

## REAL MULTIPLICATIVE INVERSES

# Why

What is the multiplicative inverse in the reals?

## Result

We can show the following.<sup>1</sup>

**Proposition 1.** The multiplicative inverse of R is, if  $R \neq 0_R$ ,

- 1. if  $0_{\mathbf{Q}} \in \mathbf{R}$ , then  $\{q \in \mathbf{Q} \mid q \le 0_{\mathbf{Q}}\} \cup \{r^{-1}\}\exists s < r, (r \notin \mathbf{R})$
- 2. If  $0_{\mathbf{Q}} \notin \mathbf{R}$ , then the additive inverse of the multiplicative inverse of the additive inverse of R.

#### **Notation**

We denote the multiplicative inverse of  $r \in \mathbb{R}$  by  $r^{-1}$ . We denote  $q \cdot (r^{-1})$  by q/r.

#### **Division**

We call the operation  $(a, b) \mapsto a/b$  real division.

<sup>&</sup>lt;sup>1</sup>The account will appear in future editions.

