

## INNER PRODUCT NORMS

## Why

An inner product gives rise to a norm naturally.

## **Definition**

PROPOSITION 1. Let  $(V, \mathbf{F})$  be a vector space. Let  $f: V \times V \to \mathbf{F}$  be an inner product such that  $f(x, x) \in \mathbf{R}$ . Let  $g: V \to \mathbf{R}$  such that

$$g(x) = \sqrt{f(x,x)}.$$

Then g is a norm.

The *norm* of a vector in an inner product space is the square root of the inner product of the vector with itself.

## Notation

