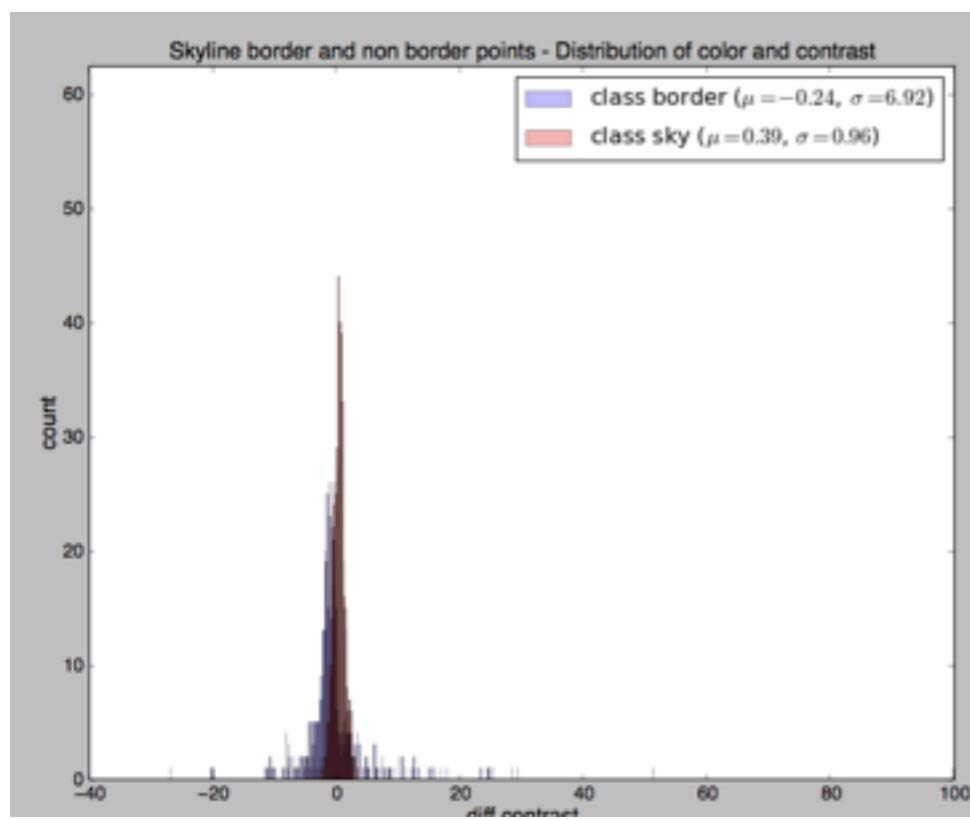


LDA look at difference in contrast, hue, blue or red, and CIE theta, all divided by their respective standard deviations.

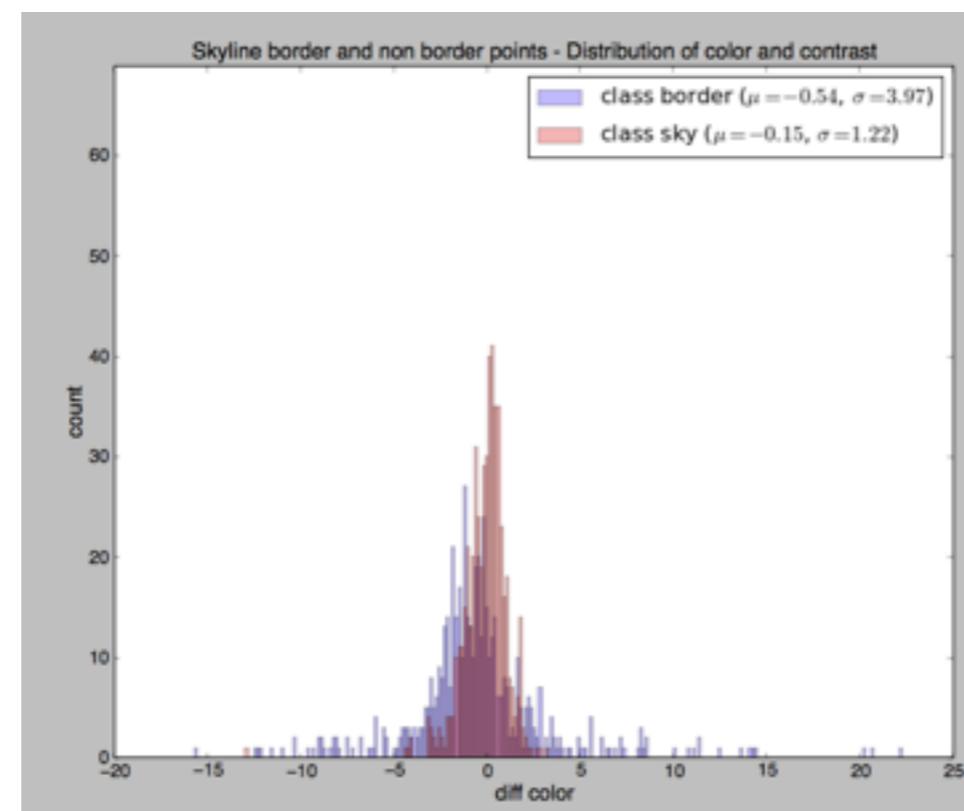
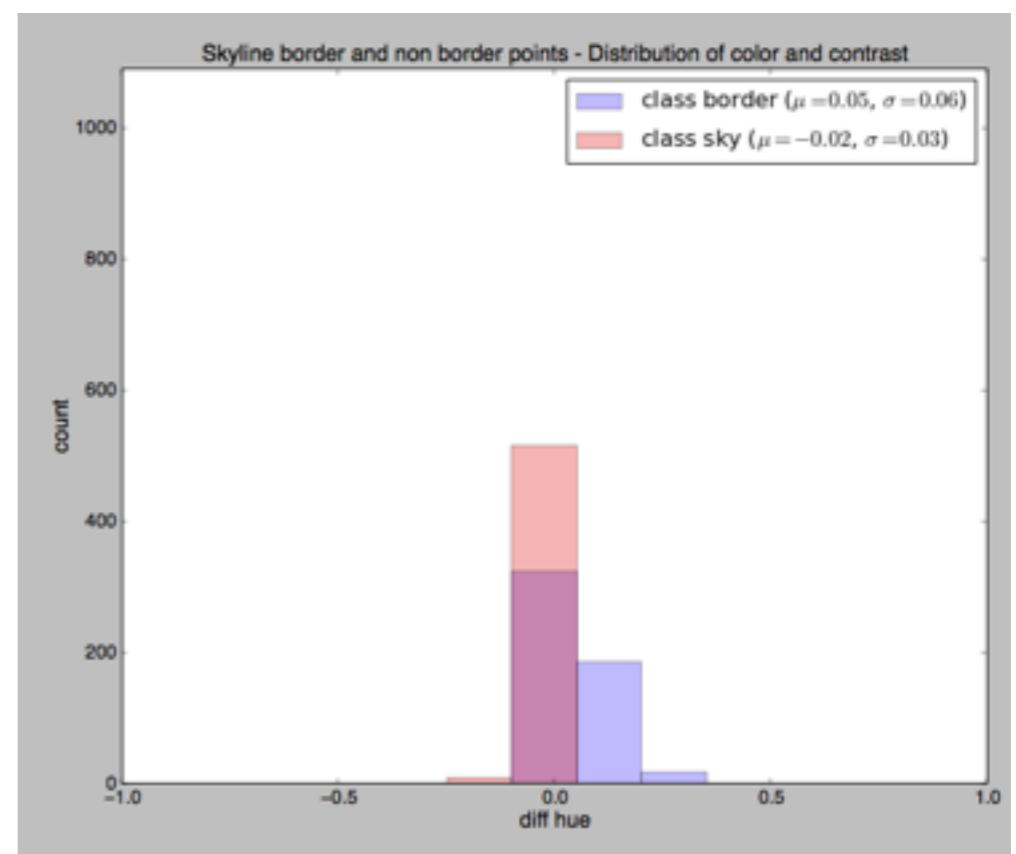
Brown & Lowe 2003, image 1



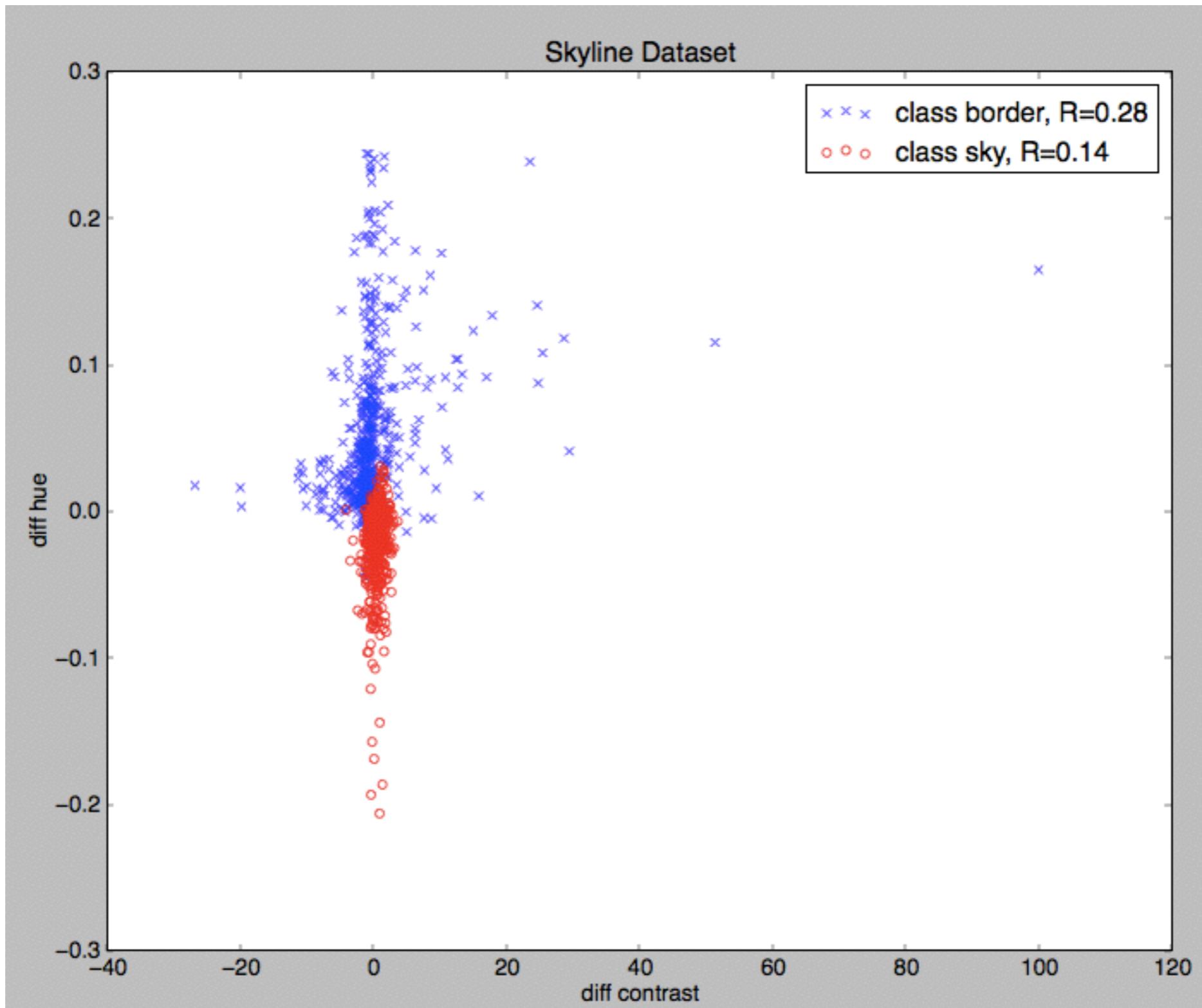
Brown & Lowe 2003, image 1



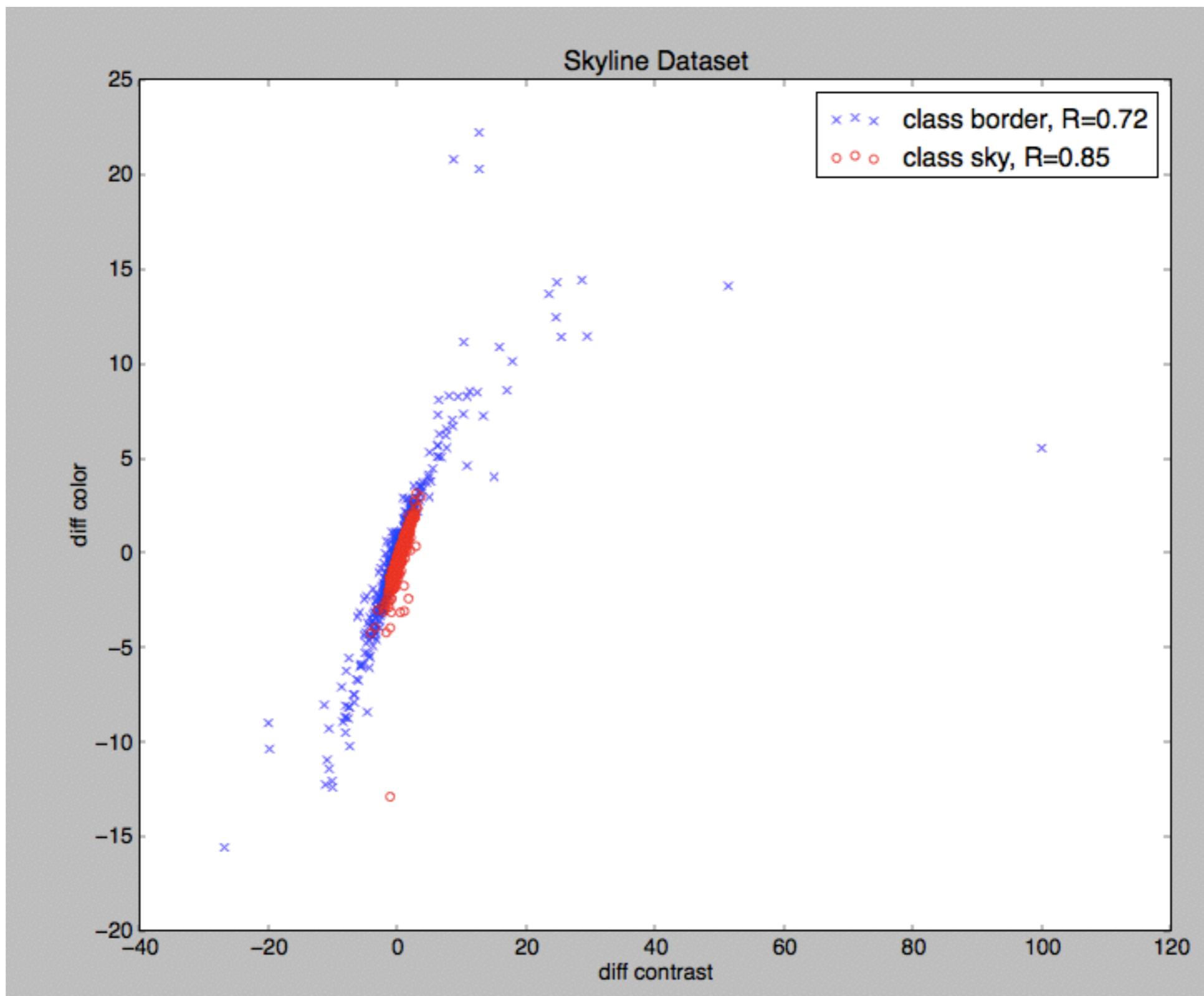
*note: the largest contrasts were removed from analysis for plot visibility



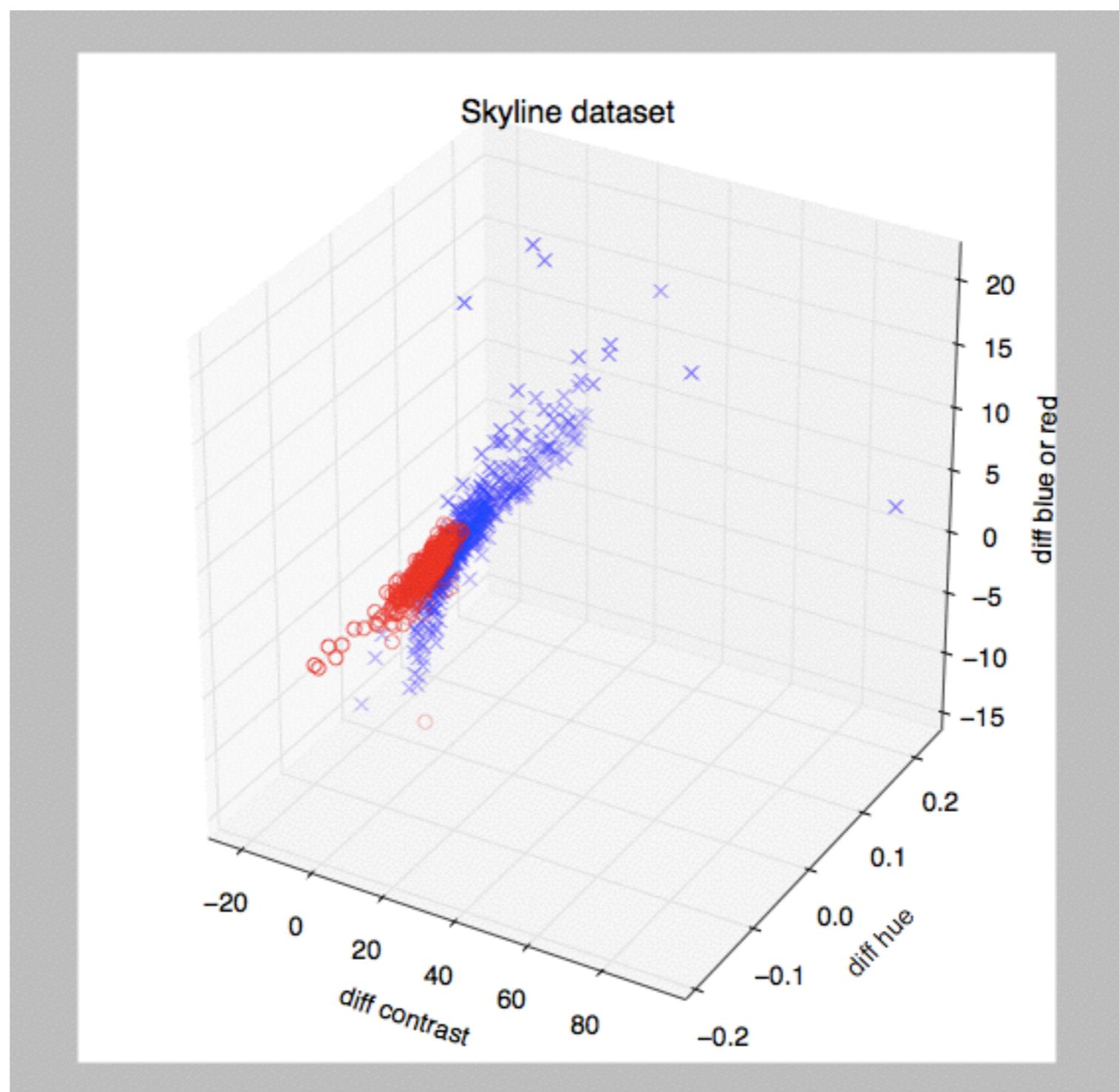
Brown & Lowe 2003, image 1



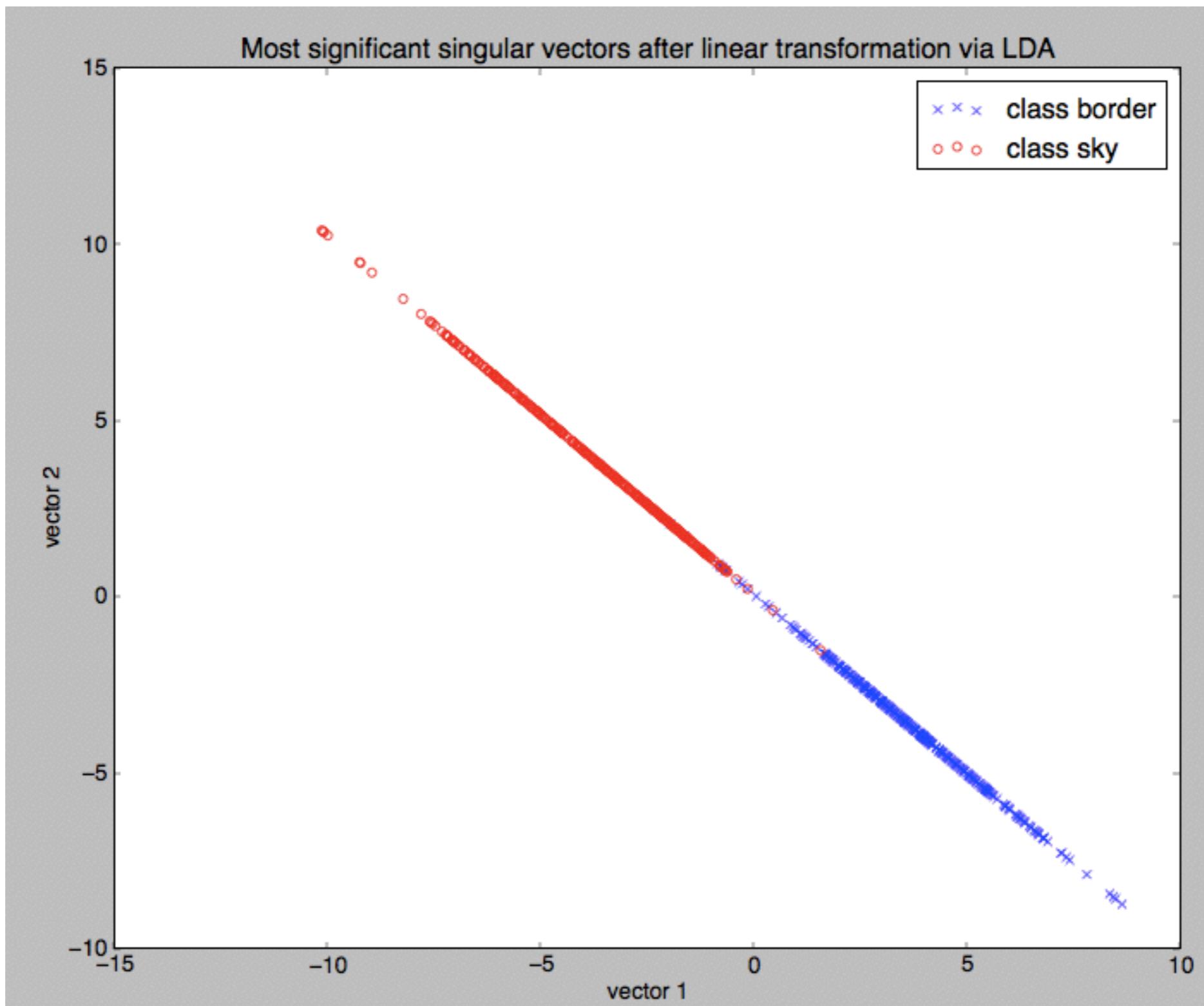
Brown & Lowe 2003, image 1



Brown & Lowe 2003, image 1

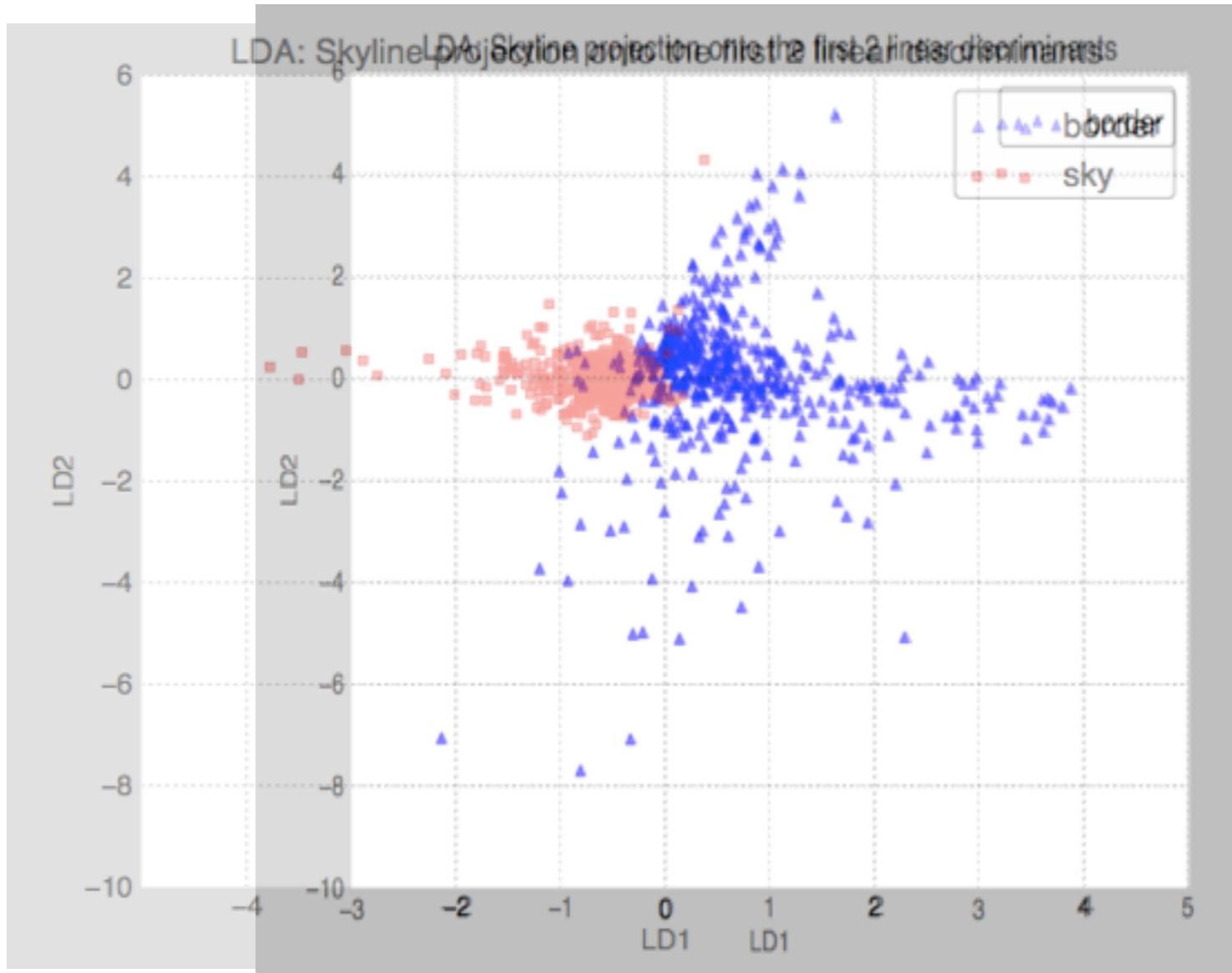


Brown & Lowe 2003, image 1



stats using 24 neighbors

Brown & Lowe 2003, image 1



http://sebastianraschka.com/Articles/2014_python_lda.html

"within-class scattering matrix": for each class i: $S_i = \sum_{x \in \text{data}} (x - m_i)(x - m_i)^T$
where $m_i = (1/n_i) \sum_{k \in \text{data}} x_k$

$\Rightarrow S_w = \sum_i S_i$

"between-class scattering matrix":

$\Rightarrow S_B = \sum_i N_i (m_i - m)(m_i - m)^T$
where m is the overall mean, and m_i and N_i are the sample mean and sizes

Solving for $A^T \nu = \lambda \nu$ where $A = S_w^{-1} \cdot S_B$, ν is eigenvector, and λ is eigenvalue
 \Rightarrow LD1 and LD2 are diff contrast and diff hue transformed by $y = W^T \cdot X$ ($= W \cdot T \cdot \text{dot}(X \cdot T)$)

contrast	hue	BorR
Mean Vector class 1: [-0.0646 0.6527 -0.0675]		
Mean Vector class 2: [0.0646 -0.6527 0.0675]		
'within-class Scatter Matrix:\n', array([[1043.6244, 204.0609, 748.2823], [204.0609, 601.5069, 250.4388], [748.2823, 250.4388, 1043.225]]))		
'between-class Scatter Matrix:\n', array([[13.1269, -132.6017, 13.7128], [-132.6017, 1339.4792, -138.5203], [13.7128, -138.5203, 14.3249]]))		
Eigenvector 1:		
[[-0.0718]	[0.9701]	
[-0.232]]		
Eigenvalue 1: 2.63e+00		
Eigenvector 2:		
[[0.0031]		
[-0.1026]		
[-0.9947]]		
Eigenvalue 2: -5.72e-18		
Eigenvector 3:		
[[0.4721]		
[0.1368]		
[0.8709]]		
Eigenvalue 3: 0.00e+00		
ok		
Eigenvalues in decreasing order:		

2.6256396264

5.716642657e-18

0.0

Variance explained:

eigenvalue 1: 100.00%

eigenvalue 2: 0.00%

eigenvalue 3: 0.00%

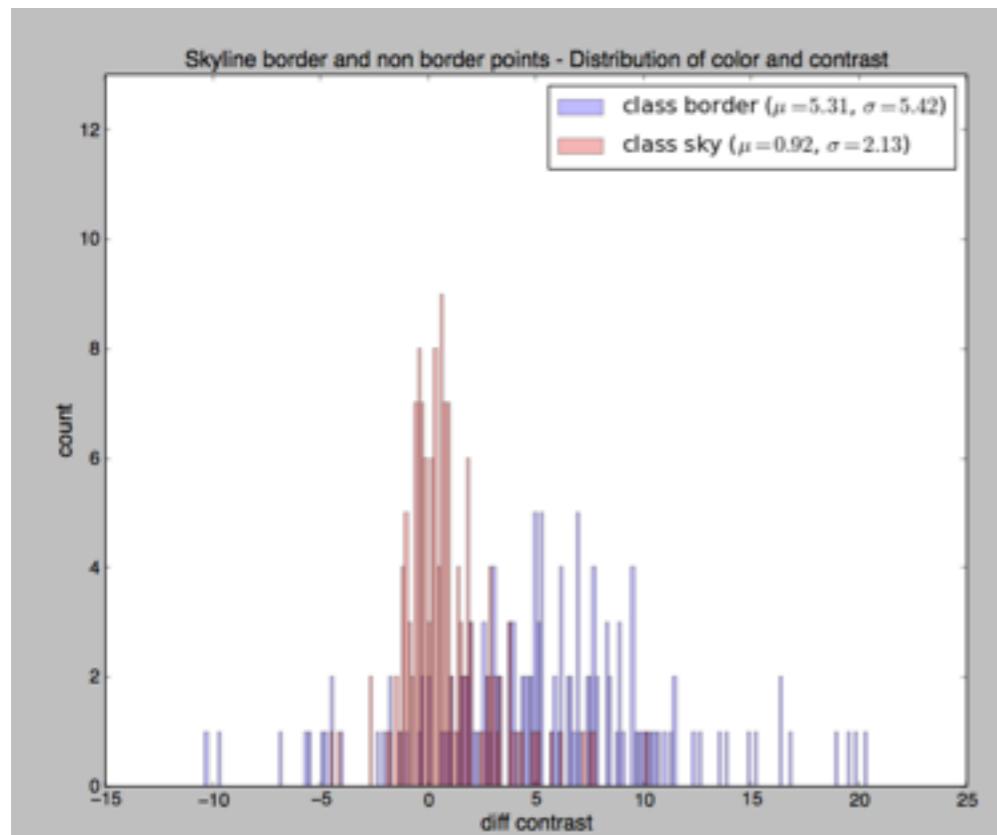
'Matrix W:\n', array([[-0.0718, 0.9701, -0.232], [0.0031, -0.1026, -0.9947]]))

LDA look at difference in contrast, hue, blue or red, and CIE theta, all divided by their respective standard deviations.

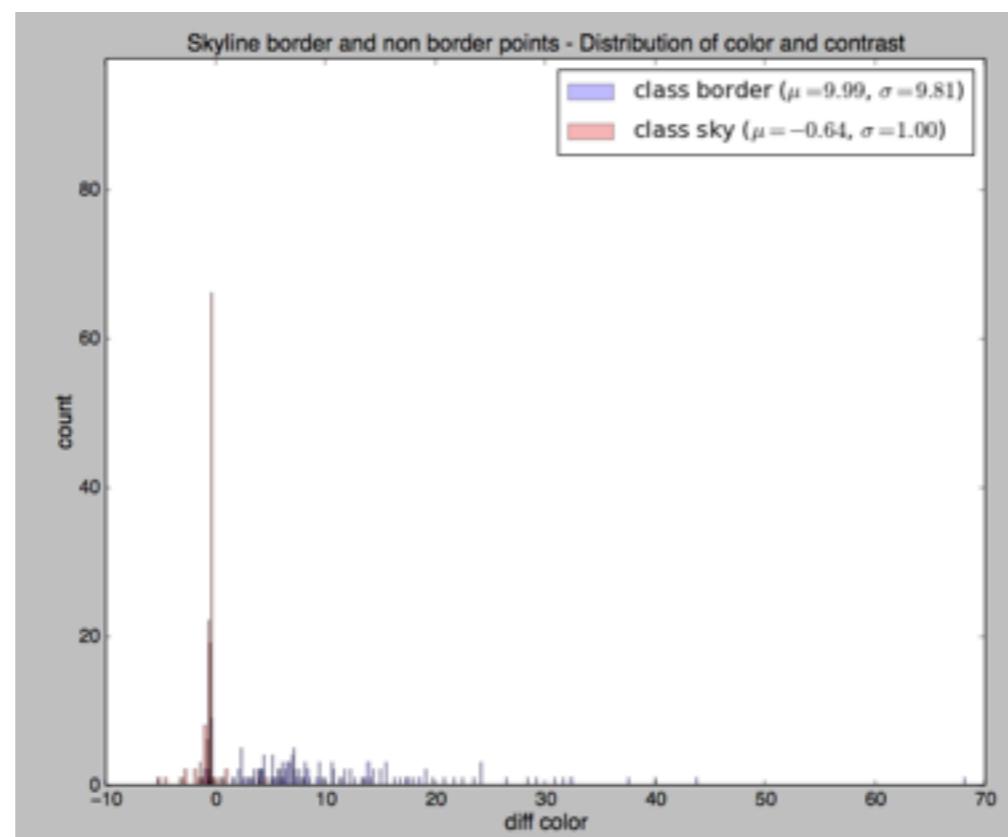
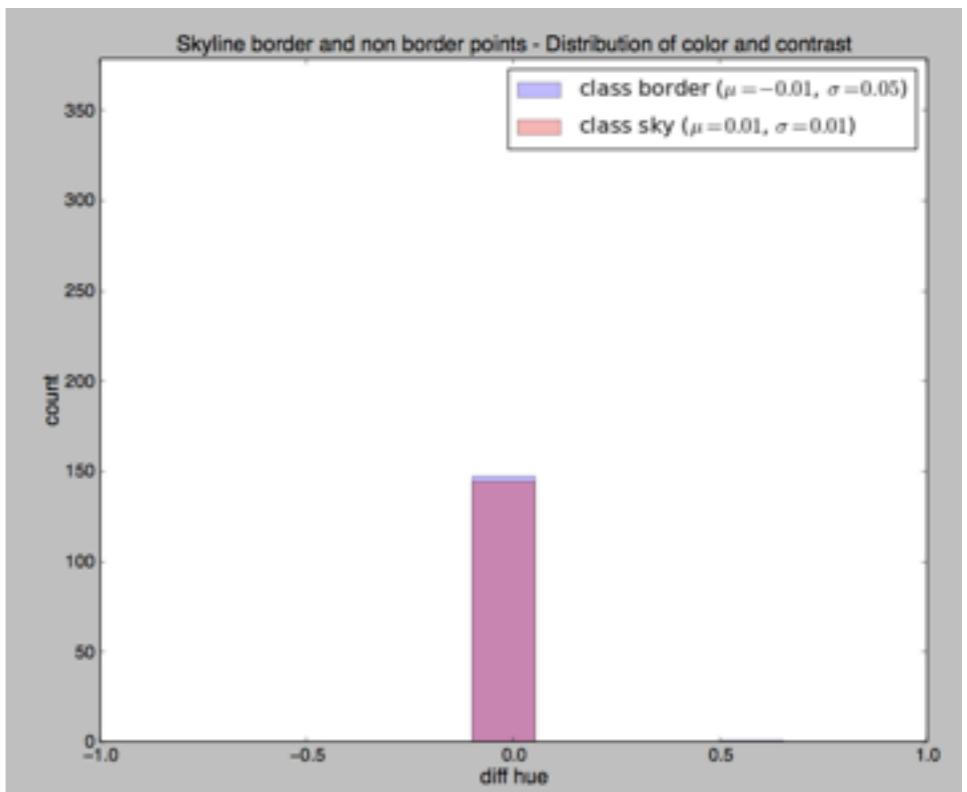
Venturi mtn range, image 1



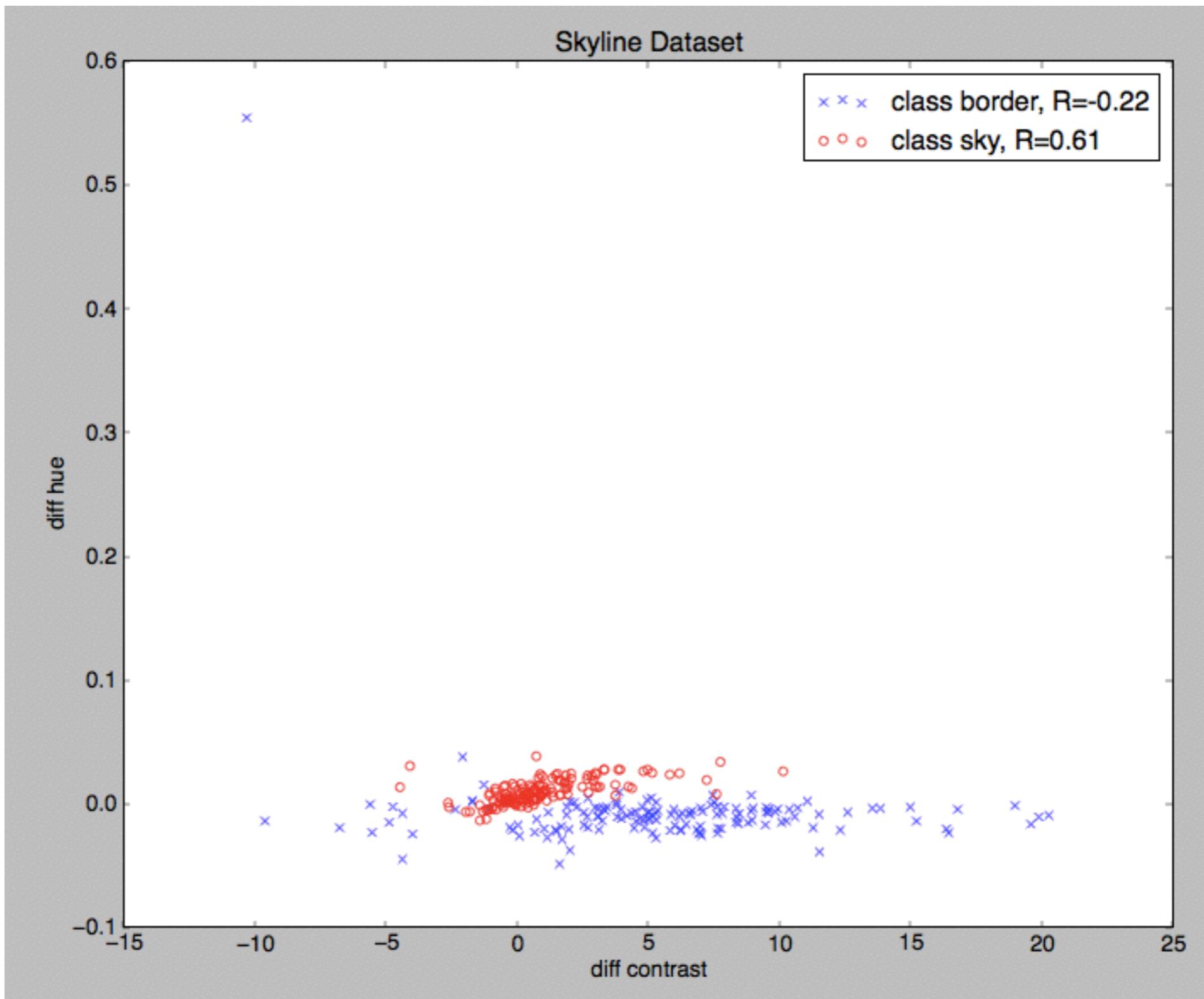
Venturi mtn range, image 1



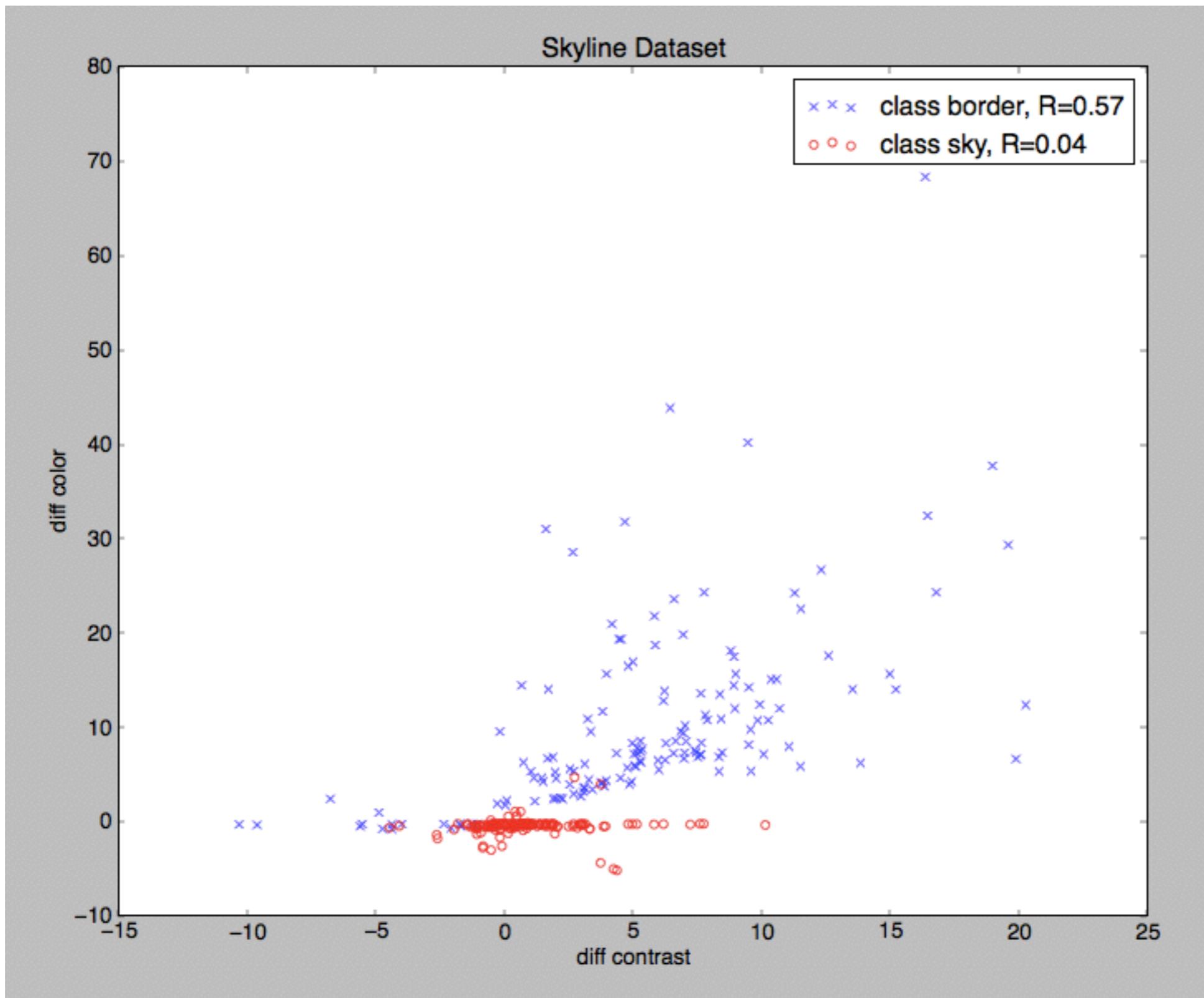
*note: the largest contrasts were removed from analysis for plot visibility



