

Heavy quark decays: Gate to new physics?

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1. What are the smallest building blocks of matter?
2. Which forces act between them?
3. How did the universe begin?

**Elementary
Particle Physics**
=
**High Energy
Physics**
Cosmology, astrophysics

Contents

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- Standard Model
- Search for new physics
- Precision flavour physics
- Flavour anomalies
- Summary

Standard Model

Standard Model of Elementary Particles

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Fermions (= matter particles): quarks and leptons with spin 1/2:

$$\left(\begin{array}{c} u_L, u_L, u_L \\ d_L, d_L, d_L \end{array} \right) \quad \left(\begin{array}{c} c_L, c_L, c_L \\ s_L, s_L, s_L \end{array} \right) \quad \left(\begin{array}{c} t_L, t_L, t_L \\ b_L, b_L, b_L \end{array} \right) \quad \left(\begin{array}{c} \nu_{e,L} \\ e_L \\ e_R \end{array} \right) \quad \left(\begin{array}{c} \nu_{\mu,L} \\ \mu_L \\ \mu_R \end{array} \right) \quad \left(\begin{array}{c} \nu_{\tau,L} \\ \tau_L \\ \tau_R \end{array} \right)$$

} fermion fields



Enrico Fermi

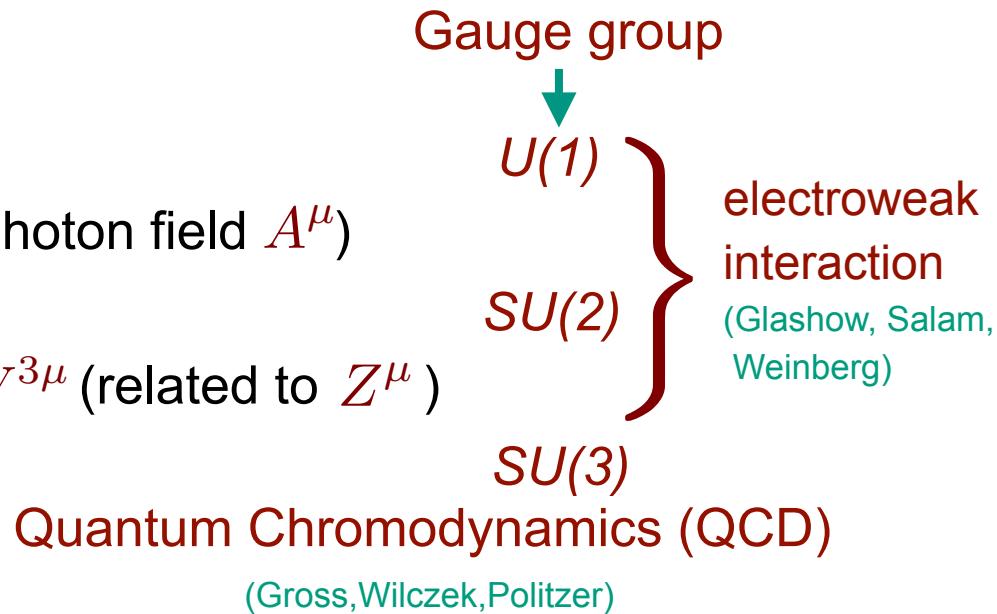
Gauge bosons

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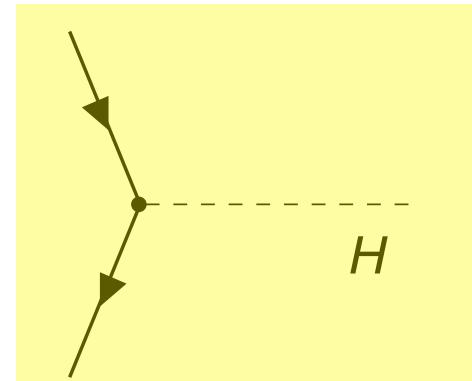
spin 1

- hypercharge:
one boson field B^μ (related to photon field A^μ)
- weak interaction:
three bosons $W^{+\mu}$, $W^{-\mu}$ and $W^{3\mu}$ (related to Z^μ)
- strong interaction:
eight gluons g_1^μ, \dots, g_8^μ



The Higgs boson h has **spin 0**. It has been discovered in **2012** by the **LHC** experiments **ATLAS** and **CMS**. It gives rise to two new types of interaction:

- the **Yukawa interaction** of the Higgs field with quarks and leptons
→ relevant for this talk,
- the **Higgs self-interaction**
→ hard to study experimentally.

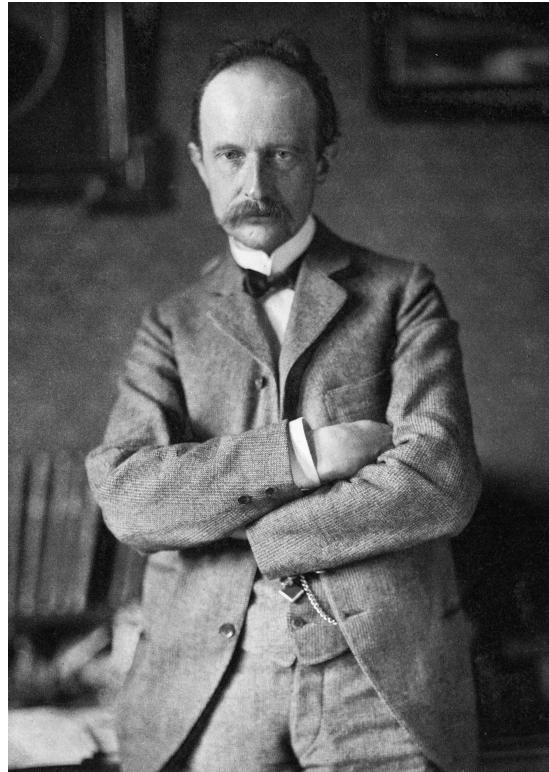


Natural units (Planck units)

$$\hbar = c = 1$$

Max Planck

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Max Planck stated that his natural units...

„...necessarily keep their relevance for all times and all,
also **extraterrestrial** and **non-human** cultures and therefore
can be denoted as natural “units of measure”.

translated from:

„...ihre Bedeutung für alle Zeiten und für alle, auch
außerirdische und **außermenschliche** Culturen notwendig
behalten und ... daher als natürliche „Maaßeinheiten“
bezeichnet werden können...“

Quark Yukawa interaction

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Three generations:

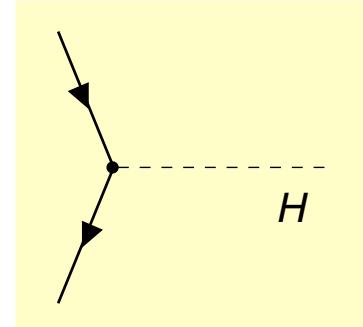
$(d_1, d_2, d_3) \equiv (d', s', b')$ for down, strange, and bottom quark
 $(u_1, u_2, u_3) \equiv (u', c', t')$ for up, charm, and top quark

Yukawa lagrangian:

$$-L_Y = Y_{jk}^d \bar{d}_L^j d_R^k \frac{h}{\sqrt{2}} + Y_{jk}^u \bar{u}_L^j u_R^k \frac{h}{\sqrt{2}} + \text{h.c.}$$

with two complex 3×3 matrices Y^d and Y^u .

→ uglier than the gauge interactions, many couplings!



Quark Yukawa interaction

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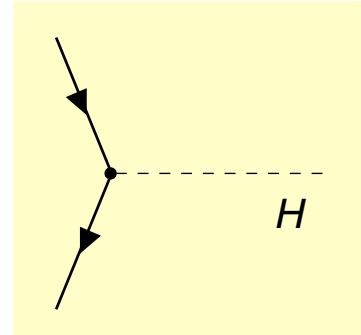
Yukawa lagrangian:

$$-L_Y = Y_{jk}^d \bar{d}_L^j d_R^k \frac{h}{\sqrt{2}} + Y_{jk}^u \bar{u}_L^j u_R^k \frac{h}{\sqrt{2}} + \text{h.c.}$$

Write $h = \sqrt{2}v + h'$, where h' represents the physical Higgs boson and v is the vacuum expectation value.

