## CS 374 Spring 2018 Homework 1

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## Problem 3 solutions:

Let us define DFA  $M=(Q,\Sigma,\delta,s,A)$  such that M defines the language

 $L = \{w \in \{0,1\}^* \mid w \text{ starts with } 0 \text{ and has an odd number of } 01 \text{ substrings}\}$ 

- $Q = \{S, R, 0, 1, 2, 3\}$
- $A = \{1, 2\}$
- $\bullet$  s = S
- $\Sigma = \{0, 1\}^*$
- q is defined by the following. Note that for some cases we use the numerical values of the state names to determine the next state.

$$- \delta(S,0) = 0$$

$$- \delta(S, 1) = R$$

$$- \delta(R,0) = R$$

$$-\delta(R,1) = R$$

$$\delta(q,0) = \begin{cases} q & \text{if } q \mod 2 = 0\\ (q+1) \mod 4 & \text{if } q \mod 2 = 1 \end{cases}$$

$$\delta(q,1) = \begin{cases} (q+1) \mod 4 & \text{if } q \mod 2 = 1\\ q & \text{if } q \mod 2 = 0 \end{cases}$$

