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The Effects of Climate Change on Tradeoffs Among Forest Ecosystem Services

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Abstract

The Effects of Climate Change on
Tradeoffs Among Forest Ecosystem Services

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DRAFT

Forests provide ecosystem services in concert with one another. Multi-objective optimization has been a successful approach used to determine forest management schemes that maximize the simultaneous provision of ecosystem services. Climate change is predicted to impact forests and their ability to provide ecosystem services; however, no studies have determined how the relationships between managed ecosystem services will change with climate. This study addresses that question using a scenario-based approach. I consider a study system in the Deschutes National Forest with competing objectives: providing habitat for the northern spotted owl, reducing fire hazard, and ensuring water quality of the watershed. I compare the tradeoffs among the objectives under three climate scenarios which vary in their intensity of assumed climate change.

I find that ...

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GLOSSARY

CLIMATE PROJECTION: The IPCC defines a climate projection as a model-derived estimate of future climate. *See* CLIMATE SCENARIO[50].

CLIMATE SCENARIO: The IPCC defines a scenario as a coherent, internally consistent and plausible description of a possible future state of the world. Herein, I use this term synonymously with CLIMATE PROJECTION, since climate projections often underlie climate scenarios [50].

CLUSTER: Here, a set of contiguous forest stands whose combined area exceeds 200 ha

ECOSYSTEM SERVICE: Benefits that people receive from ecosystems, divided into four categories: supporting, provisioning, regulating and cultural [5]. Examples include food, soil formation, water purification, carbon storage, recreation, and education.

PARETO EFFICIENT: A solution to a multi-objective mathematical program is said to be Pareto efficient if no component of the solution can be improved without compromising another component.

ACKNOWLEDGMENTS

DRAFT

Thank you to all who contributed to my earning this degree.

DEDICATION

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To ma femme and my family

Chapter 1

ASSESSING CHANGES IN TRADEOFFS AMONG ECOSYSTEM SERVICES IN THE DESCHUTES NATIONAL FOREST

1.1 Introduction

Forests play an important role in global ecological, social, and economic processes. They provide ecosystem services such as carbon storage, purification of water and air, wildlife habitat, recreation opportunities, and generate raw materials for goods such as food and lumber [18]. In managed forests, the extent to which forests provide these services depends in part on management practices. Optimal forest management seeks to ensure the sustained provision of these ecosystem services [1].

Like other ecosystems, forests will undergo changes as a result of the changing climate. Researchers anticipate new spatial distributions of tree species [36], increased sediment delivery to streams [31], and increasing disturbance regimes such as wildfires, drought, and insect infestation [65]. As this transformation occurs, forests' ability to provide ecosystem services will change. Increased frequency of disturbance regimes will impact forests' ability to store carbon [7] and provide wildlife habitat [46]. Water supplies that rely on forests' filtration capabilities may be impacted by the rising sediment levels predicted by [31].

Optimal forest management must consider the effects of the changing climate, because the time scale of forest development is of the same order as that on which climate change is predicted to operate [34]. Optimal forest management will likely differ under alternative future climates [41]. Decisions that would once have resulted in optimal achievement of ecosystem services, now under different climatic conditions, may no longer do so. Without consideration of climate change, forest management plans may restrict forests' potential to

provide ecosystem services most effectively.

Many studies have addressed the impacts of climate change on forest ecosystem services in isolation [65][7][46]. However, because forests provide these ecosystem services in concert with one another (see, for example, [63]), it is necessary to also understand how climate impacts the tradeoffs that exist among them. How does an increase in any one ecosystem service alter our ability to acquire an amount of another? Relationships such as a marginal sacrifice in one service for substantial improvement in another may no longer exist under a new climate. To better ensure the sustained provision of ecosystem services, we must understand how these tradeoffs evolve with climate.

1.1.1 A hypothetical scenario

To understand how tradeoff relationships impact management strategies and ecosystem service provision, consider the following hypothetical scenario in which a forest serves as prime habitat for a threatened bird species. The forest manager's primary objective is the conservation of this species, but the manager also performs the minimum amount of harvests necessary to negate the costs of property ownership from timber sales. To determine which stands to harvest, the manager ran an analysis, ignoring climate change, that suggested the harvest of a small set of stands near the northern perimeter of the forest as it was most accessible, served only as mediocre habitat for the bird species, and was dense with merchantable timber.

Now, climate change is reducing the area of the forest that is suitable habitat for the threatened bird species. Much of the species' remaining habitat is the area on the northern perimeter of the forest that has traditionally been harvested. Simultaneously, longer growing seasons and warmer temperatures are increasing the timber stock of other areas of the forest, making the northern stands less relatively advantageous to harvest. The manager, unaware, continues harvests in the northern stands, damaging much of what remains of the bird species' habitat.

With each ecosystem service modeled in isolation, this conflict is not fully understood,

and optimal alternatives will not be discovered. Modeled in concert, however, the forest manager would have realized that these objectives do not strongly conflict with one another - if the manager were to move the harvests to the stands near the forest's eastern perimeter, his harvests would increase only slightly while also retaining nearly all of the bird species's suitable habitat. In other words, a marginal sacrifice in one ecosystem service allows for a significant improvement in another. Without knowledge of this tradeoff structure, the manager is unnecessarily impeding the bird species's climate-driven rangeshift.

It is the impact of climate change on such tradeoff structures that I investigate in this work. I consider as a case study an area in the Deschutes National Forest known as the Drink Planning Area, or the Drink area, in which we attempt to maximize the provision of the following ecosystem services: area of habitat available to the northern spotted owl, water quality in the watershed, and reduction in fire hazard.

1.2 Methods

1.2.1 Study area

I selected for the study system the Drink Planning Area which consists of 7056 ha on the east slopes of the Cascade Mountain Range in the Deschutes National Forest (see Figure 1.1). This area makes for an adequate study system, because it provides conflicting ecosystem services which the US Forest Service seeks to simultaneously optimize.

