

### MATRIX-MATRIX PRODUCTS

## Why

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#### Definition

Let  $A \in \mathbb{R}^{l \times m}$  and  $B \in \mathbb{R}^{m \times n}$ . In this case we call A and B conformable. The matrix-matrix product of A and B is the matrix  $C \in \mathbb{R}^{l \times n}$  whose ith row  $c_i$  (for i = 1, ..., n) is defind  $c_i = Ab_i$  where  $b_i$  is the ith row of B.

#### **Notation**

We denote the matrix product of A and B by AB.

# **Properties**

Future editions will contain accounts of the following basic properties.

**Proposition 1.** Matrix multiplication is associative.

**Proposition 2.** Matrix multiplication is not commutative.

Indeed, the matrix-matrix produce of B and A may not even be defined, if B and A are not conformable.

<sup>&</sup>lt;sup>1</sup>Future editions will include.

