

Distribution Approximators

1 Why

We have a distribution to approximate. It is, for some reason, unsuitable to our needs and we want to replace it with one more suitable.

2 Definition

A distribution approximator is an approximator of a probability distribution. It is also a distribution. The criterion of approximation is any similarity function on distributions over the same space.

3 Notation

Let A be a non-empty set and $q: A \to \mathbf{R}$ be a distribution. Let $p: A \to \mathbf{R}$ be a distribution. Then $p: A \to \mathbf{R}$ is a distribution approximator of q.

4 Reasons for approximation

Infeasible to represent. If there are many outcomes, many numbers are required to specify the distribution. If $p: A^n \to \mathbb{R}$ where |A| = k, then there are k^n outcomes; take, for example, k = 2 and n = 100. So we might want to find a distribution which requires fewer numbers to express. In other words, we want a different distribution, selected from the set of those which is easier to express, which is close to the original.

Unreasonable from common sense. The distribution may be unreasonable as a result of our common sense. For example, it may give zero probability to an outcome which we know to be possible, and would like to model with non-zero probability. This may happen when working with an empirical distribution: a particular outcome does not appear in the dataset, however, our common sense suggests is possible. In this case, we want to find a different distribution, selected from the set of those which is more reasonable based on common sense, which is close to the original.

