

# The New Keynesian Transmission Mechanism: A Heterogenous Agent Perspective\*

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## Abstract

The success of the textbook three-equation New Keynesian textbook model stems from its capability to match the response of output to innovations in monetary policy. We reexamine the transmission channel of the textbook model and show that this successful result depends on the assumption that firm profits are redistributed to working households. Because these profits are large and respond countercyclically, labor supply increases after an expansionary monetary policy shock. We contrast the textbook model to a simple modification where profits are consumed by non-working capitalists. This modification renders output unresponsive to monetary policy. Expanding the textbook model with sufficiently rigid labor markets, the response of profits is no longer instrumental for the response of employment and output.

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# 1 Introduction

[NK under CM studied as approx.] New Keynesian models are often studied under the assumption of complete market [homogenous agents]. This assumption seems hard to square with the empirical evidence [Source?], but the relevance of the models can still be justified insofar as they serve as useful approximations of a world with incomplete markets.

[We challenge this presumption] In this paper we challenge this presumption. Specifically, we construct a simple heterogeneous agent perturbation of the 3-equation textbook New-Keynesian model (?). Here two classes of agents exist: workers supply labor and only receive labor market income, while capitalists receive firm profits and do not supply any labor. To make the argument clear, we first consider the case without financial trade between workers and capitalists. This perturbation of the text-book model is not capable of matching the VAR evidence on monetary and productivity shocks. Output is invariant to monetary policy shocks, and hours is invariant to productivity shocks.

[Intuition] The intuition behind this result lies on the model's supply side. This is often ignored in the exposition of New Keynesian models with complete markets, but lies at the heart of the transmission mechanism. Indeed, since the worker is operating on her intratemporal optimality condition, labor supply is governed by substitution and income effects. As the model exhibits balanced growth path preferences, these two will cancel out in the absence of a source of non-labor income. Consequently, wage changes will not be able to affect labor supply, why output becomes invariant to both monetary and productivity shocks.

[Highlights counter-factual in the textbook model] Our result also highlights a counter-factual, but unappreciated, feature of the transmission mechanism of the New-Keynesian textbook model. Usually, the demand side of the transmission mechanism in this model is emphasized.<sup>1</sup> However, as in any general equilibrium model, the movement in output must not only be consistent with consumption demand, but also with the supply of factor inputs, which in the textbook model solely consist of labor. To make labor supply move in response to a monetary shock, the size and distribution of profits play a key role. First, the mere existence of profits in the budget set of the representative agent decreases the relative income effect, and thus allows wages to affect labor supply even in the presence of balanced growth path preferences. This effect is sizable since profits make up 45 % of steady state output under a standard calibration of the textbook model. Second, owing to sticky prices average markups and profits respond countercyclically to monetary policy. This gives rise to a countercyclical income effect on labor supply, which helps to increase labor supply in response to a decrease in the nominal interest rate and *vice versa*.

[Generality of argument.] Our argument also has relevance in less stylized New-Keynesian setups. Al-

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<sup>1</sup>The standard intuition is that subject to a surprise increase in the nominal interest rate, the real interest rate increases due to sticky prices, and aggregate demand falls due to intertemporal substitution. Since, in the absence of capital, consumption equals output in equilibrium, output falls.

lowing for bond-trade between the two classes of agents still leaves output invariant to both monetary and productivity shocks [?]. Moreover, when augmenting the model with standard degree of wage stickyness the output response in the heterogenous agent perturbation is still XX % smaller than under the complete market assumption.

[Literature on NK models with agent heterogeneity] Our analysis connects to the recent literature analyzing the effect of household income and wealth heterogeneity in New-Keynesian environments, since our worker-capitalist model can be seen as highly stylized model of the same type of heterogeneity. ? studies amplification of monetary policy through redistribution and heterogeneity in marginal propensities to consume. ? studies how the precautionary savings motive affects the responsiveness to forward-guiding monetary policy. ? and ? studies richer model to uncover the effect of job uncertainty and automatic stabilizers.

[Literature using the text-book model] Secondly, the paper relates to the literature using the 3-equation model for analysis of the business cycle and business cycle policy. To name a few, ? studies the effect of news shocks. ? analyzes government spending multipliers. ? characterize optimal fiscal and monetary policy at the zero lower bound.

[Organization.] The remainder of the paper is organized as follows. In Section XX we set up our heterogeneous agent perturbation of the standard 3-equation model and relate it to the textbook model. In Section XX we use these two models to analyze monetary and TFP shocks. Section XX discusses how our results extend to a heterogenous agent model with financial trade, while Section XX discusses how the existence of wage stickyness affect our results. Section XX concludes.

## 2 Two models

We refer to the model described in ? Ch. 3 as the *standard model*. As a tool for investigating the transmission mechanism in the standard model, we will compare the impulse-responses of this model to a model where we give the profit income to a non-working household. We name the latter model the *worker-capitalist model*. In this section we describe the setup of these two models. Apart from the household sector, the models are identical in the way firm set prices and how the central bank sets the interest rate. Since these components are well-known, we will describe them only briefly.

As for notation, if not otherwise stated we will for any variable  $X_t$  denote its steady state value with  $\bar{X}$ , its value in the equilibrium under flexible price setting with  $X^n$  (the natural equilibrium), its log value with  $x_t$ , its log deviation from steady state with  $\hat{x}_t$  and its deviation from the flex price equilibrium with  $\tilde{x}_t$ .