The first objective is the reduction of fire hazard rating through the use of silvicultural treatments. The USFS chose this objective because one third of the Drink area comprises the municipal watershed for the cities of Bend, OR and Sisters, OR (see Figure 1.2) which have a combined population of approximately 90,000. Wildfires pose a threat to the watershed as they cause soil water repellency, surface runoff, and debris torrents [35].

In addition, approximately 43% of the Drink serves as habitat for the northern spotted owl (NSO) (*Strix occidentalis caurina*) (Figure 1.2). The USFS is required to protect the NSO since it is threatened and therefore protected by the Endangered Species Act of 1973

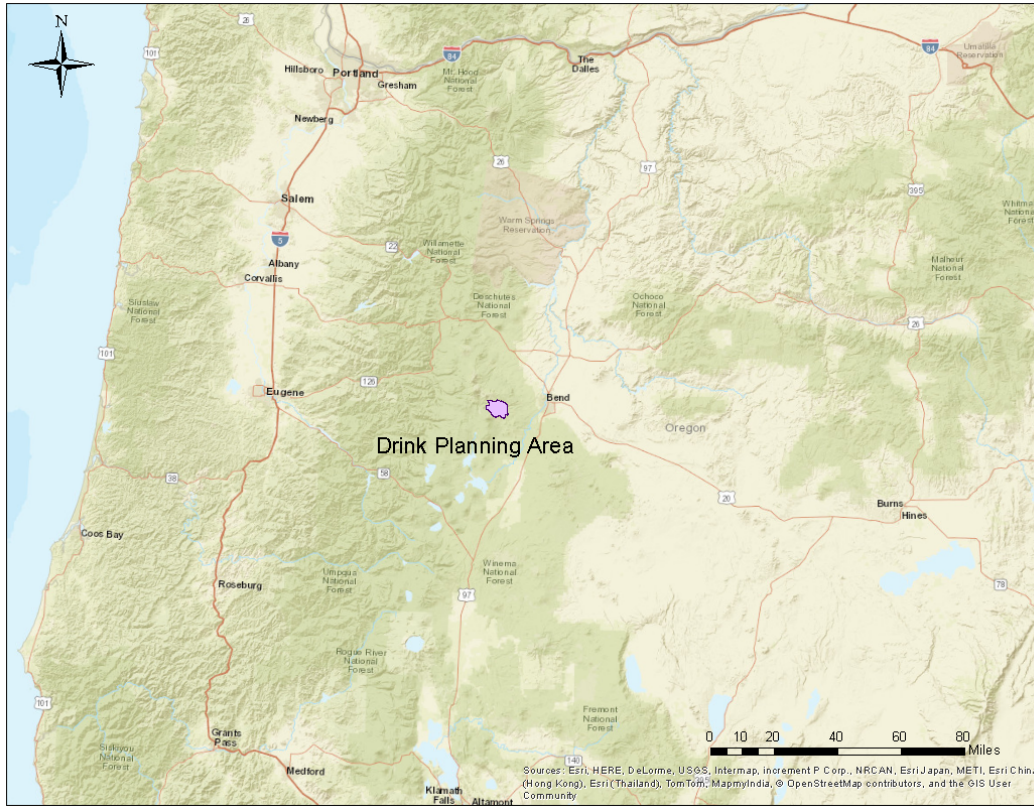


Figure 1.1: Overview of the study system, the Drink Planning Area (in purple), consisting of 7056 ha in the Deschutes National Forest.

[11]. The protection of NSO habitat is the second objective considered in this analysis.

Lastly, I aim to minimize the sediment delivered to the watershed as a result of the treatments applied to reduce fire hazard. While the treatments intend to provide long-term protection of the quality of the watershed, they also have the potential to introduce short-term increases in sediment delivery [49].

To accomplish long-term reduction in fire hazard rating for the area, I formed a strategic plan for silvicultural treatments to apply across the Drink. The treatments may be applied in each of two 20-year time periods (2015-2035 and 2035-2055) and to each of the 303 management units that comprise the Drink. The division of the management units (stands) was performed *a priori* by the Forest Service. The decision as to which treatment to perform

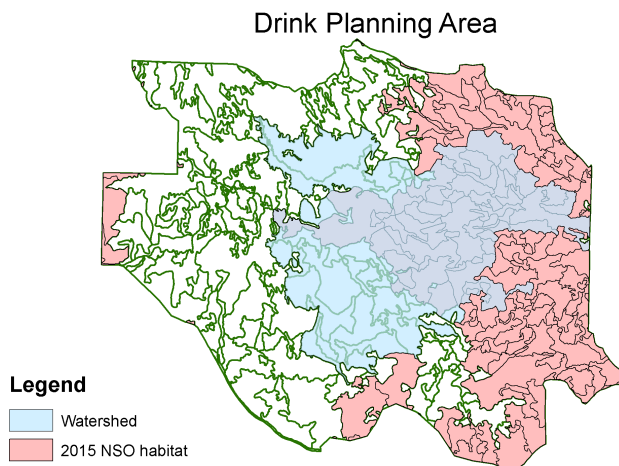


Figure 1.2: Location of the municipal watershed and the suitable NSO habitat in the Drink area at the beginning of the planning horizon (2015). Interior polygons are the 303 management units.

on a stand is entirely dependent on silvicultural characteristics; the rules used to determine the treatment applications can be found in Appendix B.

To assess the treatments' long-term efficacy, I measured the fire hazard of the Drink at the end of an 80-year planning horizon (2015-2095). I measured the area of NSO habitat at the end of each planning period to ensure that the application of treatments did not negatively impact the habitat available for the NSO. Finally, the short-term sediment contributions from performing the treatments were measured at the time of treatment, which is assumed to be at the midpoint year in the planning period (2025 for period 1, 2045 for period 2). The planning horizon including the time of these events is shown in Figure 1.4.

