Problem Set 1

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Part I

1. Income

$$E_n = w_n N_n \tag{1}$$

2. Labor market clearing

$$w_n N_n = \sum_{k \in \mathcal{K}} \beta^k X_n^k \tag{2}$$

3. Total firm revenues of country n in sector k

$$X_n^k = \sum_{i \in \mathcal{T}} X_{in}^k \tag{3}$$

4. Total expenditure of country n in sector k

$$E_n^k = \sum_{k' \in \mathcal{K}} \lambda^{kk'} \sum_{i \in \mathcal{I}} X_{in}^{k'} + \mu^k E_n \tag{4}$$

5. Total exports from country i to country n in sector k.

$$X_{ni}^{k} = \frac{T_{i}^{k} [c_{i}^{k} d_{ni}^{k}]^{-\theta^{k}}}{\Phi_{n}^{k}} E_{n}^{k}$$
(5)

6. Multilateral resistance term

$$\Phi_n^k = \sum_{i \in \mathcal{I}} T_i^k [c_i^k d_{ni}^k]^{-\theta^k} \tag{6}$$

7. Price index of composite goods from each country i in sector k

$$P_i^k = A^k [\Phi_i^k]^{-1/\theta^k} \tag{7}$$

Where A^k is a constant.

8. The price of a bundle of intermediate inputs for each sector

$$m_i^k = \prod_{k' \in \mathcal{K}} (P_i^{k'})^{\lambda^{k'k}} \tag{8}$$

9. Cost of a bundle of inputs

$$c_i^k = \Lambda^k(w_i)^{\beta_k} \prod_{k' \in \mathcal{K}} (P_i^{k'})^{\lambda^{k'k}} \tag{9}$$

where Λ^k is a constant

Part 4

Counterfactual 1: increase the TFP of country 1 in sector 1 by 20 percent. Counterfactual 2: increase the TFP of country 2 in sector 1 by 20 percent.

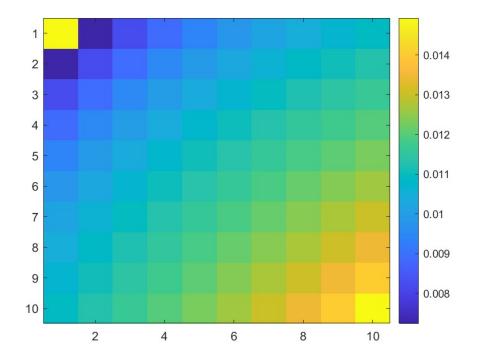


Figure 1: Counterfactual 1

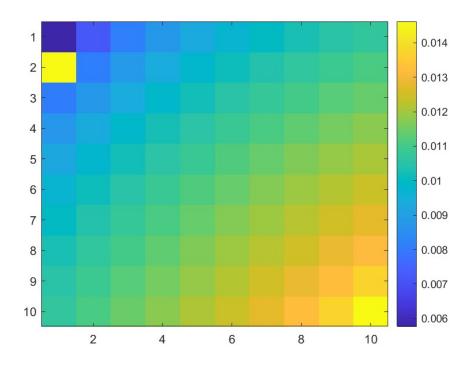


Figure 2: Counterfactual 2