

REAL LINEAR TRANSFORMATIONS

Definition

A real linear transformation is a function $f: \mathbf{R}^n \to \mathbf{R}^m$ satisfying

$$f(\alpha x + \beta y) = \alpha f(x) + \beta f(y)$$
 for all $x, y \in \mathbb{R}^n$ and $\alpha, \beta \in \mathbb{R}$

Equivalently, f is (a) homogenous $f(\alpha x) = \alpha f(x)$ and (b) additive f(x + y) = f(x) + f(y).

