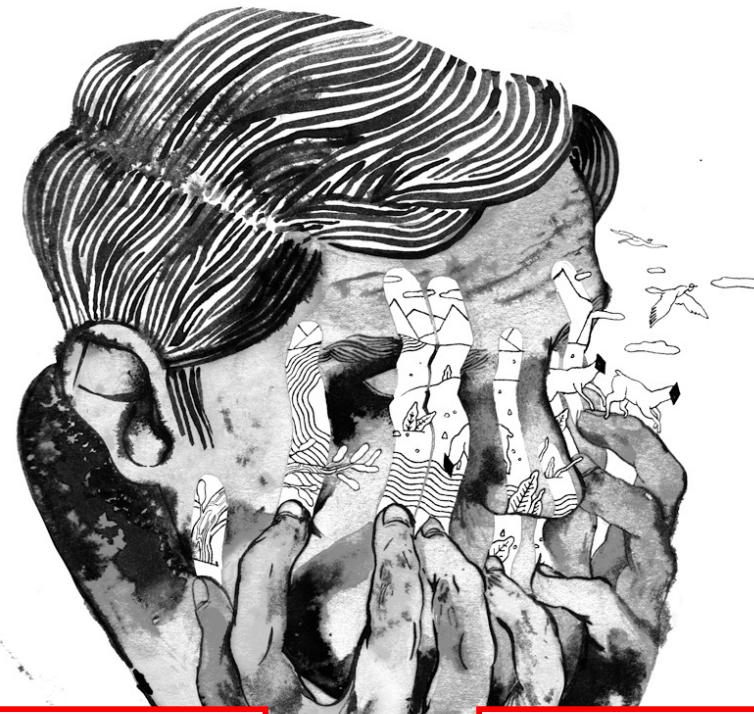


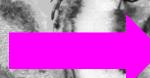
Majorana ν 's hidden in $0\nu2\beta$ decays

Zhi-zhong Xing

xingzz@ihep.ac.cn



$$(Z, A) \rightarrow (Z + 2, A) + 2e^-$$



$$(Z, A) \rightarrow (Z + 2, A) + 2\nu_e$$

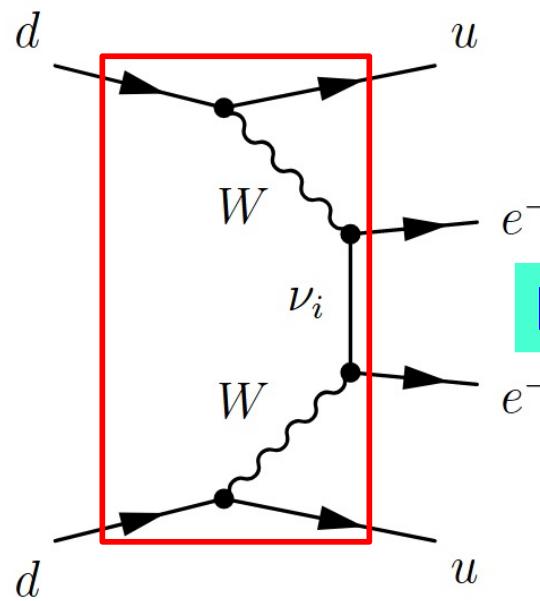
[https://margheritamorotti.com/
ettore-majorana](https://margheritamorotti.com/ettore-majorana)