### 2.1 The standard model: The representative household

The standard model has a representative household. This household derives utility from consuming a final good and disutility from working. It collects wage and profit income and can trade in a risk free nominal bond in zero net supply. The representative household's problem is

$$\begin{aligned} \max_{C_t, B_{t+1}, N_t} \quad & E_0 \sum_{t=0}^{\infty} \beta^t \left( \frac{C_t^{1-\sigma}}{1-\sigma} - \frac{N_t^{1+\varphi}}{1+\varphi} \right) \\ \text{s.t.} \quad & P_t C_t + Q_t B_t \leq B_{t-1} + W_t N_t + P_t D_t \end{aligned}$$

where  $P_t$  denotes the price level,  $C_t$  real consumption,  $Q_t$  the nominal price of the bond  $B_t$ ,  $W_t$  the nominal wage level,  $N_t$  labor supply and  $D_t$  real profit income. The solution is characterized by an Euler equation and an intratemporal optimality condition:

$$\begin{aligned} Q_t &= \beta E_t \left\{ \frac{C_{t+1}^{-\sigma}}{C_t^{-\sigma}} \frac{P_t}{P_{t+1}} \right\} \\ \frac{W_t}{P_t} C_t^{-\sigma} &= N_t^{\varphi} \end{aligned}$$

Log-linearizing around the flex-price equilibrium, we find

$$\tilde{c}_t = -\frac{1}{\sigma} (i_t - E_t \pi_{t+1} - \rho) + E_t \tilde{c}_{t+1} \quad (1)$$

$$\tilde{\omega}_t = \varphi \tilde{n}_t + \sigma \tilde{c}_t \quad (2)$$

where  $\omega_t = w_t - p_t$ ,  $\rho = -\log \beta$ ,  $i_t = -\log Q_t$  and  $\pi_t = p_t - p_{t-1}$ .

The goods market clears when

$$C_t = Y_t$$

where  $Y_t$  is total output. The bond market clears when  $B_t = 0$ , which implies that

$$C_t = \frac{W_t}{P_t} N_t + D_t$$

Log-linearizing around the flex-price equilibrium, we find

$$\tilde{c}_t = \tilde{y}_t \quad (3)$$

$$\tilde{c}_t = \bar{S}(\tilde{\omega}_t + \tilde{n}_t) + (1 - \bar{S})\tilde{d}_t \quad (4)$$

where  $\bar{S} = \frac{\bar{W}\bar{N}}{\bar{Y}\bar{P}}$  is the steady state labor income share of output.

## 2.2 The worker-capitalist model: The households

The worker-capitalist model is constructed with the purpose of isolating the effect of profits in the standard model. It has a representative worker and a representative capitalist. The worker can trade in a risk-less bond while the capitalist is constrained to be hand-to-mouth. This simplifying assumption implies that in equilibrium, each household consumes neither more nor less than its factor income, and enables us to ignore the evolution of the wealth distribution. An alternative specification would constrain the worker to be hand-to-mouth while allowing the capitalist to trade in the bond market. These two models have the same implications for the determination of labor supply, since both imply that the worker only consumes labor income in equilibrium. However, as discovered by ?, the model with a constrained worker has no determinate log-linear equilibrium under a standard Taylor rule. To be able to keep the rest of the model exactly the same as the standard model, we therefore constrain the capitalists instead.

Disallowing financial trade between the two households may seem as a non-innocent assumption. As a robustness check, we will in Section ?? consider a model where financial trade between the households is allowed. For reasonable calibrations, the results are not significantly affected.

The worker derives utility from consuming the final good and disutility from working. She collects wage income and can trade in a risk free nominal bond. In contrast to the representative household in the standard model, she does not receive any profit income. The worker's problem is

$$\begin{aligned} \max_{C_{wt}, B_{wt+1}, N_t} \quad & E_0 \sum_{t=0}^{\infty} \beta^t \left( \frac{C_{wt}^{1-\sigma}}{1-\sigma} - \frac{N_t^{1+\varphi}}{1+\varphi} \right) \\ \text{s.t.} \quad & P_t C_{wt} + Q_t B_{wt} \leq B_{wt-1} + W_t N_t \end{aligned}$$

The solution is characterized by an Euler equation and an intratemporal optimality condition:

$$\begin{aligned} Q_t &= \beta E_t \left\{ \frac{C_{wt+1}^{-\sigma}}{C_{wt}^{-\sigma}} \frac{P_t}{P_{t+1}} \right\} \\ \frac{W_t}{P_t} C_{wt}^{-\sigma} &= N_t^{\varphi} \end{aligned}$$

Log-linearizing around the flex-price equilibrium, we find

$$\tilde{c}_{wt} = -\frac{1}{\sigma}(i_t - E_t\pi_{t+1} - \rho) + E_t\tilde{c}_{wt+1} \quad (5)$$

$$\tilde{\omega}_t = \varphi\tilde{n}_t + \sigma\tilde{c}_{wt} \quad (6)$$

The capitalist receives profits and consumes them hand-to-mouth. The capitalist's problem is

$$\begin{aligned} \max_{C_{ct}} \quad & E_0 \sum_{t=0}^{\infty} \beta^t \left( \frac{C_{ct}^{1-\sigma}}{1-\sigma} \right) \\ \text{s.t.} \quad & P_t C_{wt} \leq P_t D_t \end{aligned}$$

The goods market clears when

$$C_{wt} + C_{ct} \leq Y_t$$

where  $Y_t$  is total output. The bond market clears when  $B_{wt} = 0$  which implies that

$$C_{wt} \leq \frac{W_t}{P_t} N_t$$

Log-linearizing around the flex-price equilibrium, we find

$$\bar{S}\tilde{c}_{wt} + (1 - \bar{S})\tilde{c}_{ct} = \tilde{y}_t \quad (7)$$

$$\tilde{c}_{wt} = \tilde{\omega}_t + \tilde{n}_t \quad (8)$$

where  $\bar{S} = \frac{\bar{W}\bar{N}}{\bar{Y}\bar{P}}$  is the steady state labor income share of output.

