

hw-3 (2023/09/26)

姓名:

学号:

p15: 11-(a) Show, using Proposition 1.14 and 1.17, that the statement form $((\neg(p \vee (\neg q))) \rightarrow (q \rightarrow r))$ is logically equivalent to each of the following.

(a) $((\neg(q \rightarrow p)) \rightarrow ((\neg q) \vee r))$

..... Recall that:

Proposition 1.14: If \mathcal{B}_1 is a statement form arising from the statement form \mathcal{A} by substituting the statement form \mathcal{B}_1 for one or more occurrences of the statement form \mathcal{A} in \mathcal{A}_1 , and if \mathcal{B} is logically equivalent to \mathcal{A} , then \mathcal{B}_1 is logically equivalent to \mathcal{A}_1 .

Proposition 1.17 (De Morgan's Laws): Let $\mathcal{A}_1, \mathcal{A}_2, \dots, \mathcal{A}_n$ be any statement forms. Then:

1. $(\bigvee_{i=1}^n (\neg \mathcal{A}_i))$ is logically equivalent to $(\neg(\bigwedge_{i=1}^n \mathcal{A}_i))$.
2. $(\bigwedge_{i=1}^n (\neg \mathcal{A}_i))$ is logically equivalent to $(\neg(\bigvee_{i=1}^n \mathcal{A}_i))$.

.....

Your answer: