

Matrix Similarity

1 Why

TODO

2 Definition

A first square matrix is *similar* to a second square matrix if there exists a nonsingular matrix such that the first matrix is identical to the product of the inverse of the nonsingular matrix the second square matrix and the nonsingular matrix.

2.1 Notation

Let $A,B\in \mathbf{R}^{n\times n}.$ B is similar to A if there exists a nonsingular matrix $S\in \mathbf{R}^{n\times n}$ such that

$$B = S^{-1}AS.$$

3 Equivalence Relation

Proposition 1. Similarity is an equivalence relation.