The three objectives are inherently in conflict with one another: fuel treatments drive short-term peaks in sediment delivery and potentially reduce owl habitat; minimizing short-term sediment delivery entails fewer treatments and therefore a higher fire hazard; maximizing owl habitat may require forgoing fuel treatments and again lead to higher fire hazard. In this study, I will determine how climate change impacts the tradeoffs that exist among these objectives.

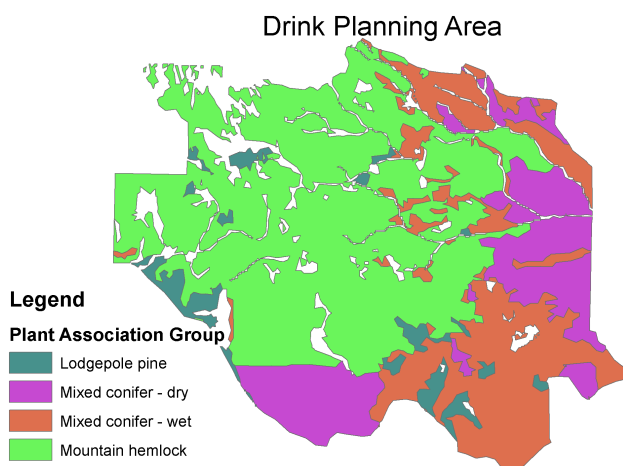


Figure 1.3: Plant association groups in the Drink Planning Area selected for treatment by the US Forest Service.

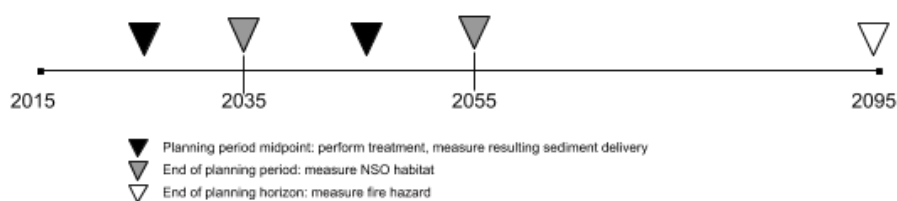


Figure 1.4: The planning horizon used in the analysis spans the 80 year period from 2015 to 2095. Treatments may be performed in the first period, the second period, both, or neither. Treatments are assumed to be performed at the mid-point years of each period (black triangles). Sediment delivery is measured on treatment years. Stands' suitability for NSO habitat is measured at the end of the planning periods (gray triangles), and fire hazard at the end of the planning horizon (white triangle).

1.2.2 *Climate Scenarios Considered*

To determine the impacts of climate change on the tradeoff structure between ecosystem services, it is first necessary to define how the impacts of climate change will be captured in the analysis. Here I use the method employed by the IPCC, namely, a scenario analysis. In a scenario analysis, multiple alternative futures are considered and no prediction is made as to which scenarios are more likely than others. There is no attempt to quantify the probability of realization of any one scenario, much like how IPCC does not attempt to quantify the probability that any particular climate model is the correct prediction of the future climate.

The alternative future climates I consider here are climate scenarios from the IPCC's Fifth Assessment [34]. Given the large number of potential future climates considered by the IPCC (see [25]) combined with the computational complexity involved in the study of each one, I selected a small subset of future climate scenarios for my analysis. I will refer to these three scenarios as “None”, “Ensemble RCP 4.5”, and “Ensemble RCP 8.5”.

The first scenario, “None”, is the assumption of no climate change. While the number of studies incorporating climate change is increasing, this is still the assumption used for many modern studies such as [55], from which this study is derived. Because it has served as the basis for many studies and assumes a static environment resembling today's, the “None” climate scenario serves as a good control against which to compare the other two climate scenarios.

As their names suggest, the second and third scenarios are ensembles. Each ensemble is comprised of 17 global circulation models (GCMs) used in the IPCC's Fifth Assessment (AR5). The selection of component GCMs in the ensembles was performed by the USFS's Climate-FVS [22] team. The list of the 17 scenarios included in the ensemble can be found in [14]. Each component GCM has a corresponding climate surface which contains a vector of 35 climate parameters at over 11,000 global locations for three time periods. The climate surfaces for the ensembles were created by averaging the values of all component GCMs for each climate parameter and each time period for each location. The result is a climate

surface that, while temporally sparse, is spatially robust. This configuration is appropriate for use in the Drink area given its variability in elevation and slow vegetation growth.

The two ensembles are comprised of the same 17 GCMs, but the assumed representative concentration pathways (RCP) in the component GCMs differ. The RCP indicates the additional radiative forcing (in W/m^2) above pre-industrial levels, with higher values of forcing indicative of more severe climate change. The GCMs in the Ensemble RCP 4.5 scenario assume $4.5 W/m^2$ of additional radiative forcing, and the GCMs in the Ensemble RCP 8.5 scenario assume $8.5 W/m^2$ of additional radiative forcing.

I chose these three scenarios because they represent a range of predicted climate change severity, from a $0^\circ C$ warming by the year 2100 under the “None” scenario to a $2.6 - 4.8^\circ C$ warming under RCP 8.5 [34].

1.2.3 Determining tradeoff relationships between ecosystem services

Given a selection of climate scenarios, I determined the tradeoff relationships between ecosystem services using multi-objective mathematical optimization [61]. This approach seeks to maximize a set of objectives subject to a set of constraints. The objectives here are the ecosystem services that the USFS prioritized for the Drink area (see §1.2.1). The set of constraints is comprised of logical constraints - such as that silvicultural treatments cannot be performed on nonforested areas - and constraints imposed by the USFS - such as labor restrictions limiting the number of hectares that may be treated in a given amount of time.

