

PRIME NUMBERS

Definition

A number $n \in \mathbb{N}$ larger than $1 \ n > 1$ is *composite* if there exists numbers $m, k \in \mathbb{N}$ (not necessarily distinct), both smaller than n, m, k < n, with $n = m \cdot k$. A number which is not composite is called *prime*.

Examples

The first few primes. Since the only number smaller than 2 is 1 and $2 \neq 1 \cdot 1$, 2 is the first and smallest prime. Likewise, $3 \neq 1 \cdot 2$, $3 \neq 1 \cdot 1$, $3 \neq 2 \cdot 2$. So 3 is the second smallest prime.

The first composite. Now consider 4. Since $4 = 2 \cdot 2$ and $2 \le 4$, 4 is the smallest composite number.

