ARE 213 Problem Set 1b

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Import Data

1a - Misspecification bias

One source of misspecification bias would be omitted variables bias. The assumption that random assignment happens conditional on the observables does not protect us against non-random assignment of some unobservable covariate.

A second source of misspecification bias would be in the functional form assumption of linearity. It could be the case that smoking has some non-linear effect on the birthweight of a baby that we would not capture in the linear model we estimated. We would want to explore nonparametric regression to evaluate the sensitivity to this misspecification.

1b - Higher order specifications

We explored using a series estimator of the following functional form:

```
dat_drop$dmage2 <- dat_drop$dmage^2</pre>
dat_drop$cigar2 <- dat_drop$cigar^2</pre>
dat drop$cigar3 <- dat drop$cigar^3
dat_drop$cig_dmag <- dat_drop$cigar*dat_drop$dmage</pre>
lm.out <- lm(dbrwt ~ stresfip+dmage+ormoth+mrace3+dmeduc+dmar+adequacy+dfage+</pre>
               orfath+dfeduc+dtotord+monpre+nprevist+disllb+birmon+dgestat+csex+dplural+
               anemia+diabetes+herpes+chyper+
               preterm+tobacco_p+cigar+alcohol+dmage2+cigar2+cigar3+cig_dmag, data = dat_drop)
summary(lm.out)
##
## Call:
## lm(formula = dbrwt ~ stresfip + dmage + ormoth + mrace3 + dmeduc +
##
       dmar + adequacy + dfage + orfath + dfeduc + dtotord + monpre +
##
       nprevist + disllb + birmon + dgestat + csex + dplural + anemia +
##
       diabetes + herpes + chyper + preterm + tobacco_p + cigar +
##
       alcohol + dmage2 + cigar2 + cigar3 + cig_dmag, data = dat_drop)
```

```
##
## Residuals:
##
       Min
                1Q
                    Median
                                       Max
##
  -2845.5
           -296.1
                      -7.8
                             291.6
                                    2658.1
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -9.054e+02
                          8.280e+01 -10.935 < 2e-16 ***
  stresfip
                7.137e-01
                           6.324e-01
                                       1.128 0.259125
## dmage
                1.140e+01
                           2.205e+00
                                       5.169 2.35e-07 ***
## ormoth
               -1.982e+01
                           3.477e+00
                                      -5.701 1.19e-08 ***
## mrace3
                           2.348e+00 -33.565
                                              < 2e-16 ***
               -7.880e+01
## dmeduc
                3.787e+00
                           8.651e-01
                                       4.377 1.20e-05 ***
## dmar
               -3.539e+01
                           4.200e+00
                                      -8.427
                                              < 2e-16 ***
                                       1.815 0.069595 .
## adequacy
                7.465e+00
                           4.114e+00
## dfage
               -6.516e-03
                           3.379e-01
                                      -0.019 0.984616
## orfath
               -1.624e+01
                           3.425e+00
                                      -4.743 2.11e-06 ***
## dfeduc
                2.500e+00
                           8.040e-01
                                       3.110 0.001872 **
## dtotord
                                       9.240
                                              < 2e-16 ***
                1.122e+01
                           1.214e+00
## monpre
                1.203e+00
                           1.413e+00
                                       0.851 0.394650
## nprevist
                1.088e+01
                          5.328e-01
                                      20.419
                                              < 2e-16 ***
## disllb
                           4.851e-03 -35.319
                                              < 2e-16 ***
               -1.713e-01
## birmon
                                      -3.032 0.002426 **
               -1.222e+00
                           4.031e-01
## dgestat
                           5.986e-01 186.230
                1.115e+02
                                              < 2e-16 ***
## csex
               -1.400e+02
                           2.738e+00 -51.154
                                              < 2e-16 ***
## dplural
               -5.853e+02
                           8.127e+00 -72.013
                                              < 2e-16 ***
## anemia
               -2.296e+01
                           1.380e+01
                                      -1.664 0.096122
## diabetes
               -1.406e+02
                           8.536e+00 -16.468
                                              < 2e-16 ***
## herpes
                                      -1.436 0.150883
               -2.518e+01
                           1.753e+01
## chyper
                1.325e+02
                           1.573e+01
                                       8.425
                                              < 2e-16 ***
## preterm
                2.642e+02
                           1.171e+01
                                      22.560
                                              < 2e-16 ***
## tobacco_p
               -1.028e+02
                           1.140e+01
                                      -9.011
                                              < 2e-16 ***
## cigar
               -1.097e+01
                           2.283e+00
                                      -4.804 1.56e-06 ***
## alcohol
                                       3.920 8.85e-05 ***
                5.537e+01
                           1.412e+01
## dmage2
               -1.786e-01
                           3.737e-02
                                      -4.780 1.75e-06 ***
                                       4.687 2.78e-06 ***
## cigar2
                           8.815e-02
                4.131e-01
## cigar3
               -3.291e-03
                           9.998e-04
                                      -3.292 0.000996 ***
## cig_dmag
               -1.495e-01
                          4.681e-02
                                      -3.194 0.001402 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 463 on 114579 degrees of freedom
## Multiple R-squared: 0.3743, Adjusted R-squared: 0.3741
## F-statistic: 2284 on 30 and 114579 DF, p-value: < 2.2e-16
```

