



## Why

We discuss inductors that produce relations consistent with their given datasets.

## Definition

Let  $(x_1, y_1), \dots, (x_n, y_n)$  be a dataset in  $X \times Y$ . Let  $\mathcal{R}$  be the set of all relations on  $X \times Y$ .

A *consistent inductor*  $\{G_n : (X \times Y)^n \rightarrow \mathcal{R}\}_n$  is one for which, for all  $n \in \mathbf{N}$ , for all  $D_n \in (X \times Y)^n$ ,  $D$  is consistent with  $G_n(D_n)$ . In other words, a consistent inductor always produces a relation with which the dataset is consistent.

The interpretation follows. Fix a relation  $R^*$ . And let every dataset “shown” to the algorithm  $G_n$  be constructed by selecting elements from  $R^*$ . In other words, every dataset is a sequence in  $R^*$ . In this case, a dataset  $D_n \in (X \times Y)^n$  is always consistent with  $R^*$  and so a consistent inductor will never “eliminate”  $R^*$ . In other words, the inductor, in order to be consistent “must eliminate” every inconsistent relation.

We may “hope” to give the algorithm a “large and diverse” dataset, so that several of the elements of  $R^*$  are included. In this case, the algorithm can “eliminate” many smaller relations in  $\mathcal{R}$  which did not include records in the dataset.

## Functionally consistent

The rub is that any dataset is consistent with the complete relation  $X \times Y$ . So we can often consider a set  $\mathcal{H} \subset \mathcal{R}$  of relations. It is common to call this a *hypothesis class*, especially for the case in which it consists of functional relations.