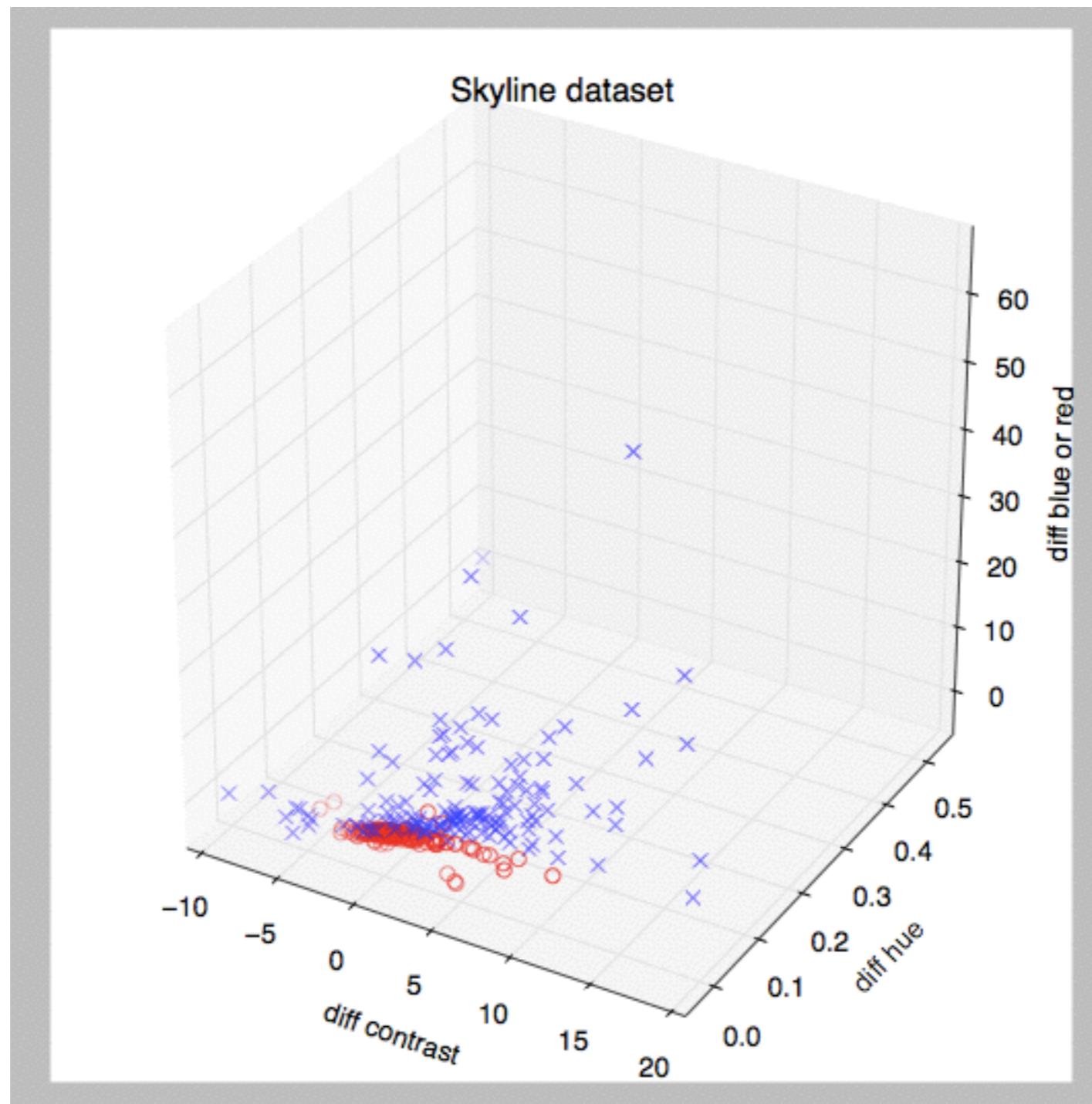
Venturi mtn range, image 1



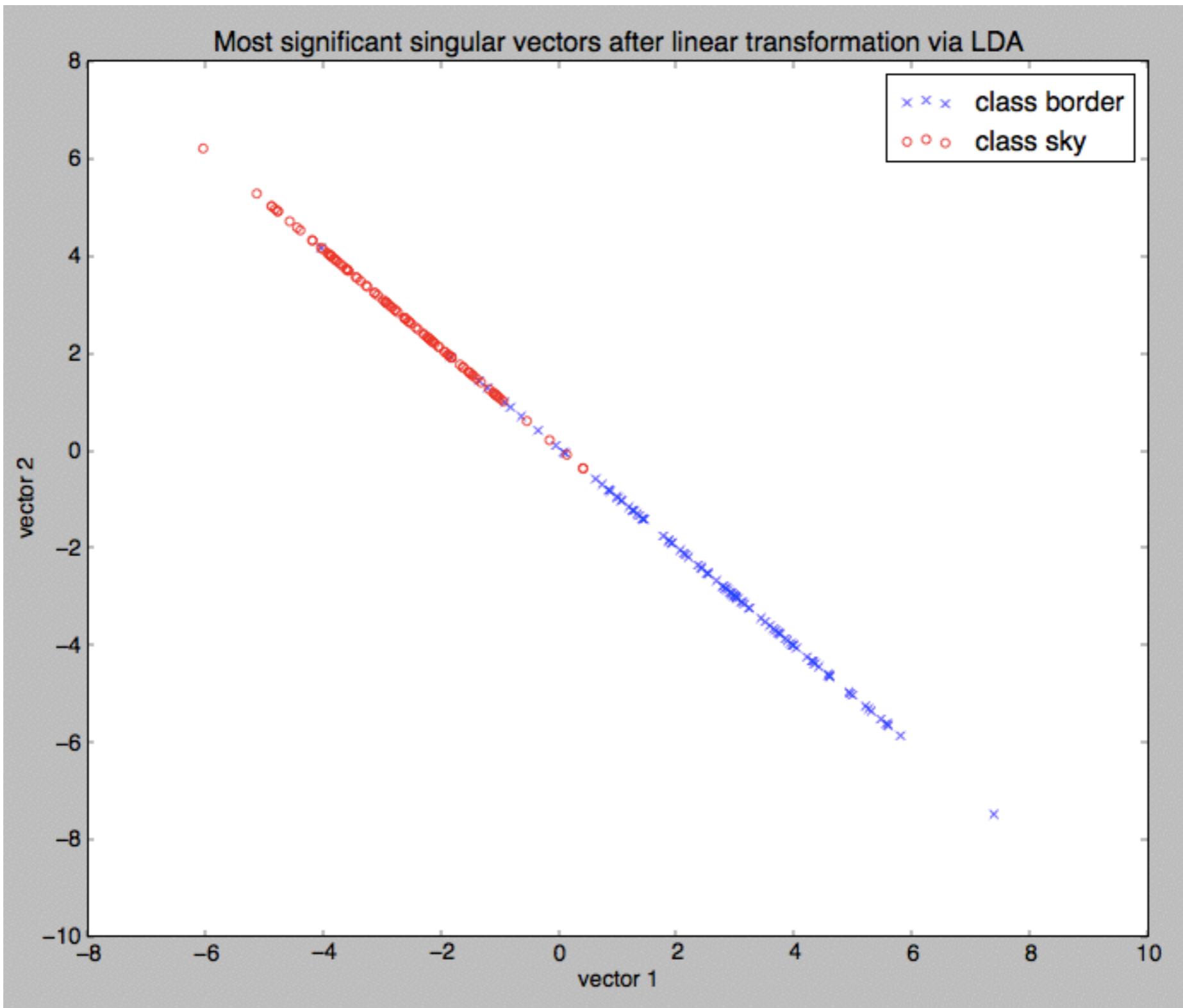
Venturi mtn range, image 1



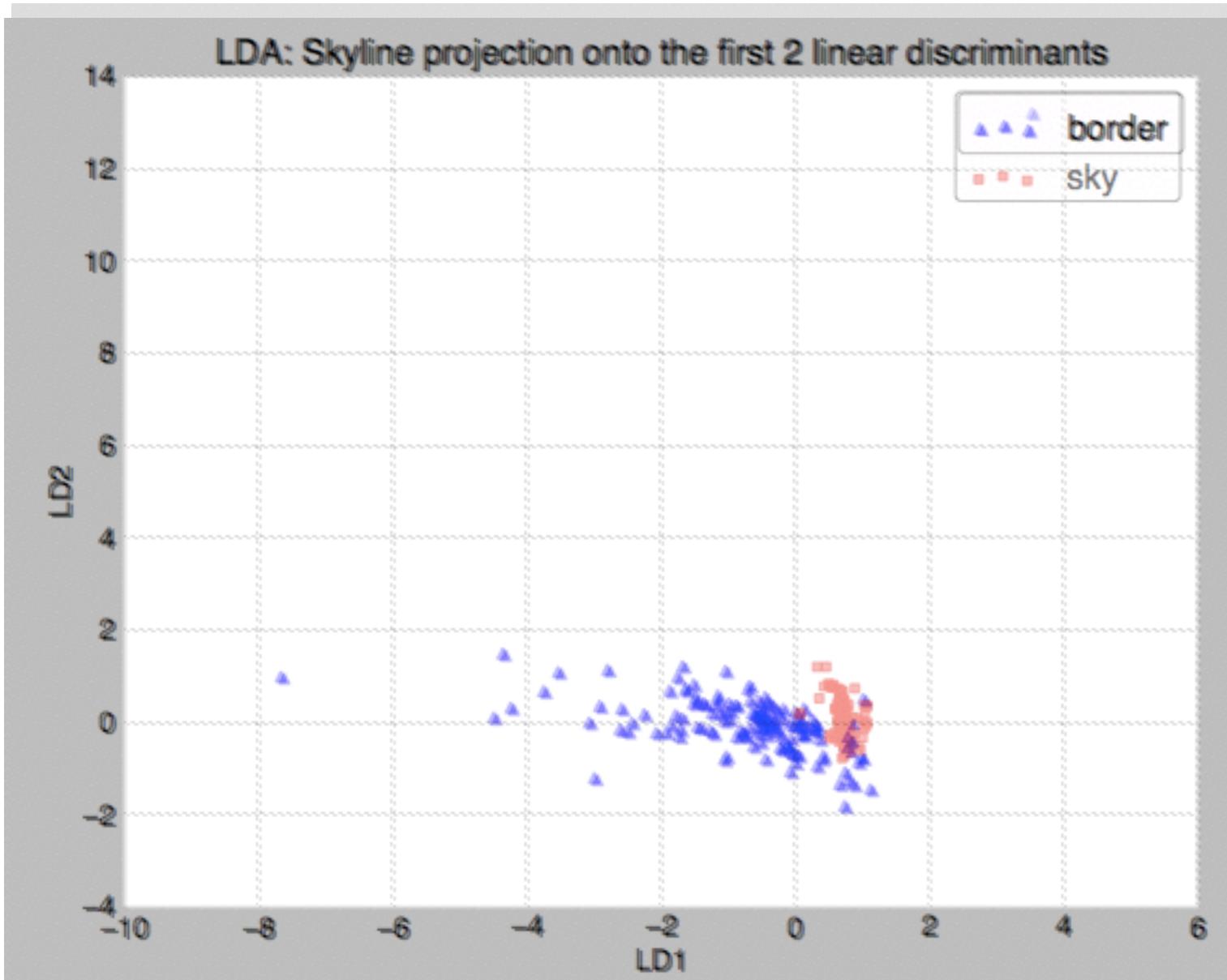
Venturi mtn range, image 1



Venturi mtn range, image 1



Venturi mtn range, image 1



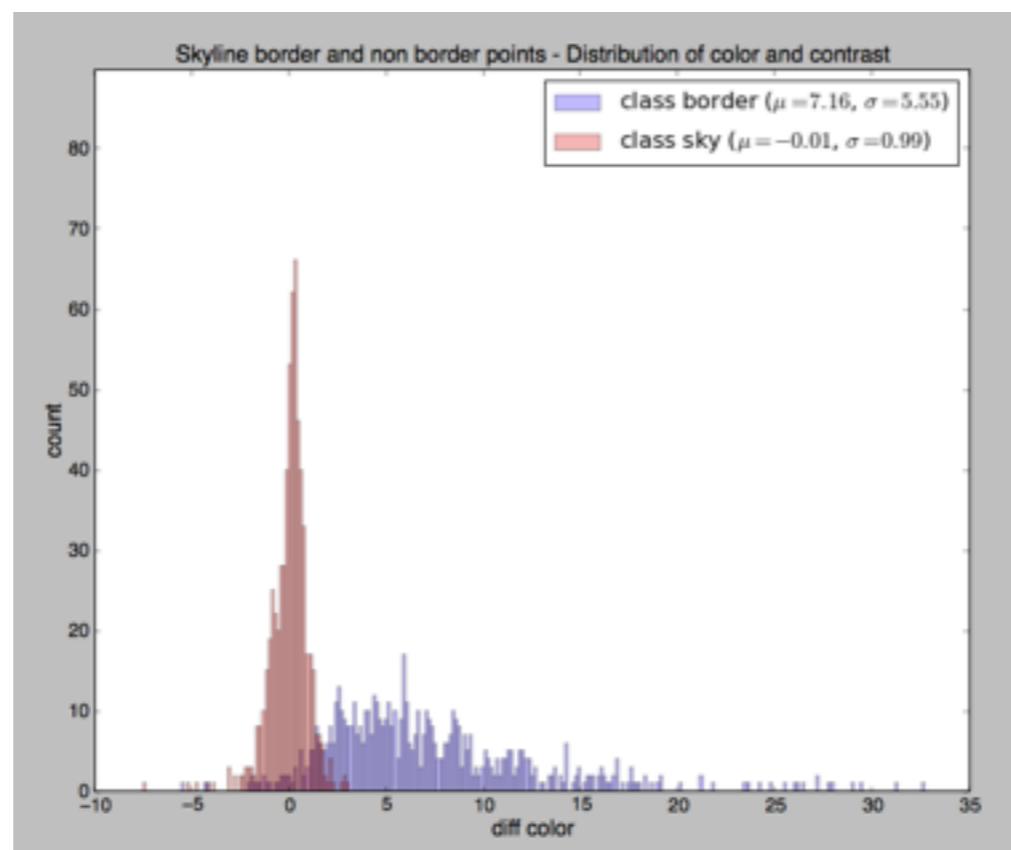
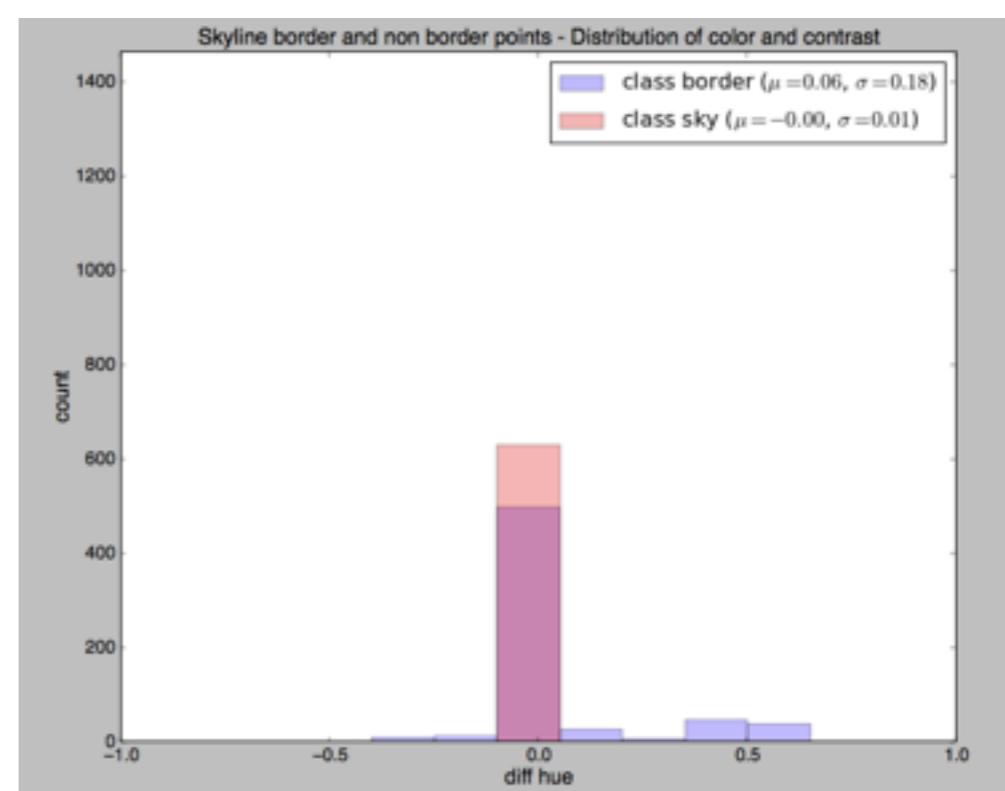
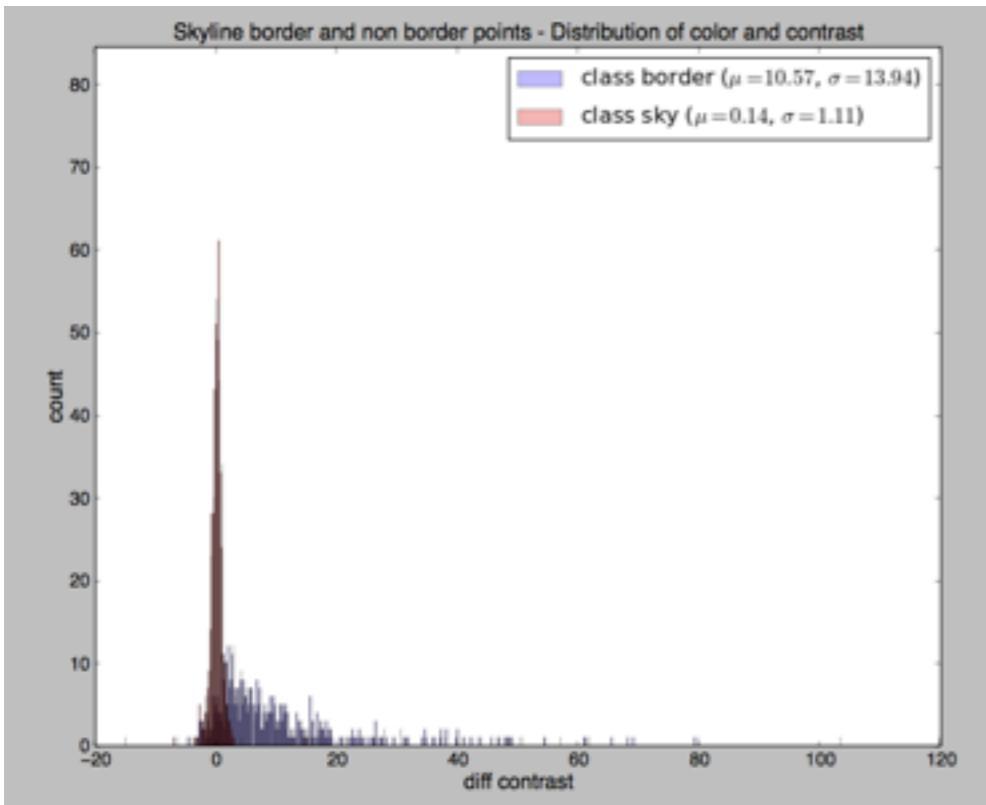
contrast	hue	BorR
Mean Vector class 1: [0.4626	-0.2326	0.5956]
Mean Vector class 2: [-0.4754	0.2391	-0.6122]
('within-class Scatter Matrix:\n', array([[227.7815, -40.2087, 108.4066], [-40.2087, 275.757 , -32.2207], [108.4066, -32.2207, 185.5247]]))		
('between-class Scatter Matrix:\n', array([[192.6906, -96.8562, 248.106], [-96.8562, 48.7642, -124.726], [248.106 , -124.726 , 319.461]]))		
Eigenvalue 1: 1.84e+00		
Eigenvector 1:	[[-0.2236]	
	[0.149]	
	[-0.9632]]	
Eigenvalue 2: 1.18e-16		
Eigenvector 2:	[[0.7602]	
	[-0.1221]	
	[-0.6381]]	
Eigenvalue 3: 2.72e-04		
ok		
Eigenvalues in decreasing order:		
1.83771695135		
0.000271576220989		
1.17934013279e-16		
Variance explained:		
eigenvalue 1: 99.99%		
eigenvalue 2: 0.01%		
eigenvalue 3: 0.00%		
('Matrix W:\n', array([[-0.2236, 0.149 , -0.9632], [0.3866, 0.9204, 0.0591]]))		

seattle test image

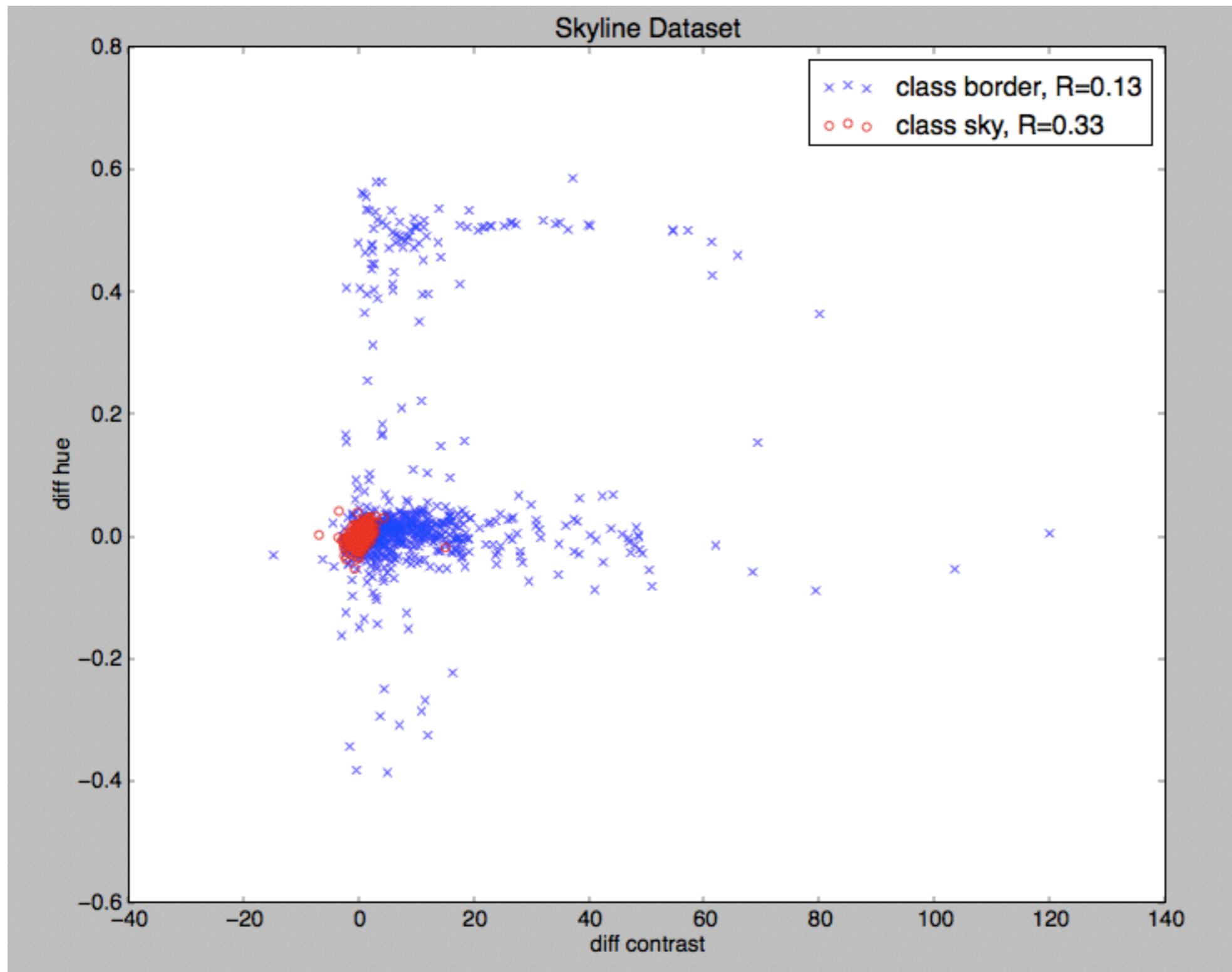


seattle test image

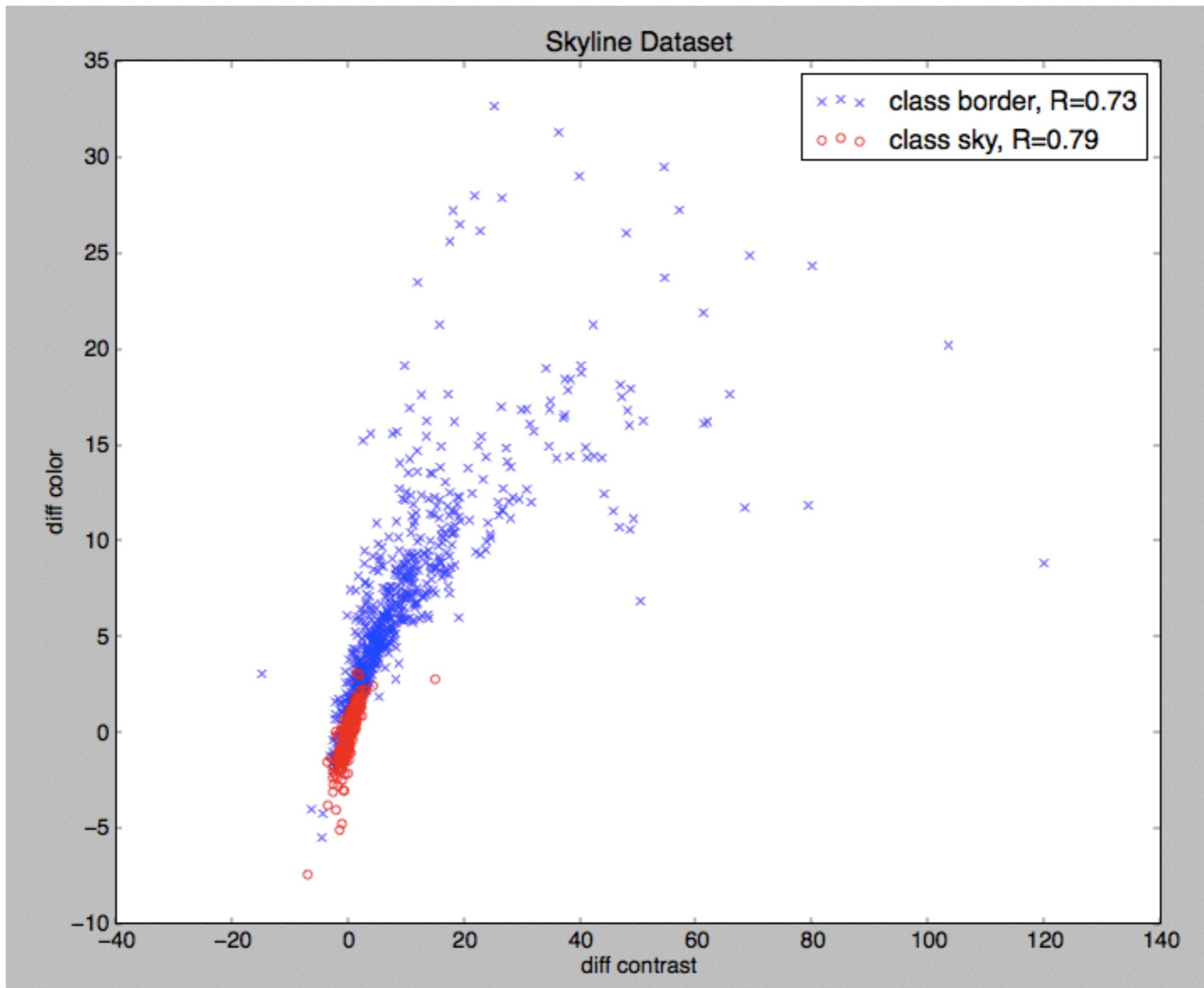
*note: the largest contrasts were removed from analysis for plot visibility



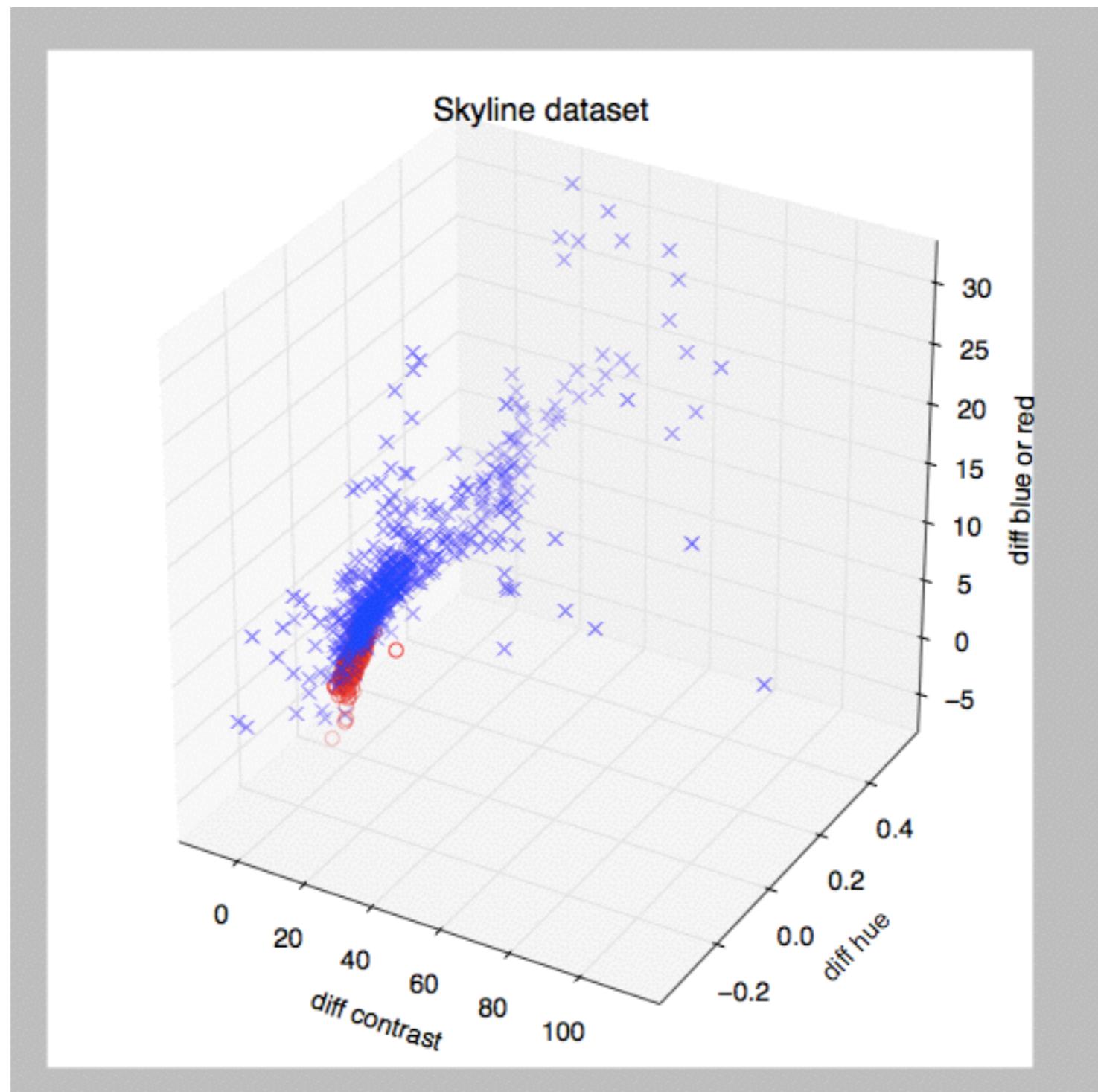
seattle test image



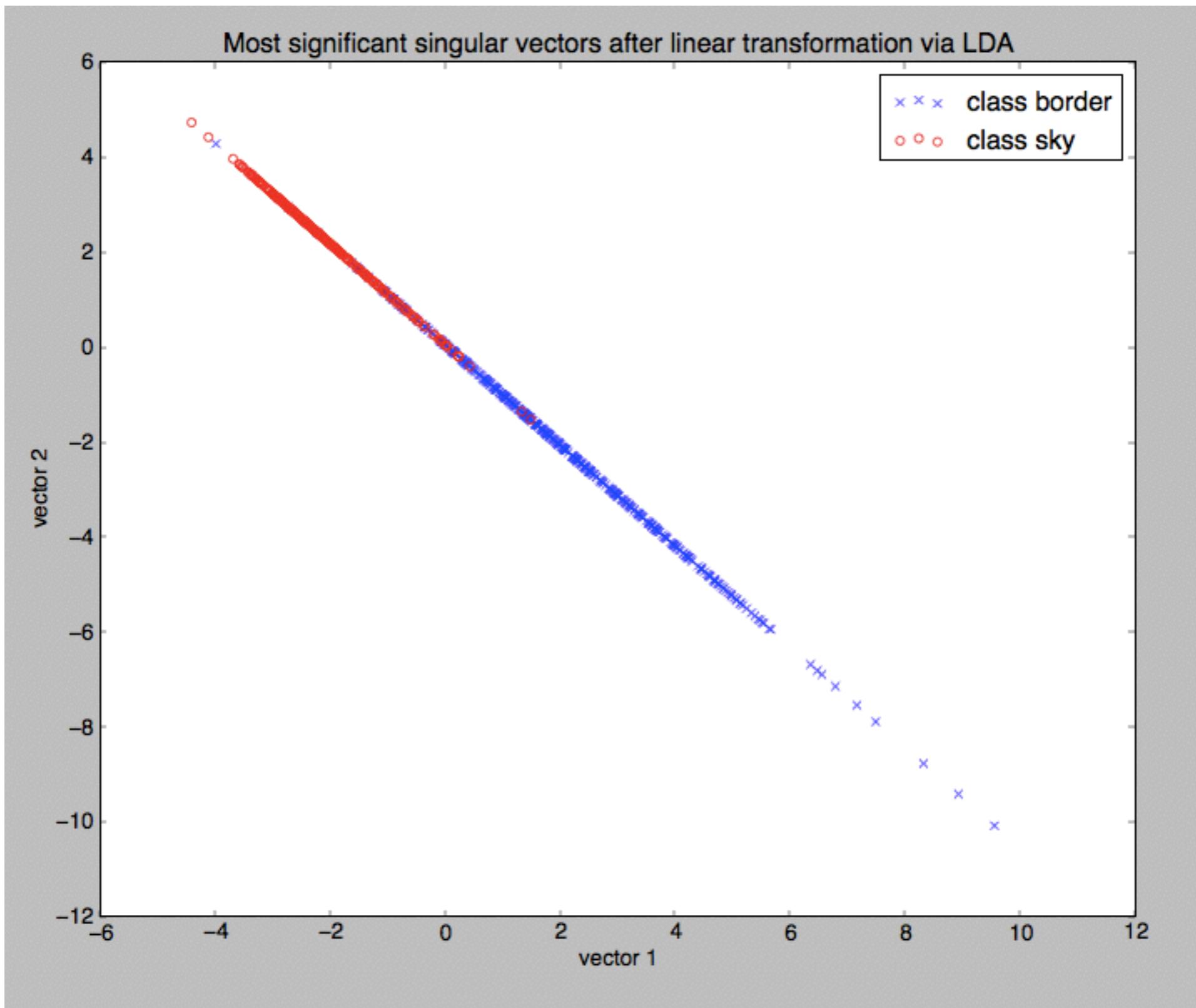
seattle test image



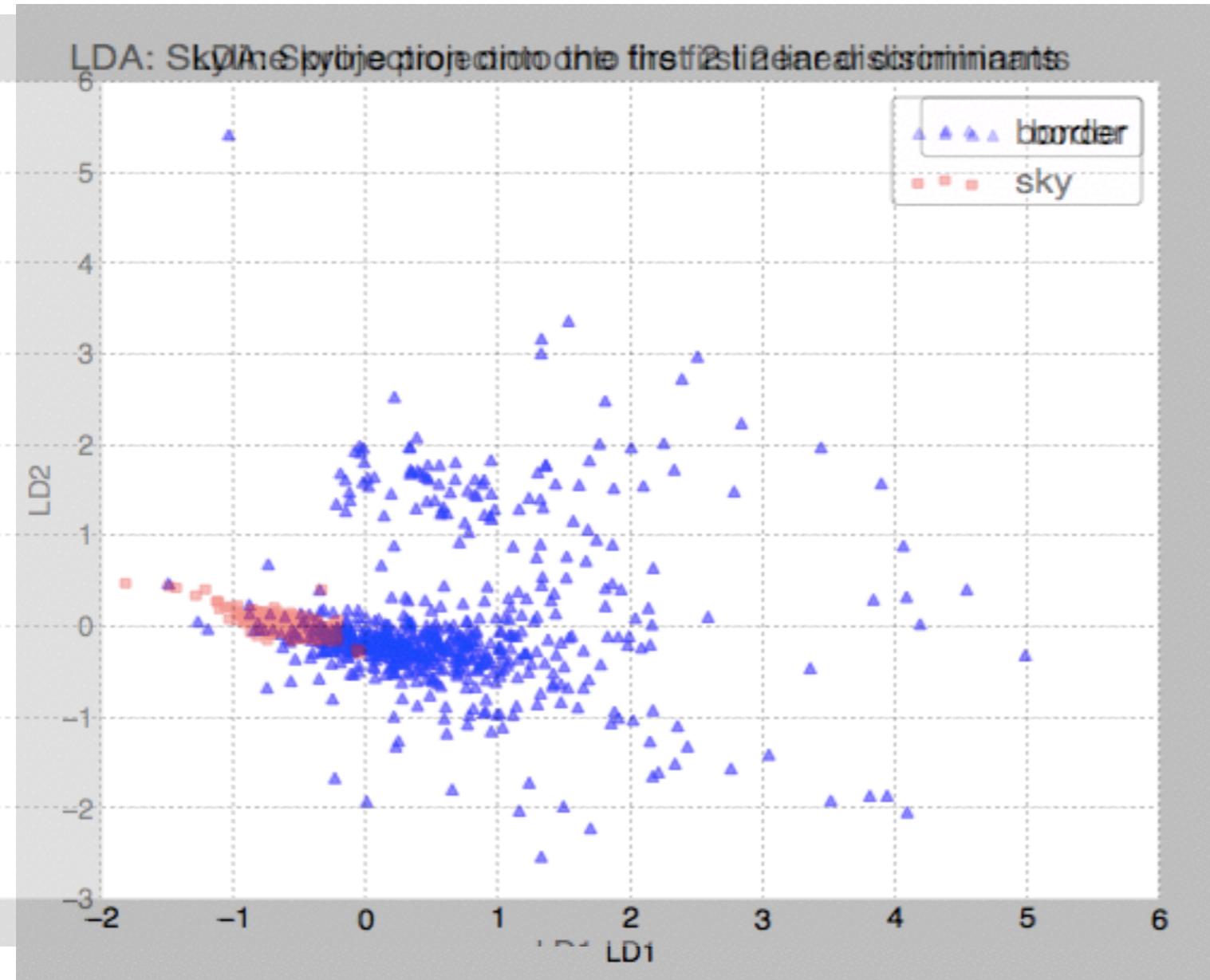
seattle test image



seattle test image



seattle test image

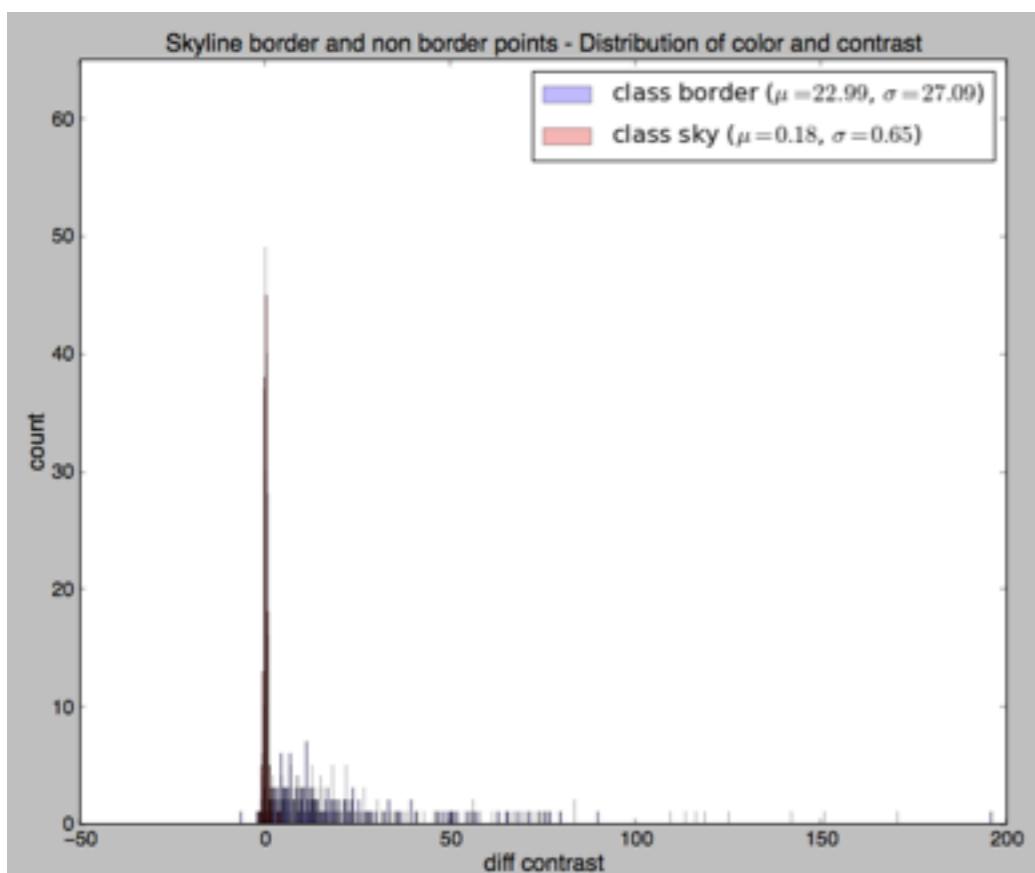


```
contrast  hue   BorR
Mean Vector class 1: [ 0.4656  0.2477  0.6669]
Mean Vector class 2: [-0.4671 -0.2485 -0.669 ]
('within-class Scatter Matrix:\n',
array([[ 985.996 ,  139.7075,  599.7238],
       [ 139.7075, 1182.4522, 237.0341],
       [ 599.7238, 237.0341, 697.8901]]))
('between-class Scatter Matrix:\n',
array([[ 822.0142,  437.3073, 1177.3651],
       [ 437.3073, 232.6457, 626.3517],
       [1177.3651, 626.3517, 1686.332 ]]))
Eigenvector 1:
[[[-0.1942]
 [ 0.0051]
 [ 0.9809]]]
Eigenvalue 1: 2.51e+00
Eigenvector 2:
[[[-0.8163]
 [ 0.392 ]
 [ 0.4243]]]
Eigenvalue 2: -5.33e-16
Eigenvector 3:
[[ 0.5968]
 [ 0.521 ]
 [-0.6102]]]
Eigenvalue 3: 1.38e-06
ok
Eigenvalues in decreasing order:
2.50953939789
1.37504566598e-06
5.33350812381e-16
Variance explained:
eigenvalue 1: 100.00%
eigenvalue 2: 0.00%
eigenvalue 3: 0.00%
('Matrix W:\n', array([[-0.1942,  0.0051,  0.9809],
       [ 0.5968,  0.521 , -0.6102]]))
```

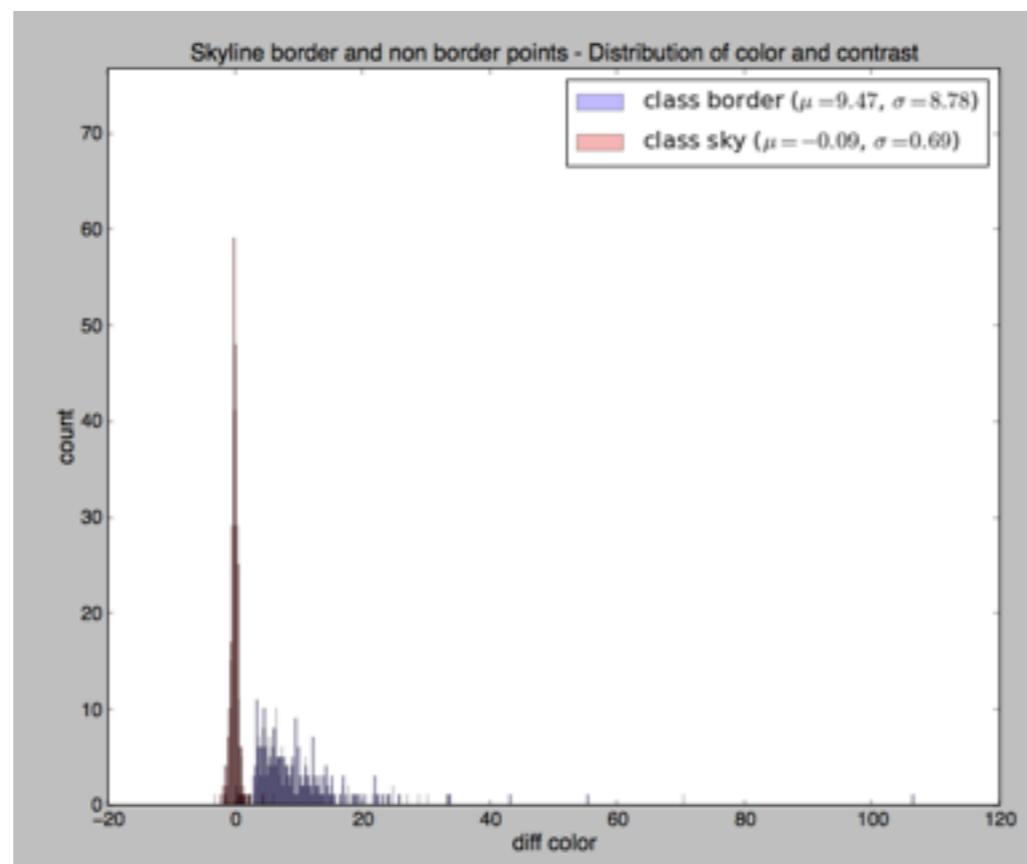
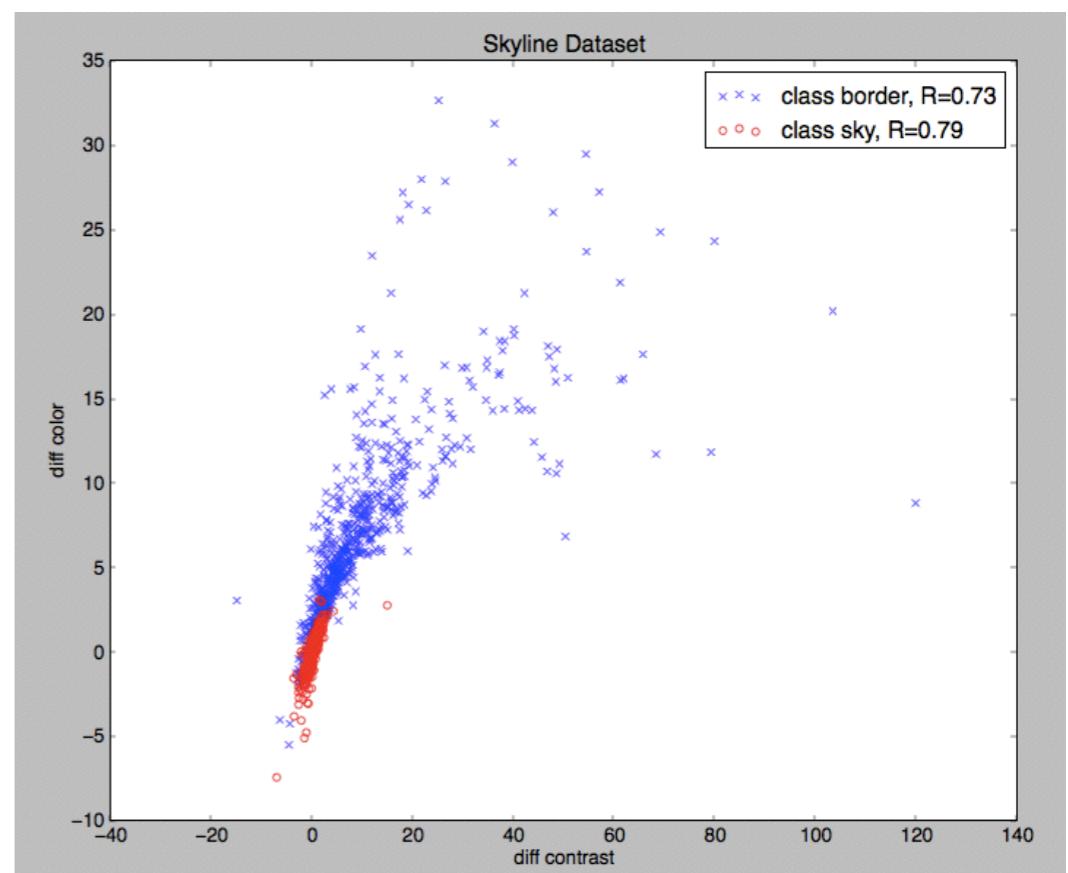
arches test image



