

SET NUMBERS AND ARITHMETIC

Why

How does the number of elements change with unions, and products.

Results

There are a few nice relations.¹ Recall from Finite Sets that the union and product of finite sets is finite. Also, the power of a finite set is finite.

Proposition 1. Let A and B be finite sets with $A \cap B = \emptyset$. Then $|A \cup B| = |A| + |B|$.

Proposition 2. Let A and B be a finite sets Then $|A \times B| = |A| \cdot |B|$.

Proposition 3. Let A and B be a finite sets Then $|A^B| = |A|^{|B|}$.

Proposition 4. Let A be a finite set. Then $|\mathcal{P}(A)| = 2^{|A|}$.

¹Proofs will appear in future editions.

