



CONDITIONAL DISTRIBUTIONS

Why

Conditioning defines a new probability mass function on the set of outcomes.

Definition

The conditional probability of any two events defines a new probability mass function over the set of outcomes which is in the second event. The conditional probability of an outcome is the probability of the second event divided into the original probability of the outcome.

Notation

Let p be a probability mass function on the set of outcomes A with the corresponding event probability function \mathbf{P} . Then the conditional probability mass function of C conditioned on B is $q : C \rightarrow \mathbf{R}$, defined so that

$$q(a) = \begin{cases} \frac{p(a)}{\mathbf{P}(B)} & \text{if } a \in B \\ 0 & \text{otherwise .} \end{cases}$$

Definition

Notation

Let R denote the set of real numbers. Let A_1, \dots, A_n be a sequence of non-empty finite sets. Let $A = \prod_{i=1}^n A_i$ Let $p : A \rightarrow R$ be a distribution on A . We denote the conditional

distribution of i on j of p by $p_{i|j} : A_i \times A_j \rightarrow R$ For $i, j = 1, \dots, n$ and $i \neq j$ p_i satisfies

$$p_{i|j}(b, c)p_j(c) = p_{ij}(b, c)$$

for every $b \in A_i$ and $c \in A_j$.

