# assignment

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# 1 Intelligent Systems Seminar Assignment 1

# Genetic algorith written in python

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#### 1.0.1 Libraries

```
[2]: import statistics
  import math
  import random
  from matplotlib import pyplot as plt
  import numpy as np
```

```
[3]: from IPython.display import set_matplotlib_formats set_matplotlib_formats('png', 'pdf')
```

# 1.1 Population generation

Agent is an arithmetic expression constructed of numbers and symbols specified below.

Each number can be used max\_number\_use times, therefore the expression can contain from 1 to len(numbers)\*max\_number\_use numbers.

After each number there is a symbol from symbols. The symbol after the last number is ignored, but may be used in future generations like an unexpressed gene in a human genome. That decision was made primarily to make crossover (based on permutations) easier to implement.

```
[4]: numbers = ['10', '25', '100', '5', '3']
symbols = ['+', '-', '*', '/']

max_number_use = 1
min_numbers_in_expresion = 1

target_value = 2512
```

```
[5]: def generate_agent():
    n_numbers = random.randint(min_numbers_in_expresion, □
    →len(numbers)*max_number_use)
    selected_numbers = random.sample(numbers*max_number_use, n_numbers)
```

```
return [(number, random.choice(symbols)) for number in selected_numbers]

def agent_to_expression(agent):
        expression = "".join(n + s for n, s in agent)
        return expression[:-1] # remove last operator

def evaluate_agent(agent):
    expression = agent_to_expression(agent)
    if len(expression) == 0: return 0
    else: return eval(expression)

def agent_to_string(agent):
    return f"{agent_to_expression(agent)} = {evaluate_agent(agent):.2f}"
```

Agent is constructed of tuples of a number and a symbol as seen below: - generate\_agent generates a random agent - agent\_to\_expression function joins the tuples together into a string, ignoring the last symbol - evaluate\_agent generates the expression and evaluates it - agent\_to\_string creates a string with expression and its value

```
[7]: a = generate_agent()
    print("Generate agent : ", a)
    print("Agent expression : ", agent_to_expression(a))
    print("Evaluated : ", evaluate_agent(a))
    print("Pretty print : ", agent_to_string(a))
```

Generate agent : [('10', '+'), ('25', '-'), ('100', '\*'), ('5', '\*'), ('3', '4')]

'+')]

Agent expression : 10+25-100\*5\*3

Evaluated : -1465

Pretty print : 10+25-100\*5\*3 = -1465.00

Here are some randomly generated agents:

```
[6]: for i in range(20):
    a = generate_agent()
    print(f"{i}. ", agent_to_string(a))
```

- $0. \quad 3-10/5 = 1.00$
- $1. \quad 5-3 = 2.00$
- $2. \quad 10-5/100 = 9.95$
- $3. \quad 100+3+10/5-25 = 80.00$
- 4. 10\*3+25\*5 = 155.00
- $5. \quad 25 = 25.00$
- $6. \quad 10 = 10.00$
- $7. \quad 25 = 25.00$
- 8. 5\*100+25-10/3 = 521.67
- 9. 3+100-5/25 = 102.80
- 10. 25-5 = 20.00

```
11. 25/5 = 5.00

12. 5/10/3+25/100 = 0.42

13. 5 = 5.00

14. 3/5 = 0.60

15. 25*3 = 75.00

16. 100-10/3*25-5 = 11.67

17. 25/5/10*100 = 50.00

18. 10/5+25-3*100 = -273.00

19. 10*5 = 50.00
```

### 1.2 Fitness

Fitness is used as a scoring function for the genetic algorithm to determine the best agents to use for reproduction.

We defined some different fitness functions, which will be compared in section *Evaluation*: -fitness\_abs returns the negative of an absolute value of the error - fitness\_inverse returns 1 over an absolute value of the error - fitness\_squared returns negative of the error squared -fitness\_log returns negative of the logarithm of the error

```
[8]: def error(agent):
    return abs(evaluate_agent(agent) - target_value)

def fitness_abs(agent):
    return -error(agent)

def fitness_inverse(agent):
    return 1/(error(agent) + 0.0001) # + 0.0001 to avoid zero devision

def fitness_squared(agent):
    return -(error(agent)**2)

def fitness_log(agent):
    return -math.log2(error(agent)+1)
```

### 1.3 Mutation

We defined 7 different types of mutation: - mutation\_change\_symbol changes a random symbol - mutation\_change\_number changes a random number - mutation\_add\_element adds a new element to the agent - mutation\_remove\_element removes a random element from the agent - mutation\_swap\_symbol swaps two random symbols

