



# Function Images

## 1 Why

We consider the set of results of a set of domain elements.

## 2 Definition

The *image* of a set of domain elements under a function is the set of their results. Though the set of domain elements may include several distinct elements, the image may still be a singleton, since the function may map all of elements to the same result.

The *range* of a function is the image of its domain. The range includes all possible results of the function. If the range does not include some element of the codomain, then the function maps no domain elements to that codomain element.

### 2.1 Notation

Let  $f : A \rightarrow B$ . We denote the image of  $C \subset A$  by  $f(C)$ , read aloud as “f of C.” This notation is overloaded: for every  $c \in C$ ,  $f(c) \in B$ , whereas  $f(C) \subset B$ . Read aloud, the two are indistinguishable, so we must be careful to specify whether we mean an element  $c$  or a set  $C$ . Following this notation for function images, we denote the range of  $f$  by  $f(A)$ .