Why

We give examples of metric spaces.

Example

Example 1. *Let n be a natural number. Let A be $\mathbf{R}^n$ and define $d : \mathbf{R}^n \times \mathbf{R}^n \to \mathbf{R}$ by*

$$d(a,b) = \sqrt{(a_1 - b_1)^2 + \cdots + (x_n - y_n)^2}.$$

(A,d) is a metric space.

Example 2. *Let A be the unit circle in $\mathbf{R}^2$. So $A = \{x \in R^2 \mid x_1^2 + b^2 = 1\}$. Let $d_1 : A \times A \to \mathbf{R}$ defined by*

$$d(a,b) = \sqrt{(a_1 - b_1)^2 + (a_2 - b_2)^2}.$$

Let $d_2 : A \times A \to \mathbf{R}$ defined as the arc length between the two points. Both (A,d_1) and (A,d_2) are metric spaces.

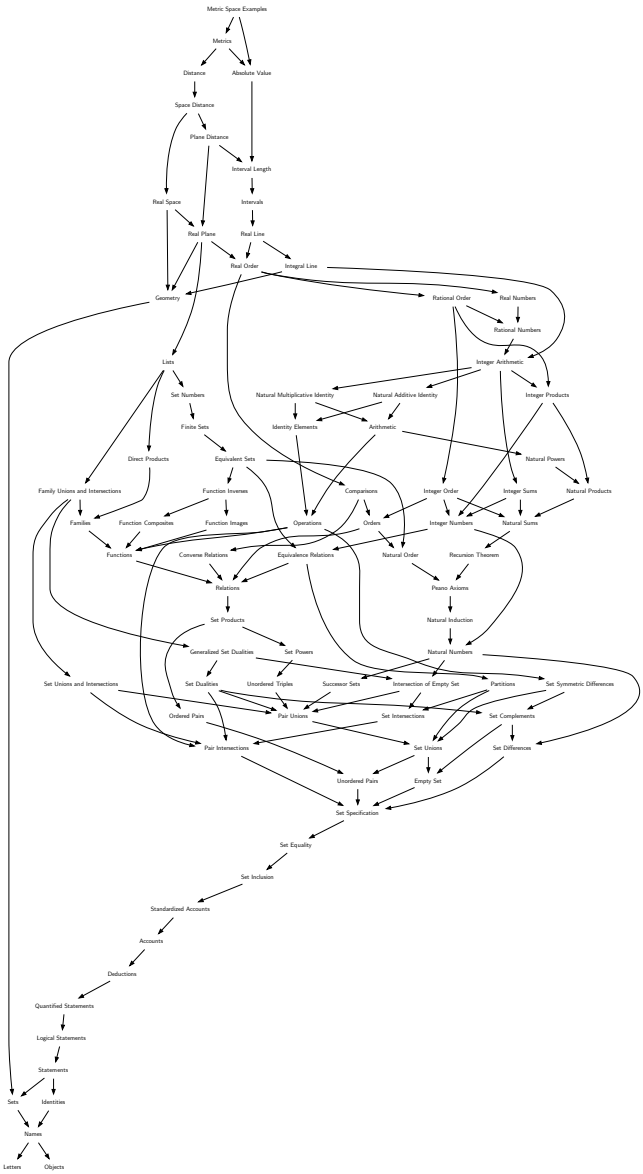
Example 3. *Let $A = C([0,1],\mathbf{R})$. Let $d_1 : A \times A \to \mathbf{R}$ be such that*

$$d_1(a,b) = \max_{x \in [0,1]} |a(x) - b(x)|.$$

Let λ be the outer cover measure. Let $d_2 : A \times A \to R$ be such that

$$d_2(a,b) = \int_{[0,1]} |f - g| d\lambda.$$

Both (A,d_1) and (A,d_2) metric spaces.


Metric Space Examples
Metrics
Distance
Absolute Value
Space Distance
Plane Distance
Interval Length
Real Space
Intervals
Real Plane
Real Line
Real Order
Integral Line
Geometry
Rational Order
Real Numbers
Rational Numbers
Lists
Integer Arithmetic
Set Numbers
Natural Multiplicative Identity
Natural Additive Identity
Integer Products
Finite Sets
Identity Elements
Arithmetic
Direct Products
Equivalent Sets
Natural Powers
Family Unions and Intersections
Function Inverses
Comparisons
Integer Order
Integer Sums
Natural Products
Families
Function Composites
Function Images
Operations
Orders
Integer Numbers
Natural Sums
Functions
Converse Relations
Equivalence Relations
Natural Order
Recursion Theorem
Relations
Peano Axioms
Set Products
Natural Induction
Generalized Set Dualities
Set Powers
Natural Numbers
Set Unions and Intersections
Set Dualities
Unordered Triples
Successor Sets
Intersection of Empty Set
Partitions
Set Symmetric Differences
Ordered Pairs
Pair Unions
Set Intersections
Set Complements
Pair Intersections
Set Unions
Set Differences
Unordered Pairs
Empty Set
Set Specification
Set Equality
Set Inclusion
Standardized Accounts
Accounts
Deductions
Quantified Statements
Logical Statements
Statements
Sets
Identities
Names
Letters
Objects