

# Tree Densities

### 1 Why

As with distributions, if a density factors according to a tree rooted at a particular vertex, it factors according to a tree rooted at any vertex. So, as before, the property of factoring according to a rooted tree is really a property of factoring according to a tree.

#### 2 Definition

### 2.1 Defining Result

**Proposition 1.** If a density factors according to a tree rooted at a vertex it factors according to that tree rooted at any vertex.

Proof. TODO

#### 2.2 Undirected Definition

A density factors according to a tree if it factors according to the tree rooted at any vertex.

## 3 Existence and Uniqueness

Trees are not a property of densities, since there is no one-toone correspondence, as demonstrated by the following propositions.

### 3.1 Existence

**Proposition 2.** A density f need not factor according to a tree.

## 3.2 Uniqueness

**Proposition 3.** A density f may factor according to multiple trees.

