

## INTEGER ARITHMETIC AND ORDER

## Why

How does arithmetic interact with integers.

## Results

**Proposition 1.** Let  $a, b, c, d \in \mathbf{Z}$ . If  $a \leq b$  and  $c \leq d$ , then  $a + b \leq c + d$ .

**Proposition 2.** Let  $a, b, c, d \in \mathbf{Z}$  with  $a, b \geq 0_{\mathbf{Z}}$ . If  $a \leq b$  and  $c \leq d$ , then  $a \cdot c \leq a \cdot d$ .

