

### INTEGER ORDER

# Why

We want to order the integers.

#### Definition

Consider  $[(a,b)], [(b,c)] \in \mathbf{Z}$ . If a+d < b+c, then we say that [(a,b)] is less than [(b,c)].<sup>1</sup> If [(a,b)] is less than [(b,c)] or equal, then we say that [(a,b)] is less than or equal to [(b,c)].

#### **Notation**

If  $x, y \in \mathbf{Z}$  and x is less than y, then we write x < y. If x is less than or equal to y, we write  $x \le y$ .

## Positive and Negative Integers

We call an integer z positive if z > 0 and we call z negative if  $z < 0.^2$  We call an integer z nonnegative if z > 0 or z = 0 and nonpositive if z < 0 or z = 0.

#### Notation

We denote the set  $\{z \in \mathbf{Z} \mid z \geq 0_Z\}$  by  $\mathbf{Z}_{++}$ .

<sup>&</sup>lt;sup>1</sup>One needs to show that this is well-defined. The account will appear in future editions.

<sup>&</sup>lt;sup>2</sup>Some authors use the term positive for the case when z > 0 or z = 0. We use the term nonnegative in this case.

