



NORMAL CONDITIONALS

Why

What of the conditional densities of a multivariate normal density.

Result

Prop. 1. *Let $f : \mathbf{R}^d \rightarrow \mathbf{R}$ be a normal density with mean $\mu \in \mathbf{R}^d$ and covariance $\Sigma \in \mathbf{S}^d$.*

$$\mu = \begin{bmatrix} \mu_x \\ \mu_y \end{bmatrix} \quad \text{and} \quad \Sigma = \begin{bmatrix} \Sigma_{xx} & \Sigma_{xy} \\ \Sigma_{yx} & \Sigma_{yy} \end{bmatrix}$$

The conditional density $f_{x|y}(\xi, \gamma)$ is $\mathcal{N}(\bar{\mu}(\gamma), \bar{\Sigma})$ where

$$\bar{\mu}(\gamma) = \mu_1 + \Sigma_{xy}\Sigma_{yy}^{-1}(\gamma - \mu_y) \text{ and } \bar{\Sigma} = \Sigma_{xx} - \Sigma_{xy}\Sigma_{yy}^{-1}\Sigma_{yx}.$$