-  $\mathtt{mutation\_swap\_number}$  swaps two random numbers -  $\mathtt{mutation\_swap\_element}$  swaps two random elements (i.e. tuples consistion of a number and a symbol ("5", "+"))

We add function mutation so that it randomly chooses between all of the mutations listed above

```
[9]: def mutation_change_symbol(agent):
    a = agent.copy()
    i = random.randrange(len(a))
```

```
number, = a[i]
    a[i] = (number, random.choice(symbols))
    return a
def mutation_change_number(agent):
    a = agent.copy()
    agent_numbers = [number for number, _ in a]
    # choose numbers that can be added without violating `max number use`
    candidate_numbers = list(filter(lambda n: agent_numbers.count(n) <__
→max_number_use, numbers))
    if len(candidate_numbers) == 0: return a
    i = random.randrange(len(a))
    _, symbol = a[i]
    a[i] = (random.choice(candidate_numbers), symbol)
    return a
def mutation_add_element(agent):
    a = agent.copy()
    agent_numbers = [number for number, _ in a]
    # choose numbers that can be added without violating `max number use`
    candidate_numbers = list(filter(lambda n: agent_numbers.count(n) __
→max_number_use, numbers))
    if len(candidate_numbers) == 0: return a
    a.insert(random.randint(0, len(a)), (random.choice(candidate_numbers),__
→random.choice(symbols)))
    return a
def mutation_remove_element(agent):
    a = agent.copy()
    if len(a) <= 1: return a # nothing to remove</pre>
    del a[random.randrange(len(a))]
    return a
def mutation_swap_symbol(agent):
   a = agent.copy()
    i = random.randrange(len(agent))
    j = random.randrange(len(agent))
    a[i], a[j] = (a[i][0], a[j][1]), (a[j][0], a[i][1])
    return a
def mutation_swap_number(agent):
```

```
a = agent.copy()
   i = random.randrange(len(agent))
   j = random.randrange(len(agent))
   a[i], a[j] = (a[j][0], a[i][1]), (a[i][0], a[j][1])
   return a
def mutation_swap_element(agent):
   a = agent.copy()
   i = random.randrange(len(agent))
   j = random.randrange(len(agent))
   a[i], a[j] = a[j], a[i]
   return a
def mutation(agent):
   mutation_functions = [mutation_change_symbol, mutation_change_number,_
→mutation_add_element, mutation_remove_element,
                          mutation swap number, mutation swap symbol,
→mutation_swap_element]
   return random.choice(mutation_functions)(agent)
```

Here is an example of all the mutations made on the same agent:

```
[15]: agent = generate_agent()
     print("Generated agent : ", agent)
     print("Change symbol : ", mutation_change_symbol(agent))
     print("Change number : ", mutation_change_number(agent))
     print("Add element : ", mutation_add_element(agent))
     print("Remove element : ", mutation_remove_element(agent))
     print("Swap symbol : ", mutation_swap_symbol(agent))
     print("Swap number
                          : ", mutation_swap_number(agent))
     print("Swap element : ", mutation_swap_element(agent))
     print("Random mutation : ", mutation(agent))
     Generated agent : [('10', '+'), ('3', '*'), ('25', '+'), ('100', '/')]
                   : [('10', '+'), ('3', '*'), ('25', '+'), ('100', '-')]
     Change symbol
     Change number : [('10', '+'), ('3', '*'), ('5', '+'), ('100', '/')]
                 : [('5', '/'), ('10', '+'), ('3', '*'), ('25', '+'), ('100',
     Add element
     '/')]
     Remove element : [('10', '+'), ('3', '*'), ('100', '/')]
                  : [('10', '*'), ('3', '+'), ('25', '+'), ('100', '/')]
     Swap symbol
                    : [('10', '+'), ('25', '*'), ('3', '+'), ('100', '/')]
     Swap number
     Swap element : [('10', '+'), ('3', '*'), ('100', '/'), ('25', '+')]
     Random mutation : [('3', '+'), ('10', '*'), ('25', '+'), ('100', '/')]
```

#### 1.4 Crossover

Crossover takes 2 parents: parent1 and parent2.

It then splits parent1 and parent2 into 2 parts and takes one part from parent1 and another from parent2 and stiches them together to create child1.

It does the same for child2, just that it takes the other 2 parts.

