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WIR SCHAFFEN WISSEN – HEUTE FÜR MORGEN

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## $a_\mu$ : Beyond the Standard Model

Seattle, 09.09.2019

- Introduction: Searching for new physics with flavour
- Explaining the anomalous magnetic moment of the muon with new physics
- $a_\mu$  and consequences for future measurements
- Correlations with the electron AMM and implications for the muon EDM
- Further Flavour anomalies and future prospects

- Dark Matter existence established at cosmological scales
  - New weakly interacting particles
- Neutrinos not exactly massless
  - Right-handed (sterile) neutrinos
- Matter anti-matter asymmetry
  - Additional CP violating interactions

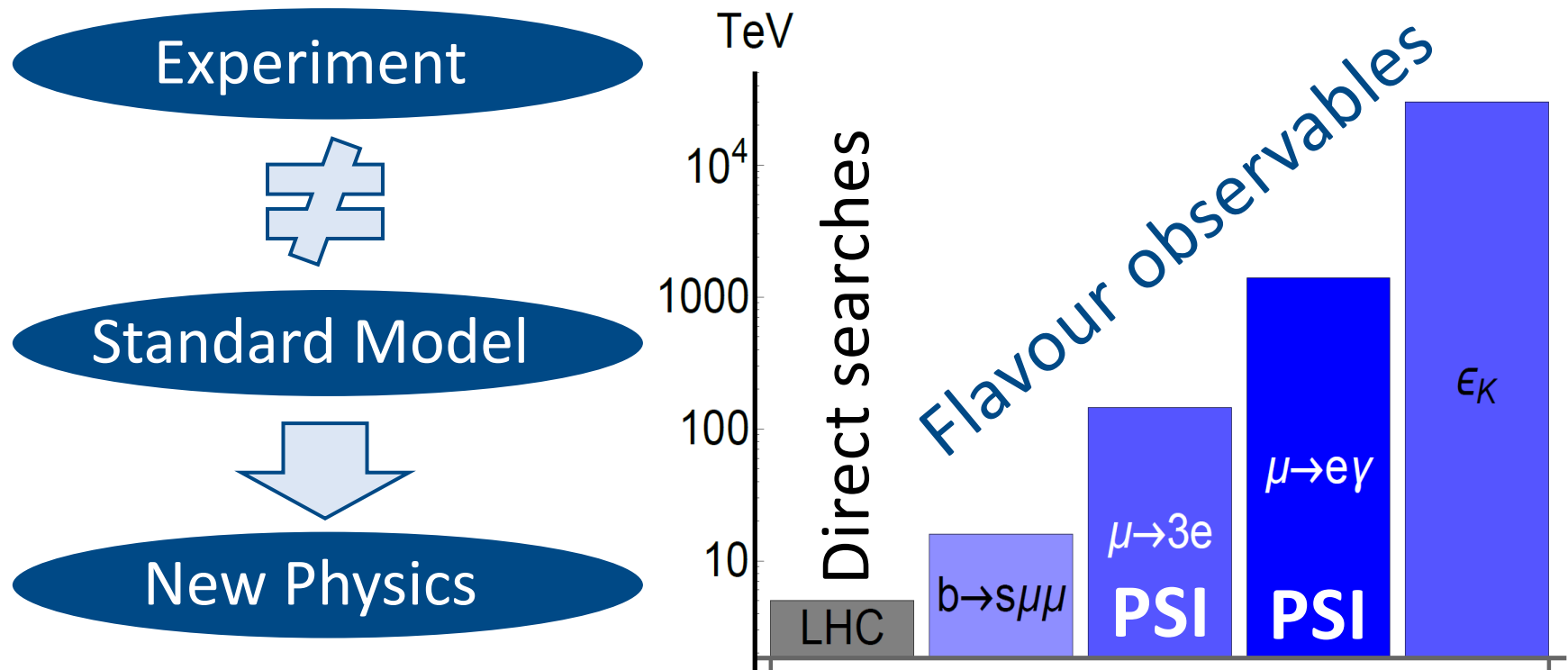
New  
particles  
and  
interactions  
exist!

The SM must be extended!  
What is the underlying fundamental theory?

# Finding New Physics with Flavour



- At colliders one produces many (up to  $10^{14}$ ) heavy quarks or leptons and measures their decays into light flavours

