



Functions

1 Why

We want a notion for a correspondence between two sets.

2 Definition

A **functional** relation on two sets relates each element of the first set with a unique element of the second set. A **function** is a functional relation.

The **domain** of the function is the first set and **codomain** of the function is the second set. The function **maps** elements **from** the domain **to** the codomain. We call the codomain element associated with the domain element the **result of applying** the function to the domain element.

2.1 Notation

Let A and B be sets. If A is the domain and B the codomain, we denote the set of functions from A to B by $A \rightarrow B$, read aloud as “A to B”.

We denote functions by lower case latin letters, especially f , g , and h . The letter f is a mnemonic for function; g and h follow f in the Latin alphabet. We denote that $f \in A \rightarrow B$ by $f : A \rightarrow B$, read aloud as “f from A to B”.

Let $f : A \rightarrow B$. For each element $a \in A$, we denote the result of applying f to a by $f(a)$, read aloud “f of a.” We sometimes drop the parentheses, and write the result as f_a , read aloud as “f sub a.” The set $\{(a, f(a)) \in A \times B \mid a \in A\}$ of ordered pairs is the **graph** of f .

Let $g : A \times B \rightarrow C$. We often write $g(a, b)$ or g_{ab} instead of $g((a, b))$. We read $g(a, b)$ aloud as “g of a and b”. We read g_{ab} aloud as “g sub a b.”