

## PROJECTIONS ON SUBSPACES

## Why

Given a vector  $x \in \mathbf{R}^n$  and a subspace  $S \subset \mathbf{R}^n$ , what is the closest point in S to x.

## Result

**Proposition 1.** Suppose  $U \in \mathbb{R}^{n \times k}$  with  $U^{\top}U = I$ . Then

$$\operatorname{proj}_U(x) = UU^{\top}x$$

