

## **Bounded Linear Continuous**

## 1 Why

All continuous functions between norm spaces are bounded linear functions.

## 2 Result

**Proposition 1.** Let  $((V_1, F), |\cdot|_1)$  and Let  $((V_2, F), |\cdot|_2)$  be two norm spaces. Let  $f: V_1 \to V_2$  be a linear function between two norm spaces. Then

- 1.  $\exists x \in V_1 \text{ such that } f \text{ is continuous at } x$ ,
- 2. f is continuous,
- $3. \ f$  is uniformly continuous, and
- 4. f is bounded,

are all equivalent conditions.