

ARRAYS

Why

We name lists of lists, and so on.

Definition

Let s be a sequence of natural numbers: $s = (n_1, ..., n_d)$. An array of size (or shape) s is a function whose domain is the set

$$I = \{ (m_1, \dots, m_d) \mid 1 \le m_1 \le n_1, \dots, 1 \le m_d \le n_d \}.$$

We call the set I the set of *indices* of the array. We call the codomain of the function the set of *values* of the array. If A is the set of values, we say that the array is in A. We call the length of s (here denoted d) the dimension of the array.

Case d=1

If the shape of the array has length one, then the array is no different from a sequence. In this case, the terminology for arrays coincides with that for sequences.

Case d=2

If the shape of the array has length two, then the array can is a *table* with n_1 rows and n_2 columns.¹ We say that the array is two-dimensional. We denote the $n_1 \times n_2$ array with elements in the set A by $A^{n_1 \times n_2}$.

Simplified indices

In the case that a is a one-dimensional array, or sequence, we use the common terminology a_i for the ith element of a In the case that a is a two dimensional array, we write a_{ij} for $a_{(i,j)}$.

¹Compare with Matrices.

