

Brief explanation

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1 Current-current correlation function

1.1 Assumptions

A transfer integral between m th atomic orbital(AO) and n th AO is denoted by t_{mn} . Current operator \hat{J} : see below of Eq.3 of <https://arxiv.org/abs/1807.01625>

1.2 Definition

Current-current correlation function C_J is defined as below

$$C_J = \langle \Psi | \hat{J} \hat{J} | \Psi \rangle \quad (1)$$

(where $|\Psi\rangle$ is a wavefunction of system) In this program, C_J is limited to a case with same time and same position (i.e. JJ has only two AO indices)

2 Spin-spin correlation function

The z component of the spin operator is given below, ignoring the constant multiple terms.

$$S^z = \sum_i (a_{i\alpha}^\dagger a_{i\alpha} - a_{i\beta}^\dagger a_{i\beta}) \quad (2)$$

Spin-spin correlation function is given below:

$$C_s = \langle \Psi | \hat{S}^z \hat{S}^z | \Psi \rangle \quad (3)$$

3 Charge-charge correlation function

Occupation number operator at site i is given below:

$$\hat{n}_i = \hat{a}_{i\alpha}^\dagger \hat{a}_{i\alpha} + \hat{a}_{i\beta}^\dagger \hat{a}_{i\beta} \quad (4)$$

Charge-charge correlation function is given below:

$$C_n^{ij} = \langle \Psi | \hat{n}_i \hat{n}_j | \Psi \rangle - \langle \Psi | \hat{n}_i | \Psi \rangle \langle \Psi | \hat{n}_j | \Psi \rangle \quad (5)$$

4 Exciton correlation

The equation for random phase approximation (RPA) is below:

$$\begin{pmatrix} A & B \\ -B^* & -A^* \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \omega \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} \quad (6)$$

The RPA wavefunction is below:

$$|\Phi\rangle = \sum_{mi} (X_{mi}|mi\rangle - Y_{mi}|im\rangle) \quad (7)$$

Note that m is the index of the occupied molecular orbital, i is the index of the virtual molecular orbital, and $|mi\rangle \equiv \hat{a}_i^\dagger \hat{a}_m |\text{HF}\rangle$. Convert X_{mi} to AO basis with molecular orbital coefficients to obtain exciton correlation.

5 Green's function for a mean-field calculation

See Eq.7 of <https://arxiv.org/abs/2002.05875>. Note in this program, real space not reciprocal space is treated.