

Experimental Mechanics : 24 Sept. 2018

## Notes on Strain Analysis

### Stress transformation

$$\left. \begin{aligned} \rightarrow \Sigma_A &= \Sigma_{xx} \cos^2 \theta_A + \Sigma_{yy} \sin^2 \theta_A + \tau_{xy} \sin \theta_A \cos \theta_A \\ \rightarrow \Sigma_B &= \Sigma_{xx} \cos^2 \theta_B + \Sigma_{yy} \sin^2 \theta_B + \tau_{xy} \sin \theta_B \cos \theta_B \\ \rightarrow \Sigma_C &= \Sigma_{xx} \cos^2 \theta_C + \Sigma_{yy} \sin^2 \theta_C + \tau_{xy} \sin \theta_C \cos \theta_C \end{aligned} \right\} \text{Principal Stress by Mohr's Circle}$$

### Mohr's Circle

$$\rightarrow \Sigma_{1,2} = \frac{1}{2} (\Sigma_{xx} + \Sigma_{yy}) \pm \frac{1}{2} \sqrt{(\Sigma_{xx} - \Sigma_{yy})^2 + 4\tau_{xy}^2}$$

$$\rightarrow \tan 2\phi = \frac{\tau_{xy}}{\Sigma_{xx} - \Sigma_{yy}}$$

### Correction factors of Strain Gages (Transverse Effects)

$$\rightarrow \Sigma_a = \underbrace{\Sigma'_a}_{\text{Measured Value}} \frac{1 - \nu K_t}{1 + K_t (\epsilon_t / \epsilon_a)} ; K_t = \frac{s_t}{s_a} \begin{matrix} \text{transverse sensitivity} \\ \text{axial sensitivity} \end{matrix}$$

Must be a known ratio

### Correction Factor ( $S_a$ )

$$S_g = \frac{AR/R}{\Sigma_a} ; S_a^* = S_a \left( \frac{1}{C.F.} \right) ; C.F. \text{ is provided correction factor}$$

$$\left. \begin{aligned} \rightarrow \Sigma'_{xx} &= \frac{1}{1 - \nu K_t} (\Sigma_{xx} + K_t \Sigma_{yy}) \\ \Sigma'_{yy} &= \frac{1}{1 - \nu K_t} (\Sigma_{yy} + K_t \Sigma_{xx}) \end{aligned} \right\} \begin{matrix} \text{Apparent related to actual strain in} \\ 2 \text{ equations} \end{matrix}$$

### Optical Measurements of Strain

→ Topics : Wave theory of light → Wave Equation → Superposition → Polarization ...