

BOSTON UNIVERSITY
GRADUATE SCHOOL OF ARTS AND SCIENCES

Dissertation

**MEASUREMENT OF THE ANOMALOUS MAGNETIC
MOMENT OF THE POSITIVE MUON TO .SOMETHING
PARTS PER BILLION**

by

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Dedication

I dedicate this thesis to

Acknowledgments

Here go all your acknowledgments. You know, your advisor, funding agency, lab mates, etc., and of course your family.

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Janusz Konrad
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(Order No.)

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Boston University, Graduate School of Arts and Sciences, 2019

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ABSTRACT

Have you ever wondered why this is called an *abstract*? Weird thing is that its legal to cite the abstract of a dissertation alone, apart from the rest of the manuscript.

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List of Abbreviations

ppm	parts per million
ppb	parts per billion
BNL	Brookhaven National Laboratory
FNAL	Fermi National Accelerator Laboratory
SM	Standard Model
SiPM	Silicon Photo-Multiplier
Geane	Geometry and Error Propagation
Geant4	Geometry and Tracking 4

Chapter 1

Introduction

While the prevailing theory for particle physics, the Standard Model (SM), has had tremendous success in describing our universe, there exist unanswered questions. These namely include the matter-antimatter asymmetry, the source of mass for the neutrinos, the existence of dark matter, and more. Many particle physics experiments are being conducted around the world in order to shed light on these questions and round out our understanding of reality. One such particular experiment being conducted is the Fermilab Muon $g - 2$ Experiment (E989) underway at the Fermi National Accelerator Laboratory (FNAL) located in Batavia, Illinois. It has the goal of measuring the magnetic moment of the muon, proportional to the g in $g - 2$, to high precision in order to compare to SM theoretical predictions. Because the magnetic moment of particles couple to all existing particles, known or unknown, (source this? reference to a later section?) this provides an avenue through which theories might be constrained, and new physics narrowed down. Indeed this experiment is the latest in a line of such experiments which have measured the magnetic moment of the muon over the past several decades, the last of which measured the magnetic moment of the muon to .54 parts per million (ppm) at Brookhaven National Laboratory (BNL) in 2001 [1].

1.1 Background

The previous $g-2$ experiment at BNL measured a discrepancy in the magnetic moment of the muon between theory and experiment with a 2.2 - 2.7 standard deviation. (Cite the final report again?) That disagreement has since grown above 3σ [6], depending on the theoretical analysis approaches used.

1.1.1 Definitions

$$\vec{\mu} = g \frac{Qe}{2m} \vec{s} \quad (1.1)$$

$$a = \frac{g-2}{2} \quad (1.2)$$

-would it be worthwhile to include my derivation on the magnetic moment like in my hep presentation?

1.1.2 Experiment History

-do I want this? I'm sort of already talking about this for E821 in the intro and background - I don't think I want to go into the older experiments

1.2 Theory

1.2.1 QED

1.2.2 Weak

1.2.3 Hadronic

1.2.4 BSM

Chapter 2

Muon g-2 at Fermilab, E989

2.1 Principle Technique

In a dipole magnetic field, particles will orbit at the cyclotron frequency

$$\omega_c = -\frac{Qe}{\gamma m}B, \quad (2.1)$$

and their spins will turn at the precession frequency

$$\omega_s = -g\frac{Qe}{2m}B - (1 - \gamma)\frac{Qe}{\gamma m}B, \quad (2.2)$$

where $Q = \pm 1$ and $e > 0$. The difference between these two frequencies gives

$$\omega_a = \omega_s - \omega_c = -\frac{g - 2}{2}\frac{Qe}{m}B = -a\frac{Qe}{m}B, \quad (2.3)$$

a measureable frequency that is directly proportional to the property of significance, the anomaly a . By measuring the spin difference frequency for muons and the magnetic field B , a_μ can be determined. In the presence of an electric field, which is useful in storing the muon beam within a dipole magnetic field, this expands to

$$\vec{\omega}_a = -\frac{Qe}{m}[a_\mu \vec{B} - (a_\mu - \frac{1}{\gamma^2 - 1})(\vec{\beta} \times \vec{E})], \quad (2.4)$$

where now the measurable quantities are vector quantities. Finally, for realistic cases of muon momentum which is non-orthogonal to the magnetic field, the spin difference

