

MEROMORPHIC FUNCTIONS

Why

The entire functions "extend" the polynomial functions. For polynomial in \mathbf{C} , we can extend the class to the (complex) rational functions in \mathbf{C} . Can we similarly extend the class entire functions?¹

Definition

A meromorphic function (or fractional function) is a function $f: \mathbf{C} \to \mathbf{C}$ for which there exists entire functions $g: \mathbf{C} \to \mathbf{C}$ and $h: \mathbf{C} \to \mathbf{C}$ so that

$$f(z) = \frac{g(z)}{h(z)}$$

for all $z \in \mathbb{C}^2$.

¹Future editions may modify.

²Future editions will continue the development.