无中微子衰变研讨会，中山大学珠海校区，2021.5.19—23

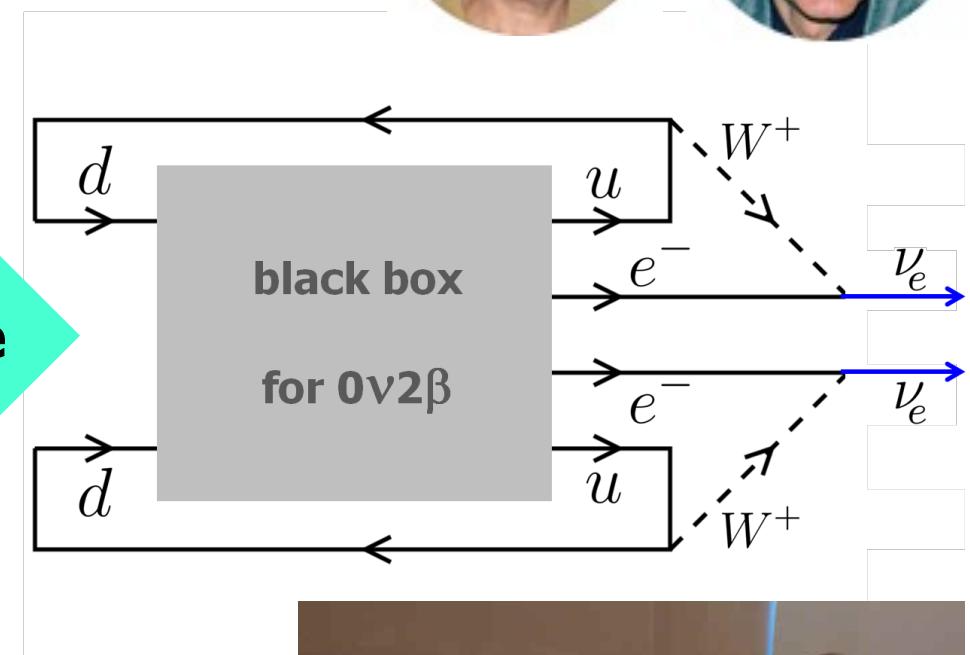
Two theorems

★ Joseph Schechter and Jose Valle suggested a theorem in June 1982: if a $0\nu2\beta$ decay happens, there must be an effective Majorana mass term.

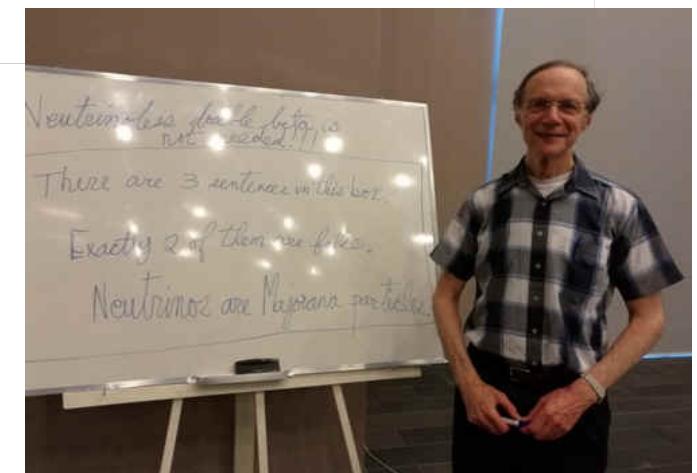
The reverse is also true.



hidden ν's emerge

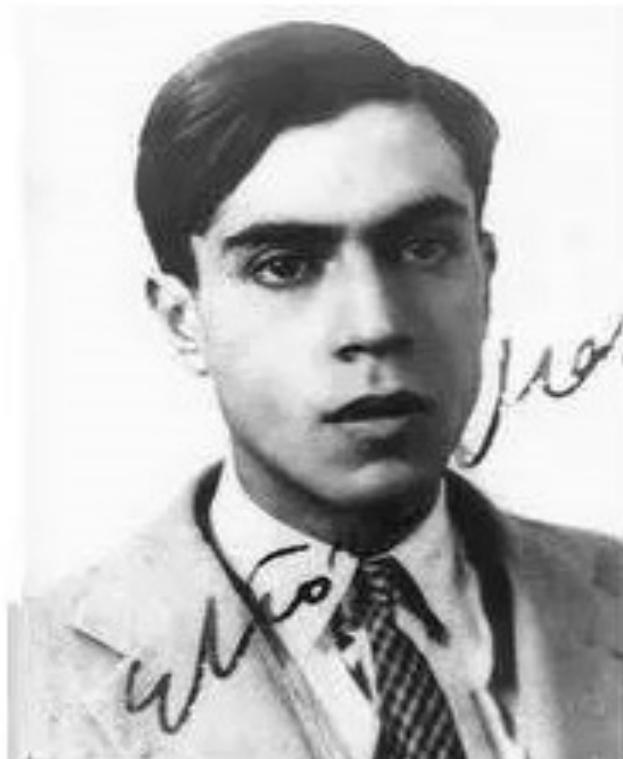


★ The Majorana-Dirac confusion theorem by Boris Kayser in October 1982: If there're no right-handed currents and the ν-masses are very small compared with the experimental energy scale, then it is impossible to tell the difference between Dirac and Majorana ν's.



