

How Useful are Posted Job Openings?*

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— *preliminary and incomplete version - please do not circulate* —

Abstract

Policy makers and researchers often evaluate labor market efficiency using announced job openings and unemployment. It is well-known that announced job-openings only constitute a fraction of all job openings in the economy, but less is known about how this fraction varies across time and firms. To inform this discussion we construct a new database with actual hires and announced job openings using data from the Danish tax authorities and Public Employment Service during 2004-2012. Using this we find that only 10-25 percent of all hires are made through announced hires, which via a simple model translates into 5-20 percent of all job openings being announced. We also find that the share of hires via announced openings being increasing in firm size, decreasing in employment growth, less used in start-ups than in existing firms and share exhibits an inverse u-shape in the firm's average wage level. Second, we set up and calibrate a simple search-and-matching model with two recruitment channels: announced and unannounced job openings. Using this model we show how the observed swings in the fraction of posted job openings significantly influences the perceived matching efficiency and Beveridge curve movements.

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1 Introduction

Job openings is a key component in labor market analysis within the search matching framework. In the canonical search matching model (*e.g.* as presented in Pissarides (2000)) hires happens as unemployed workers and job openings created by firms meet via an aggregate matching function. The success of this framework stems from its ability to match the observed labor market behaviour over the business cycles. Indeed, in the model a positive productivity shock will increase the firms' payoff from a match and thus induce it to create more job openings. As the labor market becomes tighter hiring increases and unemployment falls.

Thus, time series for job openings are key when taking the model to the data. Unfortunately, our understanding of job openings is far from full. On a conceptual level the economic content of a job opening is not clear,¹ and there are also serious challenges in measurement. Indeed, time series for job openings are often based on postings in media or at public employment services. An obvious concern is that postings via these channels are not representative for all openings, and that the firm's propensity to use these channels can vary over time.²

Not accounting for these measurement problems can lead to spurious conclusions within the search matching framework and ultimately to misguided policy. In the search matching framework movements in the Beveridge curve can only be caused by exogenous shifts in (i) the match efficiency or (ii) the job destruction rate. This observation has influenced the policy discussion in the wake of the Great Recession, where the Beveridge curve relation appears to have adversely shifted in both the United States and in Europe.³ However, as we will argue more precisely below shifts in the Beveridge curve can also be caused by change in firms recruitment behavior. Indeed, if firms substitute between observed postings and other channels this can also shift the Beveridge curve.⁴

In this paper we use new Danish data and a simple theoretical framework in order to inform this discussion. Specifically, we construct a database with firm level data on hires and job postings. Using this we compute the amount of announced and unannounced job openings and document how the share varies across time. We

¹Abraham (1983) defines a job opening as unmet labor demand, but Elsby, Michaels, and Ratner (Elsby et al.) suggest this definition could be misleading as (1) while it is relatively straightforward to identify a idle worker it is less so to identify idle resources at the firm level, (2) it is difficult to identify the amount of desired production not being undertaken due to an unfilled opening and (3) firms might choose to recruit for positions in anticipate of these being opened in the future.

²The establishment of the US Job Opening and Labor Turnover (JOLTS) Survey in December 2000 has eased these concerns. Instead of relying on job-postings JOLTS is a survey and defines a job openings as a position for which (i) work could start within 30 days and (ii) the employer is *actively recruiting* for outside the firm. However, the JOLTS only goes back to 2000 for the US and a similar surveys for Europe only exists from 2008.

³*E.g.* The president of the European Central Bank, Mario Draghi, in his speech at Jackson Hole 2015 observed: “*The euro area Beveridge curve [...] suggests the emergence of a structural mismatch across Euro area labor markets*” (Draghi, 2014).

⁴We are not new to make such a claim. Indeed, Davis et al. (2013) argue that changes in the *recruitment intensity* of firms can shift the matching function.

calibrate a simple search matching model to imitate this variation and show how this can create a shift in the perceived Beveridge curve.

We find that that only 10-25 percent of all hires during 2004-08 were made through announced openings. Using our model this translates into 5-20 percent of all job openings being announced. We find considerable variation in the use of announced openings across firm characteristics with the share of hires via announced openings being increasing in firm size, decreasing in employment growth and less used in start-ups than in existing firms. Moreover, the it exhibits an inverse u-shape in the average wage level of the firm with low and high wage firms relying the least on announced openings. We also use our calibrated model to show how decrease in the share of announced hires from 20 to 10 percent leads to a 40 percent increase in the perceived matching efficiency.

Our paper relates to a number of papers in the literature. Most close in spirit is Davis et al. (2013) who analyzes hires and job-openings (JOLTS) in the US. They find that changes in the recruitment intensity of firms partly explains the recent breakdown in the standard matching function. Previously a vast literature has related the aggregate number of job-openings, unemployed and hires through the canonical search matching model (e.g. Blanchard and Diamond (1990)). Especially relevant from this literature strand are papers using job-openings from centralized registers (Coles et al., 1996; Albaeck and Hansen, 2004; Yashiv, 2000; Sunde, 2007). Also related is the literature that analyzes the determinants of job-opening durations (Ours and Ridder, 1991; Burdett and Cunningham, 1998; Barron et al., 1997; Holzer, 1990).

The paper is organized as follows. Section 2 presents our data and shows how hires with and without observed job-openings vary across time and worker characteristics. Section 3 sets up a search matching model with announced and unannounced job-openings which we use along with the data we back of the share of unannounced openings and assess the fluctuations in this share impact on the perceived matching efficiency. Section 4 concludes and offers some thoughts on remaining work.

