

Isomorphisms

Why

We often have two alebgras for which we can identify elements of the ground set.

Definition

Let $(A, +_A)$ and $(B, +_B)$ be two algebras.¹

An isomorphism between these two algebras is a bijection $f:A\to B$ satisfying:

$$f(a+Aa') = f(a)+Bf(a')$$
 and $f^{-1}(b+Bb') = f^{-1}(b)+Af^{-1}(b')$.

¹Future editions will change this notation to avoid clashes with right and left identity elements (see *Identity Elements*).

