

CONVEX SETS

Why

We generalize convex sets to arbitrary vector spaces.

Definition

Suppose X is a vector space over \mathbf{R} . A set $C \subset X$ is *convex* if it contains the closed line segment between every pair of distinct points. In other words,

$$\lambda x + (1 - \lambda)y \in C$$
 for all $x, y \in C$ and $\lambda \in [0, 1]$.

