

# Convex Sets

## 1 Why

We speak of sets of real numbers which are like intervals.

### 2 Definition

A **convex combination** of two real numbers is an element of the closed interval they delimit. A **convex set** of real numbers contains each convex combination of any two of its elements.

#### 2.1 Notation

Denote the real numbers by R. Let  $A \subset R$ . If A is convex, then for each  $a, b \in A$ , and  $\theta \in [0, 1]$ ,

$$\theta a + (1 - \theta)b \in A$$
.

## 3 Examples

**Example 1.** The real numbers are a convex set.

Example 2. Real intervals are convex.

**Example 3.** Let a, b be non-equal real numbers. The set  $\{a, b\}$  is not convex.

Example 4. The empty set is convex

**Example 5.** Let a be a real number. The set  $\{a\}$  is convex.

**Example 6.** Let [a,b] and [c,d] be two disjoint real intervals. The set  $[a,b] \cup [c,d]$  is not convex.