

BARYCENTRIC COORDINATES

Defining result

Proposition 1. If $M = \text{aff}\{b_0, b_1, \dots, b_m\}$ then for each $x \in M$ there exists (λ_i) such that

$$x = \lambda_0 b_0 + \lambda_1 b_1 + \dots + \lambda_m b_m$$

with $\sum_{i} \lambda_{i} = 1$. The (λ_{i}) are unique if the set of vectors is affinely independent.

The *barycentric coordinates* for a vector x in the affine hull of a set of affinely independent vectors is the sequence of unique coefficients expressing the vector as an affine combination of the set of vectors.