OUTLINE

- A brief history: ideas and facts oscillated
- Salient properties of Majorana neutrinos



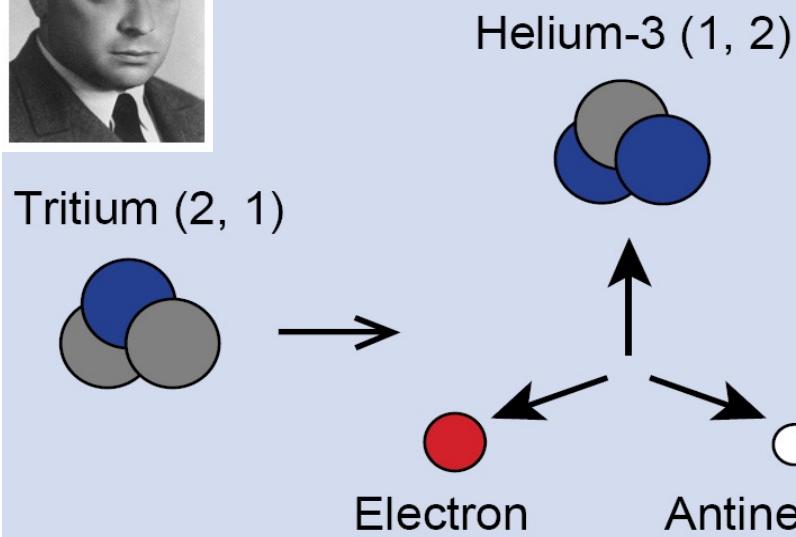
Pabina, 26 marzo 1938 - 1939
Caro Corradi,
Spero che tu non avrai troppo
tempo per leggermi e la lettera. Io sono un po' affaticato
e ritengo dovermi all'albergo Bologna, viaggiando per
una qualsiasi strada possibile. Ho poi intenzione di rimanere
all'incontro. Non mi piacerebbe per me ragionare
sull'argomento perché il caso è difficile. Come è ben detto
qualcuno per ulteriori dettagli.
Aff. E. Majorana.

Pauli (1930) and Fermi (1933)

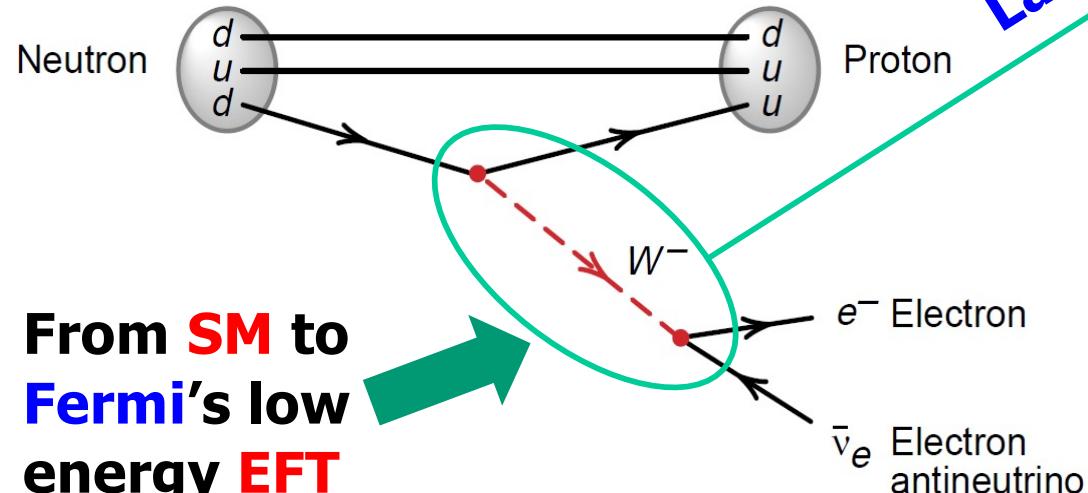
3



Three-Body Final State



$$(N, Z) \rightarrow (N-1, Z+1) + e^- + \bar{\nu}_e .$$

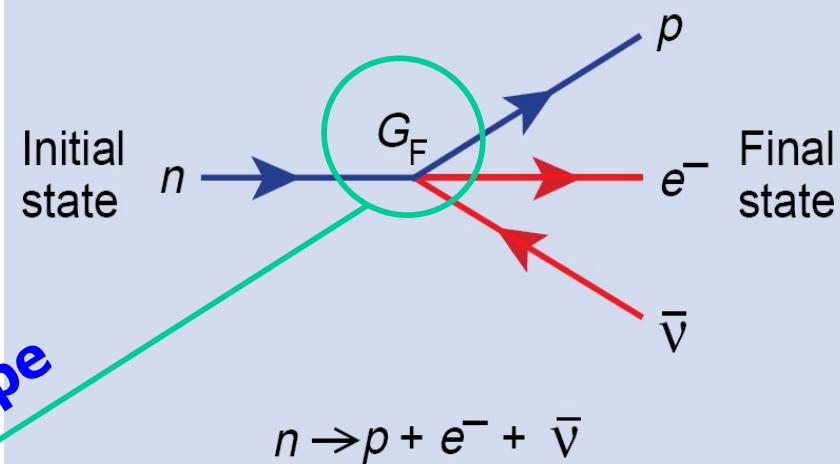


**From SM to
Fermi's low
energy EFT**



I will be remembered for this paper

Neutron Beta Decay



The seesaw-like relation:

