



## SETS

### Why

We want to talk about none, one, or several objects considered as an abstract whole.

### Definition

A *set* is an abstract object. We think of it as several objects considered as a whole. The central primitive notion is that of *belonging*. A set *contains* the objects so considered. These objects are the *members* or *elements* of the set. They belong to the set.

The objects a set contains may be other sets. In other words, an element of a set may be another set. This may be subtle at first glance, but becomes familiar with experience.

We call a set which contains no objects *empty*. Otherwise we call a set *nonempty*.

### Notation

We tend to denote sets by upper case Latin letters: for example,  $A$ ,  $B$ , and  $C$ . To aid our memory, we tend to use the lower case form of the letter for an element of the set. For example, let  $A$  and  $B$  be nonempty sets. We tend to denote by  $a$  an element of  $A$ . And similarly, we tend to denote by  $b$  an element of  $B$ .

We denote that an object  $a$  is an element of a set  $A$  by

$a \in A$ . We read the notation  $a \in A$  aloud as “a in A.” The symbol  $\in$  is a stylized lower case Greek letter  $\varepsilon$ . Since  $\varepsilon$  is read aloud “ehp-sih-lawn,”  $\in$  is a mnemonic for “element of”. We denote that an object  $a$  is not an element of the set  $A$  by  $a \notin A$ . We read this notation aloud as “a not in A.”

Sets



Objects