

## **PARTITIONS**

## Why

We divide a set into disjoint subsets whose union is the whole set. In this way we can handle each subset of the main set individually, and so handle the entire set piece by piece.

## **Definition**

A partition of a set X is a set of pairwise disjoint (see Set Decompositions) subsets of X whose union is X. We call the elements of a partition the pieces of the partition. When speaking of a partition, we commonly call the set of sets mutually exclusive (by which we mean that they are pairwise disjoint) and collectively exhaustive (by which we mean that their union is full set).

## **Notation**

Let X be a set and  $\mathcal{C}$  be a set of subsets of X.  $\mathcal{C}$  is a partition of X means  $(\forall A)(\forall B)((A \in \mathcal{C} \land A \in \mathcal{C}) \longrightarrow A \cap B = \emptyset)$  and  $\bigcup \mathcal{C} = X$ .