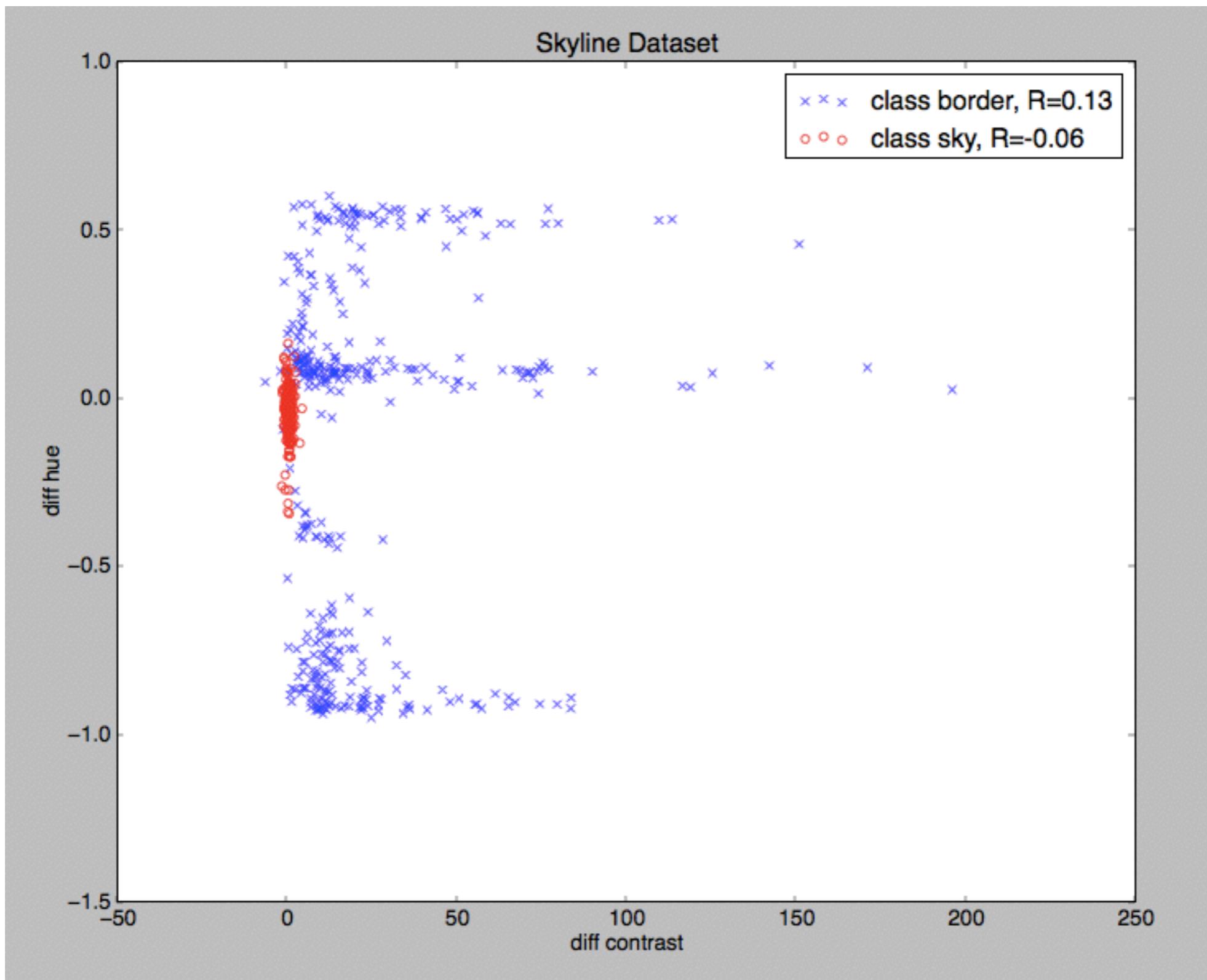
arches test image



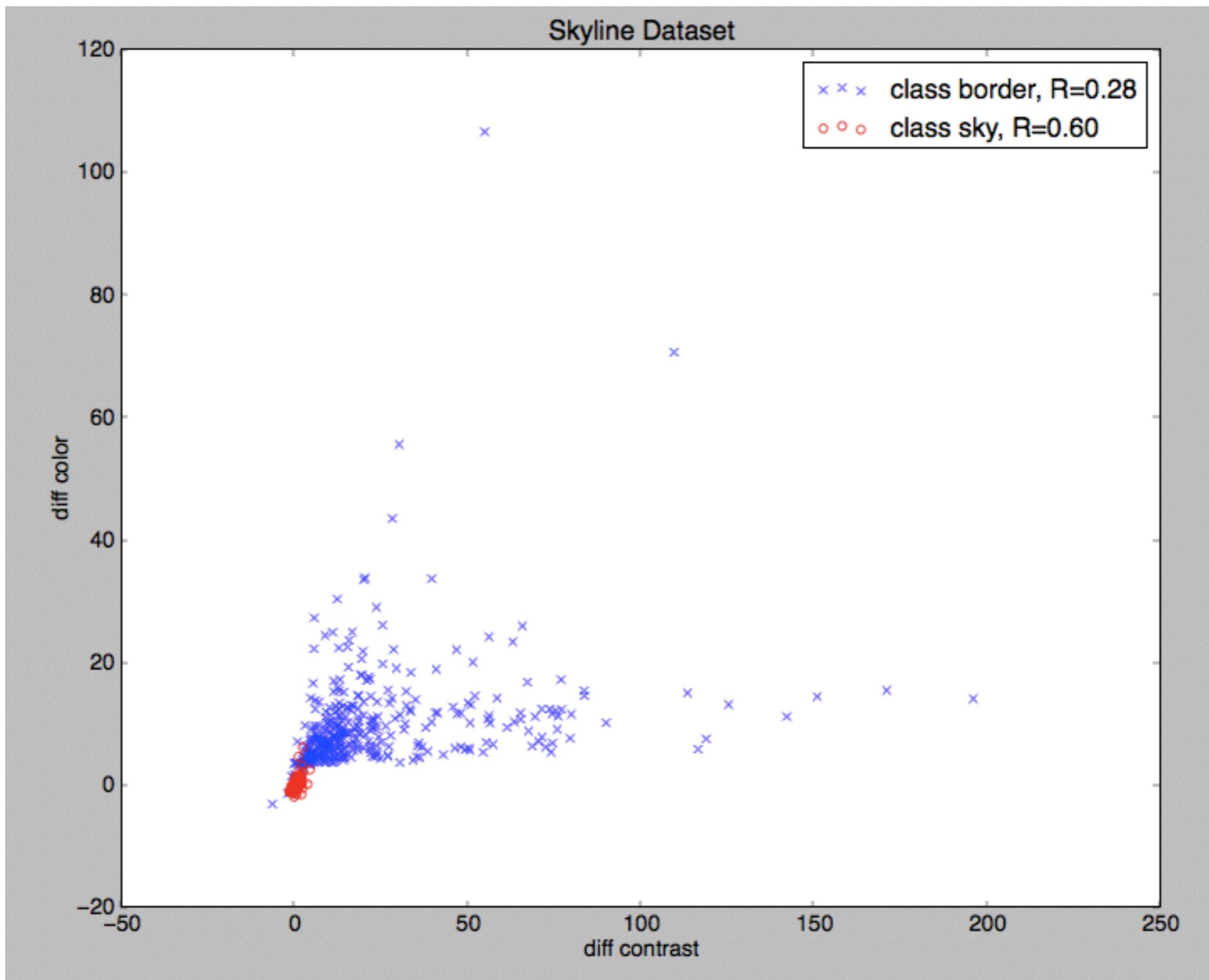
*note: the largest contrasts were removed from analysis for plot visibility



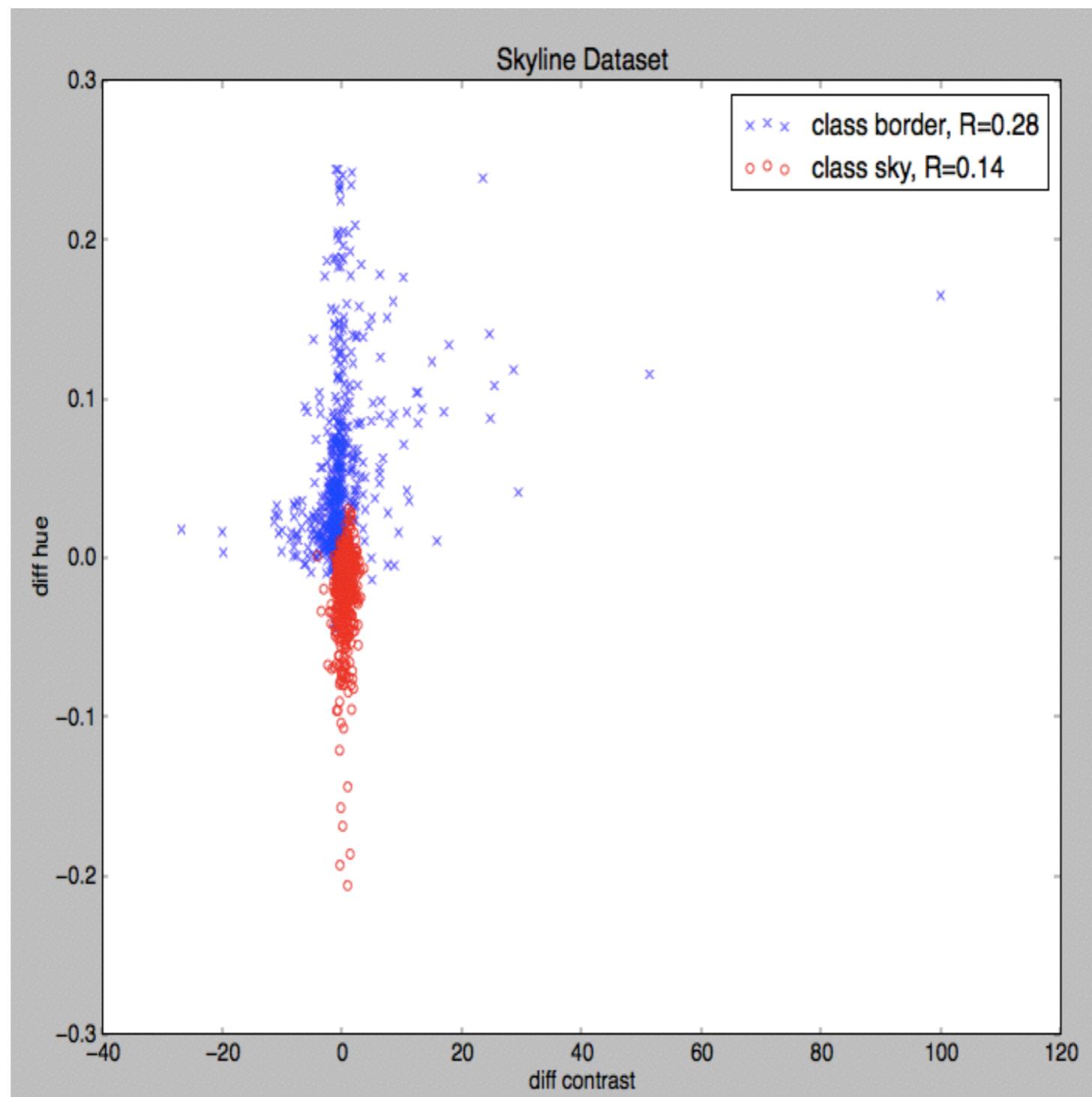
arches test image



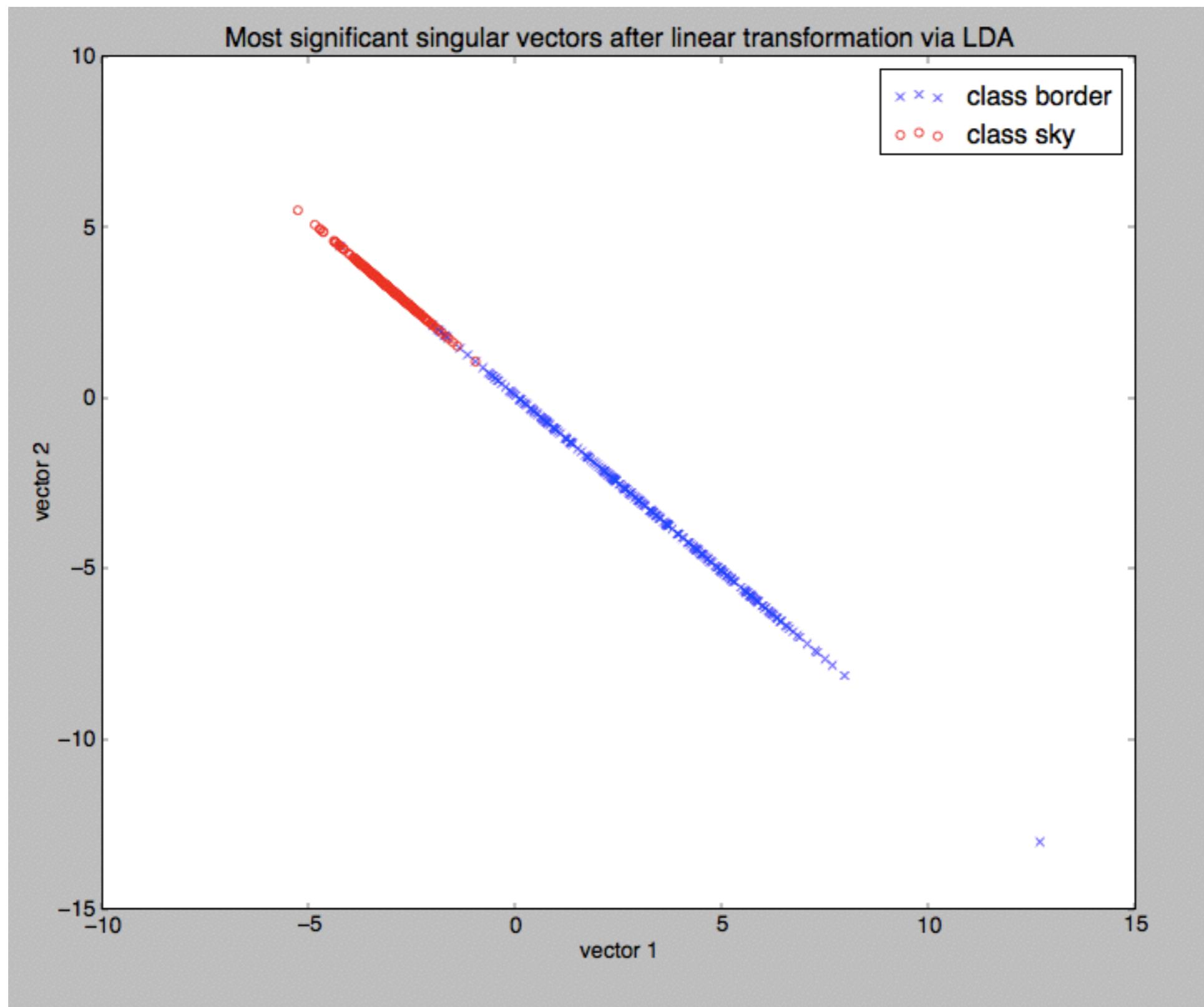
arches test image



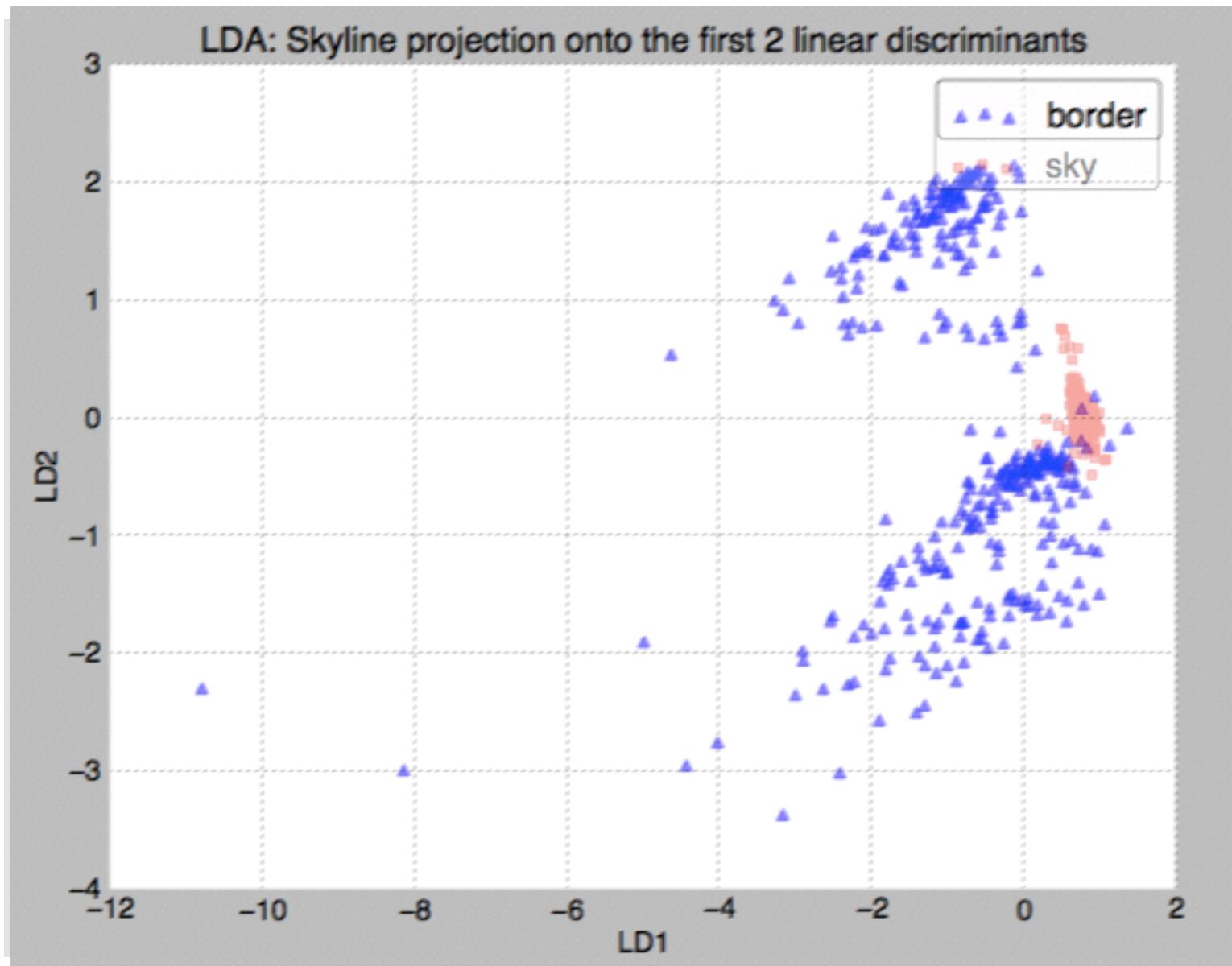
arches test image



arches test image



arches test image



contrast	hue	BorR
Mean Vector class 1: [0.5095	-0.1761	0.6067]
Mean Vector class 2: [-0.5123	0.177	-0.6099]

('within-class Scatter Matrix:\n',
array([[551.2873, 78.8521, 144.3438],
[78.8521, 722.7472, 146.1896],
[144.3438, 146.1896, 469.9548]]))
('between-class Scatter Matrix:\n',
array([[584.1418, -201.8594, 695.5218],
[-201.8594, 69.7621, -240.3494],
[695.5218, -240.3494, 828.1391]]))

Eigenvector 1:
[[-0.4385]
[0.3714]
[-0.8184]]
Eigenvalue 1: 2.72e+00

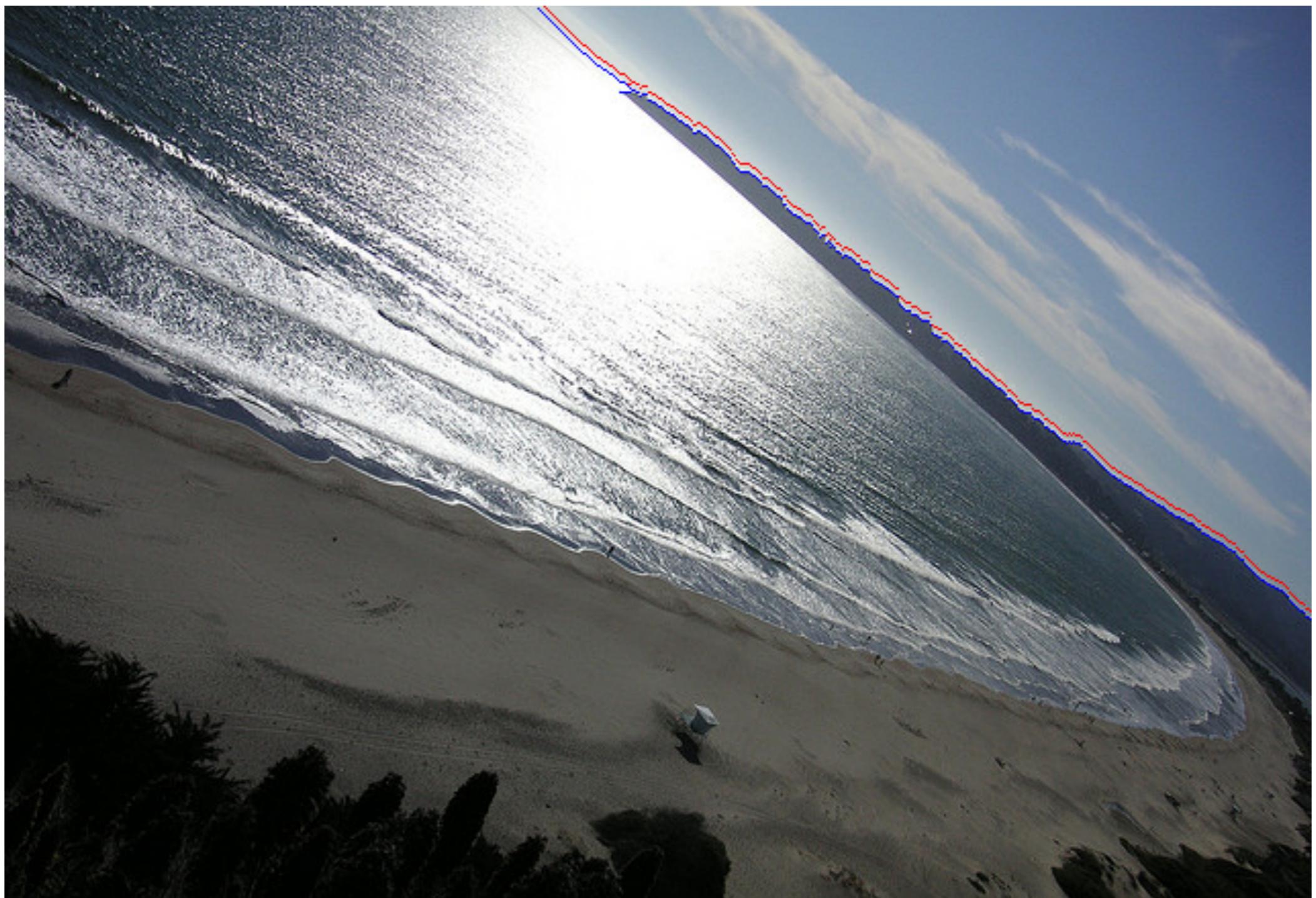
Eigenvector 2:
[[-0.749]
[0.093]
[0.656]]
Eigenvalue 2: 3.72e-16

Eigenvector 3:
[[-0.3207]
[-0.9472]
[-0.0055]]
Eigenvalue 3: 7.63e-06
ok
Eigenvalues in decreasing order:

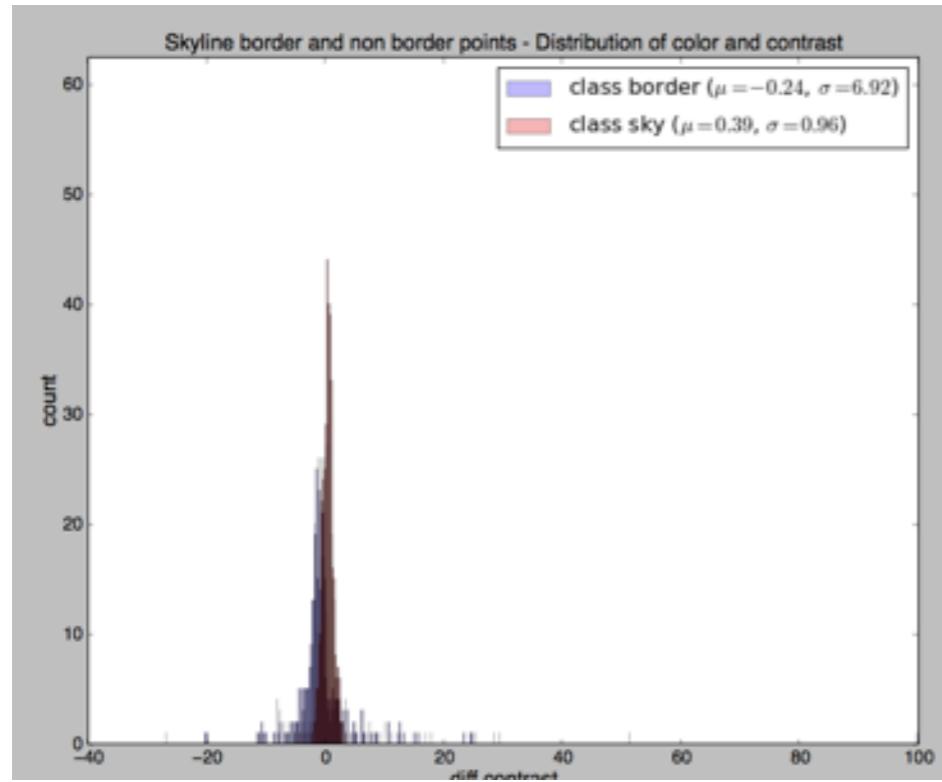
2.72354460153
7.62574597694e-06
3.7249290295e-16
Variance explained:

eigenvalue 1: 100.00%
eigenvalue 2: 0.00%
eigenvalue 3: 0.00%
('Matrix W:\n', array([[-0.4385, 0.3714, -0.8184],
[-0.3207, -0.9472, -0.0055]]))

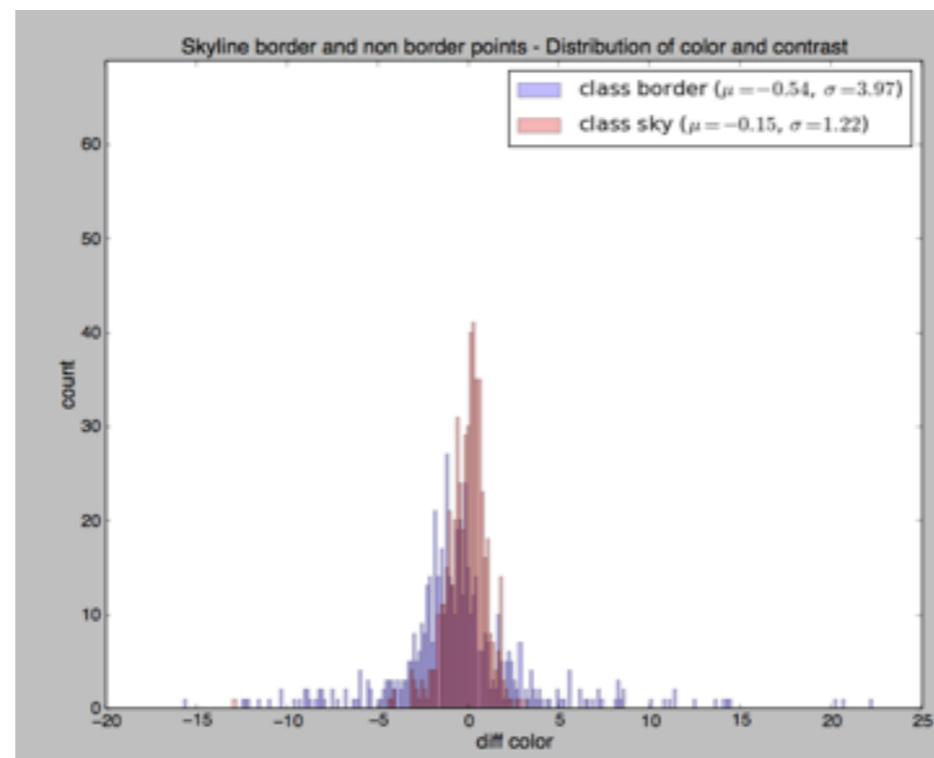
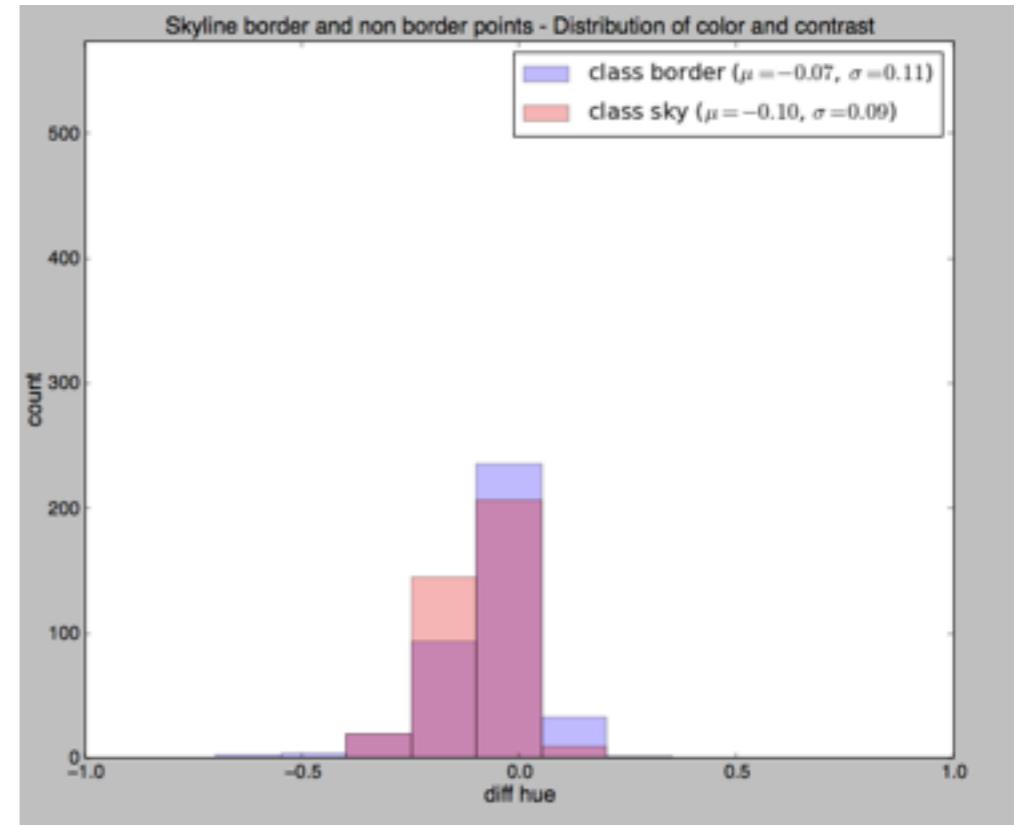
stinson test image



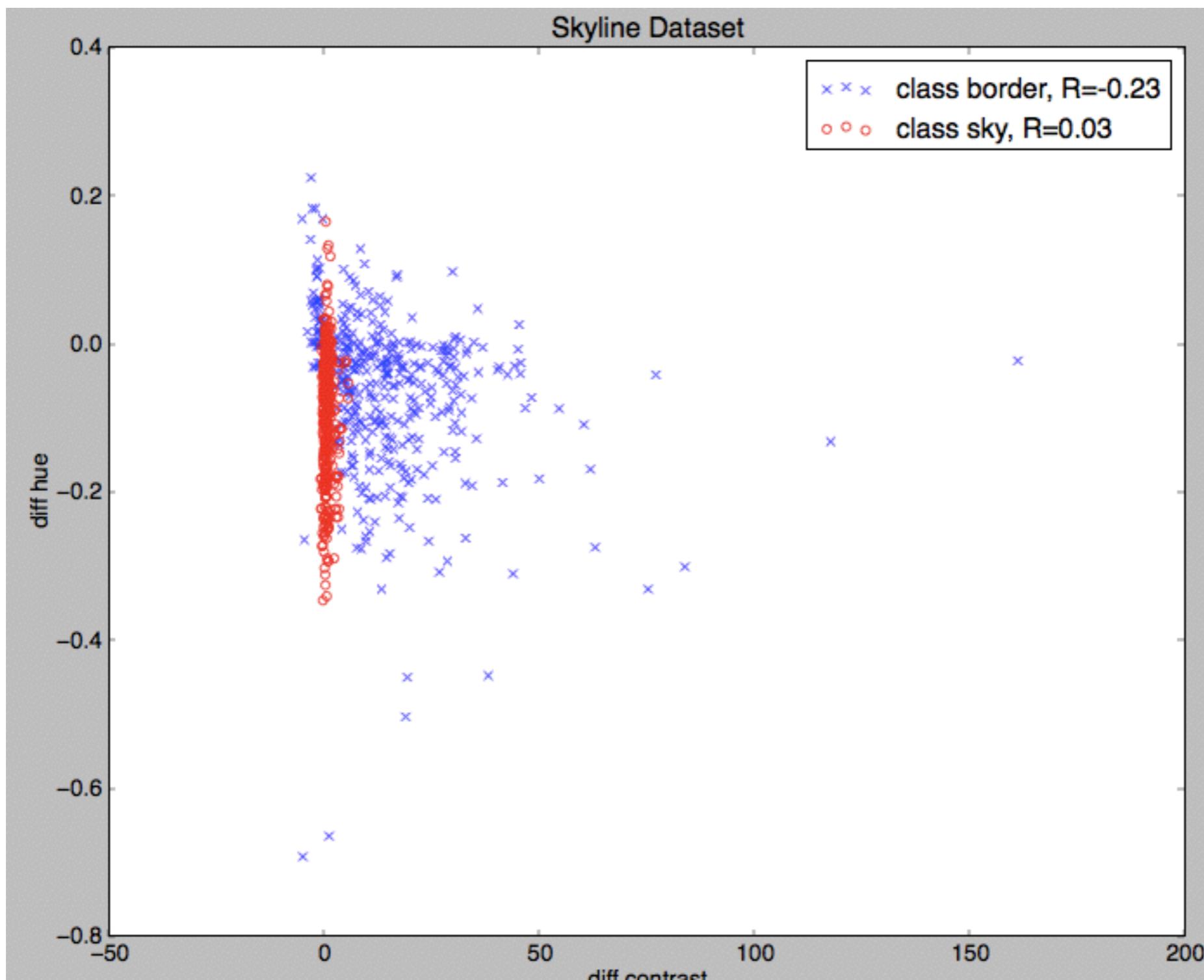
stinson test image



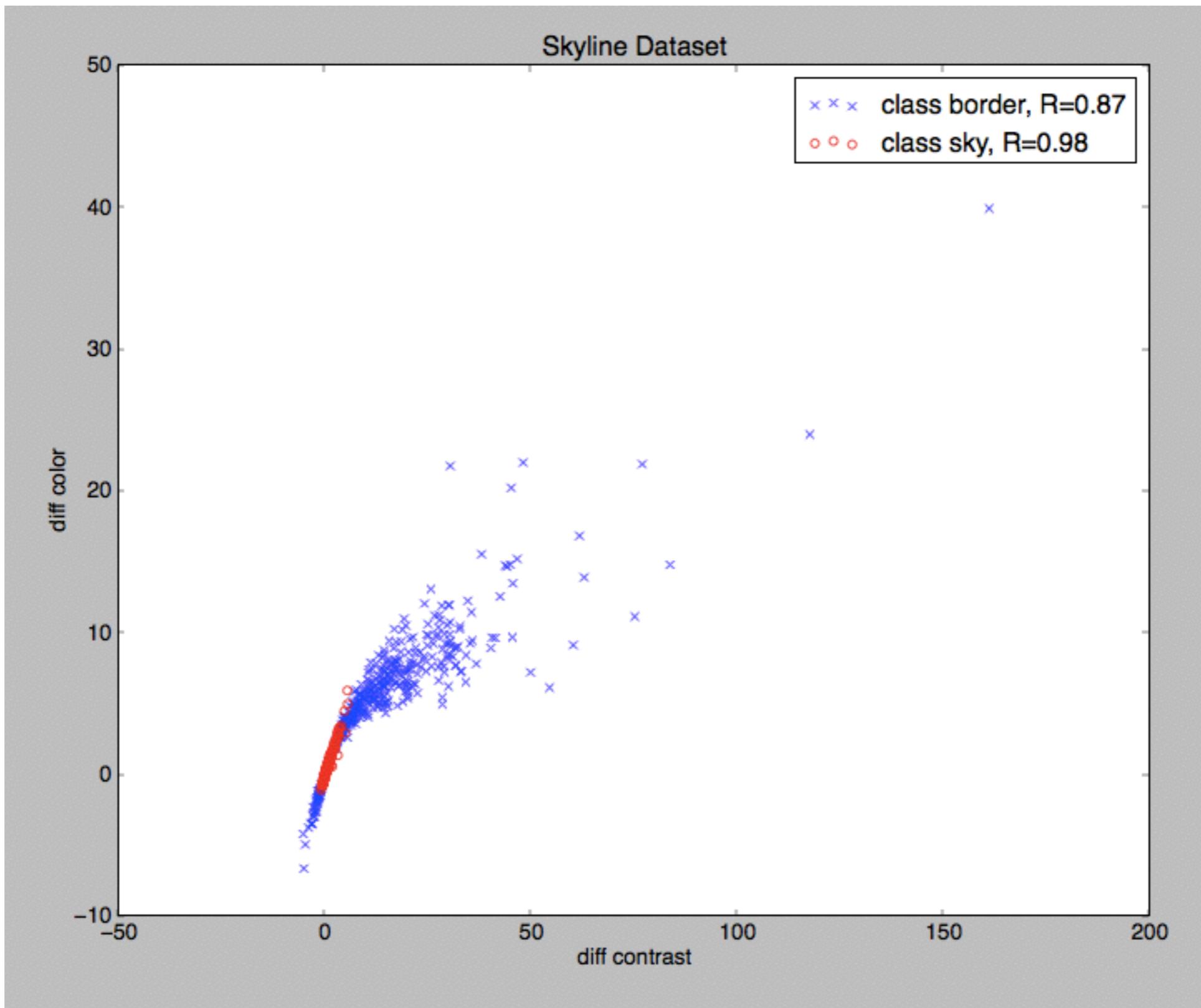
*note: the largest contrasts were removed from analysis for plot visibility



