

RICE UNIVERSITY

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by

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ABSTRACT

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In this thesis, we will unify the theory of multiple imputation, survival analysis, and propensity score analysis. While each of these fields have been studied on their own intensely, there has been little work on using the three in trio. Starting out with an incomplete dataset, we aim to impute reasonable imputations, run survival analysis on each of the imputed datasets to get survival estimates, and then do propensity score analysis to observe causal effects. I apply the methodology to cancer survival in a case study, but the methods used are general, and could be used for any type of data.

Contents

Abstract	ii
List of Illustrations	iv
List of Tables	v
1 Introduction	1
1.1 Motivation	1
1.2 Imputation	1
1.3 Survival	3
1.4 Propensity Score Analysis	4
2 Methods	5
2.1 Multiple Imputation	5
2.2 Survival analysis	8
A Appendix	9

Illustrations

Tables

Chapter 1

Introduction

1.1 Motivation

I want to develop methodology that can be used both by applied researchers and clinicians. I want it to be easy enough to describe to someone with a limited statistical background, but meaningful and valid so that the results obtained can be used in publication. The desire to have it this way stems from working on a project with both statisticians and clinicians.

Missing data is a major problem in both applied and theoretical statistics, however, it has not received attention proportional to its need. Survival analysis is a well studied field, but is relatively complete, so not much new research comes out of this field. Propensity score analysis will help us determine causal relationships when we don't have a completely randomized experiment. As one could imagine, all three of these fields are important to the applied statistician, as they will come across at least one at some point in their career. I will explain each of these three disciplines in detail before we dive into combining them.

1.2 Imputation

Imputation (specifically multiple imputation) is a way to fill in missing data, and it forms the base of our plan, all of the other analyses follow from it. Thus, we need a good understanding of it before we may proceed. Multiple imputation itself though is

a recent development, so we need to understand why it is used. At first, statisticians paid no attention to missing data, and happily discarded records for their analysis that were incomplete. This was known as complete case analysis. There are many problems with this paradigm. To begin with, you will lose a lot of statistical power when doing this, because you are literally throwing away records and thus decreasing your sample size. In addition, this can be costly to the researcher. If it costs a set amount to collect a single record, and you don't use this record, you are literally wasting money. As well, in some rare cases, incomplete data might be the only type we can get. Lastly, and most importantly, we will be biasing our estimates if we discard them. For example, if we have a random sample of people and are testing a drug, and want to run a regression on some collected covariates. Men are known to not want to give all of their information, so they leave them blank. In the analysis, we will need to discard the male samples because they are incomplete, leaving us only with women. Thus, we don't have a random sample anymore, and will get biased results. The next wave of statisticians wanted to improve upon this, so they developed what we now call today (single) imputation. In single method (such as regression, trees) is used one time to impute the missing value. While this is a little better than complete case analysis, it still has many drawbacks. Asserting that a single value is the true value is just foolish. There is always some amount of error involved, and we can in no way be 100% confident that our imputed value is correct. Furthermore, if I impute one value and you impute another, we may get totally different results from analysis on the data. This is obviously not desirable. In addition, imputing one time and calling it your data will artificially increase your sample size. You are in effect treating the imputed values as if they were real. If this was valid, we wouldn't ever need to collect samples, and we could just be armchair statisticians. While single

imputation certainly has its drawbacks, the idea of actually trying to fill in the data is an important one, and multiple imputation fills in the theoretical gaps. In 1987, Donald Rubin proposed multiple imputation as a solution [SAUCE]. The central idea is to make many datasets for the missing data, drawing the estimates for the missing data from the parameters posterior distribution. Once we have a sufficient number of datasets, we can run whatever analyses we would like on them, and then pool the results. We can get the standard errors by noting the within and between imputation variance. This is obviously much better than the first two methods because it allows is to not throw away data, as well as allowing us to quantify our uncertainty about imputing the missing values. The only real drawback of multiple imputation is that we still dont have true data, but we can be confident enough in our estimations to compensate for that. Multiple imputation use has been steadily increasing over the past 30 years, and it is now the standard for missing data.

1.3 Survival

Survival analysis is a huge field, and there have been many textbooks written about it. I only plan to introduce the topics that are relevant to my case study. For a much more detailed introduction, please see X Y Z Survival analysis on the whole is analysis of time to event data, often in the presence of censoring. The two main tools that we will be using are Kaplan-Meier estimate and Cox regression. The Kaplan-Meier estimate is a non-parametric estimate of the true survival function (the probability that you survive after a time t). Cox regression is a modelling tool that allows us to analyze the hazard ratio of a covariate. Using cox regression, we can make statements such as increasing the drug by one mg will increase its hazard by 30

1.4 Propensity Score Analysis

⚠️THIS NEEDS A LOT MORE WORK⚠️ In an ideal world, we would like to be able to do research and say that A causes B, not something along the lines of our study says that A is related to B. Using propensity score matching, we are able to get this interpretation, via Rubins causal model. Rubins causal model is a framework that allows us make causality statements, and propensity score is a tool that grants us access to the framework. The way propensity score analysis works is that we will match patients on their propensity to be in the treatment group. This is often done by logistic regression, although newer methods include regression trees and such.

