

## Real Integral Limit Inferior Bound

## 1 Why

TODO

## 2 Result

**Proposition 1.** The integral of the limit inferior of a sequence of measurable, nonnegative, extended-real-valued functions is no larger than the limit inferior of the sequence of integrals.

*Proof.* Let  $(X, \mathcal{A}, \mu)$  be a measure space, and let  $f_n : \to [0, \infty]$  a  $\mathcal{A}$ -measurable function for every natural number n. We want to show that if

 $\int \liminf_{n} f_n d\mu \le \liminf_{n} \int f_n d\mu.$ 

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