

## LINEAR FUNCTIONS

## Why

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## **Definition**

A function  $f: \mathbb{R}^n \to \mathbb{R}$  is linear if

1. 
$$f(x+y) = f(x) + f(y)$$
 for all  $x, y \in \mathbb{R}^n$  and

2. 
$$f(\alpha x) = \alpha f(x)$$
 for all  $x \in \mathbb{R}^n$  and  $\alpha \in \mathbb{R}$ .

There are simple consequences to these conditions. For example, f(0) = 0.

<sup>&</sup>lt;sup>1</sup>Future editions will include.

