

Undirected Subgraphs

Why

We look at a particular subset of vertices and the edges involved between them.

Definition

The subgraph of an undirected graph (V, E) induced by a subset of vertices $W \subset V$ is the undirected graph with vertices W and all edges between vertices in W.

Notation

Let G = (V, E) be an undirected graph. Let $W \subset V$.

$$F = \{ \{v, w\} \in E \mid v, w \in W \}.$$

The subgraph induced by W is the undirected graph (W, F).

Some authors denote the subgraph induced by W by G(W) or (W, E(W)). We avoid this notation, as it abuses G, which is no longer an ordered pair, but (in our standard function notation) now indicates a function on subsets of V with a complicated codomain. Other authors occasionally refer to the "subgraph W", instead of "the subgraph G(W)". Again, we avoid this practice.