### 2.3 Other model components

The production sector, the firm pricing problem and the central bank response function is identical in the two models and follows ? Ch. 3. We describe them briefly here.

There is a representative firm that produces the final good  $Y_t$  by combining a continuum of intermediate goods  $Y_{it}$  through the Dixit-Stiglitz aggregator with elasticity of substitution  $\epsilon_p$ . These intermediate goods are produced by a continuum of firms, indexed by  $i$ , with technology  $Y_{it} = A_t N_{it}^{1-\alpha}$ . The intermediate goods producers set their prices to maximize present discounted profits with the market discount factor  $Q_t$ . They can, however, only reset their prices with probability  $1 - \theta_p$  in every period. From these assumptions we can derive a log-linear relationship between inflation and the deviation of average marginal cost from steady state:

$$\pi_t = \beta E_t \pi_{t+1} + \lambda \hat{m}c_t \quad (9)$$

where  $\lambda = \frac{(1-\theta_p)(1-\beta\theta_p)}{\theta_p} \frac{1-\alpha}{1-\alpha+\alpha\epsilon_p}$ .

The model is closed by assuming that a central bank sets the interest rate according to a log-linear Taylor rule:

$$i_t = \rho + \phi_\pi \pi_t + \phi_y \tilde{y}_t + \nu_t \quad (10)$$

## 2.4 Parameterization

All parameters are the same in the two models. We choose the same calibration as that in ? Ch. 3. A time period should be interpreted as a quarter of a year. We set an elasticity of intertemporal substitution  $1/\sigma = 1$  (which is a special case of KPR preferences), Frisch elasticity  $\varphi = 1$ ,  $\alpha = 1/3$ ,  $\epsilon_p = 6$ ,  $\theta_p = 2/3$ ,  $\beta = 0.99$ . For the Taylor rule, we set  $\phi_\pi = 1.5$ ,  $\phi_y = 0.125$ .

For this parameterization, it is easily confirmed that the log-linear equilibrium system of both models has a unique stable solution.

### 3 Impulse-responses to a monetary policy shock

We now consider how the two models respond to the same innovation in the policy rate. We assume that innovations in the policy rate follow the process

$$\nu_t = \rho_\nu \nu_{t-1} + \epsilon_{\nu t}$$

with  $\rho_\nu = 0.5$ . We feed a positive 25 basis point shock to the models. The responses are plotted in Figure ???. In the figure, we plot deviations from the flex price equilibrium. We will refer to these deviations as "gaps".

As can be seen in Figure ??, the models respond qualitatively similar in terms of the real interest rate gap, inflation, real wages and profits. However, in the standard model, there is a substantial negative response of output and employment whereas in the worker-capitalist model, there is no response at all.

We start analyzing the responses of the worker-capitalist model, as the insights from this exercise will better enable us to uncover the mechanism in the standard model. Looking at the right-hand side of ??, we see that in response to the surprise increase in the nominal interest rate, the real interest rate increases. From the Euler Equation (??), we then know that the worker consumption gap must start out negative to follow an upward sloping path. The worker income gap must follow the same path, as worker consumption equals worker income in equilibrium. Hence, either wages, labor supply or both must initially fall. We see that it is only real wages that falls while labor supply does not move.

Why is there no response in labor supply? Because of the parametric assumption of  $\sigma = 1$  (KPR-preferences), the income and substitution effect with respect to changes in the wage level cancel. To see this, insert the market clearing condition (??) in the intratemporal optimality condition (??):

$$\begin{aligned} \varphi \tilde{n}_t + \sigma \tilde{c}_t &= \tilde{\omega}_t \\ \Rightarrow \tilde{\varphi} n_t + \sigma(\tilde{\omega}_t + \tilde{n}_t) &= \tilde{\omega}_t \\ \Leftrightarrow (\varphi + \sigma)\tilde{n}_t &= (1 - \sigma)\tilde{\omega}_t \end{aligned}$$

and under  $\sigma = 1$ :

$$\tilde{n}_t = 0$$

Since labor supply cannot move, the fall in worker consumption matches the fall in wages. And because wages fall, so does the marginal cost of production, which leads to a fall in inflation and an increase in profits. The countercyclical response of profits, however, has no effect on the equilibrium since it is consumed by the hand-to-mouth capitalists.

Having explained the responses in the worker-capitalist model, it is now easy to understand the standard model responses. As in the worker-capitalist model, the real interest rate gap increases, which leads to a fall



in the consumption gap. There is also a fall in the real wage gap and an increase in the profit gap. However, in contrast to the worker-capitalist model now hours worked and the output gap decreases. To explain this, we again insert in the market clearing condition (??) in the intratemporal optimality condition (??):

$$\begin{aligned}
& \varphi \tilde{n}_t + \sigma \tilde{c}_t = \tilde{\omega}_t \\
\Rightarrow & \quad \varphi \tilde{n}_t + \sigma \left( \bar{S}(\tilde{\omega}_t + \tilde{n}_t) + (1 - \bar{S})\tilde{d}_t \right) = \tilde{\omega}_t \\
\Leftrightarrow & \quad (\varphi + \sigma \bar{S})\tilde{n}_t = (1 - \sigma \bar{S})\tilde{\omega}_t - \sigma(1 - \bar{S})\tilde{d}_t
\end{aligned}$$

and under  $\sigma = 1$ :

$$\tilde{n}_t = \frac{1 - \bar{S}}{\varphi + \bar{S}}(\tilde{\omega}_t - \tilde{d}_t)$$

where  $\frac{1 - \bar{S}}{\varphi + \bar{S}}$  is decreasing in  $\bar{S}$  on the unit interval. Under the current parameterization, the labor share of income is close to 55 per cent. Because profits increase in response to the shock, the representative household experiences a direct income effect which depresses labor supply. This effect is naturally decreasing in the steady state labor share, as seen in (??). We also see that as the labor share decreases, the response of labor supply to changes in the real wage increases. With a larger profit income share in steady state, the relative income effect of wage changes is depressed. The labor supply schedule then become less downward sloping, and labor supply becomes more responsive to changes in the real wage level, even though we have KRP preferences.

