Why

We represent rectangles by functions.

Definition

The *characteristic function* of a A of a set X is a function from X to 2 which is 1 if the argument is in A and 0 otherwise.

If the base set is the real numbers and the subset is an interval, then the characteristic function is a rectangle with height one and the width of the interval.

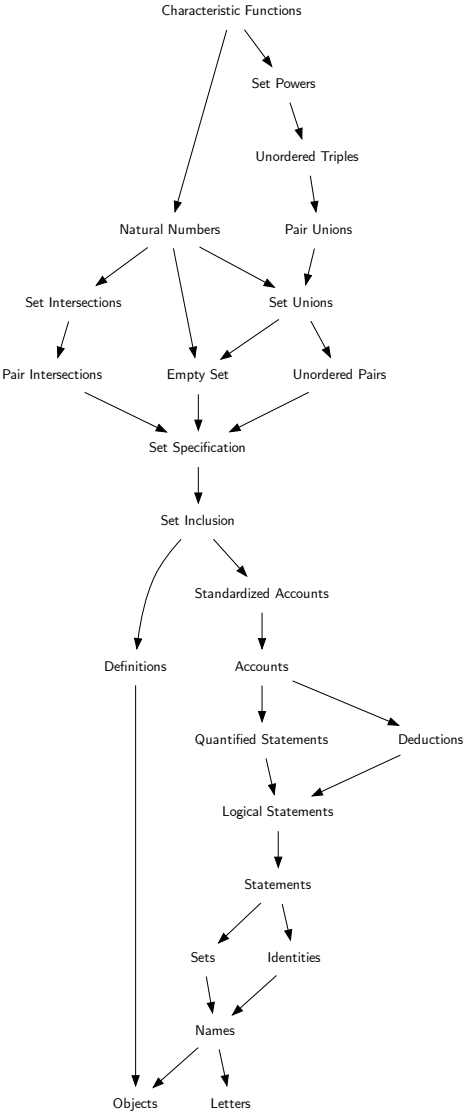
The function which assigns to each subset A of X to characteristic function of A is a one-to-one function from X^* onto 2^X.

Notation

Let A be a non-empty set and $B \subset A$. We denote the characteristic function of B in A by $\chi_B : A \to R$. The Greek letter χ is a mnemonic for "characteristic".

The subscript indicates the set on which the function is one. In other words, for all $B \subset A$, $\chi_B^{-1}(\{1\}) = B$.

If B is an interval and α is a real number then $\alpha\chi_B$ is a rectangle with height α.


Characteristic Functions
Set Powers
Unordered Triples
Natural Numbers
Pair Unions
Set Intersections
Set Unions
Pair Intersections
Empty Set
Unordered Pairs
Set Specification
Set Inclusion
Standardized Accounts
Definitions
Accounts
Quantified Statements
Deductions
Logical Statements
Statements
Sets
Identities
Names
Objects
Letters