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```
clear all; close all; clc
```

H_Trans

```
clc

%Create Homogeneous Transformations from fundamental rotations/
translations
H=H_Trans.rotZ(sym(pi/2))
H.Trans=[1;2;3];

%Access and modify sections of the transformation
Matrix=H.H
Rotation=H.Rot
Translation=H.Trans

disp('Get Euler Angles');
Euler=H.Euler
disp('Set Euler Angles');
H.Euler = [pi/2,0,0];
eval(H.Rot)
H.Euler

syms theta d a alpha

disp('Create From DH Parameters');
DH=H_Trans.fromDH([theta,d,a,alpha]);
DH.H

disp('Fast Inverse');
DH.inv.H

H_Trans().draw(1,'0')
hold on
H.draw(1,'1')
hold off
```

$H =$

H_Trans with properties:

H: [4x4 sym]
Trans: [3x1 sym]
Rot: [3x3 sym]
Euler: [3x1 sym]
Wrench: [6x1 sym]
Column: [16x1 sym]

Matrix =

[0, -1, 0, 1]
[1, 0, 0, 2]
[0, 0, 1, 3]
[0, 0, 0, 1]

Rotation =

[0, -1, 0]
[1, 0, 0]
[0, 0, 1]

Translation =

1
2
3

Get Euler Angles

Euler =

0
0
pi/2

Set Euler Angles

ans =

1.0000	0	0
0	0.0000	-1.0000
0	1.0000	0.0000

ans =

1.5708	0	0
--------	---	---

Create From DH Parameters

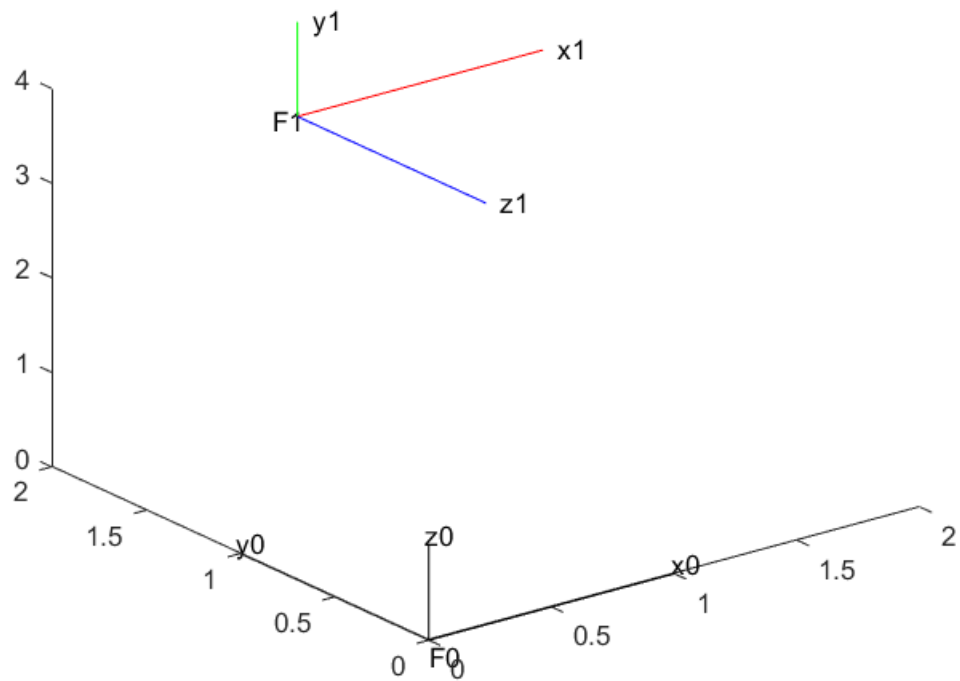
ans =

```
[ cos(theta), -1.0*cos(alpha)*sin(theta),      sin(alpha)*sin(theta),  
  a*cos(theta)]  
[ sin(theta),      cos(alpha)*cos(theta), -1.0*sin(alpha)*cos(theta),  
  a*sin(theta)]  
[      0,      sin(alpha),      cos(alpha),  
  d]  
[      0,      0,      0,  
  1.0]
```

Fast Inverse

ans =

```
[      cos(theta),      sin(theta),      0,  
  - a*sin(theta)^2 - a*cos(theta)^2]  
[ -1.0*cos(alpha)*sin(theta),      cos(alpha)*cos(theta), sin(alpha),  
  -d*sin(alpha)]  
[      sin(alpha)*sin(theta), -1.0*sin(alpha)*cos(theta), cos(alpha),  
  -d*cos(alpha)]  
[      0,      0,      0,  
  1]
```



Kin_Model

```
close all; clc;

q=sym('q',[3,1],'real');

disp('Create From DH Parameters');
kin=Kin_Model.fromDH([q(1),1,0,-pi/2;
                    q(2),0,1,0;
                    q(3),0,1,0],q);

disp('Joint Transformations')
kin.T(0,2).H
kin.T(3,1).H

disp('Forward/Inverse Kinematics')

test1=kin.forward_kin([0;0;0]);
test2=kin.forward_kin([pi/4;pi/3;3*pi/4]);
test3=kin.forward_kin([1;1;1]);

kin.inverse_kin(test1)
kin.inverse_kin(test2)
kin.inverse_kin(test3)

test4=[NaN,NaN,NaN,1;
       NaN,NaN,NaN,1;
       NaN,NaN,NaN,1;
       NaN,NaN,NaN,NaN];

result4 = kin.inverse_kin(test4)
kin.forward_kin(result4)

disp('Jacobian')
kin.J
kin.J([0;0;0])

disp('Inverse Jacobian')
kin.inv_J

Create From DH Parameters
Joint Transformations

ans =

[ cos(q1)*cos(q2), -1.0*cos(q1)*sin(q2), -1.0*sin(q1),
  cos(q1)*cos(q2)]
[ cos(q2)*sin(q1), -1.0*sin(q1)*sin(q2),  1.0*cos(q1),
  cos(q2)*sin(q1)]
[ -1.0*sin(q2),      -1.0*cos(q2),          0, 1.0 -
  1.0*sin(q2)]
[          0,          0,          0,
  1.0]
```

