

## Positive Definite Matrices

# Why

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### **Definition**

Let  $A \in \mathbb{R}^{n \times n}$  be symmetric. A is positive definite if, for all  $x \in \mathbb{R}^d$ ,  $x \neq 0$ ,  $x^{\top}Ax > 0$ . A is positive semidefinite (or nonnegative definite) if, for all  $x \in \mathbb{R}^d$ ,  $x^{\top}Ax \geq 0$ .

#### **Notation**

We denote the set of real-valued positive definite d by d matrices by  $\mathbf{S}_{++}^d$ . We denote the set of real-valued positive semidefinite d by d matrices by  $\mathbf{S}_{+}^d$ .

### Characterizations

**Proposition 1.** Let  $A \in \mathbf{S}^d$  and denote the smallest

<sup>&</sup>lt;sup>1</sup>Future editions will elaborate.

