

# Marketing And Sales Data Linear Regression

August 5, 2023

## 1 Marketing And Sales Data Linear Regression

### 1.1 Step 1: Imports

```
[1]: # Import relevant libraries and packages.  
import pandas as pd  
import seaborn as sns  
import matplotlib.pyplot as plt  
import statsmodels.api as sm  
from statsmodels.formula.api import ols
```

#### 1.1.1 Load the dataset

```
[2]: data = pd.read_csv('marketing_and_sales_data.csv')  
  
# Display the first five rows.  
data.head()
```

```
[2]:
```

	TV	Radio	Social_Media	Sales
0	16.0	6.566231	2.907983	54.732757
1	13.0	9.237765	2.409567	46.677897
2	41.0	15.886446	2.913410	150.177829
3	83.0	30.020028	6.922304	298.246340
4	15.0	8.437408	1.405998	56.594181

### 1.2 Step 2: Data exploration

```
[3]: # Display the shape of the data.  
data.shape
```

```
[3]: (4572, 4)
```

### 1.2.1 Explore the independent variables

```
[4]: # Generate descriptive statistics about independent variables.  
data[["TV", "Radio", "Social_Media"]].describe()
```

```
[4]:
```

	TV	Radio	Social_Media
count	4562.000000	4568.000000	4566.000000
mean	54.066857	18.160356	3.323956
std	26.125054	9.676958	2.212670
min	10.000000	0.000684	0.000031
25%	32.000000	10.525957	1.527849
50%	53.000000	17.859513	3.055565
75%	77.000000	25.649730	4.807558
max	100.000000	48.871161	13.981662

### 1.2.2 Explore the dependent variable

```
[5]: # Calculate the total number of missing values in the sales column.  
data["Sales"].isna().sum()
```

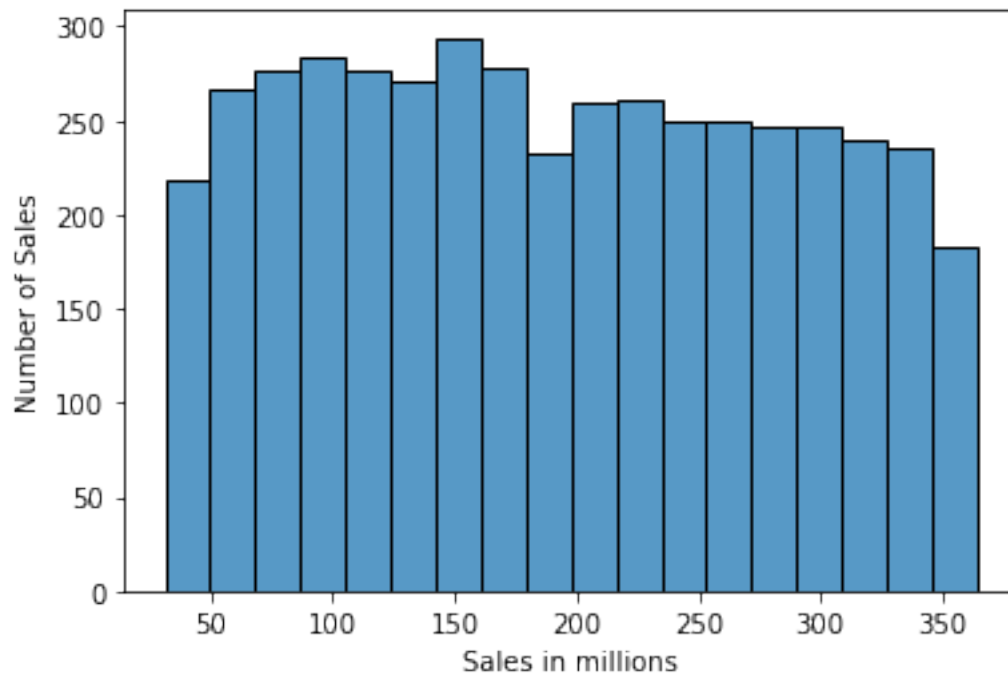
```
[5]: 6
```

### 1.2.3 Remove the missing data

```
[6]: # Subset the data to include rows where Sales is present.  
data.dropna(subset=["Sales"], axis=0, inplace=True)
```

