

#### Rooted Trees

## 1 Why

We want to talk about orienting the edges of a tree away from a given vertex.

### 2 Definition

A rooted tree is an ordered pair consisting of a tree and a distinguished vertex, which we call the root. The parent of a given non-root vertex is the first vertex on the path from the given vertex to the root. Conversely, that given vertex is the child of its parent. Since there is only one path to the root, each non-root vertex has only one parent. We define the parent of the root to be the root itself.

#### 2.1 Notation

Let T = (V, E) be a tree. We denote the tree T rooted at vertex v by (T, v).

# 3 Properties

**Proposition 1.** Let (T, v) be a rooted tree. In the directed graph corresponding to this rooted tree every vertex has one parent.

