

## Unbiased Estimators

## Why

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## Definition

Consider a random variable  $x: \Omega \to \mathbb{R}^n$ . The error of the estimate  $\xi \in \mathbb{R}^n$  is the random variable  $e: \Omega \to \mathbb{R}^n$  which is defined by  $e(\omega) = x(\omega) - \xi$ . The *bias* of an estimate is the expected value of the error. An estimate is *unbiased* if it has zero bias.

Likewise, if we have another random variable  $y: \Omega \to \mathbb{R}^m$ , then the error of the estimator  $f: \mathbb{R}^m \to \mathbb{R}^n$  is the random variable  $e: \Omega \to \mathbb{R}^n$  defined by  $e(\omega) = f(x(\omega)) - y(\omega)$ .

<sup>&</sup>lt;sup>1</sup>Future editions will include an account.

