

## CptS 453 — Homework-02

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### Problem 1:

The bounds for a *biparte* graph is as follows:

- The lower bound is when the graph is extremely skewed to one side, where  $n_i = 1$  for either side of the biparte graph and  $n_j = 200 - n_i$  is the remaining side. Thus, the lower bound is  $m = 200$ .
- The upper bound is when the graph is perfectly symmetrically, where  $n_i = n_j$ . In this case,

$$n_i = n_j = 100$$

Thus,

$$m = n_i = n_j = n_i \cdot n_j = 100 * 100 = 10,000$$

### Problem 2:

Similarly, for  $p$  and  $q$  as integers, where  $p < q$ . The lower bound of  $K_{p,q}$  is the product  $p \cdot q$ , where  $p = 1$ . The upper bound is  $((p + q)/2)^2$ .

### Problem 3:

The set of value  $k$  for which  $G_k$  is controlled by the following conditions:

- $k$  where  $k$  is prime
- $k$  where  $\|j - i\| = k \% 10$
- $k$  where  $10 \% k \neq 0$

Since I'm not used to set theory, I am just listing the related subsets. There should be a relation among these subsets.