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**MTG**  
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Group

# Evaluation of Set Class Similarity Measures for Tonal Analysis

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SMC Master Thesis Presentation

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# Outline

- Introduction:

Problem - Definitions - Objectives

- Methodology:

Systematic Description - Set Class Theory - Segmentation - Representation

- Conclusions

- Future Work

# Introduction

## **Problem**

1. Existing approaches to tonal analysis lack depth
2. Use of “non-musical” similarity measures

# Introduction

## “Evaluation of **Set Class Similarity Measures** for **Tonal Analysis**”

- Tonal Analysis:
  1. Description
  2. Representation
- Set Class Theory: Tool for description stage
- Similarity Measures: Tool for representation stage

# Introduction

## **Objectives**

1. Adopt systematic approach to description
2. Use set class theory
3. Survey set class similarity measures
4. Represent set class data using similarity measures
5. Demonstrate with analysis examples

# Methodology

## **Systematic Description**

- What does it mean to be systematic?

Mid-Level

# Methodology

## **Set Class Theory** - What?

Pitch Set:  $\{A4, C\#5, E5, A5\}$

Pitch Class Set:  $\{C\#, E, A\} = \{1,4,9\}$

Set Class:  $\{0,4,7\}$

Forte Name: 3-11B

# Methodology

## **Set Class Theory** - Why?

- An appropriate mid-level descriptive tool
- What are the differences/benefits?



# Methodology

## **Set Class Similarity Measures** - What?

- Theoretical models of similarity
- Compare subset contents
- Musical measures

# Methodology

## Set Class Similarity Measures - Survey

SIMILARITY MEASURE	C1	C2	C3.1	C3.2	C3.3	C3.4	C4	C5	C6
s.i.					X	X			
sf					X	X	X		
IcVSIM	X	X				X			
ISIM2	X	X				X			
K	X	X			X	X	X		
SIM	X	X			X	X	X		
MEMB <sub>n</sub>	X	X			X	X	X		
AMEMB2	X	X	X						
ASIM	X	X	X	X		X	X		
IcVD1	X	X	X	X		X	X		
IcVD2	X	X	X	X		X			
COS	X	X	X	X		X			
ANGLE	X	X	X	X		X			
AK	X	X	X	X		X	X		
SATSIM	X	X	X						
CSATSIM	X	X	X						
REL2	X	X				X			
%REL <sub>n</sub>	X	X	X	X	X	X	X		
TMEMB	X	X			X		X	X	
ATMEMB	X	X	X	X		X	X	X	
TSATSIM	X	X	X	X		X		X	
AvgSATSIM	X	X	X	X		X		X	
REL	X	X	X	X		X	X	X	
T%REL	X	X	X	X	X	X	X	X	
RECREL	X	X	X	X	X	X	X	X	X

(Rahn, 1979)

(Buchler, 1997)

(Buchler, 1997)

(Lewin, 1979)

(Castrén, 1994)

(Castrén, 1994)

# Methodology

## Segmentation

- Two segmentation policies:
  1. Fully Systematic (A. Martorell, 2014)

For capturing the complete SC contents
  2. Sliding Window

For tuning in to a *sets of interest*

# Methodology

## Segmentation - Fully Systematic

Example:

### Prelude in C

from *The Well Tempered Clavier*, Book One

Andante J. S. Bach

*p*

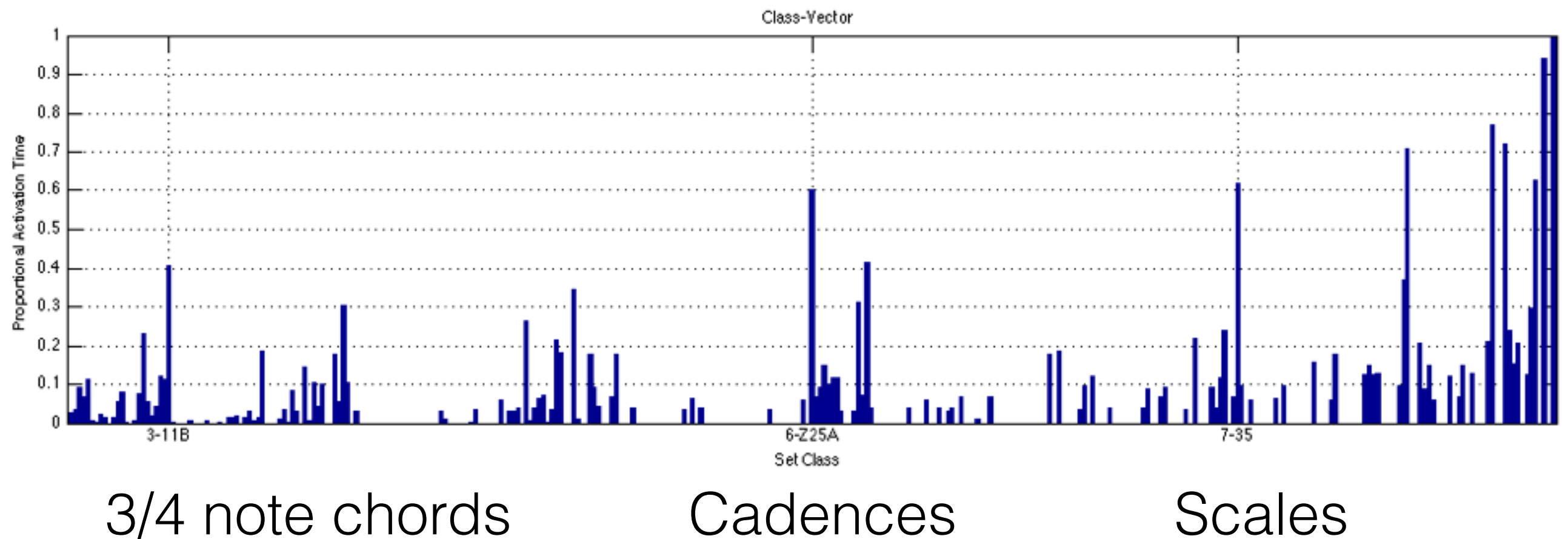
2 1

*mf*

# Methodology

## Segmentation - Fully Systematic

- Class Vector



# Methodology

## Segmentation - Sliding Window

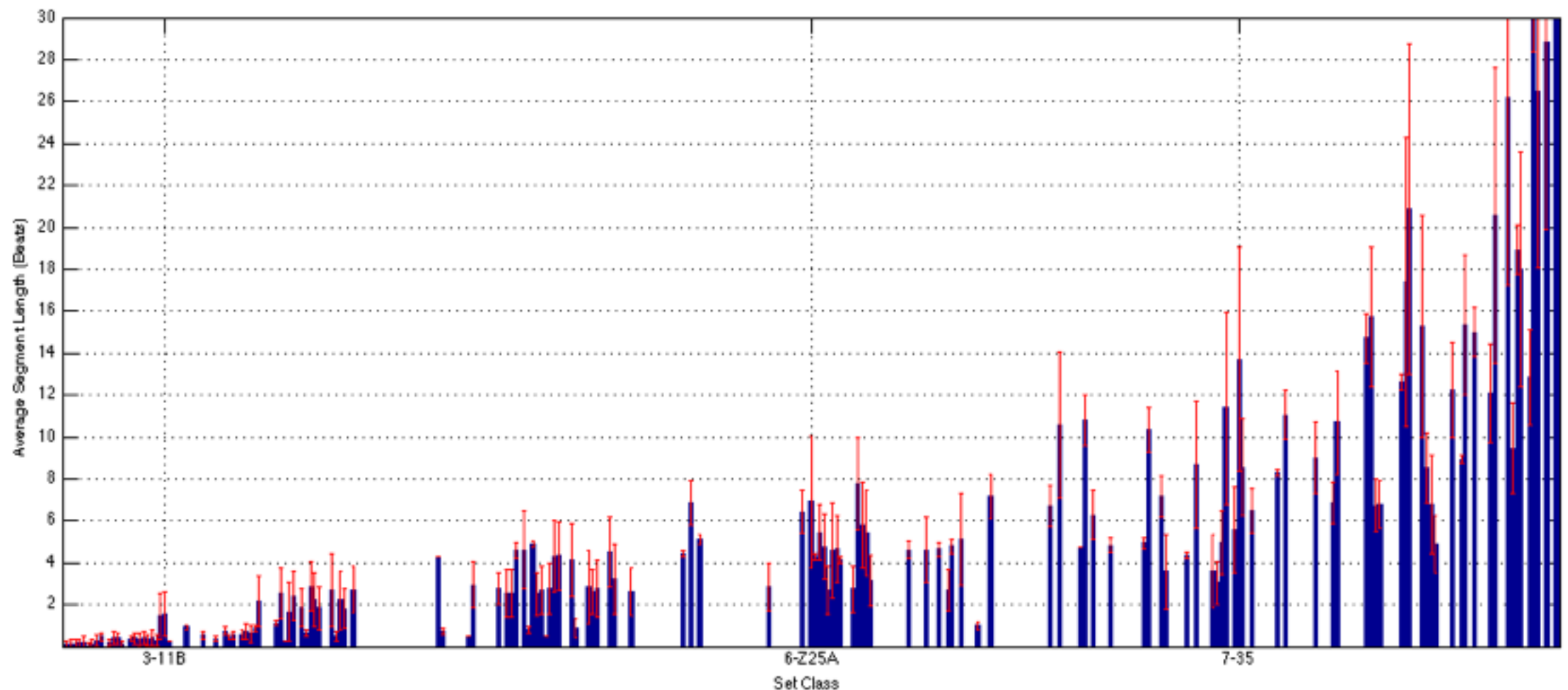
- Window and hop size selection
- What are the *sets of interest*?