The multi-objective model, or mathematical program, used for this analysis involves linear, integer, and binary variables, making it a mixed integer program (MIP). Constructing the model requires data. The treatment assignment rules for the model, the acquisition of the required data, and the projection of that data into the future are described here:

Treatment scheduling and assignment rules

I simulated the 303 stands in the Drink area over the course of an 80 year planning horizon with all treatment activity occurring in the first 40 years. The activity could be selected to

be completed in the first twenty year period, the second twenty year period, both, or neither. The type of treatment to be performed is dependent on silvicultural characteristics (see §B) and was determined *a priori* using the vegetation data described below. As a result, the model needed only to choose whether to perform a treatment on a stand in a given period; the model did not have to select which treatment to perform.

Acquisition and projection of data

The data required to solve the model include - for each climate scenario, each time period and each stand - a measure of fire hazard, determination of suitability for NSO habitat, and the amount of sediment deposited in the municipal watershed as a result of performing various thinning treatments.

As a measure for fire hazard, I chose the average fuel model of a stand according to the Anderson fuel model rating system [4]. This fuel model rating is an integer 1-13, that describes the fuel characteristics of an area, with larger fuel models corresponding to larger fuel loads, making it a suitable proxy for fire hazard. To determine the initial fuel models of each stand, I obtained the 2012 GNN structure map (<http://lemma.forestry.oregonstate.edu/data/structure-maps>) from Oregon State University’s Landscape Ecology, Modeling, Mapping & Analysis (LEMMA) group. The LEMMA group provides this data in a format compatible with the USFS’s Forest Vegetation Simulator (FVS). I used FVS’s database extension to import this data into FVS and then used FVS’s Fire and Fuels Extension[53] (FFE) to compute the average fuel model for each stand. I then used Climate-FVS to project the stands’ vegetation forward 80 years until the end of the planning horizon under each of the climate scenarios.

Through previous conversations with the USFS, it was determined that any area meeting the following characteristics would be considered ideal NSO habitat:

1. elevation less than 1830 m
2. the presence of trees with DBH no less than 76 cm

3. canopy closure of at least 60%
4. greater than 200 ha in size

I attained a digital elevation model from the US Department of Agriculture’s GeoSpatial Data Gateway to compute average stand elevation and check for the first criterion. I checked the second and third criteria using the vegetation data produced by FVS. If the first three criteria are met but the area is not 200 ha in size, it is still classified as NSO habitat but is penalized by a factor of $e = 0.5$. Since stands were generally less than 200 ha in size, the last criterion required the enumeration of all clusters of stands whose combined contiguous area exceeded 200 ha. The model checks whether all stands in such a cluster meet the first three criteria to determine whether the penalization is required.

I retrieved data on sediment delivery using the Watershed Erosion Prediction Project (WEPP) online GIS tool [28]. This tool takes as input soil textures, treatment types, years of simulation, and custom climate data. I obtained soil texture data for the area from the USDA’s Soil Survey Geographic (SSURGO) database. Treatment types are those specified in §B, and the years of simulation correspond to the planning horizon of the model. The custom climate data was obtained through the Climate-FVS climate data server [15]. Using the climate data provided by Climate-FVS in the sediment delivery simulations ensured consistency of climate parameters with the simulations for the Drink’s vegetation.

The Multi-objective MIP

The first objective in the model is to minimize the average fuel model at the end of the 80-year planning horizon:

$$\text{Minimize } F = \sum_{i \in I} \sum_{r \in R} F_{i,r} x_{i,r} \quad (1.1)$$

In equation (1.1), I sum over all stands $i \in I$ and all treatment prescriptions $r \in R$ to obtain a cumulative fire hazard metric F , which measures the total fire hazard of the area at the end of the planning horizon. The coefficients $F_{i,r}$ are the area-weighted fuel models of each

stand $i \in I$ at the end of the planning horizon if stand i is assigned to treatment prescription $r \in R$. The possible treatment prescriptions $r \in R$ are treat in the first period ($r = 1$), treat in the second period ($r = 2$), treat in both periods ($r = 3$), or do not treat ($r = 0$).

The second objective is to minimize the peak short-term sediment delivery that results from performing treatments in either period one (S_1) or period two (S_2):

$$\text{Minimize } S = \max\{S_1, S_2\} \quad (1.2)$$

The last objective is to maximize the area of suitable northern spotted owl habitat at the end of the planning horizon.

$$\text{Maximize } O = \sum_{i \in I_\omega} \left(a_i p_i + e a_i \left(\sum_{j \in R_i} x_{i,j} - p_i \right) \right) \quad (1.3)$$

The set of stands in the sum $i \in I_\omega$ are those that meet the first three criteria for NSO habitat under at least one treatment prescription $j \in R_i$, where R_i is the set of treatment prescriptions for stand i such that it meets the first three NSO habitat criteria at the end of the planning horizon. If a stand i does not meet these criteria under any treatment prescriptions (if the set $R_i = \{\emptyset\}$), then $i \notin I_\omega$. If the model assigns a stand $i \in I_\omega$ a treatment prescription $j \in R_i$, then stand i meets the first three NSO habitat criteria at the end of the planning horizon, and the variable $x_{i,j} = 1$. If, in addition, the stand i is part of a cluster of stands all meeting the first three NSO habitat criteria and whose combined contiguous area is greater than 200 ha, then the variable $p_i = 1$. Notice that when $p_i = 0$, the stand's contribution is discounted by $e = 0.5$, and when $p_i = 1$ it is not.

The objectives are subject to the following constraints. First, I define accounting variables for the sediment delivery that results from the performance of the prescribed management actions.

$$\sum_{i \in I} \sum_{r \in 1,3} s_{i,1} x_{i,r} = S_1 \quad (1.4)$$

$$\sum_{i \in I} \sum_{r \in 2,3} s_{i,2} x_{i,r} = S_2 \quad (1.5)$$

The coefficients $s_{i,t}$ are the amount of sediment (in tonnes) that would result from treating stand i in time period t .