frequency becomes

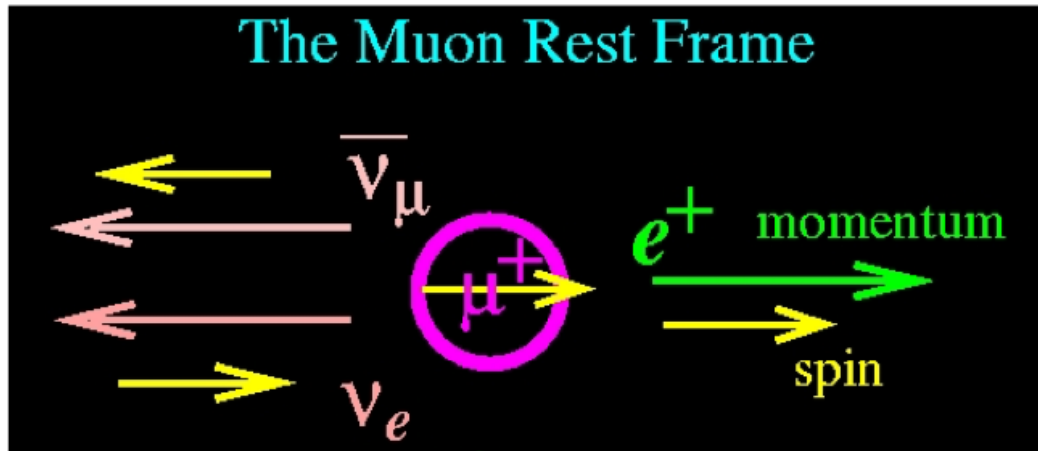
$$\vec{\omega}_a = -\frac{Qe}{m}[a_\mu \vec{B} - a_\mu \left(\frac{\gamma}{\gamma+1}\right)(\vec{\beta} \cdot \vec{B})\vec{B} - (a_\mu - \frac{1}{\gamma^2-1})(\vec{\beta} \times \vec{E})]. \quad (2.5)$$

If the motion of the muons is largely perpendicular to the magnetic field, then the second term is small and can be corrected for. If the particles have a momentum of approximately 3.09 GeV/c, the so called “magic momentum,” then the third term is small and can be corrected for. These will be talked about later.

In order to measure the spin difference frequency of the muon, a clever technique is used. Decay muons in the pion rest frame are 100% polarized due to conservation of angular momentum and the fact that the decay neutrino must have a specific helicity. Within a pion beam then the highest and lowest energy decay muons are polarized. Muons will decay to positrons with a lifetime of about 2.2 μ s, and the positrons with the highest energies will be correlated with the muon spin, a so called “self-analyzing” decay. The single available decay state for a maximum energy positron illustrates this in Figure 2.1. Thus, by acquiring a large sample of polarized muons and injecting them into a storage ring

-explain the physics -explain how we get at the physics with our ring and detectors
 -parity violation -actually write out the decay states before explaining some things -
 well shouldn't these have been talked about before?? maybe not -decay probabilities
 and all that -don't measure all decay positrons -By injecting a large ensemble of
 muons and -by measuring a subset of ensemble of muons.... -Careful with spin vs
 polarization

Figure 2.1: Make a new version of this picture, and improve this caption.: The single available decay state for maximum energy decay positrons. Due to the conservation of angular momentum and the single possible helicity states of the decay neutrino and anti-neutrino, the spin of the decay positron is exactly equal to the spin of the muon at the time of the decay.



2.2 Detector Systems

2.2.1 Calorimeters

Electromagnetic calorimeters measure the times and energies of decay positrons as they curl inward from the storage region. There are 24 calorimeters located symmetrically around the inside of the ring in close proximity to the vacuum chamber, as shown in Figure ???. They lie close to the storage region in order to measure a large fraction of the total number of observable decay positrons, including the high energy decay positrons which curl inward only slightly more than the muons themselves do. Because they are in close proximity to the storage region and by extension the magnetic field, the calorimeters must be non-magnetic in order to avoid perturbing the magnetic field. Each calorimeter consists of 54 channels of PbF_2 crystals arrayed in a 6 high by 9 wide array, which measure Cerenkov light emitted by the impinging positrons as they pass through the crystals [2]. (Picture of single calo and its crystals here.) Each crystal is $2.5 \times 2.5 \times 14 \text{ cm}^3$. The light is read out by large area silicon

photo-multiplier (SiPM) sensors.

In order to determine a_μ to the precision goal, there are modest requirements on the performance of the calorimeters. They must have a relative energy resolution of better than 5% at 2 GeV, in order for proper event selection [3]. They must have a timing resolution of better than 100 ps. The calorimeters must be able to resolve multiple incoming hits through temporal or spatial separation at 100% efficiency for time separations of greater than 5 ns in order to reduce the pileup systematic error due to the high rate. Finally, the gain of the measured hits must be stable to $< 0.1\%$ over a 200 μs time period within a fill, and unaffected by a pulse arriving in the same channel a few nanoseconds earlier. The long term gain stability over a time period of order seconds must be $< 1\%$.

