

#### **ALPHABETS**

## Why

We return to our discussion of symbols and scripts, to make precise these concepts in the language of sets and lists.

### Definition

An alphabet is a finite set. For example, let A be the set

$$\{a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z\},\$$

where a denotes the latin lower case letter "a", b denotes the latin lower case letter "b", and so on. In other words, A is the set of lowercase latin letters. It is an alphabet. By analogy with this familiar case, we frequently refer to the elements of an alphabet as "letters" or "symbols."

A word is a list of letters in an alphabet, and a phrase is a list of words. For example, (c, a, t, s) is a word in  $\mathcal{A}$  (mean to correspond to the word "cats") and

$$((c, a, t, s), (a, n, d), (d, o, g, s))$$

is a phrase in  $\mathcal{A}$  (meant to correspond to the phrase "cats and dogs").

# Strings

Let A be an alphabet. In this case (in which A is a finite set), we refer to the finite sequences of A as strings. The string whose length is zero is the empty set.

#### Notation

We denote the set of all finite sequences (strings) in A by  $\mathcal{S}(A)$ . We read  $\mathcal{S}(A)$  aloud as "the strings in A."