→ Two mass matrices $M^d = Y^d v$ and $M^u = Y^u v$!

To find the physical quark fields (d, s, b) and (u, c, t) we must diagonalise the mass matrices by unitary rotations of $\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}$ and $\begin{pmatrix} u' \\ c' \\ t' \end{pmatrix}$ (for both L and R).



Quark Yukawa interaction

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The unitary rotations diagonalising $M^d = Y^d v$ and $M^u = Y^u v$ drop out everywhere except in the coupling of the W boson:

$$L_W = \frac{g_2}{\sqrt{2}} [\bar{u}_L V \gamma^\mu d_L W_\mu^+ + \bar{d}_L V^\dagger \gamma^\mu u_L W_\mu^-]$$

weak gauge coupling

$\begin{pmatrix} u_L \\ c_L \\ t_L \end{pmatrix}$

unitary matrix 3×3

$\begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix}$

V is the
Cabibbo-Kobayashi-Maskawa
matrix or
quark mixing matrix

It is the only source of
transitions between quarks of
different fermion generations!

Cabibbo-Kobayashi-Maskawa matrix

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$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 0.97 & 0.23 & 0.0037 \cdot e^{-i\gamma} \\ -0.23 & 0.97 & 0.041 \\ 0.0085 \cdot e^{-i\beta} & -0.041 \cdot e^{i\beta_s} & 0.999 \end{pmatrix}$$

with $\gamma = 66^\circ$, $\beta = 22^\circ$, $\beta_s = 1.1^\circ$.

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 0.97 & 0.23 & 0.0037 \cdot e^{-i\gamma} \\ -0.23 & 0.97 & 0.041 \\ 0.0085 \cdot e^{-i\beta} & -0.041 \cdot e^{i\beta_s} & 0.999 \end{pmatrix}$$

with $\gamma = 66^\circ$, $\beta = 22^\circ$, $\beta_s = 1.1^\circ$. To summarise:

- The Yukawa interaction is the **only** source of transitions between quarks of different generations (**flavour violation**) in the Standard Model.
- Flavour violation **only** appears in the **W couplings**; its strength is encoded in V , e.g. the $W - \bar{u} - b$ coupling reads

$$L_{W\bar{u}b} = \frac{g_2}{\sqrt{2}} [\bar{u}_L V_{ub} \gamma^\mu b_L W_\mu^+ + \bar{b}_L V_{ub}^* \gamma^\mu u_L W_\mu^-]$$

...studies transitions between fermions of different generations.

flavour = fermion species

In the Standard Model flavour physics is the physics of the Yukawa sector.
This sector involves 10 parameters (for quarks):

- 6 quark masses \Rightarrow Yukawa couplings $y_q = \frac{m_q}{v}$
- 4 parameters in the unitary CKM matrix V :
- 3 angles
- 1 phase

\Rightarrow We “knew” Higgs couplings well before the Higgs was discovered.

Search for new physics

Energy vs. precision

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Cornerstones of quantum field theory:

- Forces are mediated by the exchange of **particles**, which are described by **fields**.
A particle of mass M mediates a force ranging over the distance $1/M$.
⇒ build colliders with higher energy to produce new heavy particles
- A particle with mass M contributes through **quantum effects** to physical processes at **energies well below M** (and is called a **virtual particle** in this context).
⇒ build high-precision experiments

We can organise particle physics in terms of hierarchical energy scales, thanks to the Appelquist-Carazzone decoupling theorem:

If a gauge theory valid at energy scale M_1 is embedded into a larger theory with new particles of mass $M_2 \gg M_1$, the effects on observables probed at the scale M_1 are suppressed by powers of M_1/M_2 .

Decoupling theorem

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Blessing:

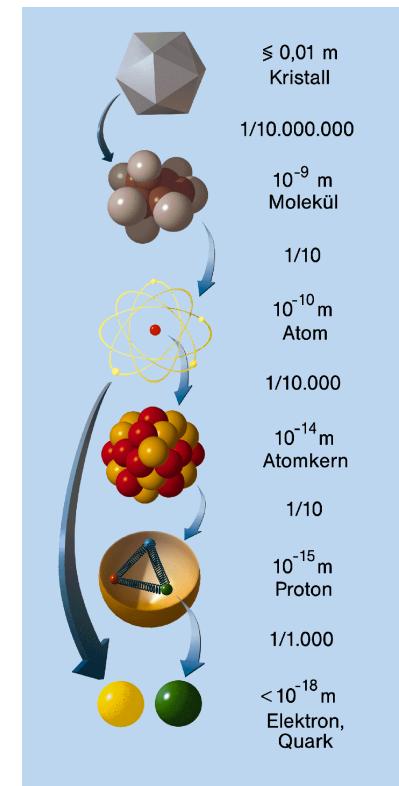
One could formulate e.g. atomic physics ($E_1 \sim 10 \text{ eV}$) without understanding nuclear physics ($E_2 \sim 100 \text{ MeV}$) and the SM ($E_2 \sim \sqrt{1/G_F} \sim 200 \text{ GeV}$) without understanding quantum gravity ($E_2 = M_{\text{Planck}} \sim \sqrt{1/G_N} \sim 10^{19} \text{ GeV}$).

Curse:

To find laws of physics beyond the SM (“new physics”) we must build colliders with $E_2 > E_{\text{SM}} \sim \sqrt{1/G_F}$ or with high statistics to reach the precision E_{SM}^2/E_2^2 .

G_F : Fermi constant

G_N : Newton constant



Physics beyond the Standard Model **KCETA**



The **Standard Model** correctly describes the physics probed at terrestrial experiments between $\sim 4\mu\text{eV}$ (Lamb shift) and $\sim 4\text{TeV}$ (LHC).

The most successful theory of science?

The **Standard Model** correctly describes the physics probed at terrestrial experiments between $\sim 4\mu\text{eV}$ (Lamb shift) and $\sim 4\text{TeV}$ (LHC).

The most successful theory of science?

The **Standard Model**

...fails in cosmology:

- no dark-matter particle
- violates **Sakharov** criteria,
no explanation of surplus of
matter over antimatter
- no explanation of dark energy

...has severe shortcomings:

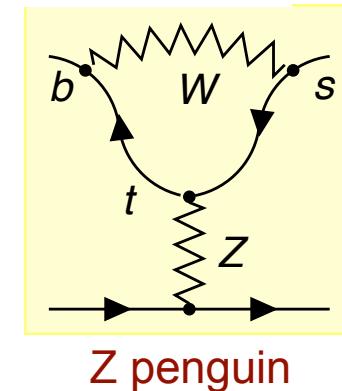
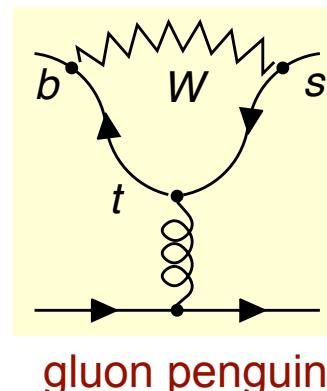
- no explanation of charge
quantisation, why is $Q(e) = 3Q(d)$?
- unclear nature of neutrino fields
- **26** or **28** free parameters,
unpredicted masses
- no gravity

Precision flavour physics

Prime strategy for precision physics: Identify observables for which the **SM contribution** is **parametrically suppressed**, while permitting unsuppressed **new-physics** contributions.

⇒ flavour-changing neutral current (FCNC) processes

In the Standard Model **FCNC** transitions are **loop-suppressed** quantum effects.



In the **flavour-changing neutral current (FCNC)** processes of the Standard Model several suppression factors pile up:

- FCNCs proceed through **electroweak loops**, no FCNC tree graphs,
- small CKM elements, e.g. $|V_{ts}| = 0.04$, $|V_{td}| = 0.01$,
- Suppression of loops with charm or down-type quarks,
 $\propto (m_c^2 - m_u^2)/M_W^2$, $(m_s^2 - m_d^2)/M_W^2$
(Glashow-Iliopoulos-Maiani effect).
- helicity suppression in radiative and leptonic decays,
because FCNCs involve only **left-handed** fields, so helicity flips bring a factor of m_b/M_W or m_s/M_W .