The standard model is thus capable to generate negative responses of employment and output to a positive innovation in the policy rate because the steady share of profit is substantial and because these profits respond countercyclically. When returned to the representative household, its responsiveness of labor supply to real wages increase while it experiences a negative income effect to monetary policy shocks.

This transmission mechanism does not seem reasonable. Few households have substantial non-labor income and there is, to our knowledge, no evidence that profit income responds procyclically to monetary policy shocks.<sup>2</sup>

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<sup>2</sup>The VAR evidence presented by ? shows that firm profits respond procyclically to monetary policy shocks.

## 4 Robustness: Allowing financial trade

In the setup of the worker-capitalist model, we disallowed financial trade between the two households. We made this assumption to simplify the analysis. As a robustness exercise, we will in this section consider the case where we allow financial trade.

Without further assumptions, allowing the capitalist to trade in the bond market implies that the model becomes non-stationary. In response to a monetary policy shock, we have seen that real wages respond procyclically and profits respond countercyclically. One household will therefore become indebted to the other. The consumption smoothing motive makes this indebtedness permanent. Hence, after a monetary policy shock, the equilibrium does not converge back to the steady state from which it started.

To allow for financial trade in the model we therefore assume that the capitalist faces quadratic bond holding costs, which ensures that the capitalist holds zero financial wealth in the long-run equilibrium. This assumption is commonly used to close two-country international macro models, see e.g. (?).

Thus, we change the capitalist problem described in Section ?? to

$$\begin{aligned} \max_{C_{ct}, B_{ct}} \quad & E_0 \sum_{t=0}^{\infty} \beta^t \left( \frac{C_{ct}^{1-\sigma}}{1-\sigma} \right) \\ \text{s.t.} \quad & P_t C_{wt} + Q_t B_{ct} \leq B_{ct-1} + P_t D_t - \frac{\zeta}{2} B_{ct-1}^2 \end{aligned}$$

with the associated Euler equation

$$Q_t = \beta E_t \left\{ \frac{(1 - \zeta B_{ct}) C_{ct+1}^{-\sigma}}{C_{ct}^{-\sigma}} \frac{P_t}{P_{t+1}} \right\}$$

Log-linearizing around the flex-price equilibrium, we find

$$\tilde{c}_{ct} = -\frac{1}{\sigma} (i_t - E_t \pi_{t+1} - \rho) + E_t \tilde{c}_{ct+1} + \zeta Y_t^n \tilde{b}_{ct} \quad (11)$$

where  $\tilde{b}_{ct}$  is defined as  $\tilde{b}_{ct} = \frac{B_{ct}}{Y_t^n}$ , i.e. the private debt-to-GDP ratio, where GDP is measured by its flex price value.

The goods and bond market clearing conditions are now

$$\begin{aligned} C_{wt} + C_{ct} + \frac{\zeta}{2} B_{ct-1}^2 &= Y_t \\ B_{ct} + B_{wt} &= 0 \end{aligned}$$

In the flex-price equilibrium, the labor share of GDP is constant and so there are no gains from financial trade. Thus  $B_{ct}^n = B_{wt}^n = 0$ . Using this and log-linearizing around the flex-price equilibrium, we find

$$\bar{S} \tilde{c}_{wt} + (1 - \bar{S}) \tilde{c}_{ct} = \tilde{y}_t \quad (12)$$

$$\tilde{c}_{wt} = \tilde{\omega}_t + \tilde{n}_t \quad (13)$$

The rest of the worker-capitalist model is unaffected.<sup>3</sup>

Before showing results, we need to calibrate  $\zeta$ . Because wages respond strongly and procyclically and profits respond strongly and countercyclically, the gains from trade between the capitalist and the worker after a monetary shock are very large. When  $\zeta \rightarrow 0$ , the debt-to-GDP ratio increases from 0 to a peak response of 92 percent, or a debt-to-worker income of 166 percent, to a 25 basis point shock with half-life of one quarter. We calibrate  $\zeta$  by constraining the response in this variable. Although still implausibly large, we constrain the debt-to-GDP to not respond more than 10 percent at peak, which implies that  $\zeta = 3$ .

We feed in the same monetary shock as in the previous section. The responses are plotted in Figure ?? . As can be seen, the worker-capitalist model still has virtually no response in output and employment. Why is this? Because the debt response is limited to 10 percent of GDP, worker consumption is still close to labor income in every period. Hence, the determination of labor supply is similar to the model without financial trade between the two households. Workers do not experience the positive income effect coming from the increase in profits. And with KRP-preferences, the income and substitution effect is still approximately of the same size, and there is no response to changes in the wage level.

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<sup>3</sup>Discuss convergence? With  $\zeta \rightarrow 0$  the log-linear solution to of this model converges to that of the standard model. With  $\zeta \rightarrow \infty$  it converges to that of the worker-capitalist model without trade.

## 5 Rigid wages: A solution

The only sources of frictions in the standard model are the assumptions of rigid price setting and monopolistic competition. Labor markets are assumed to operate without any frictions. This assumption is key for the transmission mechanism. With households reoptimizing their labor supply decision at high frequency, profits serve the dual role of producing a countercyclical income effect, as well as driving a wedge between labor income and consumption in the steady state. If constraining the households to not be able to reoptimize at high frequency, as is the case with sufficiently rigid wage setting, we should not expect this transmission mechanism to be operating.