#### 1.4.1 Functions

```
[16]: def agent_subtract(agent1, agent2):
          agent2_numbers = [n for n, _ in agent2]
          res = \Pi
          for number, symbol in agent1:
              if number in agent2_numbers: agent2_numbers.remove(number)
              else: res.append((number, symbol))
          return res
      def crossover(parent1, parent2):
          min_len = min(len(parent1), len(parent2))
          selection_start = random.randint(0, min_len)
          selection_end = random.randint(selection_start, min_len)
          child1 = parent1[selection_start:selection_end]
          child2 = parent2[selection_start:selection_end]
          child1.extend(agent_subtract(parent2, child1))
          child2.extend(agent_subtract(parent1, child2))
          return (child1, child2)
```

### 1.4.2 Step by step example

We first generate two parents parent1 and parent2:

```
[52]: parent1 = generate_agent()
    parent2 = generate_agent()
    print("parent1: ", parent1, agent_to_string(parent1))
    print("parent2: ", parent2, agent_to_string(parent2))

parent1: [('25', '-'), ('3', '-'), ('10', '*'), ('100', '+')] 25-3-10*100 = -978.00
    parent2: [('10', '+'), ('3', '*'), ('5', '-'), ('25', '/'), ('100', '*')] 10+3*5-25/100 = 24.75
```

We then select a section that overlaps both parents and initializes child1 to a section of parent1 and child2 to a section of parent2.

```
[54]: min_len = min(len(parent1), len(parent2))
selection_start = random.randint(0, min_len)
selection_end = random.randint(selection_start, min_len)
```

```
child1 = parent1[selection_start:selection_end]
child2 = parent2[selection_start:selection_end]

print("child1: ", child1, agent_to_string(child1))
print("child2: ", child2, agent_to_string(child2))
```

```
child1: [('25', '-')] 25 = 25.00 child2: [('10', '+')] 10 = 10.00
```

The rest of the elements come from the other parent by removing the numbers that already came from the first parent.

We do that using the function agent\_subtract, so that we stay within the bounds of the problem (all of the numbers can only be used once)

```
parent1_remainder: [('25', '-'), ('3', '-'), ('100', '+')] 25-3-100 = -78.00 parent2_remainder: [('10', '+'), ('3', '*'), ('5', '-'), ('100', '*')] 10+3*5-100 = -75.00
```

In the end we stich both children together using the parent\_remainder.

```
[56]: child1.extend(parent2_remainder)
    child2.extend(parent1_remainder)

print("child1 result: ", child1, agent_to_string(child1))
    print("child2 result: ", child2, agent_to_string(child2))
```

```
child1 result: [('25', '-'), ('10', '+'), ('3', '*'), ('5', '-'), ('100', '*')] 25-10+3*5-100 = -70.00 child2 result: [('10', '+'), ('25', '-'), ('3', '-'), ('100', '+')] 10+25-3-100 = -68.00
```

Example of the crossover function:

```
[57]: child1, child2 = crossover(parent1, parent2)
    print(f"parent1 : {agent_to_string(parent1)}; lenght: {len(parent1)}")
    print(f"parent2 : {agent_to_string(parent2)}; length: {len(parent2)}")
    print(f"child1 : {agent_to_string(child1)}; length: {len(child1)}")
    print(f"child2 : {agent_to_string(child2)}; length: {len(child2)}")
```

```
parent1 : 25-3-10*100 = -978.00; lenght: 4
parent2 : 10+3*5-25/100 = 24.75; length: 5
```

```
child1 : 100+10+3*5-25 = 100.00; length: 5 child2 : 25/3-10*100 = -991.67; length: 4
```

### 1.5 Selection

### 1.5.1 Top agents

The first naive approach is to order the agents by their fitness and select the top n agents.

```
[18]: def select_best_agents(population_with_fitness, n_agents):
    return list(sorted(population_with_fitness, key=lambda e: e[1],
    →reverse=True))[:n_agents]
```

Lets create a 100 agents and select the best 10.

```
error: 7.000, fitness: -3.000, agent: 100*25+5 = 2505.00, error: 22.000, fitness: -4.524, agent: 100*25-10 = 2490.00, error: 762.000, fitness: -9.576, agent: 10*25+3*5*100 = 1750.00, error: 1238.000, fitness: -10.275, agent: 25*100/10*5*3 = 3750.00, error: 1664.667, fitness: -10.702, agent: 10+100*25*5/3 = 4176.67, error: 2012.000, fitness: -10.975, agent: 100*5 = 500.00, error: 2095.333, fitness: -11.034, agent: 25*5*10/3 = 416.67, error: 2182.000, fitness: -11.092, agent: 25+10+3*100-5 = 330.00, error: 2182.000, fitness: -11.092, agent: 25+10+100*3-5 = 330.00, error: 2259.000, fitness: -11.142, agent: 5*100-25*10+3 = 253.00,
```