The benefits of this approach is that it potentially increases the accuracy of the prediction of treatment affect by removing misspecification bias. The drawbacks of this approach are the potential for overspecification, meaning the new specification is based more on the noise inherent in the data, and less on actual relationship of treatment to outcome.

1c - Using LASSO

In our application of lasso, we apply the method proposed by belloni, chernozhukov, and hansen. First we apply lasso of the treatment on the covariates. Then, we apply it on the outcome variable and the covariates and keep the set of covariates that lasso selects in either 1 or 2.

```
x_lasso <- dat_drop %>%
  select(stresfip,dmage,ormoth,mrace3,dmeduc,dmar,adequacy,dfage,
               orfath,dfeduc,dtotord,monpre,nprevist,disllb,birmon,dgestat,csex,dplural,
               anemia, diabetes, herpes, chyper,
               preterm,cigar,alcohol,dmage2,cigar2,cigar3,cig_dmag) %>% as.matrix()
y_lasso <- dat_drop %>% select(dbrwt) %>% as.matrix()
d_lasso <- dat_drop %>% select(tobacco) %>% as.matrix()
fit <- cv.glmnet(x_lasso,d_lasso)</pre>
coef(fit, s = "lambda.1se")
## 30 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                1.907495e+00
## stresfip
## dmage
                8.490930e-05
## ormoth
## mrace3
## dmeduc
               1.618641e-03
## dmar
               -2.474879e-02
## adequacy
## dfage
## orfath
## dfeduc
                7.119644e-04
## dtotord
## monpre
## nprevist
## disllb
## birmon
## dgestat
## csex
## dplural
## anemia
## diabetes
## herpes
## chyper
## preterm
## cigar
               -1.242140e-01
## alcohol
                3.149641e-02
## dmage2
## cigar2
                3.954556e-03
## cigar3
               -3.001411e-05
## cig_dmag
fit2 <- cv.glmnet(x_lasso,y_lasso)</pre>
coef(fit2, s = "lambda.1se")
```

```
## 30 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept) -5.836403e+02
## stresfip
## dmage
                1.208918e+00
## ormoth
               -1.191653e+01
## mrace3
               -6.952830e+01
               3.726878e+00
## dmeduc
               -4.919325e+01
## dmar
## adequacy
## dfage
## orfath
               -9.516559e+00
## dfeduc
               1.960426e+00
                6.732855e+00
## dtotord
## monpre
## nprevist
                8.814857e+00
               -1.635390e-01
## disllb
## birmon
               1.107724e+02
## dgestat
## csex
               -1.284371e+02
## dplural
               -5.496181e+02
## anemia
## diabetes
               -1.055891e+02
## herpes
## chyper
               6.377761e+01
## preterm
               2.166868e+02
               -1.312112e+01
## cigar
## alcohol
                1.810358e+01
## dmage2
## cigar2
## cigar3
                1.367422e-03
## cig_dmag
               -5.450084e-03
Based on the estimates of 0 in both, we drop stressip, adequacy, dfage, monpre, birmon, anemia, herpes,
dfage2, dmage2, cigar2.
lm.out <- lm(dbrwt ~ dmage+ormoth+mrace3+dmeduc+dmar+</pre>
               orfath+dfeduc+dtotord+nprevist+disllb+dgestat+csex+dplural+diabetes+chyper+
               preterm+tobacco_p+cigar+alcohol+cigar3+cig_dmag, data = dat_drop)
summary(lm.out)
##
## Call:
## lm(formula = dbrwt ~ dmage + ormoth + mrace3 + dmeduc + dmar +
       orfath + dfeduc + dtotord + nprevist + disllb + dgestat +
##
       csex + dplural + diabetes + chyper + preterm + tobacco_p +
##
##
       cigar + alcohol + cigar3 + cig_dmag, data = dat_drop)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -2840.00 -296.40
                        -7.47
                                 291.80 2652.15
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
```

