```
In [2]: from typing import Callable, List
                                       import numpy as np
                                       import matplotlib.pyplot as plt
                                       import scienceplots
                                       plt.style.use(['science', 'bright'])
      In [ ]: def sumSeries(
                                                     series: Callable[[float, int, float], float],
                                                     coefs: List[float],
                                                     args: List[float],
                                                     optimize: bool = False
                                       ) -> float:
                                                     if optimize:
                                                                   return np.sum(np.sum(func(coefs, np.array(range(coefs.size)), i)) for i in args)
                                                     else:
                                                                    sum = 0
                                                                    for x in args:
                                                                                   tmp = 0
                                                                                   for n in range(coefs.size):
                                                                                                tmp += series(coefs[n], n, x)
                                                                                   sum += tmp
                                                                    return sum
                                       func = lambda coef, n, arg: coef * np.cos(n * arg)
In [116...
                                       x = np.linspace(-2 * np.pi, 2 * np.pi, num = 10**3, endpoint = True)
In [117...
                                      N = 10
                                       coefs = np.ones(N)
                                       coefs[:int(N / 3)] = [(2 * n + 1) / 3 for n in range(int(N / 3))]
                                       coefs[int(2 * N / 3):] = [1 / n for n in range(int(2 * N / 3), N)]
                                       def getCoefArray(N: int) -> np.array:
                                                     coefs = np.ones(N)
                                                      coefs[:int(N / 3)] = [(2 * n + 1) / 3 for n in range(int(N / 3))]
                                                     coefs[int(2 * N / 3):] = [1 / n for n in range(int(2 * N / 3), N)]
                                                     return coefs
In [125...
                                       %%time
                                       sum = sumSeries(func, getCoefArray(10), x, optimize = False)
                                       print(sum)
                                      339.54563492063386
                                      CPU times: total: 31.2 ms
                                     Wall time: 18 ms
In [126... %%time
                                       sum = sumSeries(func, getCoefArray(10), x, optimize = True)
                                       print(sum)
                                       339.5456349206339
                                      CPU times: total: 15.6 ms
                                      Wall time: 14 ms
                                      \verb|C:\USers\dinoz.DESKTOP-98K3K7L\AppData\Local\Temp\ipykernel\_24064\4253160851.py:9: DeprecationWarning: Call the property of the property o
                                       ing np.sum(generator) is deprecated, and in the future will give a different result. Use np.sum(np.fromiter
                                       (generator)) or the python sum builtin instead.
                                       return np.sum(np.sum(func(coefs, np.array(range(coefs.size)), i)) for i in args)
In [128... fig, ax = plt.subplots(1, 1, figsize = (4, 4), dpi = 300)
                                       ax.set_title(r"$\sum_{n = 0} a_n \cos((n x))$")
                                       ax.plot(x, [np.sum(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r"(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r'(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r'(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ for \ i \ in \ x], \ \ label = r'(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ label = r'(func(getCoefArray(5), np.array(range(getCoefArray(5).size)), i)) \ \ label = r'(func(getCoefArray(5).size)), i) \ \ label =
                                       ax.plot(x, [np.sum(func(getCoefArray(10), np.array(range(getCoefArray(10).size)), i)) \ \ for \ i \ in \ x], \ label = range(func(getCoefArray(10), np.array(range(getCoefArray(10).size)), i)) \ \ for \ i \ in \ x], \ label = range(func(getCoefArray(10), np.array(range(getCoefArray(10).size)), i)) \ \ for \ i \ in \ x], \ label = range(func(getCoefArray(10), np.array(range(getCoefArray(10).size)), i)) \ \ for \ i \ in \ x], \ label = range(getCoefArray(10).size)), \ \ in \ \ in \ \ x], \ \ label = range(getCoefArray(10).size)), \ \ in \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ x \ \ 
                                       ax.plot(x, [np.sum(func(getCoefArray(15), np.array(range(getCoefArray(15).size)), i)) for i in x], label = r
                                       plt.legend(bbox_to_anchor = (1, 0.5), loc = 'center left')
                                       plt.show()
```