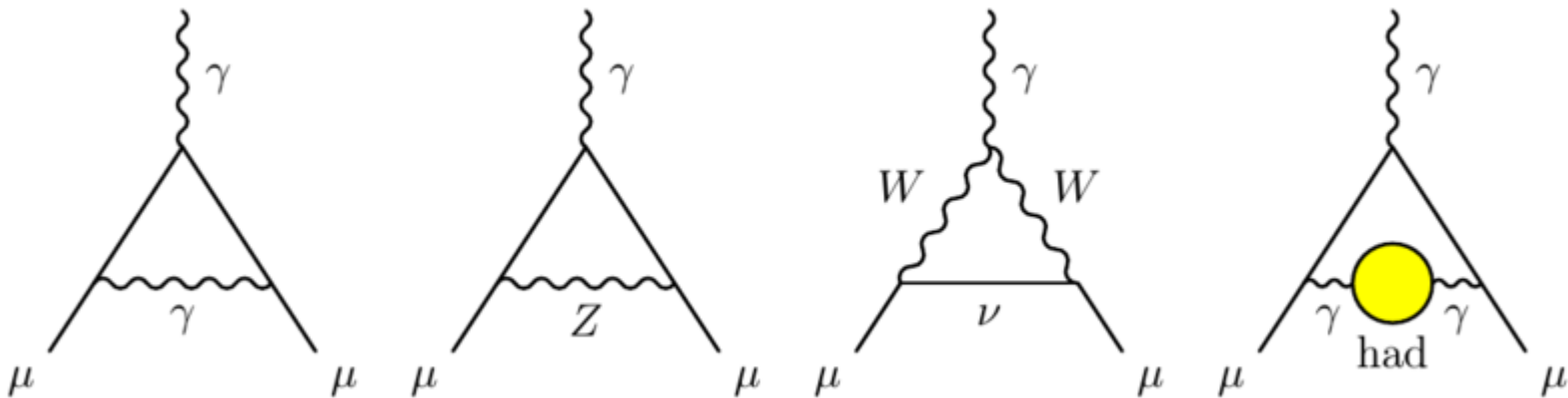


Flavour observables are sensitive to higher energy scales than collider searches

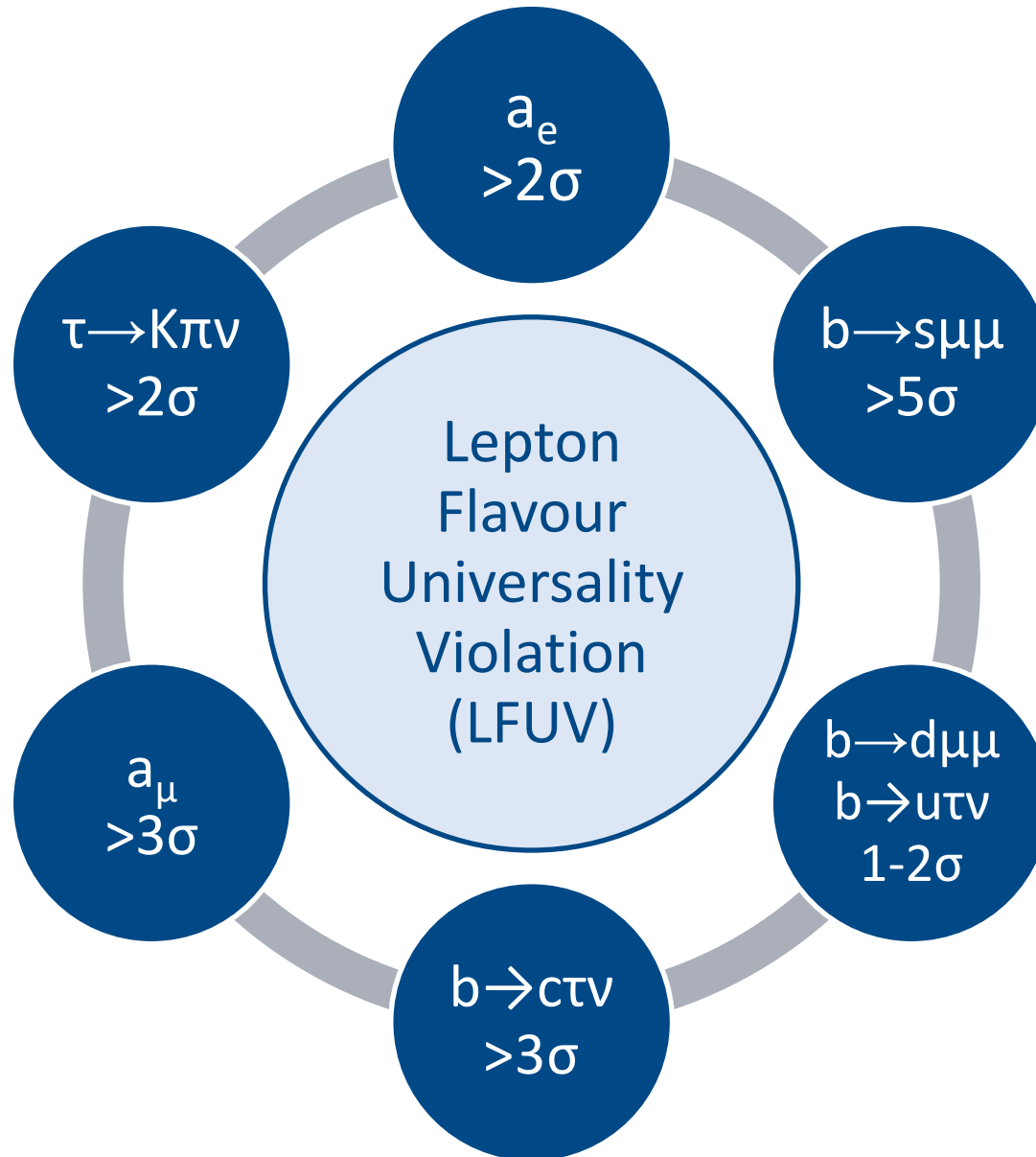
- Single measurement from BNL
- Theory prediction sound but challenging because of hadronic effects **this workshop**

$$\Delta a_\mu \approx 270(85) \times 10^{-11}$$

- Soon new experimental results from Fermilab



3 $\sigma$  deviation (order of SM-EW contribution)



Probability  
for  
statistical  
fluctuation  
< 0.0001%

$\varepsilon'/\varepsilon$   
 $\approx 3\sigma$

$B \rightarrow K\pi$   
 $> 2\sigma$

- Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = c_R^{\ell_f \ell_i} \bar{\ell}_f \sigma_{\mu\nu} P_R \ell_i F^{\mu\nu} + \text{h.c.}$$

- Anomalous magnetic moment

$$a_{\ell_i} = -\frac{4m_{\ell_i}}{e} \text{Re } c_R^{\ell_i \ell_i}$$

- Electric Dipole moment

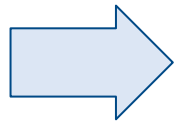
$$d_{\ell_i} = -2 \text{Im } c_R^{\ell_i \ell_i}$$

- Radiative Lepton decays

$$\text{Br}[\mu \rightarrow e\gamma] = \frac{m_\mu^3}{4\pi \Gamma_\mu} (|c_R^{e\mu}|^2 + |c_R^{\mu e}|^2)$$

Processes intrinsically connected

- Effect of the order of the EW-SM contribution needed



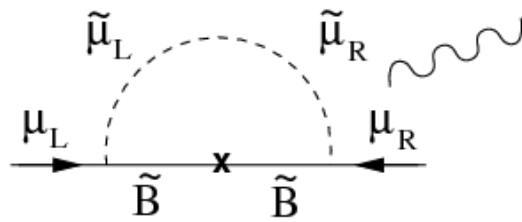
enhancement necessary

- Light particles
  - Neutral scalars
  - Neutral vector ( $Z'$  Dark Photon)
  - ALP (axion like particle)
- Chiral enhancement: Chirality flip does not come from the muon mass but rather from a NP mass inside the loop

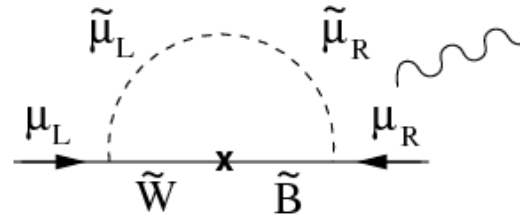
Huge  
literature

Light particles or/and chiral enhancement

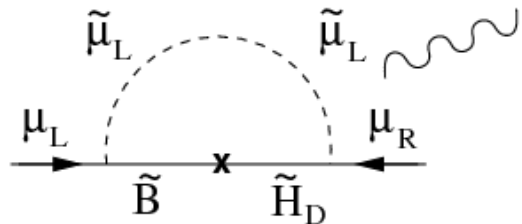




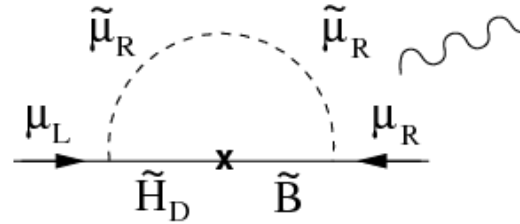
(a)



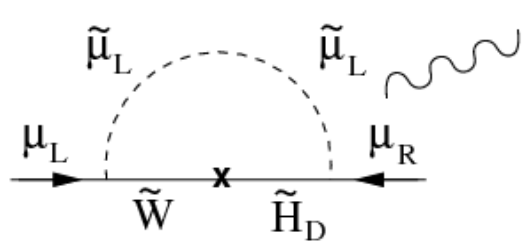
(b)



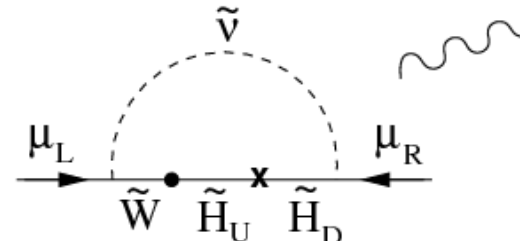
(c)



(d)



(e)

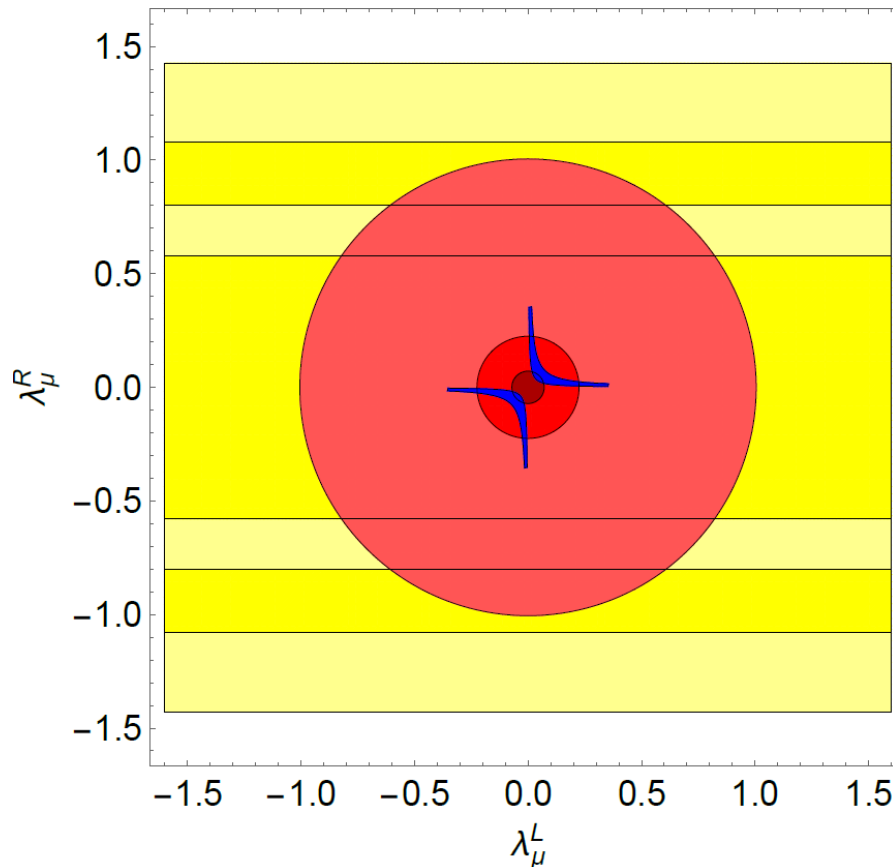


(f)