Generic models of new physics typically have new sources of unsuppressed **FCNC** transitions.

Examples:

extra Higgses \Rightarrow Higgs-mediated **FCNC's** at tree-level ,
helicity suppression possibly absent,

squarks/gluinos \Rightarrow **FCNC** quark-squark-gluino coupling,
no CKM/GIM suppression,

vector-like quarks \Rightarrow **FCNC** couplings of an extra Z' ,

$SU(2)_R$ gauge bosons \Rightarrow helicity suppression absent

Flavoured mesons

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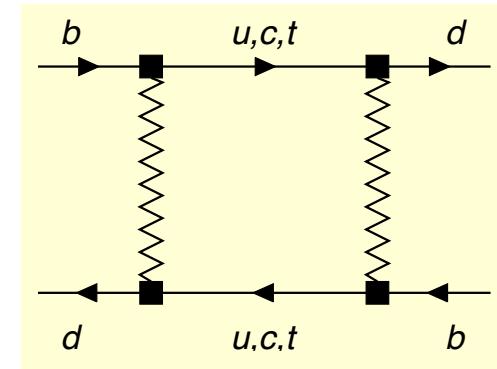
charged:

$$\begin{aligned} K^+ &\sim \bar{s}u, & D^+ &\sim \bar{c}\bar{d}, & D_s^+ &\sim \bar{c}\bar{s}, & B^+ &\sim \bar{b}u, & B_c^+ &\sim \bar{b}\bar{c}, \\ K^- &\sim s\bar{u}, & D^- &\sim \bar{c}d, & D_s^- &\sim \bar{c}s, & B^- &\sim b\bar{u}, & B_c^- &\sim b\bar{c}, \end{aligned}$$

neutral:

$$\begin{aligned} K &\sim \bar{s}d, & D &\sim \bar{c}\bar{u}, & B_d &\sim \bar{b}\bar{d}, & B_s &\sim \bar{b}s, \\ \bar{K} &\sim s\bar{d}, & \bar{D} &\sim \bar{c}u, & \bar{B}_d &\sim b\bar{d}, & \bar{B}_s &\sim b\bar{s}, \end{aligned}$$

The neutral K , D , B_d and B_s mesons mix with their antiparticles, \bar{K} , \bar{D} , \bar{B}_d and \bar{B}_s thanks to the weak interaction (quantum-mechanical two-state systems).

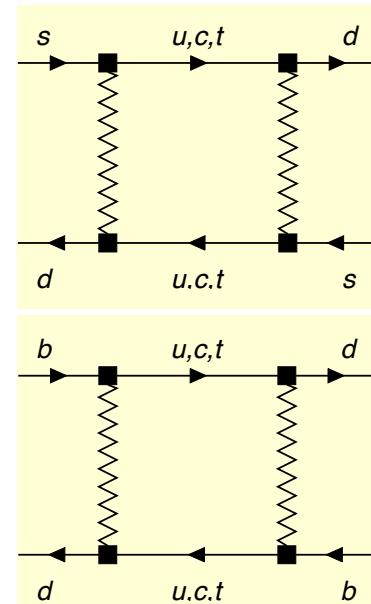


New-physics discoveries of the past KCETA



...with FCNC processes:

- Charge-parity (**CP**) symmetry violation in $K \rightarrow \pi^+ \pi^-$: Effect of top quark in $K - \bar{K}$ mixing: $\frac{m_t}{m_K} \approx 350!$ Christenson,Cronin,Fitch,Turlay; 1964
- Charm quark from $K \rightarrow \mu^+ \mu^-$ and $K - \bar{K}$ mixing
Glashow,Iliopoulos,Maiani;Gaillard
- Heaviness of top quark: $B_d - \bar{B}_d$ mixing
Schröder,Zaitsev (ARGUS at DESY) 1987
- Direct CP violation in $K \rightarrow \pi\pi$ Kleinknecht et al. (NA31,NA64 at CERN)
- ...



Recall:

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 0.97 & 0.23 & 0.0037 \cdot e^{-i\gamma} \\ -0.23 & 0.97 & 0.041 \\ 0.0085 \cdot e^{-i\beta} & -0.041 \cdot e^{i\beta_s} & 0.999 \end{pmatrix}$$

$|V_{cb}|$ is small

- ⇒ The total b decay rate Γ_{tot} is suppressed by a factor of at least $|V_{cb}|^2 = 1.8 \cdot 10^{-3}$!
- ⇒ Large B meson lifetimes!
- ⇒ Interesting branching ratios $\frac{\Gamma(B \rightarrow f)}{\Gamma_{\text{tot}}}$ enhanced!
- Motivation for dedicated B physics experiments!

Experiments

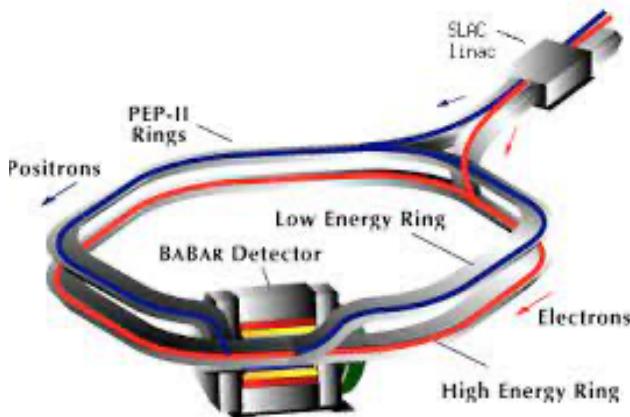
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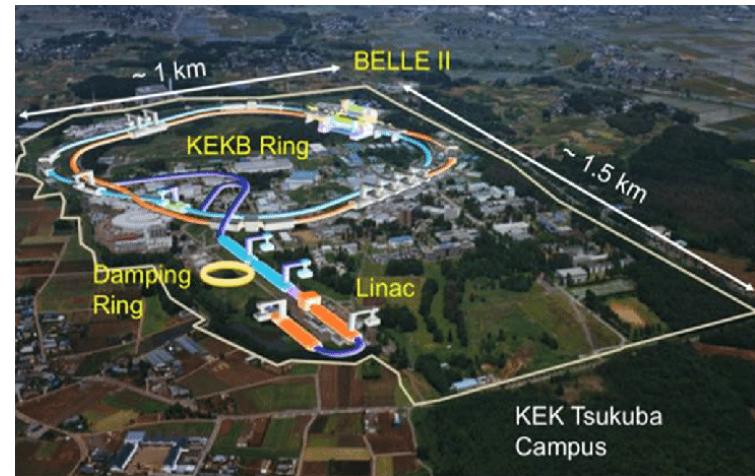
Asymmetric B factories: $e^+ e^-$ colliders with different energies of the e^+ and e^- beams (3.1 GeV vs. 9 GeV).

Center-of-mass energy: $\sqrt{s} = M_{\Upsilon(4S)} = 10.58 \text{ GeV}$.

Only $B_d \bar{B}_d$ and $B^+ B^-$ pairs produced!



PEP-II collider with BaBar experiment
SLAC, USA, 1999-2008



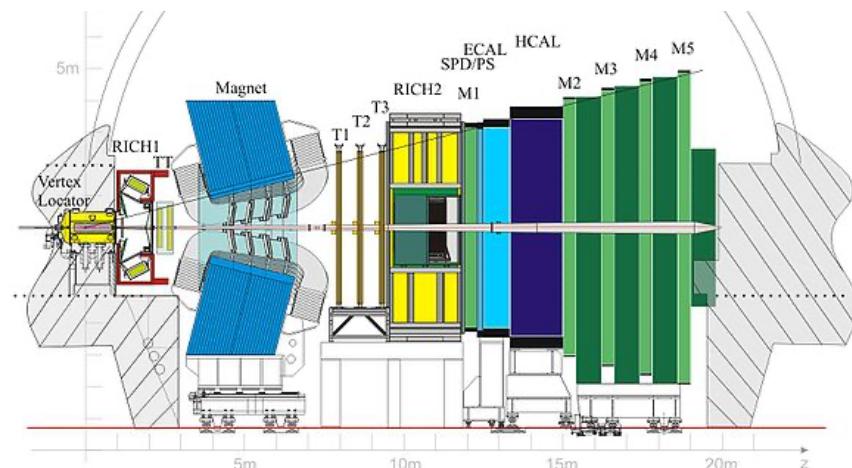
Super-KEKB collider with Belle experiment
KEK, Tsukuba, Japan, 1999-2010,
Belle II since 2018

Experiments

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LHCb at CERN, Geneva, Switzerland, since 2010: *pp* collisions



All b-flavoured hadrons are produced: $B^\pm, B_d, \bar{B}_d, B_s, \bar{B}_s, B_c^\pm, \Lambda_b$ and other baryons.
 $\Lambda_b \sim bud$

Flavour anomalies

Flavour anomalies

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In recent years several **discrepancies** between measurements (of branching ratios and/or angular decay distributions) and **SM** predictions have emerged, denoted as *flavour anomalies*.