In order to control the trigger variables p_i indicating a stand's inclusion in a 200 ha cluster of NSO habitat, I used the following two constraints:

$$\sum_{i \in D_c} \sum_{j \in R_i} x_{i,j} - |c|q_c \geq 0 \quad \forall c \in C \quad (1.6)$$

$$\sum_{c \in C_i} q_c - p_i \geq 0 \quad \forall i \in I_\omega \quad (1.7)$$

$c \in C$ are the clusters of stands whose combined area is greater than 200 ha. A cluster c contains the set of stands $i \in D_c$. Equation (1.6) specifies that all stands $i \in D_c$ within a cluster $c \in C$ must be assigned a management prescription such that they meet all NSO habitat criteria in order for the cluster trigger variable q_c to take value 1.

Equation (1.7) specifies that if no cluster $c \in C_i$ - the set of clusters that contain site i - meets NSO qualifications, then the trigger variable p_i must equal 0. If some cluster $c \in C_i$ does meet NSO qualifications, then the objective function (1.3) will draw up the value of the variable p_i to 1.

I also impose the restriction that each stand may be assigned to at most one treatment prescription.

$$\sum_{r \in R} x_{i,r} = 1 \quad \forall i \in I \quad (1.8)$$

Next, I ensured that the area treated in each time period is less than a prespecified maximum area A :

$$\sum_{i \in I} \sum_{r \in 1,3} a_i x_{i,r} = H_1 \quad (1.9)$$

$$\sum_{i \in I} \sum_{r \in 2,3} a_i x_{i,r} = H_2 \quad (1.10)$$

$$H_1 \leq A \quad (1.11)$$

$$H_2 \leq A \quad (1.12)$$

where the first two equations define the accounting variables for the areas treated in time periods 1 and 2, H_1 and H_2 , and the second two equations impose the upper bound.

Finally, I specified fluctuation constraints to bound the differences in the area treated in between time periods:

$$\ell H_1 - H_2 \leq 0 \quad (1.13)$$

$$-u H_1 + H_2 \leq 0 \quad (1.14)$$

I define a maximum of 20% fluctuation between time periods. That is, $\ell = 0.8$ and $u = 1.2$.

Together with the binary specifications on our variables (equation (1.15)), the complete model is

Minimize

$$F = \sum_{i \in I} \sum_{r \in R} F_{i,r} x_{i,r}$$

$$S = \max\{S_1, S_2\}$$

Maximize

$$O = \sum_{i \in I_\omega} \left(a_i p_i + e a_i \left(\sum_{j \in R_i} x_{i,j} - p_i \right) \right)$$

Subject to:

$$\begin{aligned}
\sum_{i \in I} \sum_{r \in 1,3} s_{i,r} x_{i,r} &= S_1 \\
\sum_{i \in I} \sum_{r \in 2,3} s_{i,r} x_{i,r} &= S_2 \\
\sum_{i \in D_c} \sum_{j \in R_i} x_{i,j} - |c| q_c &\geq 0 \quad \forall c \in C \\
\sum_{c \in C_i} q_c - p_i &\geq 0 \quad \forall i \in I_\omega \\
\sum_{r \in R} x_{i,r} &= 1 \quad \forall i \in I \\
\sum_{i \in I} \sum_{r \in 1,3} a_i x_{i,r} &= H_1 \\
\sum_{i \in I} \sum_{r \in 2,3} a_i x_{i,r} &= H_2 \\
H_1 &\leq A \\
H_2 &\leq A \\
\ell H_1 - H_2 &\leq 0 \\
-u H_1 + H_2 &\leq 0 \\
x_{i,r}, p_i, q_c &\in \{0, 1\} \quad \forall i \in I, r \in R, c \in C
\end{aligned} \tag{1.15}$$

1.2.4 Model solution

Solving a bounded and non-degenerate multi-objective optimization problem with N objectives produces a set of objective vectors (also called “solutions”) $\mathbf{z} \in Z$ where $\mathbf{z} = \langle z^1, \dots, z^N \rangle$. The set of solutions Z is referred to as the Pareto-optimal frontier or efficient frontier or, simply, frontier. The solutions comprising an efficient frontier have the special relationship such that no component of a solution \mathbf{z}^i can be improved upon without one of the other components \mathbf{z}^j ($j \neq i$) degrading. For example, this relationship in the current problem means that further reducing fire hazard would require either additional sediment deposits,

the sacrifice of NSO habitat, or both.

Thus the efficient frontier provides information on the tradeoff structure that exists between ecosystem services. Parameterizing and solving the model for each of the climate scenarios generates three frontiers: Z_{None} , $Z_{4.5}$, and $Z_{8.5}$ for the No climate change, Ensemble RCP 4.5, and Ensemble RCP 8.5 scenarios, respectively. As climate is the driver of the differences in these frontiers, the comparison of frontiers provides insight into how climate impacts the tradeoff structures between the ecosystem services.

To solve the models, I wrote my own implementation of Tóth’s Alpha-Delta algorithm [60] that is generalized for any multi-objective problem with $N \geq 2$ objectives. The Alpha-Delta algorithm finds the optimal set Z by iteratively slicing the N -dimensional objective space with a tilted $N - 1$ dimensional plane. To derive the frontiers, I used an alpha parameter of $\alpha = .01$ and delta parameters of $\delta_{Hab} = 1$ ha and $\delta_{Sed} = 0.5$ tonnes for the NSO habitat and sediment delivery objectives, respectively.

