



Multivariate Normals

1 Why

We generalize the Gaussian to d -dimensional space.

2 Definition

Let $f : \mathbf{R}^d \rightarrow \mathbf{R}$ be a density. If there exists $\mu \in \mathbf{R}^d$ and $\Sigma \in \mathbf{S}^d$ with $\Sigma \succ 0$ such that for all $x \in \mathbf{R}^d$

$$f(x) = \frac{1}{\sqrt{(2\pi)^d \det \Sigma}} \exp \left(-\frac{1}{2} (x - \mu)^\top \Sigma^{-1} (x - \mu) \right)$$

then f is a *(multivariate) gaussian density*.

2.1 Notation