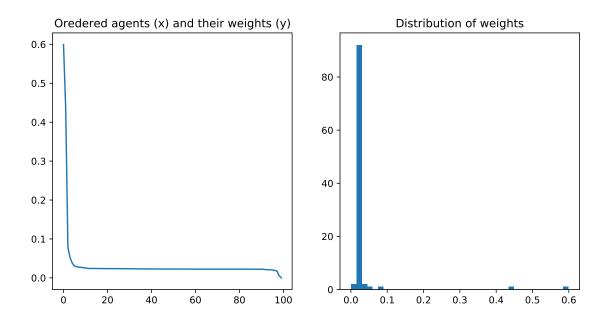
## 1.5.2 Weighted choice

Another approach is to compute wheits based on the fitness value and than make a random weighted choice of n agents.

```
[21]: def get_weights(population_with_fitness, verbose=False):
    k = 1.0 # if k is close to 1 best agents are more favored if k > 1 the
    →difference in weights between different agents gets smaller
    population_fitness = [f for a, f in population_with_fitness]
    min_fitness = min(population_fitness)
    base_fitness = -min_fitness*k
    population_with_weights = [(a, f, ((f+base_fitness)/base_fitness)**2) for
    →a, f in population_with_fitness]
```

Lets look at the distribution of the weights with logarithmic fitness function:

```
fitness: -3.000, weight: 0.599, agent: 100*25+5 = 2505.00 fitness: -4.524, weight: 0.435, agent: 100*25-10 = 2490.00 fitness: -9.576, weight: 0.078, agent: 10*25+3*5*100 = 1750.00 fitness: -10.275, weight: 0.051, agent: 25*100/10*5*3 = 3750.00 fitness: -10.702, weight: 0.038, agent: 10+100*25*5/3 = 4176.67 fitness: -10.975, weight: 0.030, agent: 100*5 = 500.00 fitness: -11.034, weight: 0.029, agent: 25*5*10/3 = 416.67 fitness: -11.092, weight: 0.027, agent: 25+10+3*100-5 = 330.00 fitness: -11.092, weight: 0.027, agent: 25+10+100*3-5 = 330.00 fitness: -11.142, weight: 0.026, agent: 5*100-25*10+3 = 253.00
```

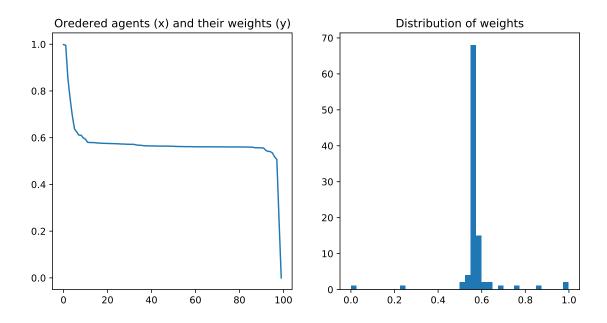


We can see that the best few agents get very large weight and the most agents get weights around 0.2 to 0.5 (depends on the population). There are some very bad agents that gat almost 0 weight.

If we use different fitness function (negative absolute error for example), we get different distrubution.

```
[27]: population_with_fitness = [(a, fitness_abs(a)) for a in population]
_ = get_weights(population_with_fitness, verbose=True)
```

```
fitness: -7.000, weight: 0.999, agent: 100*25+5 = 2505.00 fitness: -22.000, weight: 0.996, agent: 100*25-10 = 2490.00 fitness: -762.000, weight: 0.853, agent: 10*25+3*5*100 = 1750.00 fitness: -1238.000, weight: 0.767, agent: 25*100/10*5*3 = 3750.00 fitness: -1664.667, weight: 0.694, agent: 10+100*25*5/3 = 4176.67 fitness: -2012.000, weight: 0.638, agent: 100*5 = 500.00 fitness: -2095.333, weight: 0.624, agent: 25*5*10/3 = 416.67 fitness: -2182.000, weight: 0.611, agent: 25+10+3*100-5 = 330.00 fitness: -2182.000, weight: 0.611, agent: 25+10+100*3-5 = 330.00 fitness: -2259.000, weight: 0.599, agent: 5*100-25*10+3 = 253.00
```



Now we can implement a function that makes a weighted random choice based on before computed wheights:

```
[29]: def select_weighted(population_with_fitness, n_agents):
          weights = get_weights(population_with_fitness)
          return random.choices(population_with_fitness, weights=weights, k=n_agents)
[30]: population with fitness = [(a, fitness log(a)) for a in population]
      best_agents_weighted = select_weighted(population_with_fitness, 10)
      for a, f in best_agents_weighted:
          print(f"error: {error(a):.3f}, fitness: {f:.3f}, agent:___
       →{agent_to_string(a)}, ")
     error: 2420.000, fitness: -11.241, agent: 100+5-3-10 = 92.00,
     error: 22.000, fitness: -4.524, agent: 100*25-10 = 2490.00,
     error: 762.000, fitness: -9.576, agent: 10*25+3*5*100 = 1750.00,
     error: 22.000, fitness: -4.524, agent: 100*25-10 = 2490.00,
     error: 7.000, fitness: -3.000, agent: 100*25+5 = 2505.00,
     error: 22.000, fitness: -4.524, agent: 100*25-10 = 2490.00,
     error: 2506.000, fitness: -11.292, agent: 10*3/5 = 6.00,
     error: 2482.000, fitness: -11.278, agent: 10*3 = 30.00,
     error: 22.000, fitness: -4.524, agent: 100*25-10 = 2490.00,
     error: 2684.000, fitness: -11.391, agent: 3+25-10*100/5 = -172.00,
```