2 Data and definitions

We use data from four sources: (1) Job Openings from the Public Employment Service. (2) The tax records for the entire Danish working population. (3) Administrative registers from Statistics Denmark. (4) Data on unemployment from Statistics Denmark.

The job openings dataset contains all vacancies announced at the Public Employment Service from 2004 to 2013. For each opening we have a firm identifier (CVRNR), the number of positions available, the day the opening was announced, and the day the announcement was withdrawn. For all firms in Denmark we have the tax records, that contains a firm identifier (CVRNR), a personal identifier (CPR), the salary, and the first and last working day for each employee. We use the data on

the first and last day at work to construct the actual number of hires at each point in time. The administrative registers from Statistics Denmark provides information on all individuals demographics (gender, age, origin) and socio-economic background (education, employment type, income, wealth). The administrative registers also contain firm-level characteristics such as sector, size, and industry.

2.1 Definitions

An *announced job opening* is defined using the job openings dataset by the date the job posting was withdrawn, as this most likely is the last day the job seeker could apply for this job. We assess this assumption by collecting job postings from the online archive of the private provider “Jobindex.dk” of which the announcements at the public Employment Service is a subset. This data is useful as it contains data for the expected starting date and the date for withdrawal of the job posting. Figure 1 shows the distribution of months from deadline to job starting date. For a considerably fraction of the announcements the job starting is set to as soon as possible (asap). Figure 1b shows that most non-asap postings have a job starting date within two months of the deadline. As a consequence we will evaluate the sensitivity of our analysis to setting the job starting day at three, two, one, or zero months after the deadline.

[Figure 1 about here.]

A *job hire* is defined using the tax records. The hiring day is defined as the starting day of the an employment spell if the individual was not employed with the same firm in the previous 30 days.

For each job spell we define a new hire by the first working day of the year if the individual did not work at the same firm within 30 days before that hire. We only consider job hires where the job duration is more than 5 days. In 2008 the 271 municipalities in Denmark were merged to 99, and the 15 counties were replaced by five regions. A considerable number of public employees thus started working for a new employer on January 1st 2008. To separate these job starts from real job change, we use information from the Statistics Denmark on the year the employee started in the current job. For job-starts on January 1st 2008 we furthermore consider information on the firm size and the individual wage. If the individual was employed at a job in December 2011 with the same wage and/or firm size as the job start on January 1st, the new spell is not recorded as a new hire.

An *announced hire* is defined as a hire in a firm where an announced job-opening had deadline in same month. An *unannounced hire* is defined as a hire where this is not the case. If x hires are made in a firm with $y < x$ announced job-openings, then we count this as y announced hires and $x - y$ unannounced hires.

2.2 Descriptives

Figure 2 show the monthly levels of announced job hires from 2004 to 2012. We notice that the level of unannounced hires is roughly an order of magnitude larger than the level of announced hires. Both curves display business cycle movements, but the movements are stronger for announced hires. Figure 3 display the time serie for the share of announced hires out of total. This shows that announced hires account for TBD-TBD percent of all hires. The share displays a clear pro-cyclical pattern.

[Figure 2 about here.]

[Figure 3 about here.]

Table 1 provides monthly means for the key variables. The first row gives the average for the full population. A firm had on average 3.5 hires per month, but only 0.6 of these hires were through an announced opening. The average firm size is 18 full year employees.

Jobs in the public sector are more often matched through announced vacancies than jobs in the private sector, as shown by Panel B in Table 1. These public workplaces are larger on average, which might explain why larger workplaces hire relatively more workers through announced vacancies as shown from the numbers in Panel C.

Table 2 presents the ratio of announced to total number of hires by firm size for each year 2004 to 2012. In general, the ratio is increasing in firm size, but the slope of the increase is considerably smaller in the post 2008 years.

Panel C shows that the use of announced hires is increasing the firm size, which is further illustrated in Table 2 where the ratio of announced to total hires is shown for each year from 2004-12. Panel D shows that startups are less reliant on announced openings than existing firms, and Table 3 shows that the ratio is decreasing in firms' employment growth in each year. Finally, Panel E shows substantial differences in recruiting behaviour across industries, with *manufacturing* relying most on announced openings and *energy* relying least.

[Table 1 about here.]

Figure 4 shows the ratio of announced to total number of hires by wage decile.⁵ Figure 4a covers the full period and shows a clear reverse U-shape. The lowest and highest deciles have the lowest rate of announced hires. Figure 4b provides a pre- to

⁵The firms' average wage is calculated by using length of employment spell and total salary from the individual tax records to compute the average salary per day employed. For each firm we then compute the weighted average, where the individual is weighted by the length of the employment spell, such that the average wage of the individual who is employed for six months has a larger weight than the wage of the individual who was employed for three months. The wage deciles are then calculated separately for each year.

post 2008 comparison of the ration of announced to total number of hires by wage deciles. For both periods we see a clear reverse U-shape, but the level considerably lower after 2008.

[Figure 4 about here.]

[Table 2 about here.]

[Table 3 about here.]

3 The Model

In this section we set up a simple search-matching model of the labor market. The model builds heavily on the framework by the canonical model laid out in Pissarides (2000). However, in line with the empirical analysis above we will allow firms and workers to match via two channels: announced and unannounced job-openings. An announced opening is a ordinary job vacancy posting, visible for labor market analysts. An unannounced opening is a opening that is not posted publicly, but where the firm instead relies on alternative recruiting channels such as uninvited applications or networks. The only heterogeneity between announced and unannounced job openings will be differences in the cost of posting.

The purpose of this model is twofold. First, we wish to illustrate how changes in the posting behavior of firms can shift the *perceived* matching efficiency in the economy. Second, we construct a framework that empirically will allow us to trace out the shared of announced and unannounced job openings in the economy (Section 3.3).

