspace{1cm}}$, left end included (Y,N): $\underline{\hspace{1cm}}$

to $x = \underline{\hspace{1cm}}$, right end included (Y,N): $\underline{\hspace{1cm}}$

219. (1 point) Compute the 10th derivative of

$$f(x) = \frac{\cos(4x^2) - 1}{x^2}$$

at $x = 0$.

$$f^{(10)}(0) = \underline{\hspace{2cm}}$$

Hint: Use the MacLaurin series for $f(x)$.

220. (1 point) Find all the values of x such that the given series would converge.

$$\sum_{n=1}^{\infty} \frac{(-1)^n x^n}{\sqrt{n+4}}$$

Answer: _____

Note: Give your answer in interval notation.

221. (1 point) Find all the values of x such that the given series would converge.

$$\sum_{n=1}^{\infty} \frac{x^n}{n!}$$

Answer: _____

Note: Give your answer in interval notation.

222. (1 point) Find all the values of x such that the given series would converge.

$$\sum_{n=1}^{\infty} \frac{8^n (x-6)^n}{n+6}$$

Answer: _____

Note: Give your answer in interval notation

223. (1 point) Find all the values of x such that the given series would converge.

$$\sum_{n=1}^{\infty} \frac{(3x-7)^n}{n^2}$$

Answer: _____

Note: Give your answer in interval notation

224. (1 point) Suppose that

$$\frac{5x}{x+6} = \sum_{n=0}^{\infty} c_n x^n.$$

Find the following coefficients.

$c_0 =$ _____

$c_1 =$ _____

$c_2 =$ _____

$c_3 =$ _____

$c_4 =$ _____

Find the radius of convergence R of the power series.

$R =$ _____

225. (1 point) Find the Maclaurin series of the function $f(x) = 1x^3 - 6x^2 - 8x + 6$.

$$f(x) = \sum_{n=0}^{\infty} c_n x^n$$

Determine the following coefficients:

$c_0 =$ _____

$c_1 =$ _____

$c_2 =$ _____

$c_3 =$ _____

$c_4 =$ _____

Find the radius of convergence: $R =$ _____

Note: Enter *inf* if the radius of coverage is infinity .

226. (1 point) The Taylor series for $f(x) = e^x$ at $a = 4$ is $\sum_{n=0}^{\infty} c_n (x-4)^n$.

Find the first few coefficients.

$c_0 =$ _____

$c_1 =$ _____

$c_2 =$ _____

$c_3 =$ _____

$c_4 =$ _____

227. (1 point) The Taylor series of function $f(x) = \ln(x)$ at $a = 7$ is given by:

$$f(x) = \sum_{n=0}^{\infty} c_n (x-7)^n$$

Find the following coefficients:

$c_0 =$ _____

$c_1 =$ _____

$c_2 =$ _____

$c_3 =$ _____

$c_4 =$ _____

Determine the interval of convergence: _____

Note: Give your answer in interval notation

228. (1 point) The Taylor series for $f(x) = \cos(x)$ at $a = \frac{\pi}{2}$ is $\sum_{n=0}^{\infty} c_n (x - \frac{\pi}{2})^n$.

Find the first few coefficients.

$c_0 =$ _____

$c_1 =$ _____

$c_2 =$ _____

$c_3 =$ _____

$c_4 =$ _____

229. (1 point) Find the Maclaurin series of the function $f(x) = (5x^2) \sin(6x)$.

$$f(x) = \sum_{n=0}^{\infty} c_n x^n$$

Compute the following coefficients:

$$c_3 = \underline{\hspace{2cm}}$$

$$c_4 = \underline{\hspace{2cm}}$$

$$c_5 = \underline{\hspace{2cm}}$$

$$c_6 = \underline{\hspace{2cm}}$$

$$c_7 = \underline{\hspace{2cm}}$$

230. (1 point) Let $F(x) = \int_0^x \sin(7t^2) dt$.

Find the MacLaurin polynomial of degree 7 for $F(x)$.

Answer: $\underline{\hspace{2cm}}$

Use this polynomial to estimate the value of $\int_0^{0.7} \sin(7x^2) dx$.

Answer: $\underline{\hspace{2cm}}$

231. (1 point) Let $F(x) = \int_0^x e^{-2t^4} dt$.

Find the MacLaurin polynomial of degree 5 for $F(x)$.

Answer: $\underline{\hspace{2cm}}$

Use this polynomial to estimate the value of $\int_0^{0.11} e^{-2x^4} dx$.

Answer: $\underline{\hspace{2cm}}$

232. (1 point) Evaluate

$$\lim_{x \rightarrow 0} \frac{\ln(1-x) + x + \frac{x^2}{2}}{12x^3}$$

Hint: Use power series.

Answer: $\underline{\hspace{2cm}}$

233. (1 point) Represent the function $\frac{7}{(1-8x)}$ as a power series

$$f(x) = \sum_{n=0}^{\infty} c_n x^n$$

$$c_0 = \underline{\hspace{2cm}}$$

$$c_1 = \underline{\hspace{2cm}}$$

$$c_2 = \underline{\hspace{2cm}}$$

$$c_3 = \underline{\hspace{2cm}}$$

$$c_4 = \underline{\hspace{2cm}}$$

Find the radius of convergence $R = \underline{\hspace{2cm}}$.

234. (1 point) Determine whether the series is convergent or divergent. If convergent, find the sum; if divergent, enter *div*.

$$\sum_{n=1}^{\infty} \frac{n}{n+12}$$

Answer: $\underline{\hspace{2cm}}$

235. (1 point) Determine whether the series is convergent or divergent. If convergent, find the sum; if divergent, enter *div*.

$$\sum_{n=1}^{\infty} \frac{n}{\sqrt{n^2+19}}$$

Answer: $\underline{\hspace{2cm}}$

236. (1 point) Find all the values of x such that the given series would converge.

$$\sum_{n=1}^{\infty} \frac{(3x)^n}{n^2}$$

Answer: $\underline{\hspace{2cm}}$

Note: Give your answer in interval notation.