Flavour anomalies

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- $b \rightarrow s\mu^+\mu^-$: Deficit for $q^2 < 6 \text{ GeV}$, where q^2 is the invariant mass of the muon pair, statistical significance σ grows since 2013 to σ between 4.4 and 7.3 in a combination of data on $B \rightarrow K\ell^+\ell^-$, $B \rightarrow K^*\ell^+\ell^-$ with $\ell = e, \mu$ and $B_s \rightarrow \phi\mu^+\mu^-$.

$$\phi \sim s\bar{s}$$

(Alguero et al. 2022, Geng et al 2021, Hurth et al. 2022, Cornella et al. 2021)

- Anomalous magnetic moment of the muon, $(g - 2)_\mu \propto y_\mu$ Yukawa coupling deviation from SM prediction is 4.2 σ .

(Muon g-2 Coll, Fermilab, USA, 2021; BNL AGS-E821 Brookhaven, USA)

- $b \rightarrow c\tau\nu$: Enhancement of the ratios of branching ratios $B(B \rightarrow D\tau\nu)/B(B \rightarrow D\ell\nu)$ and $B(B \rightarrow D^*\tau\nu)/B(B \rightarrow D^*\ell\nu)$. Discrepancy at 3.2 σ with some inconsistency between experiments.

(BaBar, Belle, LHCb)

$$b \rightarrow s\mu^+\mu^-$$

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Measured quantities:

$$R_{K^*} = \frac{B(B \rightarrow K^*\mu^+\mu^-)}{B(B \rightarrow K^*e^+e^-)}, \quad R_K = \frac{B(B \rightarrow K\mu^+\mu^-)}{B(B \rightarrow Ke^+e^-)}, \quad B(B_s \rightarrow \phi\mu^+\mu^-)$$

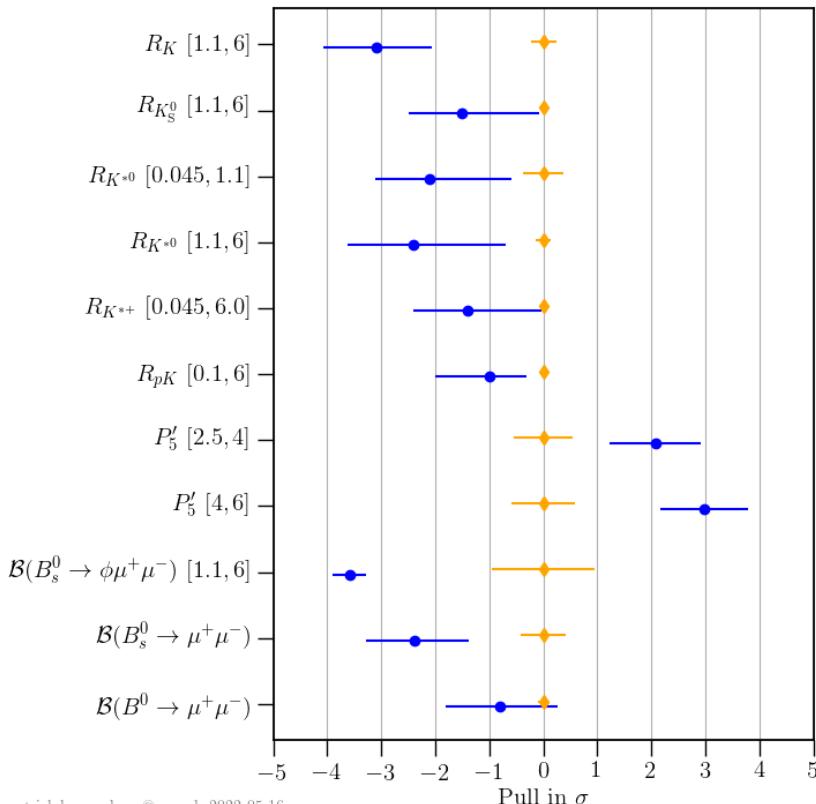
for several bins of q^2 , the invariant mass of the lepton pair.

The error of the **SM** predictions of R_K, R_{K^*} is essentially zero.

R_K, R_{K^*} are equal to 1 in the **SM** (except for very low q^2).

In $B \rightarrow K^*\mu^+\mu^-$ also angular distributions of the decay products are measured, here theory predictions and estimate of their uncertainties are more difficult. Quantity with deviation: P'_5

$b \rightarrow s\mu^+\mu^-$



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No pull of an individual quantity is above 4σ .

In **B physics** measurements are highly redundant, different observables depend on the same theoretical quantities.

→ Need combined analyses and likelihood ratio tests between best-fit point and SM point for the theoretical parameters.

Effective hamiltonian

At the energy scale of a B decay, $m_b \sim 5 \text{ GeV}$, interactions mediated by much heavier particles appear point-like.

Concept: Derive an **effective hamiltonian** with four-fermion operators:

$$H = -\frac{4G_F V_{tb} V_{ts}^*}{\sqrt{2}} \sum_{\ell, \ell' = e, \mu, \tau} [C_9^{\ell\ell'} O_9^{\ell\ell'} + C_{10}^{\ell\ell'} O_{10}^{\ell\ell'}] + \dots$$

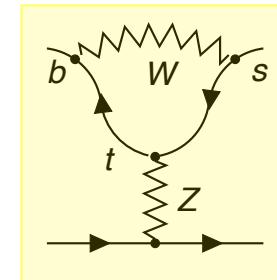
The couplings of the effective operators are called **Wilson coefficients** and are calculated from the Feynman diagrams.

We are interested in

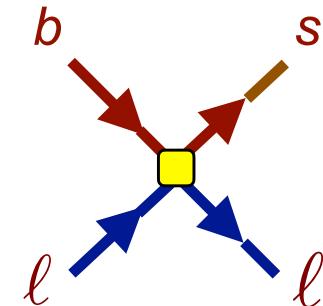
$$O_9^{\ell\ell'} = \frac{\alpha}{4\pi} [\bar{s}_L \gamma^\mu b_L] [\bar{\ell} \gamma_\mu \ell'], \quad O_{10}^{\ell\ell'} = \frac{\alpha}{4\pi} [\bar{s}_L \gamma^\mu b_L] [\bar{\ell} \gamma_\mu \gamma^5 \ell']$$

α is the QED coupling (Sommerfeld constant).