(Intercept) -8.157e+02 5.754e+01 -14.176 < 2e-16 ***

```
1.026e+00 3.377e-01
                                   3.038 0.002378 **
## dmage
              -1.979e+01 3.476e+00 -5.694 1.24e-08 ***
## ormoth
              -7.834e+01 2.342e+00 -33.457 < 2e-16 ***
## mrace3
## dmeduc
               4.273e+00 8.532e-01
                                    5.008 5.50e-07 ***
## dmar
              -3.923e+01 4.041e+00 -9.708 < 2e-16 ***
              -1.629e+01 3.425e+00 -4.757 1.97e-06 ***
## orfath
              2.363e+00 8.009e-01
## dfeduc
                                   2.951 0.003173 **
              1.147e+01 1.209e+00 9.487 < 2e-16 ***
## dtotord
## nprevist
              1.001e+01 4.082e-01 24.523 < 2e-16 ***
                                           < 2e-16 ***
## disllb
              -1.741e-01 4.816e-03 -36.155
## dgestat
              1.118e+02 5.916e-01 188.995 < 2e-16 ***
              -1.401e+02 2.738e+00 -51.167
## csex
                                           < 2e-16 ***
## dplural
              -5.839e+02 8.121e+00 -71.902 < 2e-16 ***
## diabetes
              -1.416e+02 8.532e+00 -16.592 < 2e-16 ***
## chyper
              1.323e+02 1.572e+01
                                     8.420 < 2e-16 ***
## preterm
              2.632e+02 1.171e+01 22.475
                                           < 2e-16 ***
              -1.426e+02 7.477e+00 -19.071 < 2e-16 ***
## tobacco_p
## cigar
              -2.804e+00 1.399e+00 -2.004 0.045107 *
                                    3.655 0.000257 ***
## alcohol
              5.157e+01 1.411e+01
## cigar3
               1.108e-03 3.361e-04
                                    3.296 0.000980 ***
## cig_dmag
              -1.281e-01 4.669e-02 -2.744 0.006078 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 463.1 on 114588 degrees of freedom
## Multiple R-squared: 0.3739, Adjusted R-squared: 0.3738
## F-statistic: 3259 on 21 and 114588 DF, p-value: < 2.2e-16
```

Some of these terms I would have thought would have mattered such as adequacy of care and anemia.

2 - Propensity score description

The propensity score helps solve the issue that it is hard to condition on X if X is high dimensional. However, we want to do such conditioning in order to compare between treated and control units. The propensity score helps us proxy for the probability of entering treatment and therefore after conditioning on the propensity score, the units are as good as randomly assigned.

2a - Create propensity score

```
##
       data = dat_drop)
##
## Deviance Residuals:
##
      Min
                 1Q
                     Median
                                   3Q
                                           Max
##
   -2.4737 -0.6044 -0.4261
                             -0.2816
                                        3.2548
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.794e-01 3.161e-01
                                      0.884 0.37682
## dmage
              -1.787e-02 2.570e-03 -6.953 3.57e-12 ***
## ormoth
               -4.093e-01
                          2.724e-02 -15.027
                                              < 2e-16 ***
## mrace3
                          1.389e-02 -33.667
               -4.676e-01
                                              < 2e-16 ***
## dmeduc
               -1.812e-01
                          5.485e-03 -33.030
                                             < 2e-16 ***
## dmar
               1.300e+00 2.178e-02 59.697
                                             < 2e-16 ***
               2.602e-02 1.974e-03
                                     13.186
                                             < 2e-16 ***
## dfage
## orfath
               -2.093e-01
                          2.392e-02
                                     -8.752
                                              < 2e-16 ***
## dfeduc
              -1.229e-01 5.172e-03 -23.758
                                              < 2e-16 ***
## disllb
               -1.406e-04 4.449e-05
                                     -3.161
                                              0.00157 **
               6.460e-02 5.063e-03 12.758
## isllb10
                                              < 2e-16 ***
## anemia
               -2.895e-02
                          7.769e-02
                                     -0.373
                                              0.70939
## diabetes
              -5.496e-02 5.320e-02 -1.033
                                             0.30159
## herpes
               -1.569e-01 1.072e-01 -1.464 0.14325
                4.271e-01 5.847e-02
                                      7.305 2.77e-13 ***
## phyper
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 100543 on 114609 degrees of freedom
## Residual deviance: 88060 on 114595 degrees of freedom
## AIC: 88090
##
## Number of Fisher Scoring iterations: 5
dat_drop$p.hat_all <- predict(glm( as.formula(paste( 'tobacco_p ~ ', Pcontrols)),</pre>
                              dat_drop, family = binomial(logit)),
                         type = "response") # this is important!
Pcontrols2 = 'dmage+ ormoth+ mrace3+ dmeduc+ dmar+
dfage+ orfath+ dfeduc + disllb + isllb10 + phyper'
dat_drop$p.hat_2 <- predict(glm( as.formula(paste( 'tobacco_p ~ ', Pcontrols2)),</pre>
                              dat_drop, family = binomial(logit)),
                         type = "response") # this is important!
```

