

# NEURAL NETWORKS

# Why

## Definition

A neural network is a sequence of functions from with several properties. First, the codomain and domain of two subsequence functions in the sequence match. Second, each function is a composition of a function wit We associate a neural network with a predictor which is the composition of the functions in the sequence.

#### Notation

Let  $g^1: \mathbb{R}^d \to \mathbb{R}^k$ ,  $g^2: \mathbb{R}^k \to \mathbb{R}^k$ ,  $g^3: \mathbb{R}^k \to \mathbb{R}^m$ . Then  $(g^1, g^2, g^3)$  is a neural network. Notice that the codomain of  $g^1$  ( $\mathbb{R}^k$ 

### **Activation functions**

An activation function  $h: \mathbf{R} \to \mathbf{R}$  is nonlinear.

