**Definition**

An *orthonormal family of vectors* in an inner product space is a family of vectors with unit norm.

**Proposition 1.** *An orthogonal family of vectors can be made orthonormal.*

Orthonormal Set of Vectors

Real Inner Product Norms

Orthonormal Set of Real Vectors

Real Inner Products

Norms

Real Inner Product

Functionals

Space Inner Product

Real Norm

Vectors

Space Norm

Real Vector

N-Dimensional Space

Plane Inner Product

Plane Norm

Plane Vector Sums and Differences

Space Vector

Distance

Right Triangle Sides Relation

Plane Vector

Absolute Value

Real Square Roots

Space Distance

Real Square

Plane Distance

Real Arithmetic

Interval Length

Real Multiplicative Inverse

Natural Square Roots

Intervals

Real Products

Real Additive Inverse

Real Sums

Square Numbers

Real Space

Real Plane

Real Line

Rational Multiplicative Inverse

Rational Arithmetic

Integral Line

Square

Real Order

Rational Order

Real Numbers

Rational Products

Rational Sums

Fields

Geometry

Rational Number

Rings

Integer Arithmetic

Lists

Set Numbers

Natural Multiplicative Identity

Natural Additive Identity

Integer Products

Direct Products

Finite Sets

Identity Elements

Arithmetic

Natural Powers

Equivalent Sets

Inverse Elements

Family Unions and Intersections

Function Inverses

Element Functions

Comparisons

Integer Order

Integer Sums

Natural Products

Natural Equations

Families

Function Composites

Function Images

Operations

Order

Integer Number

Natural Sums

Equations

Equivalence Relations

Functions

Converse Relations

Natural Order

Recursion Theorem

Relations

Peano Axioms

Set Products

Natural Induction

Generalized Set Dualities

Set Powers

Natural Numbers

Set Unions and Intersections

Partitions

Intersection of Empty Set

Set Dualities

Unordered Triples

Successor Sets

Set Symmetric Differences

Set Intersections

Ordered Pairs

Pair Unions

Set Complements

Pair Intersections

Set Unions

Set Differences

Unordered Pairs

Empty Set

Set Specification

Set Equality

Set Inclusion

Standardized Accounts

Accounts

Deductions

Quantified Statements

Logical Statements

Statements

Sets

Identities

Names

Letters

Objects