

#### Inverses of Composite Relations

# Why

How does inverse and converse relations interact.

#### Results

Let R be a relation between X and Y and let S be a relation between Y and Z.

**Proposition 1.**  $(RS)^{-1} = S^{-1}R^{-1}$ 

## **Identity Relations**

Recall that I is the identity relation on X if x I y if and only if x = y.

**Proposition 2.** Let R be a relation on X. Let I be the identity relation on X. Then RI = IR = R,  $RR^{-1} \supset I$ ,  $R^{-1}R \supset I$ .

### **Relation Properties**

**Proposition 3.** R is symmetric if and only if  $R \subset R^{-1}$ 