```

ans =

[      cos(q2)*cos(q3) - 1.0*sin(q2)*sin(q3),      cos(q2)*sin(q3)
+ cos(q3)*sin(q2),      0,      - (cos(q2)*sin(q3) +
cos(q3)*sin(q2))*(1.0*sin(q2) + cos(q2)*sin(q3) + cos(q3)*sin(q2))
- (cos(q2)*cos(q3) - 1.0*sin(q2)*sin(q3))*(1.0*cos(q2) +
cos(q2)*cos(q3) - 1.0*sin(q2)*sin(q3))]
[ - 1.0*cos(q2)*sin(q3) - 1.0*cos(q3)*sin(q2), cos(q2)*cos(q3)
- 1.0*sin(q2)*sin(q3),      0, (1.0*cos(q2)*sin(q3) +
1.0*cos(q3)*sin(q2))*(1.0*cos(q2) + cos(q2)*cos(q3)
- 1.0*sin(q2)*sin(q3)) - (cos(q2)*cos(q3) -
1.0*sin(q2)*sin(q3))*(1.0*sin(q2) + cos(q2)*sin(q3) +
cos(q3)*sin(q2))]
[
                                0,
                                0, 1.0,
                                0]
[
                                0,      0,
                                0,
                                1]

```

Forward/Inverse Kinematics

```

ans =

0
0
0

```

```

ans =

0.7854
1.0472
-3.9270

```

```

ans =

1.0000
1.0000
1.0000

```

```

result4 =

0.7854
0.7854
-1.5708

```

ans =

0.5000	0.5000	-0.7071	1.0000
0.5000	0.5000	0.7071	1.0000
0.7071	-0.7071	0	1.0000
0	0	0	1.0000

Jacobian

ans =

```
[ -sin(q1)*(cos(q2 + q3) + cos(q2)), -cos(q1)*(sin(q2 + q3) +  
sin(q2)), -sin(q2 + q3)*cos(q1)]  
[ cos(q1)*(cos(q2 + q3) + cos(q2)), -sin(q1)*(sin(q2 + q3) +  
sin(q2)), -sin(q2 + q3)*sin(q1)]  
[ cos(q2), -cos(q2 + q3)] 0, -cos(q2 + q3) -  
[ sin(q1), -sin(q1)] 0, -  
[ cos(q1), cos(q1)] 0,  
[ 0, 0] 1,
```

ans =

0	0	0
2	0	0
0	-2	-1
0	0	0
0	1	1
1	0	0

Inverse Jacobian

ans =

