



Motivating result

Proposition 1. *Suppose $T : V \rightarrow W$ is linear and T^{-1} exists. Then T^{-1} is linear.*

Proof. We show that T^{-1} is additive and homogenous. Let $w_1, w_2 \in W$ and define v_1 and v_2 so that

$$v_1 = T^{-1}(w_1) \quad \text{and} \quad v_2 = T^{-1}(w_2)$$

In other words,

$$Tv_1 = w_1 \quad \text{and} \quad Tv_2 = w_2$$

and so by the linearity of T ,

□

Recall that we can use the terminology *the* inverse because inverses are unique (if they exist; see **Function Inverses**).

Definition

A linear map $T \in \mathcal{L}(V, W)$ is *invertible* if there is a linear map $S \in \mathcal{L}(W, V)$ so that ST