Anemia, diabetes, and herpes were all insignificant in the calculation of the propensity score.

```
dat_drop$diff <- dat_drop$p.hat_all - dat_drop$p.hat_2
summary(dat_drop$diff)</pre>
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max. ## -0.0018225 -0.0004369 -0.0002613 0.0000000 -0.0001460 0.0517418
```

The propensity scores were very comparable with at most a 5% difference and a average difference of 0%

2b - propensity score estimation

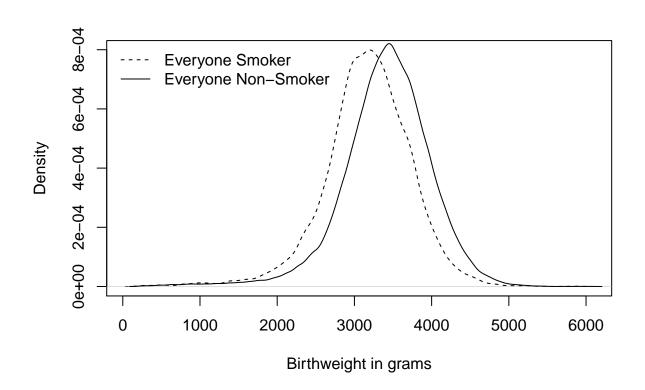
```
#Controlling for propensity scores
reg4 <- lm(dbrwt ~ tobacco_p + p.hat_2, data = dat_drop)
summary(reg4)
##
## Call:
## lm(formula = dbrwt ~ tobacco_p + p.hat_2, data = dat_drop)
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -3191.5 -311.4
                     26.9
                                   2744.6
                            359.9
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3422.731
                            2.747 1245.870 < 2e-16 ***
## tobacco_p
              -231.375
                            4.952 -46.721 < 2e-16 ***
                                    -5.506 3.68e-08 ***
## p.hat_2
               -78.835
                           14.319
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 578.4 on 114607 degrees of freedom
## Multiple R-squared: 0.02288,
                                   Adjusted R-squared: 0.02287
## F-statistic: 1342 on 2 and 114607 DF, p-value: < 2.2e-16
```

Using this approach, we estimate an average treatment effect of -231 grams as a result of smoking while pregnant. This treatment effect is consistent under unconfoundedness (i.e. random assignment of treatment conditional on the covariates) and the assumption of a constant (i.e., homogenous) treatment effect.

2c - propensity score reweighting

2d - kernel density estimator

Plotting the densities here



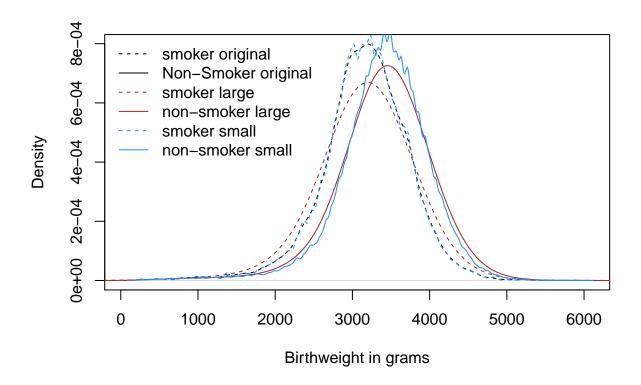
Calculating point estimate of the density

```
h = 2
y = 3000
treated <- dat_drop[dat_drop$tobacco_p==1,]
control <- dat_drop[dat_drop$tobacco_p==0,]</pre>
```

```
treatment_density <- 0</pre>
control_density <- 0
for(i in 1:nrow(treated))
{
gauss_den <- (1/sqrt(2*pi))*exp(-0.5*((y-treated$dbrwt[i])/h)^2)*
  treated$tobacco_p[i]/treated$p.hat_2[i]
treatment_density <- gauss_den + treatment_density</pre>
}
final_treat_density <- (1/(h*nrow(treated))) * treatment_density</pre>
print(final_treat_density)
## [1] 0.002763949
for(i in 1:nrow(control))
{
gauss_den <- (1/\sqrt{2*pi})*exp(-0.5*((y-\text{control}^dbrwt[i])/h)^2)*
  (1-control$tobacco_p[i])/(1 - control$p.hat_2[i])
control_density <- gauss_den + control_density</pre>
}
final_control_density <- (1/(h*nrow(control))) * control_density</pre>
print(final control density)
## [1] 0.00030146
```

