

## **VECTOR SPACE DIMENSIONS**

## Why

The number of vectors in any basis is the same.

## **Defining Result**

A vector space is *finite-dimensional* if it has a finite basis; otherwise it is it is *infinite-dimensional*.

**Prop.** 1. Every basis of a finitely spanned vector space has the same number of elements.

The dimension of a finite-dimensional vector space is the number of distinct vectors in any basis. If a vector space is finite-dimensional and every basis has n distinct elements we call it a n-dimensional vector space.