### 1.2.4 Visualize the sales distribution

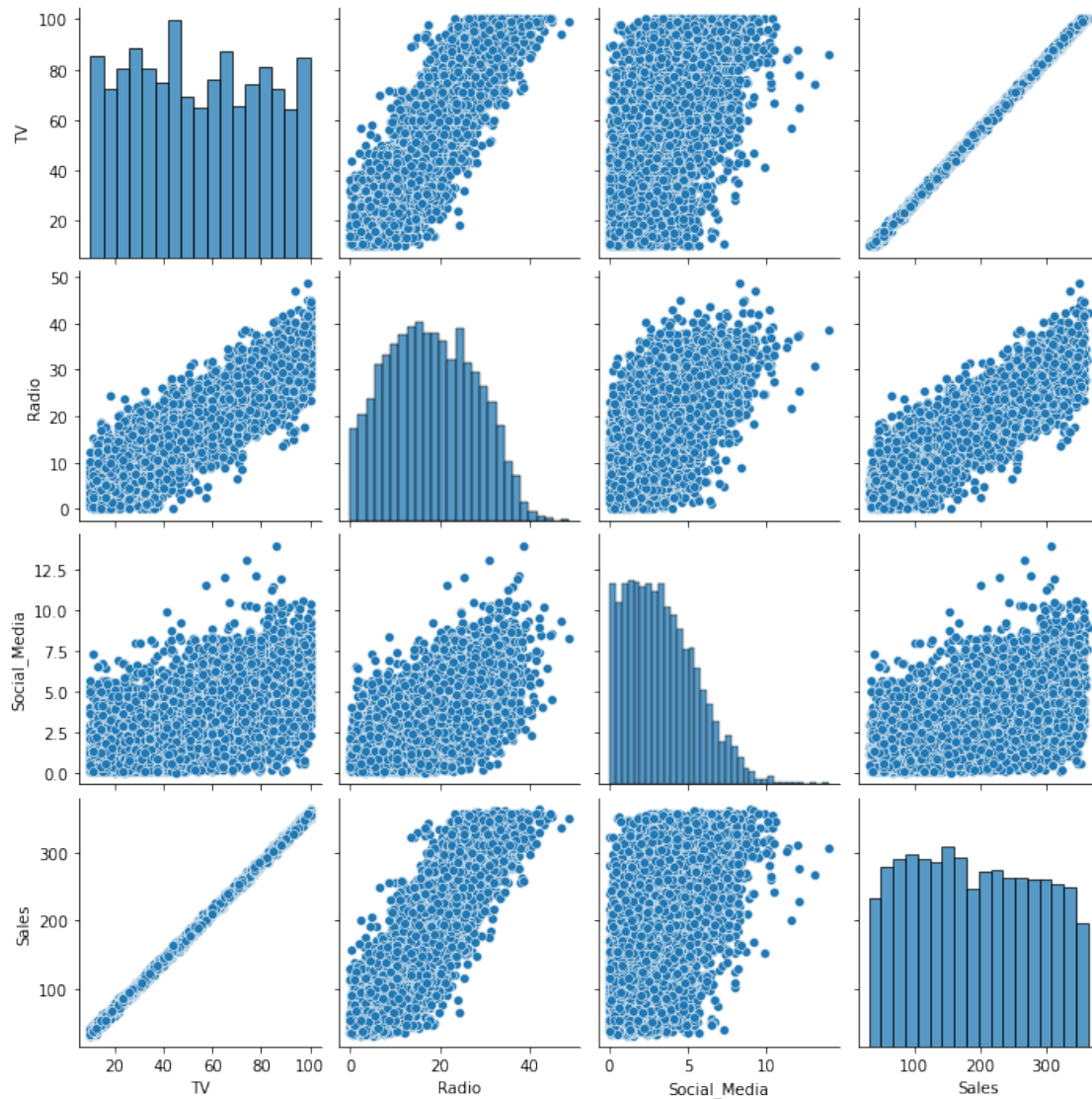
```
[7]: # Create a histogram of the Sales.  
fig=sns.histplot(data["Sales"])  
  
# Add a title  
fig.set_xlabel("Sales in millions")  
fig.set_ylabel("Number of Sales")  
plt.show()
```



