



# Permutation Matrices

## 1 Why

Permutations of the set  $\{1, 2, \dots, n\}$  correspond to matrices over  $\mathbf{N}$ .

## 2 Definition

The *matrix* corresponding to a permutation of  $\{1, 2, \dots, n\}$  is a matrix of natural numbers whose  $i, j$ th element is 1 if the permutation maps  $i$  to  $j$ ; for  $i, j \in \{1, 2, \dots, n\}$ .

## 3 Notation

Let  $\sigma : \{1, 2, \dots, n\} \rightarrow \{1, 2, \dots, n\}$  be a permutation. Let  $M \in \mathbf{N}^{n \times n}$  be such that  $M_{ij}$  is one if  $\sigma(i) = j$  and 0 otherwise. Then  $M$  is the permutation matrix of  $\sigma$ .