e.g. D. Stockinger,  
hep-ph/0609168

$\tan(\beta)$  enhanced slepton and sneutrino loops

## ■ Chirally enhanced effects via top-loops



- $B \rightarrow K^* \nu \nu$
- $B \rightarrow K^* \nu \nu$  (BELLE II)
- $Z \rightarrow \mu \mu$  (LEP)
- $Z \rightarrow \mu \mu$  (GigaZ)
- $Z \rightarrow \mu \mu$  (TLEP)
- $a_\mu(2\sigma)$
- $b \rightarrow s \mu \mu$

$$\lambda_\mu^{L,R}$$

Left-, right-  
handed  
muons-top  
coupling

E. Leskow, A.C., G. D'Ambrosio, D. Müller  
arXiv:1612.06858

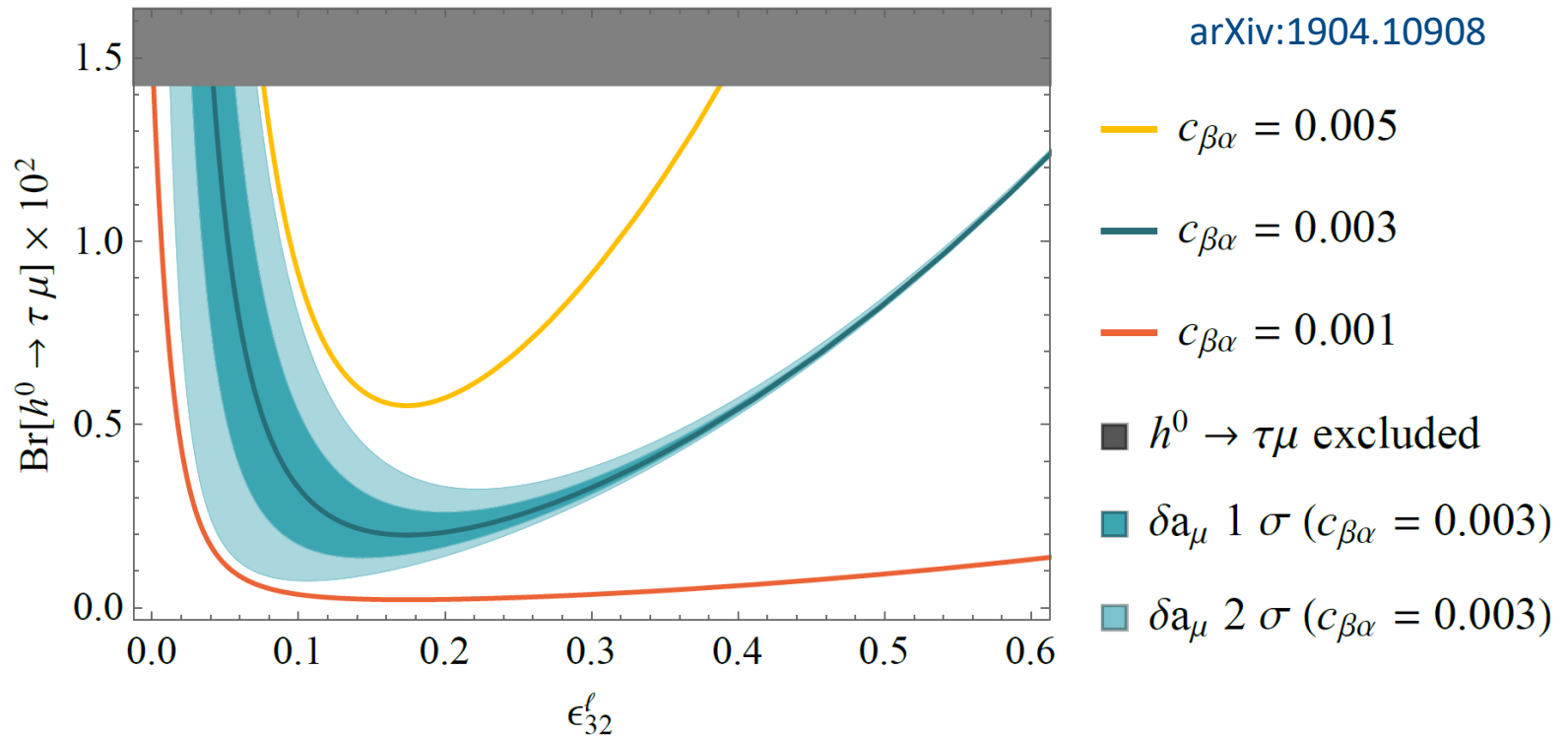
P. Arnan, D. Becirevic, F. Mescia, O. Sumensari,  
arXiv:1901.06315 [hep-ph]

$Z \rightarrow \mu \mu$  at future colliders

## ■ Chirally enhancement of $m_\tau/m_\mu$

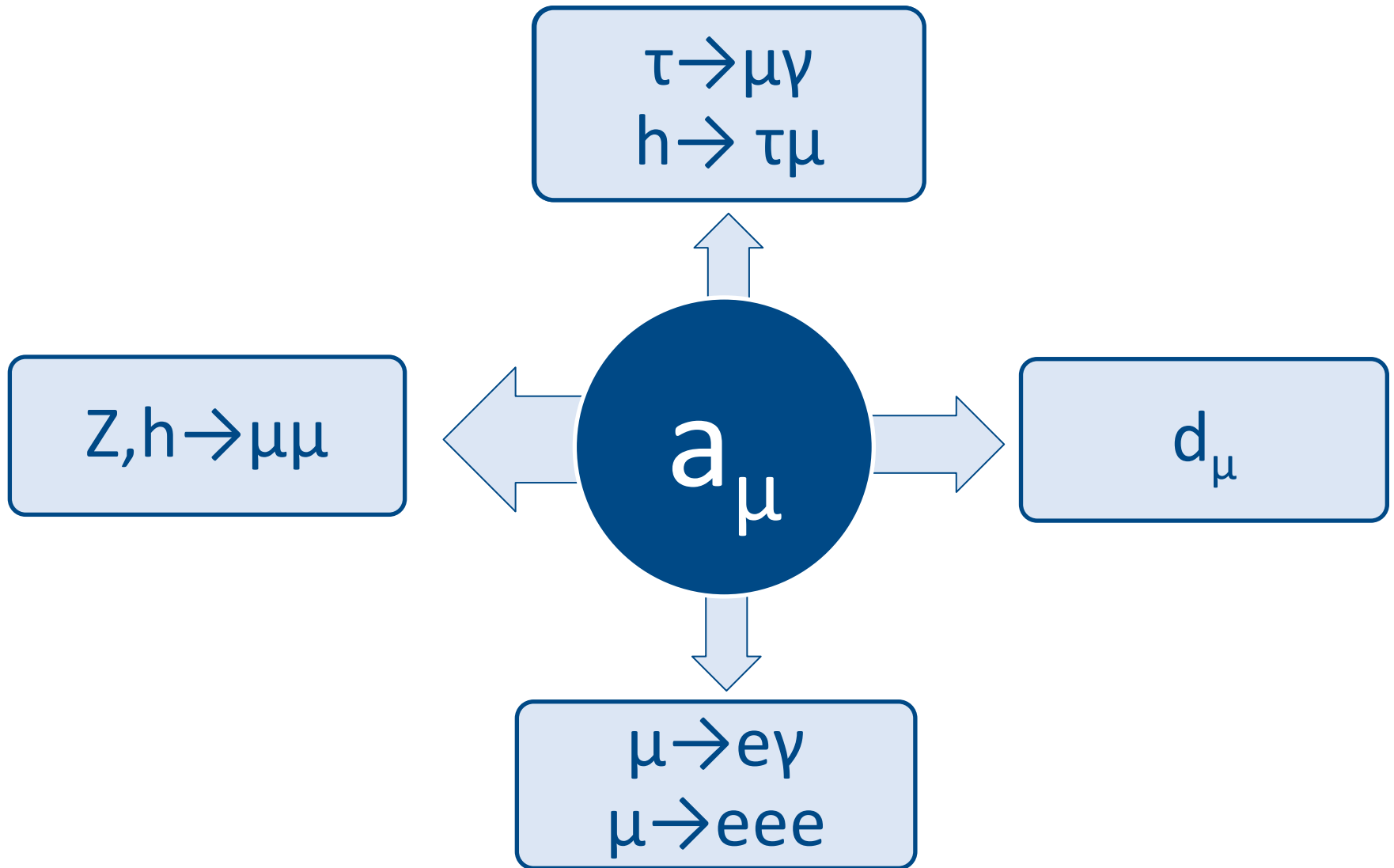
AC, D. Müller, C. Wiegand  
arXiv:1903.10440