```
[  
  
-(cos(q2)*sin(q1) + cos(q2 + q3)*sin(q1))/(cos(q2  
+ q3)^2*cos(q1)^2 + cos(q2 + q3)^2*sin(q1)^2 + cos(q1)^2*cos(q2)^2  
+ cos(q2)^2*sin(q1)^2 + 2*cos(q2 + q3)*cos(q1)^2*cos(q2) + 2*cos(q2  
+ q3)*cos(q2)*sin(q1)^2 + 1),
```

$$\frac{(\cos(q_1)(\cos(q_2 + q_3) + \cos(q_2)))}{(\cos(q_2 + q_3)^2 \cos(q_1)^2 + \cos(q_2 + q_3)^2 \sin(q_1)^2 + \cos(q_1)^2 \cos(q_2)^2 + \cos(q_2)^2 \sin(q_1)^2 + 2 \cos(q_2 + q_3) \cos(q_1)^2 \cos(q_2) + 2 \cos(q_2 + q_3) \cos(q_2) \sin(q_1)^2 + 1)},$$

$$0,$$

$$0,$$

$$\frac{0, 1/(\cos(q_2 + q_3)^2 \cos(q_1)^2 + \cos(q_2 + q_3)^2 \sin(q_1)^2 + \cos(q_1)^2 \cos(q_2)^2 + \cos(q_2)^2 \sin(q_1)^2 + 2 \cos(q_2 + q_3) \cos(q_1)^2 \cos(q_2) + 2 \cos(q_2 + q_3) \cos(q_2) \sin(q_1)^2 + 1)]}{[$$

$$\begin{aligned} & -(\cos(q_1)^3 \sin(q_2) + \cos(q_2 + q_3)^2 \cos(q_1) \sin(q_2) + \cos(q_1) \sin(q_1)^2 \sin(q_2) - \cos(q_2 + q_3) \sin(q_2 + q_3) \cos(q_1) \cos(q_2)) / (\cos(q_1)^2 \cos(q_2)^2 + \cos(q_2)^2 \sin(q_1)^2 + \cos(q_1)^4 \sin(q_2)^2 + \sin(q_1)^4 \sin(q_2)^2 + 2 \cos(q_1)^2 \sin(q_1)^2 \sin(q_2)^2 + \cos(q_2 + q_3)^2 \cos(q_1)^2 \sin(q_2)^2 + \sin(q_2 + q_3)^2 \cos(q_1)^2 \cos(q_2)^2 + \cos(q_2 + q_3)^2 \sin(q_1)^2 \sin(q_2)^2 + \sin(q_2 + q_3)^2 \cos(q_2)^2 \sin(q_1)^2 - 2 \cos(q_2 + q_3) \sin(q_2 + q_3) \cos(q_1)^2 \cos(q_2) \sin(q_2) - 2 \cos(q_2 + q_3) \sin(q_2 + q_3) \cos(q_2) \sin(q_1)^2 \sin(q_2)), \\ & \end{aligned}$$

$$\begin{aligned} & \frac{-(\sin(q_1)^3 \sin(q_2) + \cos(q_2 + q_3)^2 \sin(q_1) \sin(q_2) + \cos(q_1)^2 \sin(q_1) \sin(q_2) - \cos(q_2 + q_3) \sin(q_2 + q_3) \cos(q_2) \sin(q_1))}{(\cos(q_1)^2 \cos(q_2)^2 + \cos(q_2)^2 \sin(q_1)^2 + \cos(q_1)^4 \sin(q_2)^2 + \sin(q_1)^4 \sin(q_2)^2 + 2 \cos(q_1)^2 \sin(q_1)^2 \sin(q_2)^2 + \cos(q_2 + q_3)^2 \cos(q_1)^2 \sin(q_2)^2 + \sin(q_2 + q_3)^2 \cos(q_1)^2 \cos(q_2)^2 + \cos(q_2 + q_3)^2 \sin(q_1)^2 \sin(q_2)^2 + \sin(q_2 + q_3)^2 \cos(q_2)^2 \sin(q_1)^2 - 2 \cos(q_2 + q_3) \sin(q_2 + q_3) \cos(q_1)^2 \cos(q_2) \sin(q_2) - 2 \cos(q_2 + q_3) \sin(q_2 + q_3) \cos(q_2) \sin(q_1)^2 \sin(q_2)), \\ & \end{aligned}$$

