



## Why

Suppose we are going to make a several measurements. We associate to each element of a finite set a number. If the measurements we make are divided into proportions according to a distribution, if we make all the measurements and then average the results what do we expect to get.<sup>1</sup>

## Definition

Consider a distribution  $p$  and a real-valued function  $f$ . The *distribution expectation* of  $f$  under  $p$  is the sum of the product of the results of  $p$  and  $f$  on the elements of the set.

## Notation

Let  $A$  a finite set. Let  $p : A \rightarrow [0, 1]$  a distribution on a finite set  $A$  and let  $f : A \rightarrow \mathbf{R}$  a function on  $A$ . The expectation of  $f$  under  $p$  is

$$\sum_{a \in A} p(a)f(a).$$

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<sup>1</sup>Future editions will modify.