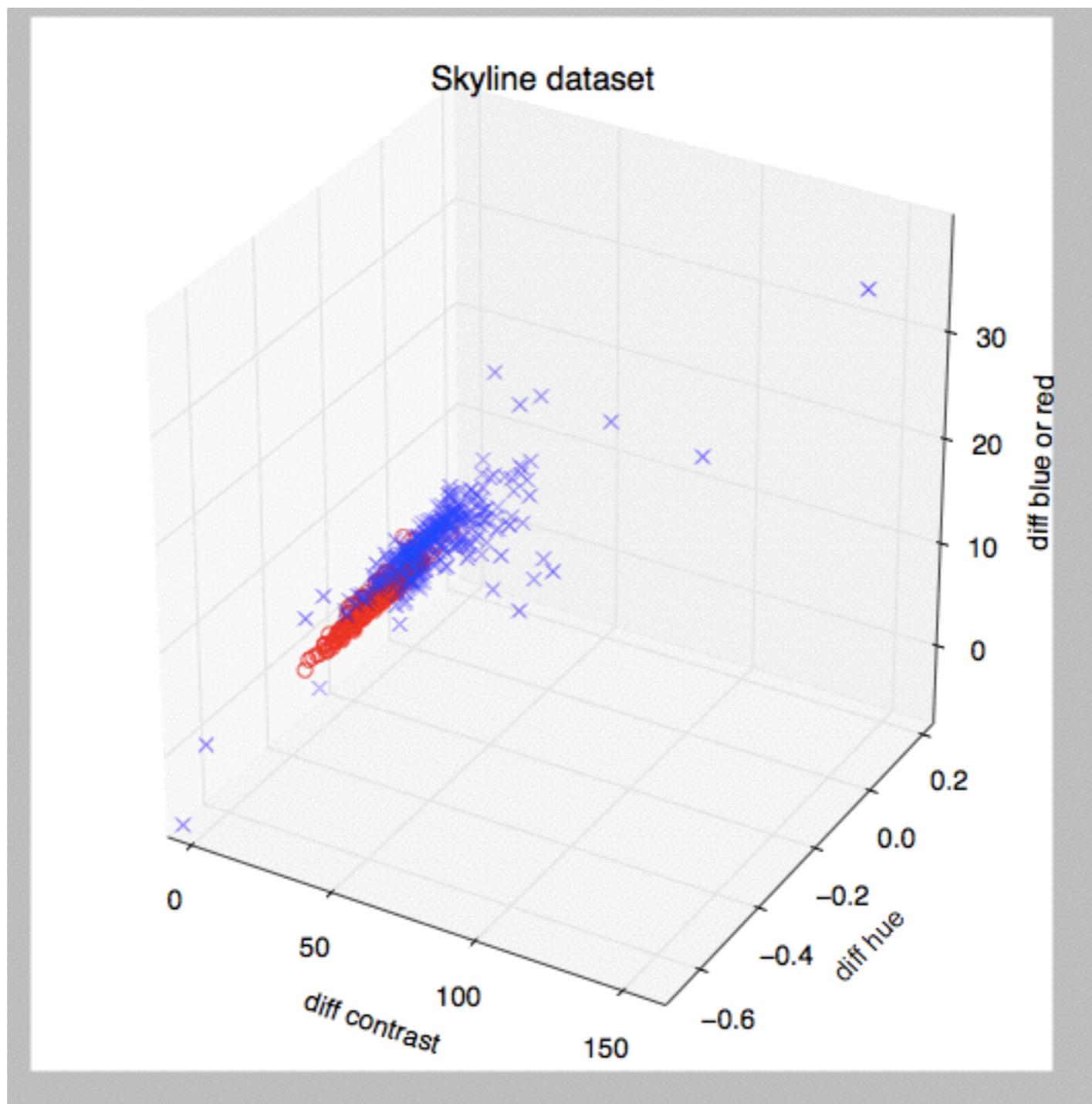
stinson test image



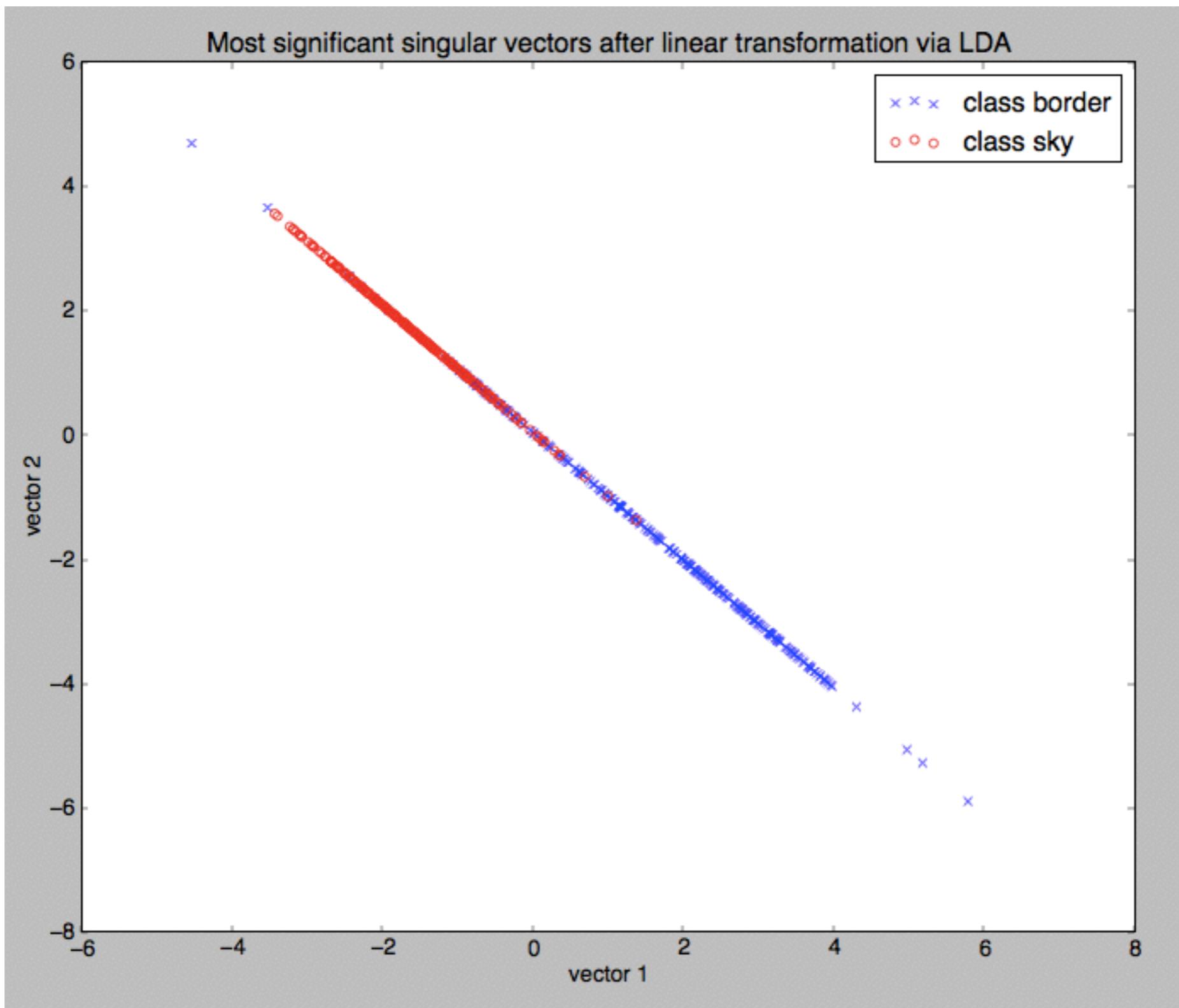
stinson test image



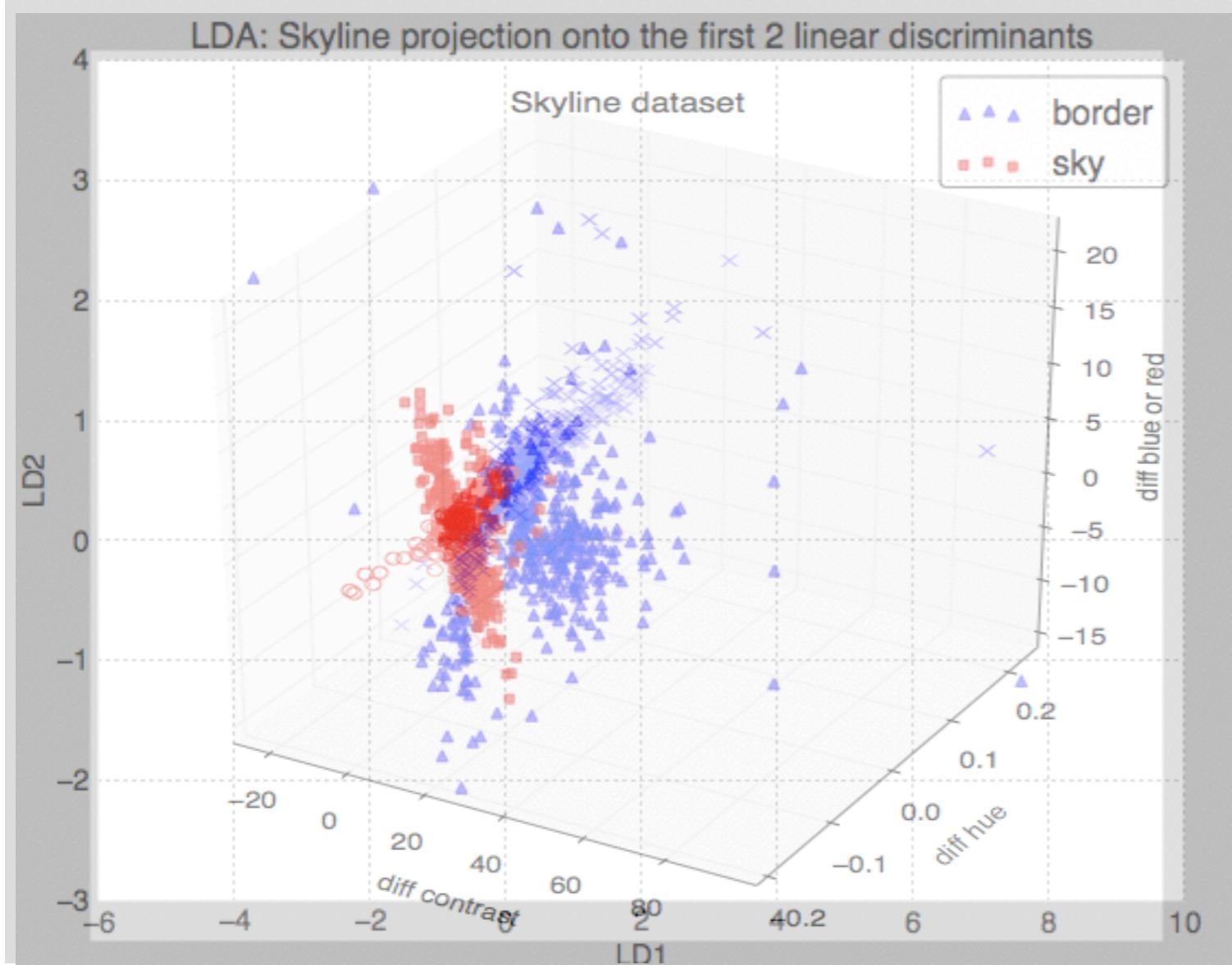
stinson test image



stinson test image



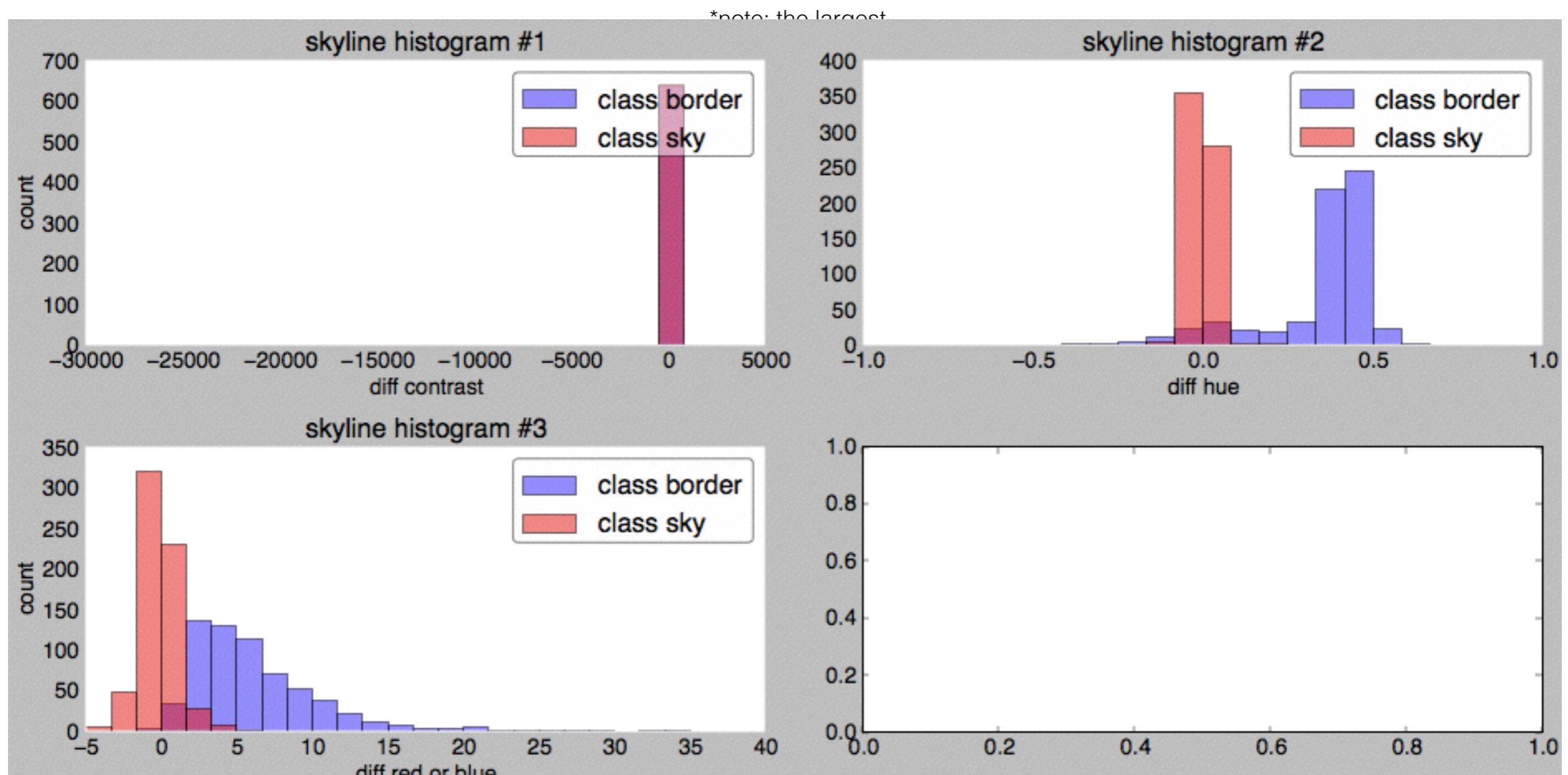
stinson test image



cloudy san jose test image

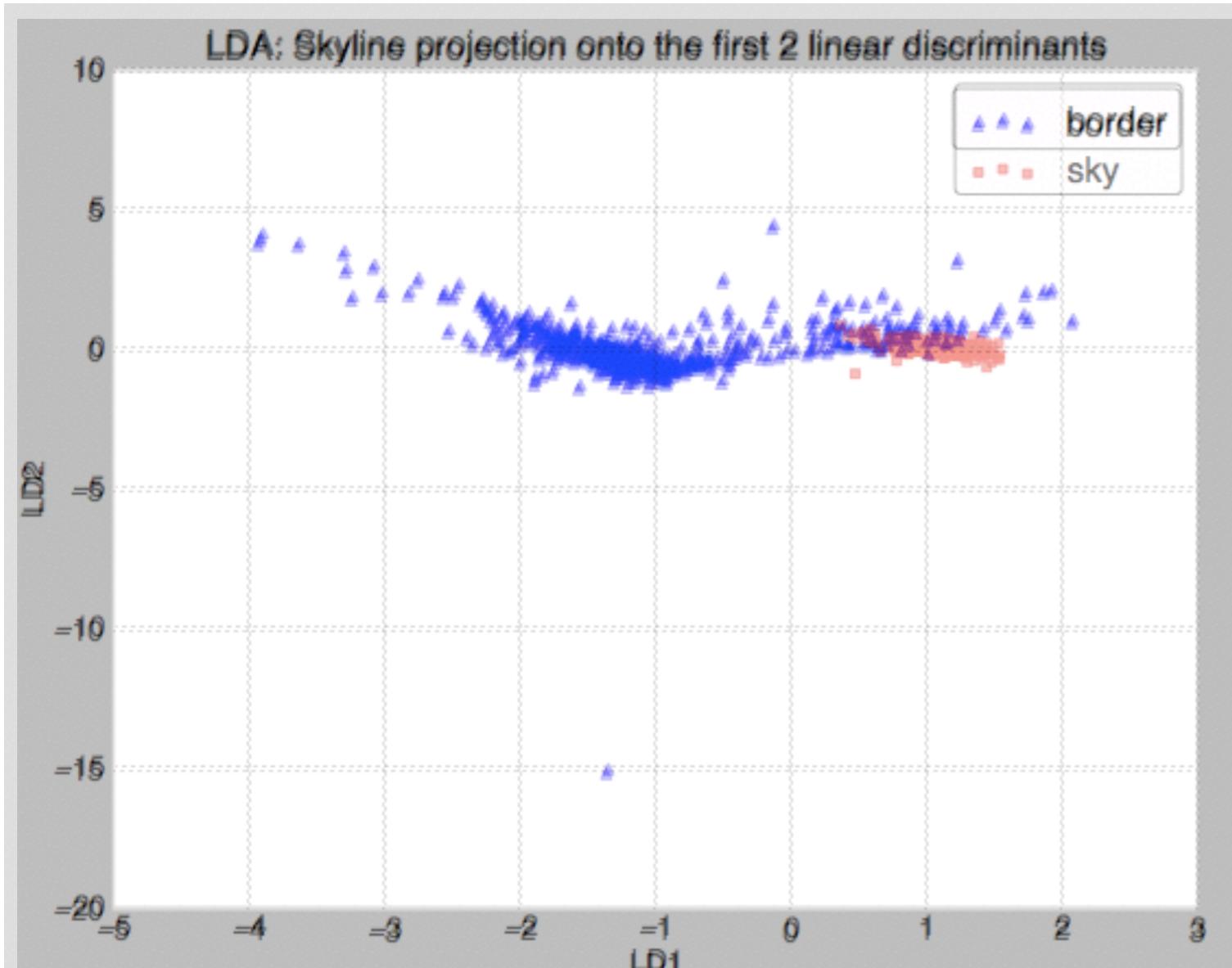


cloudy san jose test image



cloudy san jose test image

cloudy san jose test image



```
contrast  hue      BorR
Mean Vector class 1: [-0.0218  0.8184  0.6903]
Mean Vector class 2: [ 0.0218 -0.8184 -0.6903]

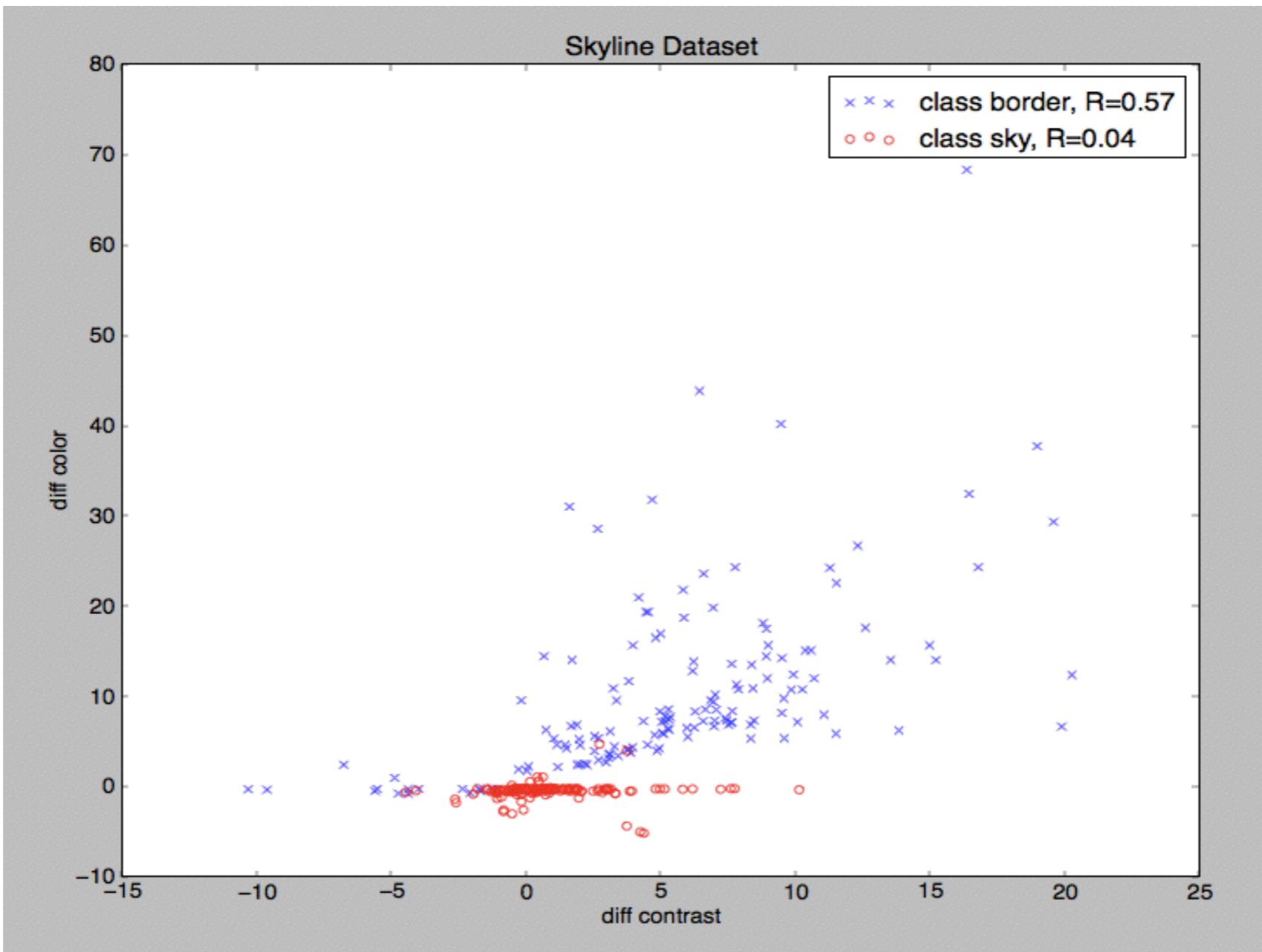
('within-class Scatter Matrix:\n', array([[ 1281.39 ,
       1.9572,  423.3152,   88.2208],
      [-1.5929,   88.2208,  671.1791]]))
('between-class Scatter Matrix:\n', array([[ 1.8299e+00,
      -6.8659e+01,  2.5761e+03,  2.1727e+03],
     [-5.7907e+01,  2.1727e+03,  1.8325e+03]]))

Eigenvector 1:
[[ 0.0097]
 [-0.9117]
 [-0.4106]]
Eigenvalue 1: 7.68e+00

Eigenvector 2:
[[-0.9952]
 [ 0.0459]
 [-0.0859]]
Eigenvalue 2: -9.73e-18

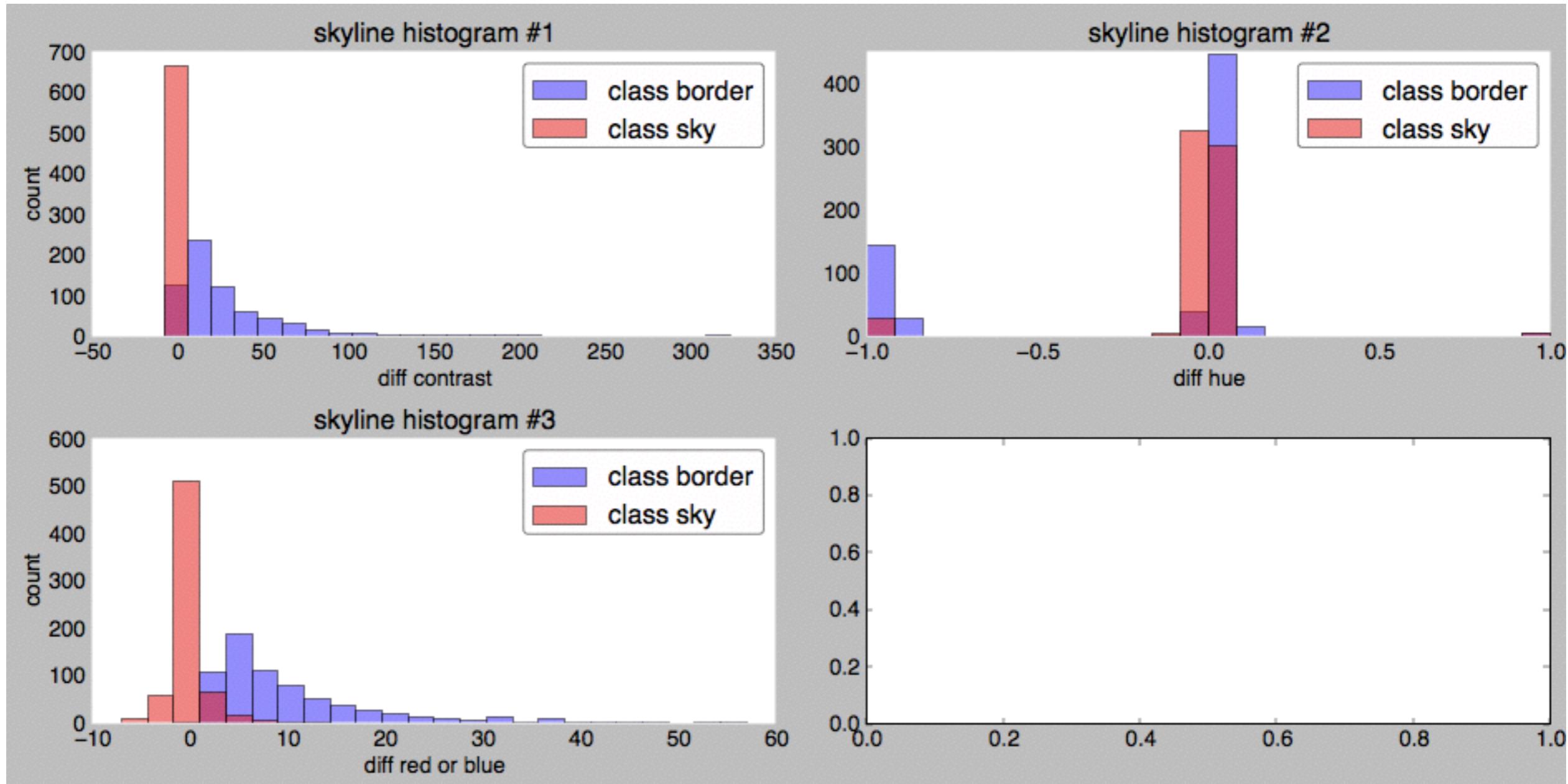
Eigenvector 3:
[[ 0.4335]
 [-0.5742]
 [ 0.6945]]
Eigenvalue 3: -3.76e-16
ok
Eigenvalues in decreasing order:
7.67840538363
3.76177431343e-16
9.72887856366e-18
Variance explained:
eigenvalue 1: 100.00%
eigenvalue 2: 0.00%
eigenvalue 3: 0.00%
('Matrix W:\n', array([[ 0.0097, -0.9117, -0.4106],
 [ 0.4335, -0.5742,  0.6945]]))
```

stonehenge test image

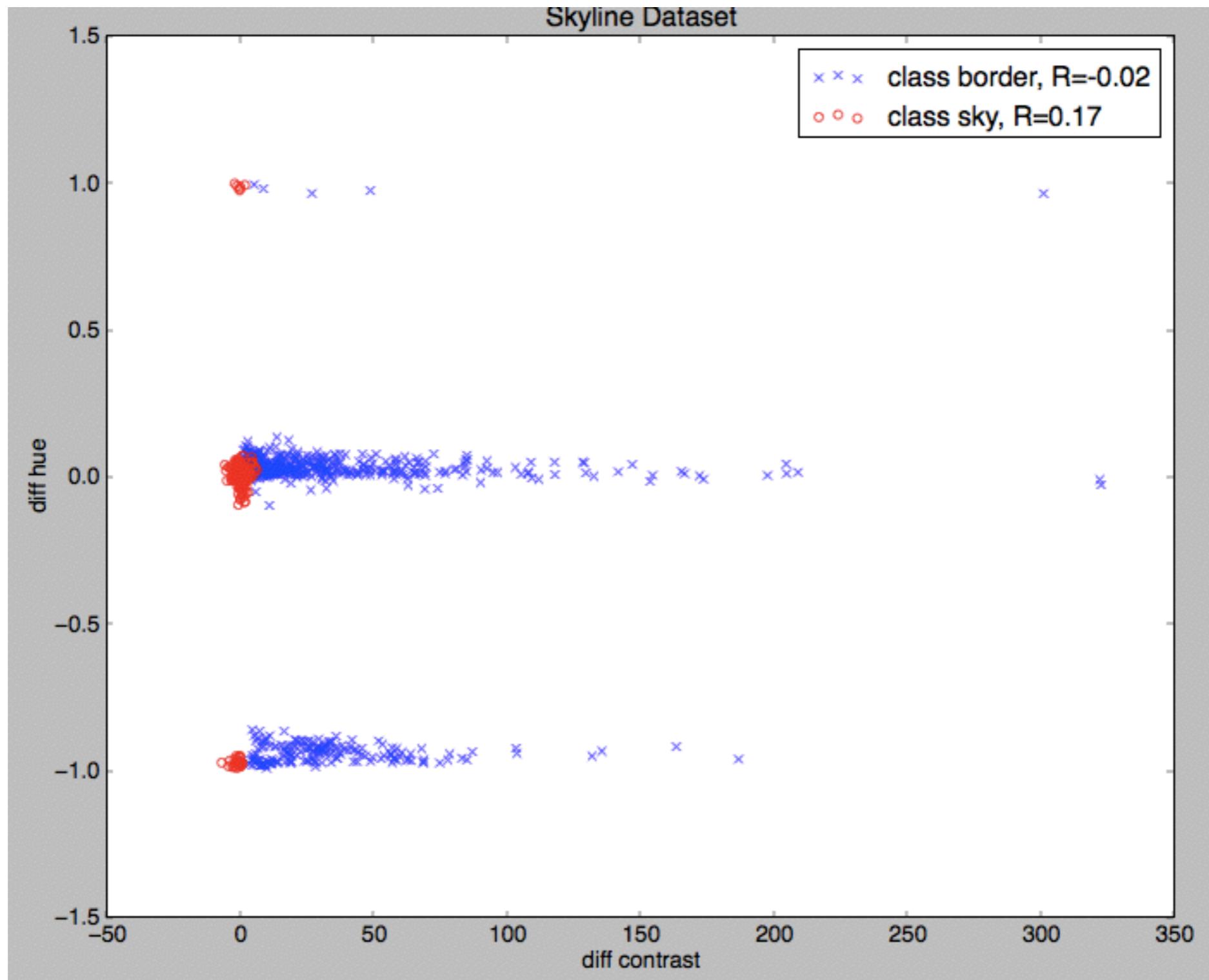


stonehenge test image

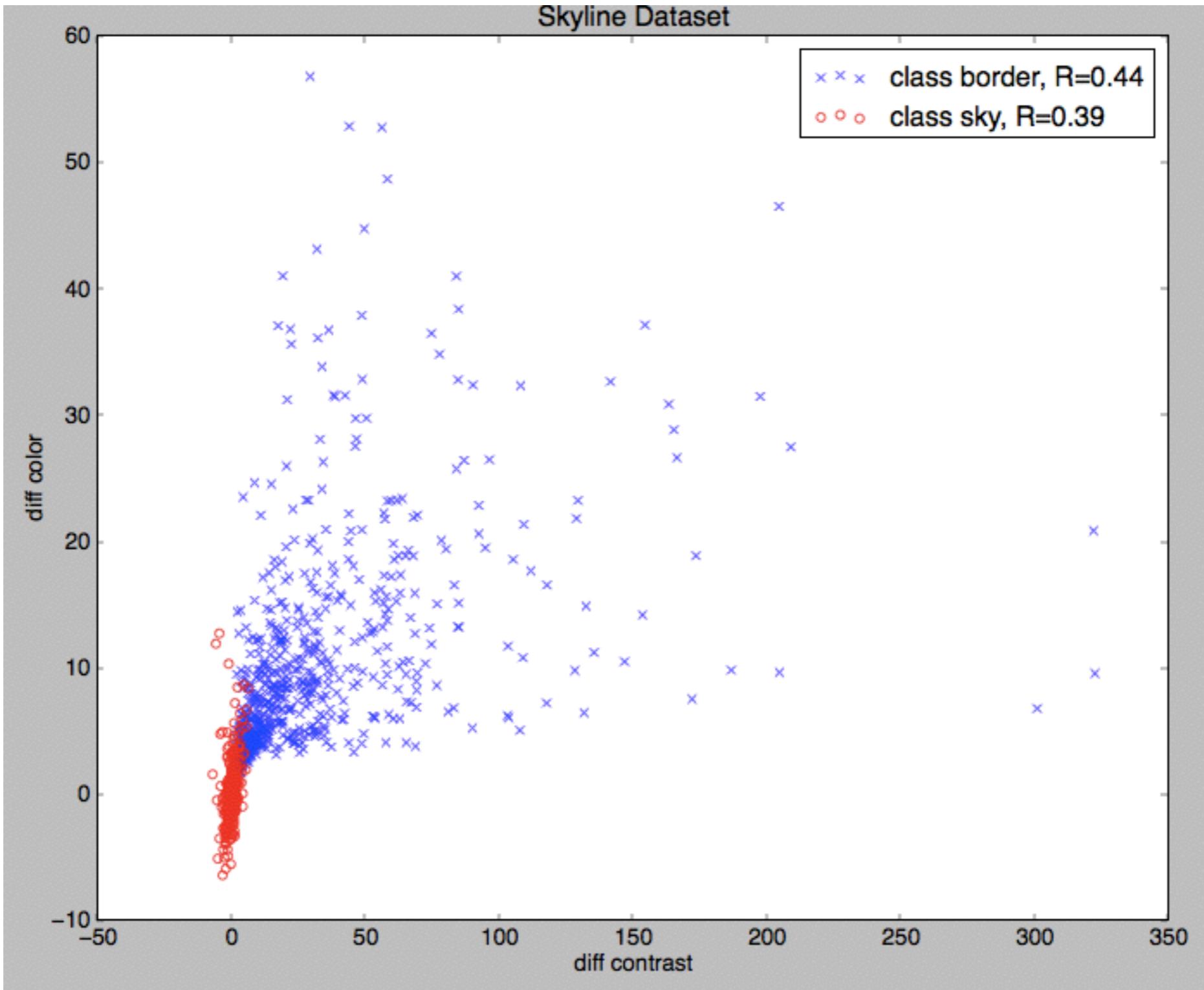
*note: the largest
contrasts
were removed
from analysis
for plot visibility



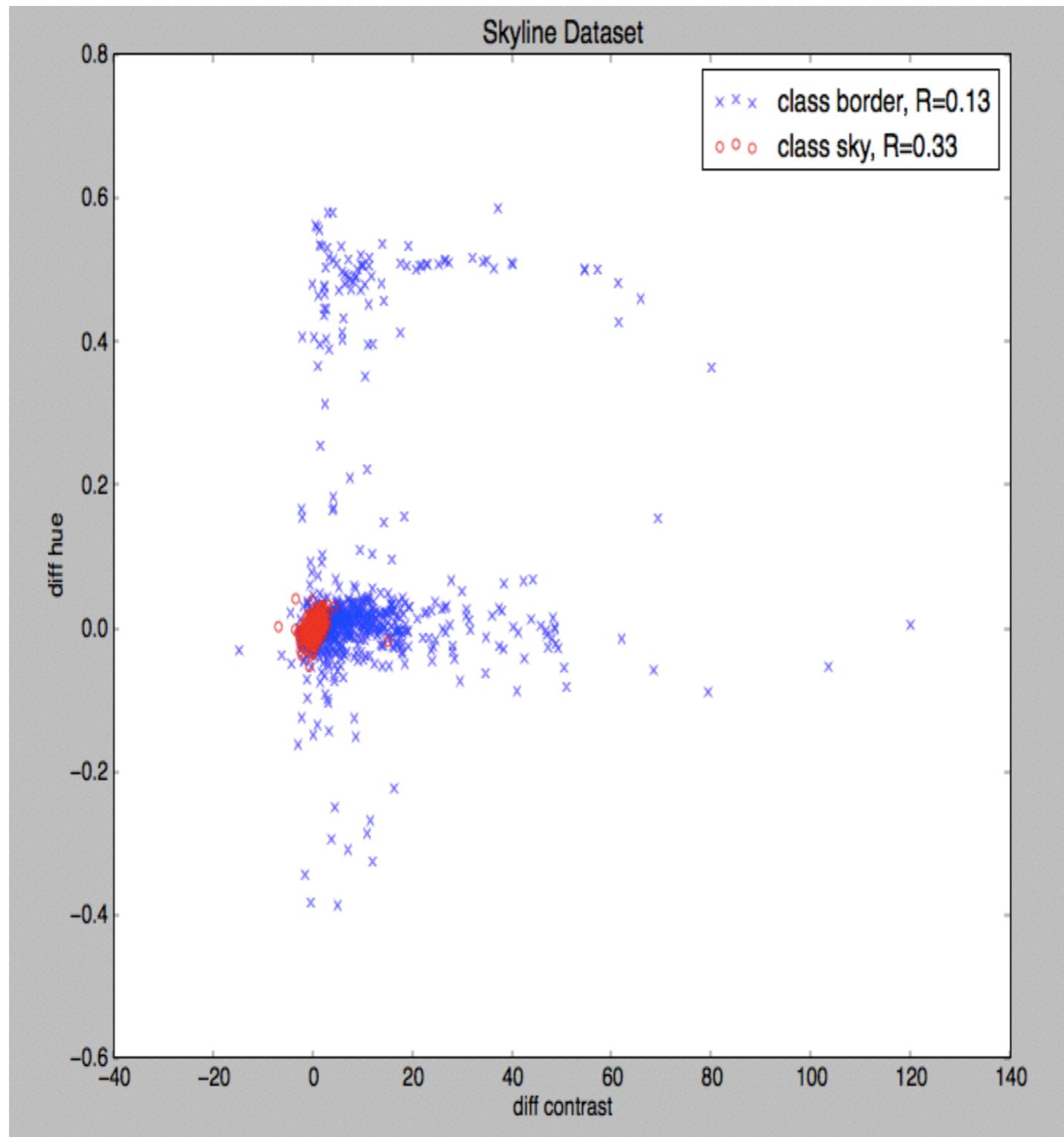
stonehenge test image



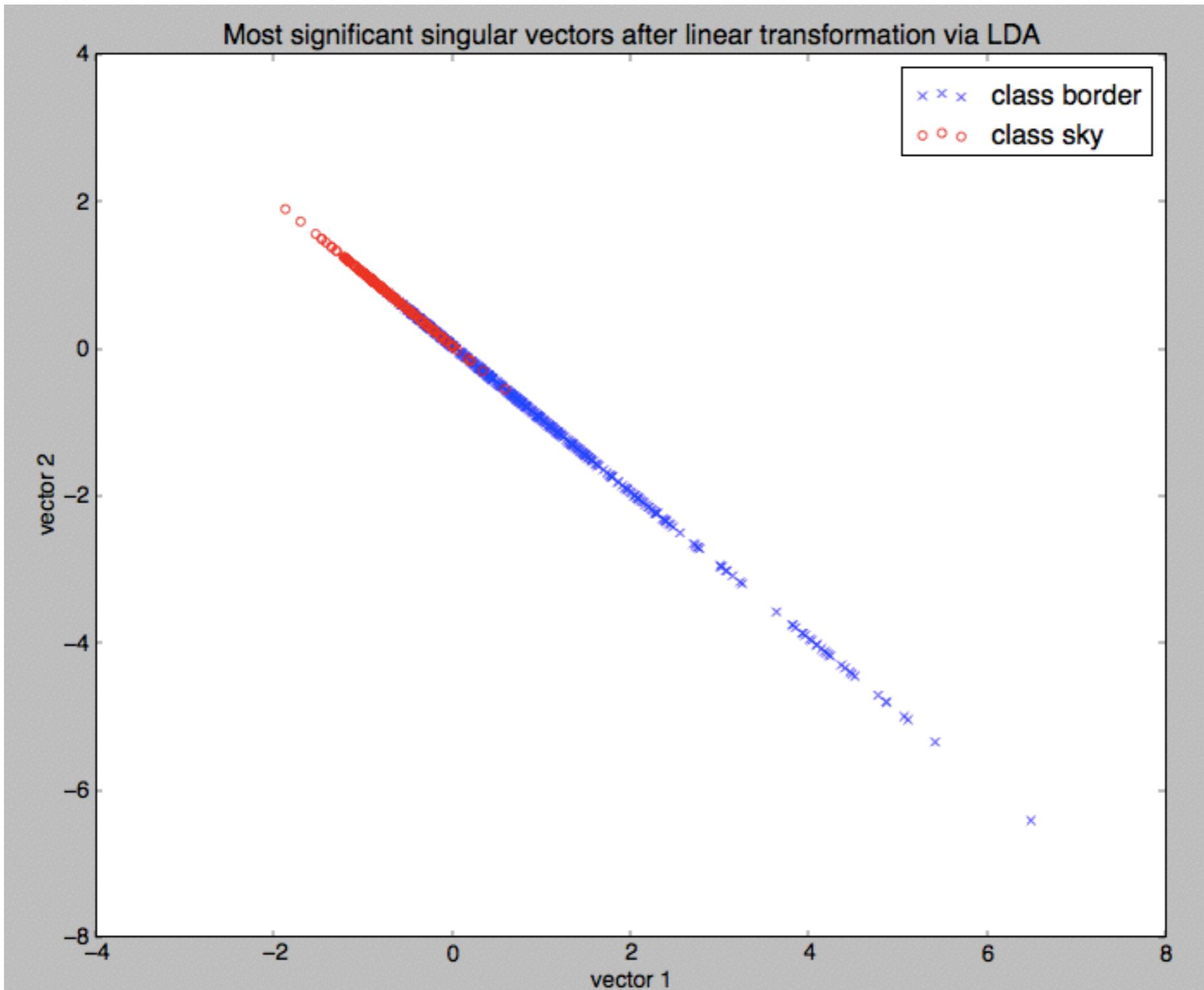
stonehenge test image



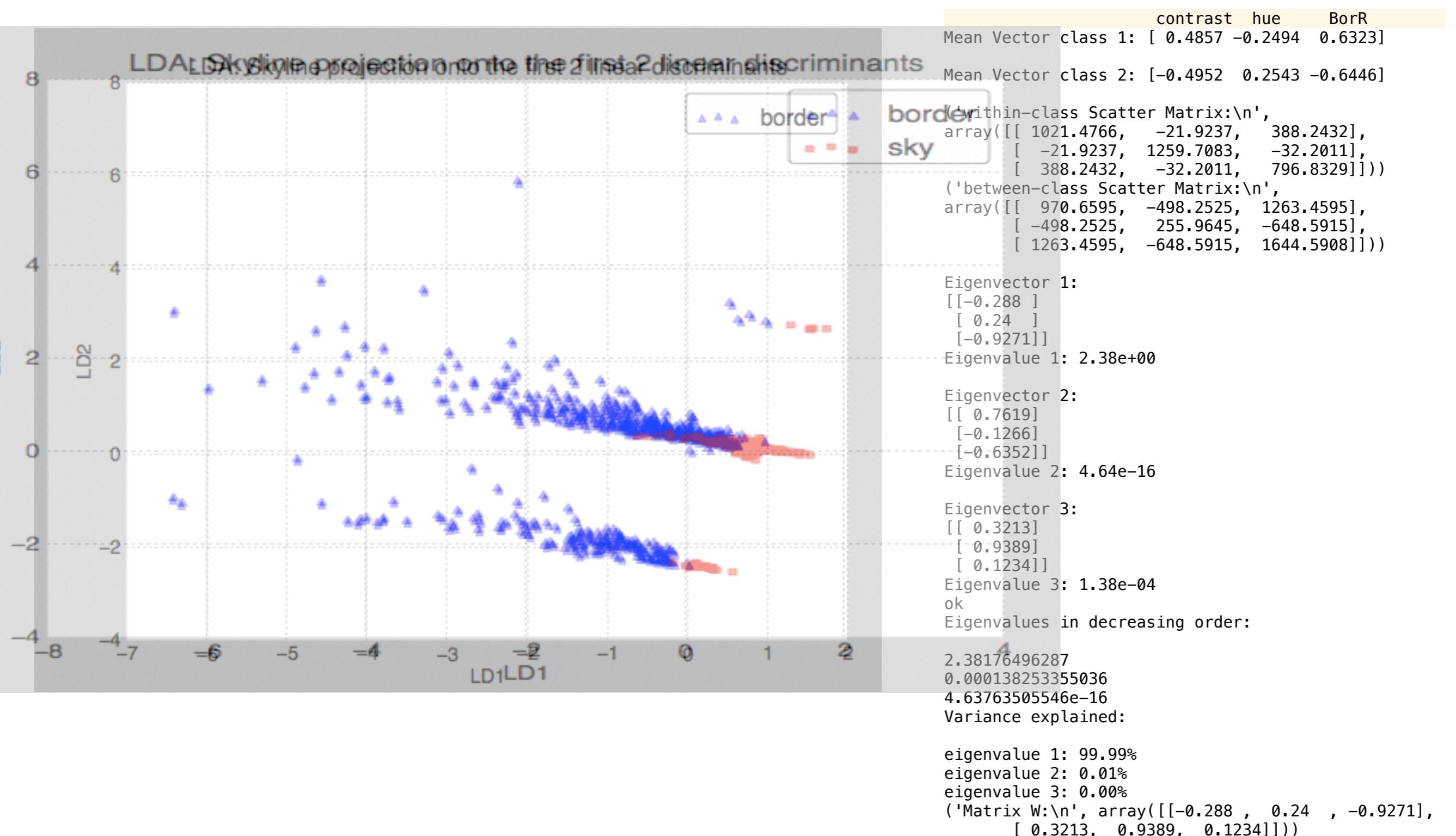
stonehenge test image



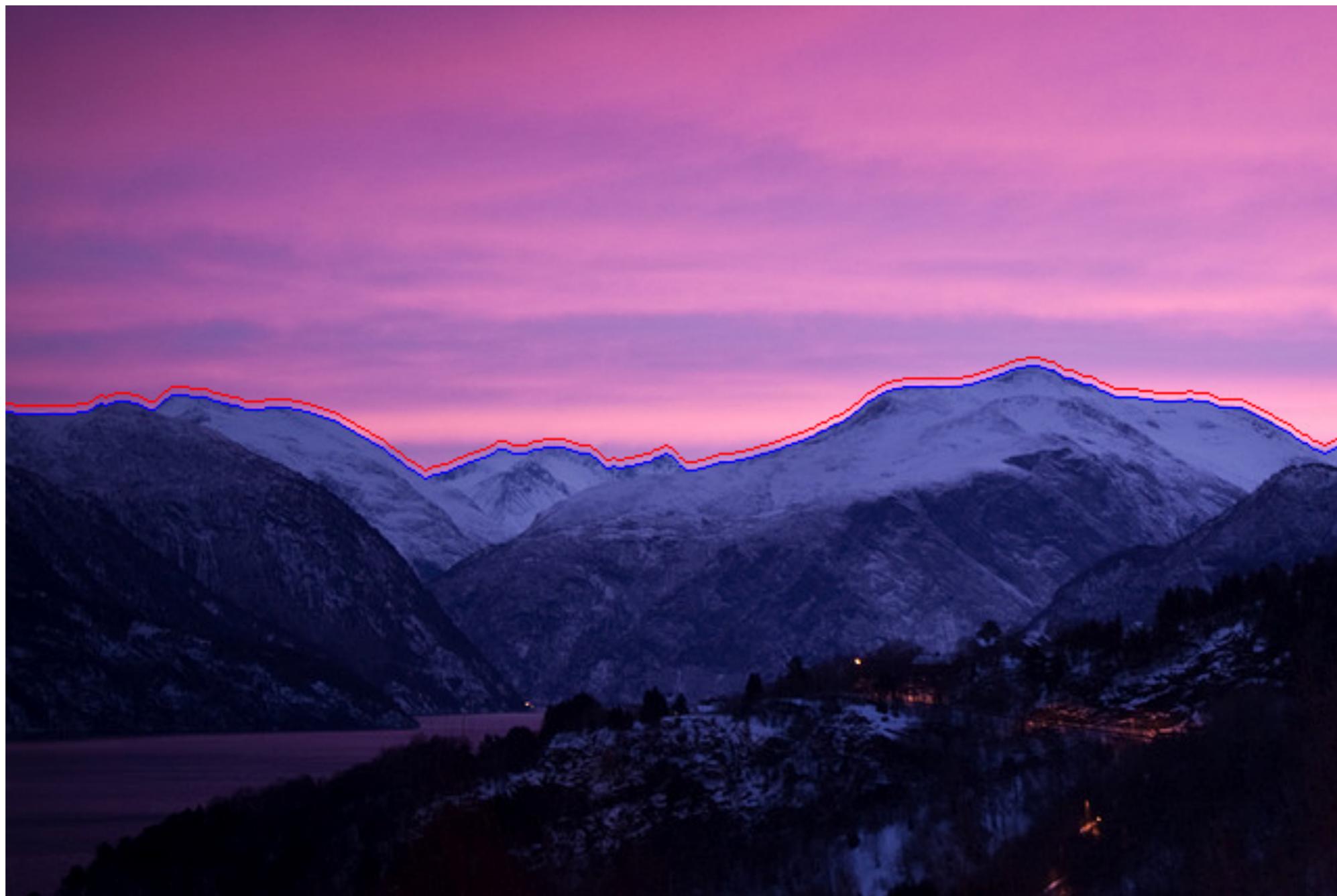
stonehenge test image



cloudy san jose test image

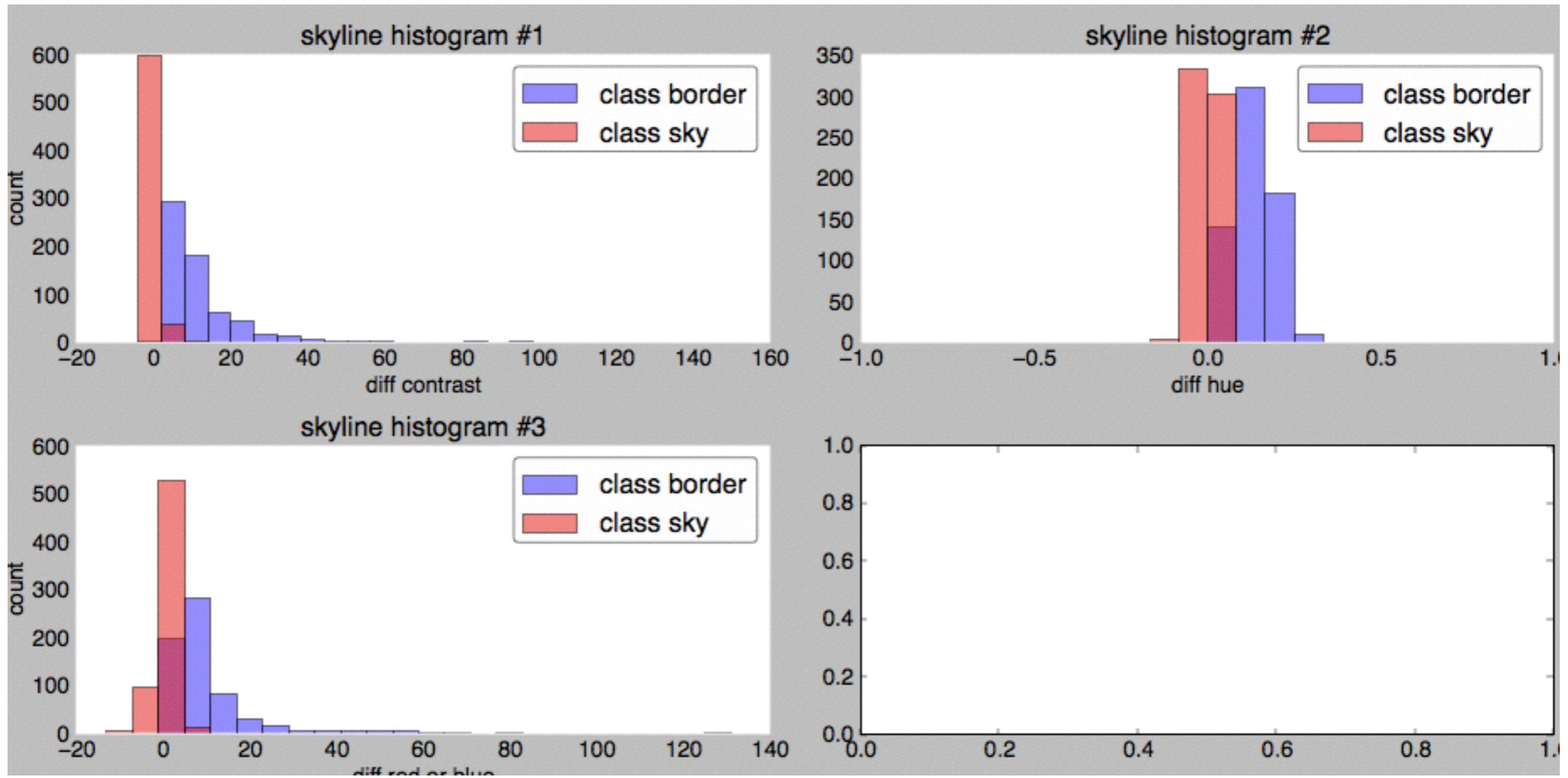


norwegian mtn range test image

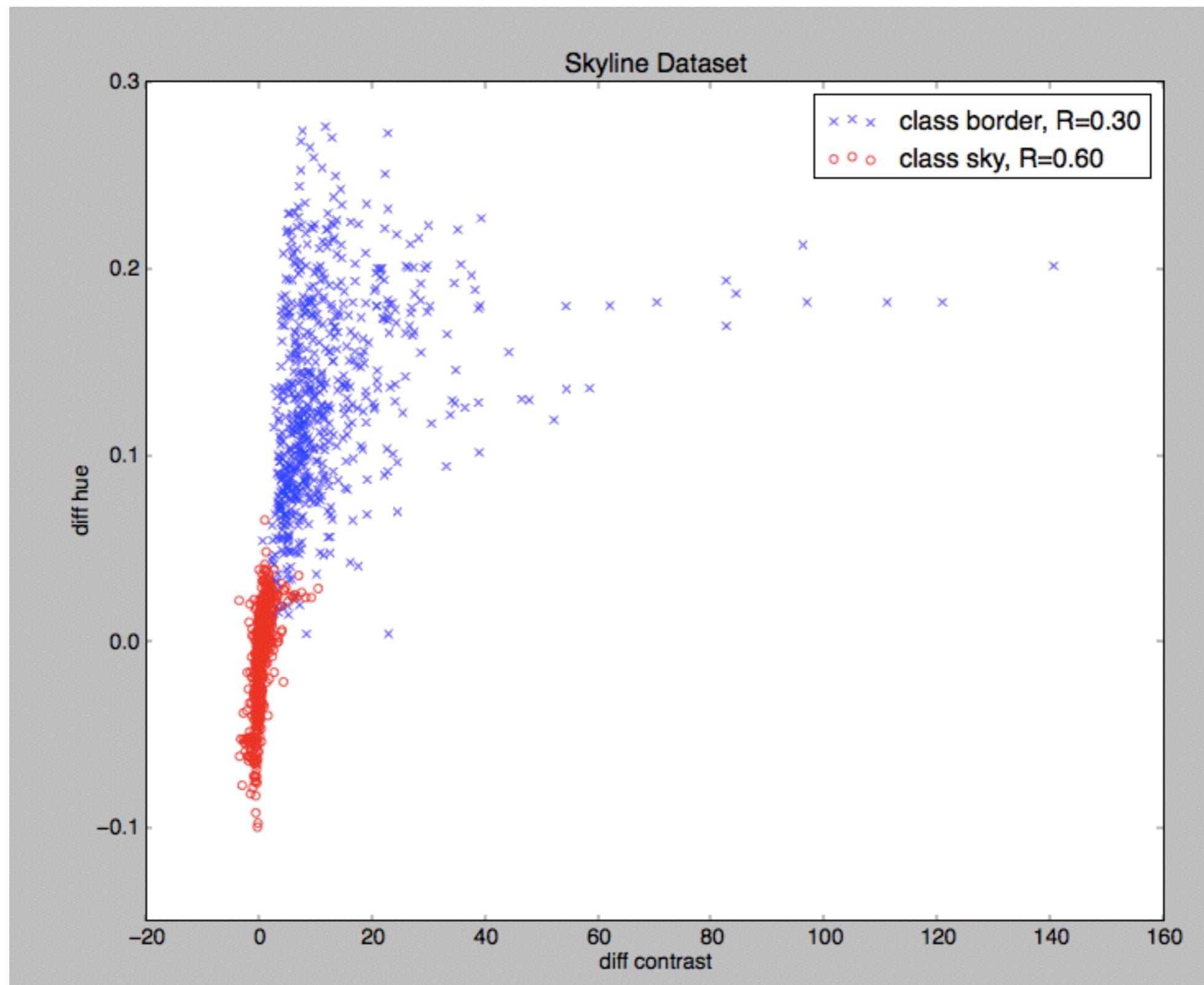


norwegian mtn range test image

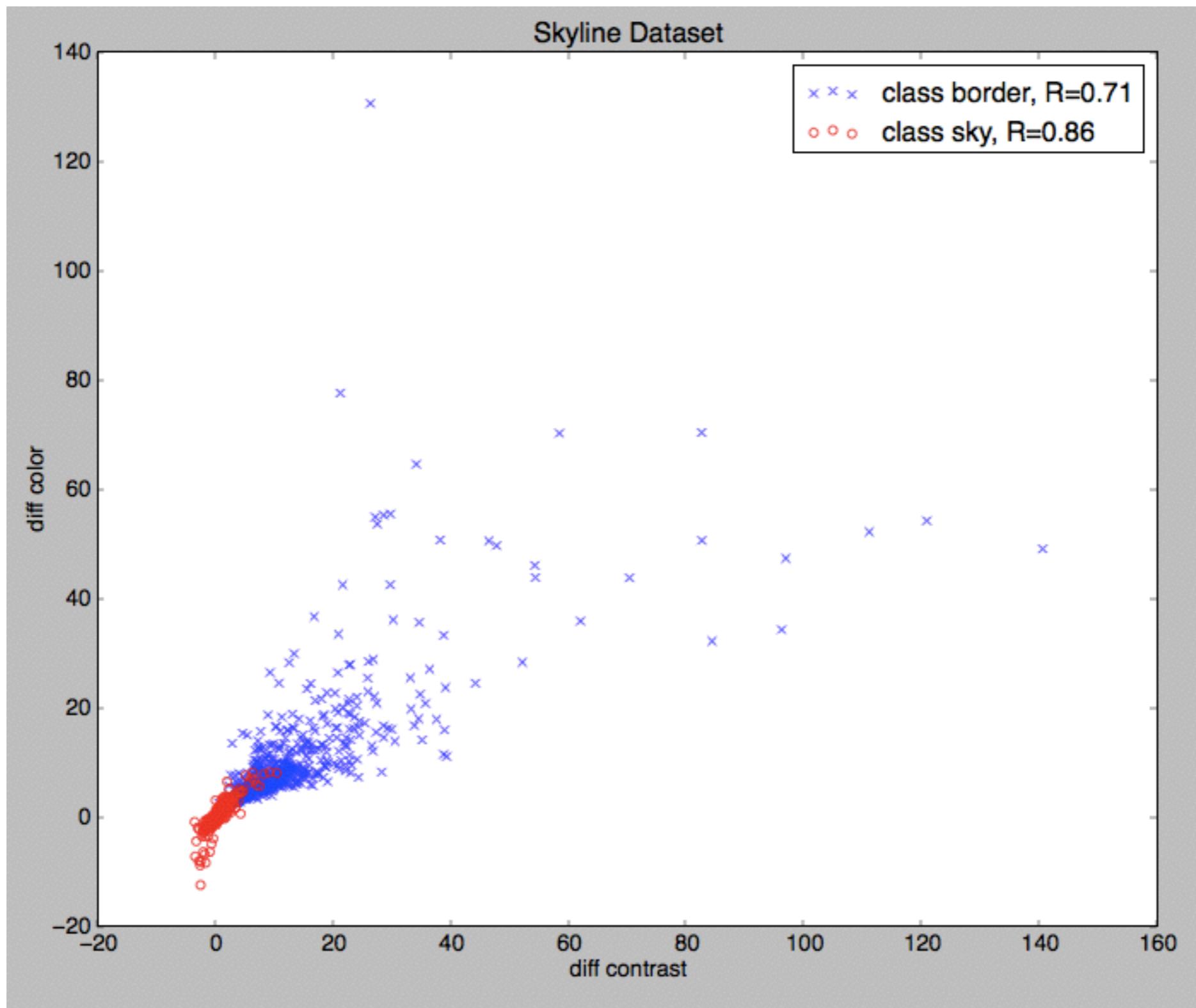
*note: the largest
contrasts
were removed
from analysis
for plot visibility