(I've condensed quite a bit this section from the TDR - is that okay?)

To satisfy these requirements SiPM sensors were chosen over PMTS...

and is wrapped in black Tedlar® foil

2.2.2 Laser System

For the gain, there is a laser system...

[5]

2.2.3 Template Fitting

2.2.4 Straw Trackers

The Muon $g - 2$ Experiment at Fermilab uses straw tracking detectors to measure decay positron trajectories for the purpose of determining the muon beam distribution and its characteristics. By fitting these tracks and extrapolating back to the average decay point, the beam can be characterized in a non-destructive fashion. This is important because of the need for matching the average observed magnetic field of the decaying muons and their resulting decay positron directions which result in the

ω_a frequency.

The trackers are also useful for determining general beam diagnostics as well as the pitch correction and to a lesser extent the electric field correction (careful here). Cross-checking separately for pileup removal, hit verification, etc. is a powerful tool. Combining them in order to provide the muon distribution that the calorimeters directly see for the ω_a calculation is perhaps the most important role of the tracker. With three trackers, approximately 5% of decaying muons will result in measureable positron tracks assuming no pileup in the tracker, many of which do not hit the nearest calorimeter.

Each tracker module consists of 4 layers of 32 straws with a stereo angle of 7.5 degrees, the first two “U” layers oriented with the tops of the straws at a greater radial position, and the second two “V” layers oriented with the bottoms of the straws at a greater radial position. A tracking module is shown in Figure 2.2. There are 3 tracker stations located at the 0th, 12th, and 18th sections of the ring, counting clockwise from the top most point of the ring where the inflector resides. Figure ?? shows this. (Station 18 was installed for the commissioning run, with station 0 planned for the fall. Station 12 might or might not be installed sometime in the future.) Each station consists of 8 tracking modules arranged in a staircase pattern that follows the curvature of the ring as seen in Figure 2.3. Further hardware and electronics information regarding the trackers will be omitted in this document.

Figure 2·2: Shown is a picture of one of the many tracking modules used in the Muon $g - 2$ experiment. The first layer of straws with a stereo angle of 7.5 degrees can be seen, with the other 3 straw layers hiding behind it. The beam direction is roughly into the page in this picture, to the left of the end of the module, and this view is what the decay positrons will see.

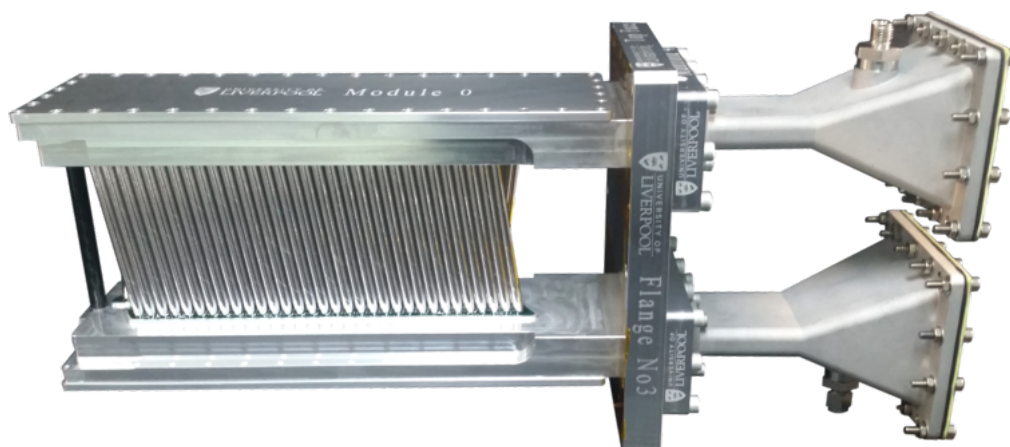
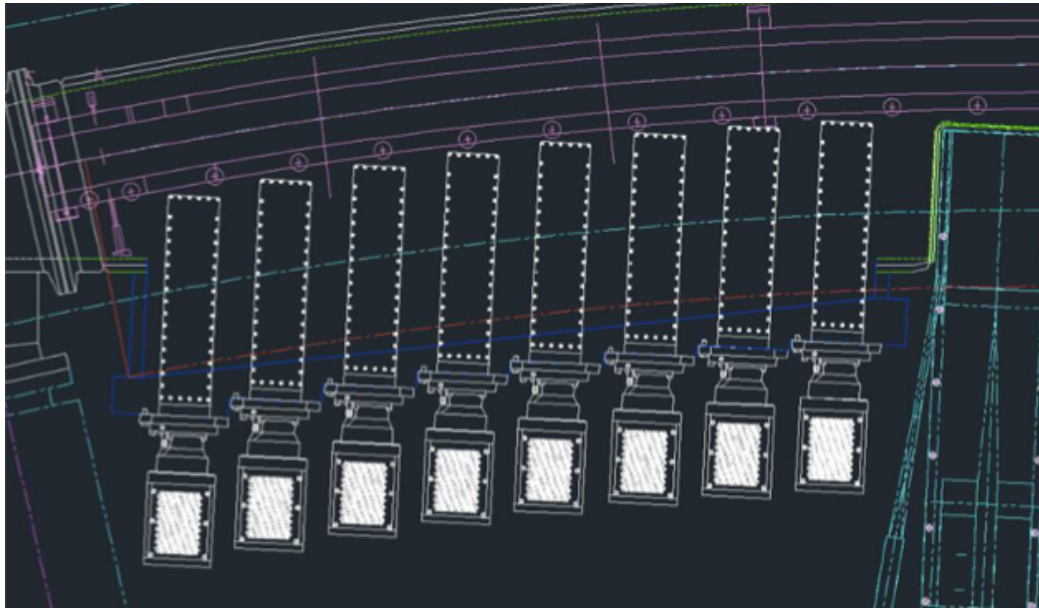


