



Equations

1 Why

If we know the result of two operations

2 Definition

An **equation** is a formula with an equality.

A **set** is a collection of objects. We use the term **object** in the usual sense of the English language. So a set is itself an object, but of the peculiar nature that it contains other objects. In thinking of a set, then, we regularly consider the objects it contains. We call the objects contained in a set the **members** or **elements** of the set. So we say that an object contained in a set is a **member of** or an **element of** the set.

2.1 Notation

We denote sets by upper case latin letters: for example, A , B , and C . We denote elements of sets by lower case latin letters: for example, a , b , and c . We denote that an object A is an element of a set A by $a \in A$. We read the notation $a \in A$ aloud as “a in A.” The \in is a stylized ϵ , which possesses the mnemonic for element. We write $a \notin A$, read aloud as “a not in A,” if a is not an element of A .

If we can write down the elements of A , we do so using a brace notation. For example, if the set A is such that it contains only the elements a, b, c , we denote A by $\{a, b, c\}$. If the elements of a set are well-known we introduce the set in English and name it; often we select the name mnemonically. For example, let L be the set of latin letters.

If the elements of a set are such that they satisfy some common condition, we use the braces and include the condition. For example, if V is the set of vowels we denote V by $\{l \in L \mid l \text{ is a vowel}\}$. The \mid is read aloud as “such that,” the notation reads aloud as “ l in L such that l is a vowel.” We call the notation $\{l \in L \mid l \text{ is a vowel}\}$ **set-builder notation**. Set-builder notation is indispensable for sets defined implicitly by some condition. Here we could have alternatively denoted V by $\{“a”, “e”, “i”, “o”, “u”\}$. We prefer the former, slightly more concise notation.

3 Two Sets

If every element of a first set is also an element of second set, we say that the first set is a **subset** of or is **contained in** the second set. Conversely, we say that the second set is a **superset** of or **contains** the first set. If a first set is a subset of a second set and the second set is a subset of the first set, we say the two sets are **equal**

We call the set of subsets of a set A the **powerset** of A . We call the set which has no members the **empty set**. The empty set is contained in every other set.

3.1 Notation

Let A and B be sets. We denote that A is a subset of B by $A \subset B$. We read the notation $A \subset B$ aloud as “ A subset B ”. We denote that A is equal to B by $A = B$. We read the notation $A = B$ aloud as “ A equals B ”. We denote the empty set by \emptyset , read aloud as “empty.” We denote the power set of A by 2^A , read aloud as “two to the A .”