In this section, we therefore explore whether assuming rigid wage setting escapes the implausible transmission mechanism of the standard model. We focus on one particular way of introducing rigid wage setting, the assumption of constant resetting probabilities (the "Calvo model") introduced by ?, which is frequently used in the literature. We will explore the role of profits in the same fashion as before; by comparing the impulse-responses of the representative agent economy to the worker-capitalist economy (without financial trade).

Constant wage resetting probabilities take the same form in both models. We only discuss the setup briefly here, for a full specification see ? Ch. 6. In the standard (worker-capitalist) model, we assume that there is a continuum of ex ante identical households (workers), indexed by  $j$ , that can trade complete state-contingent consumption claims among themselves. Each household (worker) is assumed to be a monopolistic supplier of its particular labor type and chooses  $W_{jt}$ . There is a representative intermediate aggregate factor producer that combines the particular labor types  $N_{jt}$  with the Dixit-Stiglitz aggregator into an aggregate factor input  $N_t$ , with elasticity of substitution  $\epsilon_w$ . As a consequence, each household (worker) faces labor demand schedule of the form

$$N_{jt} = \left( \frac{W_{jt}}{W_t} \right)^{-\epsilon_w} N_t \quad (14)$$

Under frictionless wage setting, households (workers) each period optimize over  $W_t$  to maximize their present discounted lifetime utility. However, households (workers) can only reset their wages with probability  $1 - \theta_w$  in each period. Conditional on resetting, households (workers) choose a wage level that maximizes their present discounted lifetime utility. Conditional on not being able to reset, they are constrained to supply the labor demanded given by (??).

From these assumptions, in addition to the model equations described in Section ??, the equilibria of both models are characterized by a "wage Phillips curve" and an accounting equation for the evolution of real wages:

$$\pi_t^w = \beta E_t \pi_{t+1}^w + \lambda_w \hat{\mu}_t \quad (15)$$

$$\omega_t^w = \omega_{t-1} + \pi_t^w - \pi_t + \Delta \omega_t^n \quad (16)$$

where  $\lambda_w = \frac{(1-\theta_w)(1-\beta\theta_w)}{\theta_w} \frac{1}{1+\epsilon_w\varphi}$  and  $\hat{\mu}_t$  is the log deviation of real wages from the average marginal rate of substitution between consumption and leisure for the households (workers).

As in ?, we set  $\epsilon_w = 6$  and  $\theta_w = \frac{3}{4}$ , which correspond to an average wage duration spell of four quarters. We feed in the same monetary shock as in the previous sections. The responses are plotted in Figure ??.

Before comparing the responses of the standard and worker-capitalist model, we discuss how adding wage rigidities in the standard model changes the responses compared to the flex price model responses shown on the left hand side of Figure ?. Adding wage rigidities to the standard model changes the magnitude of several responses. Most notably, it almost eliminates the response in real wages completely, as well as making the response of profits procyclical. The reason is that with rigid wage setting, nominal wages respond very little to the shock. Hence, nominal marginal costs of the intermediate goods firms respond only little. In response, the inflation response is muted but sufficiently strong to almost close the real wage gap. As the real wage gap is almost zero, the movement of profits is solely determined by the movement in output. Profits decrease because production decreases, but the effect is mitigated due to diminishing returns to scale.

Turning to the comparison of the responses between the standard and the worker-capitalist model, we see that they are almost indistinguishable. With an average wage resetting duration of 4 quarters, the income and substitution effects matter less for the determination of hours worked at the shorter horizon. The majority of households (workers) are instead constrained to supply whatever labor is demanded from equation (?). Labor demand follows directly from consumption demand, as labor is the sole factor of production. Thus, in response to the decline in consumption demand coming from the positive real interest rate gap in both models, output and hours worked are thus forced to adjust.

Assuming rigid wages thus seem to offer a solution to the implausible transmission mechanism in the textbook 3-equation model. In the appendix, we show that the difference between the standard and the worker-capitalist model is decreasing in  $\theta_w$ , which means that strength of this solution is increasing in the degree of wage rigidities. Whether the actual economies feature substantially rigid wage setting at the business cycle frequency is an empirical question to which we do not contribute in this paper. However, in light of our findings, to have accurate measures of the degree of rigidity seems important for proceeding with these class of model.

## 6 TFP shocks

Our paper has centered around the transmission mechanism of the standard model to monetary policy shocks. However, as we showed in Section ??, without the redistribution of profits to the representative household, labor supply is unresponsive to any movement in real wages. This is because without any non-labor income, KPR preferences implies that the income and substitution effect cancel with respect to changes in the wage level.

We follow this insight to investigate the transmission mechanism from TFP shocks to employment. In contrast to standard real business cycle models, the three-equation new-Keynesian model generates a fall in employment in response to a TFP shock. This impulse-response has been documented in US data (????), and has been interpreted as evidence in favor of the new-Keynesian model.

We proceed in the same fashion as in Section ?. We consider how the standard and the worker-capitalist models respond to the same innovation in TFP. We assume that innovations in TFP follows the process

$$a_t = \rho_a a_{t-1} + \epsilon_{at}$$

with  $\rho_a = 0.9$ . We feed a positive 1 percentage point shock to the models. The responses are plotted in Figure ?. Note that in the figure, we do not plot deviations from the flex price equilibrium, but rather deviations from steady state.

As seen in Figure ?, the standard model generates a fall in hours worked to the positive innovation in TFP. On the demand side, this response is often interpreted as an effect of the (suboptimal) Taylor rule. In response to the rise in TFP, the unit marginal cost of production falls, which generates a fall in inflation. The central bank then stimulates the economy through the Taylor rule, but not sufficiently to close the real interest rate gap. Although output rises, we then see a fall in the output gap and in hours worked.