### 1.5.3 Best plus random selection

Another approach is to comose the selection of half best agents and other half of randomly chosen agents to avoid elitisem.

```
[31]: def select_best_plus_random(population_with_fitness, n_agents):
    best_agents = select_best_agents(population_with_fitness, n_agents//2)
    best_agents.extend(random.choices(population_with_fitness, k=(n_agents -u -n_agents//2)))
    return best_agents
```

#### 1.6 Evolution function

Parameters: - population\_size: size of the population to be generated every iteration - fitness\_function: a function that takes an agent and returns its fitness value - selection\_function: a function that takes set of agents with their fitness value and retrns a subset of a few survivers - crossover\_function: a function that takes two agents and returnes two children - mutation\_function: a function that takes an agent and performs a random mutation - mutation\_probability: in mutation process each agent has a probability of mutation - survival\_probability: percentage of agents that will survive and have offspring - max\_iterations: self explanatory - fitness\_threshold: stop when agent with such fitnes value is found - keep\_best: will parents be part of next population or not - verbose: if true, print metrics for each generation - plot: if true, plot mean and max fitness in each generation

```
[32]: def evolve(
          population size, fitness function, selection function, crossover function,
       →mutation_function,
          mutation_probability=0.4, survival_probability=0.1, max_iterations=100, __
       →fitness_threshold=0, keep_best = False,
          verbose=False, plot=False
      ):
          population = [generate_agent() for _ in range(population_size)]
          min_fitness_log = []
          max_fitness_log = []
          mean_fitness_log = []
          string_log = []
          iterations = 0
          for generation in range(max_iterations):
              iterations += 1
              # evaluate population
              population with fitness = [(a, fitness function(a)) for a in population]
              population_fitness = [f for a, f in population_with_fitness]
```

```
# compute metrics
       mean_fitness = statistics.mean(population_fitness)
       max_fitness = max(population_fitness)
       min_fitness = min(population_fitness)
       # log metrics
      mean_fitness_log.append(mean_fitness)
      max_fitness_log.append(max_fitness)
       min_fitness_log.append(min_fitness)
       # make selection
      best_agents_with_fitness = selection_function(population_with_fitness,_
→math.ceil(population_size*survival_probability))
       best_agents = [a for a, _ in best_agents_with_fitness]
      population_with_fitness_sorted = list(sorted(population_with_fitness,_u
→key=lambda e: e[1], reverse=True))
       # print metrics
       string_log.append(f"Generation {generation}: fitness min: {min_fitness:.
→2f}, max: {max_fitness:.2f}, mean: {mean_fitness:.2f}; best agent:
→{agent_to_string(population_with_fitness_sorted[0][0])}")
       if max_fitness >= fitness_threshold: break
       if keep best:
           population = best_agents.copy()
       else:
           population = []
       # crossover
       for i in range(len(population), population_size, 2):
           parent1, parent2 = random.sample(best_agents, 2)
           child1, child2 = crossover_function(parent1, parent2)
           population.append(child1)
           population.append(child2)
       # mutation
       for i, agent in enumerate(population):
           if random.random() < mutation_probability:</pre>
               population[i] = mutation_function(agent)
   if verbose:
       if len(string_log) > 10:
           for line in string_log[:5]:
               print(line)
```

```
print(" ... lines omitted ... ")
    for line in string_log[-5:]:
        print(line)

else:
    for line in string_log:
        print(line)

if plot:
    plt.figure(figsize=(10,10))
    plt.plot(max_fitness_log, label="max")
    plt.plot(mean_fitness_log, label="mean")
    #plt.plot(min_fitness_log, label="min")
    plt.legend()

return (iterations, (max_fitness_log, mean_fitness_log, min_fitness_log))
```

