

Subspace Orthogonal Complements

1 Why

2 Main Result

Proposition 1. The orthogonal complement of a subspace is a subspace.

Proposition 2. Let $L \subset \mathbb{R}^n$ be a subspace. Then

$$\dim L + \dim L^{\perp} = n.$$

Proposition 3. Let b_1, \ldots, b_m be a basis for a subspace $L \subset \mathbb{R}^n$. Then $x \perp L$ if and only if $x \perp b_i$ for $i = \{1, 2, \ldots, m\}$.