

Integer Powers

Why

1

Definition

Let $a \in \mathbf{Z}$ and let $p \in \mathbf{N}$. Define the first power of a to be a. Define the second power of a to be a^2 . Define the pth power of a for $p \geq 2$ to be $a^p = aa^{p-1}$.

Negative Powers

Let $a \in \mathbf{Z}$ and let $p \in \mathbf{Z}$ with p < 0. Then define a^p to be $1/a^{-p}$. Since p is negative, -p is positive and so we have defined a^{-p} .

Zero

Define $a^0 = 1$.

¹Future editions will include. This sheet include only a very basic outline of a few definitions.