### 1.7 Evaluation

```
[34]: population_size = 100
max_iterations = 300
max_number_use = 1
```

```
Generation 0: fitness min: -15.09, max: -3.70, mean: -11.20; best agent: 25*100 = 2500.00

Generation 1: fitness min: -14.46, max: -3.32, mean: -10.66; best agent: 3+25*100 = 2503.00

Generation 2: fitness min: -12.29, max: -1.00, mean: -7.17; best agent: 10+3+25*100 = 2513.00

Generation 3: fitness min: -12.28, max: -3.32, mean: -5.46; best agent: 3+25*100 = 2503.00

Generation 4: fitness min: -12.29, max: -3.32, mean: -6.22; best agent: 3+25*100 = 2503.00

... lines omitted ...

Generation 94: fitness min: -16.15, max: -1.00, mean: -5.04; best agent:
```

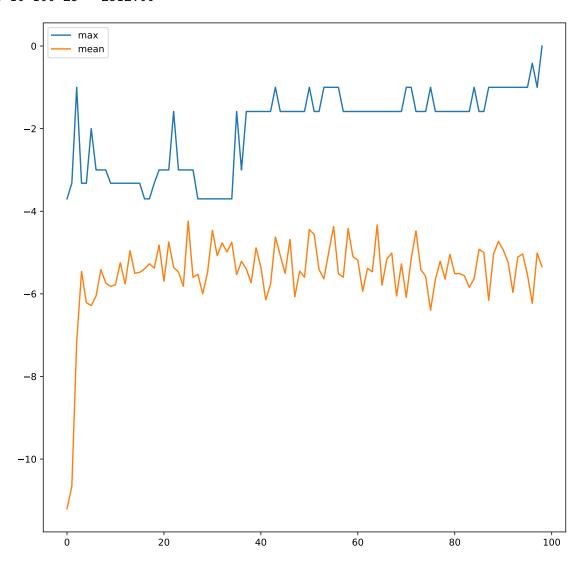
```
10+3+100*25 = 2513.00

Generation 95: fitness min: -14.46, max: -1.00, mean: -5.54; best agent: 10+3+100*25 = 2513.00

Generation 96: fitness min: -14.46, max: -0.42, mean: -6.23; best agent: 25*100+5/3+10 = 2511.67

Generation 97: fitness min: -14.46, max: -1.00, mean: -5.01; best agent: 100*25+10+3 = 2513.00

Generation 98: fitness min: -14.46, max: -0.00, mean: -5.34; best agent: 5-3+10+100*25 = 2512.00
```



## 1.7.1 Plot iterations histogram

iterative function takes no parameters and returns the number of iterations it took to complete

### 1.7.2 Comparison with random search

Random search works by generating a new random population (the same size as initial population for genetic algorithm) every iteration until the optimal agent is found.

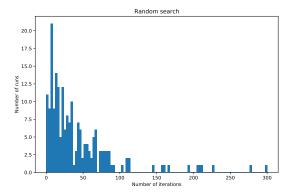
```
def random_search():
    iterations = 0
    for i in range(max_iterations):
        iterations += 1
        population = [generate_agent() for _ in range(population_size)]
        population_with_fitness = [(a, fitness_abs(a)) for a in population]
        population_fitness = [f for a, f in population_with_fitness]
        if max(population_fitness) == 0: break
```

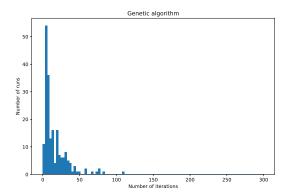
```
[38]: plt.figure(figsize=(20,6))
  plt.subplot(1, 2, 1)
  plot_iterations_histogram(
      random_search,
      title="Random search"
)

plt.subplot(1, 2, 2)
  plot_iterations_histogram(
      lambda: evolve(
            population_size,
            fitness_log,
            select_best_plus_random,
            crossover,
```

```
mutation,
    mutation_probability=0.2, survival_probability=0.2, max_iterations=300,
    keep_best=False, fitness_threshold=0
    )[0],
    title="Genetic algorithm"
)
```

Random search - mean: 41.84, min: 1, max: 297, stdev: 48.49145808838592 Genetic algorithm - mean: 15.41, min: 1, max: 109, stdev: 16.635069210501978





We can see that genetic algorithm, on average, takes less iterations than random search.

### 1.7.3 Different fitness functions

Lets see how does the choice of a fitness function effect performance. We run genetic alghorithm with each fitness function a 200 times and plot a histogram of iterations it took to find the optimal agent.

