

## CONVEX SETS

## Why

We generalize convex sets to arbitrary vector spaces.

## **Definition**

Suppose X is a vector space over  $\mathbf{R}$ . A set  $C \subset X$  is *convex* if it contains the closed line segment between every pair of distinct points. In other words,

$$\lambda x + (1 - \lambda)y \in C$$
 for all  $x, y \in C$  and  $\lambda \in [0, 1]$ .

