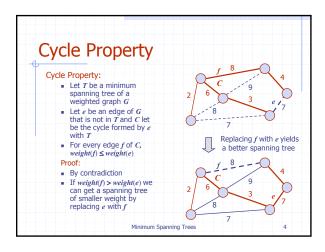
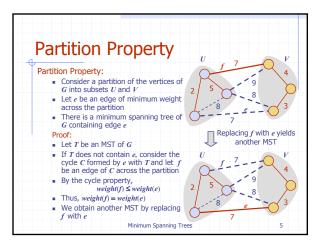
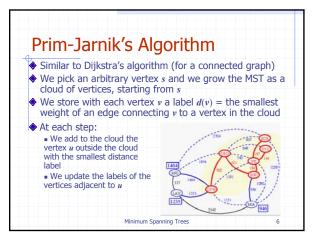
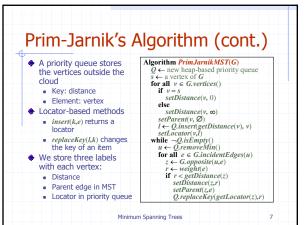


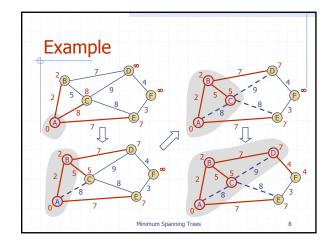
Minimum Spanning Tree Spanning subgraph ORD) 10 ■ Subgraph of a graph G containing all the vertices of G PIT Spanning tree Spanning subgraph that is DEN itself a (free) tree Minimum spanning tree (MST) Spanning tree of a weighted graph with minimum total edge weight Applications Communications networks (DFW Transportation networks Minimum Spanning Trees