Y. Abe, T. Toma, K. Tsumura  
arXiv:1904.10908



Unavoidable constraints from  $h \rightarrow \tau \mu$

# Future Implications of $a_\mu$



# Correlations with the AMM of the electron

AC, M. Hoferichter, P. Schmidt-Wellenburg, arXiv:1807.11484

See also

H. Davoudiasl, W. J. Marciano, arXiv:1806.10252

Jia Liu, Carlos E.M. Wagner, Xiao-Ping Wang, arXiv:1810.11028

...

- AMM usually used to determine  $\alpha$
- With *now* best determination of  $\alpha$  from Cs atoms

$$a_e^{\text{SM}}|_{\alpha_{\text{Cs}}} = 1,159,652,181.61(23) \times 10^{-12}$$

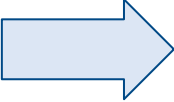

- Compared to the electron AMM measurement

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = -0.88(36) \times 10^{-12}$$

- Normalized to the lepton mass

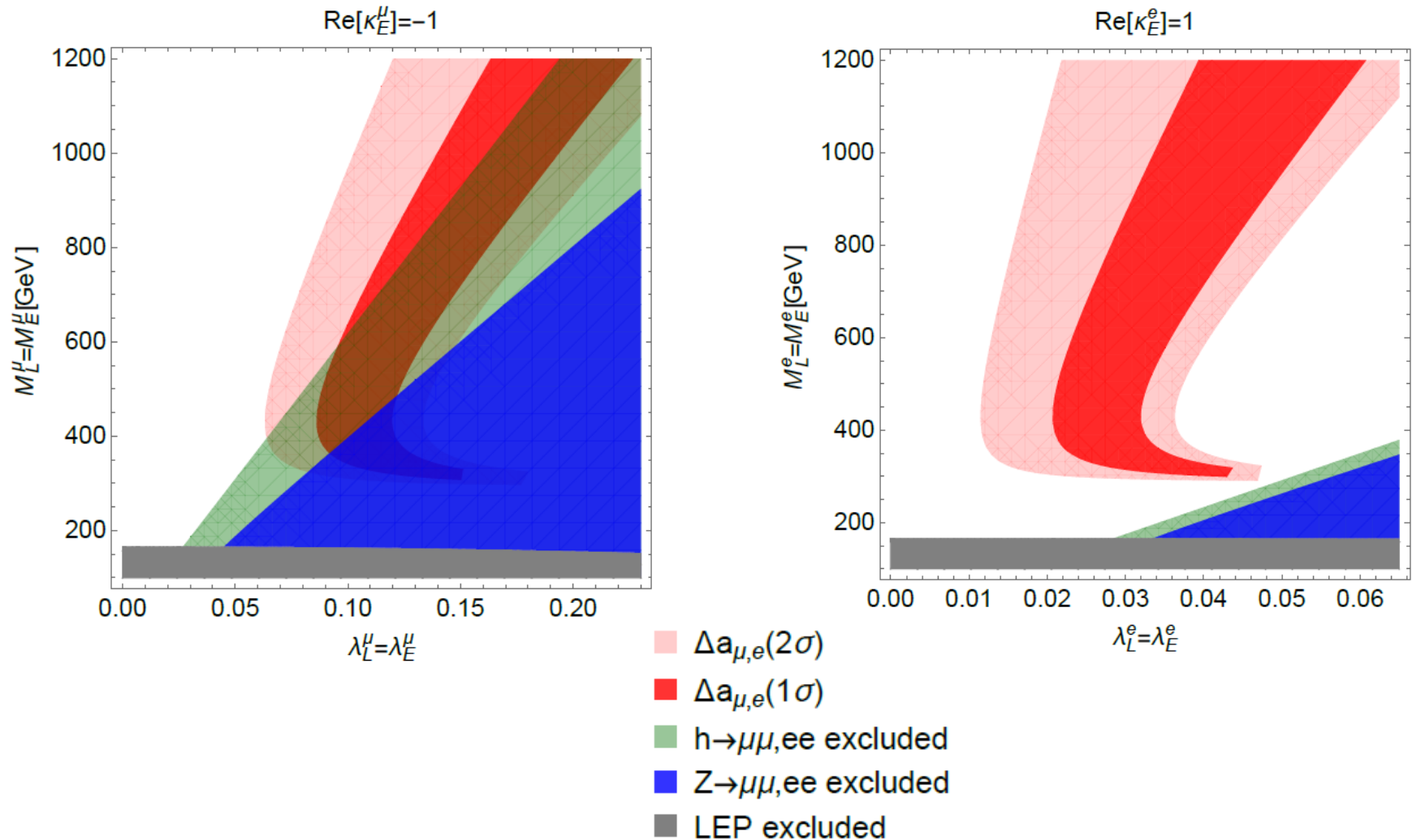
$$-3 \leq \frac{\Delta a_\mu}{m_\mu} \bigg/ \frac{\Delta a_e}{m_e} \leq -130 \quad \text{or} \quad -0.006 \leq \frac{\Delta a_\mu}{m_\mu^2} \bigg/ \frac{\Delta a_e}{m_e^2} \leq -0.26$$

2.5  $\sigma$  deviation with opposite sign than  $a_\mu$

- Opposite sign:  no single light mediator
- No Minimal Flavour Violation:  
$$\Delta a_\mu / \Delta a_e \neq m_\mu^2 / m_e^2$$
  
 generic flavour structure
- New physics with common couplings to  $\mu$  and  $e$   
$$\text{Br}[\mu \rightarrow e\gamma] = \frac{\alpha m_\mu^2}{16 m_e \Gamma_\mu} |\Delta a_\mu \Delta a_e| \sim 8 \times 10^{-5}$$
  
8 orders of magnitude too large

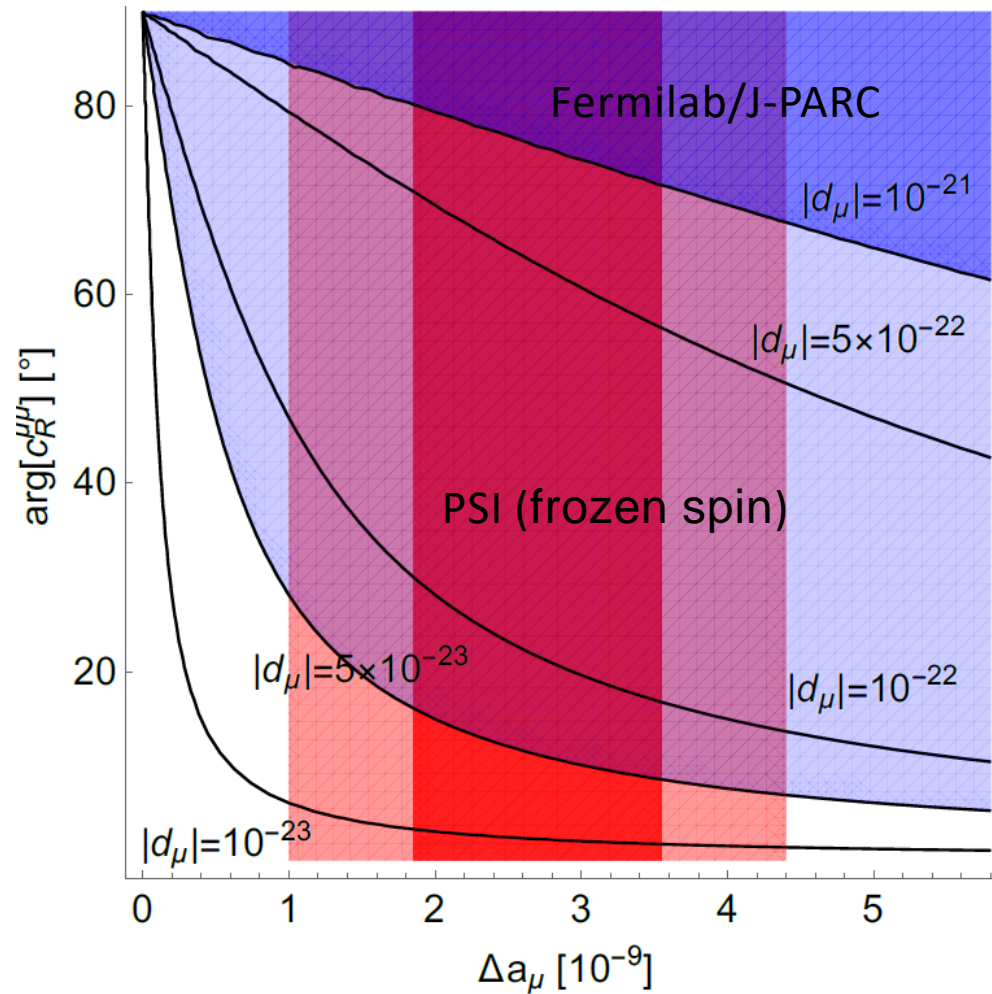
**Muon and electron sector must be decoupled**

