

K-Trees

Why

We generalize trees and discuss an example of chordal graphs.¹

Definition

Let $k \in \mathbf{N}$. A k-tree is defined indirectly. Let G = (V, E) be a complete graph and |V| = k.

The complete graph on If A k-tree is an undirected graph with at least k vertices. The only k-tree with k vertices is the complete graph.

Chordality

Prop. 1. All k-trees are chordal.

 ${\it Proof.}$ Induction on k-tree with k vertices.

 $^1\mathrm{Future}$ editions will modify, and may introduce k-trees without chordal graphs.