2e - bandwidth adjustments

You can tell that when the bandwidth is larger, the density is smoother but also has a smaller peak than the original. The smaller bandwidth, though, becomes much more noisy.



2f - benefits and drawbacks of propensity method

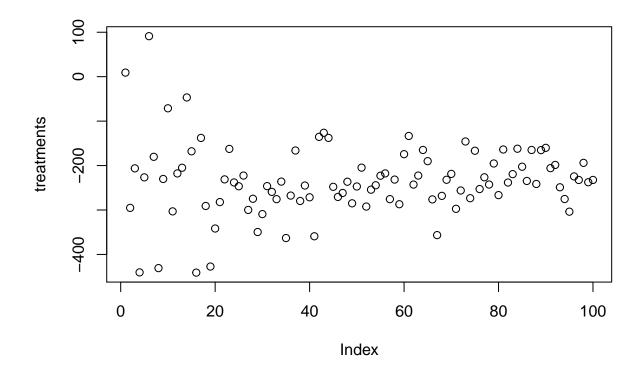
We know that propensity scores are not balanced across treated and control groups. The weighting scheme ensures that each observation is equally represented (in expectation) in the treated and control groups. According to to Hirano, Imbens, and Ridder, the weighting estimator we use is efficient. However, very low and very high propensity scores may weight observations to 0 or infinity and bias the results.

2g - Present and discuss results

- i. Must hold. The inverse weighting of propensity scores seems more reasonable if the treatment effect heterogeneity is linear in the propensity scores. If it is non-linear we might need to use a different weighting mechanism.
- ii. Need not hold. If it is non-linear we might need to use a differenet weighting mechanism. Our weighting mechanism in 2c might not be accurate.
- iii. Need not hold. Without conditioning for propensity scores we saw a systemic difference between smokers and non smokers who selected into treatment. The systematic difference was accounted for when we calculated the propensity scores.
- iv. Must hold. On taking propensity scores, we account for the exogenous variation and the decision to smoke is as good as randomly assigned. If conditional on the exogenous variables the decision to smoke is still not randomly assigned we will get biased estimnates for ATE and TOT.

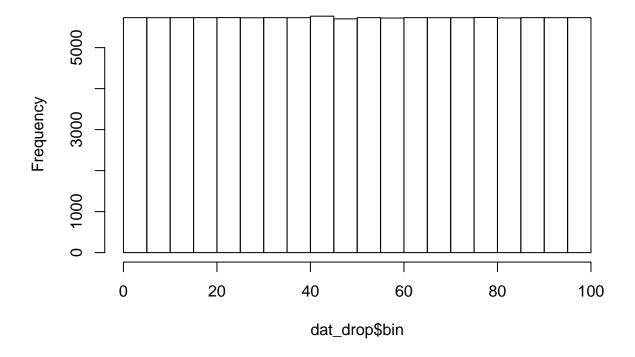
3 - Blocking non-parametric approach

```
# Create 100 equally sized bins based on propensity scores
dat_drop$bin <- cut(dat_drop$p.hat_2, quantile(dat_drop$p.hat_2, seq(0,1,0.01)),</pre>
                    include.lowest = TRUE, labels = FALSE)
# Find difference between birth weights of non-smokers and smokers in each bin, and assign weights to t
treatment_effect = 0
treatments <- c()
for(i in 1:100)
{
mean diff = mean(dat drop$dbrwt[dat drop$tobacco p==1 & dat drop$bin==i]) -
  mean(dat_drop$dbrwt[dat_drop$tobacco_p==0 & dat_drop$bin==i])
treatments <- c(treatments, mean_diff)</pre>
#print(i)
#print(mean_diff)
N <- nrow(dat_drop)</pre>
N1 <- nrow(dat_drop[dat_drop$tobacco_p==1 & dat_drop$bin == i,])
NO <- nrow(dat_drop[dat_drop$tobacco_p==0 & dat_drop$bin == i,])
weighted_mean <- mean_diff*((N1+N0)/N)</pre>
#print(weighted mean)
treatment_effect = weighted_mean + treatment_effect
}
print(treatment_effect)
## [1] -234.3858
plot(treatments)
```



hist(dat_drop\$bin)