	Chord	Set Class	Name
3 note chords	maj	{0,4,7}	3-11B
	min	{0,3,7}	3-11A
	dim	{0,3,6}	3-10
	aug	{0,4,8}	3-12
	sus4	{0,2,7}	3-9
	sus2	{0,2,7}	3-9
4 note chords	maj7	{0,1,5,8}	4-20
	min7	{0,3,5,8}	4-26
	hdim7	{0,2,5,8}	4-27A
	7	{0,3,6,8}	4-27B
	dim7	{0,3,6,9}	4-28
	min(7)	{0,1,4,8}	4-19A
	aug(7)	{0,3,4,8}	4-19B
	maj(9)	{0,2,4,7}	4-22A
	min(9)	{0,2,3,7}	4-14A
	maj6	{0,3,5,8}	4-26
	min6	{0,1,5,8}	4-20
	sus4(7)	{0,2,6,7}	4-16B
	sus4(b7)	{0,2,5,7}	4-23
5 note chords	9	{0,2,4,6,9}	5-34
	maj9	{0,1,3,5,8}	5-27A
	min9	{0,3,5,7,8}	5-27B
Cadences	V-I/IV-I	{0,1,3,5,8}	5-27A
	V7-I	{0,1,3,5,6,8}	6-Z25A
	V-IV	{0,2,4,6,7,9}	6-33B
	Pentatonic	{0,2,4,7,9}	5-35
Scales	Wholetone	{0,2,4,6,8,10}	6-35
	Diatonic	{0,1,3,5,6,8,10}	7-35
	Octatonic	{0,1,3,4,6,7,9,10}	8-28

# Methodology

## Segmentation - Sliding Window

- Average segment length vs set class

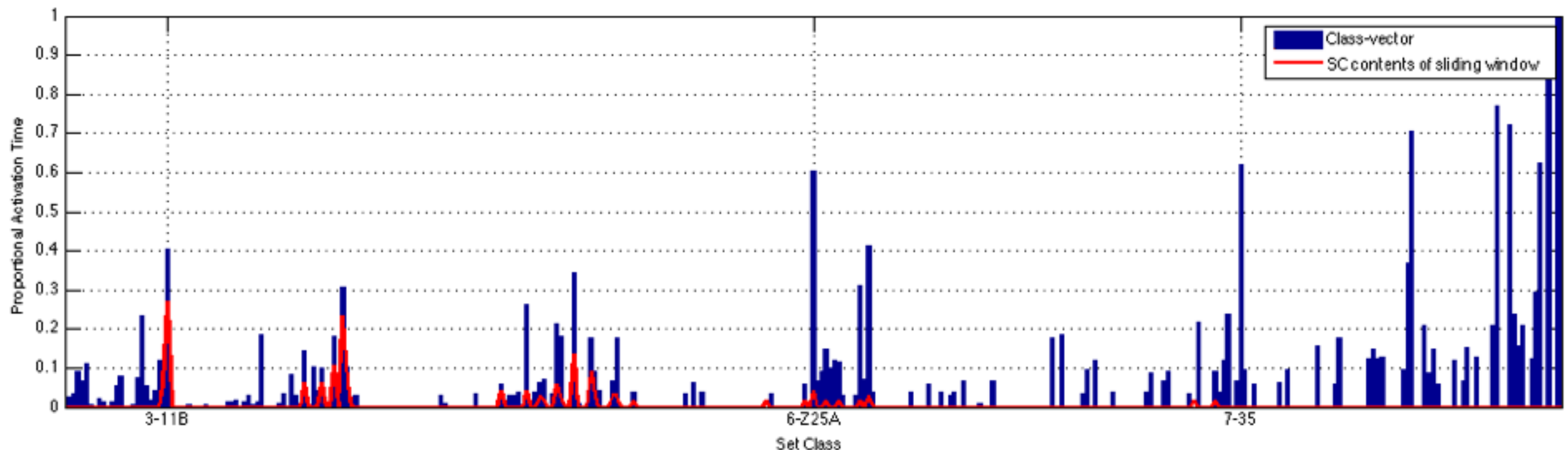


# Methodology

## **Segmentation** - Sliding Window

- Class vector + sliding window contents

(Window = 2 beats, hop = 1 beat)





# Methodology

## **Representation**

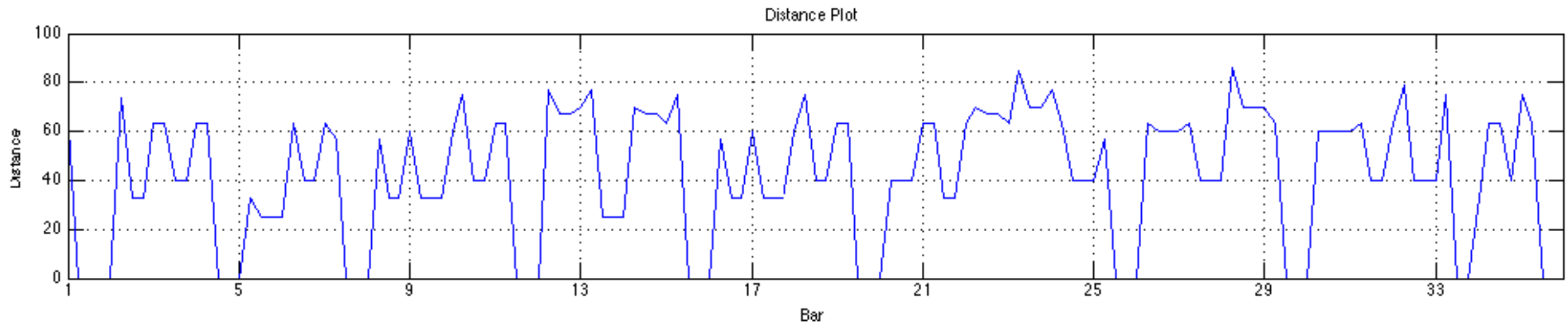
3 representation techniques:

