

## RECTANGULAR FUNCTIONS

## Why

We represent rectangles by functions.

## Definition

A rectangular function corresponds to a characteristic function of an interval. It represents a rectangle whose width is the interval and whose height is one.

## Notation

Let A be a non-empty set and  $B \subset A$ . Recall that we denote the characteristic function of B by  $\chi_B$ .

Now suppose that  $A \subset \mathbb{R}$ . If we embed  $\{0,1\} = 2 \in \mathbb{N}$  in  $\mathbb{R}$  by associating 0 to  $0_{\mathbb{R}}$  and 1 to  $1_{\mathbb{R}}$  then every characteristic function is identified with a function from  $\mathbb{R}$  to  $\mathbb{R}$ .

In particular, notice that if B is an interval and  $\alpha$  is a real number then  $\alpha \chi_B$  is a rectangle with height  $\alpha$ .

