

TRIANGLE EQUALITY

Why

The squared norm of a sum of orthogonal vectors is the sum of their squared norms.

Result

Prop. 1. Let (V, F) be an inner product space with induced norm $\|\cdot\|$. Let $x, y \in V$ be orthogonal vector. Then

$$||x + y||^2 = ||x||^2 + ||y||^2.$$

