

## Nondeterministic Finite Automata

## Definition

A nondeterministic finite automata  $N = (Q, \Sigma, \delta, q_0, F)$  is a list where Q and  $\Sigma$  are finite sets,  $\delta : Q \times \Sigma \to \mathcal{P}(Q), q_0 \in Q$  and  $F \subset Q$ . A nondeterministic finite automata with empty moves  $N = (Q, \Sigma, \delta, q_0, F)$  is a list where Q and  $\Sigma$  are finite sets,  $\delta : Q \times (\Sigma \cup \{\emptyset\}) \to \mathcal{P}(Q), q_0 \in Q$  and  $F \subset Q$ .

As with finite automata, we call Q the states,  $\Sigma$  the alphabet,  $\delta$  the transition function,  $q_0$  the start state, and F the accept states (or final states). An input  $u \in \mathsf{str}(\Sigma)$  results in a state sequence  $x \in \mathsf{str}(Q)$  with  $x_1 = q_0$  and  $x_{i+1} = \delta(x_i, u_i)$  for  $i = 1, \ldots, |u|$ .

## Main result

For any automata M, there exists a nondeterministic finite automata N such that N accepts the same languages as M.<sup>1</sup> For this reason, a language is regular if and only if some nondeterministic finite automaton accepts it.

<sup>&</sup>lt;sup>1</sup>Future editions will include an account.

