

INTEGER SUMS

Why

We want sums to follow those of natural numbers.¹

Definition

Consider $[(a,b)], [(c,d)] \in \mathbf{Z}$. We define the *integer sum* of [(a,b)] with [(c,d)] as $[(a+c,b+d)].^2$

Notation

We denote the sum of [(a,b)] and [(c,d)] by [(a,b)]+[(b,c)] So if $x,y\in \mathbf{Z}$ then the sum of x and y is x+y.

¹Future editions will modify this.

 $^{^2}$ One needs to show that this is well-defined. The account will appear in future editions.