$$\begin{aligned} & q_3) * \cos(q_1)^2 * \sin(q_2) - \cos(q_2 + q_3) * \sin(q_2 + q_3) * \sin(q_1)^2 * \sin(q_2)) / \\ & (\cos(q_1)^2 * \cos(q_2)^2 + \cos(q_2)^2 * \sin(q_1)^2 + \cos(q_1)^4 * \sin(q_2)^2 \\ & + \sin(q_1)^4 * \sin(q_2)^2 + 2 * \cos(q_1)^2 * \sin(q_1)^2 * \sin(q_2)^2 \\ & + \cos(q_2 + q_3)^2 * \cos(q_1)^2 * \sin(q_2)^2 + \sin(q_2 + \\ & q_3)^2 * \cos(q_1)^2 * \cos(q_2)^2 + \cos(q_2 + q_3)^2 * \sin(q_1)^2 * \sin(q_2)^2 \\ & + \sin(q_2 + q_3)^2 * \cos(q_2)^2 * \sin(q_1)^2 - 2 * \cos(q_2 + q_3) * \sin(q_2 \\ & + q_3) * \cos(q_1)^2 * \cos(q_2) * \sin(q_2) - 2 * \cos(q_2 + q_3) * \sin(q_2 + \\ & q_3) * \cos(q_2) * \sin(q_1)^2 * \sin(q_2)), -(\cos(q_1)^2 * \sin(q_1) * \sin(q_2)^2 \\ & + \sin(q_2 + q_3) * \cos(q_1)^2 * \sin(q_1) * \sin(q_2) + \cos(q_2)^2 * \sin(q_1) \\ & + \cos(q_2 + q_3) * \cos(q_2) * \sin(q_1) + \sin(q_1)^3 * \sin(q_2)^2 + \\ & \sin(q_2 + q_3) * \sin(q_1)^3 * \sin(q_2)) / (\cos(q_1)^2 * \cos(q_2)^2 + \\ & \cos(q_2)^2 * \sin(q_1)^2 + \cos(q_1)^4 * \sin(q_2)^2 + \sin(q_1)^4 * \sin(q_2)^2 + \\ & 2 * \cos(q_1)^2 * \sin(q_1)^2 * \sin(q_2)^2 + \cos(q_2 + q_3)^2 * \cos(q_1)^2 * \sin(q_2)^2 \\ & + \sin(q_2 + q_3)^2 * \cos(q_1)^2 * \cos(q_2)^2 + \cos(q_2 + \\ & q_3)^2 * \sin(q_1)^2 * \sin(q_2)^2 + \sin(q_2 + q_3)^2 * \cos(q_2)^2 * \sin(q_1)^2 - \\ & 2 * \cos(q_2 + q_3) * \sin(q_2 + q_3) * \cos(q_1)^2 * \cos(q_2) * \sin(q_2) - 2 * \cos(q_2 + \\ & q_3) * \sin(q_2 + q_3) * \cos(q_2) * \sin(q_1)^2 * \sin(q_2)), (\cos(q_1)^3 * \sin(q_2)^2 \\ & + \sin(q_2 + q_3) * \cos(q_1)^3 * \sin(q_2) + \cos(q_1) * \cos(q_2)^2 + \cos(q_2 \\ & + q_3) * \cos(q_1) * \cos(q_2) + \cos(q_1) * \sin(q_1)^2 * \sin(q_2)^2 + \sin(q_2 \\ & + q_3) * \cos(q_1) * \sin(q_1)^2 * \sin(q_2)) / (\cos(q_1)^2 * \cos(q_2)^2 + \\ & \cos(q_2)^2 * \sin(q_1)^2 + \cos(q_1)^4 * \sin(q_2)^2 + \sin(q_1)^4 * \sin(q_2)^2 + \\ & 2 * \cos(q_1)^2 * \sin(q_1)^2 * \sin(q_2)^2 + \cos(q_2 + q_3)^2 * \cos(q_1)^2 * \sin(q_2)^2 \\ & + \sin(q_2 + q_3)^2 * \cos(q_1)^2 * \cos(q_2)^2 + \cos(q_2 + \\ & q_3)^2 * \sin(q_1)^2 * \sin(q_2)^2 + \sin(q_2 + q_3)^2 * \cos(q_2)^2 * \sin(q_1)^2 - \\ & 2 * \cos(q_2 + q_3) * \sin(q_2 + q_3) * \cos(q_1)^2 * \cos(q_2) * \sin(q_2) - 2 * \cos(q_2 + \\ & q_3) * \sin(q_2 + q_3) * \cos(q_2) * \sin(q_1)^2 * \sin(q_2)), \end{aligned}$$

0]

Planner

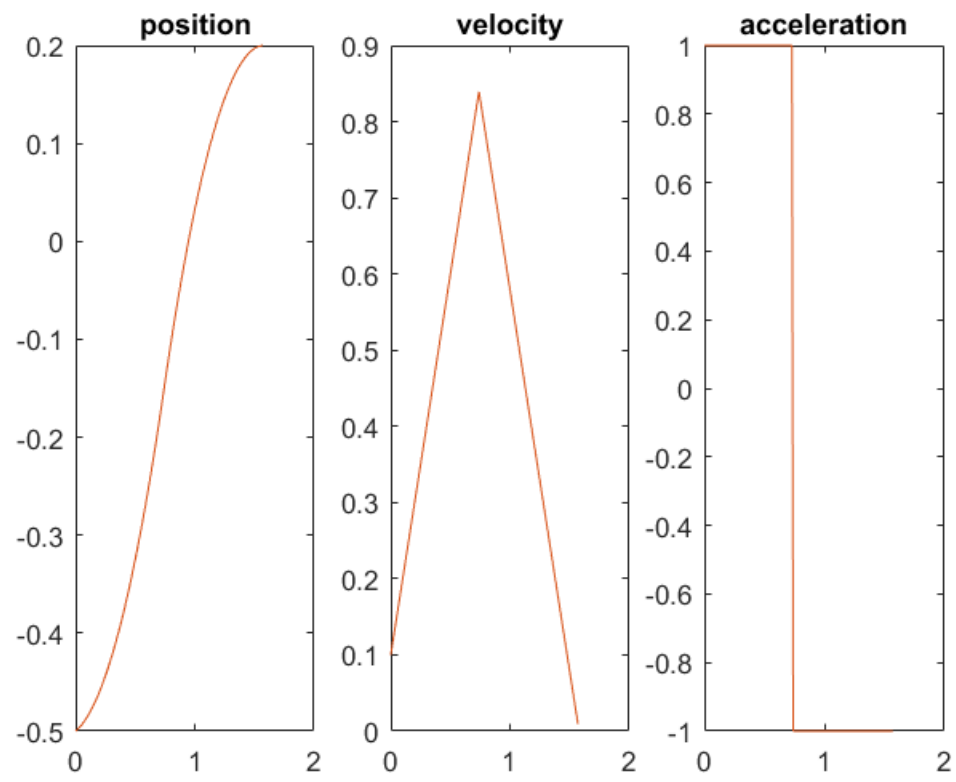
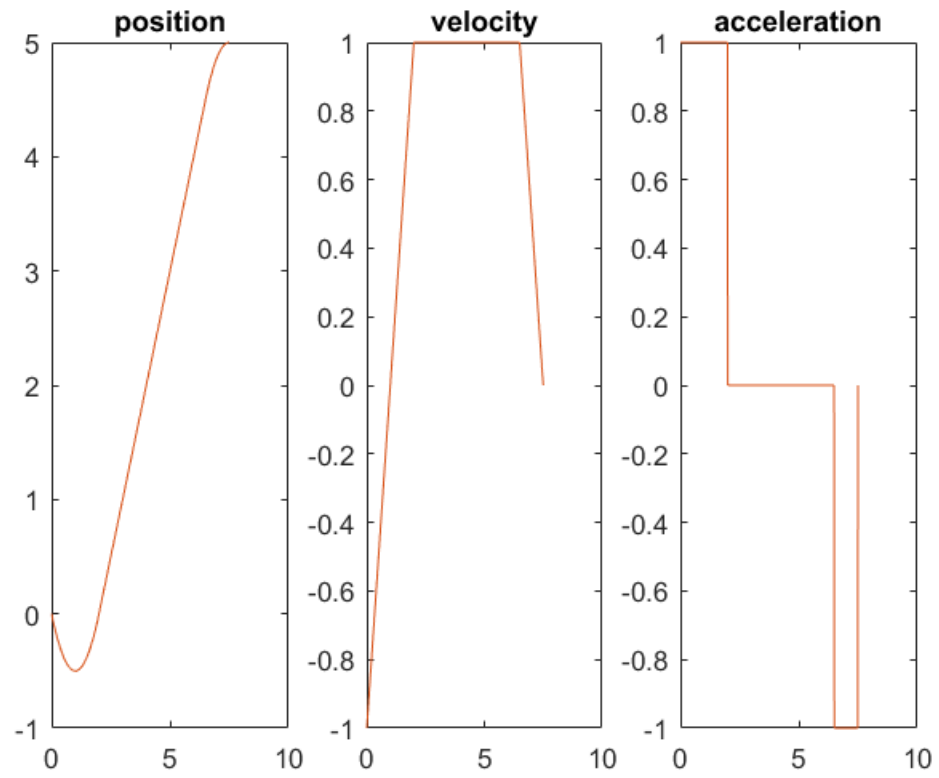
```
close all; clc;
t=sym('t','real');
t_range=0:0.02:10;