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2}$$

$$\rightarrow g \simeq 0.65$$

$$M_W \simeq 80.4 \text{ GeV}$$

$$G_F \simeq 1.166 \times 10^{-5} \text{ GeV}^{-2}$$

Goeppert-Mayer (1935)

4

★ $2\nu 2\beta$ decay: some **even-even** nuclei have an opportunity to decay to the 2nd nearest neighbor via **2** simultaneous β decays (equivalent to the β decays of two neutrons).

$$(Z, A) \rightarrow (Z + 2, A) + 2e^- + 2\bar{\nu}_e.$$

Maria Goeppert-Mayer

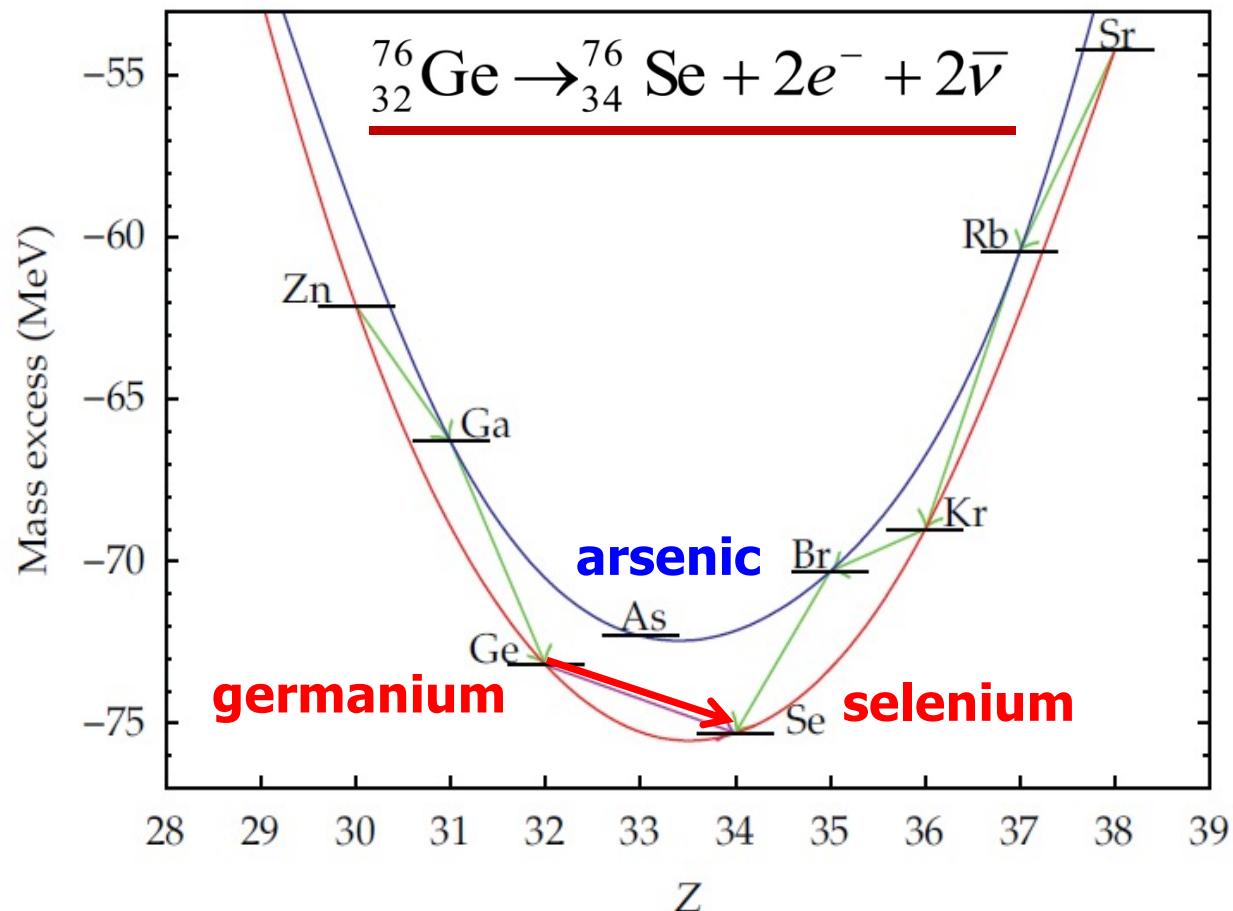
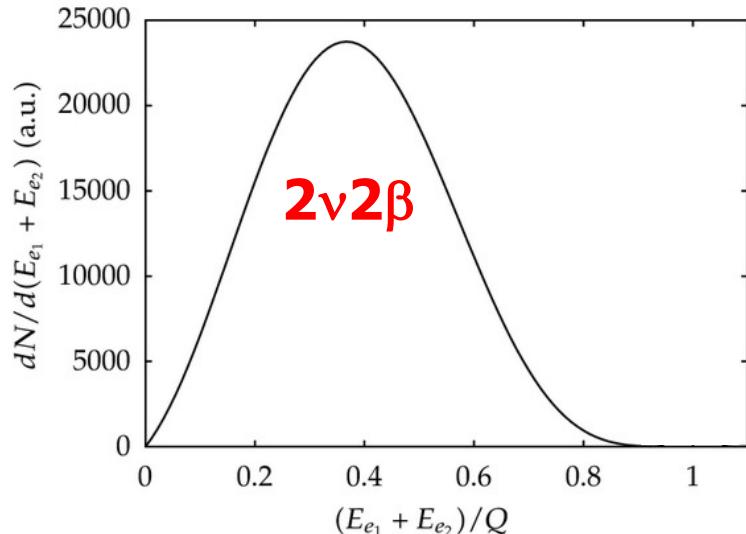


