

MULTIWAY CLASSIFICATION MODELS

Why

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Definition

The two-sample model (or the two-sample problem) has input space $\{1,2\}$ and regression function $\phi: \{1,2\} \to \mathbf{R}^2$ where $\phi(1) = (1,0)^{\top}$ and $\phi(2) = (0,1)^{\top}$. In this case, we model two populations (corresponding to 1 and 2) with different means but a common variance. The regression range is the set $\{(1,0),(0,1)\}$.

Generalizing from two to a populations gives the one-way classification model. In that case the input space is $\{1, \ldots, a\}$ and the regression function is $\phi : \{1, \ldots, a\} \to \mathbf{R}^a$ defined by $\phi(i) = e_i$ where e_i is the standard unit vector in \mathbf{R}^a .² The regression range is $\{e_1, \ldots, e_a\}$. In this case we say that the factor population takes levels $1, \ldots, a$.

If there are more than one factors, then we have a multiway classification model. For example, the two-way classification model with no interaction has input domain $X = \{1, ..., a\} \times \{1, ..., b\}$ and the regression function $\phi: X \to \mathbf{R}^{a+b}$ is defined by $\phi(i,j) = (e_i, e_j)^{\top}$.

¹Future editions will include.

²Future editions will define the standard unit vector.

