



INTEGER RATIONAL HOMOMORPHISM

Why

Do the integer numbers correspond (in the sense *Homomorphisms*) to elements of the rationals.

Main Result

Indeed, roughly speaking the integers correspond to rationals whose denominator is 1. Denote by $\tilde{\mathbf{Q}}$ the set $\{[(a, b)] \in \mathbf{Q} \mid b = 1_{\mathbf{Z}}\}$.

Proposition 1. *The rings $(\tilde{\mathbf{Q}}, +_{\mathbf{Q}} \mid \tilde{\mathbf{Q}}, \cdot_{\mathbf{Q}} \mid \tilde{\mathbf{Q}})$ and $(\mathbf{Z}, +_{\mathbf{Z}}, \cdot_{\mathbf{Z}})$ are homomorphic.¹*

Proof. The function is $f : \mathbf{Z} \rightarrow \mathbf{Q}$ with $f(z) = [(z, 1)]$.² □

¹Indeed, more is true and will be included in future editions. There is an *order perserving* ring homomorphism.

²The full account will appear in future editions.