1.2.5 Comparing Tradeoffs under each Climate Change Scenario

No standardized procedure exists for comparing frontiers or measuring the conflict between objectives within a frontier. To address the former, I draw on methods used in the field of evolutionary multi-objective optimization (EMO). To address the latter, I apply methods used in objective pruning in many-objective optimization.

Comparing frontiers

Researchers in the field of EMO develop algorithms to generate a set of non-dominated solutions that best represent the true Pareto-optimal frontier [19]. To test their algorithms, they compare their resulting frontiers to a known Pareto front for benchmark multi-objective optimization problems [39]. There is no assurance of optimality of the solutions derived using these algorithms, so they require a means of comparing the resulting frontiers to determine if one algorithm produces a “better” non-dominated frontier than another. Zitzler et al. provide a review of comparison methods in [70]. These methods aim to quantify certain

traits about a frontier that can be used to measure their success in approximation of the true frontier.

My motivation in comparing frontiers is different from EMO in that, rather than comparing non-dominated sets produced by identical models, I aim to compare frontiers generated by models with the same structure but different parameterizations. As a result, not all comparison methods are applicable, such as the indicator for the number of Pareto points contained in the frontier (all points on my frontiers are Pareto-optimal). However, other comparison methods still have value in our analysis. I chose a subset of these methods: the binary epsilon and binary hypervolume indicators, and the unary distance, unary hypervolume, and unary spacing indicators.

Note that use of some comparison methods for the frontiers requires the normalization of the objective space. This is because the climate scenarios may significantly alter the bounds on the achievable values of the ecosystem services, resulting in frontiers whose objective spaces will not necessarily overlap and with incomparable distributions of solutions within. The chosen normalization of each frontier is the unit hypercube, with each objective bounded between 0 and 1, yielding a frontier bounded by $[0, 1]^N$. Without loss of generality, I convert all objectives to maximization, define the nadir solution to be at the origin and the ideal solution to be at the point $\vec{1}$. The nadir solution \mathbf{z}_{nad} of a frontier of points $z \in Z$ is defined as the objective vector with components

$$\mathbf{z}_i^{\text{nad}} = \inf_z \{z_i\} \quad \forall 1 \leq i \leq N \quad (1.16)$$

and the ideal solution is the objective vector with components

$$\mathbf{z}_i^{\text{ideal}} = \sup_z \{z_i\} \quad \forall 1 \leq i \leq N \quad (1.17)$$

Binary epsilon indicator I_ϵ Given two frontiers, Z_1 and Z_2 , the binary epsilon indicator is defined as [70]

$$I_\epsilon(Z_1, Z_2) = \inf_{\epsilon \in \mathbb{R}} \{ \forall \mathbf{z}_2 \in Z_2 \exists \mathbf{z}_1 \in Z_1 : \mathbf{z}_1 \succeq_\epsilon \mathbf{z}_2 \} \quad (1.18)$$

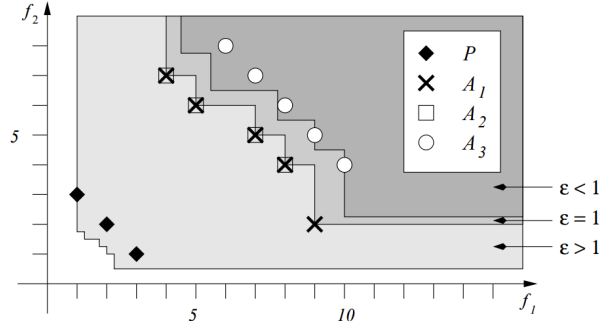


Figure 1.5: Any frontier Z with solutions in the light gray area (closest to origin) would have $I_\epsilon(Z, A_1) > 1$; $I_\epsilon(A_1, A_1) = I_\epsilon(A_2, A_1) = 1$; any frontier Z existing only in the darker gray areas such as A_3 would have $I_\epsilon(Z, A_1) < 1$

where \succeq_ϵ is the ϵ -dominance relationship:

$$\mathbf{z}_1 \succeq_\epsilon \mathbf{z}_2 \iff \forall 1 \leq i \leq N : \epsilon \mathbf{z}_1^i \geq \mathbf{z}_2^i \quad (1.19)$$

That is, ϵ is the minimum factor by which all points in one frontier Z_1 must be multiplied such that all solutions in Z_1 at least weakly dominate all solutions in the other frontier Z_2 .

Unary hypervolume indicator I_{H1} and binary hypervolume indicator I_{H2} For a frontier Z comprised of solutions $\mathbf{z} = \langle z^1, \dots, z^N \rangle$ and with the objective space defined such that the origin is the nadir point, then the volume of a single solution \mathbf{z}_i is the volume of the hyperrectangle r_i whose diagonal corners are the origin and the solution \mathbf{z}_i . The hypervolume of the frontier is the volume of the union of the hyperrectangles corresponding to the solutions in the frontier:

$$I_{H1}(Z) = \text{vol} \left(\bigcup_{i=1}^{|Z|} r_i \right) \quad (1.20)$$

Then define the binary hypervolume indicator of two frontiers Z_1 and Z_2 as [69]

