

## EXCHANGEABLE SINGULAR DECOMPOSITION

## Why

Suppose a measure is not exchangeable with another. Then what. We can separate out the troubleome piece; perhaps it can be handled separately.  ${\it TODO}$ 

## Result

**Prop. 1.** Let (X, A) be a measurable space. Let  $\mu$  be a measure on (X, A). Let  $\nu$  be a finite signed measure or complex measure or  $\sigma$ -finite measure on (X, A). There there is a unique decomposition  $\nu = \nu_a + \nu_s$  where  $\nu_a \ll \mu$  and  $\nu_s \perp \mu$ .

The above is also called *Lebesgue's Decomposition Theorem*.