Histogram of dat_drop\$bin



The result from this weighted mean difference method shows that on average, babies of smokers have lower birth weights by 234 grams as compared to babies of non-smokers. This is almost equal to the ATE of -232 grams found in the previous question where we did not block as per propensity scores. These equal results show that there are no systematic differences between smokers and non-smokers based on the other covariates included in the study. A quick check of the number of data points within the bins shows that we have balanced blocking as well since the data is uniformly distributed across the bins. Furthermore, a plot of all of the mean treatment effects in each bin shows a pretty stable line for each bin.

4 - low birth weights

```
# Create a low birth weight indicator variable
dat_drop$low <- 0
dat_drop$low[dat_drop$dbrwt < 2500] <- 1

# Find difference between proportion of low birth weights between non-smokers and smokers in each bin,
treatment_effect = 0
treatments <- c()

for(i in 1:100)
{

mean_diff = mean(dat_drop$low[dat_drop$tobacco_p==1 & dat_drop$bin==i]) -
    mean(dat_drop$low[dat_drop$tobacco_p==0 & dat_drop$bin==i])</pre>
```

```
treatments <- c(treatments, mean_diff)</pre>
#print(i)
#print(mean_diff)
N <- nrow(dat_drop)</pre>
N1 <- nrow(dat_drop[dat_drop$tobacco_p==1 & dat_drop$bin == i,])
NO <- nrow(dat_drop[dat_drop$tobacco_p==0 & dat_drop$bin == i,])
weighted_mean <- mean_diff*((N1+N0)/N)</pre>
#print(weighted mean)
treatment_effect = weighted_mean + treatment_effect
}
print(treatment_effect)
## [1] 0.04452343
# Difference in proportion of low birthweight babies between smokers and non-smokers
low_diff <- (nrow(dat_drop[dat_drop$low ==1 & dat_drop$tobacco_p==1,])/</pre>
               nrow(dat_drop[dat_drop$tobacco_p==1,]) - nrow(dat_drop[dat_drop$low ==1 &
low diff
```

[1] 0.04514949

The result shows that smokers have a 4.45 pc higher proportion of low birthweight babies than do non-smokers. This is almost equal to the absolute difference of 4.52 pc in the proportion of low birth weight babies between smokers and non-smokers. Hence, we can say that there are no systematic differences in birth weights between the bins/blocks created, indicating that we have a uniform distribution of data across the bins.

5 - Summarize results

Drawing on our results from the previous assignment where we found that birth weights of smokers were on average 231.8 gms lower than the birth weights of non-smokers, we now allow the relationship between birth weight and the explanatory variables to assume a non-linear functional form. In order to ensure that the selection into treatment does not differ in some meaningful way from the units that do not select into treatment, we condition the regression on propensity scores. The propensity scores are calculated using all the pre-determined covariates and quadratic terms for age of mother and father, based on observation of the functional form and results of the LASSO regression estimate. The results show that the average treatment effect of smoking increased to 234 gms on controlling for the propensity scores, showing that some of the difference in birth weights between smokers and non-smokers was due to systematic differences in how smokers selected into the treatment. In order to balance the propensity scores across treatment and control groups, we use a weighting method which ensures that smokers and non-smokers are equally represented across both groups. The results for this regression show that the ATE is 232 gms which is the same as our previous result from the conditional regression. However, the treatment on treated effect is found to be 229 gms showing that the difference in birth weights is lower for those who actually selected into treatment and control versus those who had the highest likelihood of being in either group. We also use a blocking method based on propensity scores to confirm that there are no block-wise differences between smokers and non-smokers with similar propensity scores. The results indicate an ATE of 234.3 gms which is almost equal to the ATE found previously, showing that there are no systematic differences between smokers and non-smokers based on the other covariates included in the study. Using the blocking method, we also find that smokers have a 4.45 pc higher proportion of low birthweight babies than do non-smokers.