3.1 The model

The Matching Functions

A non-standard element in our model will be the existence of two matching function - each with one type of job-openings. Unemployed search on both markets, while firms will only post a fraction of all their openings (see below). Specifically, unemployed workers and announced openings are matched according to the function

$$M_A(U, O_A) = AU^\alpha O_A^{1-\alpha} \quad (1)$$

while unemployed and unannounced openings are matched according to

$$M_U(U, O_A) = AU^\alpha O_U^{1-\alpha} \quad (2)$$

It follows that the probability of filling an announced opening is $m_A(\theta) \equiv \frac{M_A(U, O_A)}{O_A}$, where $\theta = \frac{O_A}{U}$, while the probability for a unemployed to match into a announced

opening is $\theta m_A(\theta)$. Similarly, the probability of filling an unannounced opening is $m_U(\kappa)$, where $\kappa = \frac{O_U}{U}$, while the chance for an unemployed to matching in to such a position is $\kappa m_U(\kappa)$.

[Figure 5 about here.]

Workers

Let us proceed to describe the value functions of employed and unemployed workers, V_e and V_u . When employed the worker enjoys a real wage of w , while loosing the job with an exogenous rate q . Thus, we can write the value function of being employed as

$$rV_e = w + q(V_u - V_e) \quad (3)$$

When unemployed the worker receives unemployment benefits of z , while matching into a job with probability $\theta m_A(\theta) + \kappa m_A(\kappa)$. Therefore, the value function of being unemployed reads

$$rV_u = z + [\theta m_A(\theta) + \kappa m_A(\kappa)](V_u - V_e) \quad (4)$$

Firms

The value of a filled position depends on the firm's income stream from the position (productivity minus wage) plus the expected net loss from the possibility of job destruction.

$$r\Pi_e = y - w + q(\Pi_{A/U} - \Pi_e) \quad (5)$$

The value of a posting and unposted job-opening, respectively, reads as below.

$$r\Pi_A = -C_a + m_A(\theta)(\Pi_E - \Pi_A) \quad (6)$$

$$r\Pi_U = -C_u + m_A(\theta)(\Pi_E - \Pi_U) \quad (7)$$

Here C_a reflects the job-posting cost, while C_u reflects the cost of recruiting via other channels.

Assuming that job-opening are created until there is no profit to gain from creating additional openings⁶ ($\Pi_U = \Pi_A = 0$) we get two labour demand curves.

$$\frac{C_a}{m(\theta)} = \frac{C_u}{m(\kappa)} = \frac{y - w}{r + q} \quad (8)$$

⁶The free entry condition holds

Wage bargaining

Wages are determined via usual Nash bargaining, why workers and firm split the surplus from the match via the usual Nash-bargaining solution.

$$\beta \Pi_E = (1 - \beta) (V_u - V_e) \quad (9)$$

Here β is the bargaining strength of the worker.

The Augmented Beveridge curve

Finally, we can note that the dynamics of unemployed in this model will follow the following dynamics.

$$\dot{U} = \dot{N} + qL - [\theta m_A(\theta) + \kappa m_U(\kappa)] U \quad (10)$$

which in steady state relates the unemployment rate to both types of job-openings via an *augmented Beveridge curve*.

$$u = \frac{n + q}{\theta m_A(\theta) + \kappa m_A(\kappa) + n + q} \quad (11)$$

While the standard Beveridge curve is an object in two dimensions (u, o) , this augmented Beveridge curve is an object in three dimensions (u, o_a, o_u) . This also mean that the object often measured in data (u, o_a) is merely a *perceived* Beveridge curve. As we will illustrate below this opens up for alternative channels through which the perceived Beveridge curve can shift.

[Figure 6 about here.]

Equilibrium

In sum, the equilibrium of our model is described by 6 equations with 6 unknown variables.

$$u = \frac{n + q}{\theta m_A(\theta) + \kappa m_A(\kappa) + n + q} \quad (12)$$

$$\frac{C_a}{m(\theta)} = \frac{C_u}{m(\kappa)} = \frac{y - w}{r + q} \quad (13)$$

$$w = \beta y + r(1 - \beta)V_u \quad (14)$$

$$V_e - V_u = \frac{\beta}{1 - \beta} \frac{y - w}{r + q} = \frac{w - z}{\theta m_A(\theta) + \kappa m_A(\kappa) + r + q} \quad (15)$$

3.2 Mechanisms

The relative cost of announced job openings is a key variable in the model. An increase in the cost of announced to unannounced openings will induce firms to shift their recruitment efforts from the announced to the unannounced market. This will lead to the share of announced openings and hires being decreasing in C_a/C_u as illustrated in Figure 7a.

The relative cost of announced job openings will also impact on the perceived matching efficiency. Figure 7b shows how the perceived Beveridge curve shifts inwards in response to an increase in the relative cost of announced job openings as firms respond to the higher cost of job announced openings by recruiting relatively more in the unannounced market. This will lower the ratio of announced job openings to unemployed which displays the inwards shift in the Beveridge curve. Similarly, the perceived matching efficiency will increase when the relative cost of announced openings increases.

What are the takeaway from this simple numerical exercise? First, the introduction of two recruitment channels, one announced and one unannounced, causes the *Beveridge curve* to be an object in three dimensions (u, o_a, o_u) . Second, the two dimensional object often measured in data is merely a *perceived* Beveridge curve. Third, the change in the cost of posting announced job-openings, which in the standard model leads to movements along the Beveridge curve, can in this augmented model shift the perceived matching efficiency and thus the Beveridge curve. These observations motivates the importance of accounting for the share of announced and unannounced job openings when analysing the labor market.

