



Convex Sets

1 Why

2 Definition

The *closed line segment between* two points in n -dimensional space is the set of points which can be expressed as the sum of the first point and a scalar multiple of the difference between the second point and the first; where the scalar is in the interval $[0, 1]$. Thus, the closed line segment between two points is a subset of the line through the two points.

A *convex set* contains every closed line segment between any two points. Every affine set is convex. Thus, convex sets are more general.

2.1 Notation

Let x and y in \mathbf{R}^n is the set

$$\{x + a(y - x) \mid 0 \leq a \leq 1, x, y \in \mathbf{R}^n\}.$$

the *open line segment* between x and y is the closed line segment with the points x and y .

Proposition 1. *Every affine set is convex.*