

## PARAMETERIZED DISTRIBUTIONS

## Why

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## Definition

A parametric distribution family (parametric density family) on X is a family of distributions (densities)  $\{p^{(\theta)}\}_{\theta\in\Theta}$  on X. We call the index set  $\Theta$  (see Families) the parameters.

Similarly, a parametric conditional distribution family (parametric conditional density family) on Z from X is a family  $\{q^{(\theta)}\}_{\theta\in\Theta}$  whose terms  $q^{(\theta)}:Z\times X\to \mathbf{R}$  are such that  $q^{(\theta)}(\cdot,\xi):Z\to\mathbf{R}$  is a distribution (density) for every  $\xi\in X$ .

A conditional distribution  $q:Z\times X\to \mathbb{R}$  is functionally parametrizable if there exists a function  $f:X\to\Theta$  and parameteric distribution family  $\{p^{(\theta)}\}_{\theta\in\Theta}$  on Z satisfying  $q(\cdot,\xi)\equiv p^{(f(\xi))}$ . In this case we call f the parametrization function and we call  $\{p^{(\theta)}\}_{\theta\in\Theta}$  the parameterized family. We call  $\{f,\{p^{(\theta)}\}_{\theta}\}$  a functionally parameterized conditional distribution on Z from X. All conditional distributions  $q:Z\times X\to\mathbb{R}$  are functionally parametrizable, since  $\{q(\cdot,\xi)\}_{\xi\in X}$  with parameters X and identity parameterization satisfies the conditions.

## **Examples**

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<sup>&</sup>lt;sup>1</sup>Future editions will include.

<sup>&</sup>lt;sup>2</sup>Future editions will include.