1. Distance plot
2. Autocorrelation
3. Self-similarity matrix

# Methodology

## Representation - Distance Plot

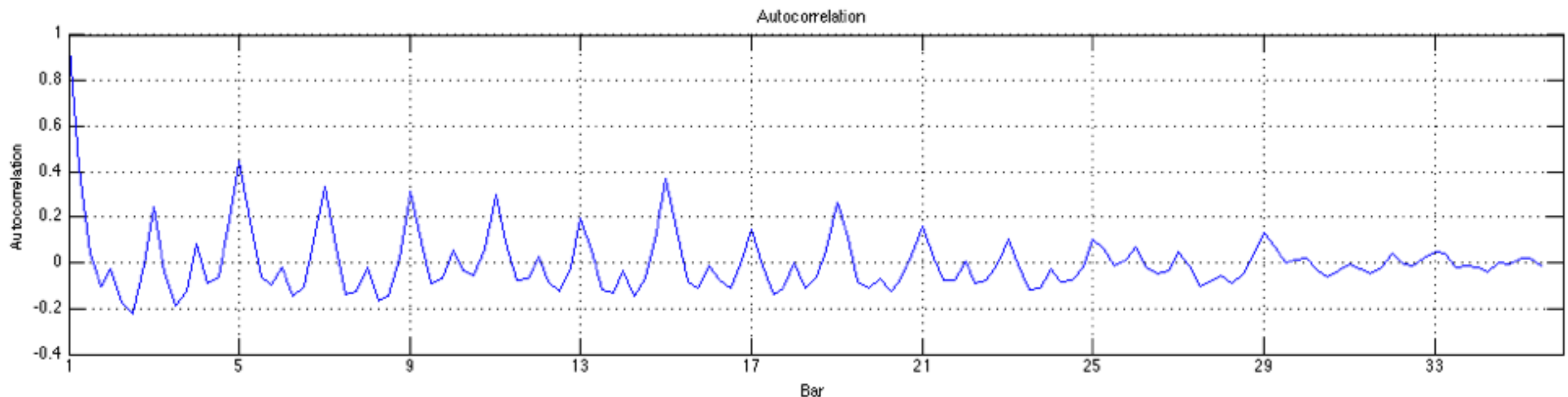
- Represents tonal change in time with respect to comparison set
- Comparison set selection (3-11B)