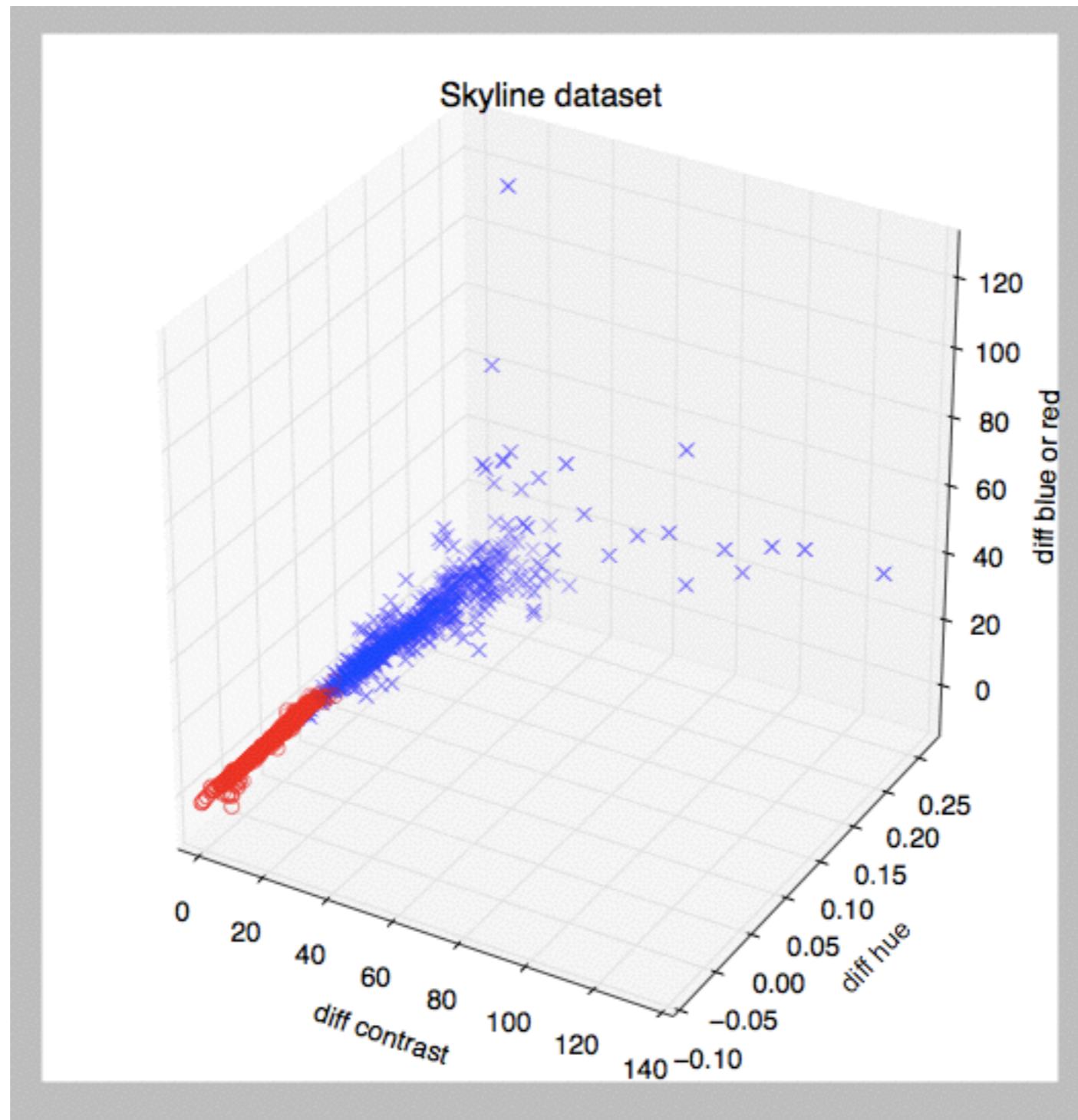
norwegian mtn range test image



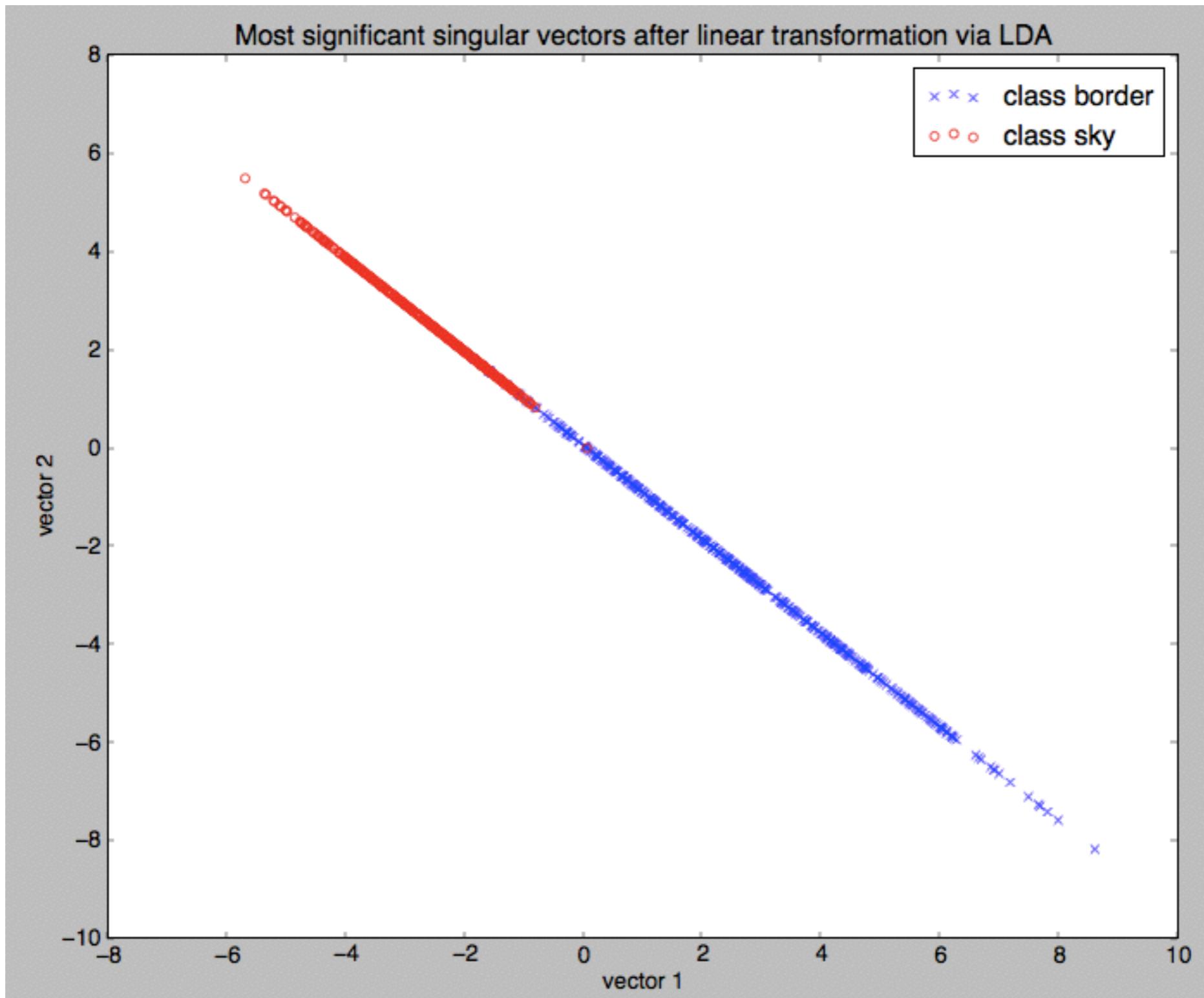
norwegian mtn range test image



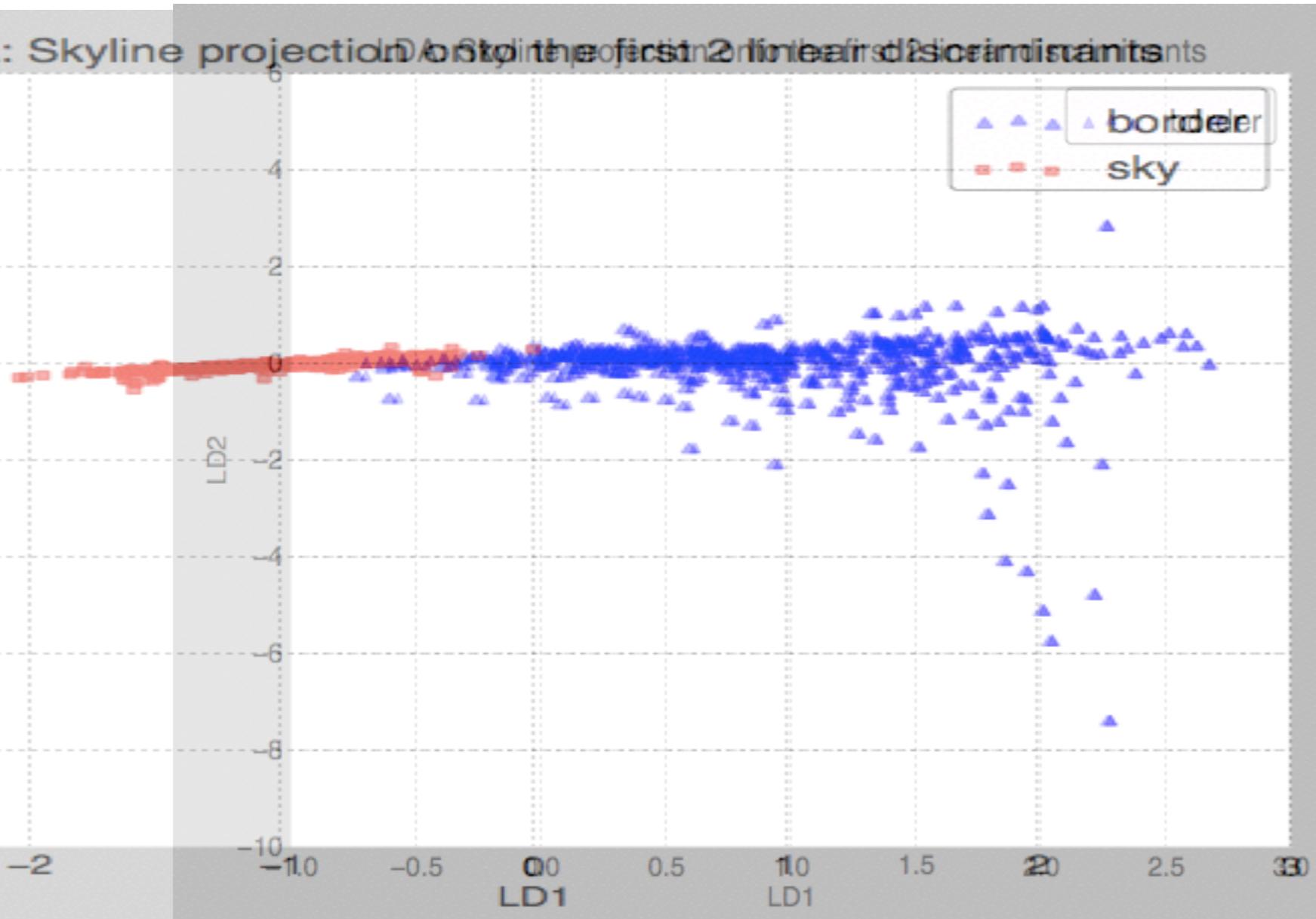
norwegian mtn range test image



norwegian mtn range test image



norwegian mtn range test image



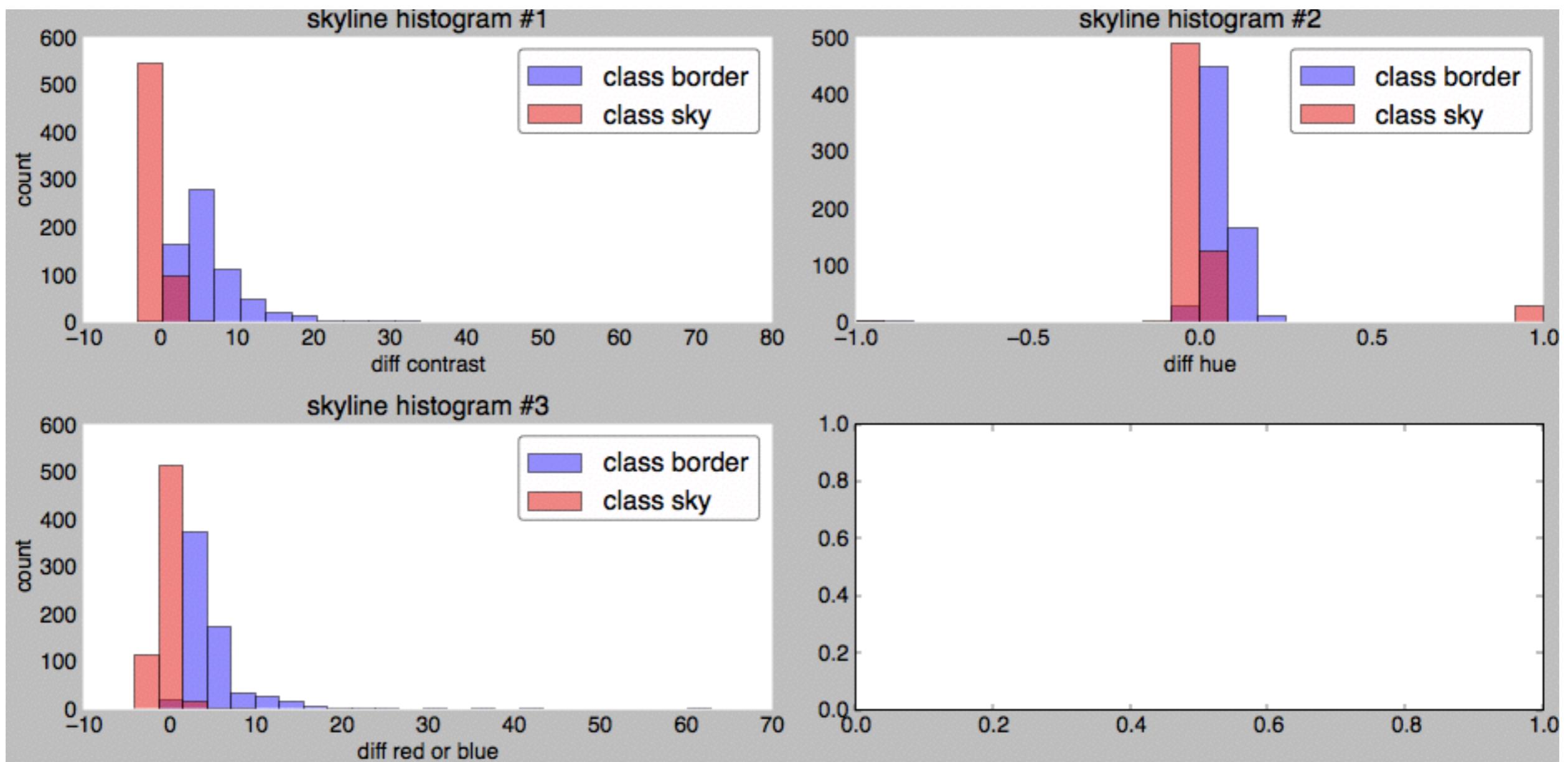
	contrast	hue	BorR
Mean Vector class 1:	[0.532	0.8454	0.5258]
Mean Vector class 2:	[-0.532	-0.8454	-0.5258]
'within-class Scatter Matrix:\n',			
array([[917.7271,	171.4775,	652.0411],	
[171.4775,	365.1207,	153.523],	
[652.0411,	153.523 ,	926.0844]])	
'between-class Scatter Matrix:\n',			
array([[1086.8187,	1727.1143,	1074.2097],	
[1727.1143,	2744.6379,	1707.0766],	
[1074.2097,	1707.0766,	1061.7469]])	
Eigenvector 1:			
[[0.0203]			
[0.997]			
[0.0749]]			
Eigenvalue 1:	7.65e+00		
Eigenvector 2:			
[[-0.8529]			
[0.2526]			
[0.4568]]			
Eigenvalue 2:	-3.80e-16		
Eigenvector 3:			
[[0.6005]			
[-0.6593]			
[0.4525]]			
Eigenvalue 3:	2.64e-16		
ok			
Eigenvalues in decreasing order:			
7.64994769908			
3.79939460534e-16			
2.63875429893e-16			
Variance explained:			
eigenvalue 1: 100.00%			
eigenvalue 2: 0.00%			
eigenvalue 3: 0.00%			
('Matrix W:\n', array([[0.0203, 0.997 , 0.0749],			
[-0.8529, 0.2526, 0.4568]]))			

half dome test image

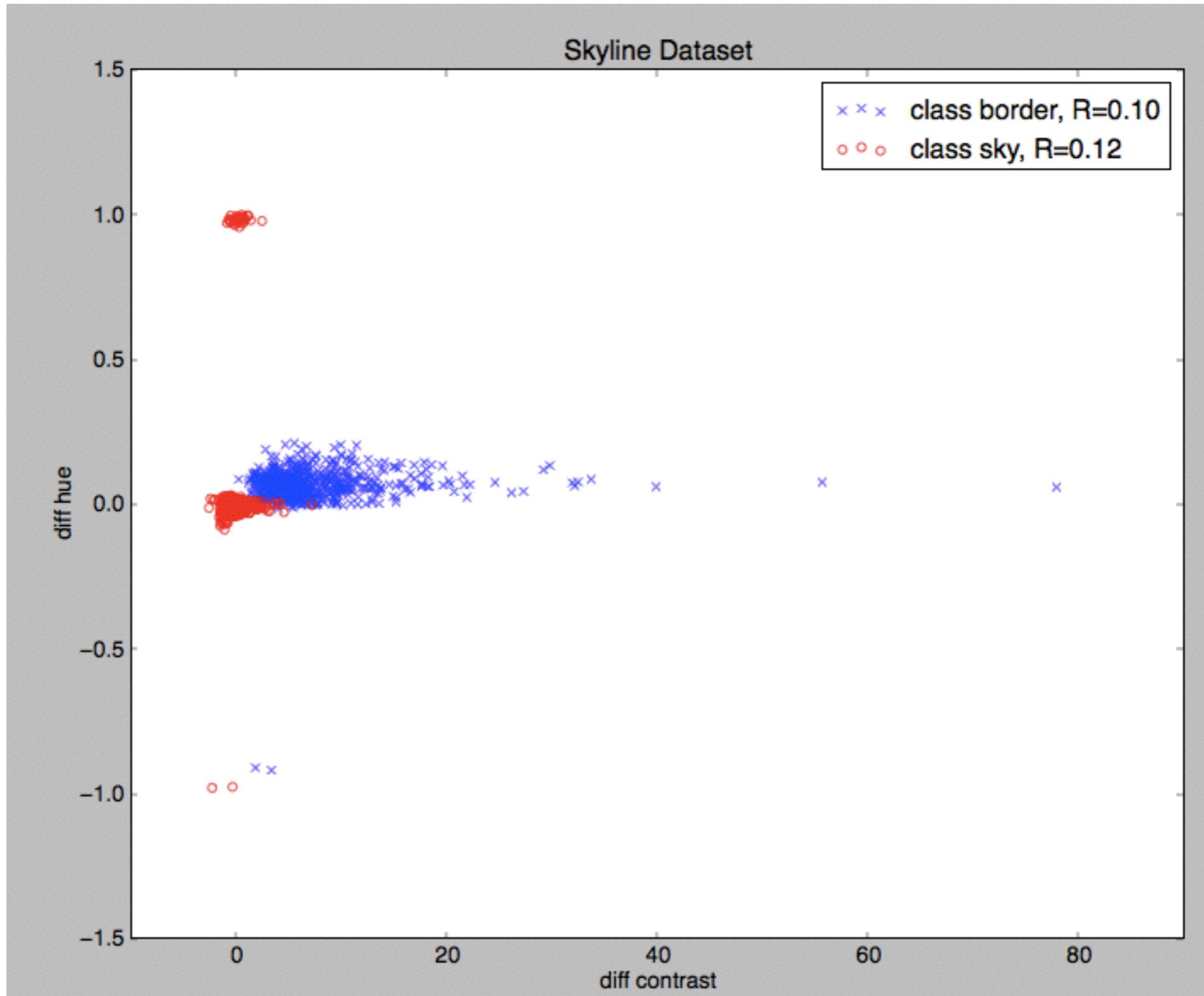


half dome test image

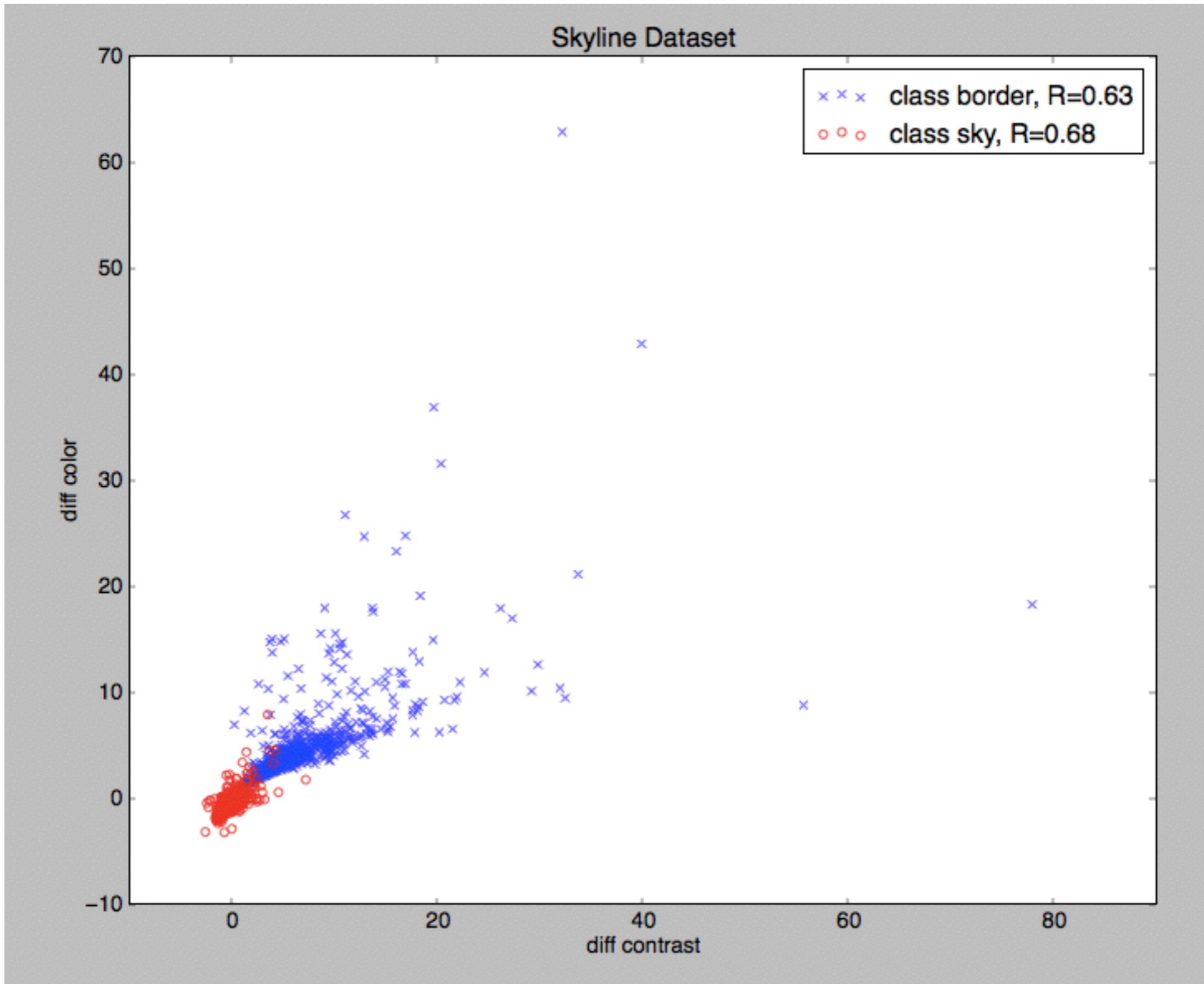
*note: the largest contrasts were removed from analysis for plot visibility



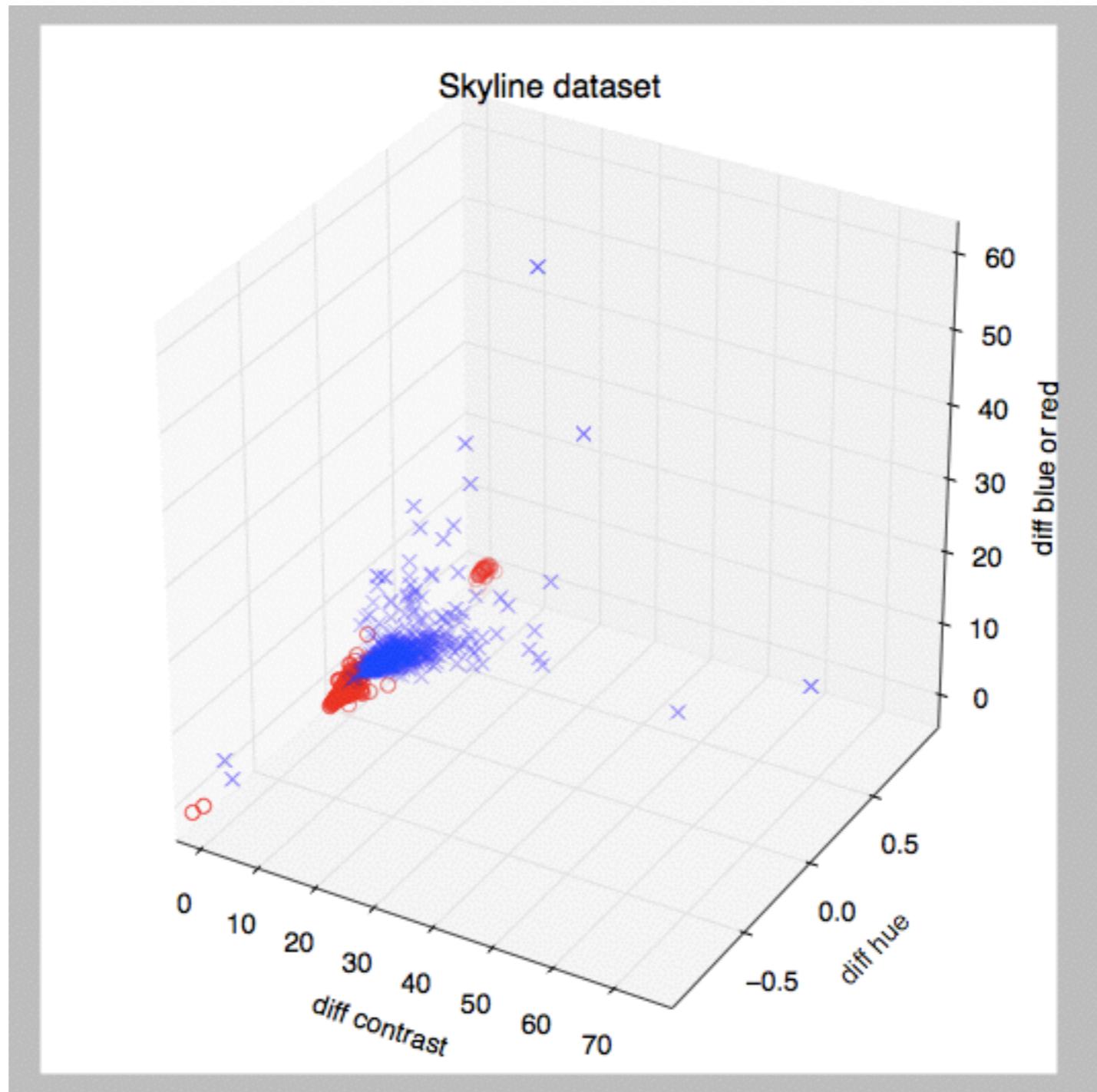
half dome test image



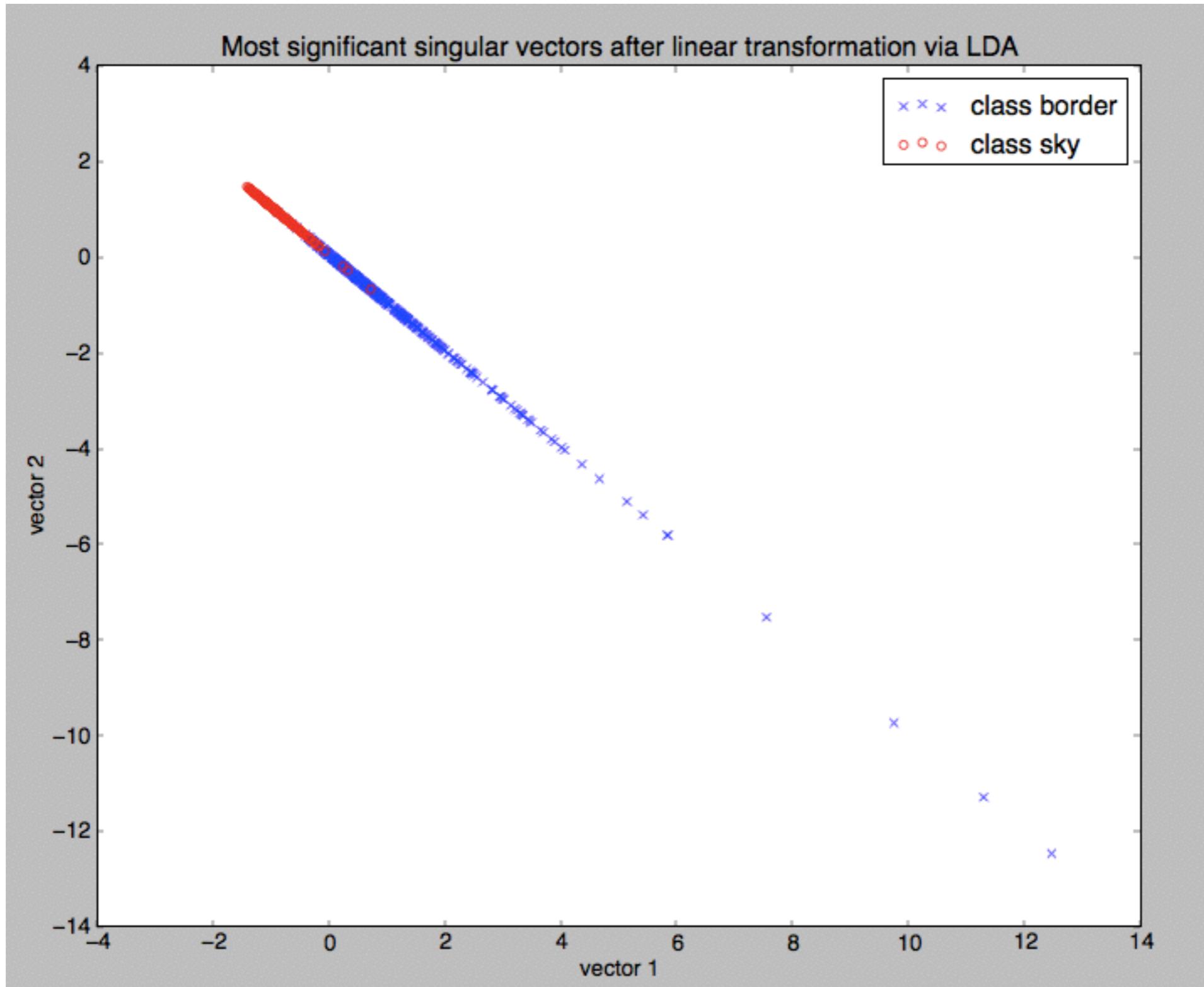
half dome test image



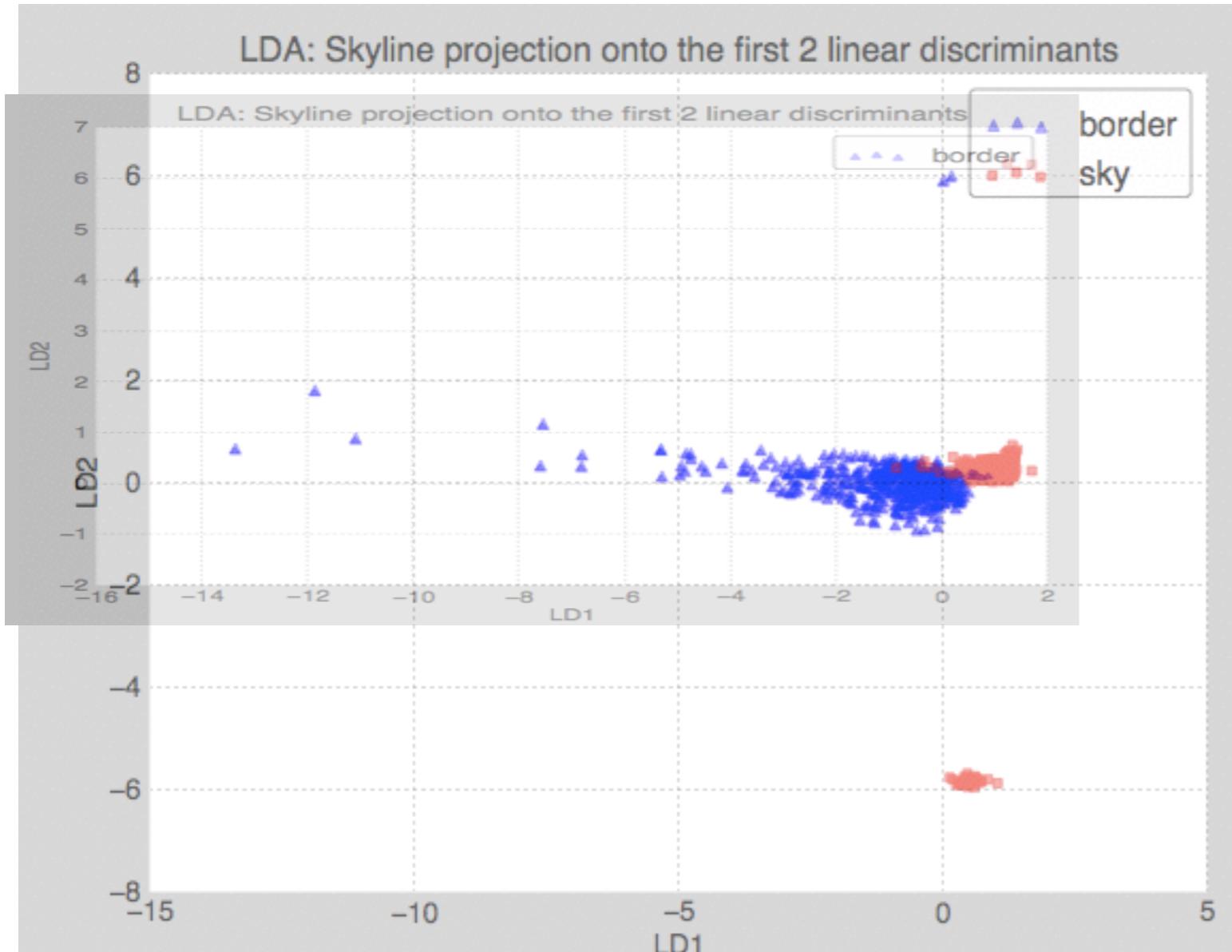
half dome test image



half dome test image



half dome test image

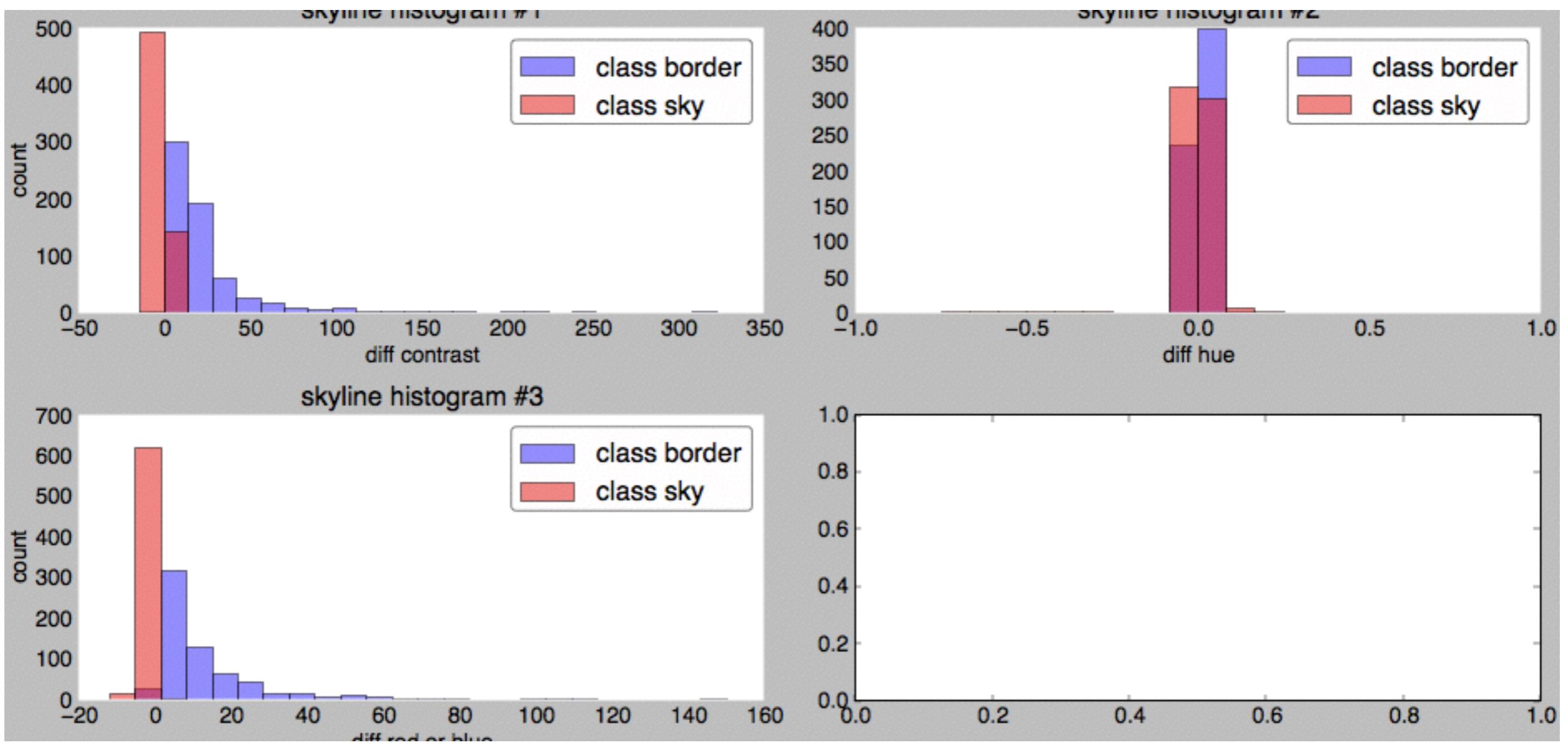


contrast	hue	BorR
Mean Vector class 1: [0.6417 0.0902 0.642]		
Mean Vector class 2: [-0.6496 -0.0913 -0.6499]		
('within-class Scatter Matrix:\n', array([[761.5521, 44.8379, 477.9533], [44.8379, 1295.2502, 5.0539], [477.9533, 5.0539, 761.1327]]))		
('between-class Scatter Matrix:\n', array([[1633.3849, 229.5507, 1634.0138], [229.5507, 32.2908, 229.6391], [1634.0138, 229.6391, 1634.6431]]))		
Eigenvector 1: [[-0.6996], [-0.068], [-0.7113]]		
Eigenvalue 1: 2.65e+00		
Eigenvector 2: [[-7.0727e-01], [3.1674e-04], [7.0695e-01]]		
Eigenvalue 2: 3.25e-16		
Eigenvector 3: [[0.138], [-0.9904], [0.0012]]		
Eigenvalue 3: 2.35e-05		
ok		
Eigenvalues in decreasing order:		
2.6497347051		
2.34976030589e-05		
3.24516324072e-16		
Variance explained:		
eigenvalue 1: 100.00%		
eigenvalue 2: 0.00%		
eigenvalue 3: 0.00%		
('Matrix W:\n', array([[-0.6996, -0.068 , -0.7113], [0.138 , -0.9904, 0.0012]]))		

costa rica test image

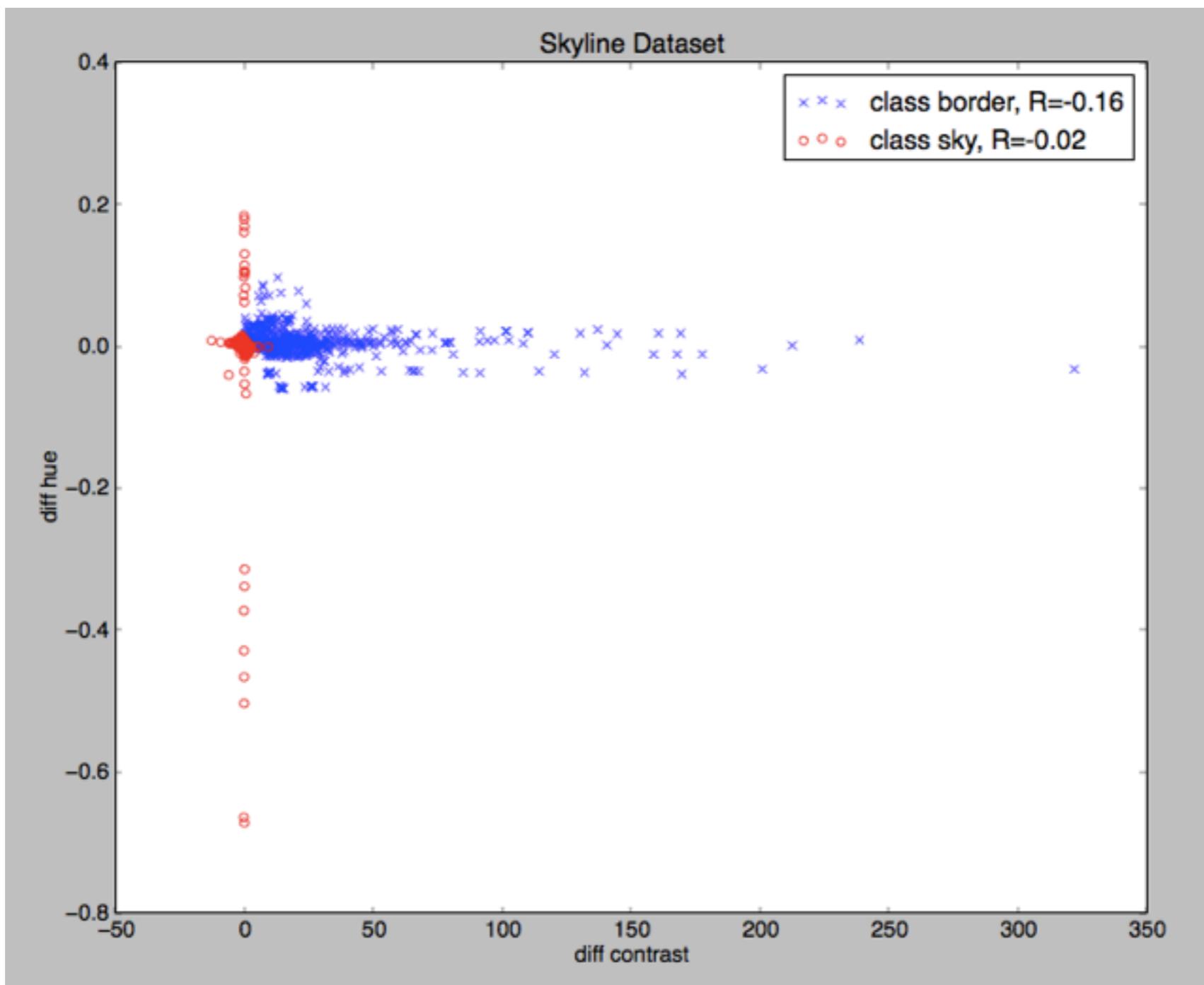


costa rica test image

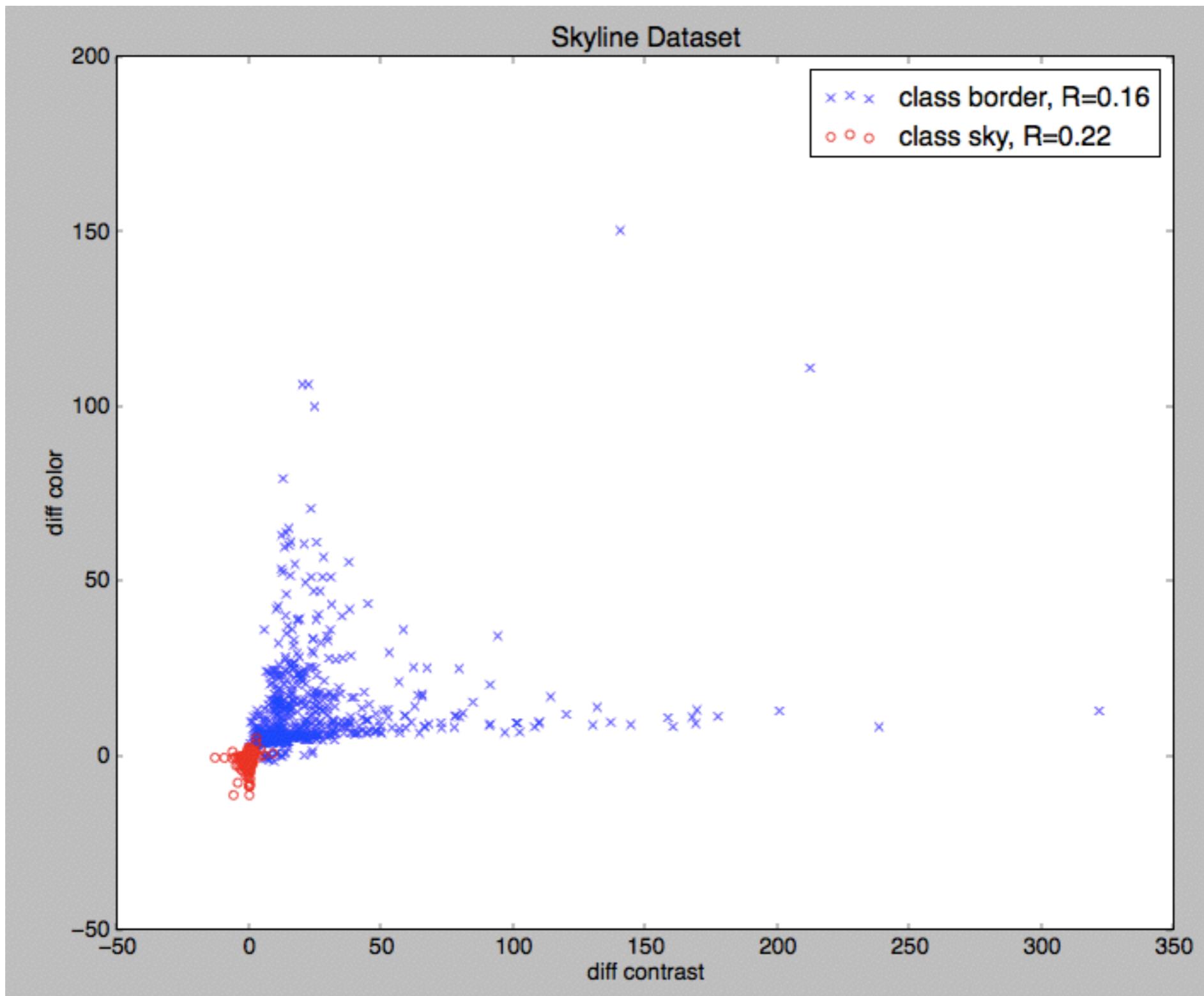


costa rica test image

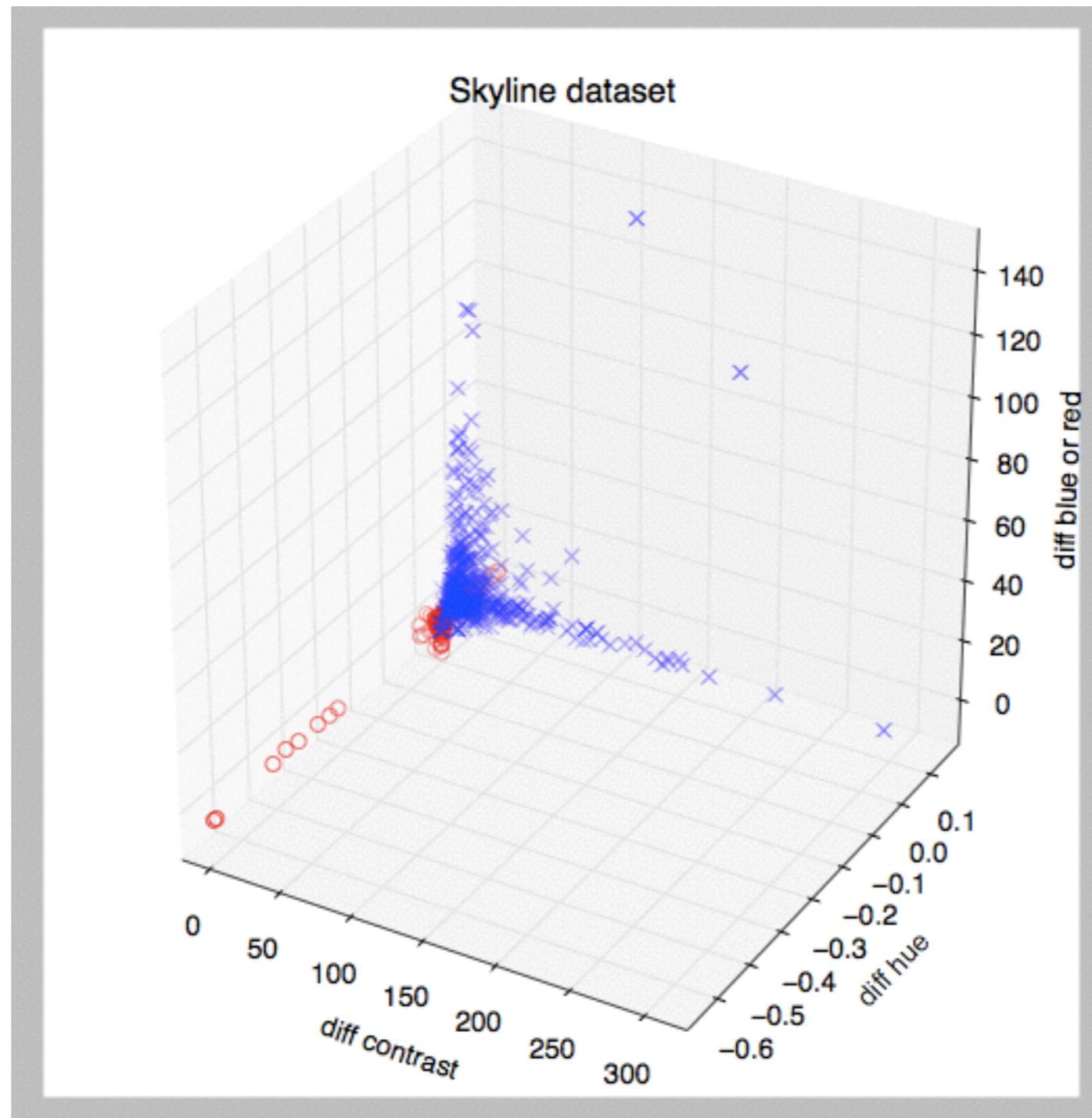
*note: the largest
contrasts
were removed
from analysis
for plot visibility



