

REAL STRICTLY CONVEX FUNCTIONS

Why

We want a condition for a unique minimizer.

Definition

Suppose $X \subset \mathbf{R}$ is convex. A function $f: X \to \mathbf{R}$ is *strictly convex* if

$$f(tx + (1-t)y) < tf(x) + (1-t)f(y)$$

for all $t \in [0, 1]$ and $x, y \in X$.

f is strictly concave if -f is convex.

