

OUTCOME VARIABLE MOMENTS

Definition

Let $x:\Omega\to \mathbb{R}$ a random variable and $p:\Omega\to \mathbb{R}$ a distribution. The mean square of x is $\mathsf{E}(x^2)$. Define $\mu=\mathsf{E}(x)$. We can express $\mathsf{E}(x^2)=\mathsf{E}(x)^2+\mathsf{cov}(x)$ since

$$\begin{aligned} \mathbf{cov}(x) &= \mathbf{E}((x-\mu)^2) = \mathbf{E}(x^2 - 2\mu x + \mu^2) \\ &= \mathbf{E}(x^2) - 2\mu \mathbf{E}(x) + \mu^2 \\ &= \mathbf{E}(x^2) - \mu^2 \end{aligned}$$

The *n'th moment* of x is $\mathbf{E}(x^n)$. The mean is the first moment. The covariance is the second moment minus the square of the first moment.

