### Why

It happens that all circulant matrices have the same eigenvectors.

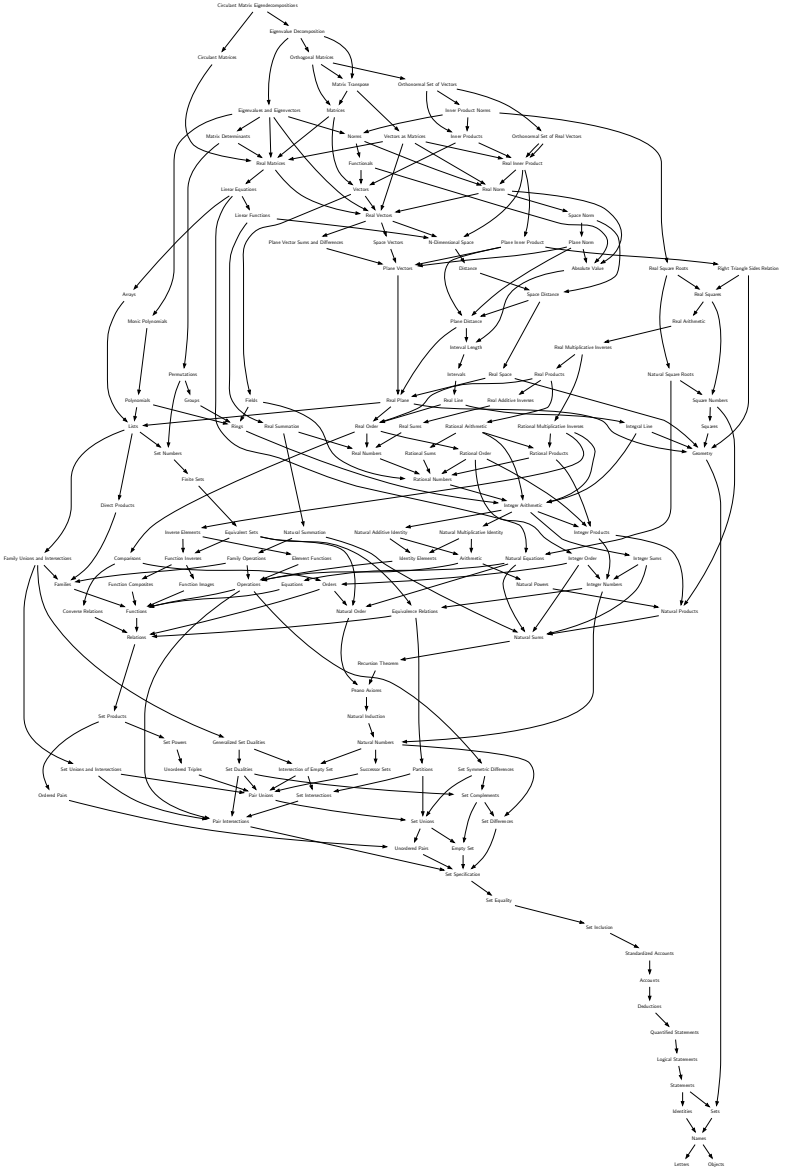
### Definition

Recall that $C$ is circulant then

$$C = c_0 I + c_1 S + c_2 S^2 + \cdots + c_{n-1} S^{n-1}.$$

So $q \in \mathbf{R}^d$ is an eigenvector of $C$ if and only if it is one of $S$.[1]

[1] Future editions will complete this development.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Successor Sets
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Pair Intersections
Set Unions
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Unordered Pairs
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Set Specification
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