q_d = [t/8;0.2;sin(2*t)];

x0=[ 0      ,0;
     -0.5   ,0.1;
     0.2    ,0.1];

plan1=Planner.fromSym(q_d(1));
plan2=Planner.trapezoid(x0(2,:),[q_d(2),0],1,1);
plan3=Planner.fromSym(q_d(3));
plan=Planner.join({plan1,plan2,plan3});

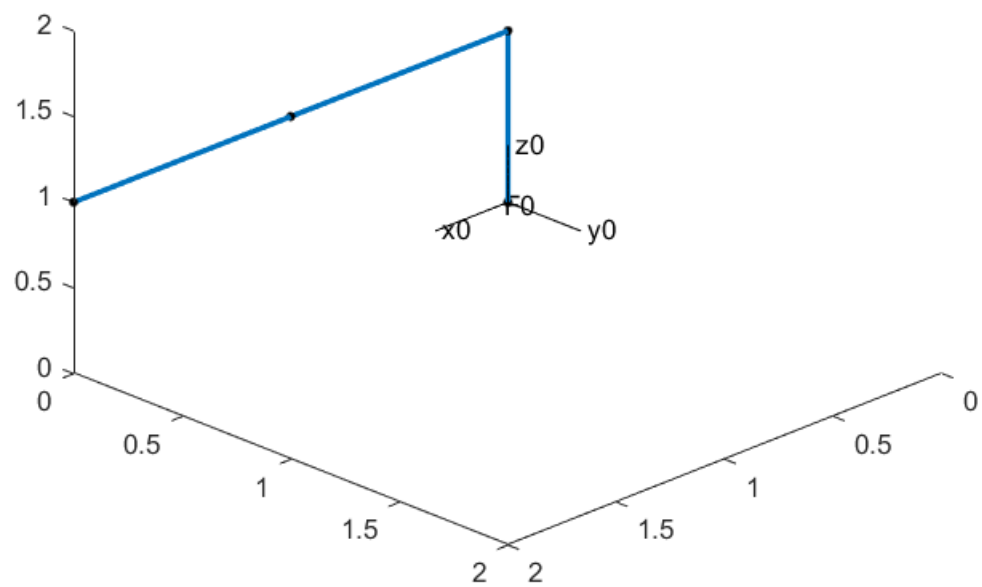
testTrapezoid([0,-1],[5,0],1,1);
testTrapezoid(x0(2,:),[q_d(2),0],1,1);
```

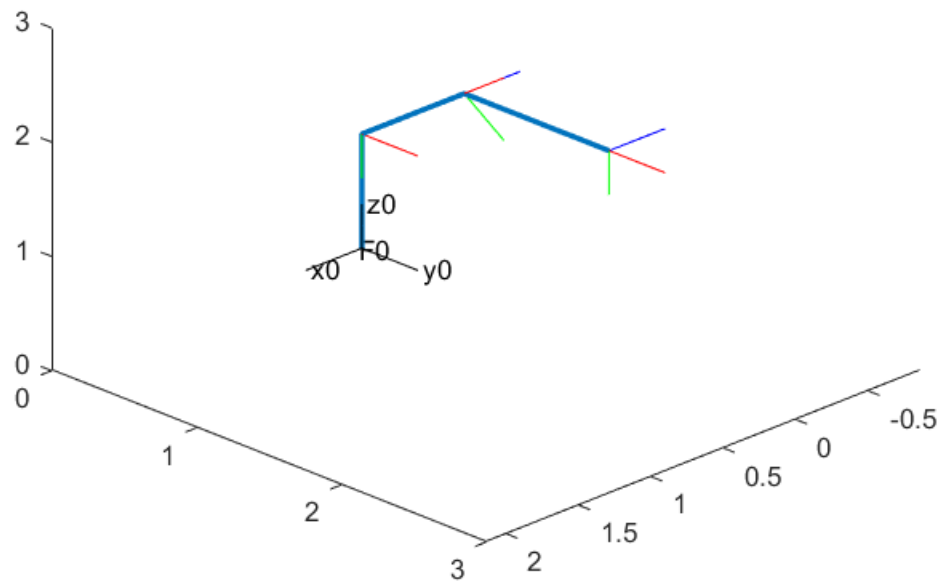


Draw/Plot

```
close all; clc;

kin.draw([0;0;0],0,[],{'linewidth',2},[1,1,1])
figure
kin.draw([pi/2;-pi/4;pi/4],1,[],{'linewidth',2},[1,1,1])
```





Dyn_Model

```
close all; clc;

model=Dyn_Model(kin);

model=model.add(H_Trans([-0.5,0,0]),5,10,1);
model=model.add(H_Trans([-0.5,0,0]),5,10,2);
model=model.add(H_Trans([-0.5,0,0]),5,10,3);

model.b=[1;1;1];

model.g_dir=[0;0;-1];

disp('Calculating Dynamics');
model = model.calculateDynamics();

