

TREES

Why

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Definition

An undirected graph is a *tree* if it is connected and acyclic. An undirected graph is a *forest* if it is acyclic. Each connected component of a forest is a tree, motivating the definition.

Properties

Proposition 1. There is a unique path between any two vertices of a tree.

Proof. Such a path exists because the tree is connected. Such a path is unique because the existence of two separate paths would create a cycle. \Box

¹Future editions will include.

