



CONVEX HULLS

Why

Definition

The *convex hull* of a subset of n -dimensional space is the intersection of all convex sets containing the set.

Notation

We denote the convex hull of $S \subset \mathbf{R}^n$ by **conv** S .

Characterization

PROPOSITION 1. Let $S \subset \mathbf{R}^n$. **conv** S is the set of all convex combinations of elements of S .

PROPOSITION 2. The convex hull of $\{b_1, \dots, b_m\} \subset \mathbf{R}^n$ consists of all vectors

$$\lambda_1 b_1 + \lambda_2 b_2 + \dots + \lambda_m b_m.$$

where $\lambda_i \geq 0$ and $\sum_i \lambda_i = 1$.

