



**Definition**

Given a ring  $(R, +, \cdot)$  with additive group  $(R, +)$ . A subset  $I \subset R$  is called a *left ideal* if

1.  $(I, +)$  is a subgroup of  $(R, +)$
2.  $r \cdot x \in I$  for every  $r \in R$  and  $x \in I$

Similarly, it is called a *right ideal* if (2) is replaced with  $x \cdot r \in I$  for every  $r \in R$  and  $x \in I$ . If  $I$  is an *ideal* if it is both a left and right ideal.