# Model with new vector-like leptons



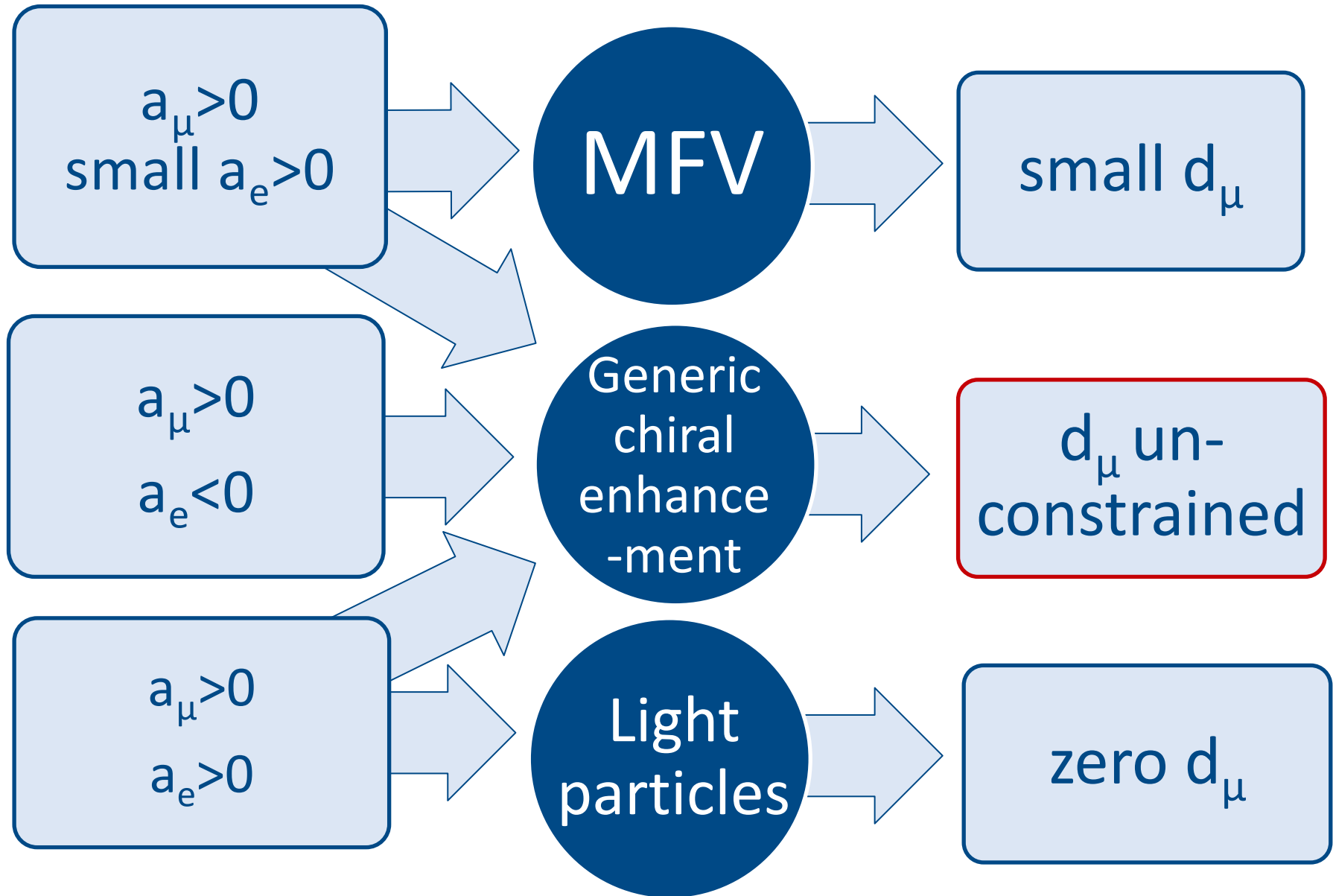
Works for  $a_e$  but tension with  $a_\mu$



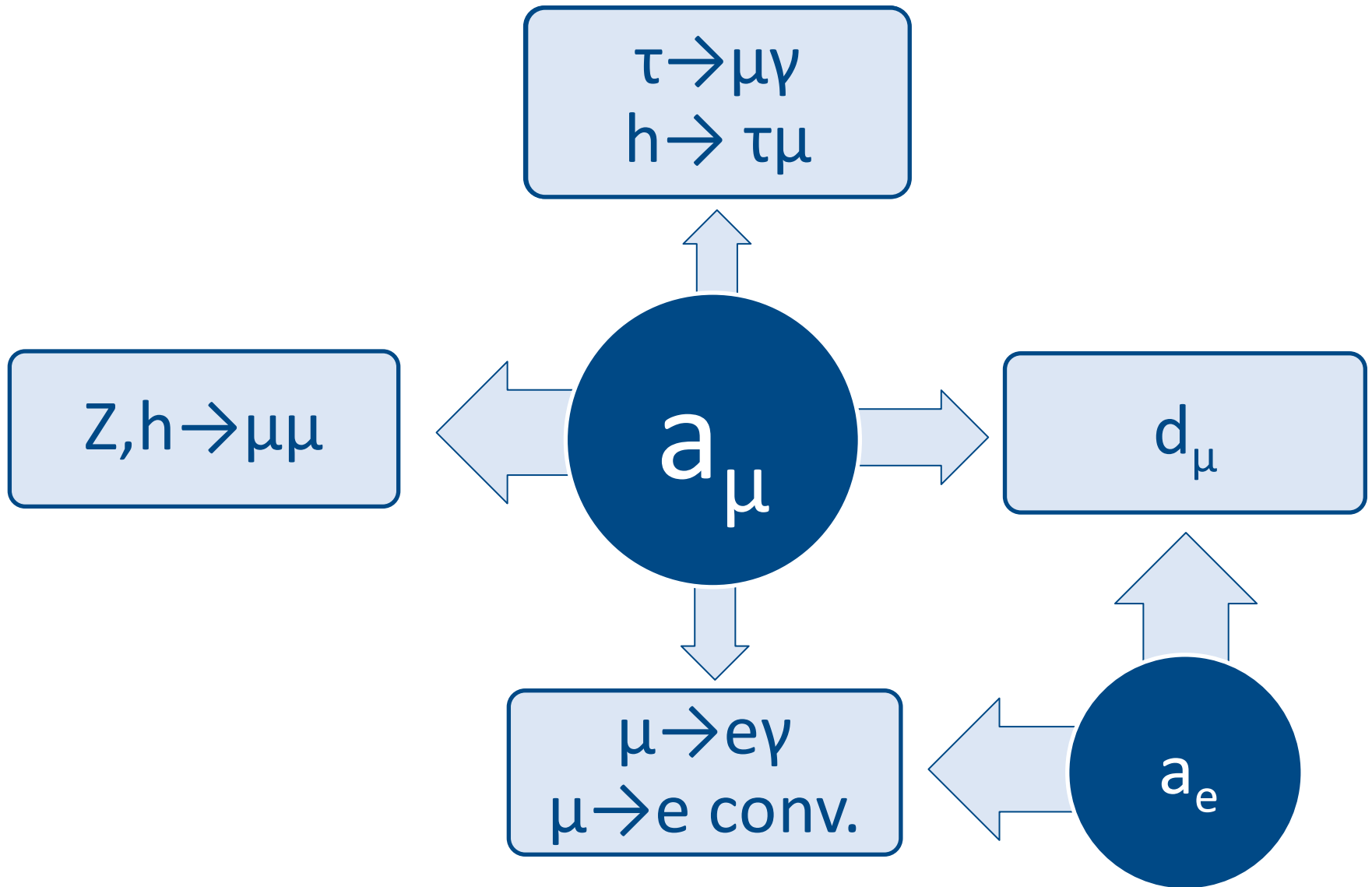


Dedicated experiment needed?