necessary conditions:

$$m(Z, A) > m(Z + 2, A)$$

$$m(Z, A) < m(Z + 1, A)$$

Electron energy spectrum



Majorana (1937)

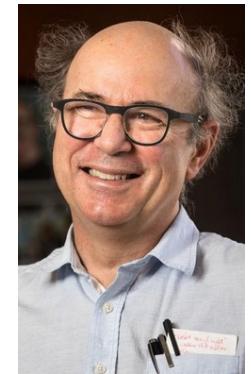
5

★ Ettore Majorana: theory of the symmetry of electrons and positrons
— an idea as mysterious as Majorana's personality.

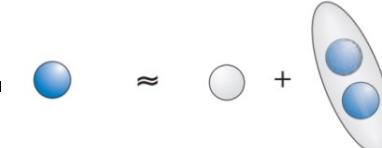
“...there is now no need to assume the existence of antineutron or antineutrinos. The latter particles are indeed introduced in the theory of positive beta-ray emission; the theory, however, can be obviously modified so that the beta-emission, both positive and negative, is always accompanied by the emission of a neutrino.”

Our judgement today:

- No, antineutron ≠ neutron (100%)
- Ja, antineutrinos = neutrinos (99%?)



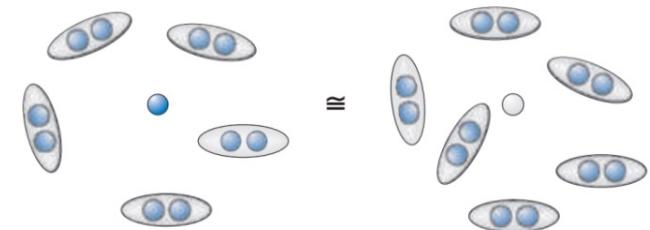
★ Majorana fermions are a new form of matter.



★ Majorana neutrinos are truly *New Physics* beyond SM, and have profound implications for the Universe.