Figure 2-3: Tracker modules are arranged in the shown staircase pattern. In green and dark blue is the edge of the vacuum chamber (where the dark blue identifies the modification that was made to the old vacuum chambers), and it can be seen that vacuum chamber walls lie at the ends of the outside tracking modules. The position of a calorimeter can be seen in cyan at the right. The dark red spots are the locations of the outside magnet pole tips. From the shown geometry one can see that many positrons will hit either the tracker or the calorimeter but not both due to the acceptance differences.



Chapter 3

Magnetic Field Measurement

3.1 Trolley

Chapter 4

Straw Tracking Analysis

4.1 Straw Tracking Intro

As was talked about briefly in section 2.2.4, the straw trackers are used to provide information about the muon beam, as well as info for the calorimeters. The straw track reconstruction is performed in several stages. The “Track Finding” stage takes incoming hits and decides which hits should be grouped together to form a single track for a single positron. The “Track Fitting” stage fits the measured positions of these individual hits and forms a single track describing the trajectory of the incident positron. Finally the “Track Extrapolation” stage takes the fitted track information and extrapolates the position and momentum components to the regions of interest, namely the storage region and the calorimeter.

-see the previous section for the hardware information... -Geane (Geometry and Error Propagation)

4.2 Track Finding

4.3 Track Fitting

The Geane fitting routines originated in Fortran with the EMC collaboration, and was used in the precursor E821 experiment as well as the PANDA experiment with some success [4], [7]. (I’m not actually aware of a useful reference for it’s use in E821, and there are some other instances of its use as well in other experiments. In E821

there was a single tracking chamber which was never put to full use.) The core error propagation routines were at some point added to Geant4 under the `error_propagation` directory which is included in all default installs. The tracking code strengths lie with its direct implementation and access to the Geant4 geometry and field, and its ability to handle the field inhomogeneties. The Geane fitting algorithm code which makes use of the Geant4 error propagation routines follows the structure of [4] and is detailed in the Formalism section in this paper. It is a relatively straight forward least squares global χ^2 minimization algorithm.

Because of the proximity of the trackers to the muon beam, they will lie within a region of varying magnetic field. The radial field of the trackers rises from 0 Tesla at the outer ends to roughly .3 Tesla at the inner top and bottom ends, and the vertical field drops approximately 50% from the storage dipole field of 1.451 Tesla. Shown in Figures 4.1 and 4.2 is the location of the tracker with respect to the horizontal and vertical fields respectively. These large field gradients over the tracking detector region and the long extrapolation distance back to the muon decay point are special to Muon $g - 2$. This is one of the main motivations for using the Geane fitting algorithm and routines, which has direct access to the field.

4.4 Track Extrapolation

Figure 4.1: Shown is the vertical field of the $g - 2$ magnet in and around the storage region as calculated in Opera 2D. The center of the storage region lies at 7.112 m along the x axis. The black box shows the rough location of the tracker with respect to the field (size exaggerated slightly). It can be seen that there is a large inhomogeneity within the tracker space, going from left to right.

