

Family Set Operations

1 Why

Family set operations are common. TODO: this works for infinite stuff too

2 Definition

We define the set whose elements are the objects which are contained in at least one family member the *family union*. We define the set whose elements are the objects which are contained in all of the family members the *family intersection*.

2.1 Notation

We denote the family union by $\bigcup_{\alpha \in I} A_{\alpha}$. We read this notation as "union over alpha in I of A sub-alpha." We denote family intersection by $\bigcap_{\alpha \in I} A_{\alpha}$. We read this notation as "intersection over alpha in I of A sub-alpha."

2.2 Results

Proposition 1. For an indexed family $\{A_{\alpha}\}_{{\alpha}\in I}$ in S, if $I=\{i,j\}$ then

$$\bigcup_{\alpha \in I} A_{\alpha} = A_i \cup A_i$$

and

$$\cap_{\alpha \in I} A_{\alpha} = A_i \cap A_j.$$

Proposition 2. For an indexed family $\{A_{\alpha}\}_{{\alpha}\in I}$ in S, if $I=\emptyset$, then

$$\bigcup_{\alpha \in I} A_{\alpha} = \emptyset$$

and

$$\cap_{\alpha \in I} A_{\alpha} = S.$$

Proposition 3. For an indexed family $\{A_{\alpha}\}_{{\alpha}\in I}$ in S.

$$C_S(\cup_{\alpha\in I}A_\alpha)=\cap_{\alpha\in I}C_S(A_\alpha)$$

and

$$C_S(\cap_{\alpha\in I}A_\alpha) = \bigcup_{\alpha\in I}C_S(A_\alpha).$$