

PAC Learning

1. H_1 is consistent with a set of training examples (D) if and only if $H_1(x) = C(x)$ for training examples $(x, c(x))$ in D. It is given that, H_1 is identical to the set of all possible target concepts C , hence H_1 is consistent.

2. Given 20 parameters, $|H_1| = 2^{20}$

3. The number of training examples required to learn would be given by:

$$m \geq \frac{1}{\epsilon} \left(\ln |H| + \ln \left(\frac{1}{\delta} \right) \right)$$

Given: $\epsilon = 0.01, 1 - \delta = 0.95$

$$m \geq 72,682,050$$

4. No, the given Hypothesis H_2 is not consistent as this is not identical to C for all the training examples as in H_2 (x_a, x_b) map to X whereas in C which is identical to H_1 , X as a vector maps to Y .

5. Given that there are 20 x_a and x_b , $|H_2| = (n * (n - 1) / 2) * 16 = 3,040$

6. The minimum number of training examples can be calculated as above:

$$m \geq 1,102$$

7. Hypothesis H_2 has a higher bias since it has a lower number of features as compared to $|H_2|$.