

Normal Mutual Information

1 Why

What is the differential mutual information between two components of a multivariate normal.

2 Result

Proposition 1. Let $g \sim \mathcal{N}(\mu, \Sigma)$. Then the mutual information between component i and component j is

$$-\frac{1}{2}\ln(1-\rho_{ij}^2)$$

where ρ_{ij} is the correlation between components i and j.