“Majorana returns”
— Frank Wilczek
Nature Physics 2009

Majorana zero mode

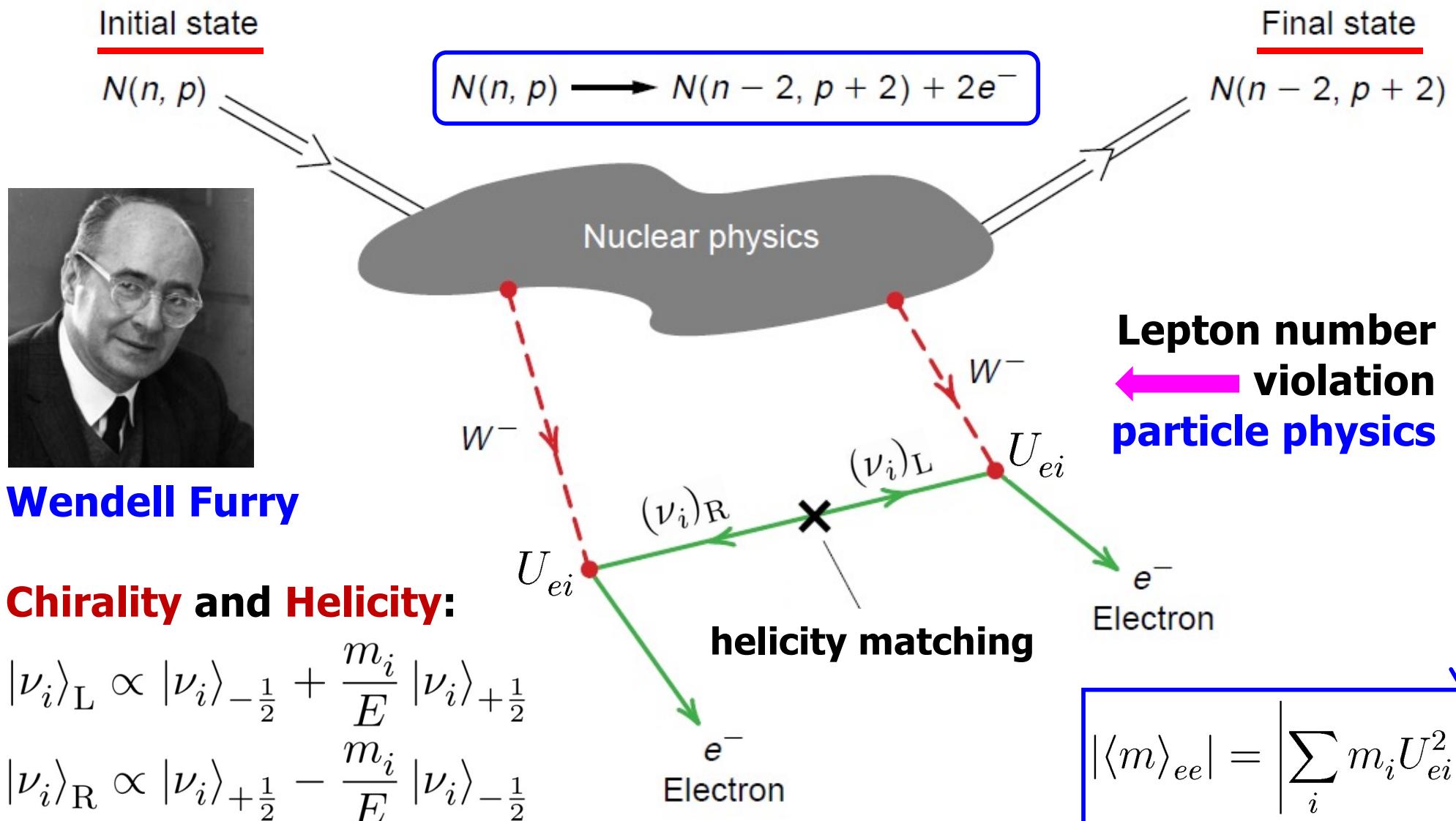


Furry (1939)

6

★ A $0\nu2\beta$ decay may occur if massive ν 's have the Majorana nature, as first pointed out by Furry in 1939.