$$I_{H2}(Z_1, Z_2) = I_{H1}(Z_1 + Z_2) - I_{H1}(Z_2) \quad (1.21)$$

Relation	Solutions		Frontiers	
Strictly dominates	$\mathbf{z}^1 \succ \mathbf{z}^2$	\mathbf{z}_i^1 is better than $\mathbf{z}_i^2 \quad \forall 1 \leq i \leq N$	$Z_1 \succ Z_2$	$\exists \mathbf{z}^1 \in Z_1 \succ \text{succ} \mathbf{z}^2 \quad \forall \mathbf{z}^2 \in Z_2$
Dominates	$\mathbf{z}^1 \succ \mathbf{z}^2$	$\exists 1 \leq i \leq N : \mathbf{z}_i^1$ is better than \mathbf{z}_i^2 , and \mathbf{z}_i^1 is not worse than $\mathbf{z}_i^2 \quad \forall 1 \leq i \leq N$	$Z_1 \succ Z_2$	every $\mathbf{z}^2 \in Z_2$ is dominated by at least one $\mathbf{z}^1 \in Z_1$
Better			$Z_1 \triangleright Z_2$	every $\mathbf{z}^2 \in Z_2$ is weakly dominated by at least one $\mathbf{z}^1 \in Z_1$ and $Z_1 \neq Z_2$
Weakly dominates	$\mathbf{z}^1 \succeq \mathbf{z}^2$	\mathbf{z}^1 is at least as good as \mathbf{z}^2 in all objectives	$Z_1 \succeq Z_2$	All solutions in $\mathbf{z}^2 \in Z_2$ are weakly dominated by a solution $\mathbf{z}^1 \in Z_1$
Incomparable	$\mathbf{z}^1 \parallel \mathbf{z}^2$	Neither \mathbf{z}^1 nor \mathbf{z}^2 weakly dominates the other	$Z_1 \parallel Z_2$	Neither Z_1 nor Z_2 weakly dominates the other

Table 1.1: Definitions of dominance relations between solutions and frontiers [70]

Name of indicator	Relation					
	\succ	\triangleright	\succeq	$=$	\parallel	
I_ϵ	$I_\epsilon(Z_1, Z_2) < 1$	-	$I_\epsilon(Z_1, Z_2) \leq 1 \quad I_\epsilon(Z_2, Z_1) > 1$	$I_\epsilon(Z_1, Z_2) \leq 1$	$I_\epsilon(Z_1, Z_2) = 1 \quad I_\epsilon(Z_2, Z_1) = 1$	$I_\epsilon(Z_1, Z_2) > 1 \quad I_\epsilon(Z_2, Z_1) > 1$
I_{H2}	-	-	$I_{H2}(Z_1, Z_2) > 0 \quad I_{H2}(Z_2, Z_1) = 0$	$I_{H2}(Z_1, Z_2) \geq 0 \quad I_{H2}(Z_2, Z_1) = 0$	$I_{H2}(Z_1, Z_2) = 0 \quad I_{H2}(Z_2, Z_1) = 0$	$I_{H2}(Z_1, Z_2) > 0 \quad I_{H2}(Z_2, Z_1) > 0$
I_d	-	-	-	-	-	-
I_s	-	-	-	-	-	-

Table 1.2: Tests using indicators to determine dominance relationships between frontiers [70]. While general tests of dominance relationships may not be available for some metrics (any cell with '-'), conclusions may still be drawn. For instance, $I_d(Z_1) < I_d(Z_2) \Rightarrow Z_2 \not\triangleright Z_1$.

where $I_{H1}(Z_1 + Z_2)$ is the unary hypervolume indicator of the merged frontier consisting of all solutions from frontiers Z_1 and Z_2 . The binary hypervolume indicator provides the volume of frontier Z_1 that is not contained within frontier Z_2 . Larger values of I_{H1} correspond to frontiers occupying larger fractions of the objective space, indicating less conflict between the objectives. For frontiers Z_1 and Z_2 in comparable scales (that is, in normalized objective spaces), if $I_{H2}(Z_1, Z_2) > I_{H2}(Z_2, Z_1)$ this indicates less conflict between objectives in Z_1 than in Z_2 . I_{H2} can also be used to determine other dominance relationships between frontiers (see Tables 1.1 and 1.2).

I developed a custom algorithm to solve for the unary hypervolume indicator. The details of the algorithm may be found in §A.

Unary distance indicator I_d The unary distance indicator used for the analysis is analogous to the unary distance indicator described in [17], but instead of computing the distance to a reference Pareto frontier I measure the average distance from the frontier to the ideal

solution:

$$I_d = \frac{\sum_{\mathbf{z} \in Z} \|\mathbf{z}^{\text{ideal}} - \mathbf{z}\|}{N} \quad (1.22)$$

Smaller values of I_d correspond to frontiers that are closer to the ideal solution, which implies less conflict between the objectives.

Unary Spacing Indicator I_s The unary spacing indicator, or Schott's spacing metric[54], computes the standard deviation of the distance between points in the frontier, defined as

$$I_s = \sqrt{\frac{1}{N-1} \sum_{\mathbf{z} \in Z} (d_z - \bar{d})^2} \quad (1.23)$$

where

$$d_z = \min_{\mathbf{y} \in Z, \mathbf{y} \neq \mathbf{z}} \|\mathbf{z} - \mathbf{y}\| \quad (1.24)$$

and \bar{d} is the average of all d_z . In EMO, the spacing indicator provides a measure of an algorithm's ability to search the frontier space uniformly. Here, the spacing metric provides a measure of the flexibility afforded to the decision maker under each climate scenario. Larger spacing metrics imply larger sacrifices between decisions and less flexibility.

Quantifying conflict between objectives within a frontier

The above methods provide frontier-level metrics of conflict and tradeoffs. To determine the degree of conflict between two objectives within a single frontier, we employ an approach used in many-objective optimization. Given the increased difficulty in solving many-objective optimization problems [38], researchers in this field seek to reduce the number of objectives considered in the model. To determine which objectives most strongly influence the shape of the frontier, they compute the correlation between each pair of objectives [20]. The objective pairs with the most negative correlation are most in conflict. To rank the relative conflict between objectives in each climate scenario, I compute their Pearson correlation coefficients:

$$\rho_{X,Y} = \frac{\text{cov}(X,Y)}{\sigma(X)\sigma(Y)} \quad (1.25)$$

where, for objectives x and y , X and Y are

$$X = \{\mathbf{z}_x^1, \mathbf{z}_x^2, \dots, \mathbf{z}_x^{|Z|}\} \quad (1.26)$$

$$Y = \{\mathbf{z}_y^1, \mathbf{z}_y^2, \dots, \mathbf{z}_y^{|Z|}\} \quad (1.27)$$

1.3 Results and Discussion

DRAFT

The frontiers for each climate scenario can be found in Figure ...

