

Vector Space Isomorphisms

1 Why

In some sense, \mathbb{R}^n is the only finite-dimensional vector space. In what sense?

2 Definition

An *isomorphism* is an invertible linear transformation between two vector spaces. Two vector spaces are *isomorphic* if there exists and isomorphism between them.

3 Key Result

Proposition 1. Two finite-dimensional vector spaces are isomorphic if and only if they have the same dimension.

Corollary 2. Two finite-dimensional vector spaces are isomorphic if and only if they have the same dimension.

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