

Monotonic Functions

Why

We can generalize the notion of real monotone functions to functions between any two sets with total partial orders.

Definition

Let (A, \geq_A) and (B, \geq_B) be two partially ordered sets. $f: A \to B$ is *isotonic* if it is order preserving and *antitonic* if it is order reversing. A function is *monotonic* if it is either antitonic or isotonic.¹

Examples

2

¹Future editions may modify this terminology.

 $^{^2\}mathrm{Future}$ editions will include. A nice example is monotonic matrix functions.

