

REAL RATIONAL FUNCTIONS

Why

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Definition

A real rational function (or rational function) is a function $f: \mathbb{R} \to \mathbb{R}$ for which there exists polynomials $a, b \in \mathbb{R}^d$ with corresponding polynomial functions $p: \mathbb{R} \to \mathbb{R}$ and $q: \mathbb{R} \to \mathbb{R}$ so that f(x) = p(x)/q(x) for all $x \in \mathbb{R}$.

In this case we call a the numerator polynomial (and p the numerator function) and b the denominator polynomial (and q the denominator function). Of course, the language rational is in reference to the fact that if p and q are integer-valued functions, then the function f is a rational-valued function (see Rational Numbers).

¹Future editions will include.