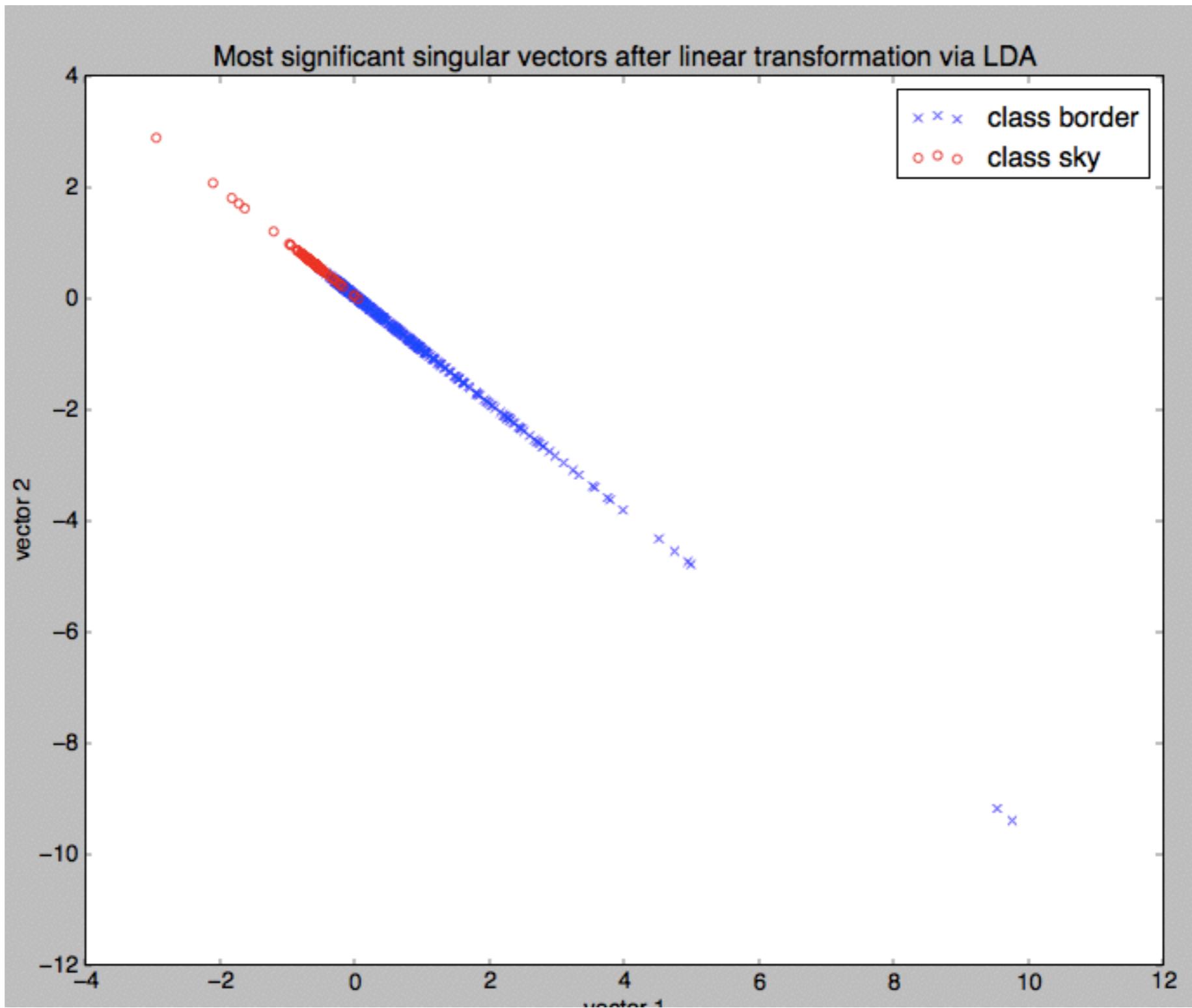
costa rica test image



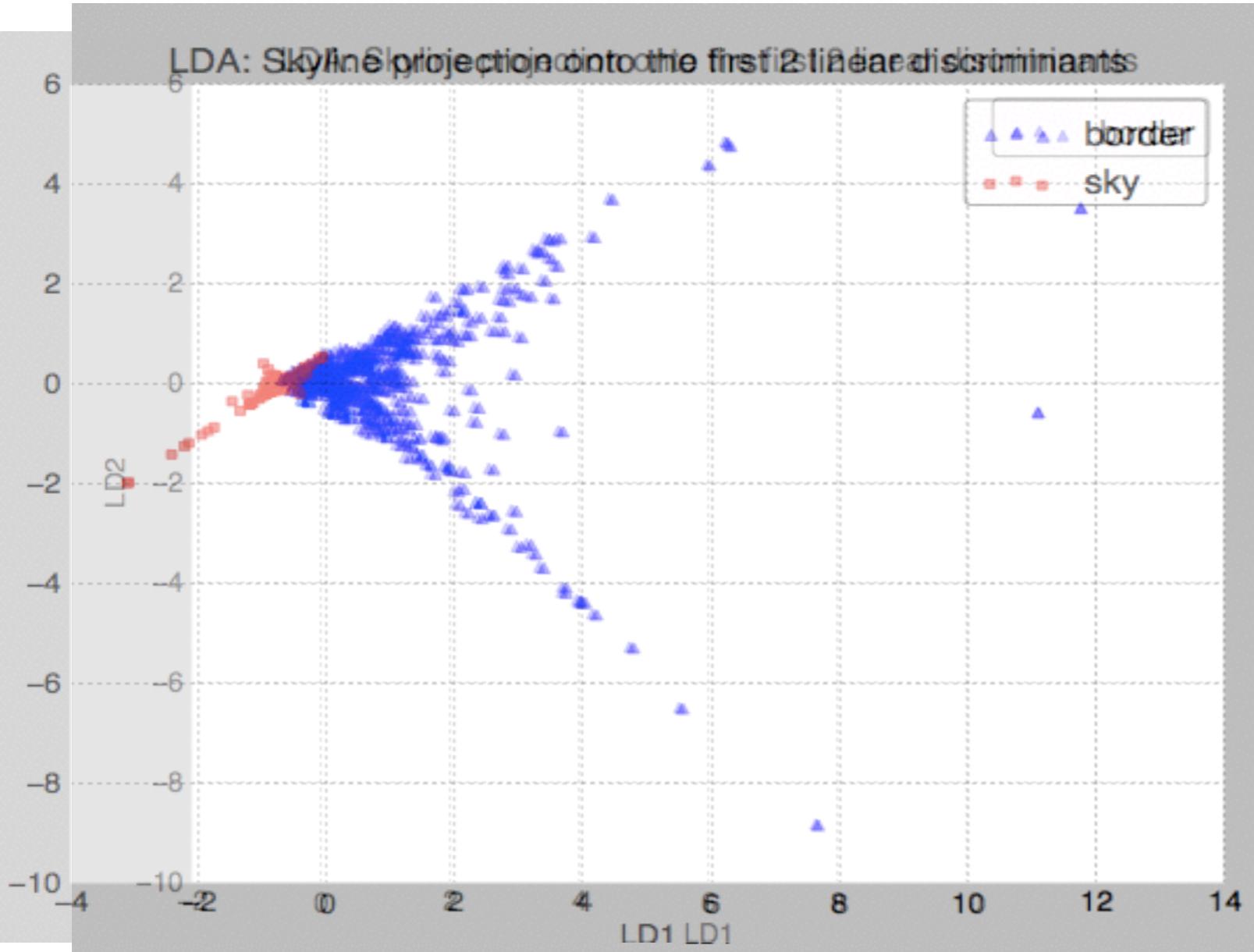
costa rica test image



costa rica test image



costa rica test image



contrast	hue	BorR
Mean Vector class 1: [0.4859	0.0796	0.5429]
Mean Vector class 2: [-0.4859	-0.0796	-0.5429]

('within-class Scatter Matrix:\n',
array([[973.2139, -57.7232, 150.8659],
[-57.7232, 1265.9211, -60.9599],
[150.8659, -60.9599, 898.4743]]))
('between-class Scatter Matrix:\n',
array([[902.3582, 147.8859, 1008.2539],
[147.8859, 24.2368, 165.241],
[1008.2539, 165.241 , 1126.577]]))

Eigenvector 1:
[[-0.7482]
[0.1301]
[0.6506]]

Eigenvalue 1: -2.22e-16

Eigenvector 2:
[[0.6076]
[0.1558]
[0.7788]]

Eigenvalue 2: 1.94e+00

Eigenvector 3:
[[0.4266]
[-0.8679]
[-0.2545]]

Eigenvalue 3: 0.00e+00

ok

Eigenvalues in decreasing order:

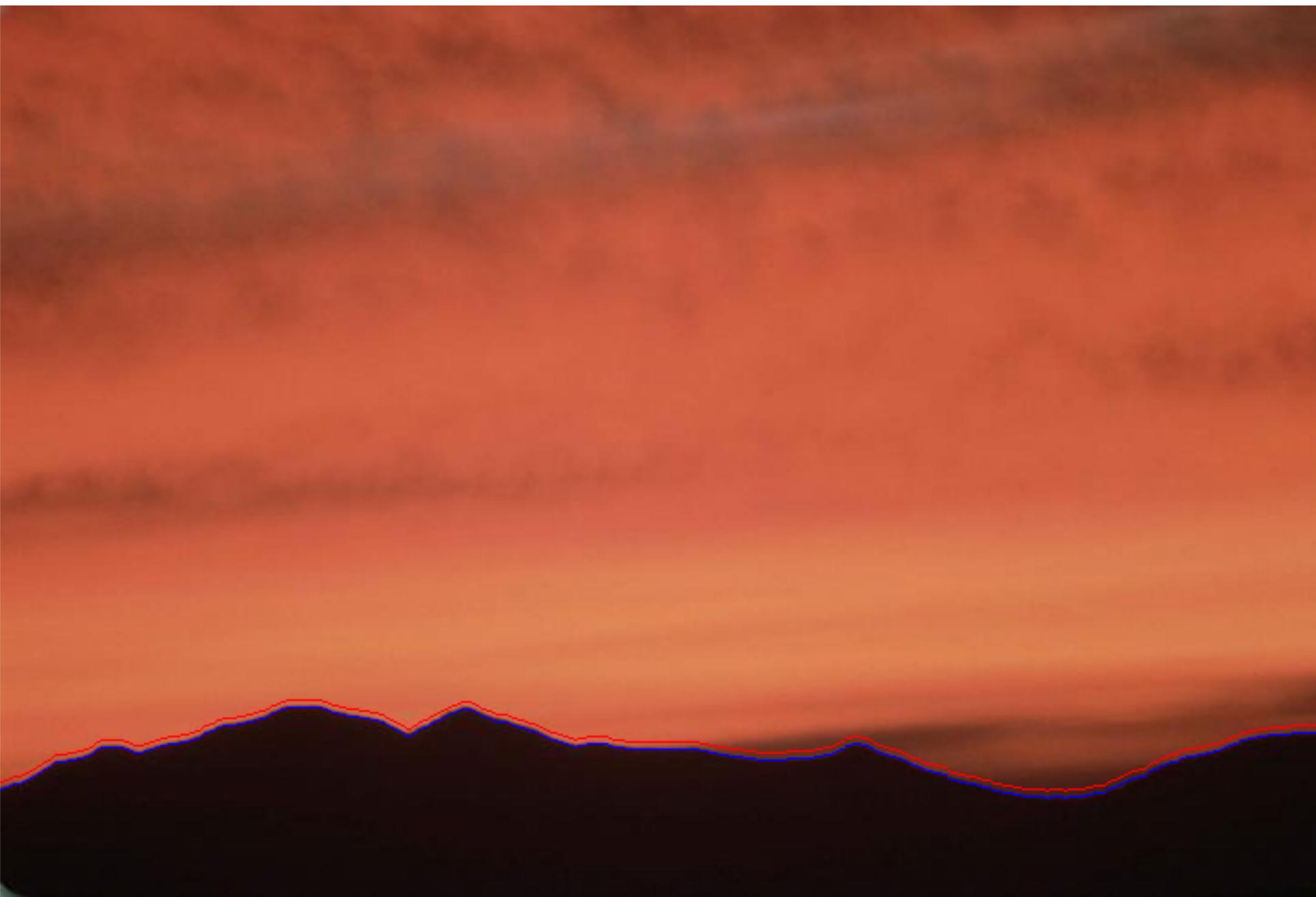
1.93847827798
2.22044604925e-16
0.0

Variance explained:

eigenvalue 1: 100.00%
eigenvalue 2: 0.00%
eigenvalue 3: 0.00%

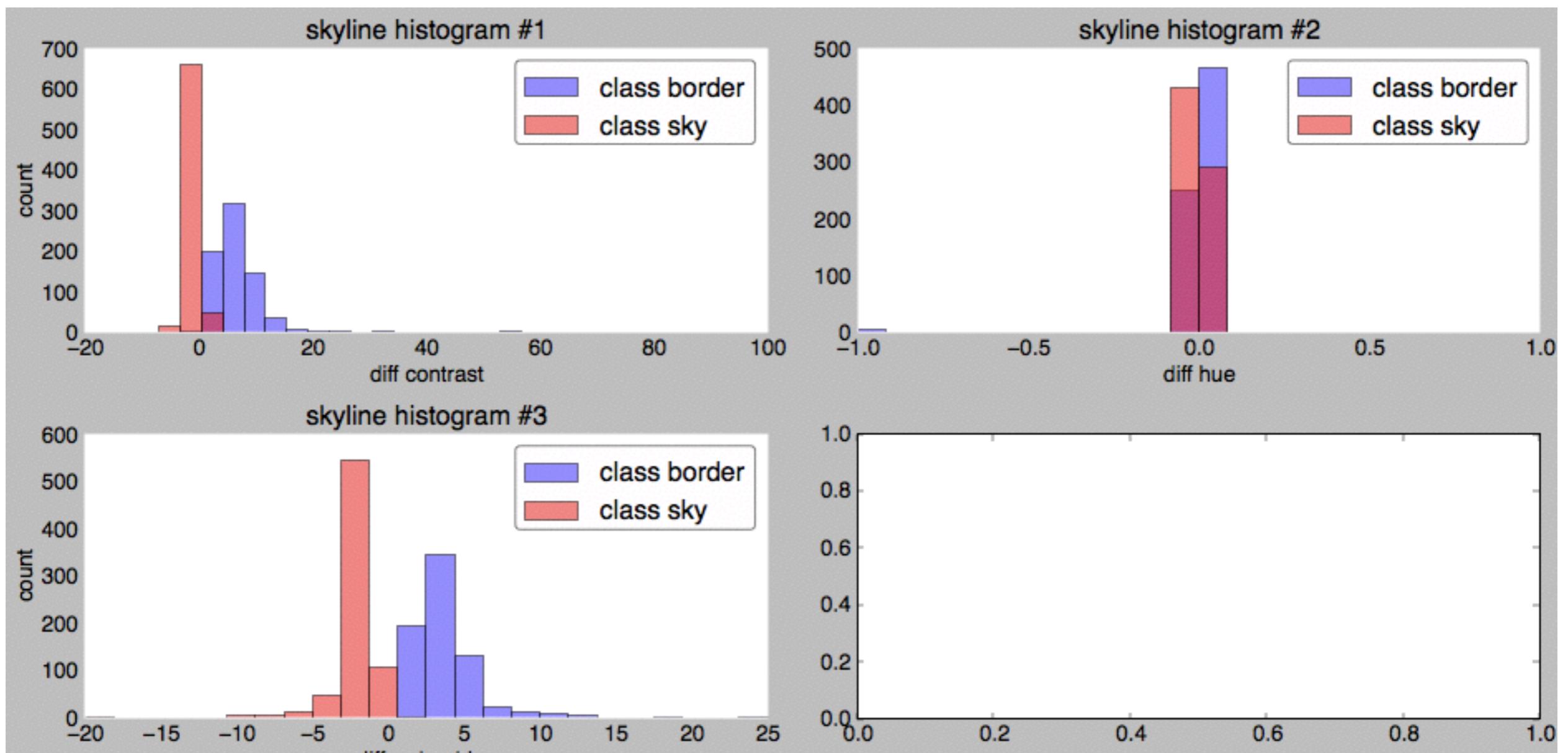
('Matrix W:\n', array([[0.6076, 0.1558, 0.7788],
[-0.7482, 0.1301, 0.6506]]))

new mexico test image

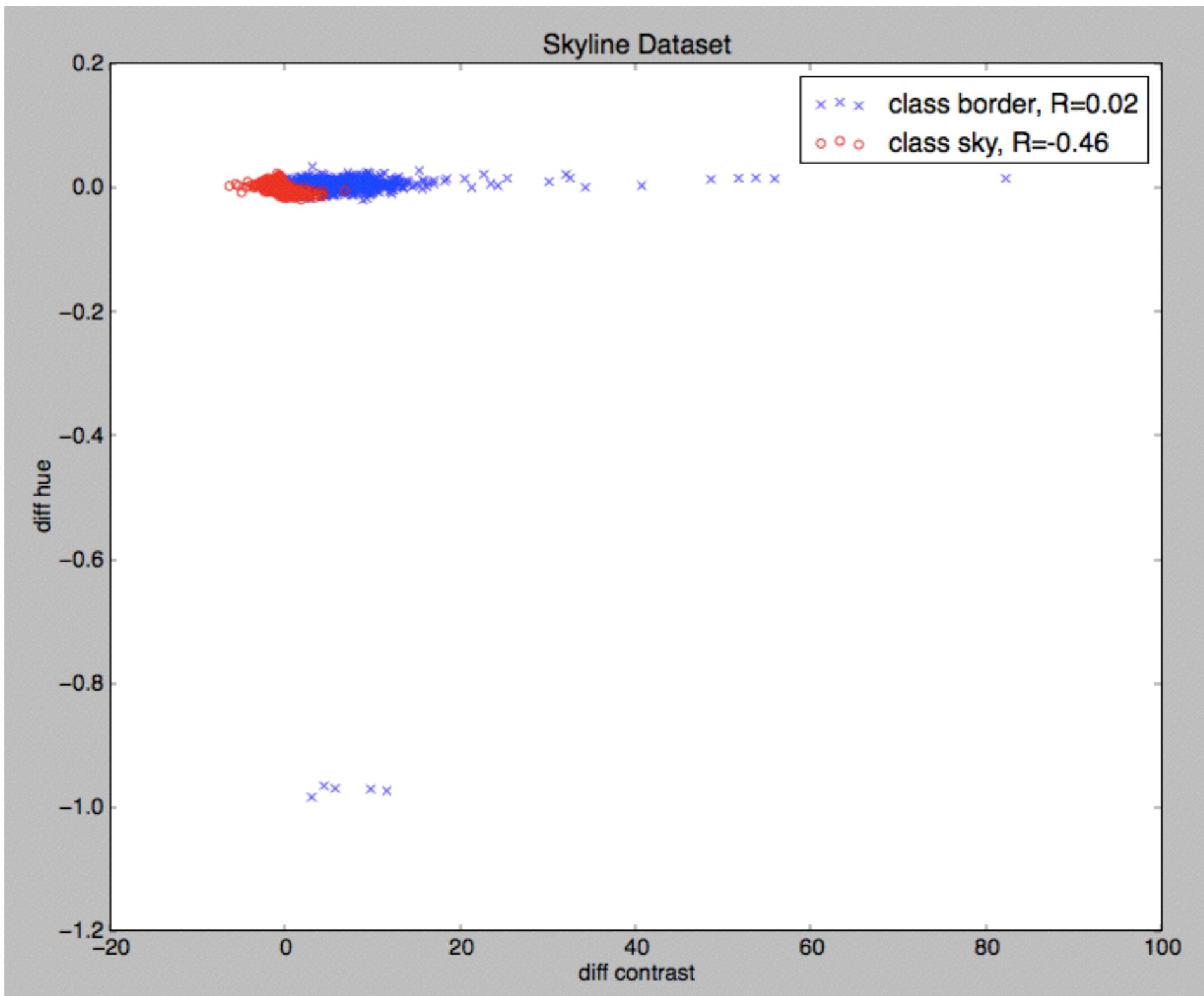


new mexico test image

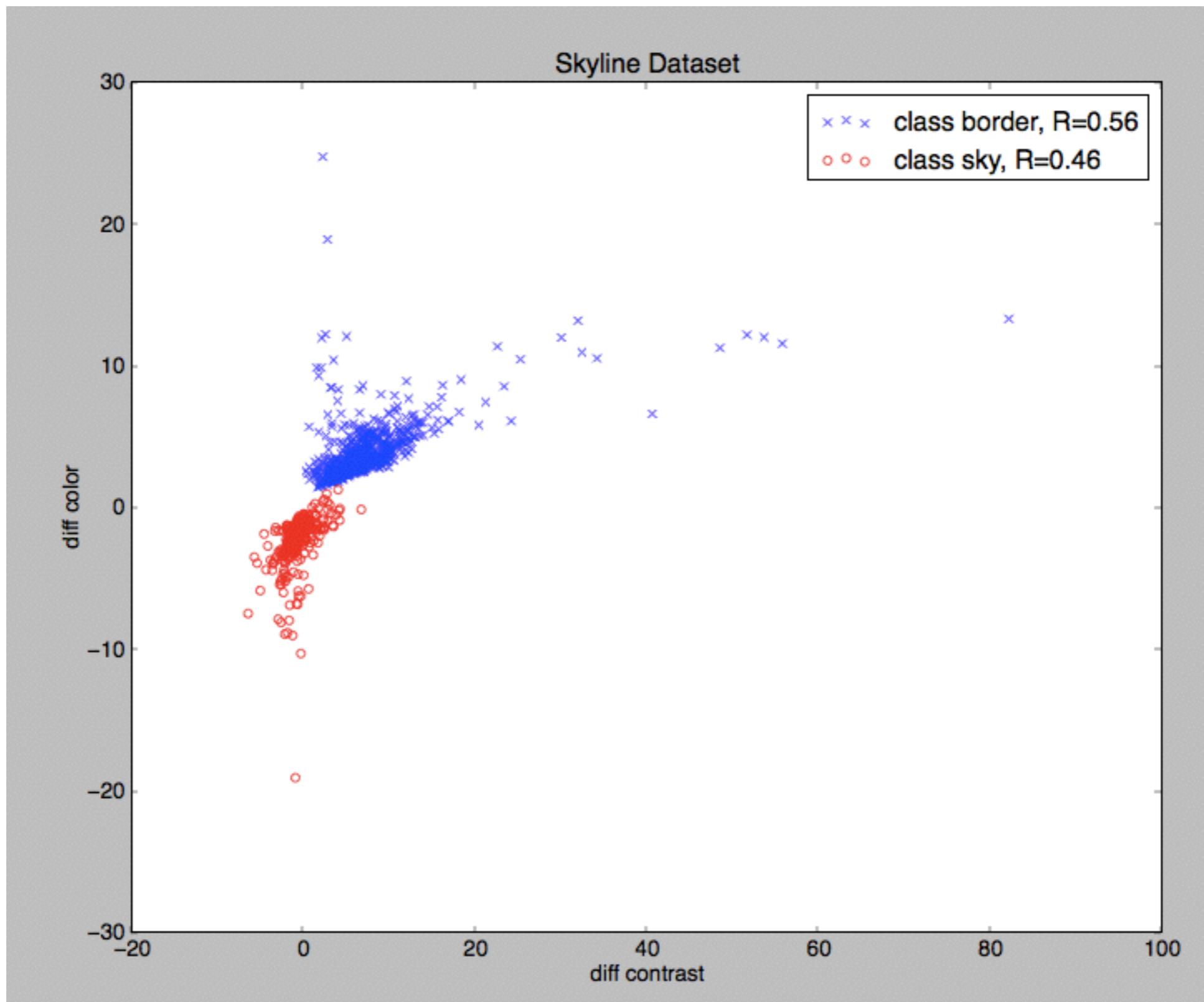
*note: the largest
contrasts
were removed
from analysis
for plot visibility



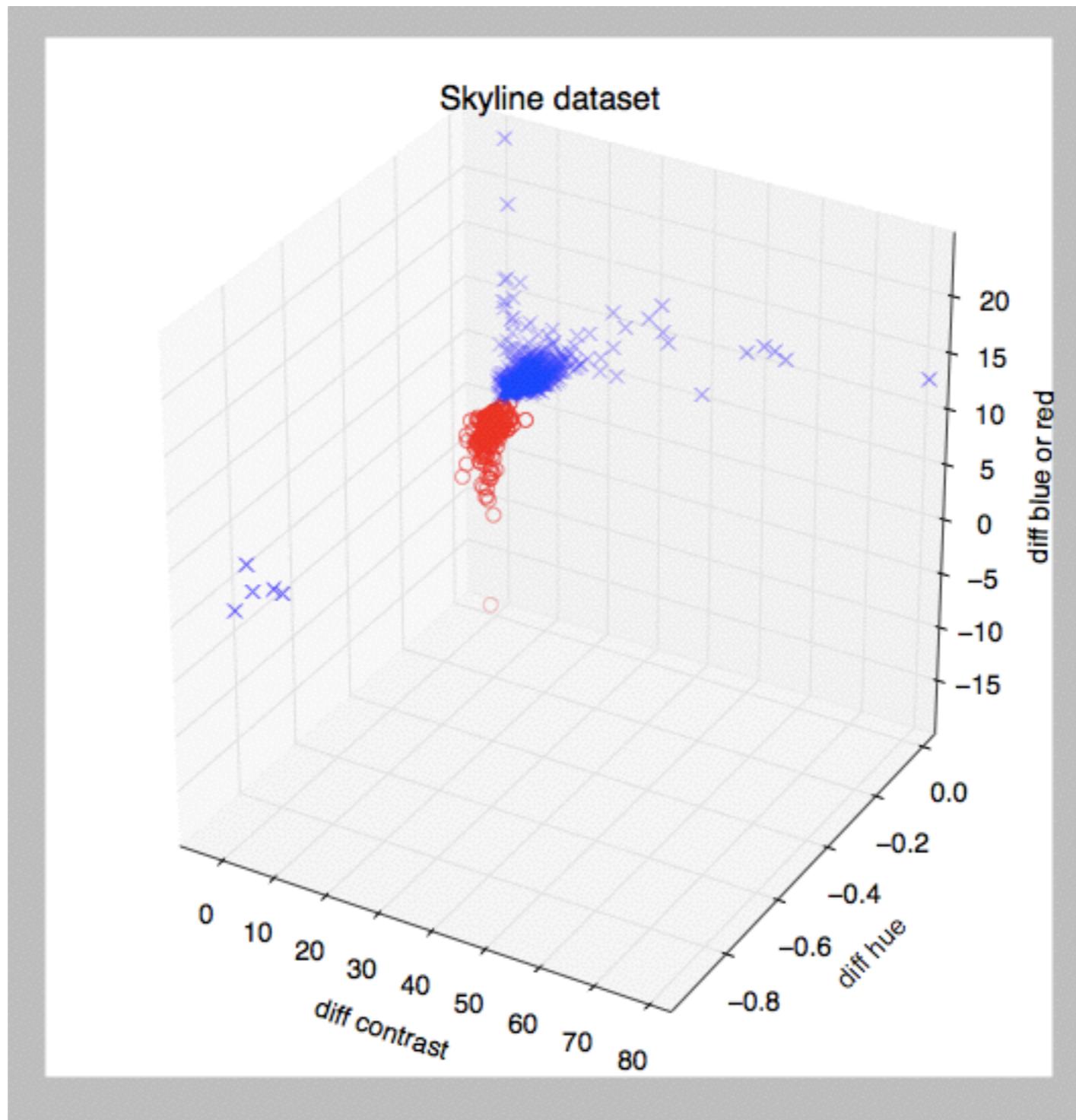
new mexico test image



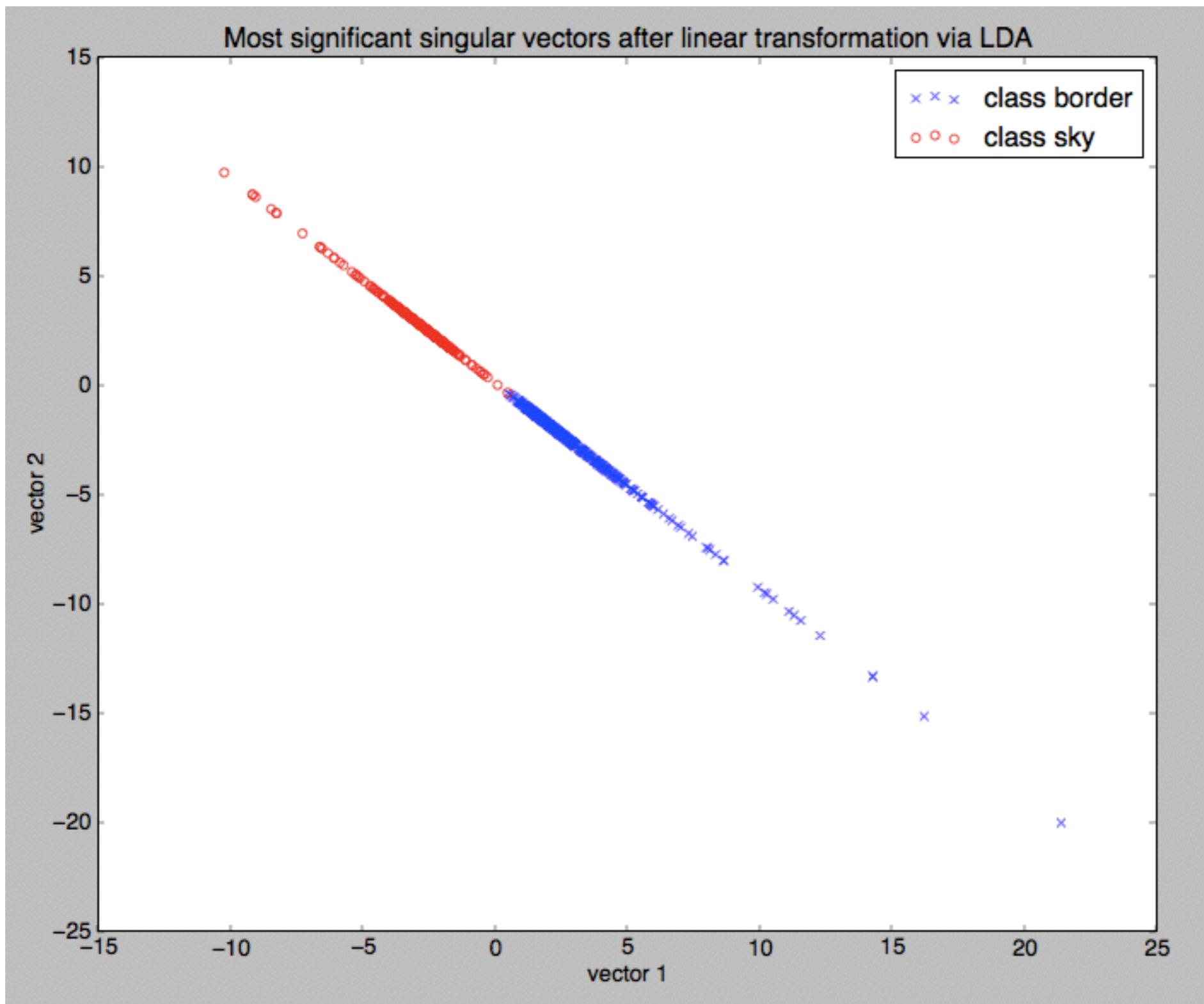
new mexico test image



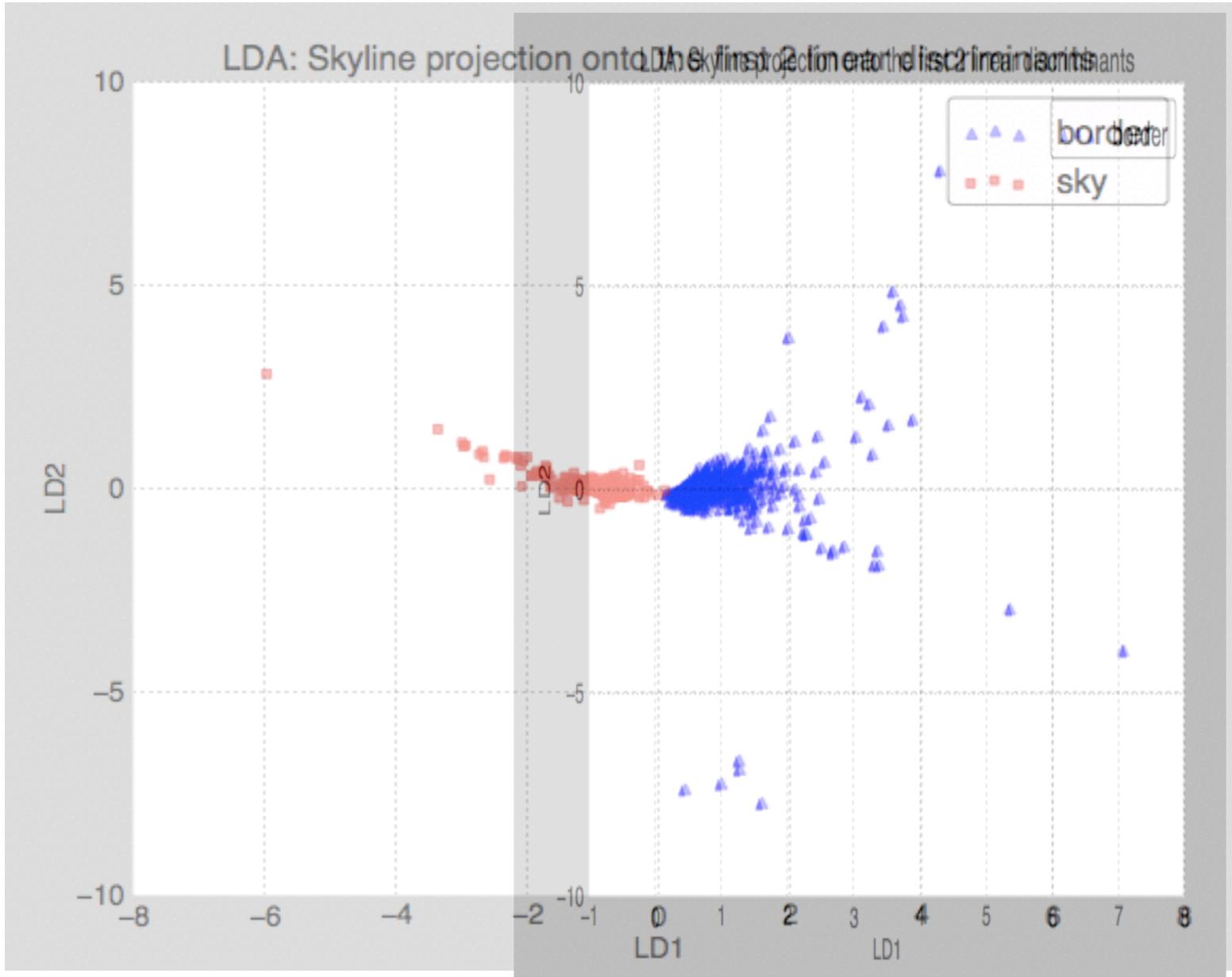
new mexico test image



new mexico test image



new mexico test image



```
contrast  hue  BorR
Mean Vector class 1: [ 0.6753 -0.0221  0.855 ]
Mean Vector class 2: [-0.6753  0.0221 -0.855 ]

('within-class Scatter Matrix:\n',
array([[ 788.788 ,      9.6141,   282.9405],
       [ 9.6141,  1449.2931,  -22.6902],
       [ 282.9405,  -22.6902,  390.0885]]))
('between-class Scatter Matrix:\n',
array([[ 1.9836e+03,  -6.4859e+01,   2.5115e+03],
       [ -6.4859e+01,   2.1207e+00,  -8.2118e+01],
       [ 2.5115e+03,  -8.2118e+01,  3.1797e+03]]))

Eigenvector 1:
[[ 0.0441]
 [ 0.0082]
 [ 0.999 ]]
Eigenvalue 1: 8.18e+00

Eigenvector 2:
[[-0.2189]
 [-0.9645]
 [ 0.148 ]]
Eigenvalue 2: -5.35e-17

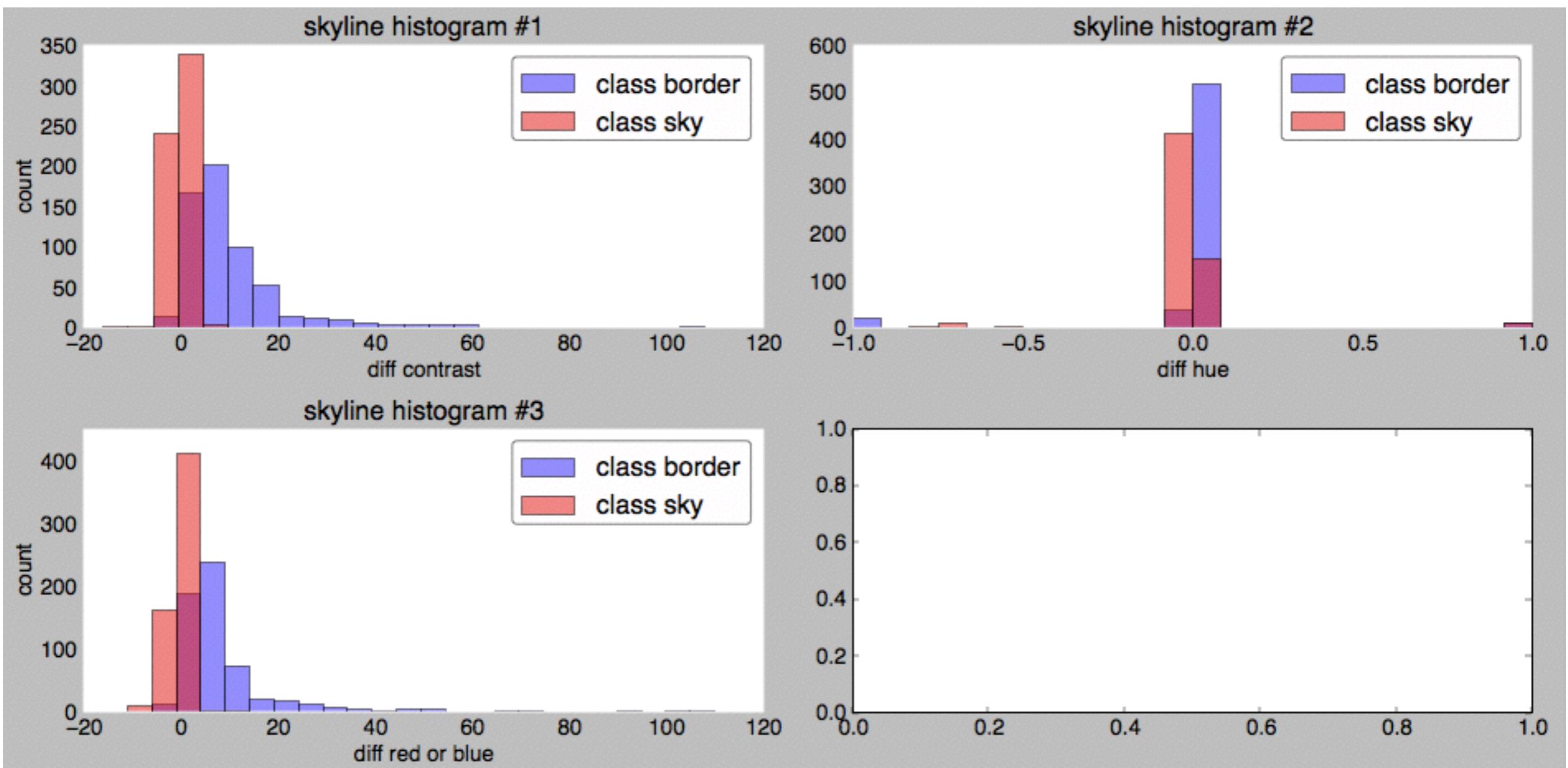
Eigenvector 3:
[[ 0.7191]
 [ 0.4153]
 [-0.5572]]
Eigenvalue 3: -5.75e-16
ok
Eigenvalues in decreasing order:
8.1758993237
5.74979825745e-16
5.35110530569e-17
Variance explained:
eigenvalue 1: 100.00%
eigenvalue 2: 0.00%
eigenvalue 3: 0.00%
('Matrix W:\n', array([[ 0.0441,  0.0082,  0.999 ],
 [ 0.7191,  0.4153, -0.5572]]))
```

arizona test image

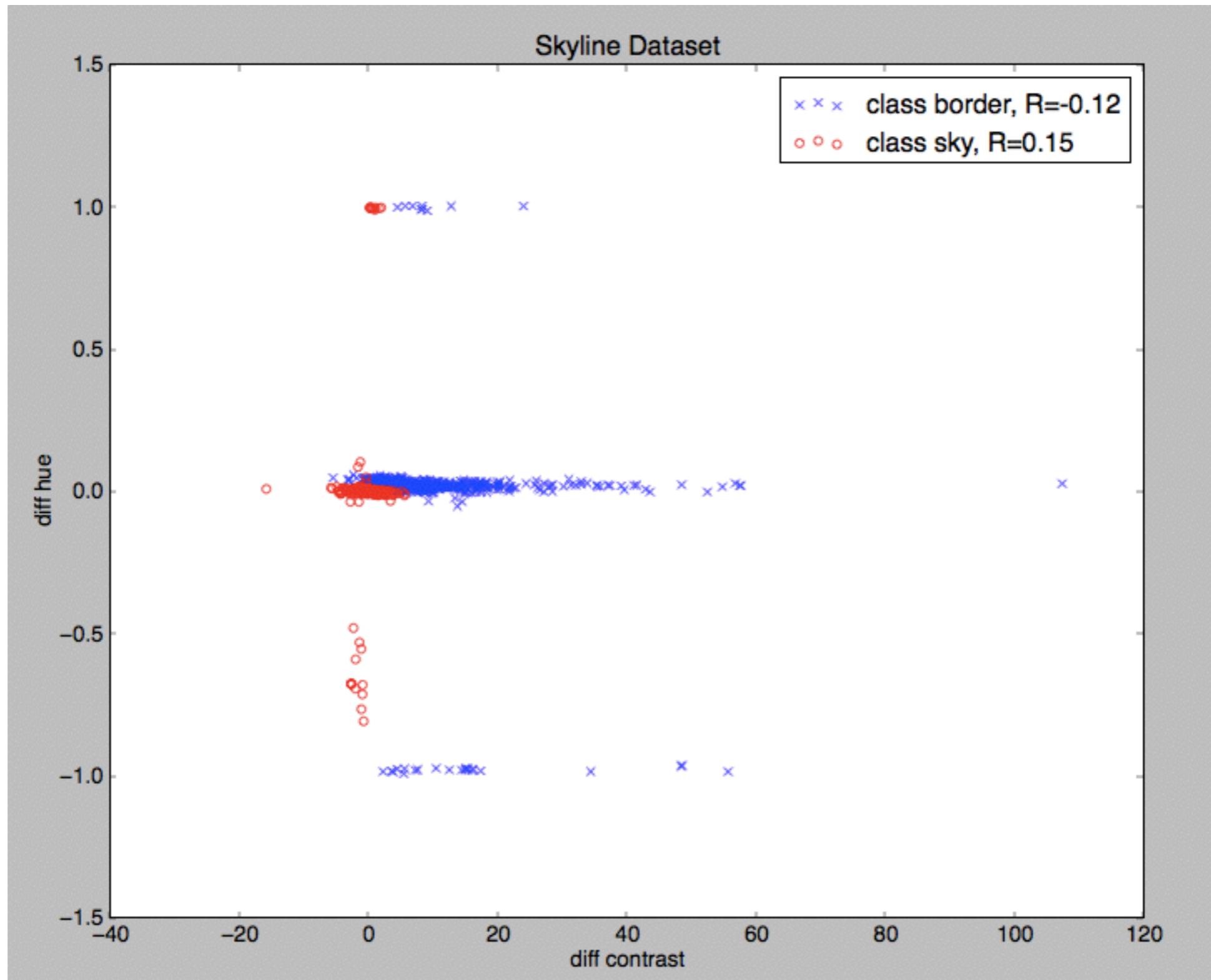


arizona test image

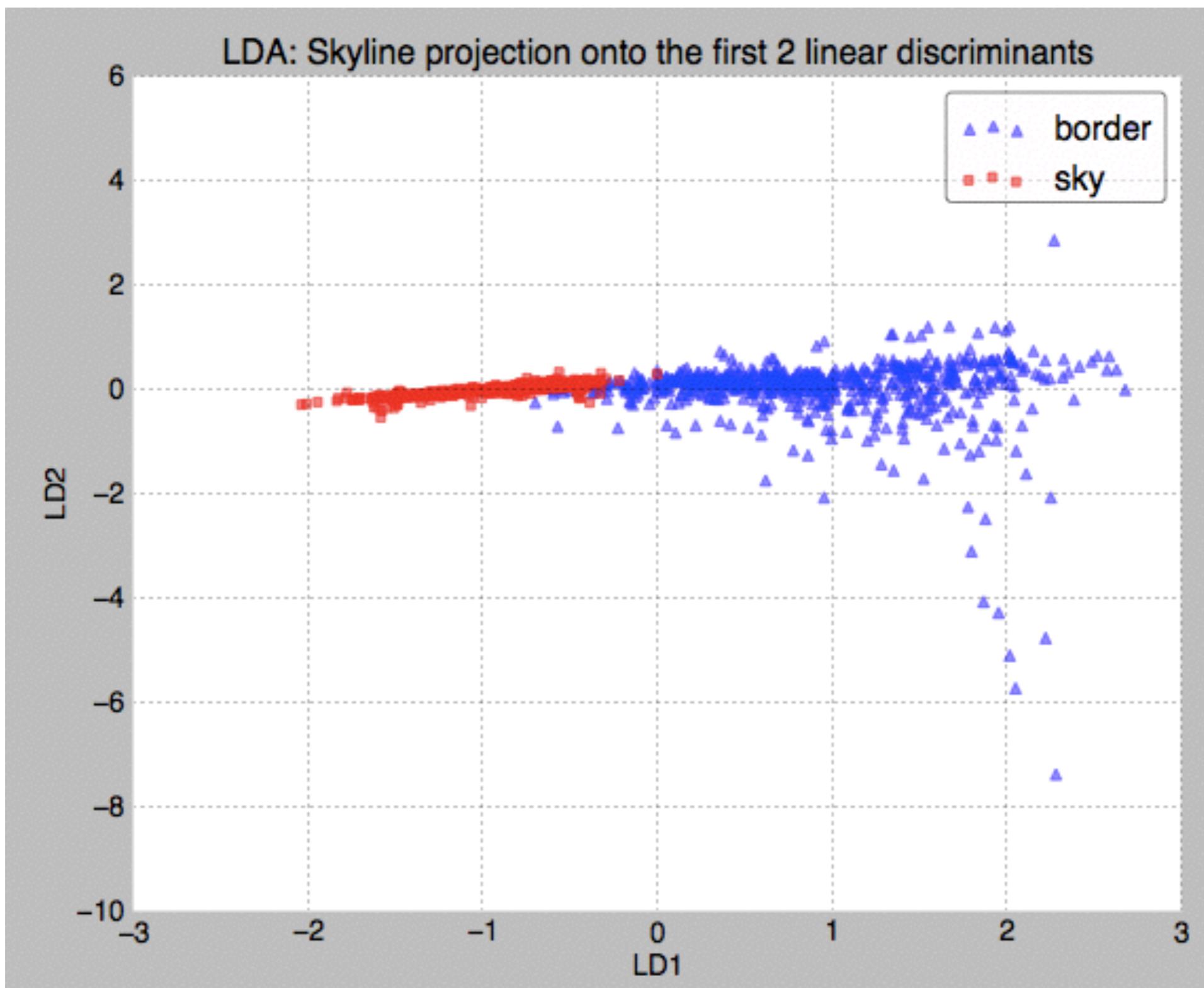
*note: the largest contrasts were removed from analysis for plot visibility



