

## Real-Valued Random Variable Expectation

## Definition

The expectation (or expected value) of a real-valued random variable defined on a probability space is its integral with respect to the probability measure. The expectation of a random variable is also called its mean.

## Notation

Let  $(X, \mathcal{A}, \mu)$  be a probability space and  $f: X \to \mathbf{R}$  be a random variable. We denote the expectation of f by  $\mathbf{E}f$ , defined:

$$\mathbf{E}f = \int f d\mu.$$