Turning to the supply side, the increase in real wages has a positive effect on labor supply, *ceteris paribus*. This effect arises due to profit income being large in steady state, so that the relative income effect of wages is depressed. The fall in hours must therefore be a consequence of the large increase in profits, which brings a positive income effect.

Again, this transmission mechanism does not survive the worker-capitalist model. In this model, workers do not experience the positive income effect from the rise in profits. Workers only experience the rise in wages, but with KPR preferences, this does not affect labor supply. Hence, it is not only the design of monetary policy that is crucial for the response in hours in the standard model, but also the income effect from the large rise in profits.

## 7 Discussion

## References

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## A Figures

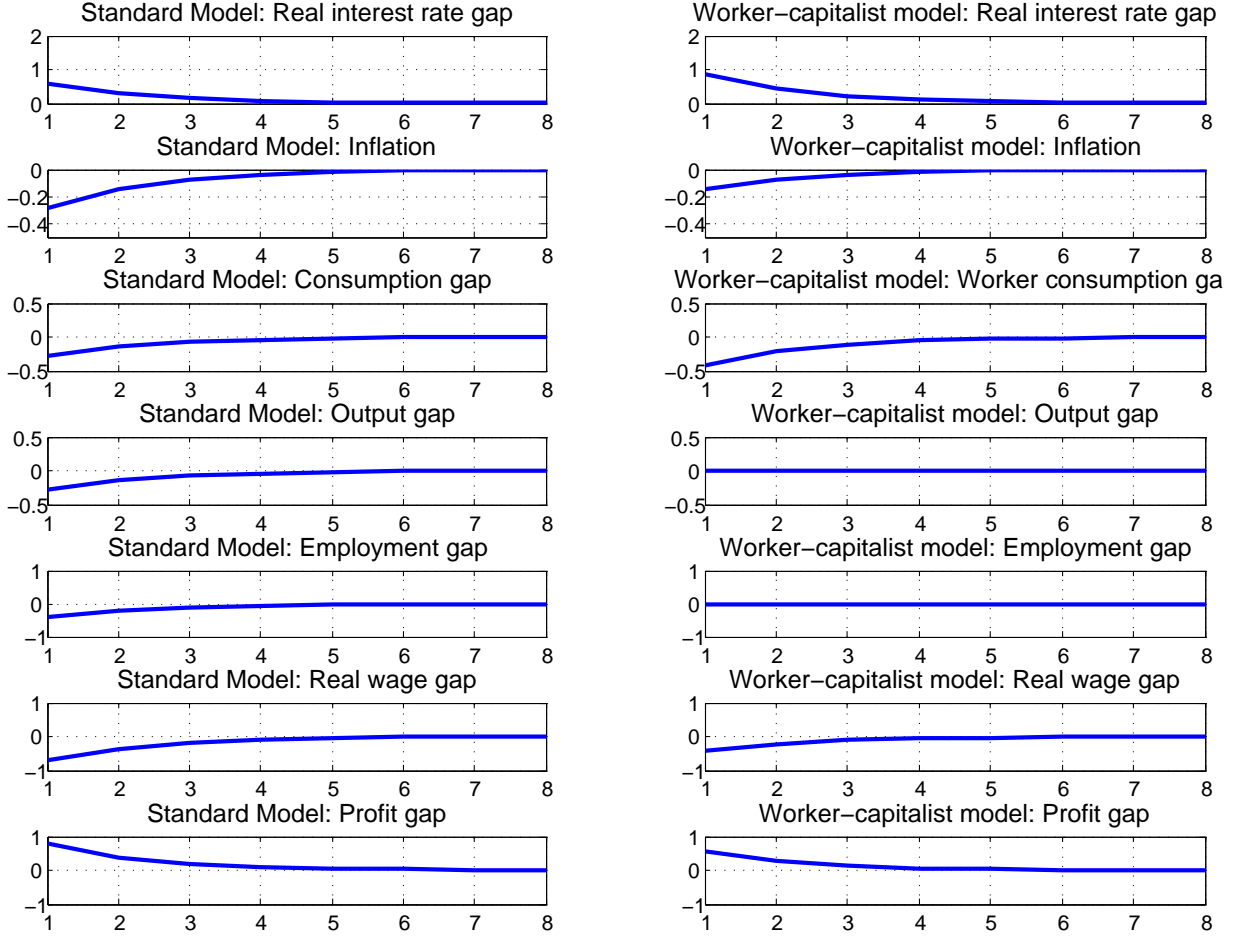


Figure 1: Equilibrium responses to positive 25 basis shock in the policy rate. The left panel shows the standard model, the right panel the worker-capitalist model. Inflation and interest rates are expressed in yearly terms, while the other variables are expressed in quarterly terms.