M=model.M
G=model.G

Calculating Dynamics

M =
```

```

[ (5*cos(2*q2 + q3))/2 + (25*cos(2*q2))/8 + (5*cos(2*q2 + 2*q3))/8 +
  (5*cos(q3))/2 + 5,
  0,
  0]
[
  0, 5*cos(2*q1 + 2*q2 + 2*q3) + 5*cos(2*q1 + 2*q2) +
  5*cos(q3) + 35/2, 5*cos(2*q1 + 2*q2 + 2*q3) + (5*cos(q3))/2 + 25/4]
[
  0,
  (5*cos(q3))/2 + 25/4,
  5*cos(2*q1 + 2*q2 + 2*q3) +
  5*cos(2*q1 + 2*q2 + 2*q3) +
  25/4]

G =

0
- (981*cos(q2 + q3))/40 - (2943*cos(q2))/40
  -(981*cos(q2 + q3))/40

```

Simulate

```

close all; clc;

Kp=[10;10;10];
Kv=[10;10;10];

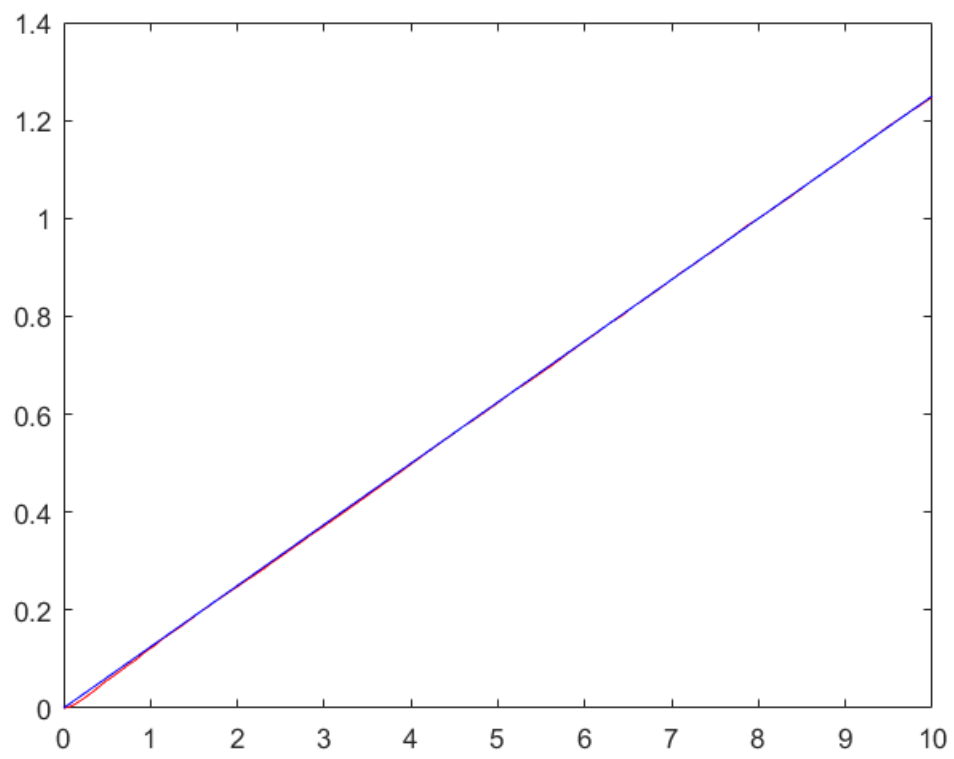
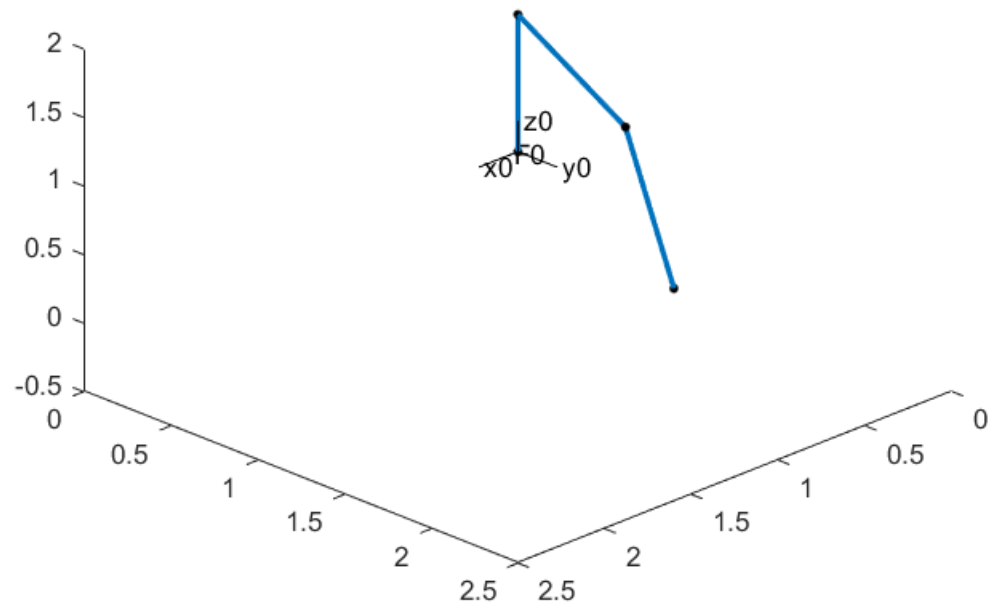
control=Controller.ComputedTorque(@model.inverse_dyn,Kp,Kv);
noise=@(a,t)0.02*randn(size(a));