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Four-fermion interaction as in
Fermi theory of beta decay:



Semileptonic FCNC operators

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Operators:

$$O_9^{\ell\ell'} = \frac{\alpha}{4\pi} [\bar{s}_L \gamma^\mu b_L] [\bar{\ell} \gamma_\mu \ell'], \quad O_{10}^{\ell\ell'} = \frac{\alpha}{4\pi} [\bar{s}_L \gamma^\mu b_L] [\bar{\ell} \gamma_\mu \gamma^5 \ell']$$

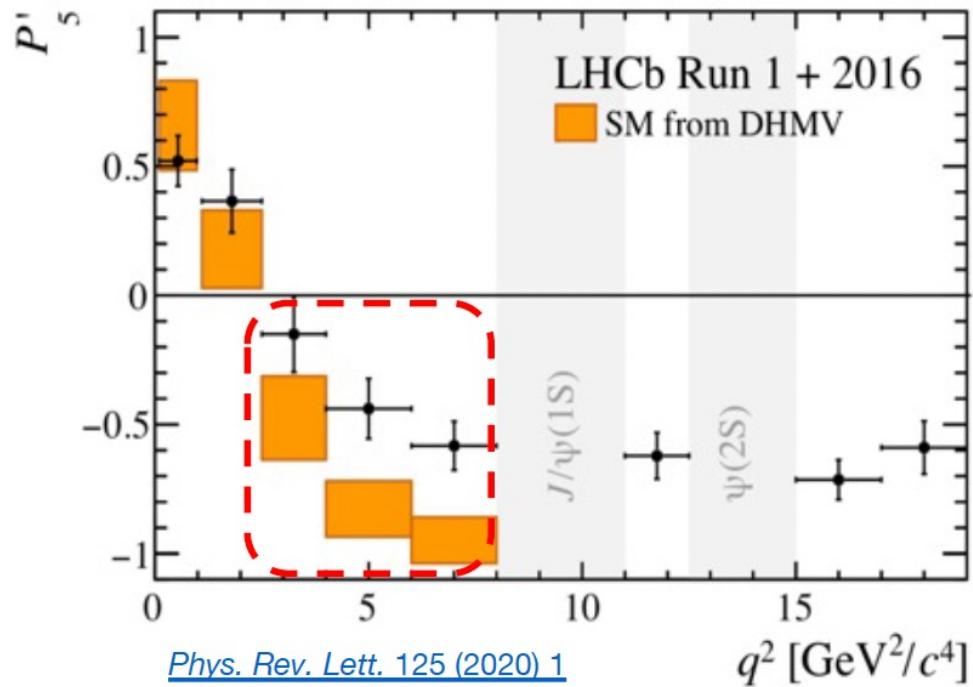
Coefficients: In the Standard Model

$$C_{9,10} \equiv C_{9,10}^{ee} = C_{9,10}^{\mu\mu} = C_{9,10}^{\tau\tau}$$

and

$$C_{9,10}^{\ell\ell'} = 0 \quad \text{for } \ell \neq \ell'$$

Angular distribution



The decay $B \rightarrow K^* \ell^+ \ell^-$ can be described by three angles and q^2 .

P'_5 is calculated from the number of decays counted in a certain direction characterised by these angles.

Lepton flavour universality

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$$R_{K^*} = \frac{B(B \rightarrow K^* \mu^+ \mu^-)}{B(B \rightarrow K^* e^+ e^-)} \quad \text{and} \quad R_K = \frac{B(B \rightarrow K \mu^+ \mu^-)}{B(B \rightarrow K e^+ e^-)}$$

are predicted to 1 in the SM, because W , Z , and photon couple to all charged leptons with the same coupling:

lepton universality of the electroweak interaction

Experimental results

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$$\underline{B^0 \rightarrow K^{*0} \ell^+ \ell^-} \text{ (3 fb}^{-1}\text{)}$$

$$R_{K^{*0}} = 0.66^{+0.11}_{-0.07}(\text{stat}) \pm 0.03(\text{syst})$$

$$[0.045 < q^2/\text{GeV}^2 < 1.1]$$

$$R_{K^{*0}} = 0.69^{+0.11}_{-0.07}(\text{stat}) \pm 0.05(\text{syst})$$

$$[1.1 < q^2/\text{GeV}^2 < 6.0]$$

2.2–2.5 σ deviation from SM in each bin. [\[JHEP 08 \(2017\) 55\]](#)

$$\underline{B^+ \rightarrow K^+ \ell^+ \ell^-} \text{ (9 fb}^{-1}\text{)}$$

with same trend in other $b \rightarrow s\mu^+\mu^-$ modes

$$R_{K^+} = 0.846^{+0.042}_{-0.039}(\text{stat})^{+0.013}_{-0.012}(\text{syst})$$

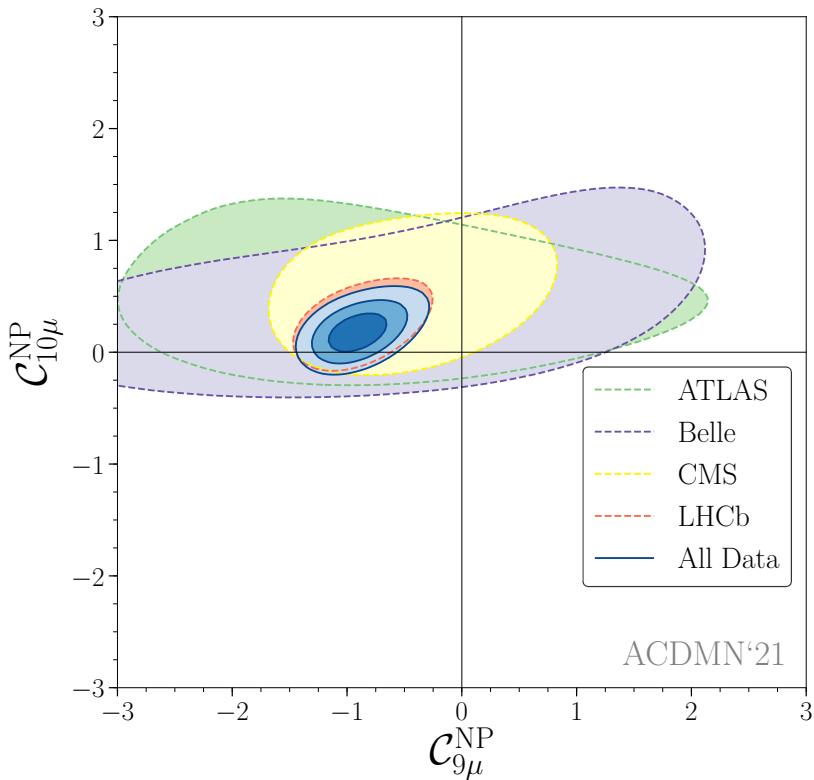
3.1 σ deviation from SM.

[\[Nature Physics 18, \(2022\) 277-282\]](#)

courtesy of Johannes Albrecht, LHCb

Global fit

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Operators:

$$O_9^{\ell\ell'} = \frac{\alpha}{4\pi} [\bar{s}_L \gamma^\mu b_L] [\bar{\ell} \gamma_\mu \ell'],$$

$$O_{10}^{\ell\ell'} = \frac{\alpha}{4\pi} [\bar{s}_L \gamma^\mu b_L] [\bar{\ell} \gamma_\mu \gamma^5 \ell']$$

Fit to new-physics (NP) contribution to $C_{9,10}^{\mu\mu}$ using all data (also those complying with the SM).

(Alguero et al, *Eur.Phys.J.C* 82 (2022) 4, 326)

Explanations

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Experimental issues:

The combined significance of the anomaly is too large for a statistical fluctuation.

Could the efficiencies for e or μ detection be incorrectly estimated?

LHCb measures double ratios:

$$\underbrace{\frac{B(B \rightarrow K^{(*)} \mu^+ \mu^-)}{B(B \rightarrow K^{(*)} e^+ e^-)}}_{R_{K^{(*)}}} \cdot \underbrace{\frac{B(B \rightarrow K^{(*)} J/\psi [\rightarrow e^+ e^-])}{B(B \rightarrow K^{(*)} J/\psi [\rightarrow \mu^+ \mu^-])}}_{\frac{B(J/\psi \rightarrow e^+ e^-)}{B(J/\psi \rightarrow \mu^+ \mu^-)}} = 1 \text{ (measured)}$$

J/ψ is a narrow (c, \bar{c}) resonance with mass 3.1 GeV contributing to $B \rightarrow K^{(*)} \ell^+ \ell^-$ for $q^2 = (3.1 \text{ GeV})^2 = 9.6 \text{ GeV}^2$.

Explanations

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Experimental issues:

To first approximation the e and μ efficiencies cancel from the ratio

$$\frac{B(B \rightarrow K^{(*)} \mu^+ \mu^-)}{B(B \rightarrow K^{(*)} e^+ e^-)} \cdot \frac{B(B \rightarrow K^{(*)} J/\psi [\rightarrow e^+ e^-])}{B(B \rightarrow K^{(*)} J/\psi [\rightarrow \mu^+ \mu^-])} ,$$

but in the interesting bins $q^2 \in [0.045, 1.1]$ and $q^2 \in [1.1, 6]$ the angle between the two leptons is smaller than for $q^2 = (3.1 \text{ GeV})^2 = 9.6 \text{ GeV}^2$.

