

## JOINT DISTRIBUTIONS

## Why

Suppose we flip a coin n times. How should we define a probability distribution on  $\{0,1\}^n$ . Suppose instead we flip n different coins, each once. How now?

## Discussion

If we model the outcome that coin i lands heads as 1 and that it lands tails by 0, then we are asking to treat of uncertain outcomes from the set  $\{0,1\}^n$  of length-2 sequences.

Here  $x \in \{0,1\}^n$  could correspond to the outcome of flipping one coin n times or the outcome of flipping n different coins. This is a simple example of a frequent and obvious phenomenon in mathematics wherein the same mathematical model (here the outcome set) can be used to model different situations in the real world (c.f. numbers, etc.).

## Definition

Consider a distribution over a product of n sets, where the product is indexed by the first n natural numbers. We call the distribution a *joint distribution* with n components.

