



GEOMETRY

Why

We need some basic geometric concepts.¹

Definitions

A *point* is that which has no part.² A *line* is a breadthless length. The *extremities of a line*³ are points. A *straight line* is a line which lies evenly with the points on itself. A *surface* is that which has length and breadth only. The *extremities of a surface* are lines.

A *plane surface* is a surface which lies evenly with the straight lines on itself. A *plane angle* is the inclination to one another of two lines in a plane which meet one another and do not lie in a straight line. And when the lines containing the angle are straight, the angle is called *rectilineal*. When a straight line set up on a straight line makes the adjacent angles equal to one another, each of the equal angles is *right*, and the straight line standing on the other side is called a *perpendicular* to that on which it stands.

An *obtuse angle* is an angle greater than a right angle. An *acute angle* is an angle less than a right angle. A *boundary* is

¹This sheet will be expanded into several in future editions.

²This and all that follows is taken (nearly) verbatim from Heath's translation of the Book I of Euclid's Elements. In future editions, there will be a reference to the Litterae manuscript of this text.

³We have departed from Heath and made extremity here a term.

that which is an extremity of any thing. A *figure* is that which is contained by any boundary or boundaries. A *circle* is a plane figure contained by one line such that all the straight lines falling upon it from one point among those lying within the figure are equal to one another. The point is called the *center* of the circle. A *diameter* of the circle is any straight line drawn through the center and terminated in both directions by the circumference of the circle, and such a straight line also bisects the circle.⁴

⁴We end here. Of course, Euclid goes on to discuss semicircles, rectilinear figures, etc.