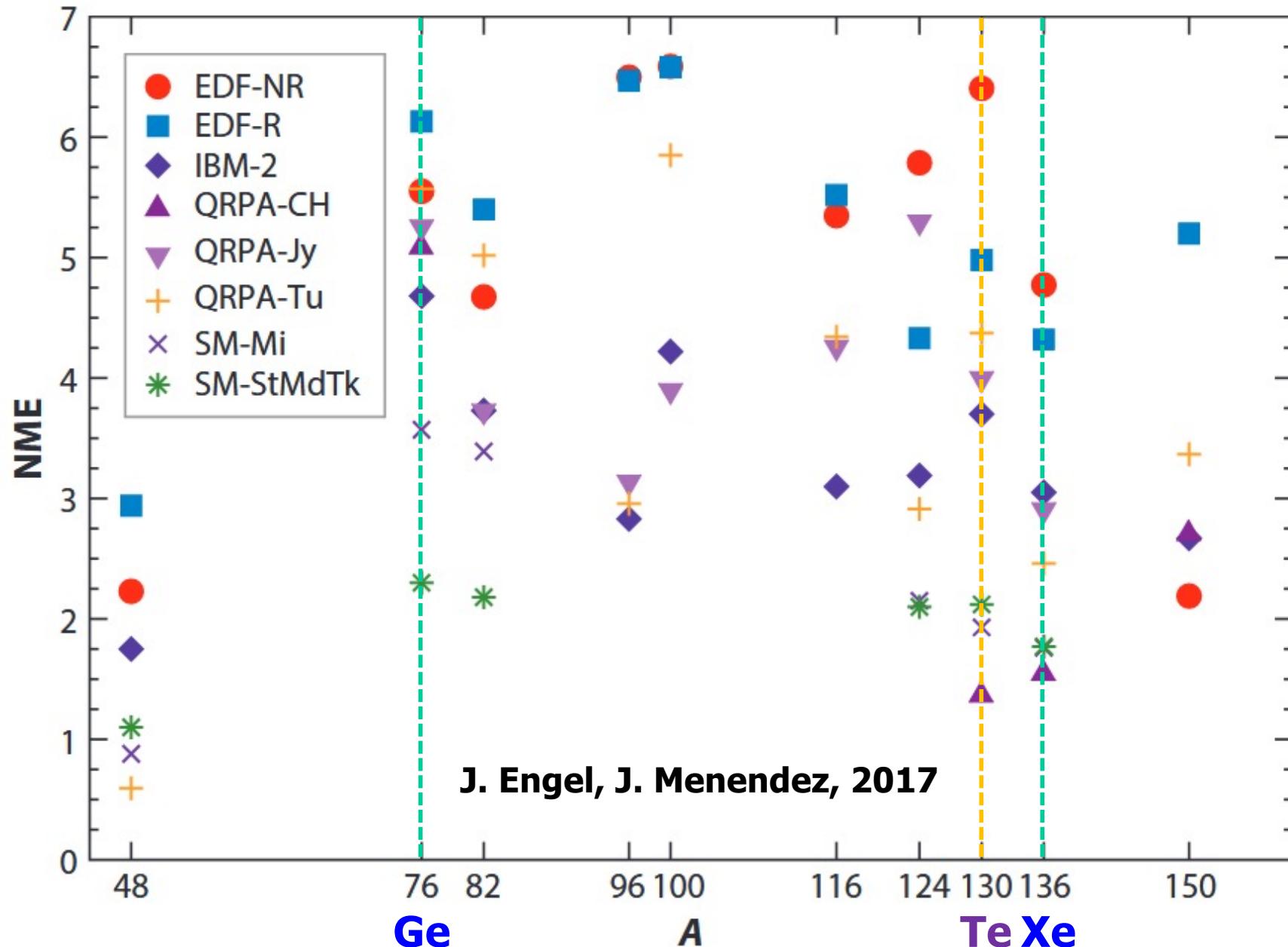
$$T_{1/2}^{0\nu} = (G^{0\nu})^{-1} |M^{0\nu}|^{-2} |\langle m \rangle_{ee}|^{-2}$$



Nuclear matrix elements

7

★ Big uncertainties associated with nuclear matrix elements (NMEs):



Half-life lower limits

8

★ Current experimental constraints on the half-life of the $0\nu2\beta$ decay.

$$T_{1/2}^{0\nu} = (G |\mathcal{M}|^2 \langle m_{\beta\beta} \rangle)^{-1} \simeq 10^{27-28} \left(\frac{0.01 \text{ eV}}{\langle m_{\beta\beta} \rangle} \right)^2 \text{ years}$$

