Extremal Trace Problems