



## Why

A probability event function is a measure on the set of outcomes.

## Definition

A *probability measure* is a finite measure on a measurable space which assigns the value one to the base set. A finite measure can always be scaled to a probability measure, so these measures are standard examples of finite measures.

A *probability space* is a measure space whose measure is a probability measure. The word “space” is natural, since the notion of a measure generalized the notion of volume in real space (see **Real Space** and **N-Dimensional Space**). The *outcomes* of a probability space are the elements of the base set. The *set of outcomes* is the base set. The *events* are the elements of the sigma algebra. The measure in a probability space corresponds to the event probability function.

## Notation

Let  $(A, \mathcal{A})$  be a measurable space.<sup>1</sup> We denote the sigma-algebra by  $\mathcal{A}$ , as usual. We denote a probability measure by  $\mathbf{P}$ , a mnemonic for “probability,” and intended to remind of the event probability function. Thus, we often say “Let  $(A, \mathcal{A}, \mathbf{P})$ ”

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<sup>1</sup>Often, other authors will denote the set of outcomes (here denoted by  $A$ ) by  $\Omega$ , a mnemonic for “outcomes.”

be a probability space.”

### **Properties**