Currently all LHCb data on $R_{K^{(*)}}$ are re-analysed by a new team.

“Extraordinary claims require extraordinary evidence.”

(Sherlock Homes in The Sign of Four)

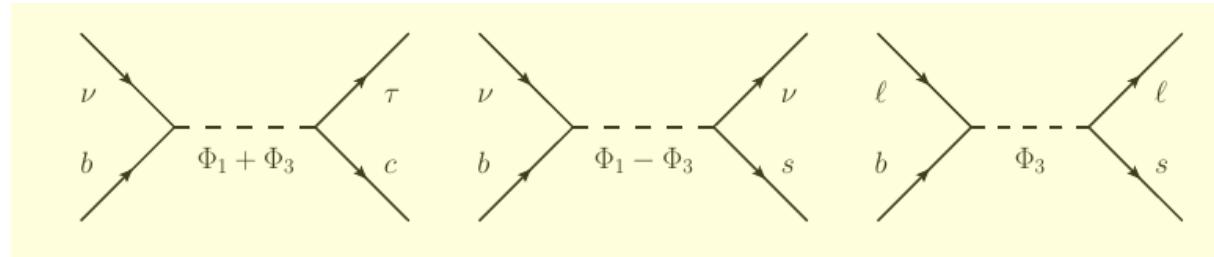
Explanations

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New physics:

- Leptoquarks:
 - bosons with quark-lepton coupling
 - can also explain $(g - 2)_\mu$ and $b \rightarrow c\tau\nu$ anomalies



- appear in **SU(4)** gauge theories, where lepton number is the fourth colour
- Z' boson related to a new gauged U(1) symmetry, maybe $L_\mu - L_\tau$ (difference of muon and tau lepton number)
- may help with $(g - 2)_\mu$ but not with $b \rightarrow c\tau\nu$

$$b \rightarrow c\tau\bar{\nu}$$

studied through

$$R(D) = \frac{B(B \rightarrow D\tau\bar{\nu})}{B(B \rightarrow D\ell\bar{\nu})}$$

and

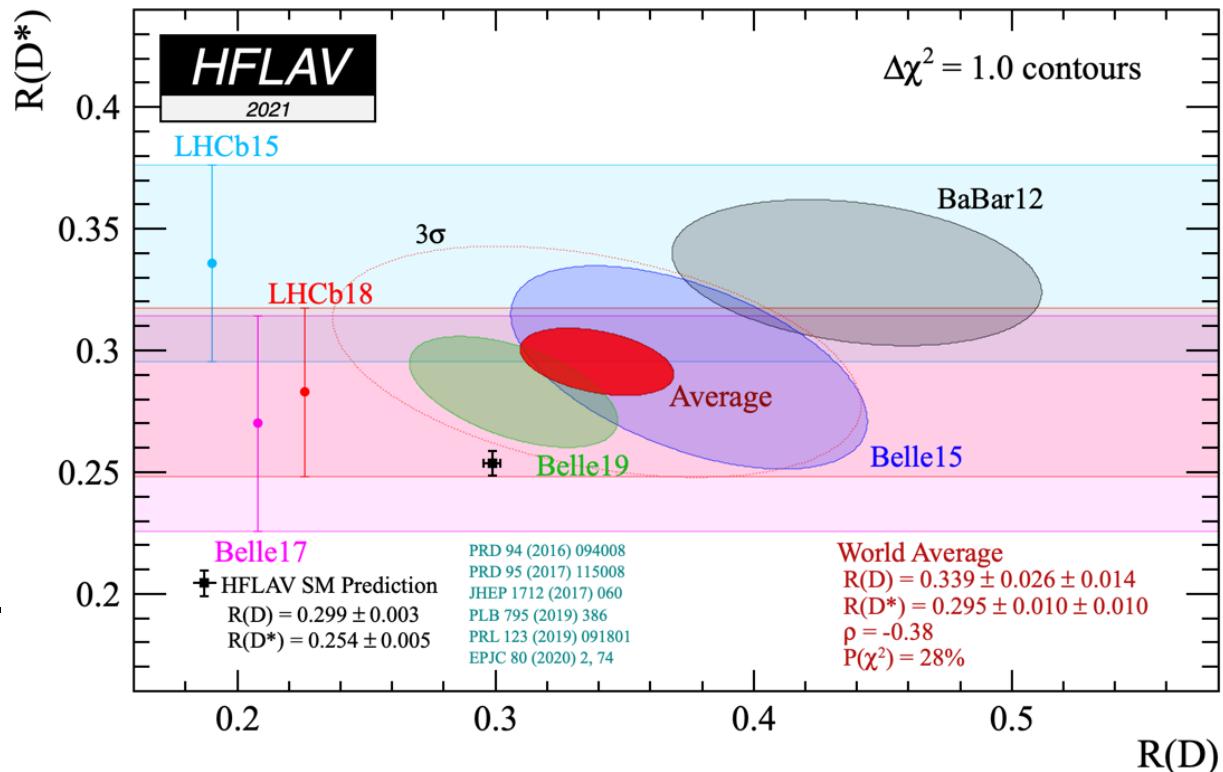
$$R(D^*) = \frac{B(B \rightarrow D^*\tau\bar{\nu})}{B(B \rightarrow D^*\ell\bar{\nu})}$$

at

BaBar, Belle, LHCb and
in the future also Belle II.

Here $\ell = e, \mu$.

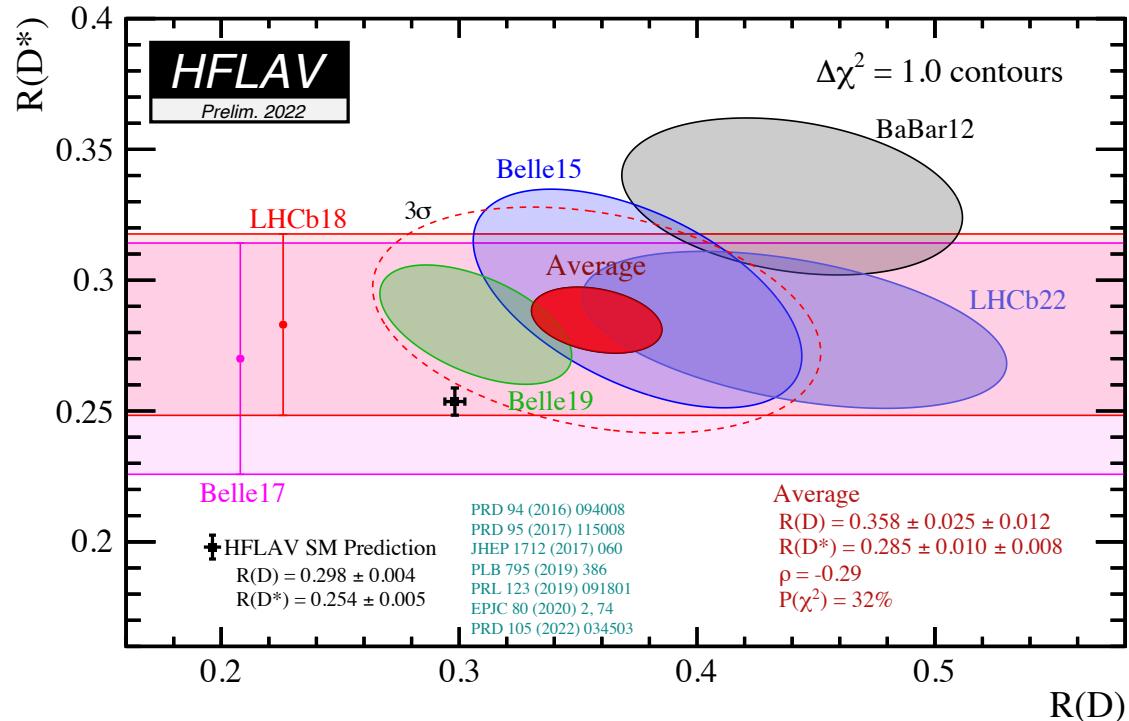
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$b \rightarrow c\tau\bar{\nu}$

New development: first combined measurements of $R(D)$ and $R(D^*)$ by LHCb,
supporting large $R(D)$ of BaBar,
increasing consistency between all measurements .

