



Why

We consider knapsack problems in which there is more than one knapsack.

Definition

Given $p : \{1, \dots, n\} \rightarrow \mathbf{R}$, $w : \{1, \dots, n\} \rightarrow \mathbf{R}$ and $c \in \mathbf{R}_+^n$, find $x : \{0, \dots, m\} \times \{0, \dots, n\} \rightarrow \{0, 1\}$ to

$$\begin{aligned} & \text{maximize} && \sum_{i=1}^m \sum_{j=1}^n p_j x_{ij} \\ & \text{subject to} && \sum_{j=1}^n w_j x_{ij} \leq c_i, \quad i = 1, \dots, m \\ & && \sum_{j=1}^n x_{ij} \leq 1, \quad i = 1, \dots, n \\ & && x_{ij} \in \{0, 1\} \quad i = 1, \dots, m, j = 1, \dots, n \end{aligned}$$

Here x_{ij} is one if and only if item j is assigned to knapsack i . The above is called the *multiple knapsack problem* (or *0-1 multiple knapsack problem*).

