

Tree Normals

1 Why

We name multivariate normal densities which factor according to a tree. These densities require tabulating fewer numbers.

2 Definition

A tree multivariate normal or tree normal density is a multivariate normal density which factors according to a tree.

2.1 Fewer numbers

A multivariate normal on \mathbb{R}^n requires tabulating n numbers for the mean and n(n+1)/2 numbers for the covariance matrix. If it factors according to a tree, we need only n numbers to specify the covariance (one for the one-variable marginal, and n-1 for the covariance of the two-variable conditionals).