

#### INDUCTORS

## Why

We want to talk about learning associations between objects in time or space.

#### Definition

Let A and B be sets. An *inductor* is a function mapping a dataset of records in  $A \times B$  to a function from A to B. We call the elements of A the *precepts* and the elements of B the *postcepts*.

We call a function from the precepts to the postcepts a *predictor*. We call the result of a precept under a predictor a *prediction*. An inductor maps datasets to predictors. A predictor maps precepts to postcepts.

#### Notation

Let D be a dataset of size n in  $A \times B$ . Let  $g: A \to B$ , a predictor, which makes prediction g(a) on precept  $a \in A$ . Let  $f: (A \times B)^n \to (A \to B)$ , an inductor. Then f(D) is the predictor which the inductor associates with dataset D.

# Other terminology

Many authorities call the precepts the *independent variables*, *inputs*, *covariates*, *pattern* or *observations*. Similarly, some call the postcepts the *dependent variables*, *outputs*, *targets*, *outcomes* or *observational outcomes*. Some call a predictor an

*input-output* mapping. A predictor is sometimes called a *point* predictor.<sup>1</sup> Some authors refer to a prediction as a quess.

### Learning algorithms

We use a predictor to make guesses on precepts which do not appear in the dataset that was used to construct the predictor. We refer to the task of proposing a predictor for a particular dataset a *learning problem*.

It is common in this context to refer to an inductor as a learning algorithm and call the task or problem of constructing a predictor from a dataset supervised learning. By supervision, we mean to indicate that we have the postcepts corresponding to the precepts.

In line with this usage, the postcepts are often called *labels* and the labels are said "to provide supervision." In this context, the dataset used to construct the predictor (i.e., the argument to the inductor) is called the *training dataset*.

<sup>&</sup>lt;sup>1</sup>Future editions may remove this. The intuition for the word point is from the real numbers, which we need not have discussed for this point.