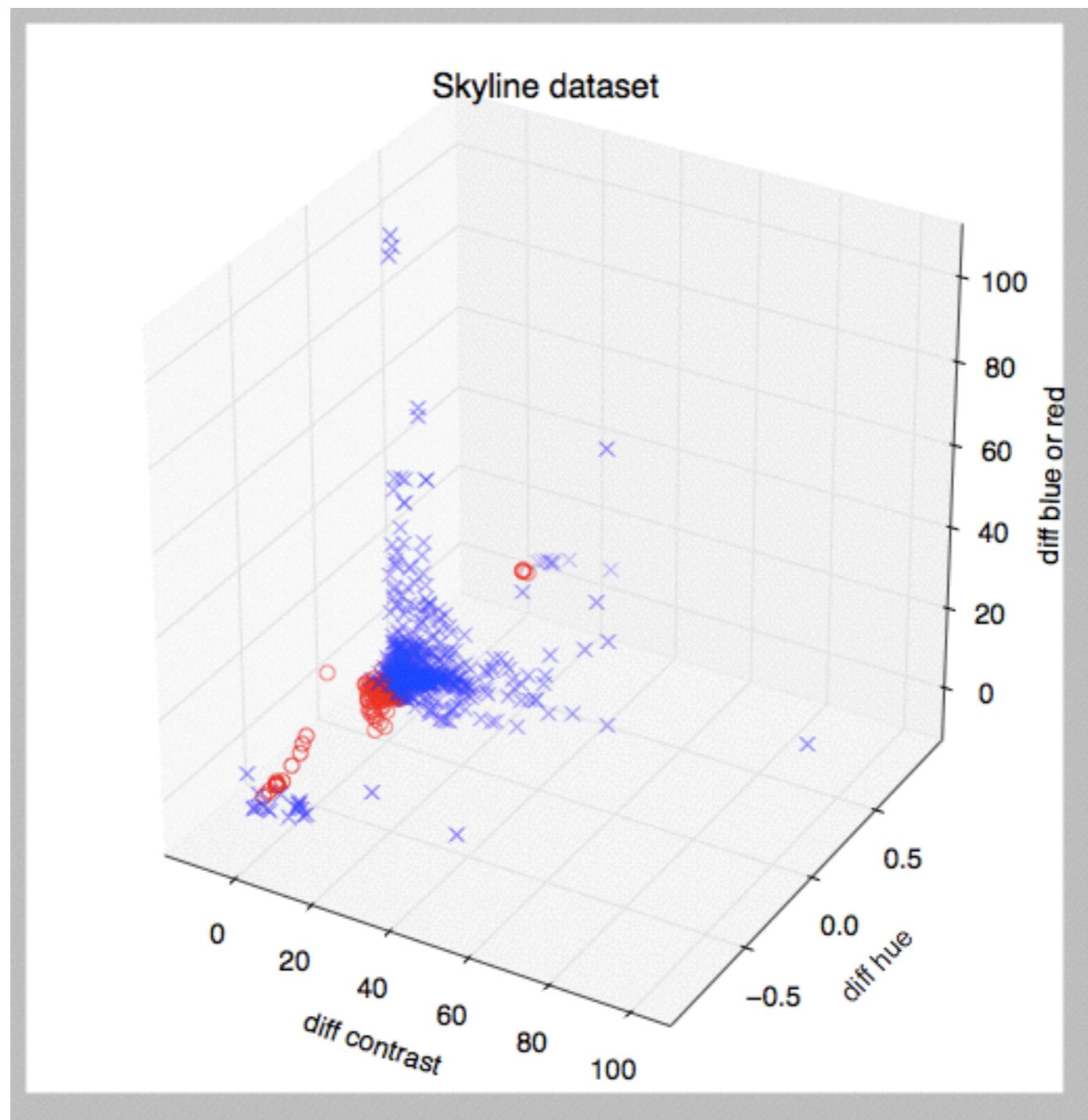
arizona test image



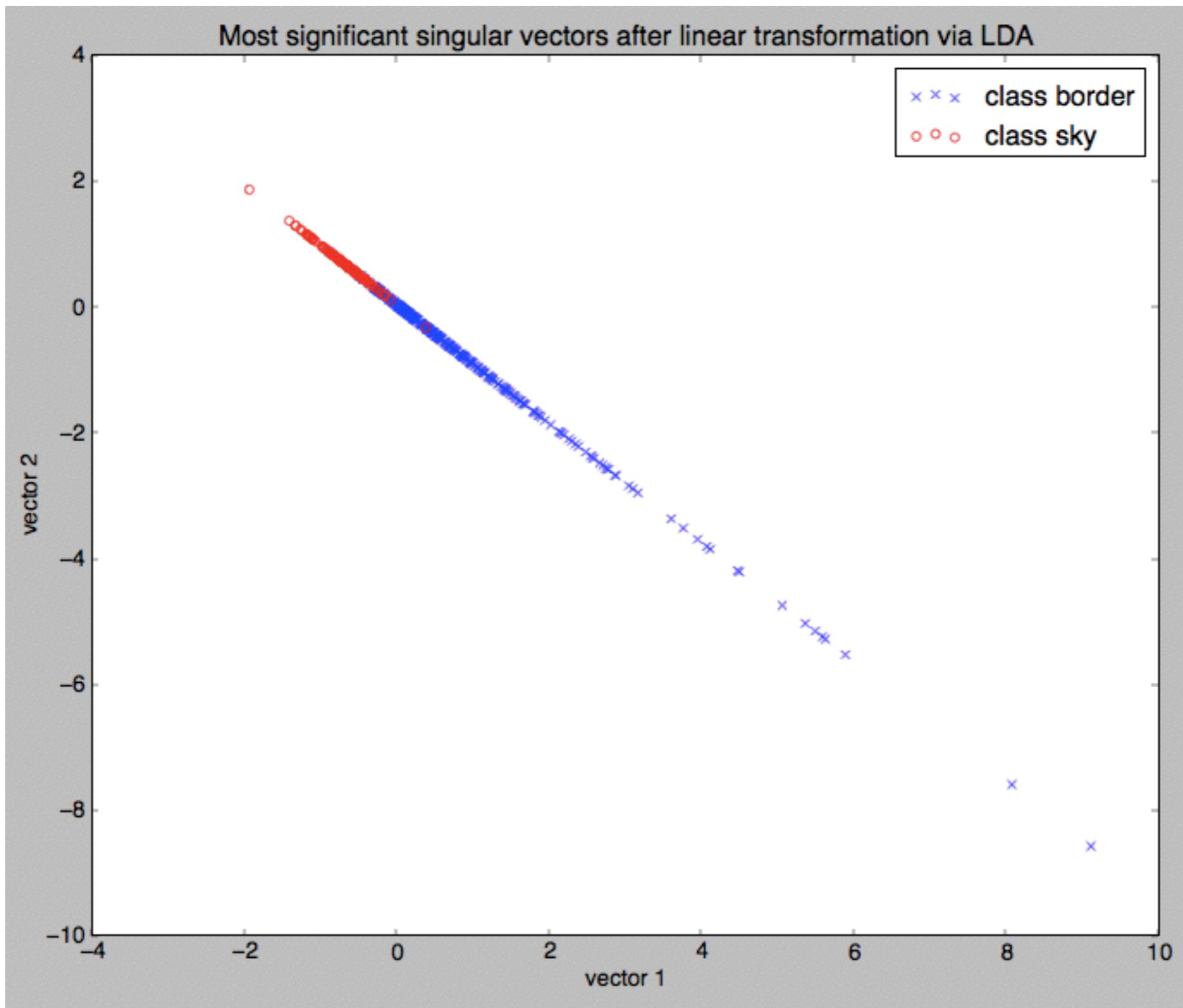
arizona test image



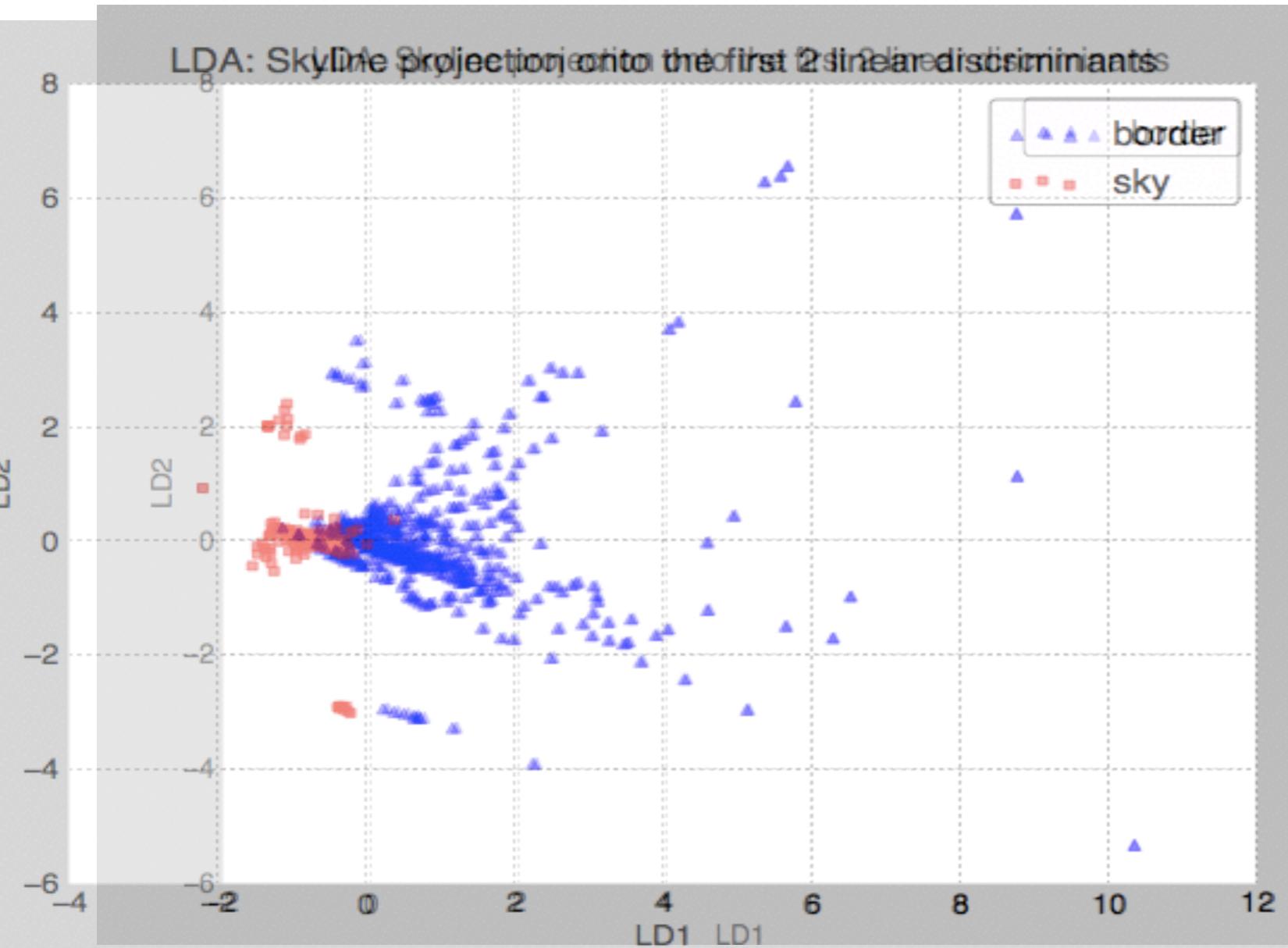
arizona test image



arizona test image



arizona test image



contrast	hue	BorR
Mean Vector class 1: [0.5665	-0.0133	0.4794]
Mean Vector class 2: [-0.5665	0.0133	-0.4794]

('within-class Scatter Matrix:\n',
array([[797.197 , -81.2466, 148.9749],
[-81.2466, 1173.7936, -53.2171],
[148.9749, -53.2171, 904.2197]]))
('between-class Scatter Matrix:\n',
array([[1.1304e+03, -2.6457e+01, 9.5650e+02],
[-2.6457e+01, 6.1922e-01, -2.2387e+01],
[9.5650e+02, -2.2387e+01, 8.0934e+02]]))

Eigenvector 1:
[[0.8274]
[0.0678]
[0.5575]]

Eigenvalue 1: 1.99e+00

Eigenvector 2:
[[0.1211]
[-0.9779]
[-0.1702]]

Eigenvalue 2: 4.64e-17

Eigenvector 3:
[[-0.5307]
[-0.5874]
[0.611]]

Eigenvalue 3: -1.99e-16

ok

Eigenvalues in decreasing order:

1.98975976216
1.98998572492e-16
4.6372972206e-17

Variance explained:

eigenvalue 1: 100.00%
eigenvalue 2: 0.00%
eigenvalue 3: 0.00%

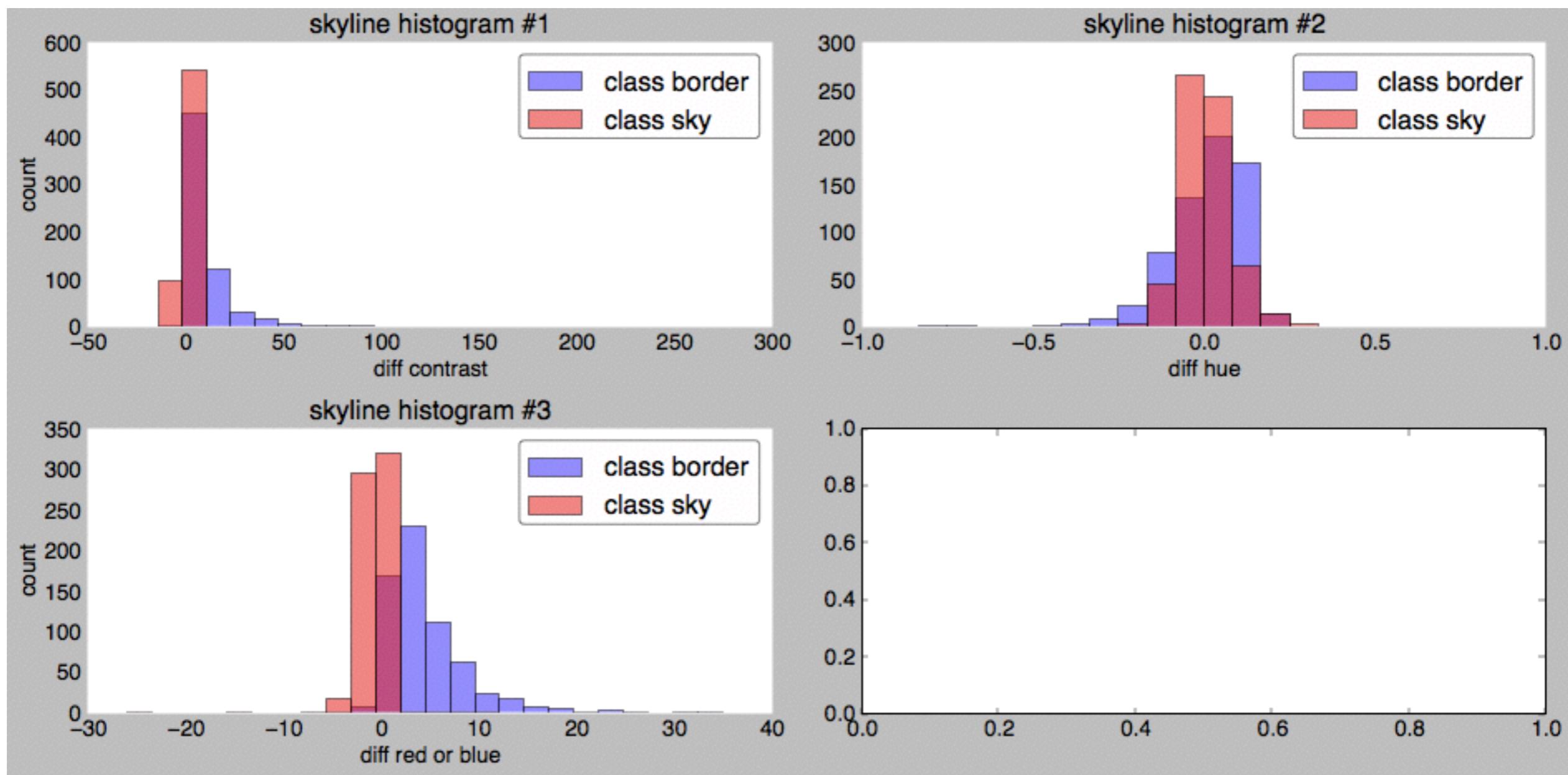
('Matrix W:\n', array([[0.8274, 0.0678, 0.5575],
[-0.5307, -0.5874, 0.611]]))

rainbow test image

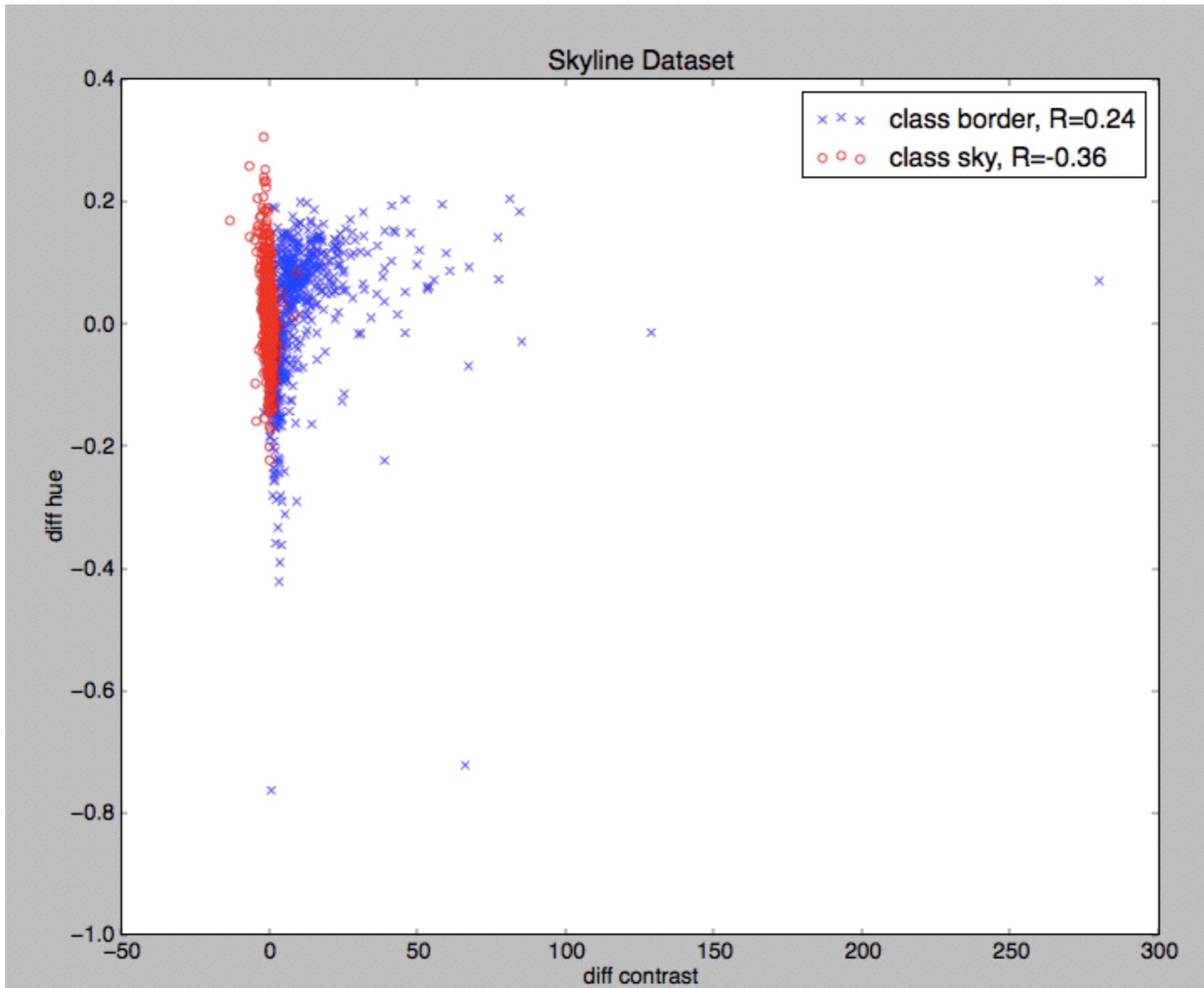


rainbow test image

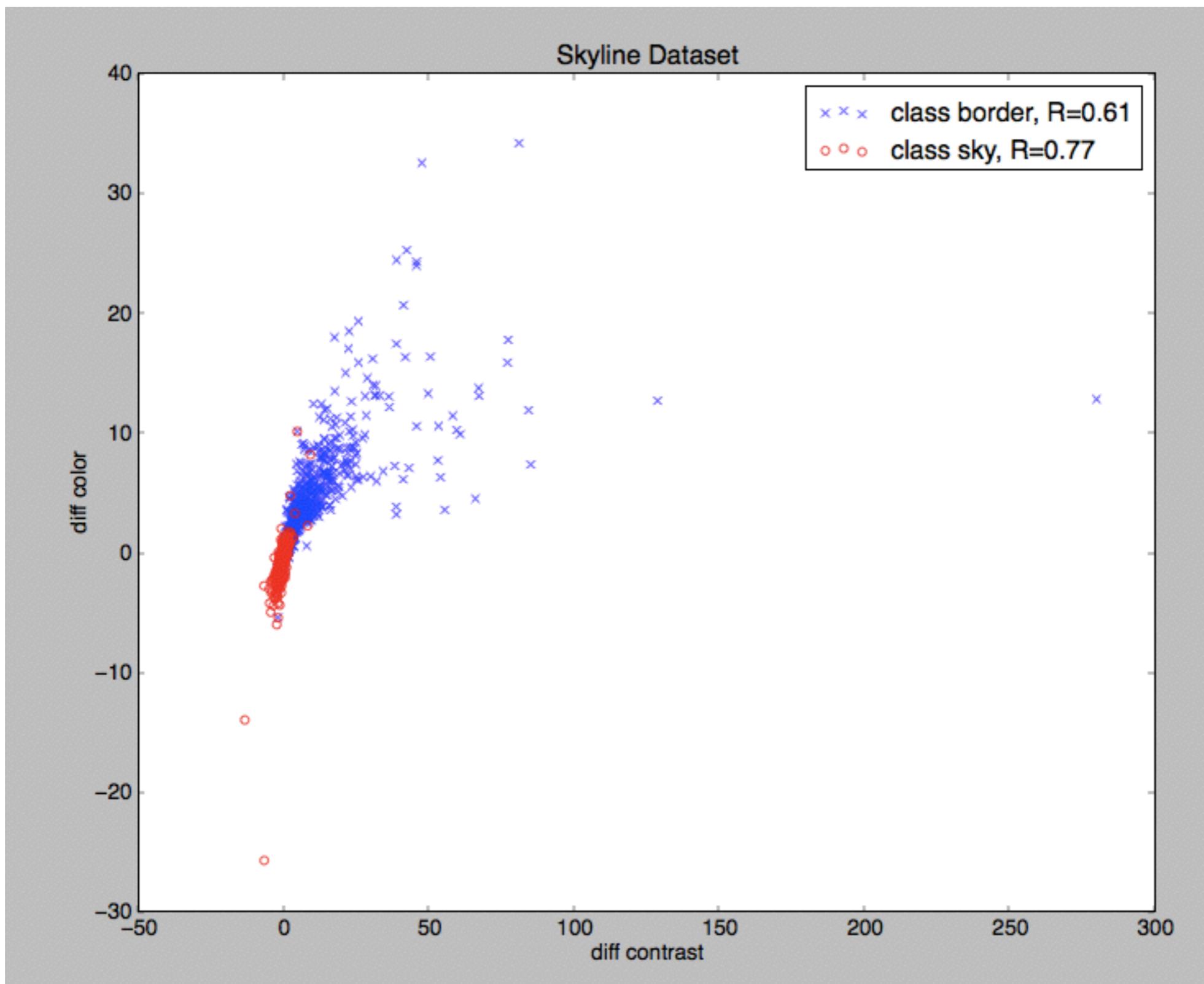
*note: the largest contrasts were removed from analysis for plot visibility



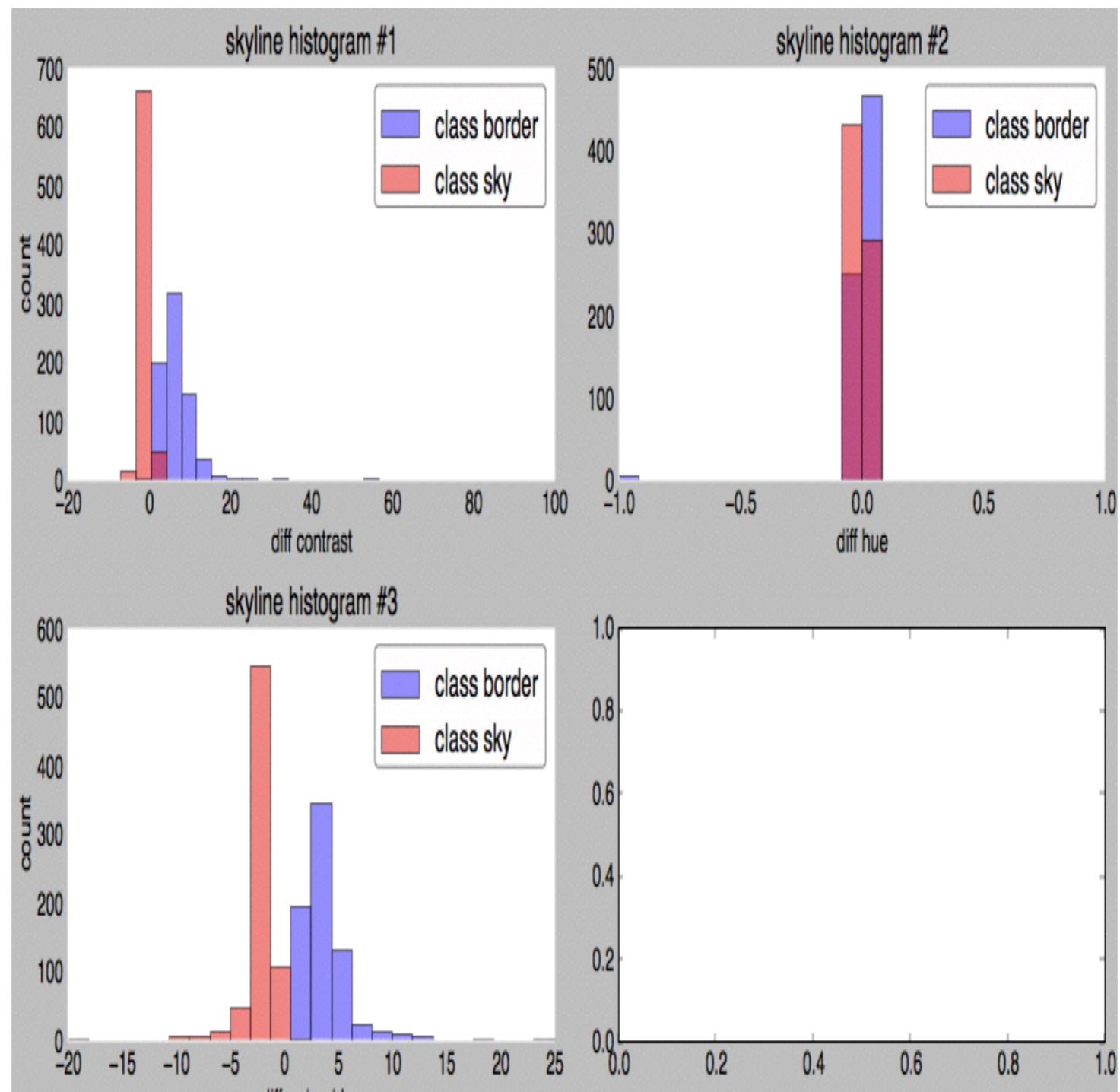
rainbow test image



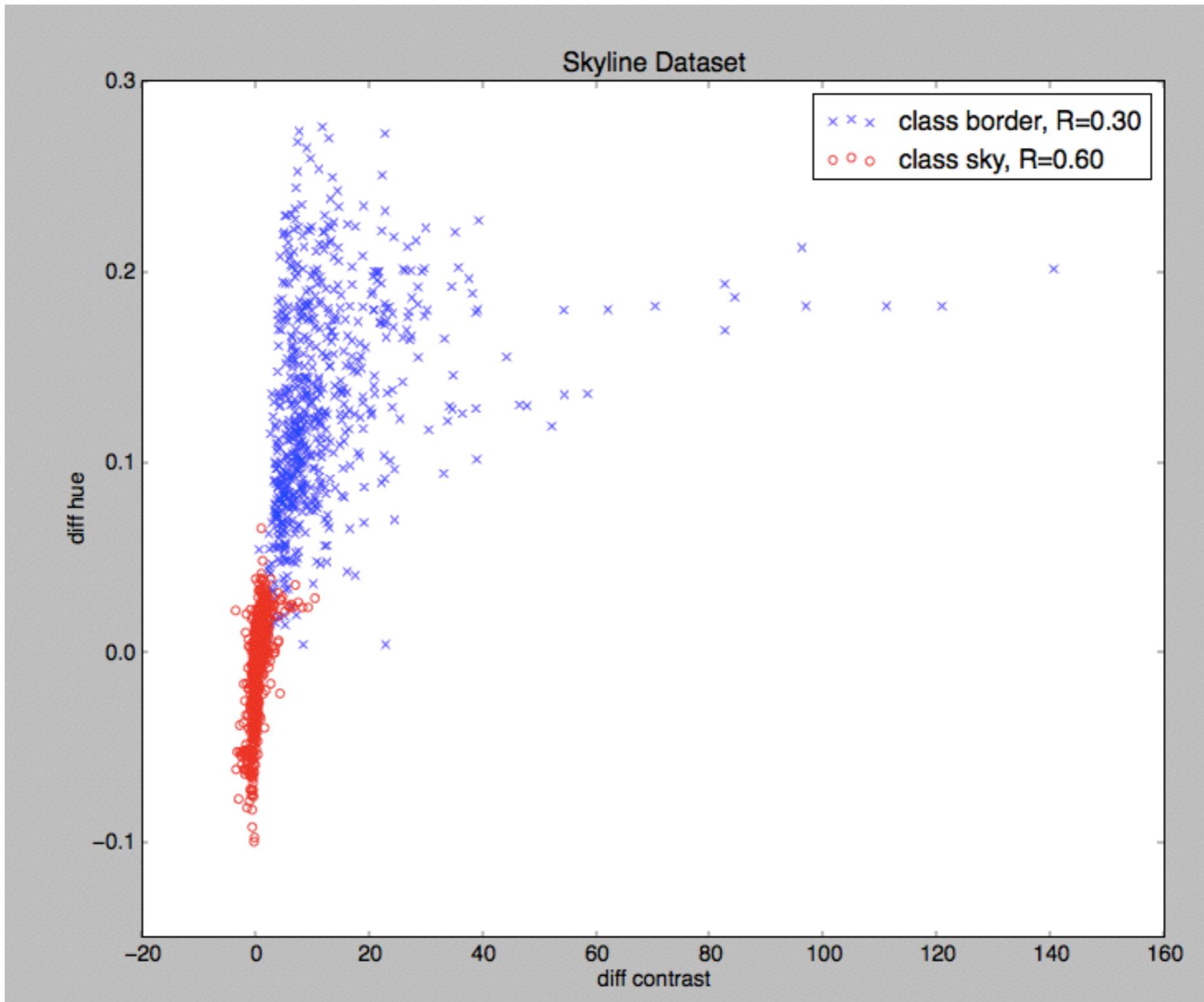
rainbow test image



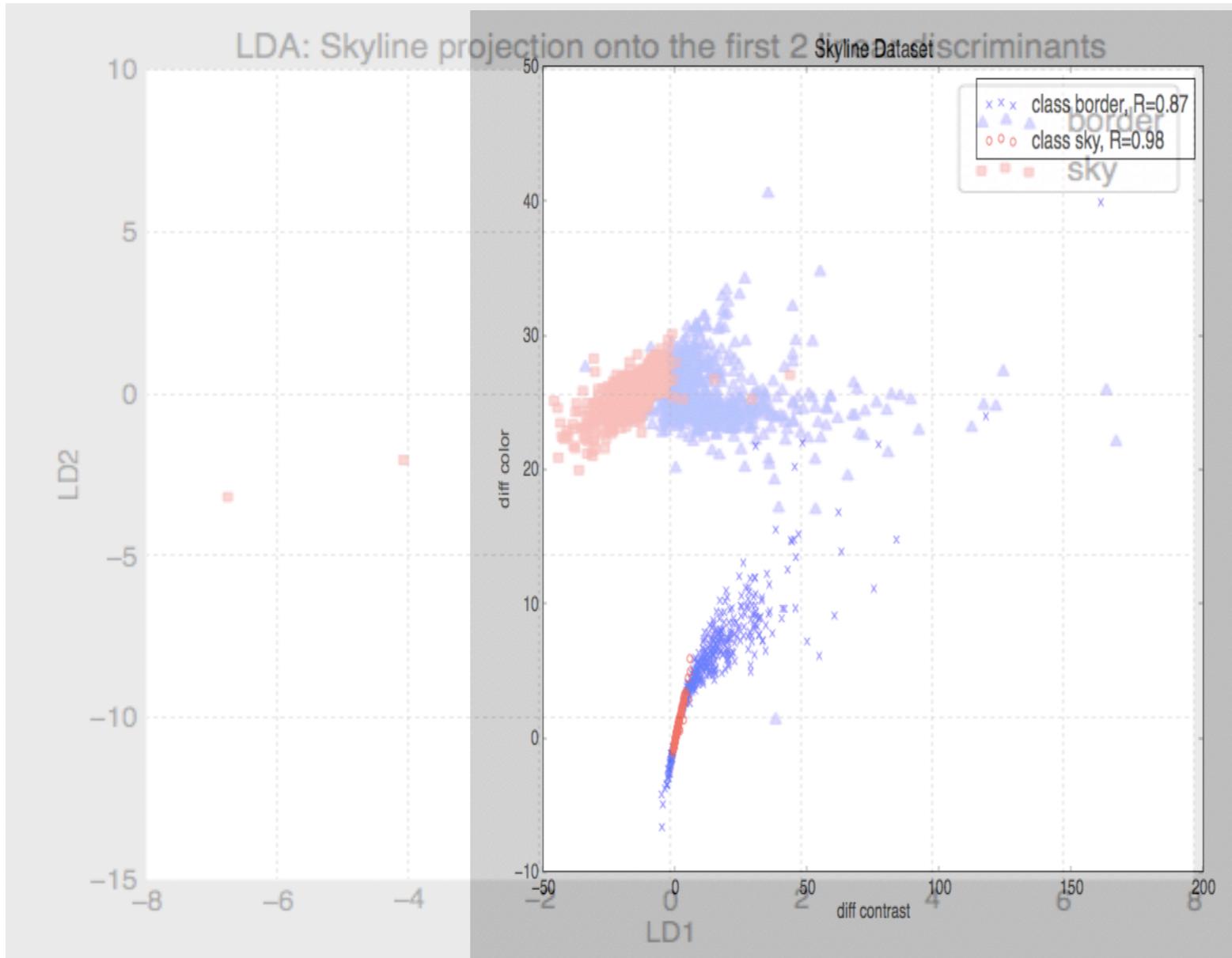
rainbow test image



rainbow test image

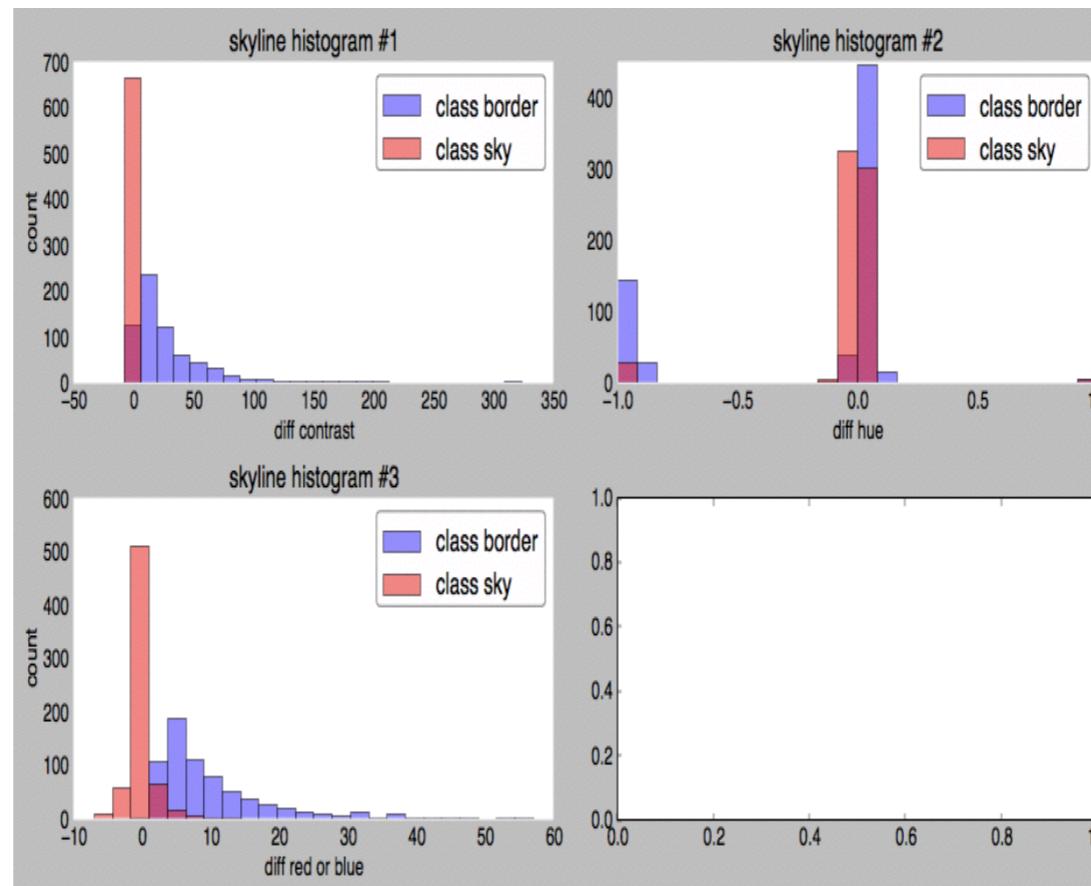
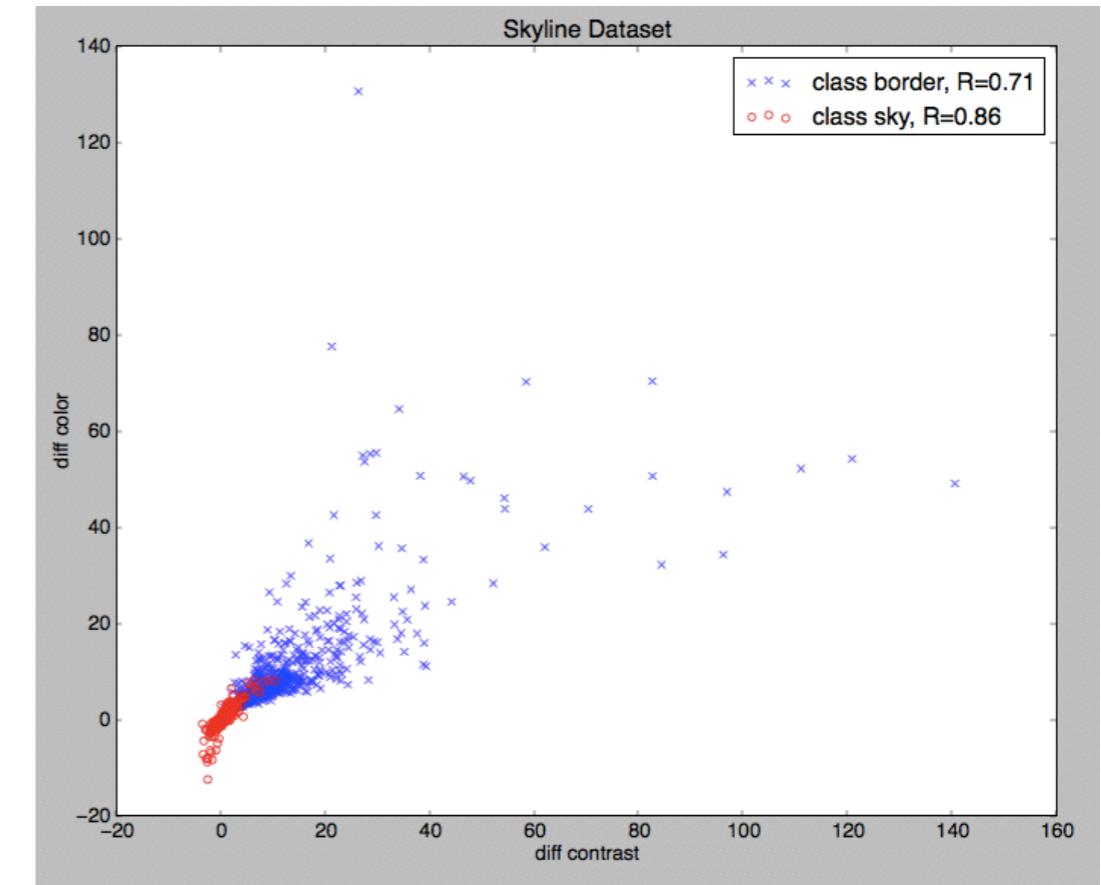
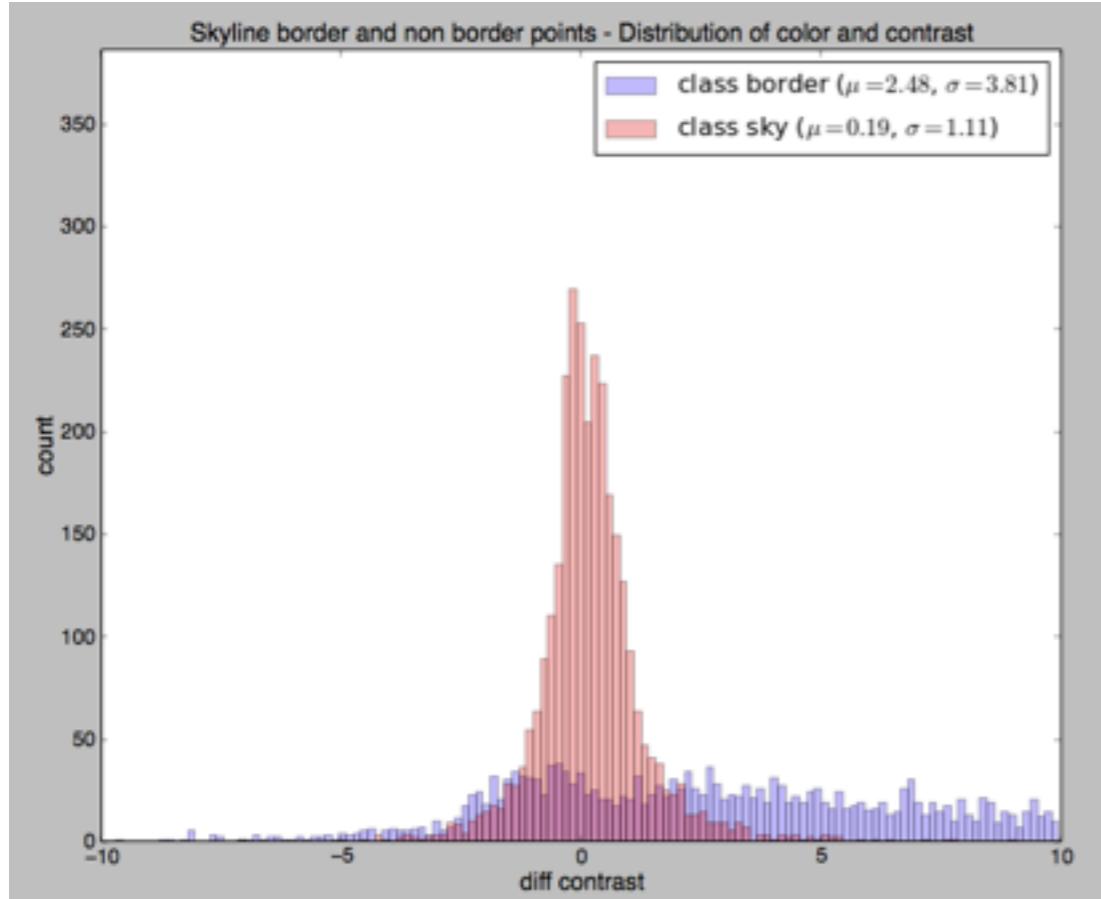


rainbow test image

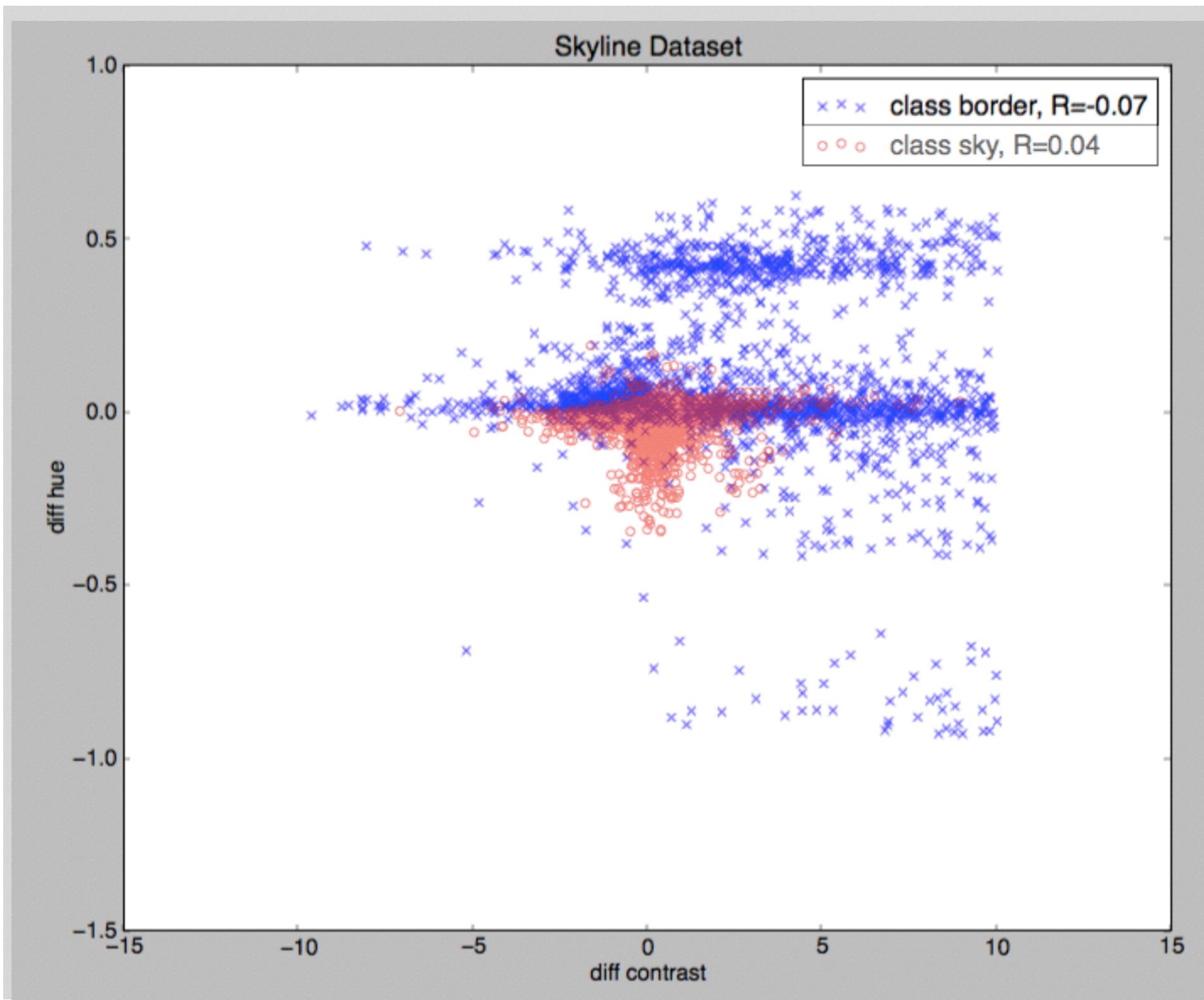


	contrast	hue	BorR
Mean Vector class 1:	[0.417	0.0386	0.6287]
Mean Vector class 2:	[-0.4183	-0.0387	-0.6306]
Eigenvalue 1:	2.21e+00		
Eigenvalue 2:	-1.62e-16		
Eigenvalue 3:	1.60e-06		
ok			
Eigenvalues in decreasing order:			
eigenvalue 1:	100.00%		
eigenvalue 2:	0.00%		
eigenvalue 3:	0.00%		
('Matrix W:\n', array([[-0.0376, -0.2417, 0.9696], [-0.5153, -0.7638, 0.3887]])))			

