

Natural Square Roots

Why

We want to solve equations with squares.

Definition

Let m be a square number. We want to find n to satisfy

$$n^2 = m$$
.

We call such an n a square root of m.

Proposition 1. The square root of a square number is unique.

This result motivates defining a function the square root function which square numbers to their roots.

Notation

Let $S \subset \mathbf{N}$ denote the set of square numbers. Let $f: S \to N$ be the function such that f(s) is the square root of s. We denote the result of f on n by \sqrt{n} .