[Figure 7 about here.]

3.3 Calibrating the Model

We will now use the data from section 2 to calibrate the key parameters in the model laid out above. Our calibration is shown in Table 4. The elasticity of the matching function, α , is obtained by estimating the matching function for announced openings. The bargaining power β is sat such that the Hosios condition holds. The relative cost of job openings, C_a/C_u , is calibrated such that the model matches the share of hires via unannounced openings observed in the data. The level of C_a is chosen so as to match a monthly job-finding probability of 0.20. The value of unemployment benefits is sat to match a net replacement rate of 0.5. Finally, the job destruction rate and real interest rate are sat to 0.15 and 0.05, respectively.

[Table 4 about here.]

3.4 How much does the share of unannounced openings vary?

We can now use the model and the data to address our first question: how much does the share of unannounced job openings vary across time? Indeed, if we let μ_t be the share of hires made through unannounced openings (Figure 2) we can use the model to get the following expression for the share of unannounced job openings.⁷

$$\frac{O_u}{O_a} = \left(\frac{1 - \mu_t}{\mu_t} \right)^{\frac{1}{1-\alpha}} \quad (16)$$

Using this expression on the data we can plot the time series for the stock of unannounced openings and the share of unannounced openings as a ratio of total (Figure 8a and 8b). Some observations can be made from these two figures: (i) Unannounced openings accounts for the majority of job openings and (ii) during the recession (2008-09) the stock of these openings fell by much less than announced openings, (iii) the markets share of unannounced openings vary substantially over the business cycle. Taken together this indicates that announced openings only accounts for a small share and of all openings and that the share varies substantially across time.

[Figure 8 about here.]

3.5 What are consequences of swings in market shares for labor market analysis?

To address this question we will assess what happens to the matching efficiency when the share of unannounced hires increases from 75 to 90 percent as was observed from 2008 to 2010. Specifically, we will calibrate C_a/C_u so as to achieve these shares, and assess how the perceived matching efficiency differs across these two calibrated models.

Table 9 shows the result. An increase in the share of unannounced hires from 80 to 90 percent will, in the given calibration, increase the perceived matching efficiency by approx. 40 percent. Clearly, here the reason is not that the actual matching efficiency has gone up. Instead, it is simply a consequence of a drop in the share of announced openings caused by the higher posting costs. The table also illustrates that the separate estimation of the two matching function, obviously, is robust to fluctuations in the job posting costs. The similar mechanism is illustrated in Figure 9. Here we show that the increase the share of unannounced openings causes an outwards shift in the Beveridge curve.

[Figure 9 about here.]

[Table 5 about here.]

⁷See appendix 5.2 for derivation

4 Concluding remarks

This paper provides new evidence on firms recruiting behaviour. We create a new firm-level data set on job-openings and hires in Denmark and show that only 10-25 percent of all hires are made through announced job-openings. Using a simple model we translate this into 5-20 percent of all job openings being announced. We also find considerable degree of variation across firm characteristics. The use of announced job openings is increasing in firm size, decreasing in employment growth and less used in start-ups than in existing firms. Moreover, the use of announced job openings exhibits an inverse u-shape in the firm's average wage level, with low- and high-wage firms relying the least on announced job openings. Accounting for swings in the use of announced job openings is important insofar that a decrease(increase) in the use of announced job-openings will cause a increase(decrease) in the perceived matching efficiency. Indeed, in our calibrated model a decrease in the use of announced job-openings from 20 to 10 percent (as observed in 2008-09) will increase the perceived matching efficiency by approx. 40 percent.

Important aspect are still work in progress. First, we need to understand the role of compositional changes across firms in the observed time variation in the share of announced hirings. Second, we have not yet exploited the worker dimension of our hiring data in order to understand how hiring channels differ across observables on the individual level. Third, we need to understand how our measure for job-openings relates to more all-encompassing surveys such as the JOLTS.

5 Appendix

5.1 Solution Algorithm

First note that (13) can be used to find a $\kappa(\theta)$

$$\kappa = \left(\frac{A_u/C_u}{A_a/C_a} \right)^{1/\alpha} \quad (17)$$

Then note that 13 also yields $w(\theta)$

$$w(\theta) = y - \frac{\theta^\alpha(r+q)}{A_a/C_a} \quad (18)$$

Using this along with (15) we can then find θ by solving this function numerically.

$$\frac{\beta}{1-\beta} \frac{y-w(\theta)}{r+q} = \frac{w(\theta)-z}{\theta m_A(\theta) + \kappa m_A(\kappa(\theta)) + r+q} \quad (19)$$

This procedure yields solutions for θ , κ , w . By means of (12) we can then back out u .

5.2 Calibration of C_a/C_u

Let μ be share of announced hires observed in the data. Then, we can easily back out the corresponding fraction of unannounced to announced openings.

$$\frac{M(U, O_A)}{M(U, O_A) + M(U, O_U)} = \mu \Rightarrow \frac{1}{1 + \left(\frac{O_U}{O_A} \right)^{1-\alpha}} = \mu \Rightarrow \frac{O_u}{O_a} = \left(\frac{1-\mu}{\mu} \right)^{\frac{1}{1-\alpha}} \quad (20)$$

From one of the model's equilibrium conditions (13) we know that this fraction can be written as a function of relative job posting costs.

$$\frac{C_a}{C_u} = \frac{m(\theta)}{m(\kappa)} \Rightarrow \frac{C_a}{C_u} = \left(\frac{O_u}{O_a} \right)^\alpha \quad (21)$$

