

## Powers and Intersections

## Why

How does the power set relate to an intersection?

## **Notation Preliminaries**

First, if we have a set of sets—denote it  $\mathcal{C}$ —and all members are subsets of a fixed set—denote it E—then the set of sets is a subset of  $E^*$ . In this case, we can write

$$\bigcap \{X \in E^* \mid x \in \mathcal{C}\}$$

Which is a sort of justification for the notation

$$\bigcap_{X\in\mathcal{C}}X.$$

## **Basic Properties**

Here are some basic interactions between the powerset and intersections.<sup>1</sup>

Proposition 1.  $A^* \cap F^* = (A \cap F)^*$ 

Proposition 2.  $\bigcap_{X \in \mathcal{A}} A^* = (\bigcap_{X \in \mathcal{A}} A)^*$ 

Proposition 3.  $\bigcap_{X \in E^*} X = \emptyset$ 

<sup>&</sup>lt;sup>1</sup>Future editions will expand on these propositions and provide accounts of them.

