

## **POLYHEDRA**

## Why

We generalize real polyhedra to aribtrary inner product spaces.

## Definition

Suppose X is a vector space with an inner product  $\langle \cdot, \cdot \rangle$  over  $\mathbf{R}$ . A set  $P \subset X$  is a polyhedron (called a polyhedral set) if there exists  $c_1, \ldots, c_m \in X$  and  $\alpha_1, \ldots, \alpha_m \in \mathbf{R}$  so that

$$P = \{x \in X \mid \langle x, c_i \rangle \le \alpha_i \text{ for } i = 1, \dots, m\}$$

In other words, if the set can be described by finitely many inequalities.

As before, a polyhedron is a *polytope* if it is bounded.