## B Derivations and Proofs

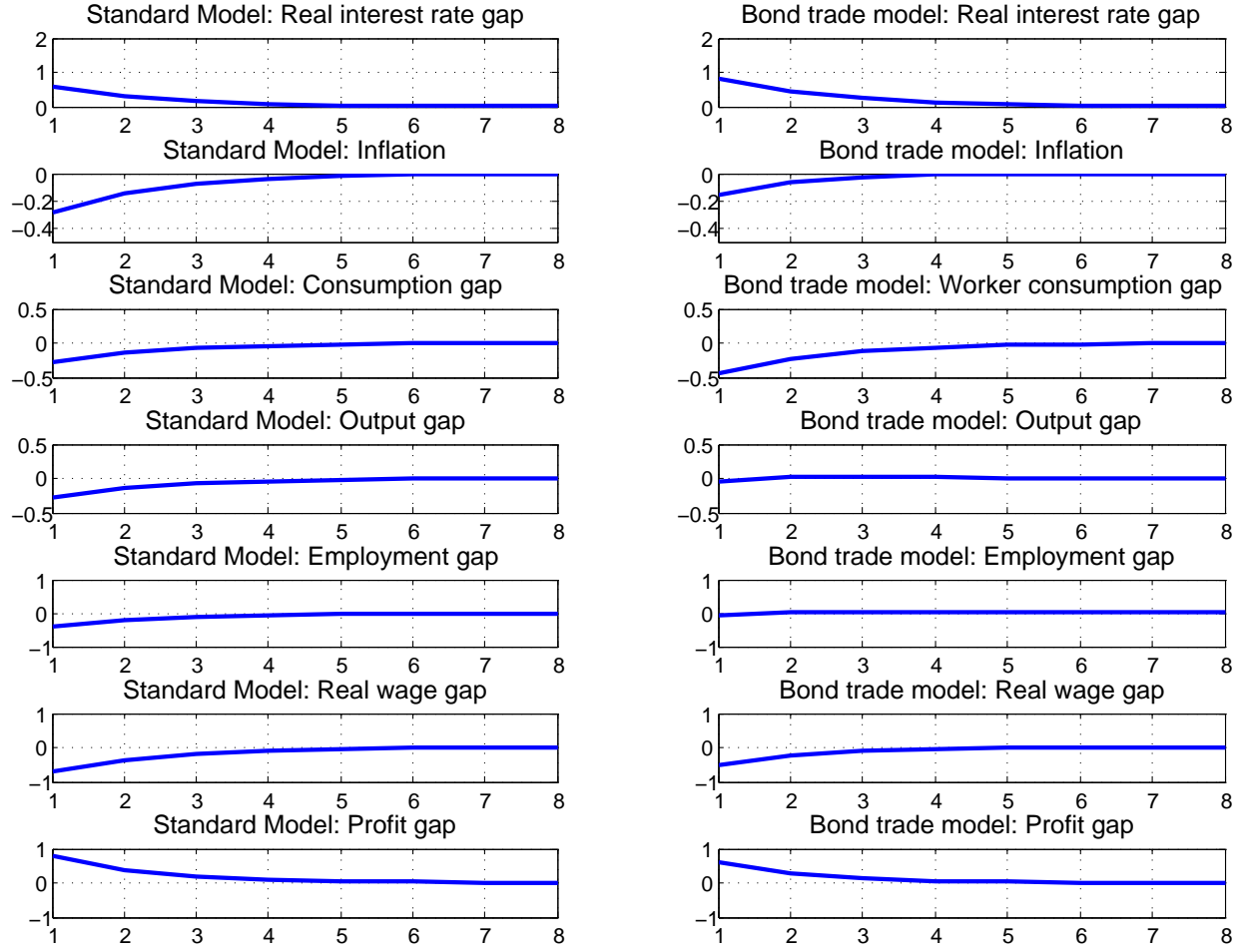


Figure 2: Equilibrium responses to positive 25 basis shock in the policy rate. The left panel shows the standard model, the right panel the worker-capitalist model with financial trade. Inflation and interest rates are expressed in yearly terms, while the other variables are expressed in quarterly terms.

