



# Real Limiting Bounds

## 1 Why

We can think of a limit as existing when the limit of upper bounds and lower bounds on final parts of the sequence coincide.

## 2 Definition

The *limit superior* of a sequence of real numbers is the limit of the sequence of suprema of final parts of the sequence. Similarly, the *limit inferior* of a sequence of real numbers is the limit of the sequence of infima of final parts of the sequence.

The limit of the sequence exists if and only if the If the limit superior and the limit inferior coincide, then the sequence has a limit which is defined to be the limiting value of each of those two sequences.

$$\liminf_n f_n$$

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