### 1.3 Step 3: Model building

```
[8]: # Create a pairplot of the data.  
sns.pairplot(data)
```

```
[8]: <seaborn.axisgrid.PairGrid at 0x7f1bba294c50>
```



### 1.3.1 Build and fit the model

```
[9]: # Define the OLS formula.
ols_formula="Sales ~ TV"

# Create an OLS model.
OLS=ols(data=data, formula=ols_formula)

# Fit the model.
model=OLS.fit()

# Save the results summary.
```

```

model_result=model.summary()

# Display the model results.
model_result

```

```

[9]: <class 'statsmodels.iolib.summary.Summary'>
"""

```

```

                                OLS Regression Results
=====
Dep. Variable:                  Sales    R-squared:                  0.999
Model:                            OLS    Adj. R-squared:            0.999
Method:                 Least Squares    F-statistic:                4.527e+06
Date:                 Sat, 05 Aug 2023    Prob (F-statistic):          0.00
Time:                 14:58:58    Log-Likelihood:             -11393.
No. Observations:          4556    AIC:                        2.279e+04
Df Residuals:              4554    BIC:                        2.280e+04
Df Model:                   1
Covariance Type:            nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
Intercept	-0.1263	0.101	-1.257	0.209	-0.323	0.071
TV	3.5614	0.002	2127.776	0.000	3.558	3.565

```

=====
Omnibus:                 0.051    Durbin-Watson:              2.002
Prob(Omnibus):           0.975    Jarque-Bera (JB):           0.030
Skew:                   0.001    Prob(JB):                   0.985
Kurtosis:               3.012    Cond. No.                   138.
=====

```

Warnings:

```

[1] Standard Errors assume that the covariance matrix of the errors is correctly
specified.
"""

```

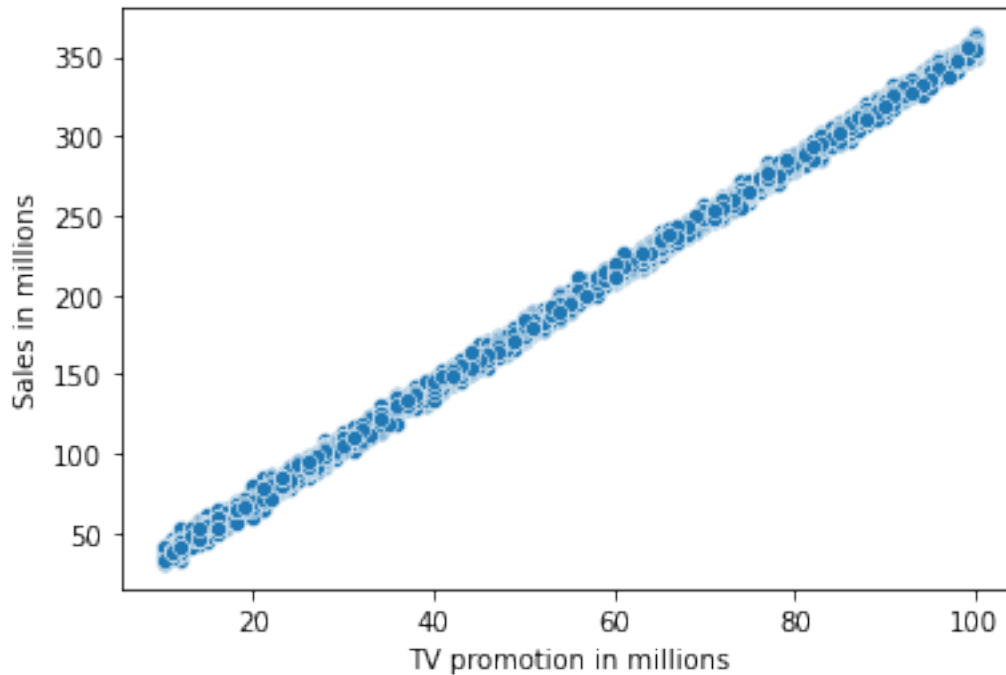
### 1.3.2 Check model assumptions

To justify using simple linear regression, we should check that the four linear regression assumptions are not violated.

These assumptions are: - Linearity requires a linear relationship between the independent and dependent variables. - Independent Observations states that each observation in the dataset is independent. - Normality states that the errors are normally distributed. - Homoscedasticity is that the residuals have a constant variance for all values of independent variables.

### 1.3.3 Model assumption: Linearity