# Implications for Muon EDM



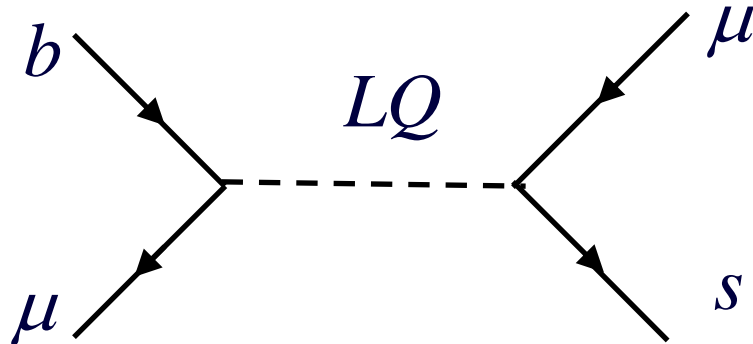
# Future Implications of $a_\mu$





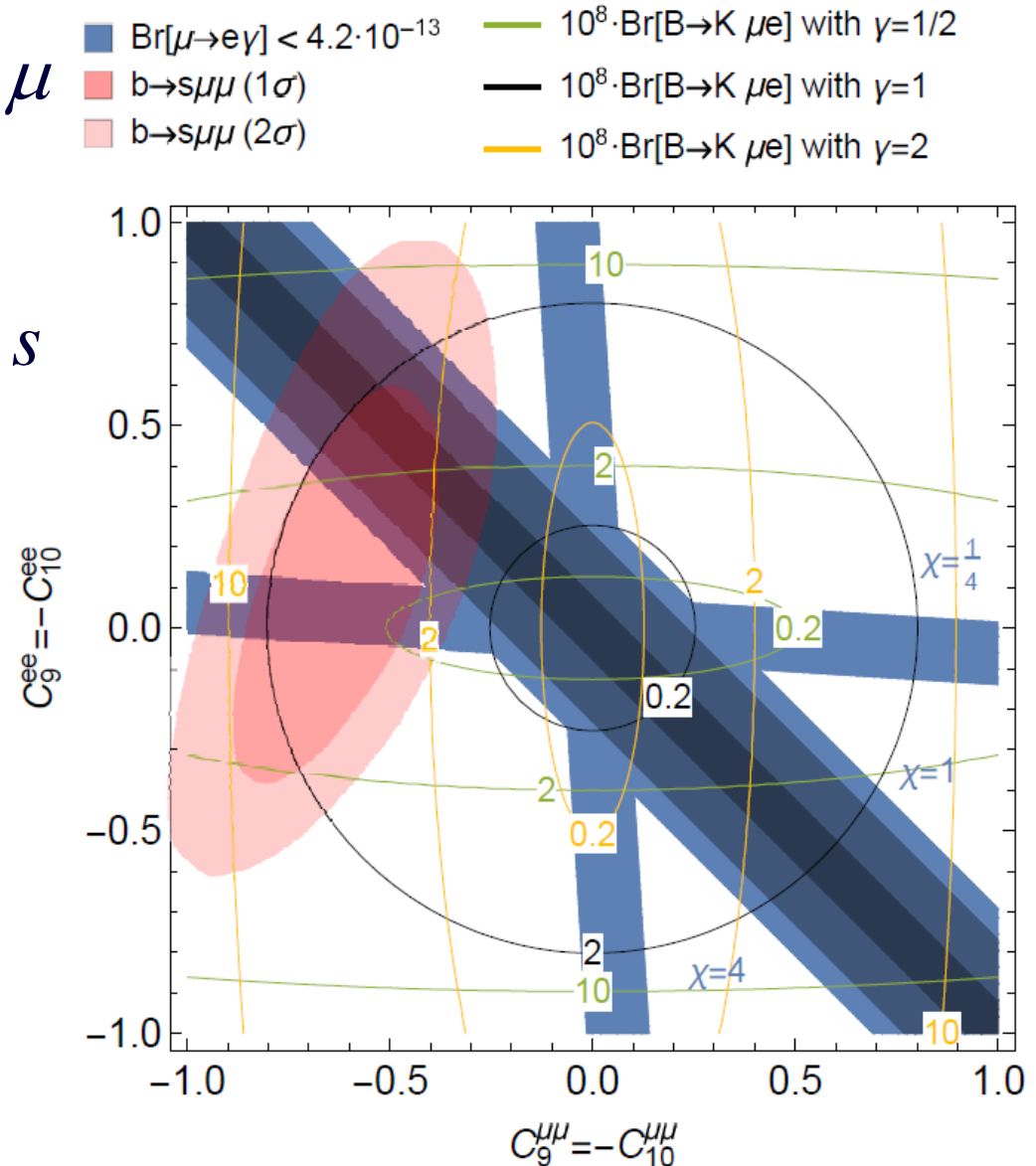
# Including LFVU in $b \rightarrow sll$

# $b \rightarrow s \mu^+ \mu^-$ : Leptoquarks

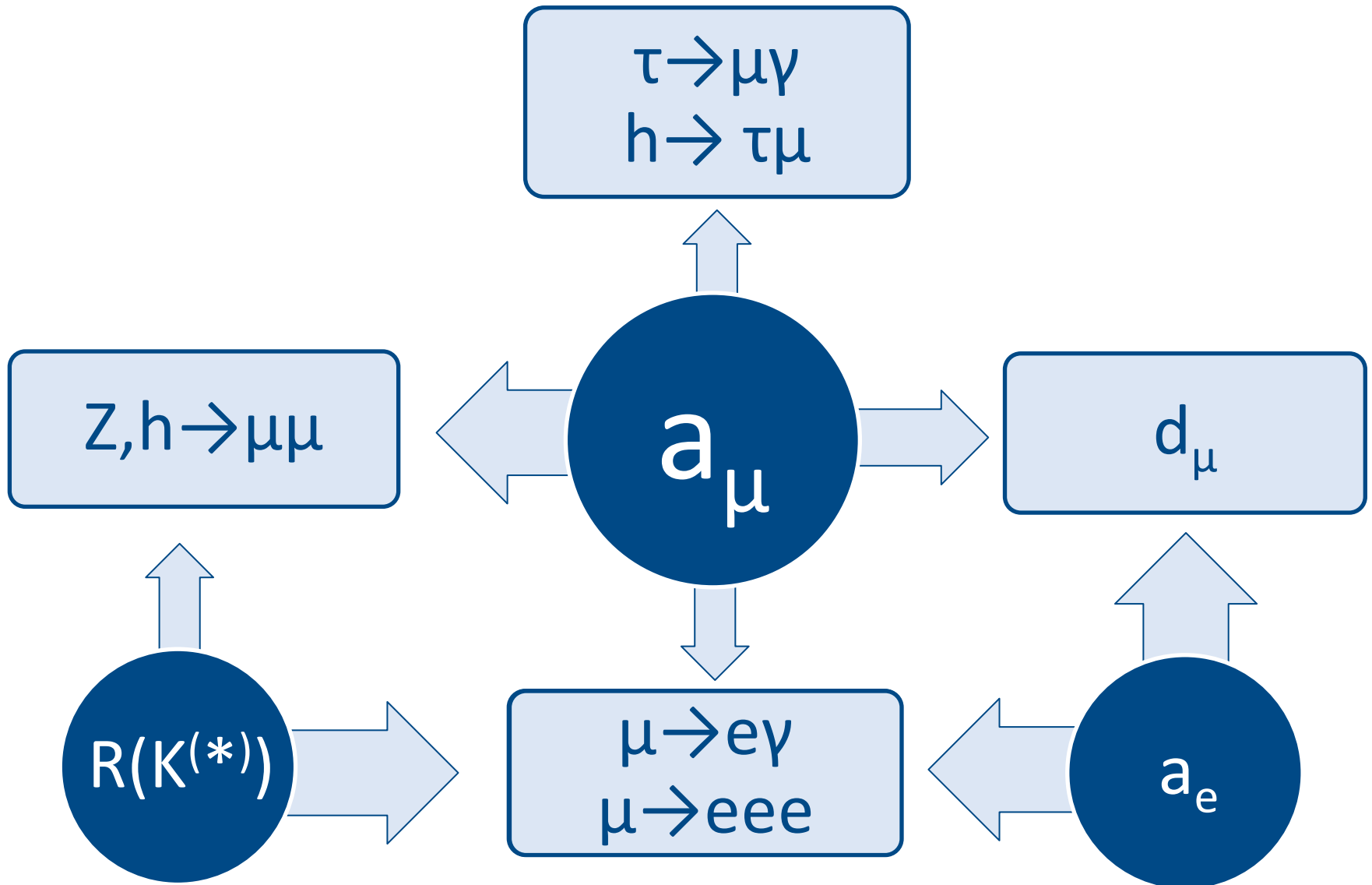


- Small effect in  $B_s$  mixing

Lepton flavour violation

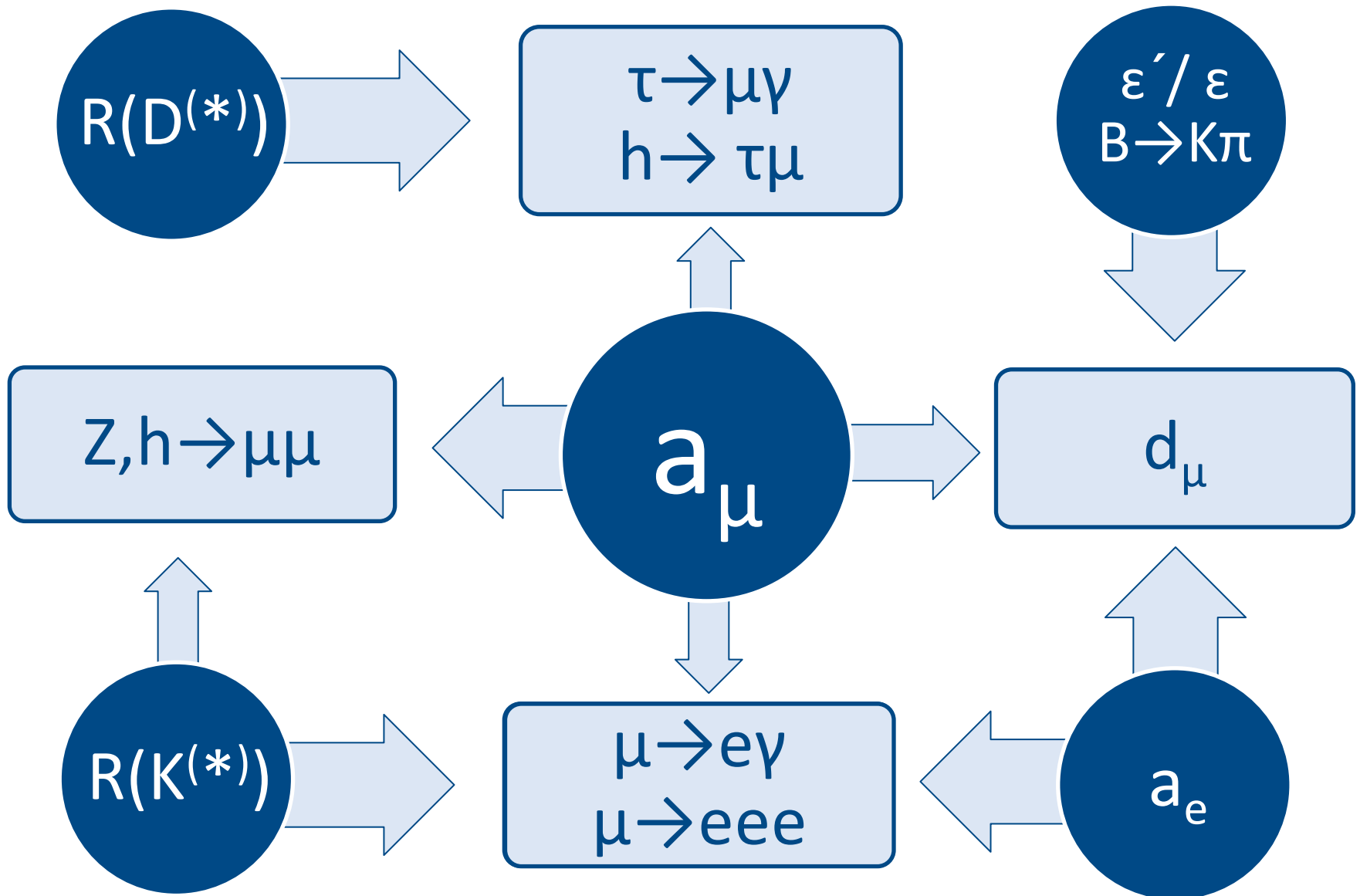


# Future directions



Many more  
