Why

How does the power set relate to an intersection?

Notation Preliminaries

First, if we have a set of sets—denote it $\mathcal{C}$—and all members are subsets of a fixed set—denote it E—then the set of sets is a subset of E^*. In this case, we can write

$$\bigcap\{X \in E^* \mid x \in \mathcal{C}\}$$

Which is a sort of justification for the notation

$$\bigcap_{X \in \mathcal{C}} X.$$

Basic Properties

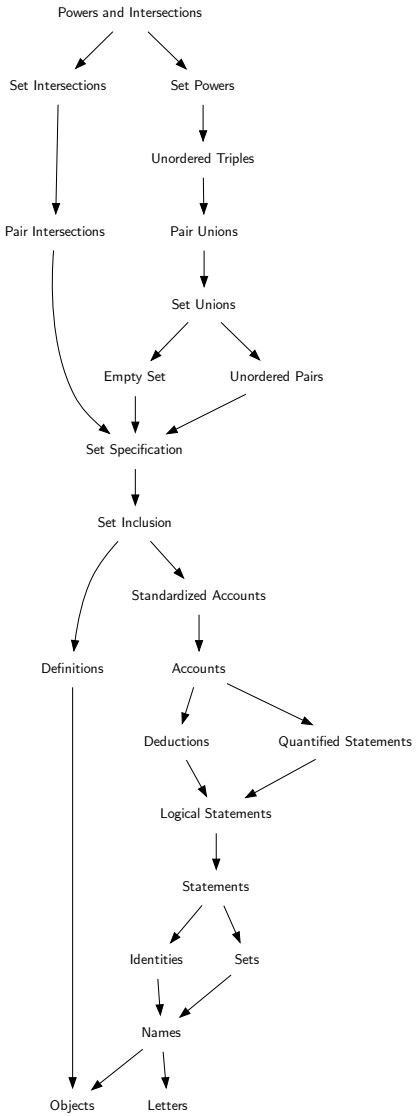
Here are some basic interactions between the powerset and intersections.[1]

Proposition 1. $A^* \cap F^* = (A \cap F)^*$

Proposition 2. $\bigcap_{X \in \mathcal{A}} A^* = \left(\bigcap_{X \in \mathcal{A}} A\right)^*$

Proposition 3. $\bigcap_{X \in E^*} X = \varnothing$

[1] Future editions will expand on these propositions and provide accounts of them.


Powers and Intersections
Set Intersections
Set Powers
Unordered Triples
Pair Intersections
Pair Unions
Set Unions
Empty Set
Unordered Pairs
Set Specification
Set Inclusion
Standardized Accounts
Definitions
Accounts
Deductions
Quantified Statements
Logical Statements
Statements
Identities
Sets
Names
Objects
Letters