

SEQUENTIAL DECISIONS

Why

We want to discuss making several decisions at different stages.

Definition

Let A be a set of actions and O a set of outcomes. Let $\{A'_{o,a}\}$ be a family of action sets, $\{O'_{o,a}\}$ be a family of outcome sets and $\{\leq_{o,a}\}$ be a family of preferences indexed by $O \times A$.

We call the sequence $(A, O, \{A'_{s,a}\}, \{O'_{s,a}\}, \{\leq_{s,a}\})$ a twostage decision problem. The intuition is that we will select an action $a \in A$ prior to observing an outcome $o \in O$. We will then face the simple decision problem $(A'_{s,a}, O'_{s,a}, \leq_{s,a})$.

A *preference* for the two stage decision problem is a total order on the set

$$\{(a, o, a', o') \mid a \in A, o \in O, a' \in A'_{a,o}, o' \in O'_{a,o}\}.$$

A two-stage decision problem is a sequence (A, O, A, O, A,

