

REAL INTEGRAL HOMOGENEITY

Why

If we scale an integrable function is the resulting function integrable? If so, what is its integral?

Result

Proposition 1. Suppose $f : \mathbb{R} \to \mathbb{R}$ is integrable. Then for any $\lambda \in \mathbb{R}$, the function λf is integrable and

$$\int \lambda f = \lambda \int f$$

