

Set-Builder Notation

1 Why

We specify some subset of a known set via a property.

2 Definition

Let A be a nonempty set. We use the notation

$$\{a \in A \mid ---- \}$$

to indicate a subset of A that satisfies some property specified after the |. We read the symbol | aloud as "such that." We read the whole notation aloud as "a in A such that..."

We call the notation **set-builder notation**. Set-builder notation avoids enumerating elements.

3 Example

For example, let L be the set of Latin letters and V the set of Latin vowels. One notation for V is $\{l \in L \mid l \text{ is a vowel}\}$. A second notation for V is $\{a, e, i, o, u\}$. For this set, an English

description will do. This notation is really indispensable for sets which have many members, too many to reasonable write down.