

# REAL CONVEX HULLS

# Why

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## Definition

The  $convex\ hull$  of a subset of n-dimensional space is the intersection of all convex sets containing the set.

### Notation

We denote the convex hull of  $S \subset \mathbf{R}^n$  by conv S.

## Characterization

**Prop. 1.** Let  $S \subset \mathbb{R}^n$ . conv S is the set of all convex combinations of elements of S.

**Prop. 2.** The convex hull of  $\{b_1, \ldots, b_m\} \subset \mathbb{R}^n$  consists of all vectors

$$\lambda_1 b_1 + \lambda_2 b_2 + \dots + \lambda_m b_m.$$

where  $\lambda_i \geq 0$  and  $\sum_i \lambda_i = 1$ .

<sup>&</sup>lt;sup>1</sup>Future editions will include.

