

## **SUBSEQUENCES**

## Why

We want to select particular terms of sequence.

## **Definition**

A *subindex* is a monotonically increasing function from and to the natural numbers. Roughly, it selects some ordered infinite subset of natural numbers. A *subsequence* of a first sequence is any second sequence which is the composition of the first sequence with a subindex.

## Notation

Let  $i : \mathbb{N} \to \mathbb{N}$  such that  $n < m \longrightarrow i(n) < i(m)$ . Then i is a subindex. Let  $b = a \circ i$ . Then b is a subsequence of a. We denote it by  $\{b_{i(n)}\}_n$  and the nth term by  $b_{i(n)}$ .