```
[10]: # Create a scatterplot comparing X and Sales (Y).
fig=sns.scatterplot(x=data["TV"], y=data["Sales"])
fig.set_xlabel("TV promotion in millions")
fig.set_ylabel("Sales in millions")
plt.show()
```



### 1.3.4 Model assumption: Independence

As each marketing promotion (i.e., row) is independent from one another, the independence assumption is not violated.

### 1.3.5 Model assumption: Normality

```
[11]: # Calculate the residuals.
residuals= model.resid

# Create a 1x2 plot figures.
fig, axes = plt.subplots(1,2, figsize=(8,4))

# Create a histogram with the residuals.
sns.histplot(residuals, ax=axes[0])
```

```

# Set the x label of the residual plot.
axes[0].set_xlabel("Residuals")

# Set the title of the residual plot.
axes[0].set_title("The distribution of residuals")

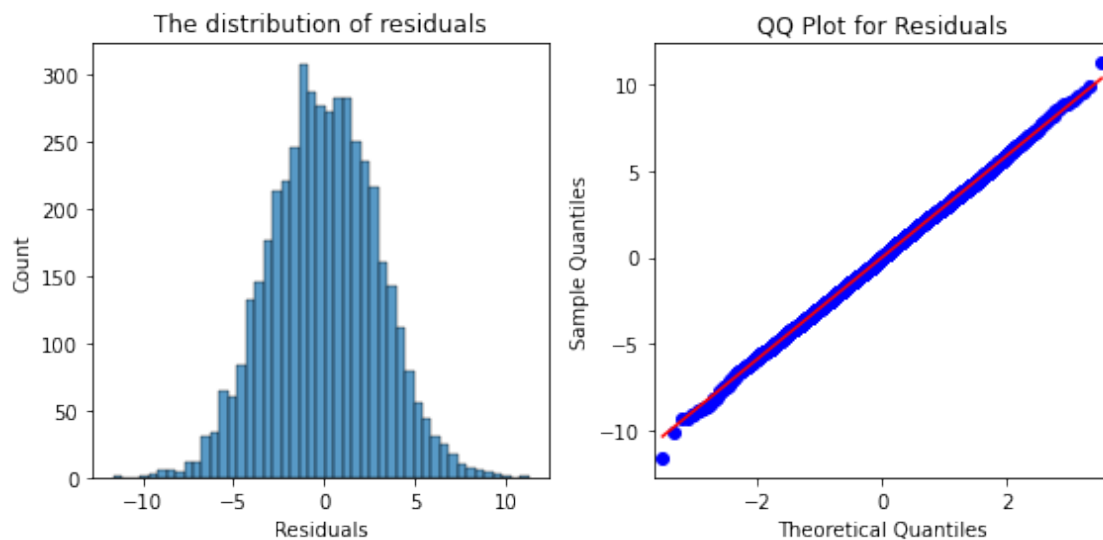
# Create a Q-Q plot of the residuals.
sm.qqplot(model.resid, line="s", ax=axes[1])

