



## Results

**Proposition 1.** *Given  $a \in \mathbf{R}$ , define  $f : \mathbf{R} \rightarrow \mathbf{R}$  by*

$$f(x) = a^x \quad \text{for all } x \in \mathbf{R}$$

*Then  $f$  is differentiable and its derivative is the function  $f' : \mathbf{R} \rightarrow \mathbf{R}$  defined by*

$$f'(x) = \ln(a)a^x \quad \text{for all } x \in \mathbf{R}$$

This proposition encompasses the special case  $f(x) = e^x$  then  $f'(x) = e^x$ .