# Methodology

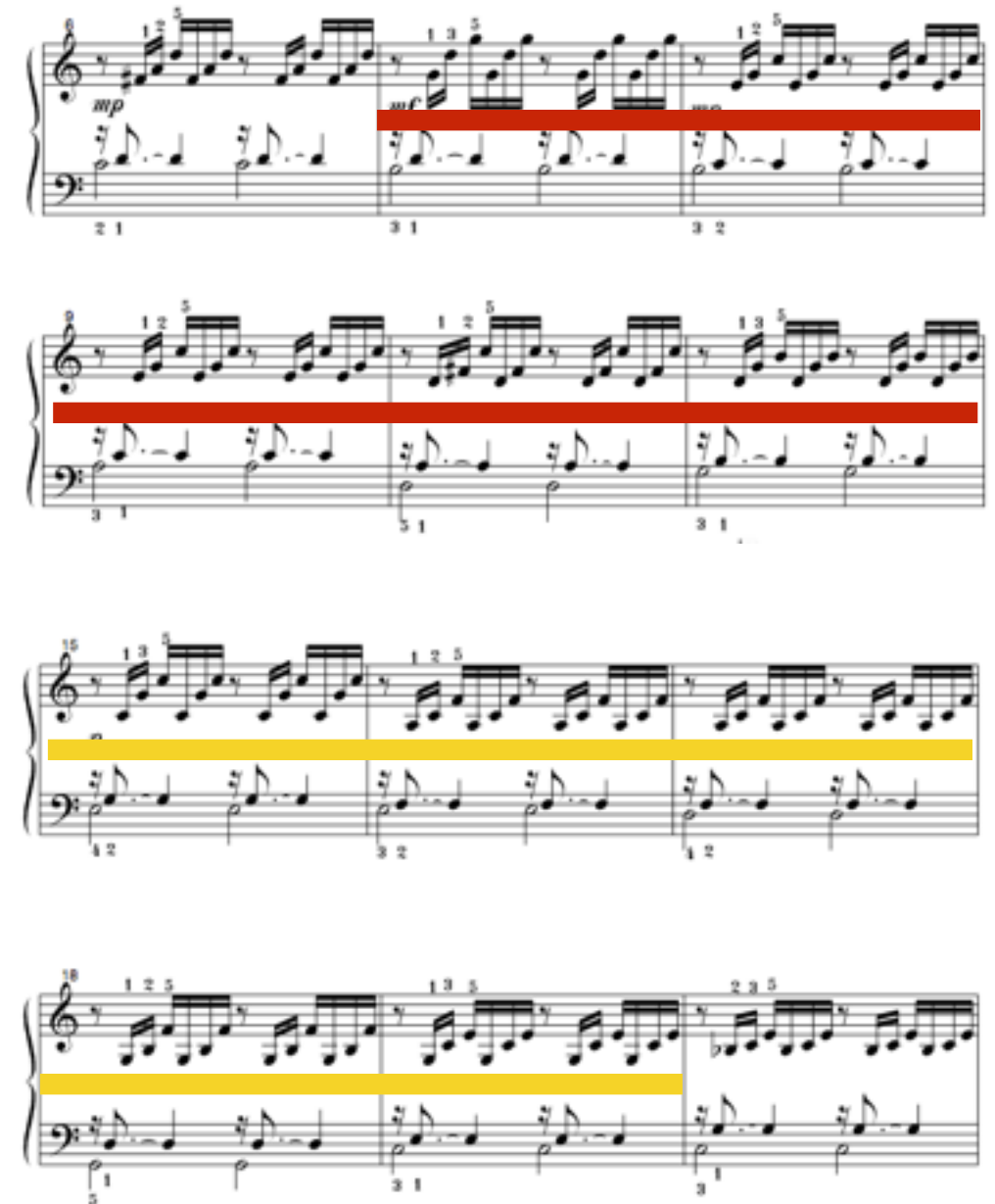
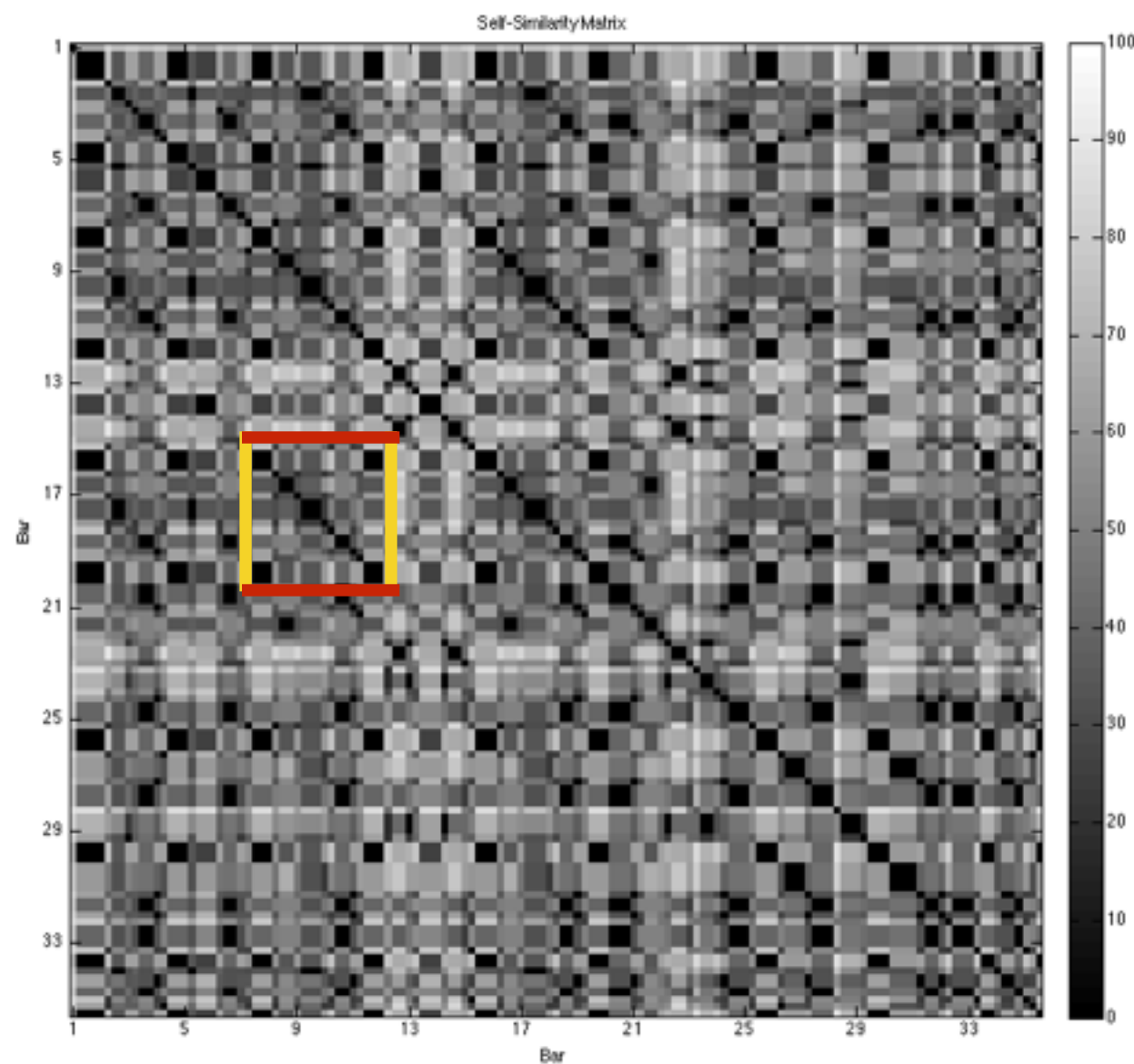
## Representation - Autocorrelation

