

## CONTINUOUS LINEAR FUNCTIONALS

## Why

We can characterize the continuous linear functionals.

## Main result

**Proposition 1.** Let F be a linear functional on a normed space  $(V, \|\cdot\|)$ . The following are equivalent:

- 1. F is continuous;
- 2. F is continuous at 0;
- 3.  $\sup_{\|x\| \le 1} \{ |F(x)| \} < \infty.^1$

For this reason we often call continuous linear functionals the bounded linear functionals or call them continuous bounded linear functionals.

<sup>&</sup>lt;sup>1</sup>Future editions will include an account, and that will fill out this sheet.