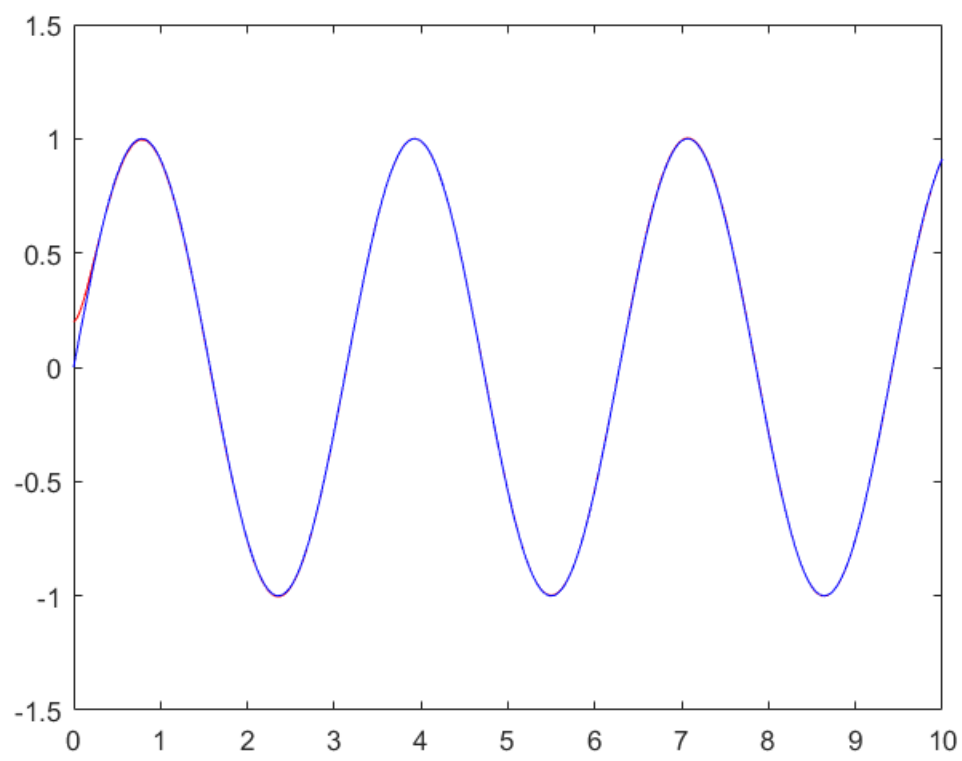
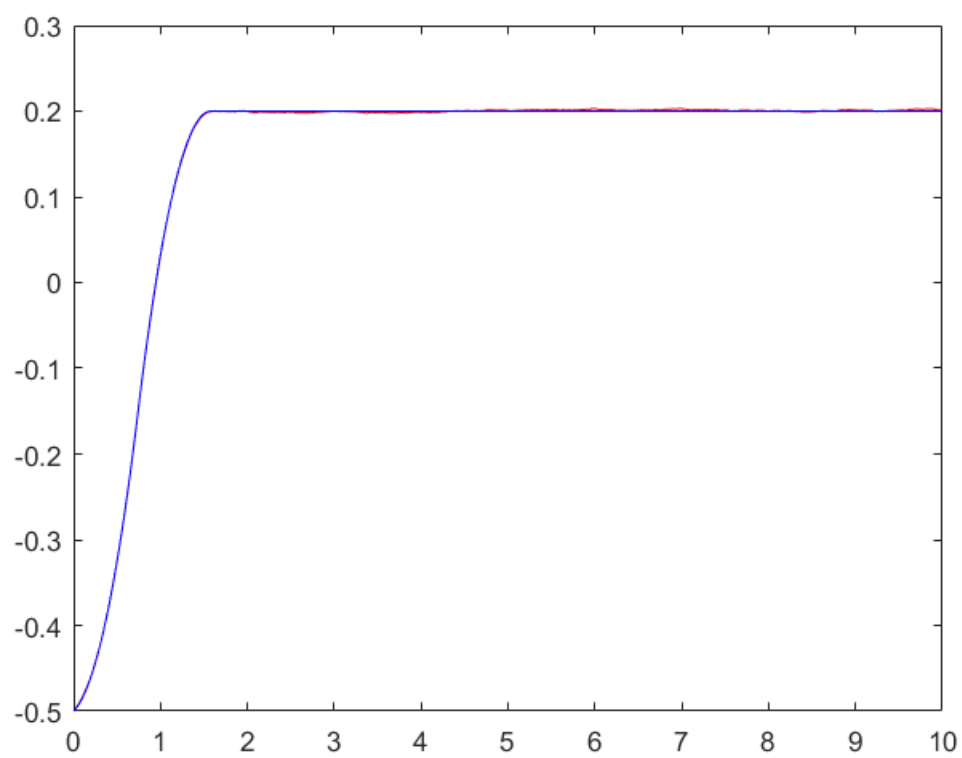
options =
  odeset('RelTol',1e-4,'AbsTol',1e-4.*ones(numel(model.q)*2,1));

