



**Definition**

A real function  $f : \mathbf{R} \rightarrow \mathbf{R}$  is *linear* (a *linear function*) if

$$f(\alpha x + \beta y) = \alpha f(x) + \beta f(y) \quad \text{for all } x, y, \alpha, \beta \in \mathbf{R}$$



