



Why

We want to model physical phenomena.

Definition

A *differential equation* is an equation relating functions and their derivatives.

Basic Example

For example, let $f : \mathbf{R} \rightarrow \mathbf{R}$ be differentiable everywhere and denote the derivative of f by $f' : \mathbf{R} \rightarrow \mathbf{R}$. Suppose that there exists $\alpha \in \mathbf{R}$ so that for all $x \in \mathbf{R}$,

$$f'(x) = \alpha f(x).$$

Solutions

The *solution* of a differential equation is a function (or functions) which satisfy the equation.¹

¹Future editions will expand.

