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pymwp: A Static Analyzer Determining Polynomial Growth Bounds

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```
void main(int X1, int X2, int X3)
while (X1 < 10) {
    X1 = X2 + X3;
 // X1' X2'
```

For input variables of an imperative program:

Does there exist a polynomially bounded data-flow relation between variables' **initial** values and **final** values?

That is, \forall n, is $X_n \rightsquigarrow X'_n$ polynomially bounded?

```
void main(int X1, int X2, int X3)
while(X1 < 10){
   X1 = X2 + X3;
 // X1' X2' X3'
```

Yes. Here is a bound:

$$X1' \leq \max(X1, X2+X3)$$

$$\land X2' \leq X2$$

$$\wedge X3' \leq X3$$

mwp-flow analysis¹

Calculus for resource analysis of imperative programs.

while
$$(X1 < 10)$$

 $X1 = X2 + X3$

0 – no dependency

m – maximal (of linear)

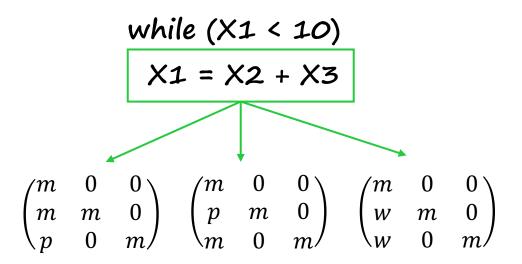
w – weak polynomial

p - polynomial

¹Neil D. Jones and Lars Kristiansen. "A flow calculus of mwp-bounds for complexity analysis". In: ACM Trans. Comput. Log. 10.4 (Aug. 2009), 28:1–28:41. doi: 10.1145/1555746.1555752.

mwp-flow analysis¹

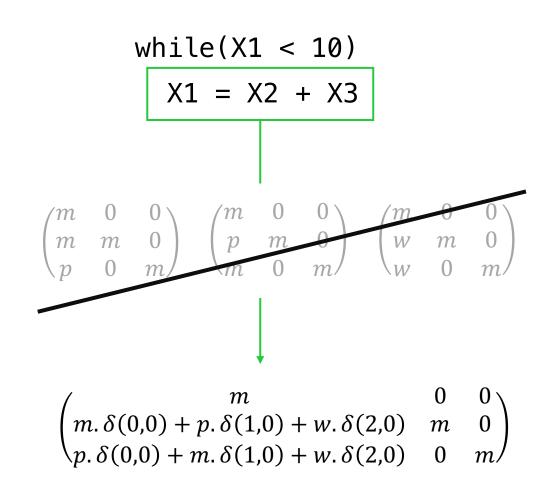
- 3ⁿ derivation paths
- Some may fail



¹Neil D. Jones and Lars Kristiansen. "A flow calculus of mwp-bounds for complexity analysis". In: ACM Trans. Comput. Log. 10.4 (Aug. 2009), 28:1–28:41. doi: 10.1145/1555746.1555752.

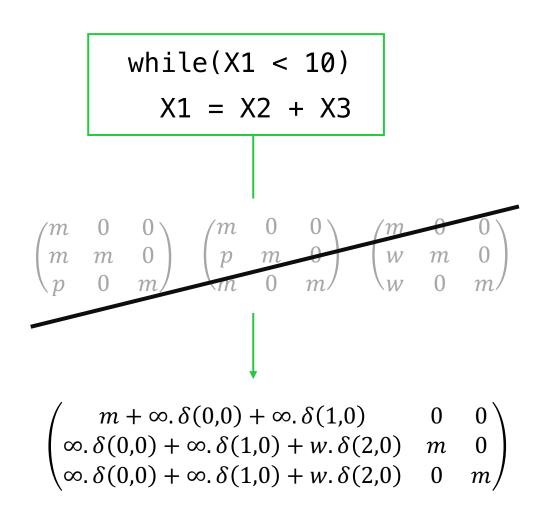
Automating mwp

✓ Internalize non-determinism



Automating mwp

- ✓ Internalize non-determinism
- √ Handle derivation failure
- 0 no dependency
- *m* maximal (of linear)
- w weak polynomial
- p polynomial
- ∞ non-polynomial / failure



Aubert, Clément, et. al. "mwp-Analysis Improvement and Implementation: Realizing Implicit Computational Complexity". In: FSCD 2022. Vol. 228. LIPIcs, 2022, 26:1–26:23. doi: 10.4230/LIPIcs.FSCD.2022.26.

```
void main(int X1, int X2, int X3)
while(X1 < 10){
    X1 = X2 + X3;
 // X1' X2'
```

We were here

$$\begin{pmatrix} m + \infty \cdot \delta(0,0) + \infty \cdot \delta(1,0) & 0 & 0 \\ \infty \cdot \delta(0,0) + \infty \cdot \delta(1,0) + w \cdot \delta(2,0) & m & 0 \\ \infty \cdot \delta(0,0) + \infty \cdot \delta(1,0) + w \cdot \delta(2,0) & 0 & m \end{pmatrix}$$

But we *actually* want

$$X1' \le max(X1, X2+X3)$$

 $\land X2' \le X2 \land X3' \le X3$

Obtaining bounds compactly and efficiently

$$\begin{pmatrix} m + \infty \cdot \delta(0,0) + \infty \cdot \delta(1,0) & 0 & 0 \\ \infty \cdot \delta(0,0) + \infty \cdot \delta(1,0) + w \cdot \delta(2,0) & m & 0 \\ \infty \cdot \delta(0,0) + \infty \cdot \delta(1,0) + w \cdot \delta(2,0) & 0 & m \end{pmatrix}$$

Find the derivation choices that lead to ∞ then simplify.

$$[\{0,1,2\}] \rightarrow [\{2\}]$$

$$\begin{pmatrix} m & 0 & 0 \\ w & m & 0 \\ w & 0 & m \end{pmatrix}$$

```
void main(int X1, int X2)
X1 = X2 + X2;
while(X1 < 10){
    X1 = X1 * X1;
```

When derivation fails (--fin)

Problematic flows:

$$X1 \rightarrow X1 \parallel X2 \rightarrow X1$$

pymwp is an automatic static analyzer for (subset of) C code, to determine if inputs' value growth is polynomially bounded.

run in terminal

run in browser



statycc.github.io/pymwp/demo



source code + docs: statycc/pymwp