

## NORMAL CONDITIONALS

## Why

What of the conditional densities of a multivariate normal density.

## Result

**Prop.** 1. Let  $f : \mathbf{R}^d \to \mathbf{R}$  be a normal density with mean  $\mu \in \mathbf{R}^d$  and covariance  $\Sigma \in \mathbf{S}^d$ .

$$\mu = \begin{bmatrix} \mu_x \\ \mu_y \end{bmatrix} \quad and \quad \Sigma = \begin{bmatrix} \Sigma_{xx} \& \Sigma_{xy} \\ \Sigma_{yx} \& \Sigma_{yy} \end{bmatrix}$$

The conditional density  $f_{x|y}(\xi,\gamma)$  is  $\mathcal{N}(\bar{\mu}(\gamma),\bar{\Sigma})$  where

$$\bar{\mu}(\gamma) = \mu_1 + \Sigma_{xy} \Sigma_{yy}^{-1} (\gamma - \mu_y) \text{ and } \bar{\Sigma} = \Sigma_{xx} - \Sigma_{xy} \Sigma_{yy}^{-1} \Sigma_{yx}.$$

