



Random Variables Joint Law

1 Why

We name the image measure of a collection of real-valued random variables.

2 Definition

The *joint law* of an ordered finite family of n real-valued random variables is the image measure of the tuple-valued function whose components are the individual random variables.

2.1 Notation

Let R denote the set of real numbers and let R^n denote set of n -tuples of real numbers. Let f_1, \dots, f_n be random variables defined on a probability space (X, \mathcal{A}, μ) . Define $f : X \rightarrow R^n$ by $(f(x))_i = f_i(x)$. The joint law is the image measure of f .

We denote the joint law of $\{f_i\}$ by $\mu_{f_1, \dots, f_n} : \mathcal{A} \rightarrow [0, \infty]$. We defined it by

$$\mu_{f_1, \dots, f_n}(A) = \mu(\{x \in X \mid f(x) \in A\}).$$

for all A in the topological sigma algebra on R^n .