

REAL LIMITING BOUNDS

Why

We can think of a limit as existing when the limit of upper bounds

and lower bounds on final parts of the sequence coincide.

Definition

The $limit\ superior$ of a sequence of real numbers is the limit of

the sequence of suprema of final parts of the sequence. Similarly,

the $limit\ inferior$ of a sequence of real numbers is the limit of the

sequence of infima of final parts of the sequence.

The limit of the sequence exists if and only if the If the limit

superior and the limit inferior coincide, then the sequence has a

limit which is defined to be the limiting value of each of those two

sequences.

 $\lim \inf_{n} f_n$

 $\liminf_{n} f_n$

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