Thus, C_a/C_u can be calibrated as

$$\frac{C_a}{C_u} = \left(\frac{1-\mu}{\mu} \right)^{\frac{\alpha}{1-\alpha}} \quad (22)$$

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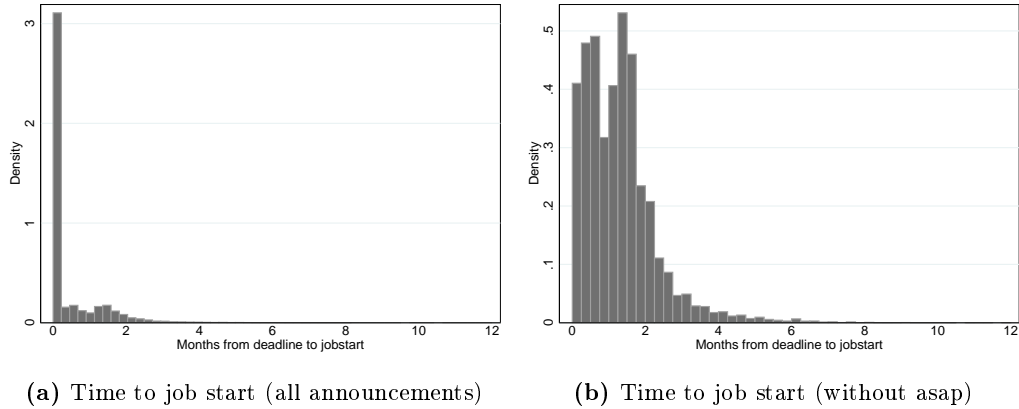


Figure 1: Time to job start from deadline, measured in months. The data is collected from Jobindex.dk's online archive 2008-2014. In Figure 1a the job start date of “as soon as possible” openings is set equal to the application deadline. In Figure 1b these job openings are removed.

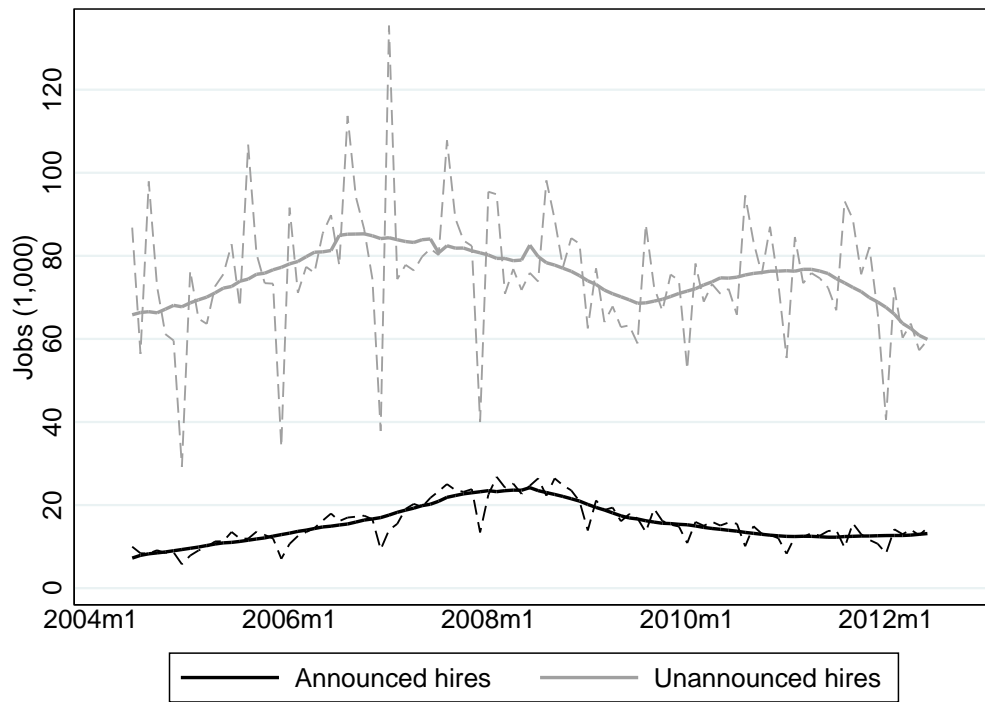


Figure 2: Hires through announced and unannounced positions. The dashed lines indicate the unadjusted monthly levels, the solid lines are six month moving average (with equal weights).

