



## Normal Conditionals

### 1 Why

What of the conditional densities of a multivariate normal density.

### 2 Result

**Proposition 1.** *Let  $f : \mathbf{R}^d \rightarrow \mathbf{R}$  be a normal density with mean  $\mu \in \mathbf{R}^d$  and covariance  $\Sigma \in \mathbf{S}^d$ .*

$$\mu = \begin{bmatrix} \mu_x \\ \mu_y \end{bmatrix} \quad \text{and} \quad \Sigma = \begin{bmatrix} \Sigma_{xx} & \Sigma_{xy} \\ \Sigma_{yx} & \Sigma_{yy} \end{bmatrix}$$

*The conditional density  $f_{x|y}(\xi, \gamma)$  is is  $\mathcal{N}(\bar{\mu}(\gamma), \bar{\Sigma})$  where*

$$\bar{\mu}(\gamma) = \mu_1 + \Sigma_{xy}\Sigma_{yy}^{-1}(\gamma - \mu_y) \text{ and } \bar{\Sigma} = \Sigma_{xx} - \Sigma_{xy}\Sigma_{yy}^{-1}\Sigma_{yx}.$$