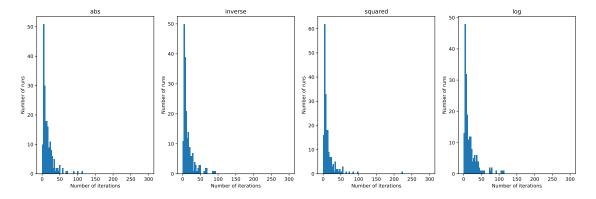
```
mutation_probability=0.2, survival_probability=0.2, 

→max_iterations=300, keep_best=False, fitness_threshold=fitness_threshold

)[0],

title=label
)
```

```
abs - mean: 15.38, min: 1, max: 112, stdev: 16.598892013637595 inverse - mean: 15.075, min: 1, max: 92, stdev: 16.478686554236166 squared - mean: 14.17, min: 1, max: 223, stdev: 21.162949989576276 log - mean: 17.185, min: 1, max: 111, stdev: 19.892696445160382
```

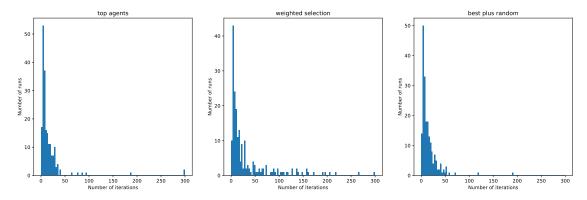


We found out that all fitness functions perform about the same.

### 1.7.4 Different selection functions

```
[46]: selection_functions = [(select_best_agents, "top agents"), (select_weighted,__
       →"weighted selection"), (select_best_plus_random, "best plus random")]
      plt.figure(figsize=(20,6))
      for j, (selection function, label) in enumerate(selection functions):
          plt.subplot(1, len(selection_functions), j+1)
          plot_iterations_histogram(
              lambda: evolve(
                  population_size,
                  fitness_log,
                  selection_function,
                  crossover,
                  mutation,
                  mutation_probability=0.2, survival_probability=0.2,
       →max_iterations=300, keep_best=True, fitness_threshold=0
              )[0].
              title=label
          )
```

top agents - mean: 16.23, min: 1, max: 300, stdev: 33.87350248873404 weighted selection - mean: 34.42, min: 1, max: 300, stdev: 51.03416532236766 best plus random - mean: 14.815, min: 1, max: 191, stdev: 19.20612274129708



We can see from the results that by selecting just the top few agents sometimes the evolution process does not converge. We think that is because we loose the diversity of the population and get stuck in a local optimum.

By also selecting some worse agents the evolution always converges.

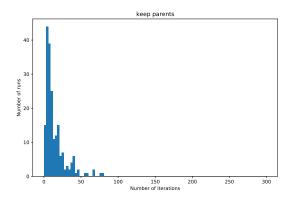
We found that the best selection method for this problem is selecting half of the best agents and half of random agents.

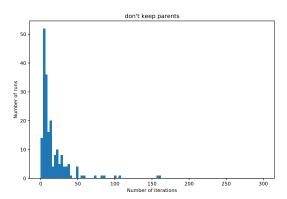
### 1.7.5 Keep parents or not

```
[42]: selection_functions = [(True, "keep parents"), (False, "don't keep parents")]
      plt.figure(figsize=(20,6))
      for j, (keep, label) in enumerate(selection_functions):
          plt.subplot(1, len(selection_functions), j+1)
          plot_iterations_histogram(
              lambda: evolve(
                  population_size,
                  fitness_log,
                  select_best_plus_random,
                  crossover,
                  mutation,
                  mutation_probability=0.2, survival_probability=0.2,
       →max_iterations=300, keep_best=keep, fitness_threshold=0
              )[0],
              title=label
          )
```

keep parents - mean: 13.855, min: 1, max: 79, stdev: 14.093513066399158

don't keep parents - mean: 16.1, min: 1, max: 159, stdev: 21.96456717204499





Keeping parents appears to converge a bit faster.

## 1.8 Bonus task: minimize expression length

```
[47]: max_number_use = 5
min_numbers_in_expresion = 1
```

For this task we have to define a new fitness function that also takes into account the expression length.

```
[48]: def fitness_length(agent):
    return fitness_inverse(agent) + 3/(len(agent)+5)
```

