

## INTERVALS

## Why

We name and denote subsets of the set of real numbers which correspond to segments of a line.

## Definition

Take two real numbers, with the first less than the second.

An *interval* is one of four sets:

- 1. the set of real numbers larger than the first number and smaller than the second; we call the interval *open*.
- the set of real numbers larger than or equal to the first number and smaller than or equal to the second number; we call the interval closed.
- 3. the set of real numbers larger than the first number and smaller than or equal to the second; we call the interval open on the left and closed on the right
- 4. the set of real numbers larger than or equal to the first number and smaller than the second; we call the interval *closed on the left* and *open on the right*.

If an interval is neither open nor closed we call it half-open or half-closed

We call the two numbers the *endpoints* of the interval. An open interval does not contain its endpoints. A closed interval contains its endpoints. A half-open/half-closed interval contains only one of its endpoints. We say that the endpoints *delimit* the interval.

## Notation

Let a, b be two real numbers which satisfy the relation a < b.

We denote the open interval from a to b by (a, b). This notation,

although standard, is the same as that for ordered pairs; no confusion arises with adequate context.  $^{1}$ 

We denote the closed interval from a to b by [a,b]. We record the fact  $(a,b) \subset [a,b]$  in our new notation.

We denote the half-open interval from a to b, closed on the right, by (a,b] and the half-open interval from a to b, closed on the left, by [a,b).<sup>2</sup>

The unit interval is the set  $[0_R, 1_R]$  and we sometimes denote it by I.

<sup>&</sup>lt;sup>1</sup>In future editions, we may use (a, b) or even (a, b).

<sup>&</sup>lt;sup>2</sup>Some authors use ]a, b], [a, b[ and ]a, b[.