such possible  
correlations...

# Future directions





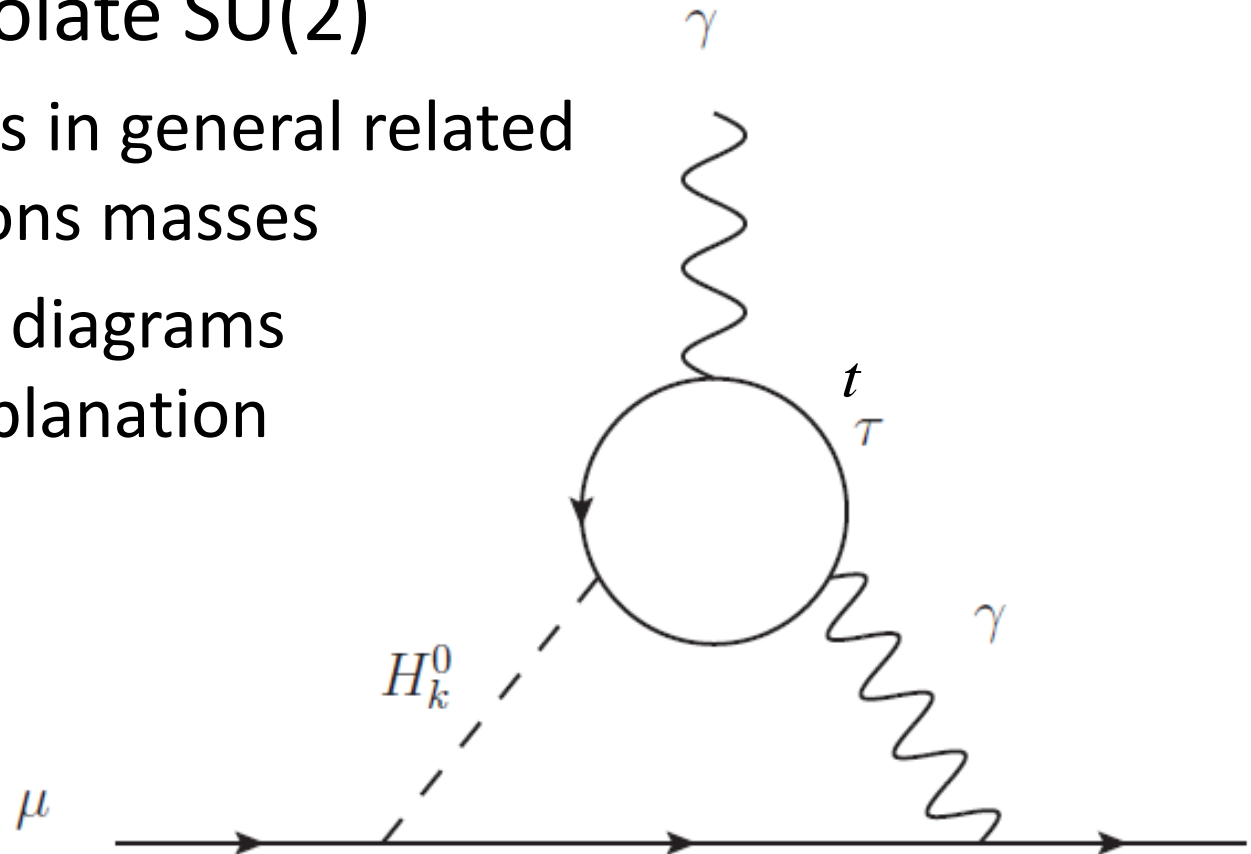
# Backup

- MSSM
  - Constrained MFV does not work
  - With generic A-terms has problem with vacuum stability
  - With large  $\tan(\beta)$  and flavour violation
- 2HDMs & LQs: Problems with  $\mu \rightarrow e\gamma$
- Extra dimensions
  - Can only explain the muon or the electron AMM because of  $\mu \rightarrow e\gamma$