- Autocorrelation of distance plot
- Peaks represent recurring patterns

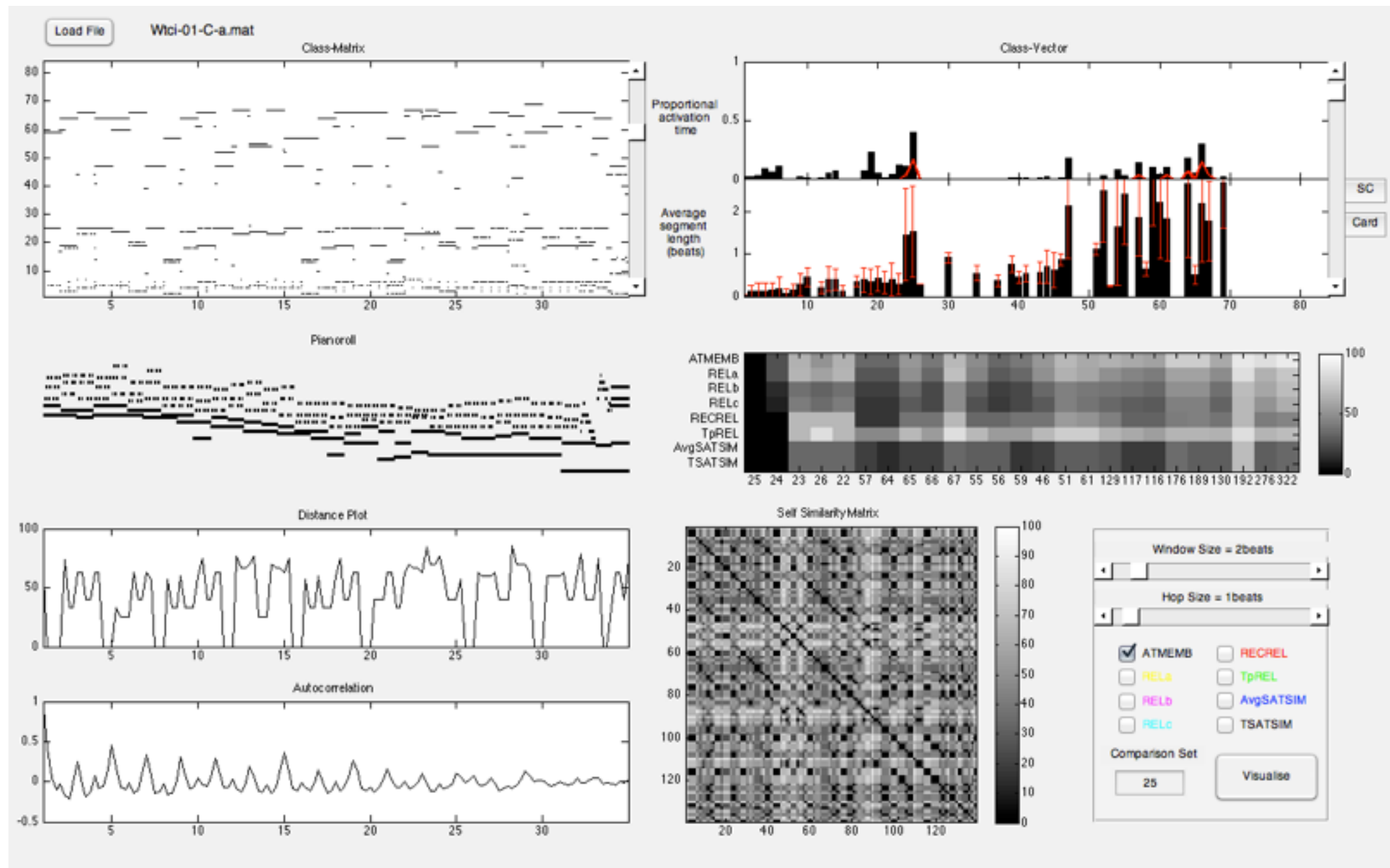


# Methodology

## Representation - Self-Similarity Matrix



# Representation - Analysis Tool



# Conclusions

## Conclusions

- Set class tonal analysis
- Analysis Outcomes

## Contribution

- Similarity measure survey
