

## MONOTONIC FUNCTIONS

## Why

We can generalize the notion of real monotone functions to functions between any two sets with total partial orders.

## **Definition**

Let  $(A, \geq_A)$  and  $(B, \geq_B)$  be two partially ordered sets.  $f: A \to B$  is *isotonic* if it is order preserving and *antitonic* if it is order reversing. A function is *monotonic* if it is either antitonic or isotonic.<sup>1</sup>

## ${\bf Examples}^2$

 $<sup>^{1}\</sup>mathrm{Future}$  editions may modify this terminology.

<sup>&</sup>lt;sup>2</sup>Future editions will include. A nice example is monotonic matrix functions.

