

Convex Multivariate Functions

Why

We generalize convex functions to \mathbf{R}^n .

Definition

Let A be a convex subset of \mathbb{R}^n . The function $f:A\to\mathbb{R}$ is *convex* if for any $a,b\in A$ and $t\in[0,1]$,

$$f(ta + (1-t)b) \le tf(a) + (1-t)f(b).$$

It is concave if -f is convex.