- Analysis Tool

# Future Work

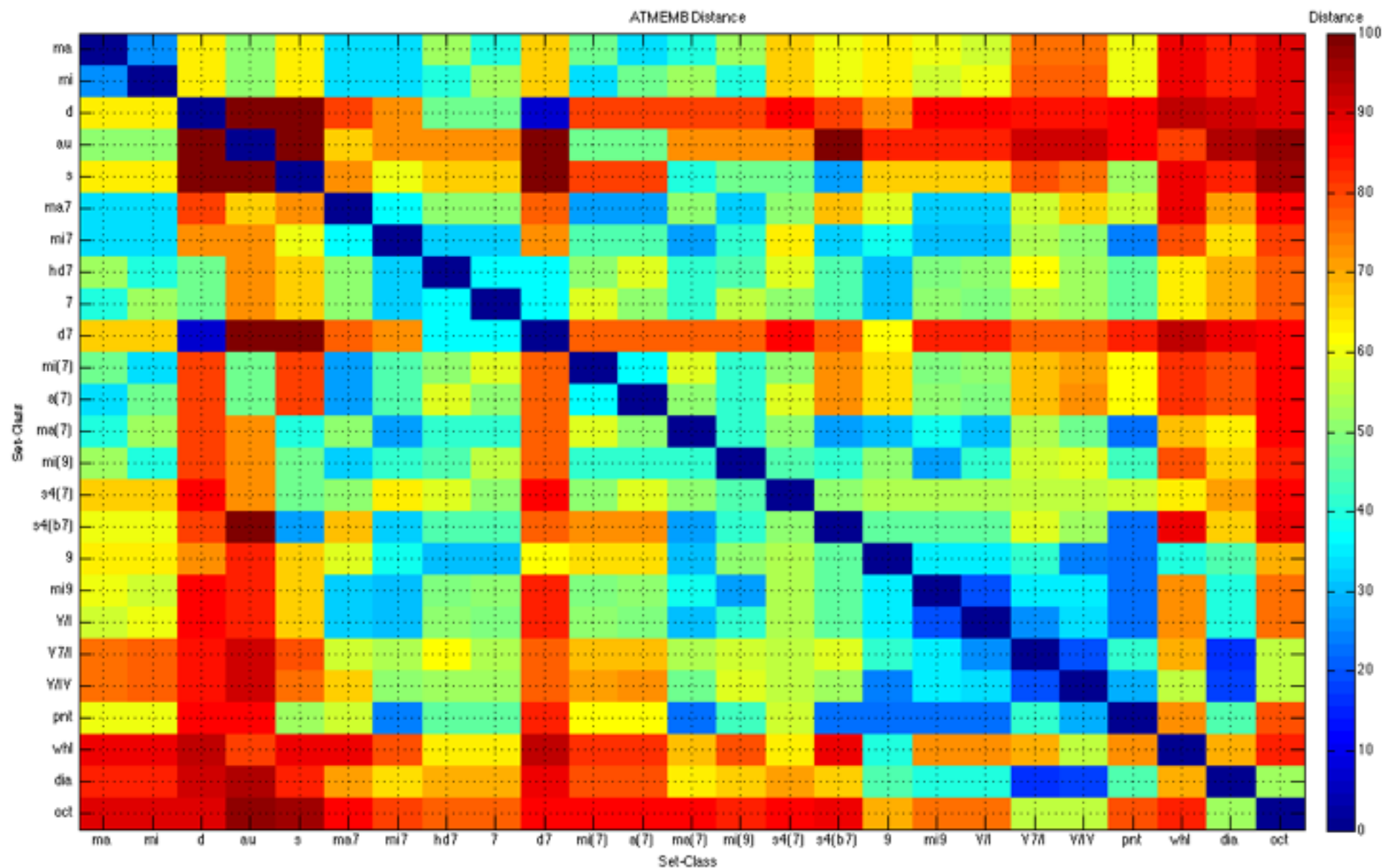
- Pending Work
  - Comprehensive explanation of parameter selection
- Future Work
  - Set class based feature vectors

Questions?



# Methodology

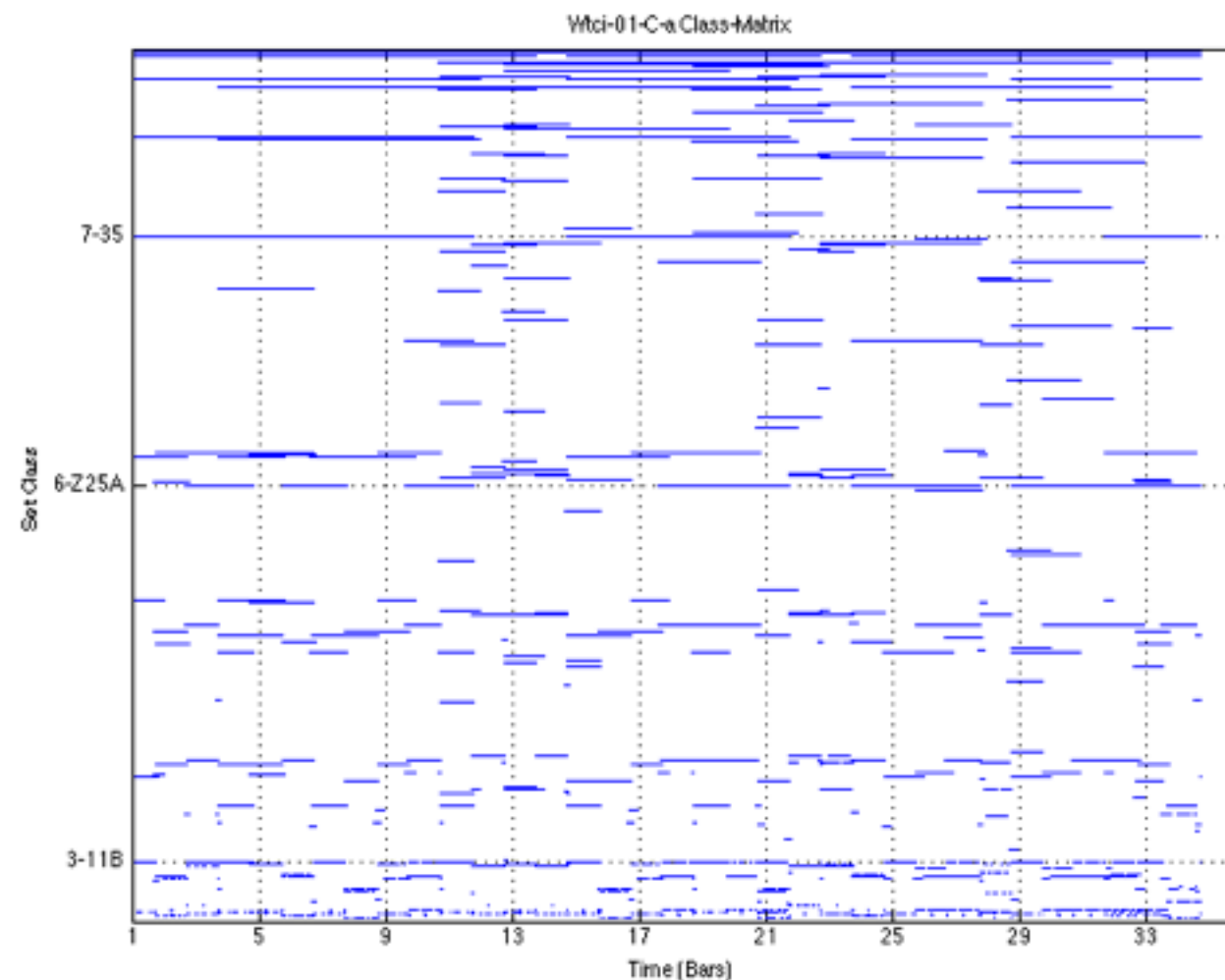
## Set Class Similarity Measures - Survey