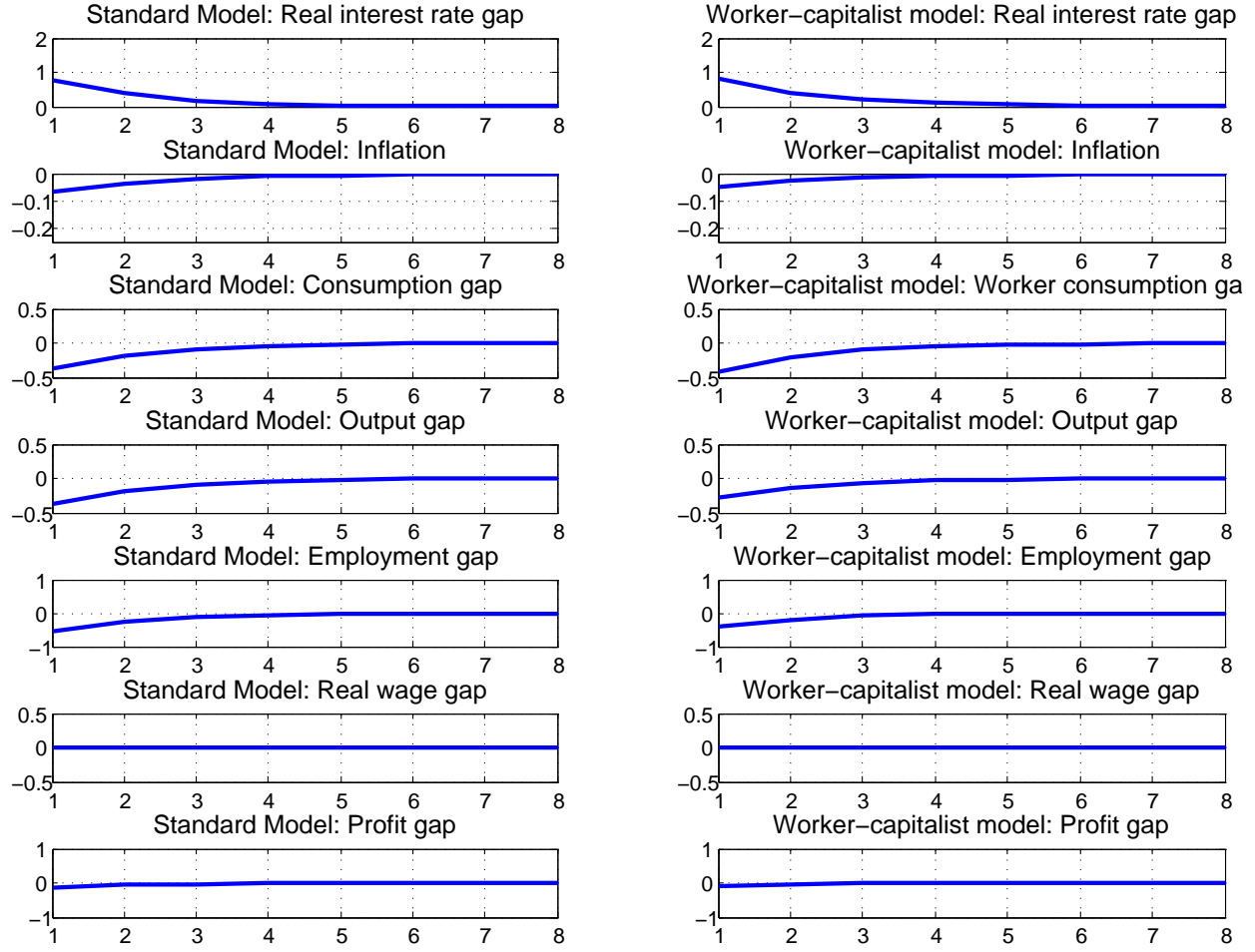


Figure 3: Equilibrium responses to positive 25 basis shock in the policy rate. The left panel shows the standard model, the right panel the worker-capitalist model. Inflation and interest rates are expressed in yearly terms, while the other variables are expressed in quarterly terms.

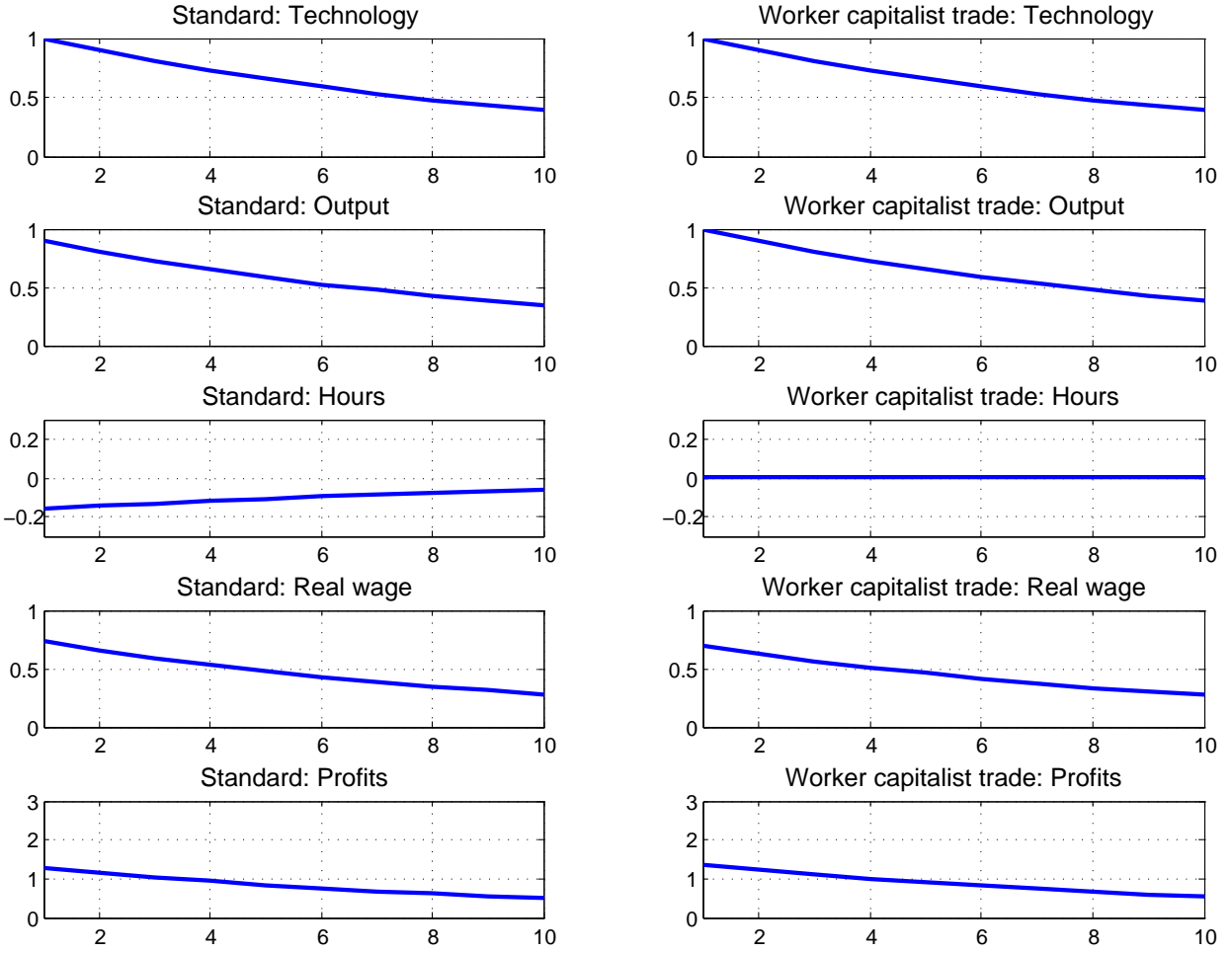


Figure 4: Equilibrium responses to positive 1 percentage point shock in TFP. The left panel shows the standard model, the right panel the worker-capitalist model.