

Measure Derivatives

1 Why

TODO

2 Definition

2.1 Defining Result

Proposition 1. Let (X, \mathcal{A}) be a measurable space. Let μ, ν be sigma-finite measures with $\nu \ll \mu$. Then there exists $g: X \to [0, \infty)$ such that

$$\nu(A) = \int_A g d\mu$$

for all $A \in \mathcal{A}$.

Proof. TODO \Box

Some call the above the ${\bf Radon\text{-}Nikodym\ theorem}$.

2.2 Notation

TODO