# Set the title of the Q-Q plot.
axes[1].set_title("QQ Plot for Residuals")

# Use tight_layout() function to add space between plots.
plt.tight_layout()

# Show the plot.
plt.show()

```



### 1.3.6 Model assumption: Homoscedasticity

```

[12]: # Create a scatterplot with the fitted values from the model and the residuals.
fitted_values=model.predict(data["TV"])
fig=sns.scatterplot(x=fitted_values, y=residuals)

# Set the x-axis label.
fig.set_xlabel("Fitted Values")

```

```

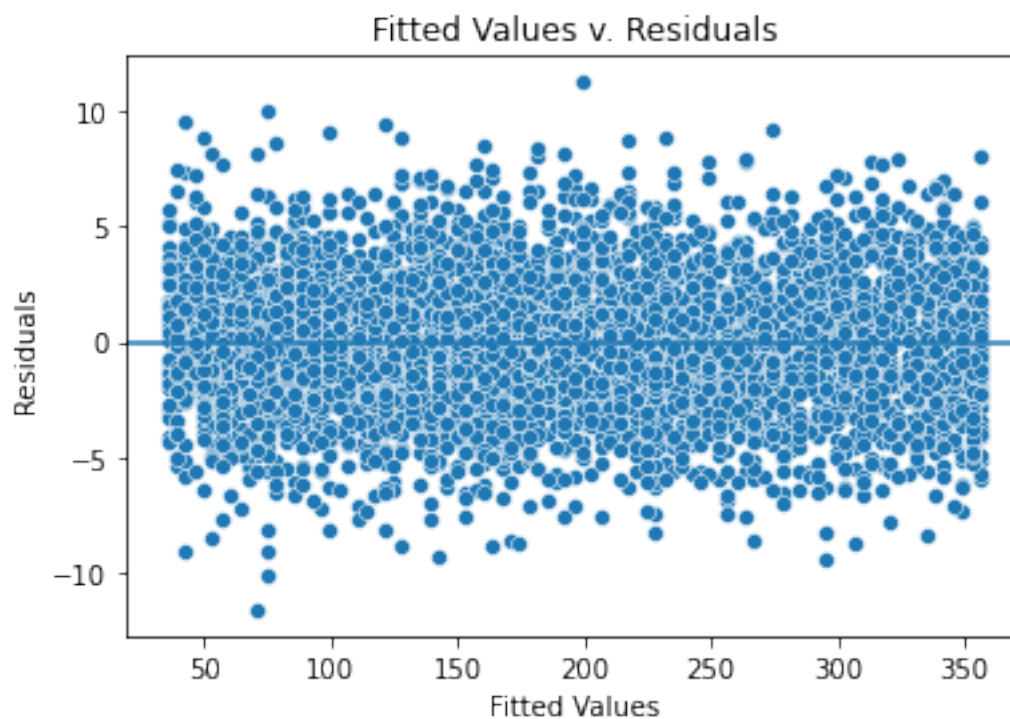
# Set the y-axis label.
fig.set_ylabel("Residuals")

# Set the title.
fig.set_title("Fitted Values v. Residuals")

# Add a line at y = 0 to visualize the variance of residuals above and below 0.
fig.axhline(0)

# Show the plot.
plt.show()

```



## 1.4 Step 4: Results and evaluation

### 1.4.1 Display the OLS regression results

```

[13]: # Display the model_results defined previously.
      model_result

```

```

[13]: <class 'statsmodels.iolib.summary.Summary'>
      """

```



```

=====
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Warnings:

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```

## 1.5 Conclusions

- Sales are evenly distributed between 25 and 350 million.
- TV has the strongest positive linear relationship with sales compared to radio and social media.
- The model has a high R-squared value of 0.999, indicating that 99.9% of the variation in sales can be explained by the TV promotional budget.
- The p-value for the TV coefficient is 0.0000, and the 95% confidence interval is [3.558, 3.565], indicating high confidence in the impact of TV on sales.
- The coefficients for Intercept and TV are -0.1263 and 3.5614, respectively, meaning an increase of one million dollars in the TV promotional budget leads to an estimated increase of 3.5614 million dollars in sales.
- Increasing the TV promotional budget should be prioritized to boost sales.