

## MULTIWAY CLASSIFICATION MODELS

## Why

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## Definition

The two-sample model (or the two-sample problem) has input space  $\{1,2\}$  and regression function  $\phi:\{1,2\}\to \mathbb{R}^2$  where  $\phi(1)=(1,0)^{\top}$  and  $\phi(2)=(0,1)^{\top}$ . In this case, we model two populations (corresponding to 1 and 2) with different means but a common variance. The regression range is the set  $\{(1,0),(0,1)\}$ .

Generalizing from two to a populations gives the *one-way* classification model. In that case the input space is  $\{1, \ldots, a\}$  and the regression function is  $\phi : \{1, \ldots, a\} \to \mathbb{R}^a$  defined by  $\phi(i) = e_i$  where  $e_i$  is the standard unit vector in  $\mathbb{R}^{a,2}$  The regression range is  $\{e_1, \ldots, e_a\}$ . In this case we say that the factor population takes levels  $1, \ldots, a$ .

If there are more than one factors, then we have a multiway classification model. For example, the two-way classification model with no interaction has input domain  $X = \{1, ..., a\} \times \{1, ..., b\}$  and the regression function  $\phi: X \to \mathbf{R}^{a+b}$  is defined by  $\phi(i, j) = (e_i, e_j)^{\top}$ .

<sup>&</sup>lt;sup>1</sup>Future editions will include.

<sup>&</sup>lt;sup>2</sup>Future editions will define the standard unit vector.