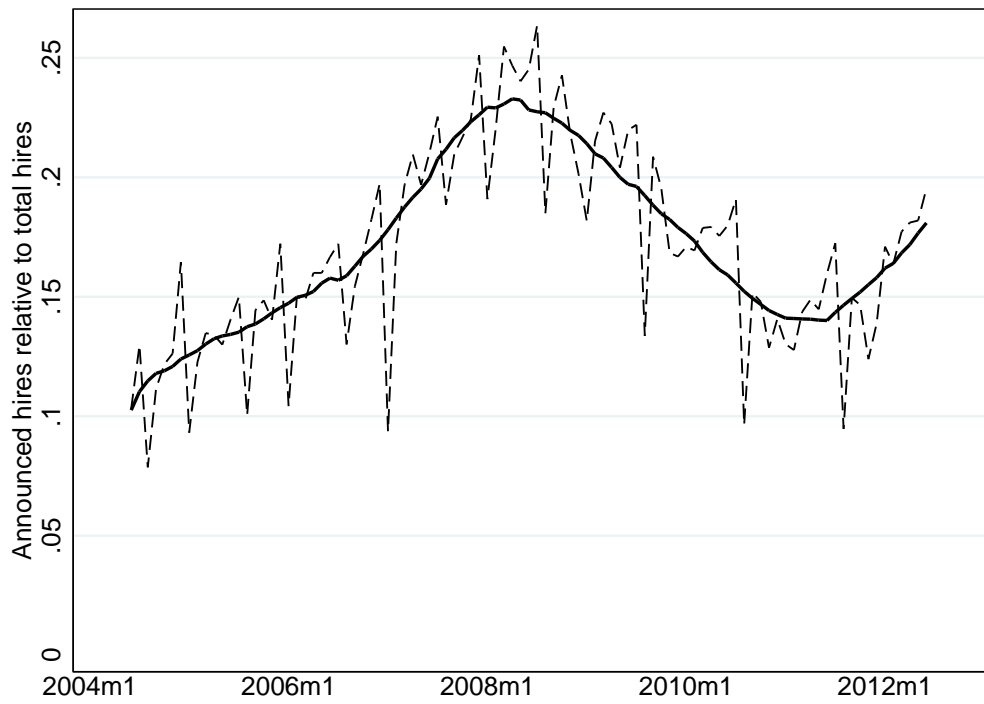
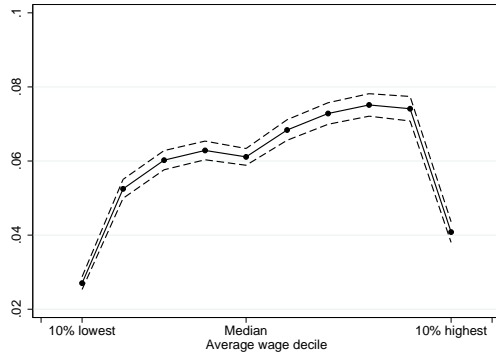
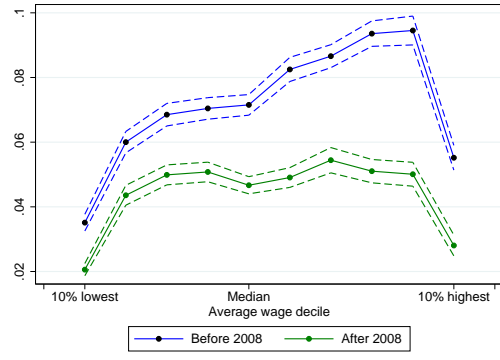


Figure 3: The share of announced hires out of total hires. The dashed lines indicate the unadjusted monthly levels, the solid lines are six month moving average (with equal weights).



(a) All years



(b) Pre-Post 2008

Figure 4: The ratio of announced hires to total hires by wage decile. The wage is the average wage in the firm.

