

## INTEGER RATIONAL HOMOMORPHISM

## Why

Do the integer numbers correspond (in the sense of Homomorphisms) to elements of the rationals.

## Main Result

Indeed, roughly speaking the integers correspond to rationals whose denominator is 1. Define

$$\tilde{Q} := \{ [(a,b)] \in \mathbf{Q} \mid b = 1_{\mathbf{Z}} \}.$$

**Proposition 1.** The rings  $(\tilde{\mathbf{Q}}, +_{\mathbf{Q}} \mid \tilde{\mathbf{Q}}, \cdot_{\mathbf{Q}} \mid \tilde{\mathbf{Q}})$  and  $(Z, +_{\mathbf{Z}}, \cdot_{\mathbf{Z}})$  are homomorphic.<sup>1</sup>

*Proof.* The function is 
$$f: \mathbf{Z} \to \mathbf{Q}$$
 with  $f(z) = [(z,1)]^2$ 

<sup>&</sup>lt;sup>1</sup>Indeed, more is true and will be included in future editions. There is an *order* perserving ring homomorphism.

<sup>&</sup>lt;sup>2</sup>The full account will appear in future editions.

