



# Barycentric Coordinates

## 1 Why

TODO

## 2 Defining Result

**Proposition 1.** *If  $M = \mathbf{aff}\{b_0, b_1, \dots, b_m\}$  then for each  $x \in M$  there exists  $(\lambda_i)$  such that*

$$x = \lambda_0 b_0 + \lambda_1 b_1 + \dots + \lambda_m b_m$$

*with  $\sum_i \lambda_i = 1$ . The  $(\lambda_i)$  are unique if the set of vectors is affinely independent.*

The *barycentric coordinates* for a vector  $x$  in the affine hull of a set of affinely independent vectors is the sequence of unique coefficients expressing the vector as an affine combination of the set of vectors.



Barycentric Coordinates



Affinely Independent Vectors



Affine Hulls



Affine Sets



N-Dimensional Space



Real Numbers



Space



Rational Numbers



