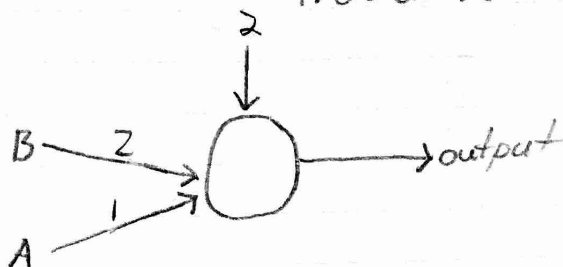


Problem 2

a)



$$1 = \text{True} \quad 0 = \text{False}$$

$$(A \wedge B) \Leftrightarrow (A \wedge B)$$

A	B	0
1	1	0
1	0	0
0	1	0
0	0	0

b) i) Input A = $x_1(w_{x1a}) + x_2(w_{x2a}) + x_3(w_{x3a}) + 1(w_{h1a})$

$$= .3(.4) + .8(.4) + .1(.4) + .3$$

$$= .78$$

$$\text{Output A} = \frac{1}{1 + e^{-\text{input}}} = \frac{1}{1 + e^{-.78}} = \boxed{.686}$$

Input B = $x_1(w_{x1b}) + x_2(w_{x2b}) + x_3(w_{x3b}) + 1(w_{h1b})$

$$= .3(-.2) + .8(-.2) + .1(-.2) + .3$$

$$= -.06 + -.16 + -.02 + .3 = .06$$

$$\text{Output B} = \frac{1}{1 + e^{-\text{input}}} = \frac{1}{1 + e^{-.06}} = \boxed{.515}$$

Input C = $A(w_{ac}) + B(w_{bc}) + 1(w_{h2c})$

$$= .686(.4) + .515(-.2) + .3$$

$$= .2744 + -.103 + .3$$

$$= .4714$$

$$\text{Output C} = \frac{1}{1 + e^{-\text{input}}} = \frac{1}{1 + e^{-.4714}} = \boxed{.616}$$

ii) a) $\Delta C = (1 - .616) \cdot .616 =$ $\Delta A = (.685)(1 - .685)(.4)(.0908) = \boxed{.6078}$

$$\Delta B = (.515)(1 - .515)(-.2)(.0908) = \boxed{-.00454}$$

b) $\Delta w_{ac} = .2(.0908)(.685) = .0124 + .4 = \boxed{.4124}$

$$\Delta w_{bc} = .2(.0908)(.515) = .0093 + -.2 = \boxed{-.1907}$$

$$\Delta w_{h2c} = .2(.1)(.0908) = .0182 + .3 = \boxed{.3182}$$

c) $\Delta w_{3a} = .2(.1) \cdot .685(1 - .685)(.4124)(.0908) = .0001616 + .4 = \boxed{.4001}$

$$\Delta w_{x2b} = (.2)(.8)(.515)(1 - .515)(-.1907)(.0908) = -.000692 + -.2 = \boxed{-.200692}$$

$$\Delta w_{x1a} = .2(.4124)(.0908)(1 - .685)(.685)(.3) = .000488 + .4 = \boxed{.400488}$$

$$\Delta w_{x1b} = .2(.4)(.515)(1 - .515)(-.1907)(.0908) = -.000346 + -.2 = \boxed{-.200346}$$

$$\Delta w_{x2a} = .2(.8)(.685)(1 - .685)(.4124)(.0908) = .0012928 + .4 = \boxed{.4012928}$$

.06038365

$$\Delta_{w3b} = .2(.1)(.515)(1-.515)(-.1907)(.0908) = -.0000872 = \boxed{-.200087}$$

$$\Delta_{wh1a} = .2(.685)(1-.685)(.4124)(.0908) = .0016243 = \boxed{.30162}$$

$$\Delta_{wh1b} = .2(.515)(1-.515)(-.1907)(.0908) = -.0008653 = \boxed{-.300865}$$