



Why

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Definition

An ordered graph is *filled* or *monotone transitive* if all higher neighborhoods induce complete subgraphs.

Notation

Let $G_\sigma = (V, E, \sigma)$ be an ordered graph. G_σ is filled if

$$u, v \in \text{adj}^+(v) \longrightarrow \{u, v\} \in E.$$

In other word, if $i < j < k$ so that $\{\sigma(i), \sigma(j)\} \in E$ and $\{\sigma(i), \sigma(k)\} \in E$ then $\{\sigma(j), \sigma(k)\} \in E$.

Chordality

PROPOSITION 1. *If (V, E, σ) is a filled graph, then (V, E) is chordal.*

Proof. Take the vertex with the lowest index on a cycle of length greater than three. Take □

¹Future editions will expand. For example, this sheet is needed for perfect elimination orderings.