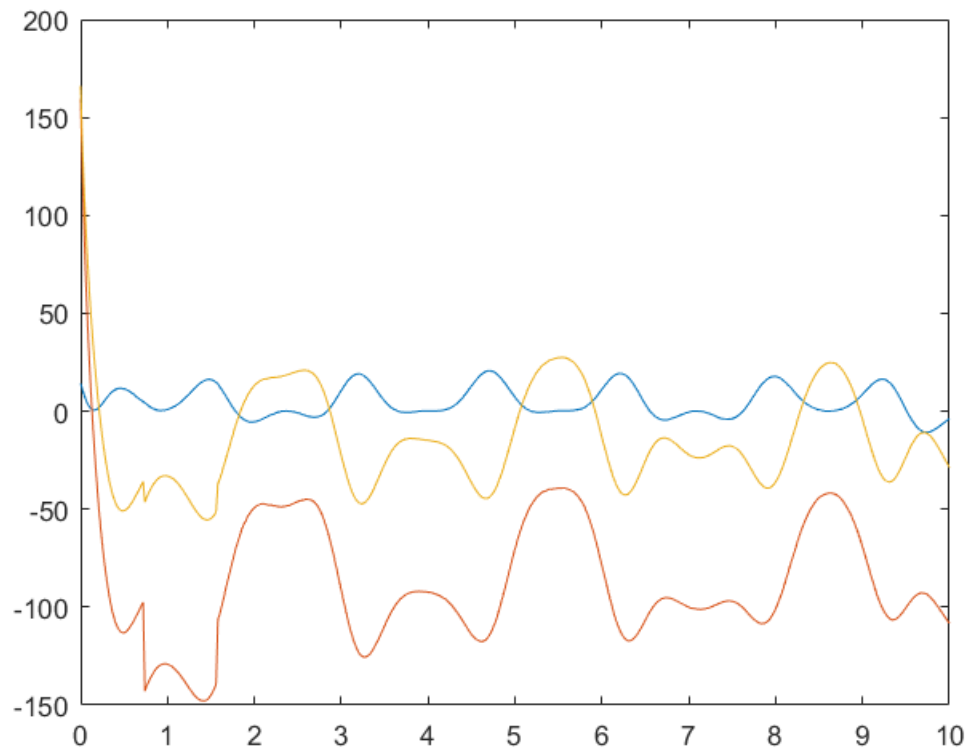
model.simulate({plan,control,noise},t_range,x0,options,{0.01,false,{0,
[],{'linewidth',2},[1,1,1]}});

Beginning Simulation
Simulation Complete

```







Workspace Planning

```
close all; clc;

t=sym('t','real');
t_range=0:0.02:10;

q=sym('q',[6,1],'real');

disp('Calculating Kinematics');
kin=Kin_Model.fromDH([q(1),1,0,pi/2;
                    q(2),-0.1,0,0;
                    0,0,1,0;
                    q(3),0.1,0,0;
                    0,0,1,pi/2;
                    q(4),0.1,0,-pi/2;
                    q(5),0.1,0,-pi/2;
                    q(6),0.1,0,pi/2],q);

disp('Creating Path');
r=.25;
p0=[.75;.75;.75];
z_t=r-2*r/t_range(numel(t_range))*t+p0(3);
r_t=sqrt(r^2-(z_t-p0(3))^2);
p_d=[p0(1)+r_t*cos(10*t);p0(2)+r_t*sin(10*t);z_t];
```

```

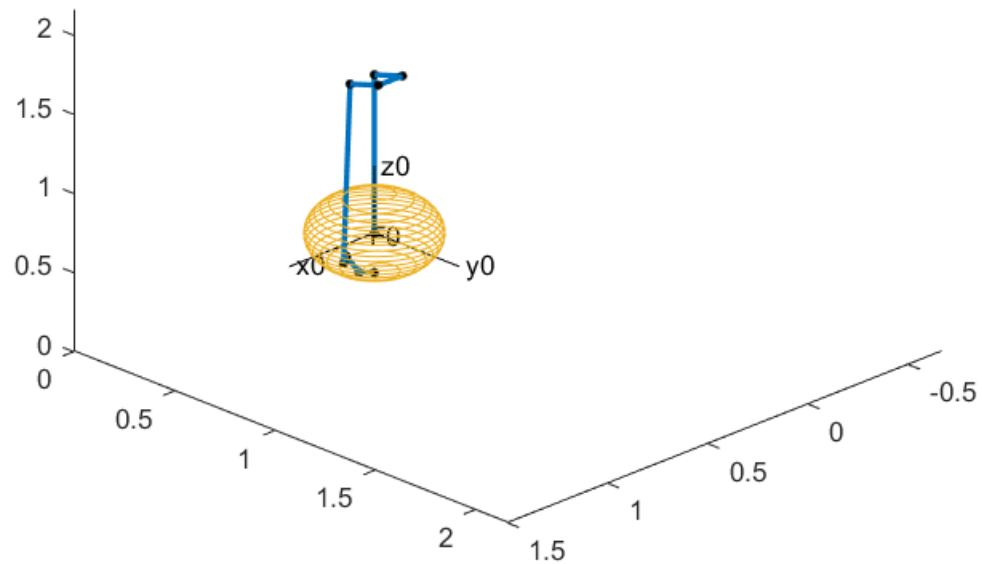
x_d=[NaN,NaN,NaN,p_d(1);
      NaN,NaN,NaN,p_d(2);
      NaN,NaN,NaN,p_d(3);
      NaN,NaN,NaN,NaN];

plan=Planner.fromSym(x_d);
disp('Converting to Joint Space');
plan=Planner.toJointSpace_func(plan,t_range,[],@kin.inverse_kin);

D=evalf(plan,t_range. ');
kin.simulate(D(:, :, 1). ', 0.01, true, {0, [], {'linewidth', 2}, [1, 1, 1]});

Calculating Kinematics
Creating Path
Converting to Joint Space

```



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