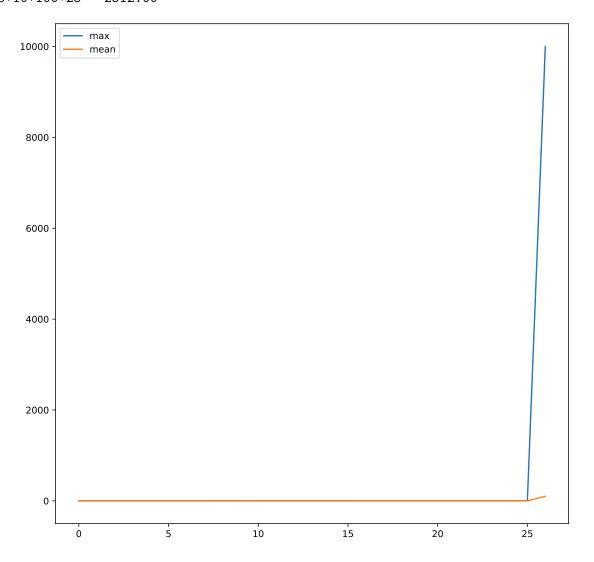
```
Generation 0: fitness min: 0.10, max: 0.50, mean: 0.21; best agent: 100 = 100.00 Generation 1: fitness min: 0.12, max: 0.50, mean: 0.35; best agent: 100 = 100.00 Generation 2: fitness min: 0.13, max: 0.50, mean: 0.42; best agent: 100 = 100.00 Generation 3: fitness min: 0.13, max: 0.50, mean: 0.46; best agent: 100 = 100.00 Generation 4: fitness min: 0.18, max: 0.50, mean: 0.47; best agent: 100 = 100.00 ... lines omitted ... Generation 22: fitness min: 0.30, max: 1.33, mean: 0.67; best agent: 10+3+25*100 = 2513.00
```

```
Generation 23: fitness min: 0.27, max: 1.33, mean: 0.71; best agent: 10+3+25*100 = 2513.00

Generation 24: fitness min: 0.30, max: 1.33, mean: 0.67; best agent: 10+3+25*100 = 2513.00

Generation 25: fitness min: 0.25, max: 1.33, mean: 0.71; best agent: 3+10+25*100 = 2513.00

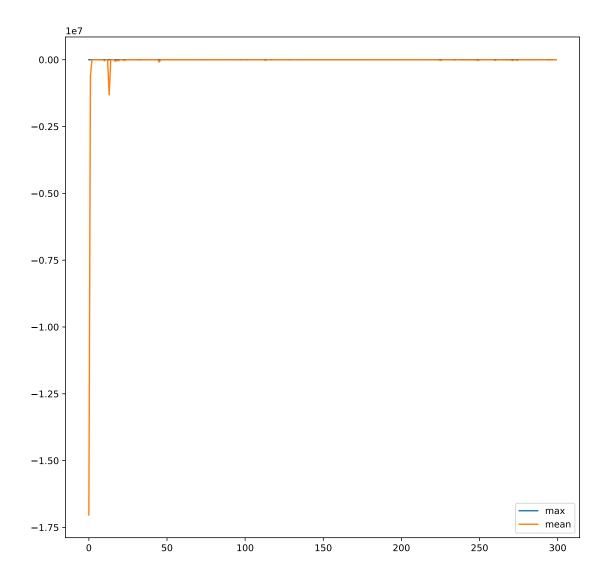
Generation 26: fitness min: 0.30, max: 10000.30, mean: 100.72; best agent: 5-3+10+100*25 = 2512.00
```



```
fitness_length_2,
    select_best_plus_random,
    crossover,
    mutation,
    fitness_threshold=0,
    mutation_probability=0.4, survival_probability=0.2, max_iterations=300,
    verbose=True, keep_best=False, plot=True
)

Generation 0: fitness min: -1687501777.00, max: -33.58, mean: -17032506.61; best
agent: 3-10/5-25/3/5+5/100*25-5+25*100+10/5*10 = 2515.58
Generation 1: fitness min: -29995176.15, max: -33.58, mean: -606836.21; best
```

```
agent: 3-10/5-25/3/5+5/100*25-5+25*100+10/5*10 = 2515.58
Generation 2: fitness min: -123210.98, max: -33.58, mean: -3373.95; best agent:
3-10/5-25/3/5+5/100*25-5+25*100+10/5*10 = 2515.58
Generation 3: fitness min: -252341.00, max: -30.02, mean: -5014.97; best agent:
3/5+5/100*25-5+10/3/25-5+25*100+10/5*10 = 2511.98
Generation 4: fitness min: -122507.58, max: -30.02, mean: -2641.06; best agent:
3/5+5/100*25-5+10/3/25-5+25*100+10/5*10 = 2511.98
... lines omitted ...
Generation 295: fitness min: -22506.00, max: -8.00, mean: -1565.32; best agent:
10+25*100 = 2510.00
Generation 296: fitness min: -247506.00, max: -8.00, mean: -7072.95; best agent:
25*100+10 = 2510.00
Generation 297: fitness min: -22494.00, max: -8.00, mean: -1462.92; best agent:
25*100+10 = 2510.00
Generation 298: fitness min: -2580.00, max: -8.00, mean: -1221.17; best agent:
25*100+10 = 2510.00
Generation 299: fitness min: -122496.00, max: -8.00, mean: -2515.62; best agent:
10+25*100 = 2510.00
```



Depending on the fitness function we get either shorter but slightly incorrect expression or long and correct one.