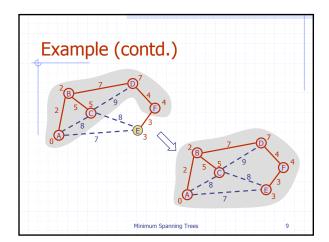


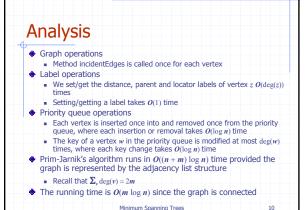


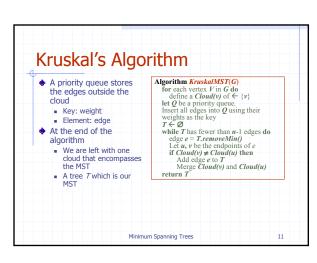


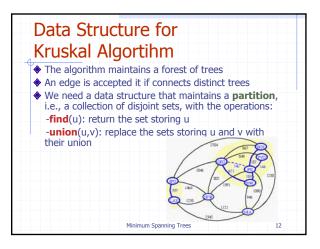






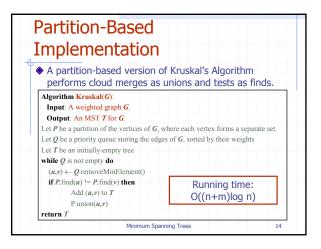


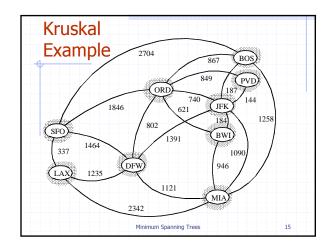


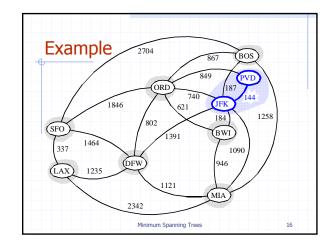


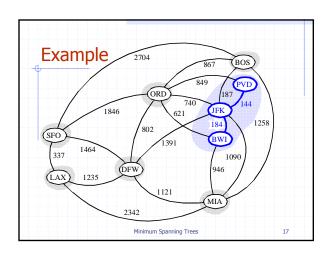
Representation of a
Partition

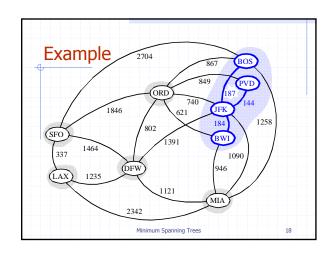
• Each set is stored in a sequence
• Each element has a reference back to the set
• operation find(u) takes O(1) time, and returns the set of which u is a member.
• in operation union(u,v), we move the elements of the smaller set to the sequence of the larger set and update their references
• the time for operation union(u,v) is min(n_u,n_v), where n_u and n_v are the sizes of the sets storing u and v
• Whenever an element is processed, it goes into a set of size at least double, hence each element is processed at most log n times



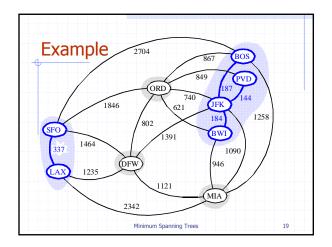


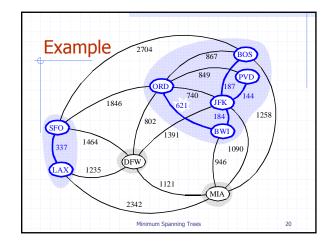


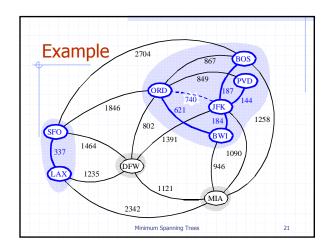


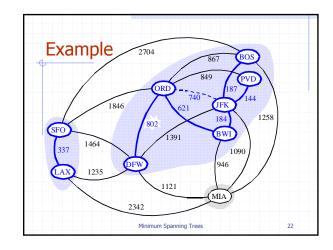


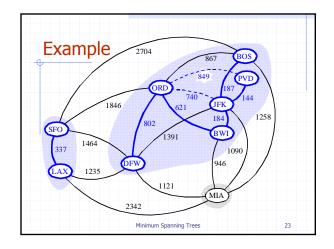
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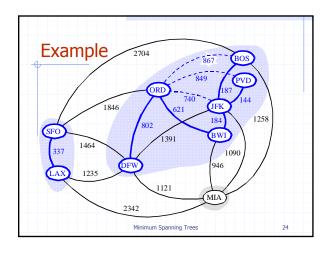


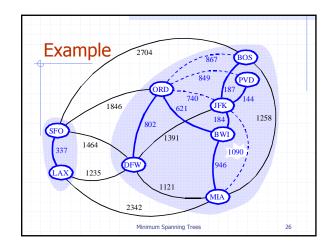


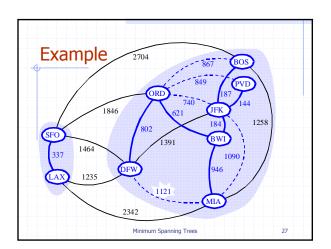


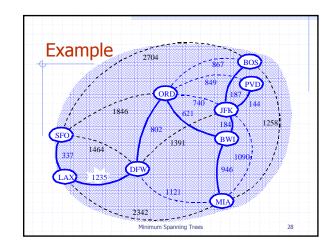












Baruvka's Algorithm ◆ Like Kruskal's Algorithm, Baruvka's algorithm grows many "clouds" at once. Algorithm BaruvkaNST(G) T ← V {just the vertices of G} while T has fewer than n-1 edges do for each connected component C in T do Let edge e be the smallest-weight edge from C to another component in T. if e is not already in T then Add edge e to T return T ◆ Each iteration of the while-loop halves the number of connected components in T. ■ The running time is O(m log n).

