



## Why

We consider elements of one set which are not contained in another set.

## Definition

Let  $A$  and  $B$  denote sets. The *difference* between  $A$  and  $B$  is the set  $\{x \in A \mid x \notin B\}$ . In other words, the difference between  $A$  and  $B$  is the set of all points of  $A$  which do not belong to  $B$ .

It is not necessary that  $B \subset A$ ; the difference is called *proper* if  $A \supset B$ . This terminology is from that of **proper subsets**.

## Notation

We denote the difference between  $A$  and  $B$  by  $A - B$ . Some authors use  $-$  or  $\sim$ , but we will avoid this.

## Properties

The following are straightforward.<sup>1</sup>

**Proposition 1.**  $A - \emptyset = A$

**Proposition 2.**  $A - A = \emptyset$

---

<sup>1</sup>Accounts will appear in future editions.