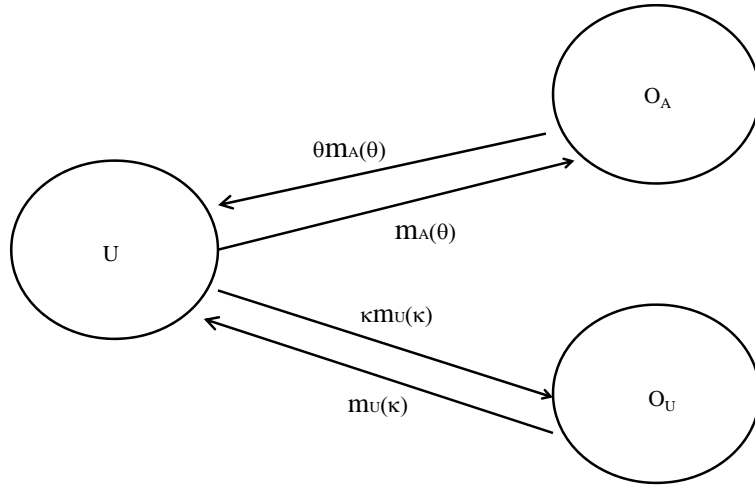


Figure 5: Illustration of flows in the model

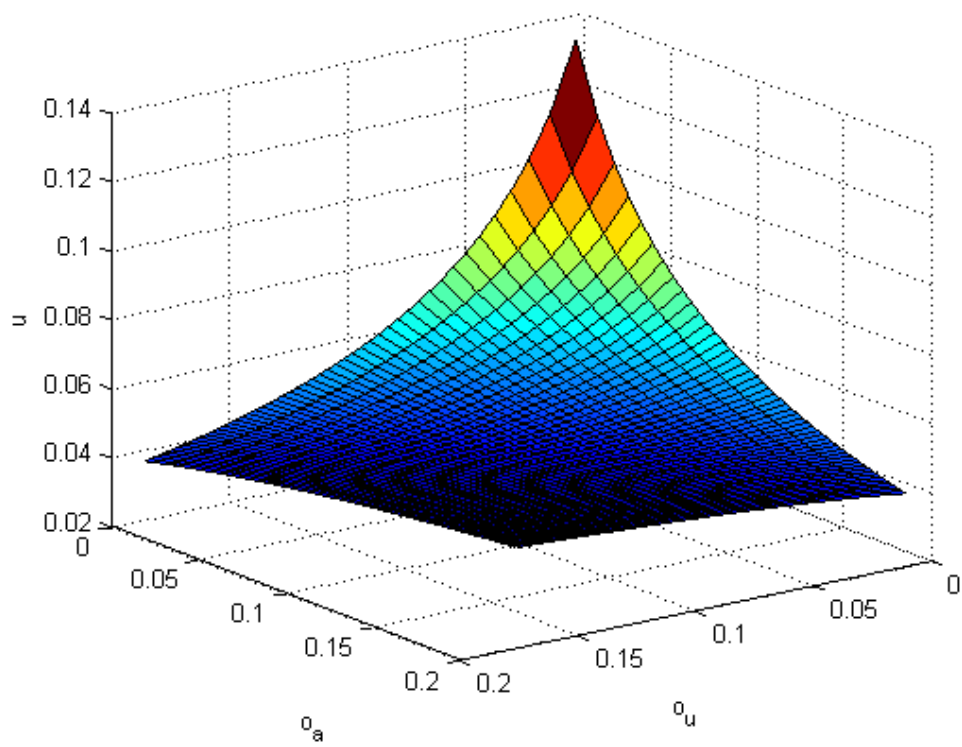
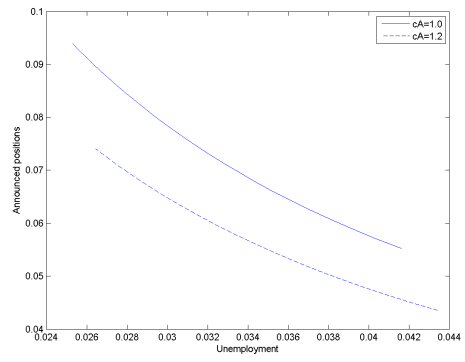
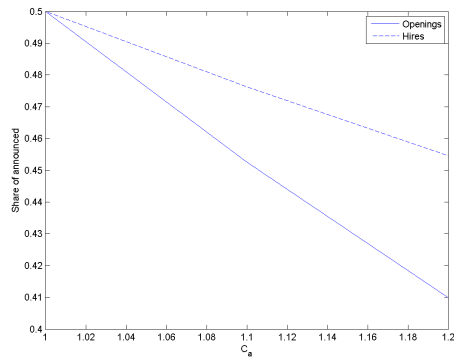
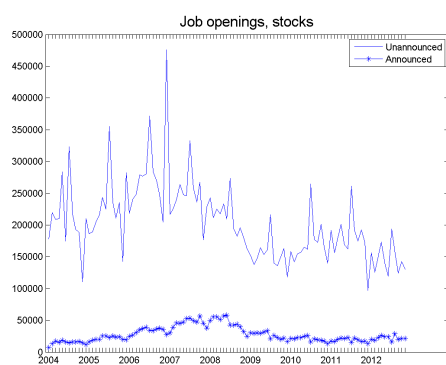


Figure 6: The threedimensional Beveridge Curve.

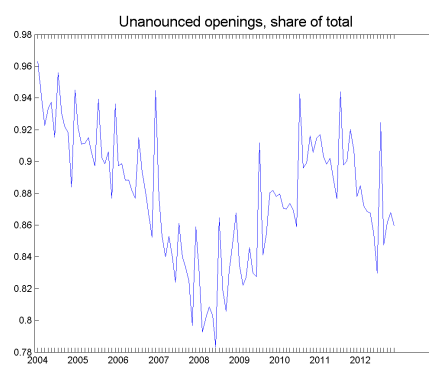


- (a) Shares of announced positions and hires as function of the cost of posting announced job openings.
(b) Perceived Beveridge Curve for two values of announcing job openings

Figure 7: Numerical illustrations



(a) Job openings



(b) Shares

Figure 8: Announced and unannounced openings

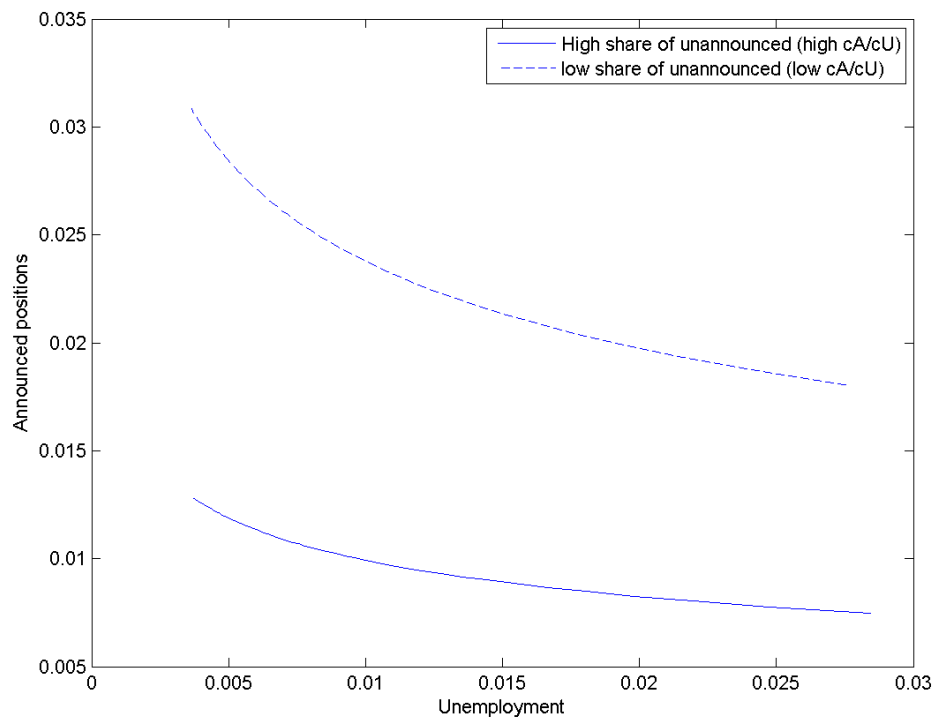


Figure 9: Perceived Beveridge Curve for $C_a/C_u \in \{1.41, 1.73\}$.

