



# Real Functions

## 1 Why

We define functions mapping real numbers to real numbers.

## 2 Definition

A **real function** is a real-valued function on a subset of real numbers. The domain is often an interval.

### 2.1 Notation

$f : \mathbf{R} \rightarrow \mathbf{R}$ .  $f$  is a real function. To speak of functions defined on intervals, let  $a, b \in \mathbf{R}$ .  $g : [a, b] \rightarrow \mathbf{R}$ . is a real function defined on a closed interval.  $h : (a, b) \rightarrow \mathbf{R}$  is a real function defined on an open interval.

We regularly declare the interval and the function in one pass: Let  $f : [a, b] \rightarrow \mathbf{R}$ , read aloud as “ $f$  from closed  $a$   $b$  to  $\mathbf{R}$ .” Or, let  $f : (a, b) \rightarrow \mathbf{R}$  read aloud as “ $f$  from open  $a$   $b$  to  $\mathbf{R}$ ”.