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$$b \rightarrow c\tau\bar{\nu}$$

Lepton-flavour universality violation in a tree-level decay (all HFLAV):

$$R(D)$$

exp : $0.358 \pm 0.025 \pm 0.012$

SM : 0.298 ± 0.004

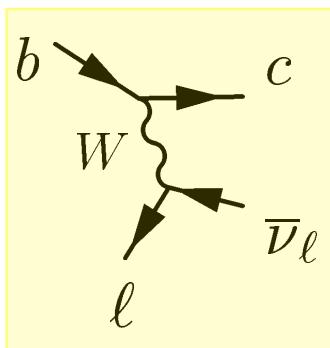
significance: 3.2σ

$$R(D^*)$$

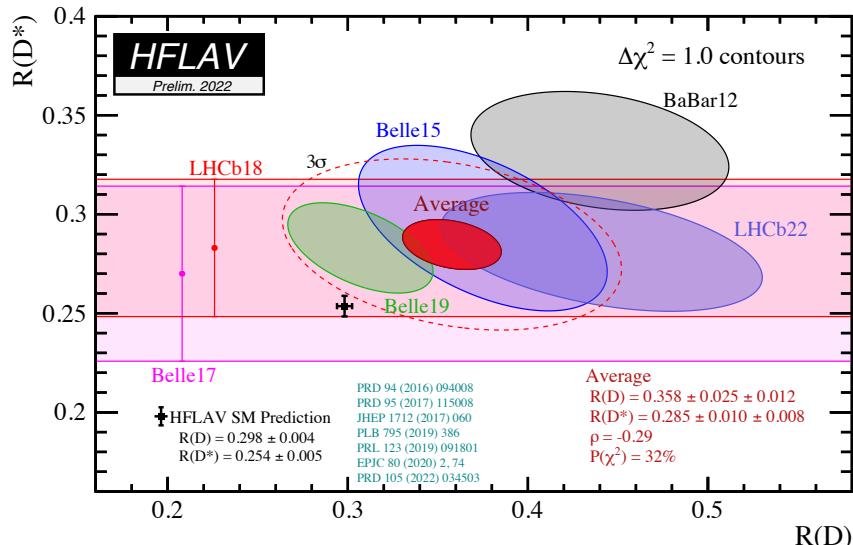
$0.285 \pm 0.010 \pm 0.008$

0.254 ± 0.005

- tensions among different experimental analyses
- effect is (too?) large



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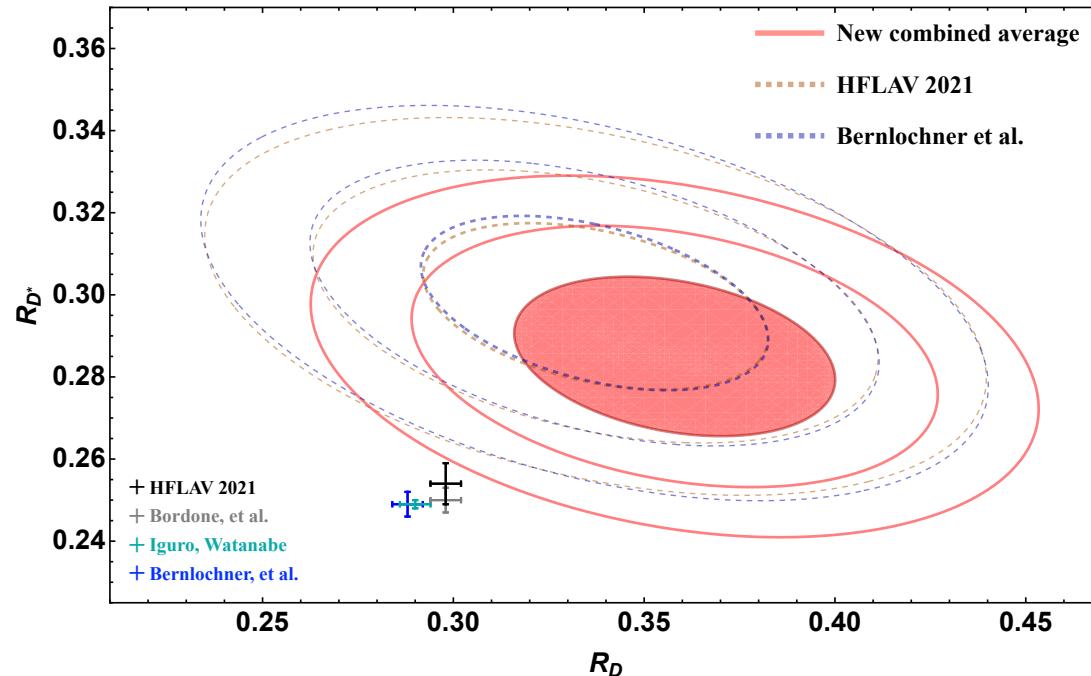
Heavy Flavour Averaging Group,
<https://hflav.web.cern.ch/content/semileptonic-b-decays>

$b \rightarrow c\tau\bar{\nu}$

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S. Iguro, T. Kitahara, R. Watanabe, arXiv:2210.10751



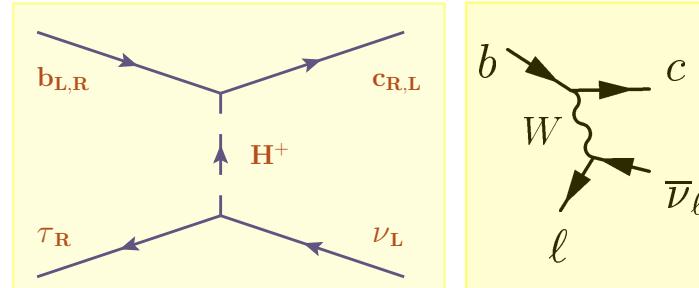
New-physics explanations

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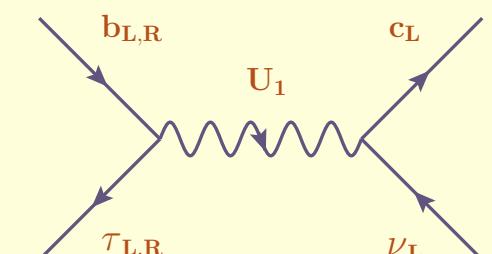
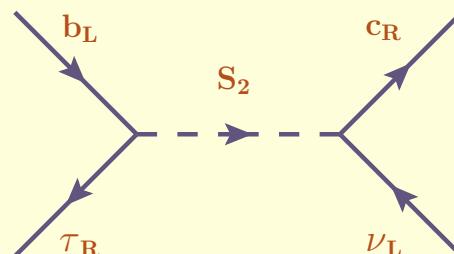
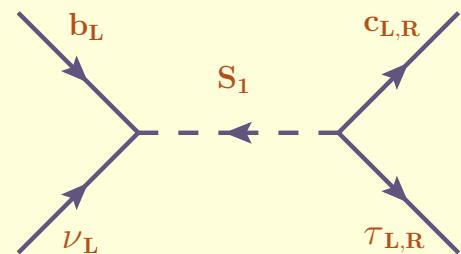


$b \rightarrow c\tau\bar{\nu}$ was known to be sensitive to effects of a hypothetical charged Higgs boson since 1992.

