



FAMILIES

Why

Sometimes a function's range is more important than the function itself.

Definition

Let I and X denote sets. A *family* is a function $x : I \rightarrow X$. We call an element of I an *index*, I the *index set*, the range of x the *indexed set*, and the value of x at an index i a *term*.

Experience shows that it is useful to discuss sets using indices, especially when discussing a set of sets.

Notation

Let A and I be non-empty sets. We use I as a mnemonic for “index” set. Let $a : I \rightarrow A^*$ be a family. For $i \in I$, we follow the function notation and denote the result of applying a to i by a_i .

We denote the range of the family by family of a_α indexed with I by $\{a_\alpha\}_{\alpha \in I}$, which is short-hand for set-builder notation. We read this notation “a sub-alpha, alpha in I.”

