

## Countable Probability Distributions

## 1 Why

We want to extend our notion of probability distribution to a set with infinite elements, but only countably many.

## 2 Why

Consider a set A. If A has n elements, then a probability distribution on A is  $p: A \to \mathbf{R}$  where p(a) = 1/n. There is a natural candidate.

What if A is the set of natural numbers  $\mathbb{N}$ . The principle difficulty is that not all sequences of real numbers  $a: \mathbb{N} \to \mathbb{R}$  are summable.

A (countable) probability distribution on  $\mathbb{N}$  is  $p:\mathbb{N}\to\mathbb{R}$  where  $p\geq 0$  and

$$\sum_{n=1}^{\infty} p(n) = 1.$$

