

Complete Inner Product Decomposition

Prop. 1. Let (V, F) be a complete inner product space. Let M be a closed subspace. then

$$H = M \oplus M^{\perp}$$
.

That is for all $x \in V$, there exists unique $z \in M$ and $q \in M^{\perp}$ such that x = z + w.