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Table 1: Statistics by firm characteristics - monthly averages 2004-2012

	HT	OA	HA	HU	HA/HT	Size
All	3.49	1.08	0.58	2.91	0.06	18.01
<i>By wage decile</i>						
0-20% (lowest)	2.25	0.51	0.16	2.08	0.04	3.81
20-40%	2.81	0.70	0.31	2.50	0.06	8.19
40-60%	3.93	1.23	0.76	3.17	0.06	13.06
60-80%	4.94	2.01	1.30	3.64	0.07	25.07
80-100% (highest)	4.00	1.22	0.55	3.44	0.06	40.61
<i>By sector</i>						
Unknown	3.55	1.11	0.53	3.03	0.07	19.52
Central government	5.96	1.57	1.10	4.85	0.08	27.80
Regional government	13.42	7.53	6.04	7.38	0.09	24.52
Municipalities	11.00	6.67	5.08	5.92	0.11	18.42
Public companies	40.35	27.11	20.79	19.56	0.23	65.77
Private sector	2.66	0.59	0.25	2.40	0.04	15.59
<i>By firm size (# of employees)</i>						
2-3	2.30	0.61	0.31	1.99	0.03	2.37
3-4	2.57	0.82	0.40	2.17	0.05	3.72
5-9	3.18	0.88	0.48	2.69	0.06	6.95
10-19	3.89	1.33	0.76	3.13	0.07	13.92
20-49	4.46	1.52	0.81	3.66	0.09	30.56
>49	9.70	3.30	2.01	7.70	0.12	130.20
<i>By firm growth (year-to-year change in # of employees)</i>						
New firm	2.17	0.43	0.14	2.03	0.03	2.68
<-10%	5.34	2.00	1.19	4.16	0.07	11.77
-10-0%	2.48	0.54	0.26	2.22	0.06	28.25
0%	1.89	0.40	0.17	1.73	0.05	7.66
0-10%	2.64	0.57	0.25	2.39	0.06	32.43
10-25%	2.56	0.67	0.32	2.23	0.06	21.38
>25%	4.99	1.81	1.04	3.95	0.07	20.73
<i>By industry</i>						
Construction	1.90	0.47	0.16	1.74	0.06	16.92
Energy	2.88	0.22	0.11	2.77	0.03	44.50
Finance	4.32	2.69	1.02	3.29	0.07	20.04
Trade, hotel & restaurants	2.73	0.70	0.35	2.38	0.08	13.49
Manufacturing	3.03	0.98	0.43	2.60	0.10	47.91
Farms, fisheries & mining	2.39	0.40	0.19	2.20	0.06	37.07
Public & private services	7.00	1.73	1.07	5.93	0.07	21.28
Transportation, mail and com.	3.59	1.00	0.45	3.14	0.07	22.66
Unknown	1.40	0.08	0.03	1.36	0.02	0.87

Notes: HT: Total number of hires. OA: Number of announced vacancies. HA: Number of hires related to an announced vacancy. HU: number of hires without a post vacancy. HA/HT: Hires through vacancies in relation to the total number of hires. Size: firm size (by the number of employees.). Sector is only known for 2008-2012.

Table 2: The ratio of announced hires to total hires, by firm size 2004-2012

	# Employees (full year equ.)					
	<3	3-4	5-9	10-19	20-49	>50
2004	0.029	0.040	0.048	0.056	0.076	0.101
2005	0.041	0.051	0.059	0.077	0.097	0.138
2006	0.051	0.063	0.072	0.094	0.119	0.168
2007	0.046	0.061	0.074	0.095	0.115	0.155
2008	0.034	0.060	0.070	0.095	0.113	0.156
2009	0.025	0.039	0.049	0.064	0.068	0.100
2010	0.024	0.036	0.046	0.056	0.060	0.086
2011	0.024	0.035	0.046	0.055	0.059	0.084
2012	0.028	0.037	0.045	0.059	0.065	0.087

Table 3: The ratio of announced hires to total hires, by firm growth 2004-2012

	Growth in # Employees (full year equ.)					
	<-10%	10-0%	No change	0-10%	10-25%	>25%
2004	0.065	0.071	0.037	0.074	0.052	0.058
2005	0.084	0.095	0.049	0.097	0.074	0.075
2006	0.101	0.112	0.059	0.121	0.096	0.089
2007	0.096	0.107	0.057	0.114	0.094	0.090
2008	0.085	0.079	0.071	0.074	0.067	0.082
2009	0.049	0.042	0.021	0.047	0.046	0.057
2010	0.047	0.037	0.053	0.039	0.042	0.051
2011	0.047	0.038	0.075	0.040	0.035	0.052
2012	0.054	0.040	0.024	0.042	0.041	0.053

Table 4: Calibration

Parameter	Value	Source / Calibration
y	10	Normalisation
r	.05	
q	.15	
z	4.8	Replacement rate=0.5
β	.8	Hosios condition
α	.8	Estimated matching function
$A_a = A_u$	1	Normalisation
C_u	.87	Monthly job-finding rate=0.2
C_a/C_u	[1.73, 1.41]	Share of unannounced hires $\in (0.90, 0.80)$

Table 5: Estimated matching function, $\log(h) = A + \alpha u + (1 - \alpha)o$

	A	α	$1 - \alpha$
$h = \text{total hires, } o = \text{announced openings}$			
$C_a/C_u = 1.41$	2.07	.8	.2
$C_a/C_u = 1.71$	2.89	.8	.2
$h = \text{announced hires, } o = \text{announced openings}$			
$C_a/C_u = 1.41$	0	.8	.2
$C_a/C_u = 1.71$	0	.8	.2
$h = \text{unannounced hires, } o = \text{unannounced openings}$			
$C_a/C_u = 1.41$	0	.8	.2
$C_a/C_u = 1.71$	0	.8	.2