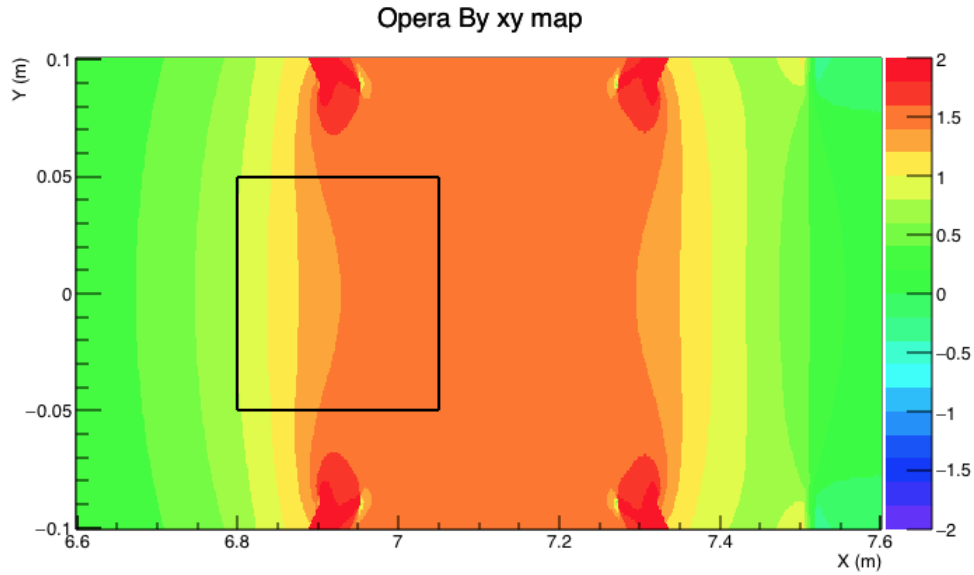
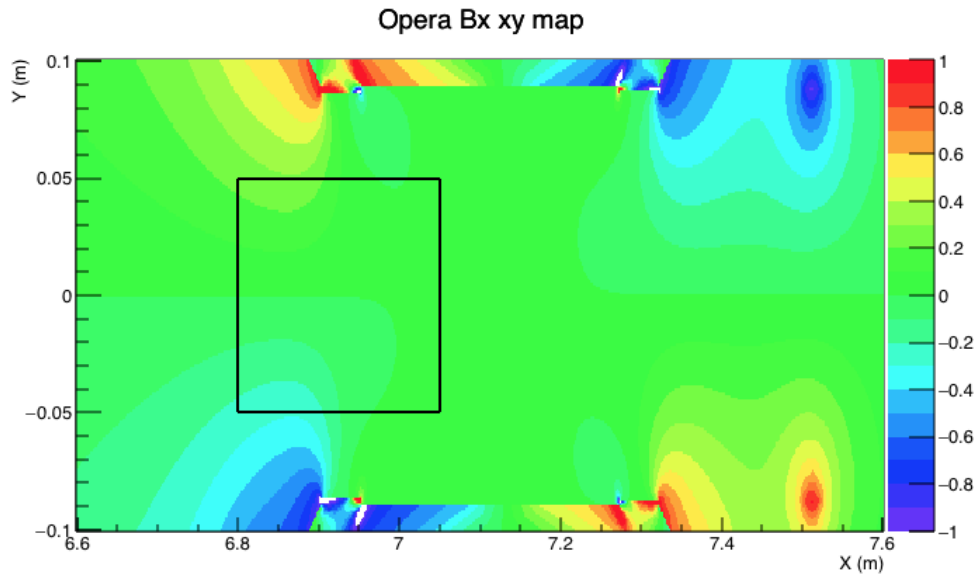


Figure 4.2: Shown is the radial field of the $g - 2$ magnet in and around the storage region as calculated in Opera 2D. The center of the storage region lies at 7.112 m along the x axis. The black box shows the rough location of the tracker with respect to the field (size exaggerated slightly). It can be seen that there is a large homogeneity at the inner upper and lower ends compared to the right center. The shape of the pole pieces and tips can readily be seen.



Chapter 5

ω_a Measurement

5.1 Data

5.2 Spectra Making

5.2.1 Clustering

5.2.2 Histogramming

5.3 Fitting

5.4 Systematic Errors

Chapter 6

Conclusion

6.1 Final Value

test4

Appendix A

Proof of xyz

This is the appendix.

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Joe Graduate

Basically, this needs to be worked out by each individual, however the same format, margins, typeface, and type size must be used as in the rest of the dissertation.