



## Orthonormal Matrices

### 1 Why

TODO

### 2 Definition

An *orthonormal* matrix is a matrix whose columns are an orthonormal family of vectors.

Some authors call these *orthogonal* matrices or *real orthogonal* or *unitary* matrices.

#### 2.1 Notation

Let  $A \in \mathbf{F}^{m \times n}$ . Something something

$$AA^T = I.$$

### 3 Characterizations

**Proposition 1.** *A matrix is orthonormal if and only if its transpose product with the matrix is the identity.*

**Proposition 2.** *A matrix is orthonormal if and only if its transpose is orthonormal.*