Chapter 2

Methods

2.1 Multiple Imputation

I want the framework we use to be easy to use and understand, so that it can easily be discussed among clinicians and other non statistically minded people. On the same token, I want the methods and theory to be sound from a statistical point of view. For the three parts that we are combining, I try to pick the optimal theory and software packages to achieve this. Our first decision comes as to what paradigm we should impute under. It should be noted that as long as we can produce valid imputations, the choice of method does not matter. However, since the base of our analysis starts with imputation, we need to make sure that we pick a good method. Everything that follows in the analysis is dependent on our imputed data, so it is necessarily the case that bad imputation will lead to poor results (be it bias, high variability, loss in statistical power). There are two main divisions in multiple imputation, and they are joint modelling and full conditional specification. In joint modelling, we assume that the data can be described by a multivariate distribution (specified by the user), and draw imputations from a joint distribution of the unknowns for the rows, given what we do know and their associated hyperparameters. There has been extensive research on using the normal model for this, and research shows that it even performs well under non-normality. R packages for joint modelling imputation include Amelia (source), NORM, and cat (Schafer source) On the other hand, there is fully conditional speci-

fication. In this paradigm, missing data is imputed on a variable by variable case on the columns, based off of a specification of the imputation model for each imputed variable. These full conditionals should factor to specify the joint distribution. We are going to have to specify something, there is no escaping that, but I think that it is easier for the average person (especially a clinician) to be able to define a single distribution rather than to guess at a multivariate. In addition, in the survival analysis setting, we will naturally have time variables be only positive, whereas others can take any value. Trying to fit a parametric distribution with these stipulations will be very hard, so we will be relegated to using a general distribution (like the normal), which will certainly elicit a poor fit. So, the fully conditional specification will be our choice. Now that we have choose the paradigm, we need to select an implementation of it. Many exist (such as MICE, mi, etc.ect). I wanted to select the implementation that combined ease of use, understanding, and programming. What I decided upon was a method called MICE- Multiple imputation via chained equations. (SOURCE). MICE is a MCMC method that under compatibility, is a gibbs sampler, where we obtain samples from the joint by sampling from the full conditionals. Compatibility means that knowing the full conditionals allows you to know the joint. Specifically ¶¶See 4.5.4 in van buuren¶¶ The user defines the full conditionals, so it is possible that the joint may only exist implicitly, and not actually have a functional form. This is an obvious disadvantage of this method, but multiple studies have shown that MICE is robust to this flaw, even when using highly incompatible models¶¶sources for this¶¶. Mice has been shown in simulation studies to yield unbiased estimates with proper coverage. In order to use mice, we must have that the missingness in our data is missing at random (MAR). What this means is that the probability of a covariate being missing is related to another covariate that we have collected (for example,

obese teens may not want to volunteer their weight, but knowing their sex and age will alert us to this). The opposite of this is MNAR- missing not at random. This is when the probability of a covariate being missing is dependent on another covariate that we don't have, for example, if obese male teens don't want to volunteer their weight, but we don't collect age or gender. MICE will work under both MAR and MNAR, but performs much better under MAR. There are tests for testing ??, but they aren't very widely used) Once we have the correct assumptions, we need to set up our full conditionals. This may take a while for large datasets, but the extra time spent will ensure a better model. We choose what predictors will go into imputation, and what method to use (regression, predictive mean matching, logistic regression, etc.). For variables that are derived from others, we impute the others and then compute that variable, in a process known as passive imputation. Since mice is an iterative process, we must choose how many iterations we will do until convergence. The literature suggests only 5 is enough (source), but with modern computation, we can easily exceed this, even with large data. As well, we need to decide how many datasets to impute. Once again, 5 will do, but more is better, since it will cut down on simulation error (find where I wrote up the reasons why). We need to verify that our imputations are valid once we complete them. The overarching idea that we need to pay attention to is does the data look like it could have been real data. We can assess this in many ways, including density plots, box and whisker plots, etc. Once we have m imputed datasets, we may run any valid analysis (regression, computing any statistic) on each imputed dataset INDIVIDUALLY. We may then use Rubin's rules (source) [put the steps in later], to pool our estimates. This will give us a point estimate, as well as proper variance for the quantity we have in mind. Rubin's rules assumes normality, so if our statistic in mind is not asymptotically normal, we need

to transform it towards normality before we pool.

2.2 Survival analysis

Now that we have the multiple imputation datasets created, we may run our analysis. The analyses, as stated in the previous section are heavily based on Rubins pooling rules. We are interested in some basic survival quantities (Kaplan-Meier survival estimates for certain groups, cox regression to determine hazard ratio), as well as some more advanced ones (survival in the competing risks setting). Following rubins rules, we run the individual analyses on each of the m datasets, and then pool our results. This works fine for the cox model, as the regression coefficients are asymptotically normally distributed. In many of the MI packages, there are functions to model and pool with cox regression. Care needs to be taken to ensure that our analysis is valid (ie that we do in fact have proportional hazards). We can go about this in two ways. The first is to check the assumptions on each individual model fit to each dataset. This may prove to be an arduous task, but with graphical tools such as shiny, this isnt too bad. We may also stack our multiple imputations on top of eachother, and run one huge model (thus our MI data are acting as replicates). This will produce unbiased estimates, but the standard errors will be too low. So, this tool may be used as a graphical check, but the results from the inference of this cannot be trusted(source for all of the above). Once we have verified that the model follows the assumptions, we may trust its results, and perform inference on the parameters using the obtained total variance.

Appendix A

Appendix

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