

## PLANE DISTANCE

## Why

What is the distance between two points in a plane?

## Definition

We define the distance between two points in the plane as the length of the line segment connecting them.<sup>1</sup> In terms of their coordinates  $(x_1, x_2), (y_1, y_2) \in \mathbb{R}^2$ , the plane distance of two points is

$$\sqrt{(x_1-y_1)^2+(x_2-y_2)^2}$$
.

This is sometimes referred to as the *Euclidean distance*. We have thus defined a function mapping  $\mathbb{R}^2 \times \mathbb{R}^2$  into  $\mathbb{R}$ .

<sup>&</sup>lt;sup>1</sup>This intuition will be expanded in future editions.