Most popular models do not work

## ■ Scalars: violate SU(2)

- Couplings in general related to fermions masses
- Barr-Zee diagrams make explanation possible



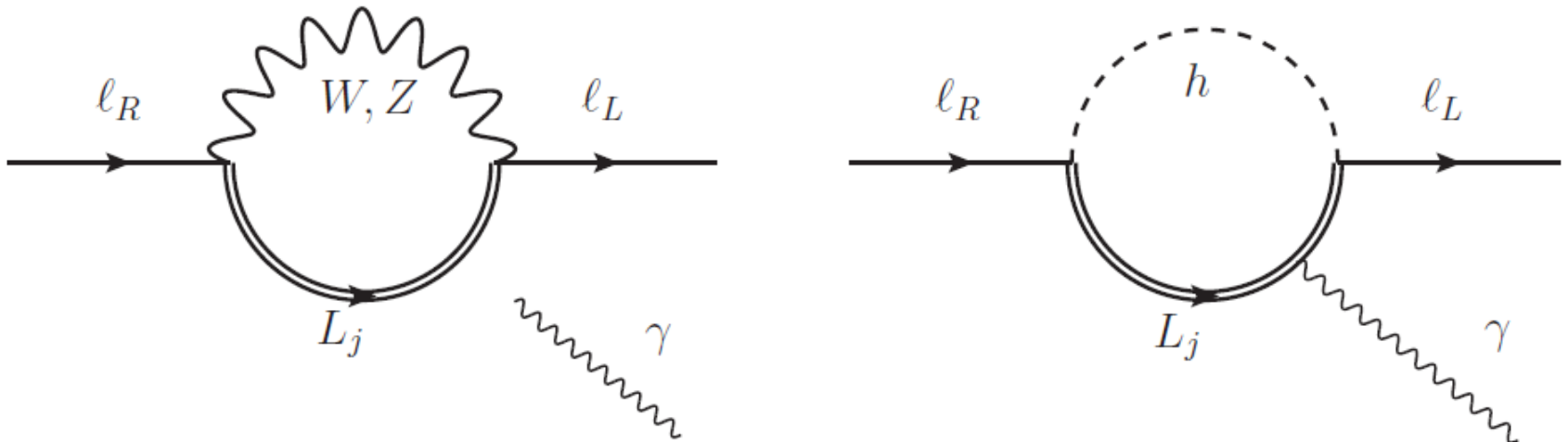
Explanation difficult but possible

- Add neutral scalar
  - Effect in  $a_\mu$  possible without affecting  $h \rightarrow \mu\mu$
- Impose abelian flavour symmetry (e.g.  $L_\mu - L_\tau$ ) in order to avoid  $\mu \rightarrow e\gamma$
- More minimal model with one generation of vector-like fermions possible if  $a_e$  is explained by the SM Higgs and  $a_\mu$  via a new scalar
- New scalar could be  $L_\mu - L_\tau$  flavon

Many realizations possible

$$\mathcal{L}_M = -M_L \bar{L}_L L_R - M_E \bar{E}_L E_R + \text{h.c.},$$

$$\begin{aligned} \mathcal{L}_H = & -\kappa_L \bar{L}_L H E_R - \kappa_E \bar{L}_R H E_L \\ & - \lambda_L \bar{L}_L \ell_R H - \lambda_E \bar{E}_R \tilde{H} \ell_L + \text{h.c.} \end{aligned}$$



Chirally enhanced by  $v\kappa_{L,R}/m_\mu$

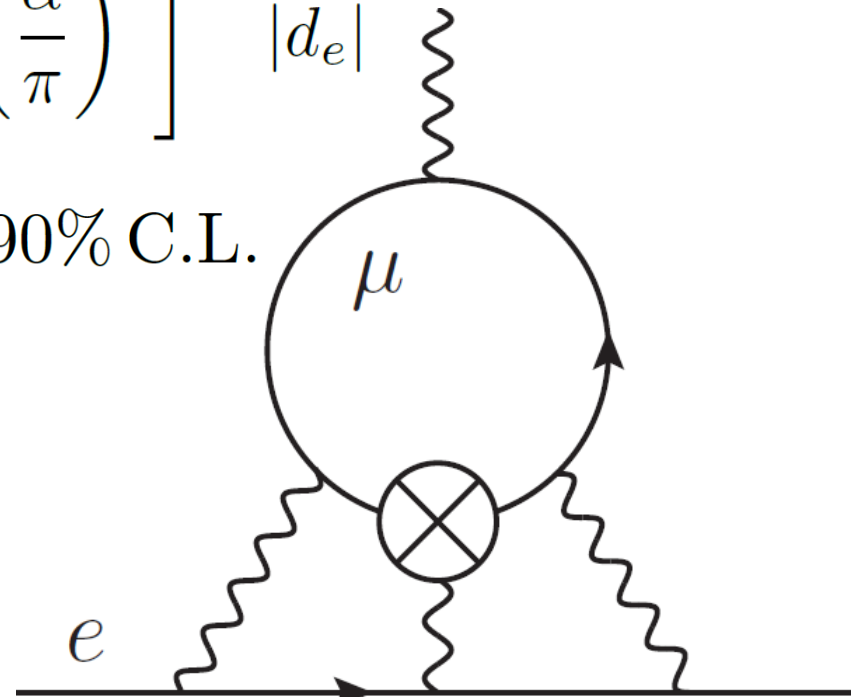
- MFV:
- Contribution only starts at the 3-loop level

$$|d_\mu| \leq \left[ \left( \frac{15}{4} \zeta(3) - \frac{31}{12} \right) \frac{m_e}{m_\mu} \left( \frac{\alpha}{\pi} \right)^3 \right]^{-1} |d_e|$$

$$|d_\mu| \leq 0.9 \times 10^{-19} e \text{ cm} \quad 90\% \text{ C.L.}$$

- Direct limit

$$|d_\mu| < 1.5 \times 10^{-19} e \text{ cm}$$



Improvement of direct limit important

- Enhancement by the mass of the fermion in the loop

$$c_R^{fi} = \frac{e}{16\pi^2} \Gamma_\Psi^{\mu L*} \Gamma_\Psi^{\mu R} M_\Psi \frac{f\left(\frac{M_\Psi^2}{M^2}\right) + Qg\left(\frac{M_\Psi^2}{M^2}\right)}{M^2}$$

$Q, M_\Psi$  = charge, mass of the fermion       $f, g$  = loop functions

- MSSM:  $(\tan(\beta))$
- Leptoquarks:  $m_t/m_\mu$
- Model with vector like fermions:  $m_\Psi/m_\mu$

Enhancement from new sources of EW breaking

# $L_\mu$ - $L_\tau$ model for $a_\mu$ and $h \rightarrow \tau\mu$

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W. Altmannshofer, M. Carena, AC, 1604.08221

- $L_\mu$ - $L_\tau$  flavour symmetry
- Flavon mixes with the Higgs
- $\tau \rightarrow \mu\gamma$  is protected
- $a_\mu$  is not protected
- Effects in  $h \rightarrow \mu\mu$