(Grzadkowski,Hou, Phys. Lett. B **283** (1992) 427)



Leptoquarks:



spin 0, SU(2) singlet, $Q=1/3$

spin 0, SU(2) doublet, $Q=2/3$

spin 1, SU(2) singlet, $Q=2/3$

New-physics explanations

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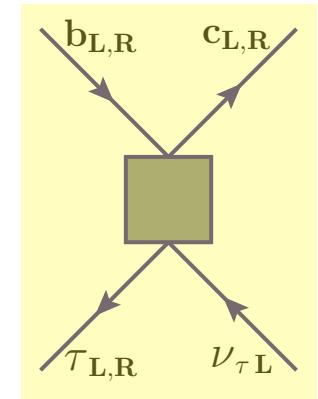
As in the case of $b \rightarrow s\mu^+\mu^-$ we can accomodate all types of new physics in terms of effective four-quark operators.

$$O_V^L = \bar{c}_L \gamma^\mu b_L \bar{\tau}_L \gamma_\mu \nu_{\tau L},$$

$$O_S^R = \bar{c}_L b_R \bar{\tau}_R \nu_{\tau L},$$

$$O_S^L = \bar{c}_R b_L \bar{\tau}_R \nu_{\tau L},$$

$$O_T = \bar{c}_R \sigma^{\mu\nu} b_L \bar{\tau}_R \sigma_{\mu\nu} \nu_{\tau L}.$$



(Blanke,Crivellin,de Boer,UN,Nisandzic,Kitahara,*Phys.Rev.D* 100(2019) 3, 035035)

New-physics explanations

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Fit the corresponding coefficients $C_V^L, C_S^{R,L}, C_T$ to $R(D)$, $R(D^*)$, and the tau polarisation asymmetry

$$P_\tau(D^*) = -0.38 \pm 0.51_{-0.16}^{+0.21} \quad (\text{Belle 2017})$$

and the fraction of longitudinally polarised D^* mesons

$$F_L(D^*) = 0.60 \pm 0.08 \pm 0.035 \quad (\text{Belle 2018})$$

Blanke,Crivellin,de Boer,Kitahara,Moscati,UN,Nisandzic, *Phys.Rev.D* 99 (2019) 7, 075006;
Blanke,Crivellin,de Boer,Kitahara,UN,Nisandzic, *Phys.Rev.D* 100(2019) 3, 035035

New-physics explanations

coefficients

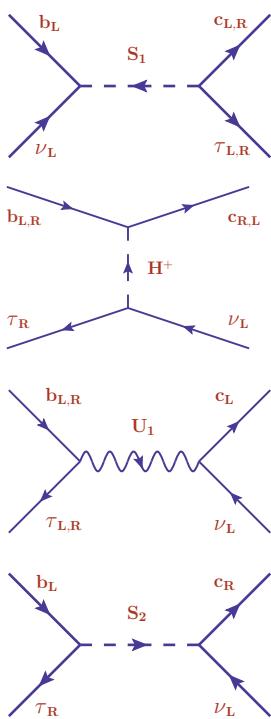
real C_V^L , $C_S^L = -4C_T$

real C_S^R , C_L^L

real C_V^L , C_S^R

$\text{Re}[C_S^L = 4C_T]$, $\text{Im}[C_S^L = 4C_T]$

motivated by



All scenarios fit the $B \rightarrow D^{(*)}\tau\bar{\nu}$ data, with different predictions for $F_L(D^*)$ and $B(B_c^+ \rightarrow \tau^+\nu)$.

- H^+ : either $B(B_c^+ \rightarrow \tau^+\nu) > 0.3$ or $R(D^*)$ will come down, larger $F_L(D^*)$.
- S_1 and U_1 : smaller (SM-like) $F_L(D^*)$; U_1 can also explain $b \rightarrow s\mu^+\mu^-$ and $(g-2)_\mu$.
- S_2 : similar to H^+ , but small $F_L(D^*)$ testable at ATLAS and CMS.

Sum rule for $b \rightarrow c\tau\bar{\nu}$

$R(D^*)$ and $R(D)$ are correlated with

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$$R(\Lambda_c) = \frac{B(\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu})}{B(\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu})} , \quad \text{where } \Lambda_b \sim bud, \quad \Lambda_c \sim cud :$$

$$\frac{\mathcal{R}(\Lambda_c)}{\mathcal{R}_{\text{SM}}(\Lambda_c)} = 0.262 \frac{\mathcal{R}(D)}{\mathcal{R}_{\text{SM}}(D)} + 0.738 \frac{\mathcal{R}(D^*)}{\mathcal{R}_{\text{SM}}(D^*)} + x.$$

with $|x| < 0.05$ in any scenario of new physics.

(Blanke, Crivellin, de Boer, UN, Nisandzic, Kitahara, *Phys. Rev. D* 100(2019) 3, 035035)

Sum rule for $b \rightarrow c\tau\bar{\nu}$

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$$\frac{\mathcal{R}(\Lambda_c)}{\mathcal{R}_{\text{SM}}(\Lambda_c)} = 0.262 \frac{\mathcal{R}(D)}{\mathcal{R}_{\text{SM}}(D)} + 0.738 \frac{\mathcal{R}(D^*)}{\mathcal{R}_{\text{SM}}(D^*)} + x.$$

Our 2019 prediction:

$$R(\Lambda_c) = R_{\text{SM}}(\Lambda_c) (1.15 \pm 0.04) = 0.38 \pm 0.01 \pm 0.01$$

Tension with 2022 LHCb measurement:

$$R(\Lambda_c) = 0.242 \pm 0.026 \pm 0.040 \pm 0.059$$

(LHCb, *Phys.Rev.Lett.* 128 (2022) 19, 191803)

→ with future data either $R(D^{(*)})$ will come down or $R(\Lambda_c)$ will go up.

New-physics explanations

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2022 updates include

$$R(J/\psi) = 0.71 \pm 0.17 \pm 0.18 \text{ (Belle 2018)}$$

vs. $R(J/\psi)_{\text{SM}} = 0.258 \pm 0.004$ (HPQCD)

and

$$R(\Lambda_b) = 0.242 \pm 0.026 \pm 0.040 \pm 0.059 \text{ (LHCb 2022)}$$

vs. $R(\Lambda_b)_{\text{SM}} = 0.324 \pm 0.004$ (Detmold et al. 2015)

2022 updates:

Iguro, Kitahara, Watanabe,

Global fit to $b \rightarrow c\tau\nu$ anomalies 2022 mid-autumn, arXiv:2210.10751

Fedele, Blanke, Crivellin, Iguro, Kitahara, UN, Watanabe,

Impact of $\Lambda_b \rightarrow \Lambda_c \tau\nu$ measurement on New Physics in $b \rightarrow c l\nu$ transitions, arXiv:2211.14172.

$$\frac{R(\Lambda_c)}{R(\Lambda_c)_{\text{SM}}} = 0.280 \frac{R(D)}{R(D)_{\text{SM}}} + 0.720 \frac{R(D^*)}{R(D^*)_{\text{SM}}} + x$$

Fedele, Blanke, Crivellin, Iguro, Kitahara, UN, Watanabe, arXiv:2211.14172.

Prediction unchanged:

$$R(\Lambda_c) = 0.380 \pm 0.012 \pm 0.005$$

compared to 2019:

$$R(\Lambda_c) = 0.38 \pm 0.01 \pm 0.01$$

The sum rule assumes that new physics only affects the τ mode.
Can one relax the constraint by permitting new physics also in
 $b \rightarrow c\ell\nu$ with a light lepton $\ell = e, \mu$?

⇒ Even in a fit permitting arbitrary new physics in both τ and light lepton modes does not relieve the tension between $R(D^{(*)})$ and $R(\Lambda_c)$.

Fedele, Blanke, Crivellin, Iguro, Kitahara, UN, Watanabe, arXiv:2211.14172.

Summary

Summary

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- Flavour physics probes **virtual effects of heavy particles** with masses far above the reach of high- p_T experiments.
- Predictions of **BSM theories** for **B physics** observables are highly **correlated**, because many quantities depend on few (calculable) coefficients encoding the BSM effects. → **intrinsic redundancy of B physics**
- Combining all data on $b \rightarrow s\mu^+\mu^-$ data reveals a tension on the Standard Model with a significance between 4.4σ and 7.3σ in likelihood ratio tests.
- $b \rightarrow s\mu^+\mu^-$ can be explained with a leptoquark with mass below **40 TeV**.
→ Precision physics can give guidance for the design of future collider.
- Leptoquarks can also explain anomalous data in $(g - 2)_\mu$ and $b \rightarrow c\tau\bar{\nu}$.
- The new LHCb measurement of $R(\Lambda_c)$ points to inconsistent measurements of at least one of $R(D)$, $R(D^*)$, or $R(\Lambda_c)$ irrespective of the presence of BSM physics.
→ Redundancy of B physics helps to **disentangle BSM physics from mistakes**.

$b \rightarrow s\mu^+\mu^-$ penguin diagrams

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wake-up call for new physics?