

FLASH CODE

Why

Can flashlights speak?

Speech can be made to correspond to words. And words are sequences of letters. So, roughly, can we communicate letters with a flashlight? No sounds allowed.

Discussion

Well, what can we do with a flashlight? Turn it on and off. So we can blink light. Here's a thought: One blink means a. Two blinks means b. Three blinks means c. Four blinks means d. And so on.

Here's the rub: how do we know when one letter stops, and another begins. Put another way, does 7 blinks mean (g), or (b,a,d), since 2+1+4=7, or (c,d), since 3+4=7, or (d,c) and so on. If we change the game, maybe we can change the color of the flashlight. Or give a half-flash. Is a half-flash a "quick" flash, or is it a flash in which we have covered up half of the end of the flashlight?

The first question is a clue. The duration of the blink. How about the duration between blinks? A one second pause in between blinks of a particular a letter. A three second pause for blinks in between letters. A five second pause for a space, to indicate a change of a word? Or an additional symbol, a "space", in our alphabet, communicated with 27 (!) blinks?

Definition

Denote a blink by \star . The flash $code^1$ for the alphabet A (the latin lower case letters) is the function $f: A \to \mathsf{str}(\{\star\})$ defined by $f(a) = \star$, $f(b) = \star\star$, $f(c) = \star\star\star$, $f(c) = \star\star\star\star$ and so on. We call f(a) the code word of $a \in A$. It is a sequence of blinks.

The idea is that if we give someone the *code word* f(a) for a letter of our alphabet $a \in A$, they will be able to tell us a. In the language of functions, we want f to have an inverse. Clearly, f is invertible.

It is natural to extend the flash code for A to strings of A. Let \square represent a long pause. Then we encode a sequence $x \in \mathsf{str}(A)$ by applying f to each element of x in turn, and including a \square in between. The flash code for the strings $\mathsf{str}(A)$ is the function $g: \mathsf{str}(A) \to \mathsf{str}(\{\star, \square\})$ defined recursively, as $g(x) = f(x_1)$ if |x| = 1 and $g(x) = f(x_1) \square g(x_{2:n})$ when |x| > 1. For example, we encode the word (string) (b, a, d) as

$$\star \star \Box \star \Box \star \star \star \star \tag{1}$$

Now suppose we are given a sequence as shown in (1). Well, so long as f is invertible, we look can decode the codewords (the blinks, in this case) in between the squares and recover the word.

¹The etymology of code is from the Latin codex, in the legal tradition of a list of statutes. We may well use the term correspondence, or function, but code is standard.