1.4 Conclusion

DRAFT

I find that climate change has positive impacts on the tradeoff structure between managed ecosystem services in the Drink Area ...

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Appendix A

COMPUTING A FRONTIER'S HYPERVOLUME INDICATOR

Given a set of Pareto optimal solutions \mathcal{P} to a multi-objective mathematical programming model with a set of objectives O of cardinality $N := |O|$, this algorithm computes the volume V of the objective space bounded by the Pareto frontier defined by the solutions $x \in \mathcal{P}$. The objectives are assumed to be normalized so that the objective space is the N -dimensional unit hypercube with the origin and the point $\vec{1}$ defining the nadir objective vector and the ideal objective vector, respectively. That is, all objectives are assumed to be maximized with bounds $[0, 1]$.

The algorithm projects the objective space into $N - 1$ dimensions by eliminating the dimension associated with an (arbitrarily-chosen) objective $p \in O$. The set of objectives is $\bar{O} := O \setminus \{p\}$. It is assumed that $x \in \mathcal{P}$ are sorted in descending order according to p . The algorithm proceeds by sequentially adding solutions to the $(N - 1)$ -dimensional space, and calculating the contribution to the frontier volume as a product of the volume contribution in $N - 1$ dimensions and its achievement in objective p .

Let \bar{V}_x be the $(N - 1)$ -dimensional volume contribution of solution x and x_p be the achievement of solution x in objective p . Further, let F be the set of non-dominated solutions in $N - 1$ dimensions. I compute the N -dimensional volume of the frontier V as follows.

Figure A.1: Algorithm to compute the unary hypervolume indicator of a Pareto frontier.

```

1:  $V \leftarrow 0$ 
2:  $\bar{V} \leftarrow 0$ 
3:  $F \leftarrow \emptyset$ 
4: for all  $x \in \mathcal{P}$  do
5:    $\bar{V}_x \leftarrow \prod_{o \in \bar{O}} x_o - \bar{V}$ 
6:   for all  $f \in F$  do
7:     if  $f_o < x_o \forall o \in \bar{O}$  then
8:        $F \leftarrow F \setminus \{f\}$ 
9:     end if
10:  end for
11:  for all  $o \in \bar{O}$  do
12:     $F_{x,o} := \{f \in F : f_o > x_o\}$ 
13:    Sort  $f \in F_{x,o}$  in ascending order by their  $o$ th component,  $f_o$ 
14:     $v_i \leftarrow x_o$ 
15:    for all  $f \in F_{x,o}$  do
16:       $v_t \leftarrow f_o$ 
17:       $\delta_o := v_t - v_i$ 
18:       $\bar{V}_x \leftarrow \bar{V}_x + \delta_o \prod_{\sigma \in \bar{O} \setminus \{o\}} f_\sigma$ 
19:       $v_i \leftarrow v_t$ 
20:    end for
21:  end for
22:   $F \leftarrow F \cup \{x\}$ 
23:   $\bar{V} \leftarrow \bar{V} + \bar{V}_x$ 
24:   $V \leftarrow V + x_p \bar{V}_x$ 
25: end for

```

Appendix B

TREATMENT SPECIFICATION FOR THE DRINK AREA

TREATMENT SPECIFICATION FOR THE DRINK PLANNING AREA

Stand density index ¹	Crown bulk density, kg/m ³	Number of trees <18 cm dbh per ha	Fuel model	Combined basal area of mountain hemlock and white fir >46 cm dbh, (m ²)	Treatment
Lodgepole pine plant association					
<87	NA	NA	NA	NA	Prescribed burning ²
>=87	>0.037	>49	>=10	NA	Thin & Pile and burn slash and fuels ³
			<10	NA	Thin & Pile and burn slash
Mixed conifer wet or Mountain Hemlock plant associations					
<87	NA	NA	NA	NA	Prescribed burning
>=87	>0.037	>49	=10	>7.5	Thin & Pile and burn slash and fuels & Prescribed burning
			<=7.5	Thin & Pile and burn slash and fuels	
			>=11	NA	Thin & Pile and burn slash and fuels
			<10	NA	Thin & Pile and burn slash
	<=0.037	<=49	=10	>=7.5	Prescribed burning
		NA	=10	>=7.5	Prescribed burning
	NA	NA	=6,8,9 or 10	NA	Prescribed burning (if prescribed burning occurred in period 1; the treatment applies to second period only)
	Mixed Conifer dry plant association				
<87	NA	NA	NA	NA	Prescribed burning
>=87	>0.037	>49	=10 or 11	NA	Thin & Pile and burn slash and fuels & Prescribed burning
			>=12	NA	Thin & Pile and burn slash and fuels
			<10	NA	Thin & Pile and burn slash
			<=49	=10 or 11	NA
	<=0.037	NA	=10 or 11	NA	Prescribed burning
	NA	NA	=6,8,9 or 10	NA	Prescribed burning (if prescribed burning occurred in period 1; the treatment applies to second period only)

Unless otherwise specified, vegetation conditions are assessed at the beginning of each planning period. If the conditions are met a corresponding combination of treatments is scheduled. No treatment is applied if none of the criteria is met.

¹ The stand density index is in metric units; conversion to imperial units is need for simulations using Forest Vegetation simulator.

² Prescribed burning is an application of prescribed fire, a fire ignited by management actions to meet specific objectives (Glossary of Wildland Fire Terminology, 2012).

³ Pile and burn slash assumes removal of the cut trees only, while pile and burn slash and fuels involves removal of the materials that were on the ground before thin (Wall, Powers, 2012; personal communication).