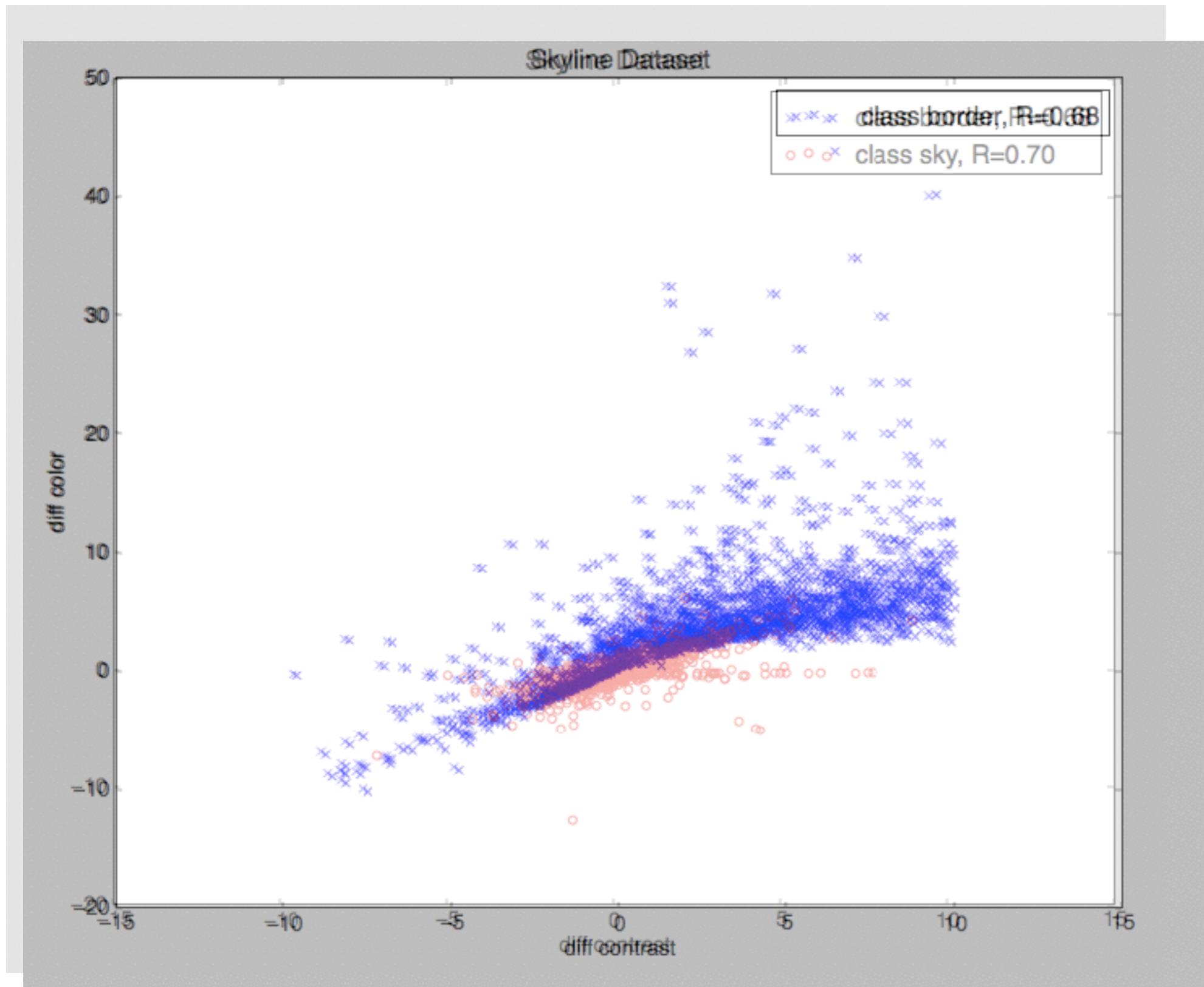
All BLUE SKY data in one:



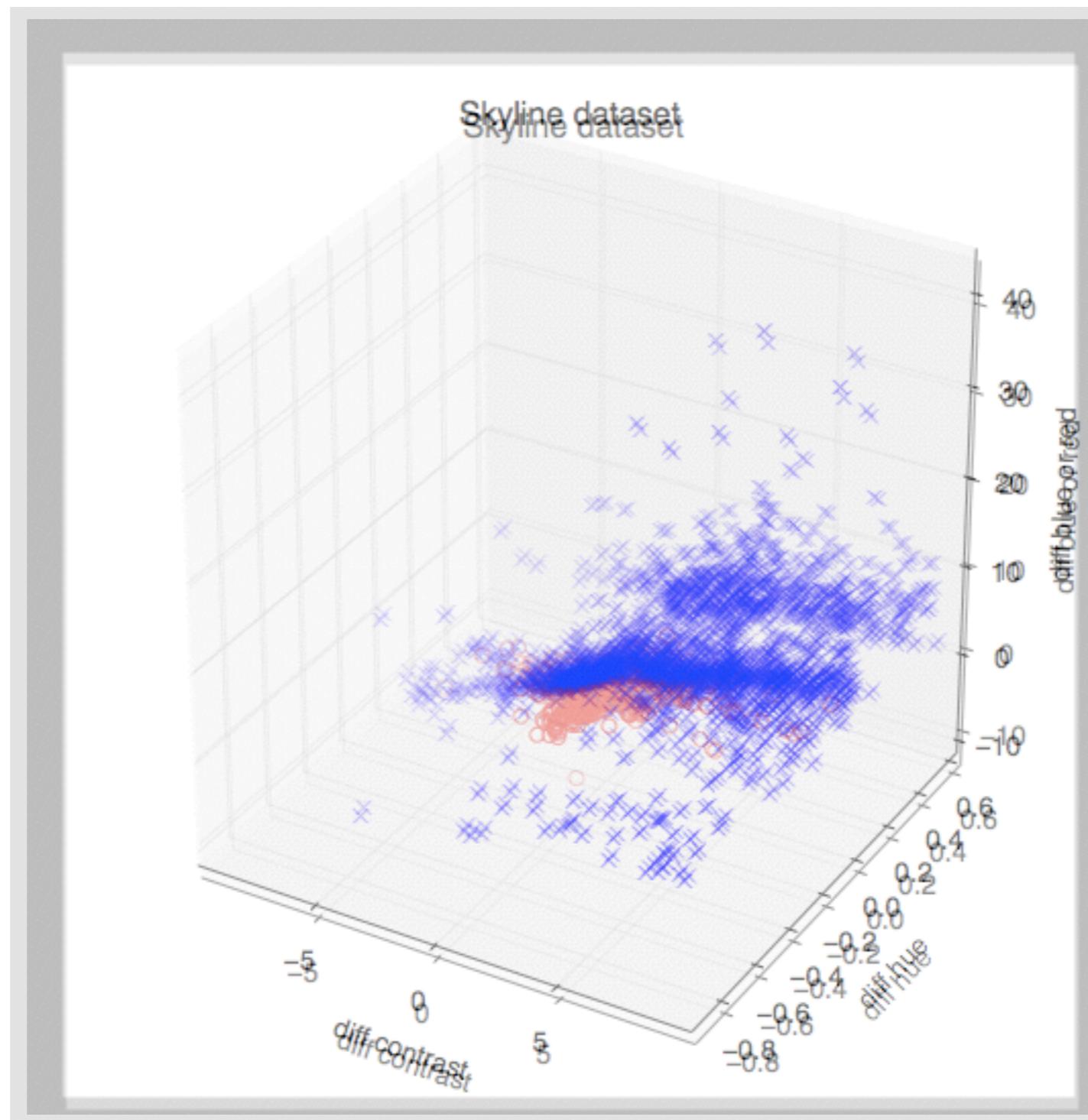
All BLUE SKY data in one:



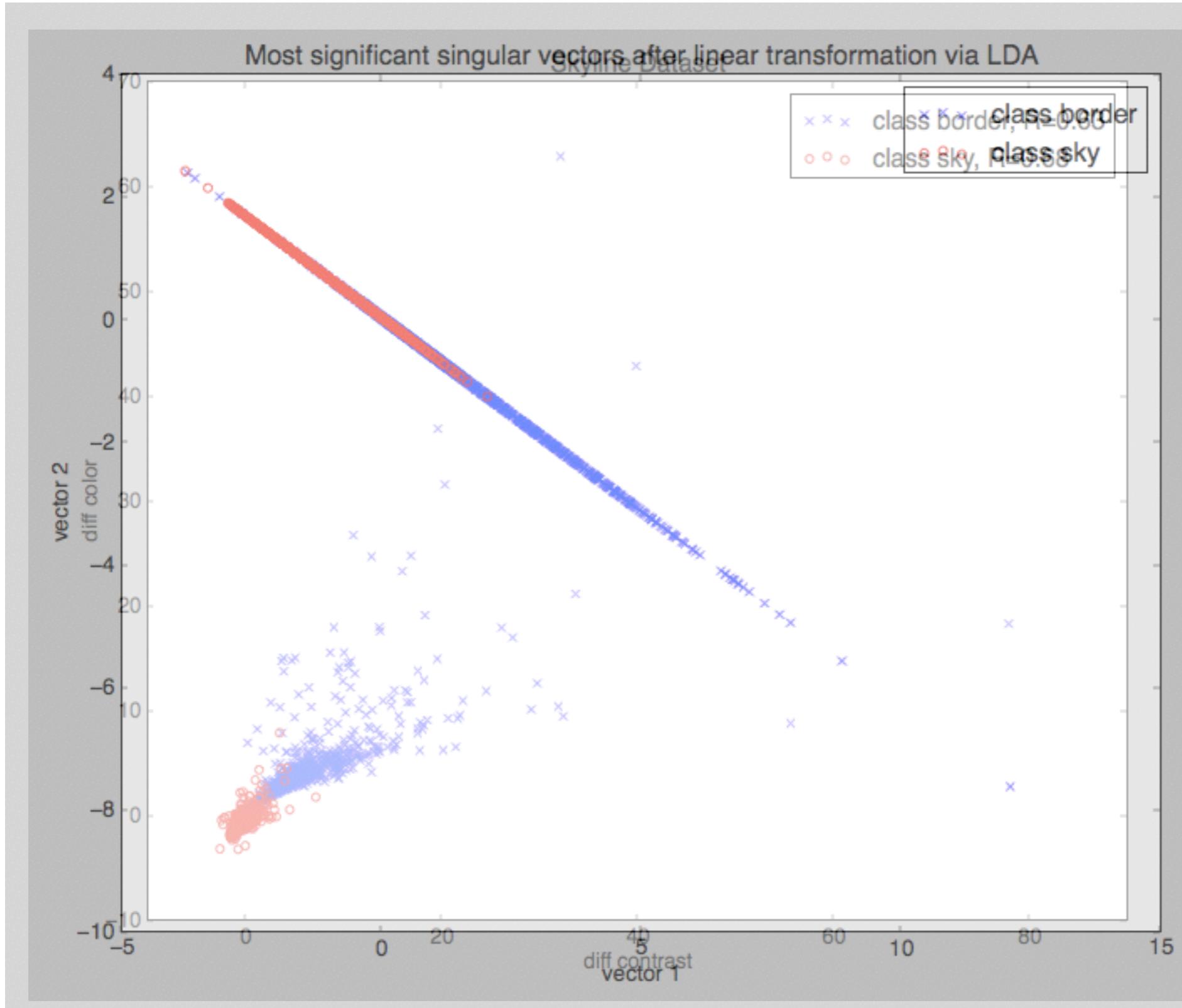
All BLUE SKY data in one:



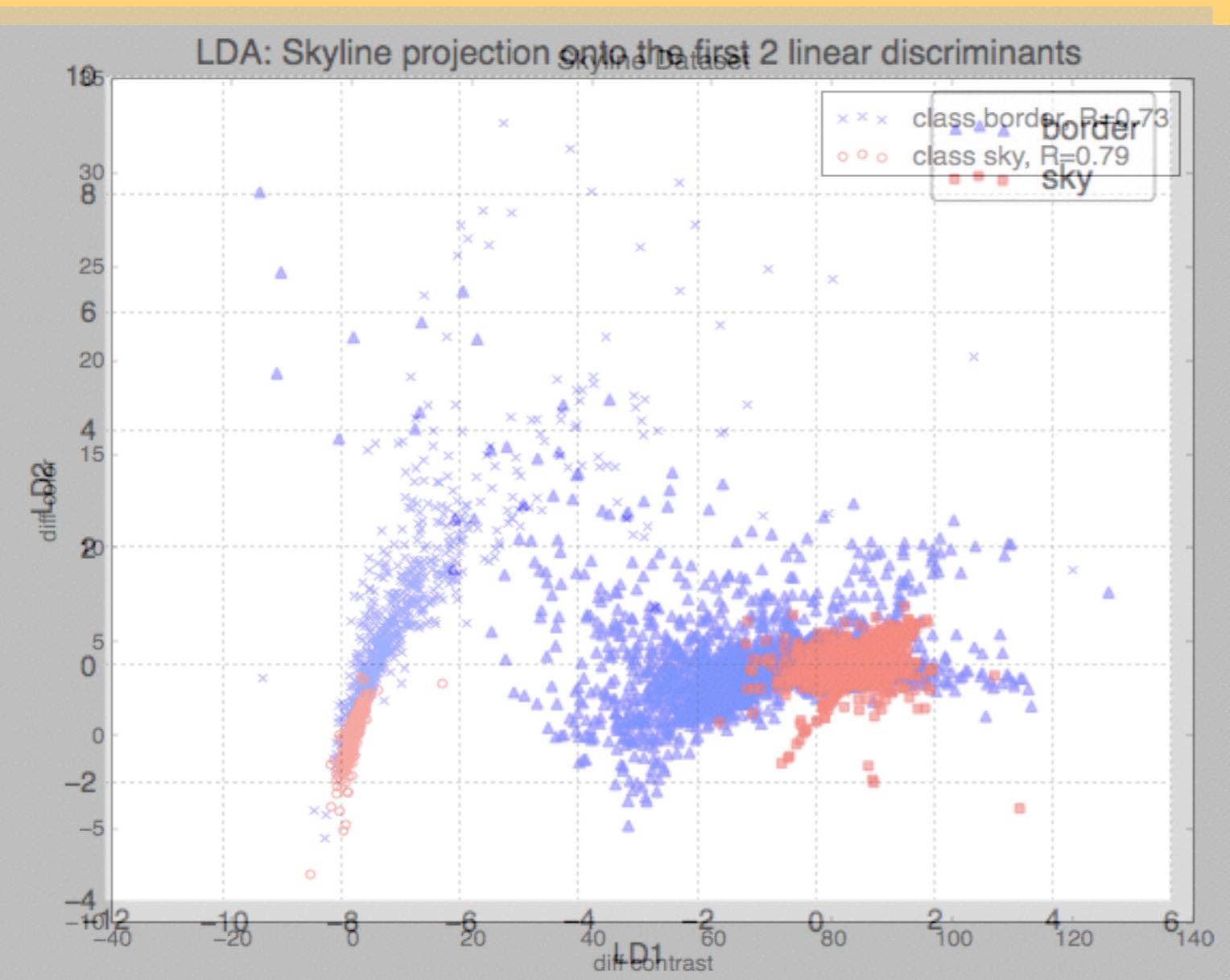
All BLUE SKY data in one:



All BLUE SKY data in one:

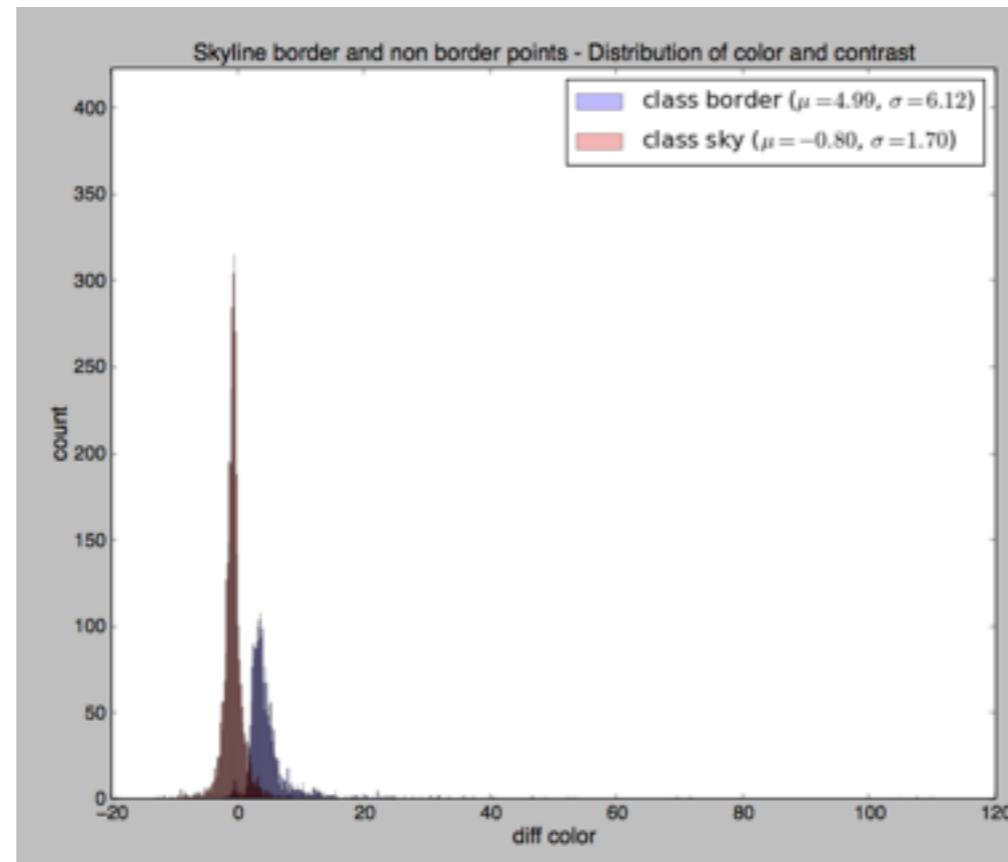
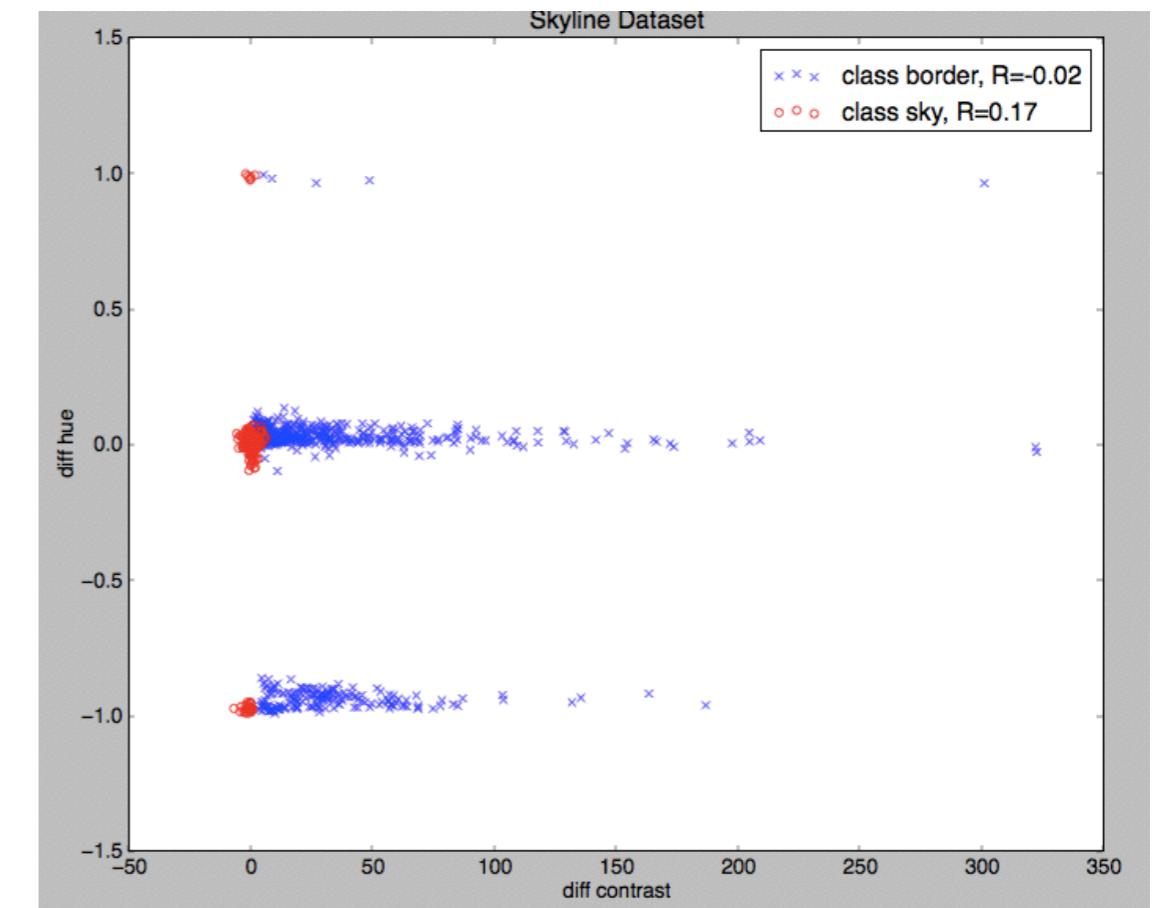
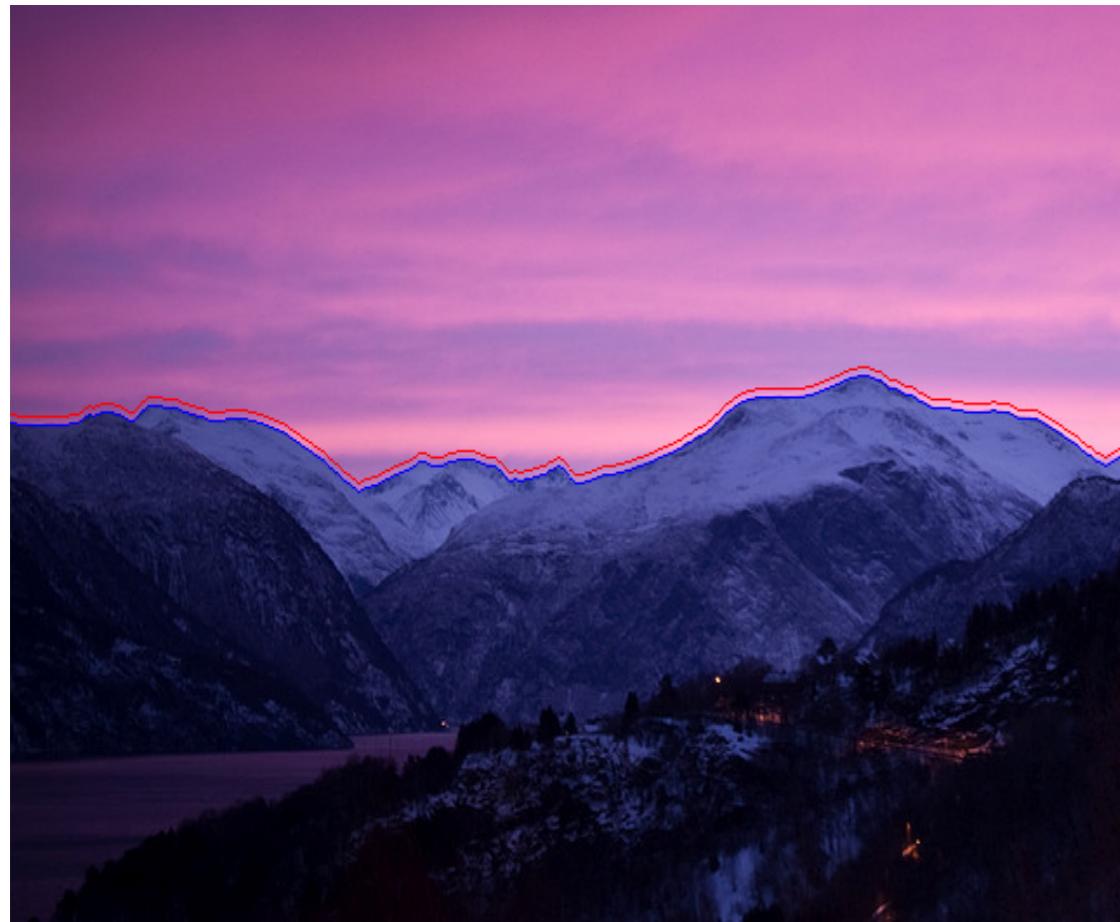


All BLUE SKY data in one:

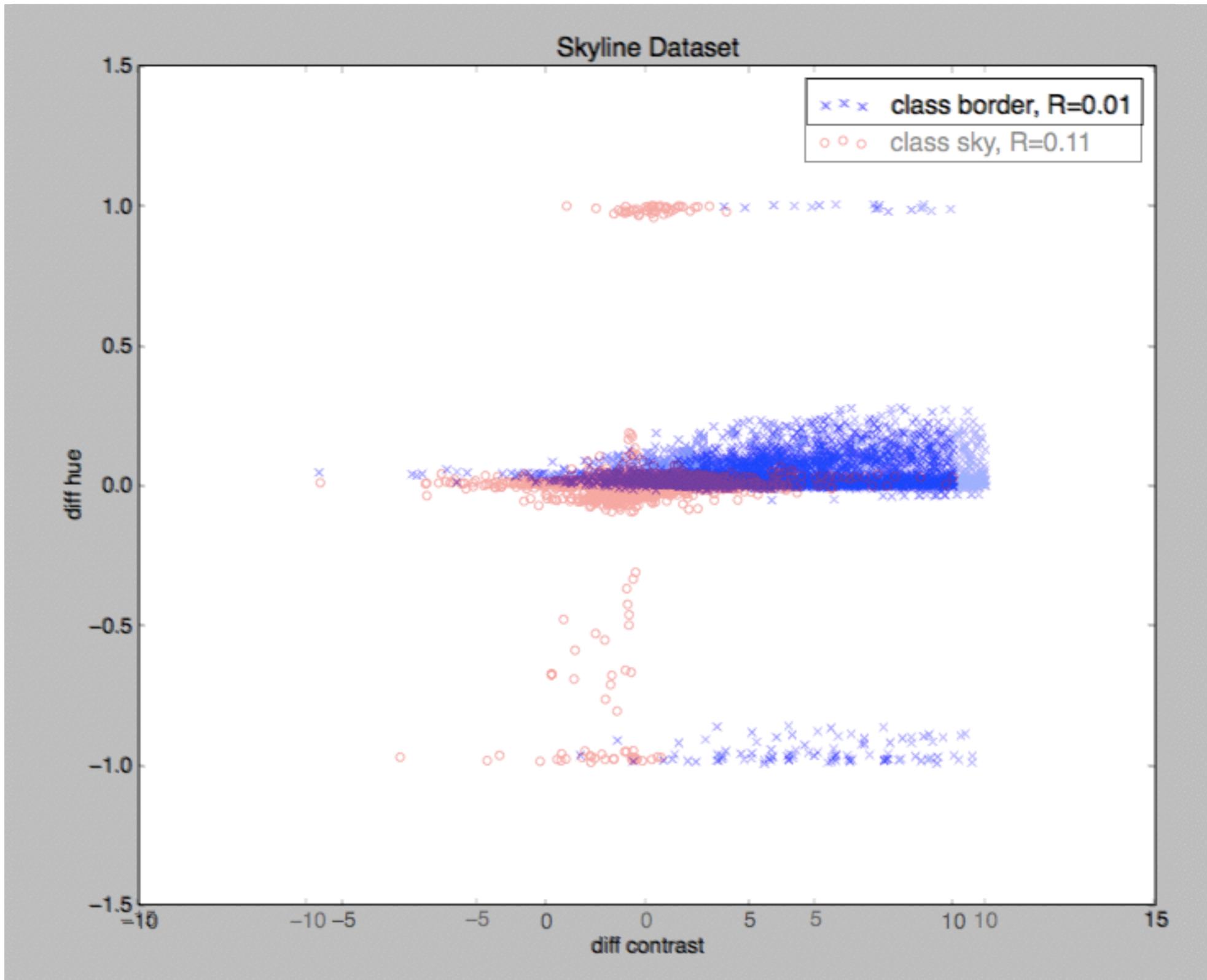


unfortunately, not separable when all blue sky image data is combined

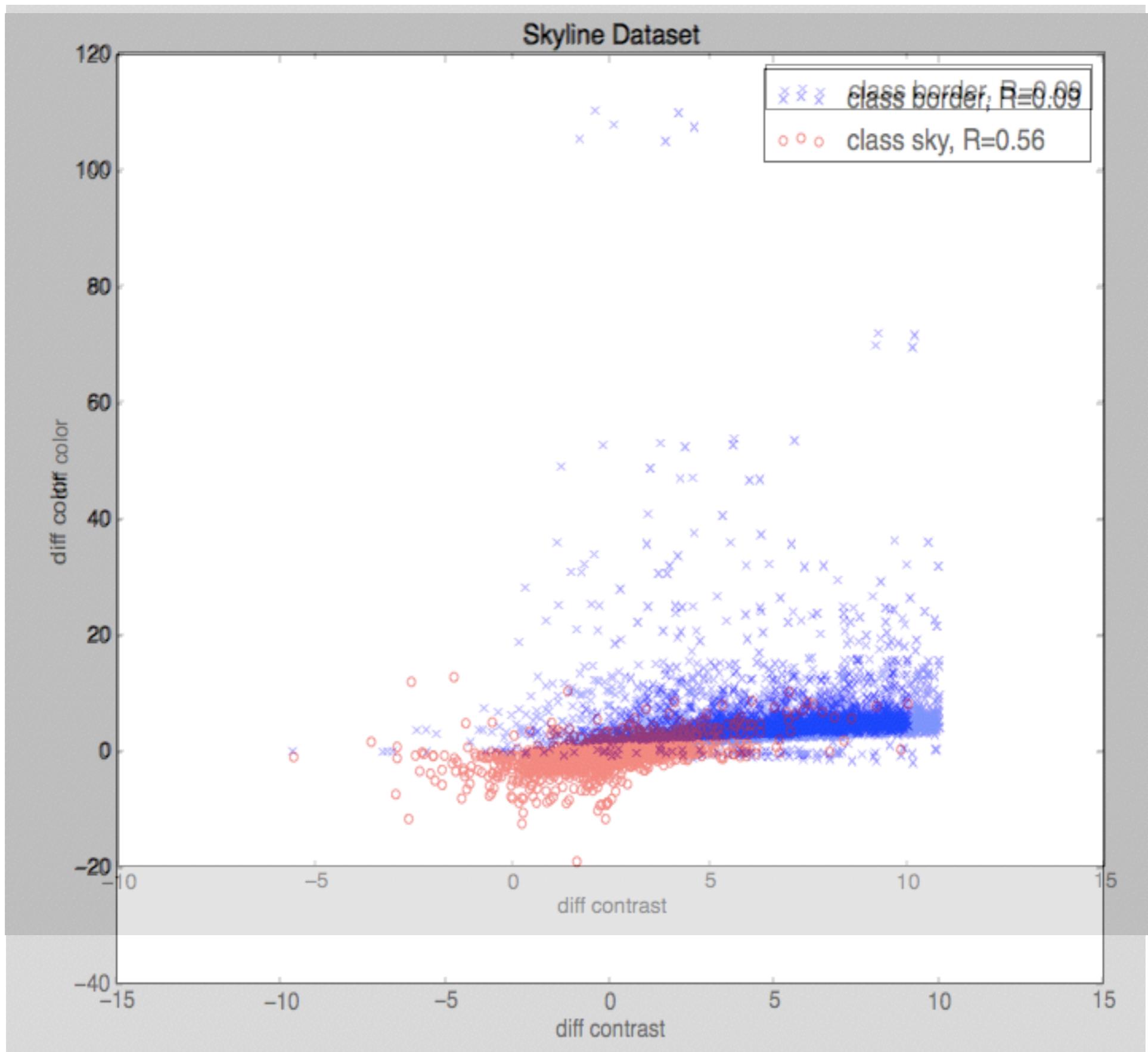
All RED SKY data in one



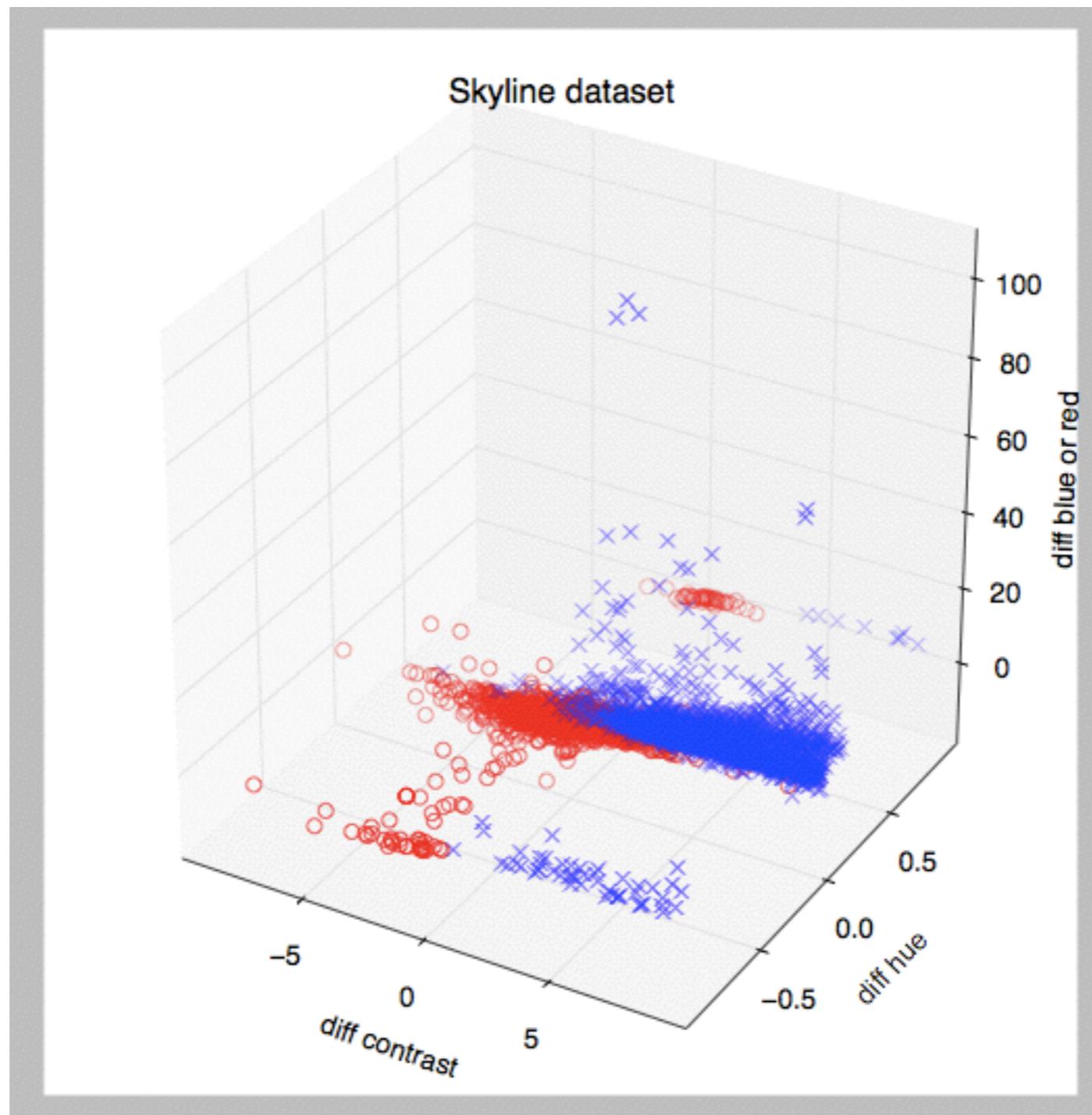
All RED SKY data in one



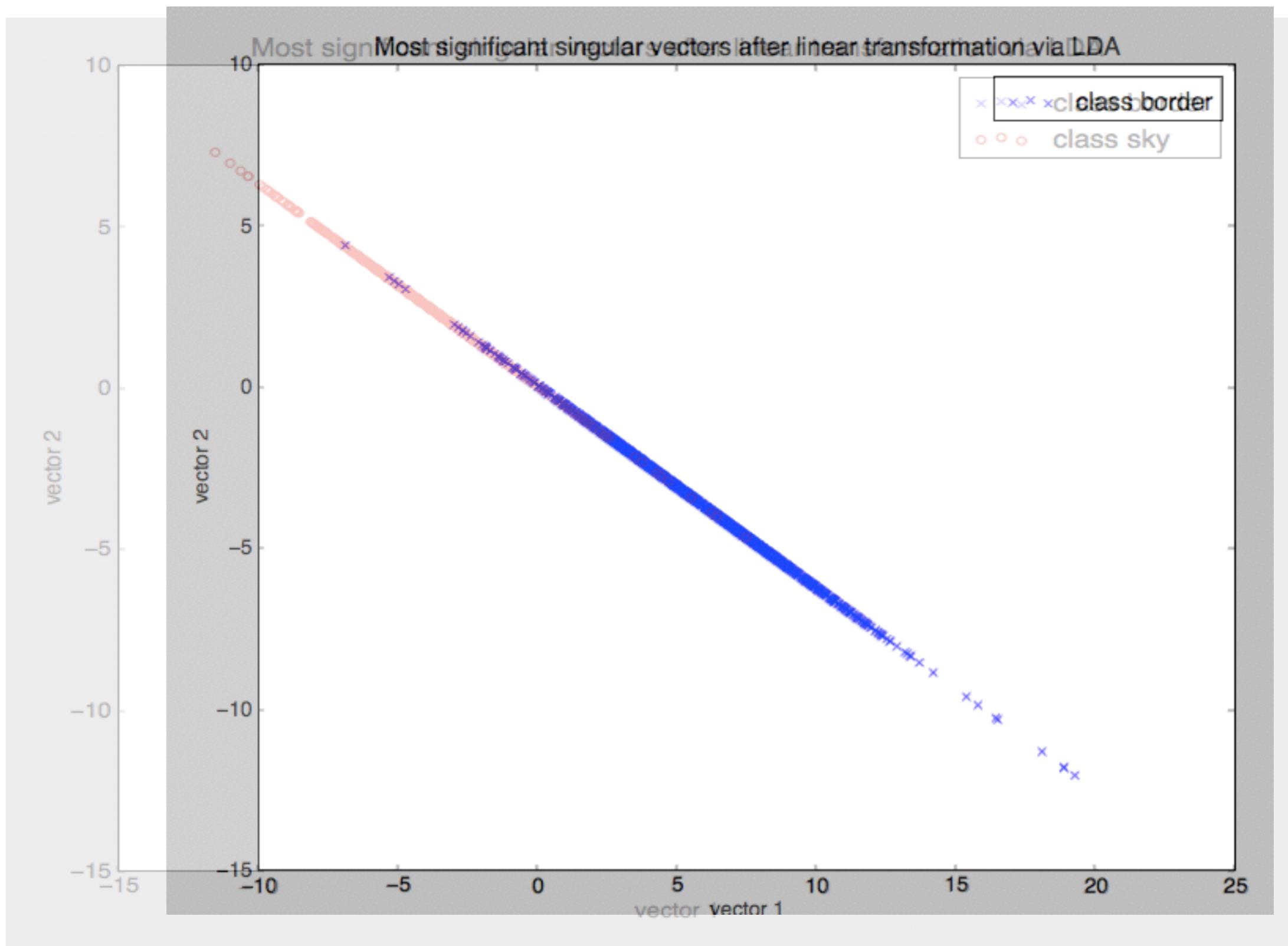
All RED SKY data in one



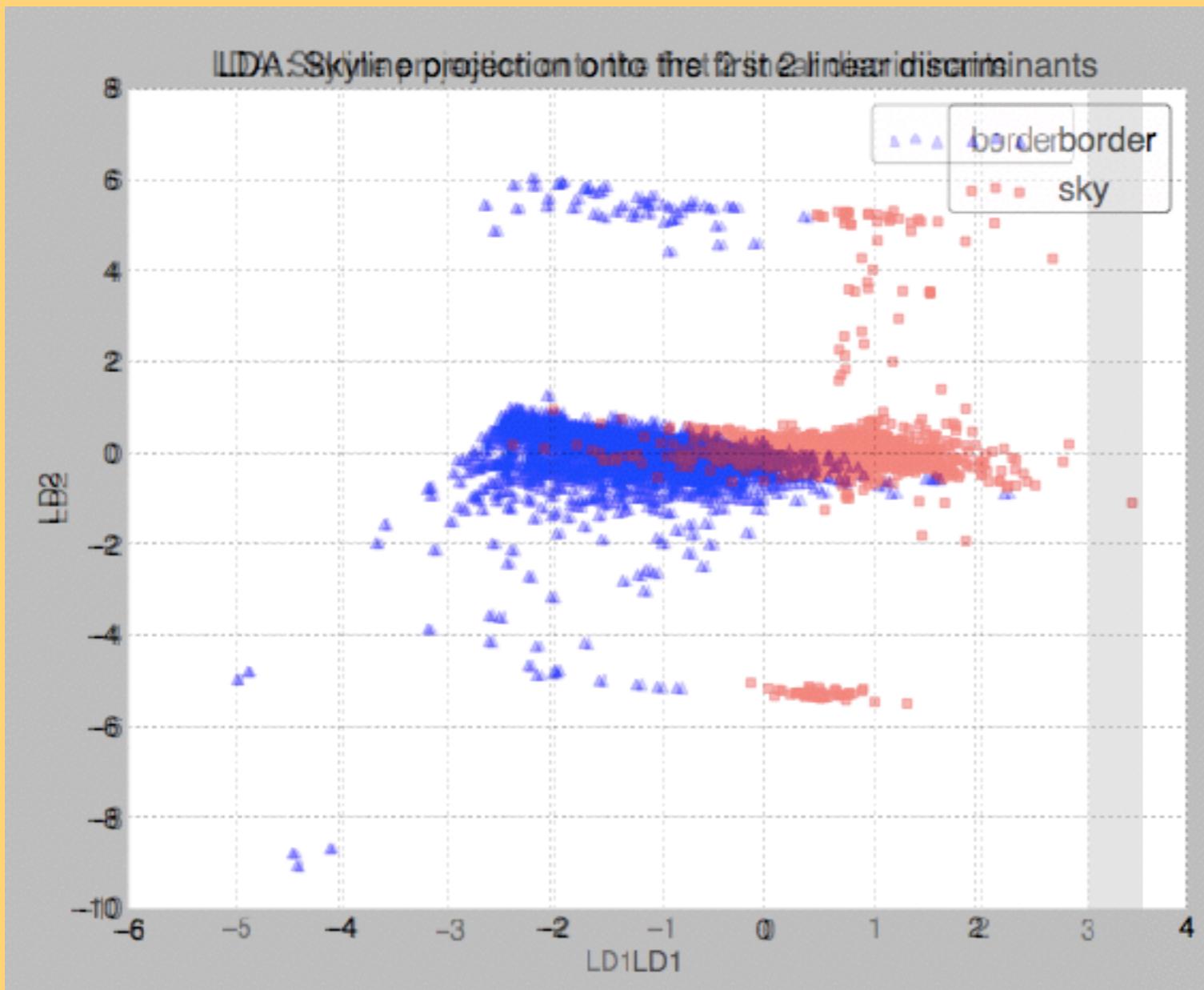
All RED SKY data in one



All RED SKY data in one,



All RED SKY data in one, filtered for $\text{math.abs}(\text{contrastDiff}) > 1$ AND $\text{math.abs}(\text{blueOrRedDiff}) > 1$ for border points and the opposite for sky points:



unfortunately, not separable when all blue sky image data is combined

contrast	hue	BorR
Mean Vector class 1: [1.0824	0.1032	0.7375]
Mean Vector class 2: [-0.6573	-0.0627	-0.4479]
('within-class Scatter Matrix:\n', array([[1809.2505, 175.4663, 476.6231],		
[175.4663, 6229.4697, 77.5903],		
[476.6231, 77.5903, 4199.1555]]))		
('between-class Scatter Matrix:\n', array([[13799.5234, 1692.8768, 9535.2608],		
[1692.8768, 538.8659, 1286.4054],		
[9535.2608, 1286.4054, 6629.8085]]))		
Eigenvector 1:		
[[-0.9805]		
[-0.0072]		
[-0.1964]]		
Eigenvalue 1: 8.25e+00		
Eigenvector 2:		
[[-0.5214]		
[-0.2835]		
[0.8049]]		
Eigenvalue 2: -2.90e-16		
Eigenvector 3:		
[[0.3829]		
[-0.8305]		
[-0.4044]]		
Eigenvalue 3: 6.22e-02		
ok		
Eigenvalues in decreasing order:		
8.24847354789		
0.062191641456		
2.89500454678e-16		
Variance explained:		
eigenvalue 1: 99.25%		
eigenvalue 2: 0.75%		
eigenvalue 3: 0.00%		
('Matrix W:\n', array([[-0.9805, -0.0072, -0.1964],		
[0.3829, -0.8305, -0.4044]]))		