# Methodology

## **Segmentation** - Fully Systematic

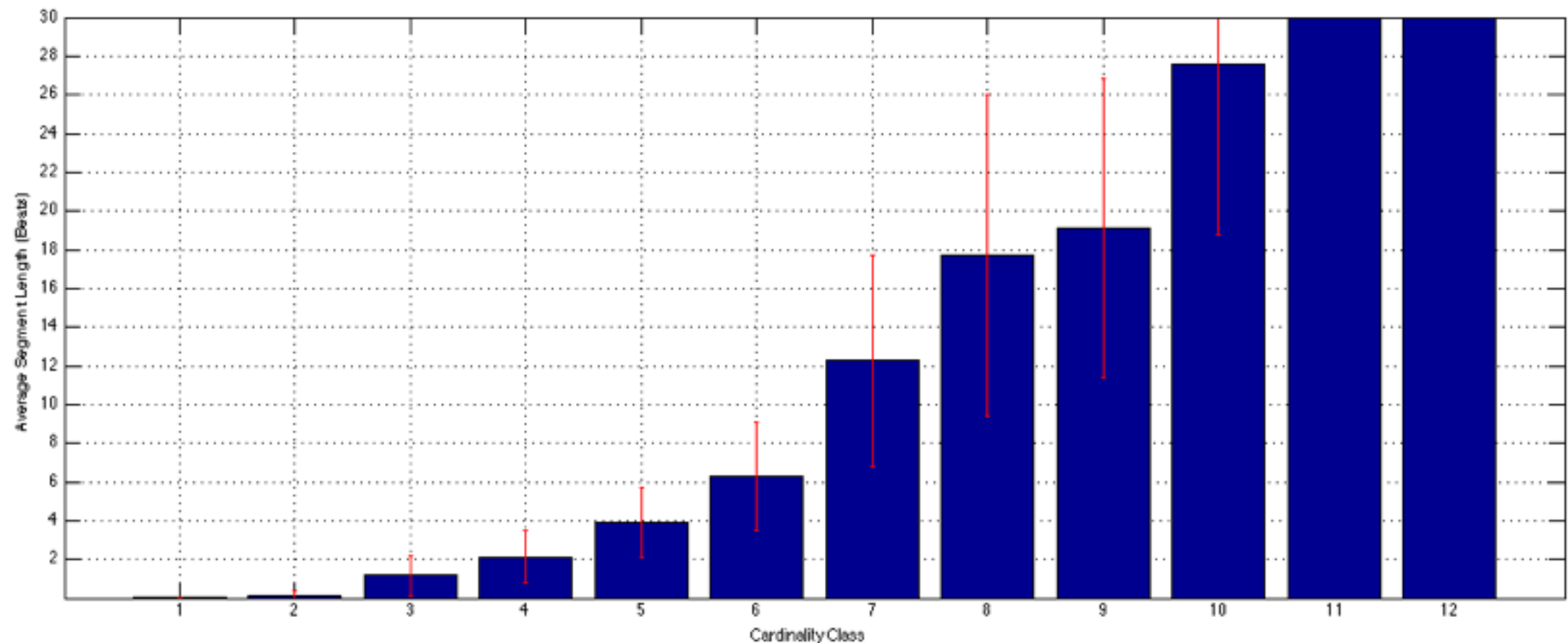
- Class Matrix



# Methodology

## **Segmentation** - Sliding Window

- Average segment length vs cardinality



# Representation

## **Analysis Tool** - Preliminary Findings

- Sets of interest
  - 6-Z25A / 5-27A
  - 7-35
  - 8-23
- Measures
  - ATMEMB/REL
  - TpREL
  - AvgSATSIM/TSATSIM