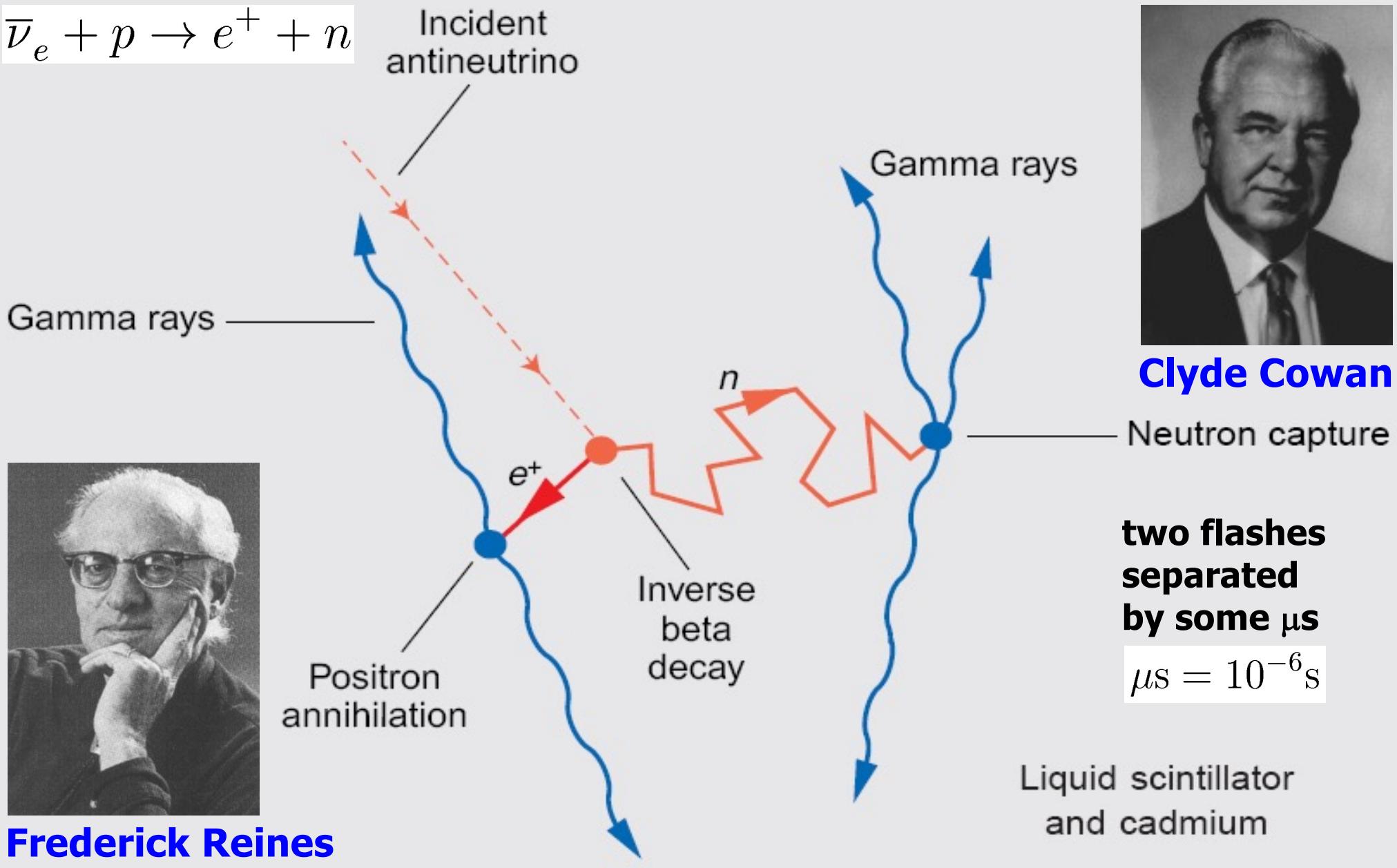
Isotope	$T_{1/2}^{0\nu} (\times 10^{25} \text{ years})$	$\langle m_{\beta\beta} \rangle (\text{eV})$	Experiment	Reference
^{48}Ca	$>5.8 \times 10^{-3}$	$<3.5\text{--}22$	ELEGANT-IV	159
^{76}Ge	>8.0 ★	$<0.12\text{--}0.26$	GERDA	160
GERDA 2020	$T_{1/2} > 1.8 \times 10^{26} \text{ yr at 90\% C.L.}$		MAJORANA DEMONSTRATOR	161
^{82}Se	$>3.6 \times 10^{-2}$	$<0.89\text{--}2.43$	NEMO-3	162
^{96}Zr	$>9.2 \times 10^{-4}$	$<7.2\text{--}19.5$	NEMO-3	163
^{100}Mo	$>1.1 \times 10^{-1}$	$<0.33\text{--}0.62$	NEMO-3	164
^{116}Cd	$>2.2 \times 10^{-2}$	$<1.0\text{--}1.7$	Aurora	165
^{128}Te	$>1.1 \times 10^{-2}$	NE	C. Arnaboldi et al.	166
^{130}Te	>1.5	$<0.11\text{--}0.52$	CUORE	126
^{136}Xe	>10.7 ★	$<0.061\text{--}0.165$	KamLAND-Zen	167
	>1.8	$<0.15\text{--}0.40$	EXO-200	168
^{150}Nd	$>2.0 \times 10^{-3}$	$<1.6\text{--}5.3$	NEMO-3	169

Reines and Cowan (1956)

9

★ The 1st good news: electron antineutrinos were discovered in 1956.

$$\bar{\nu}_e + p \rightarrow e^+ + n$$

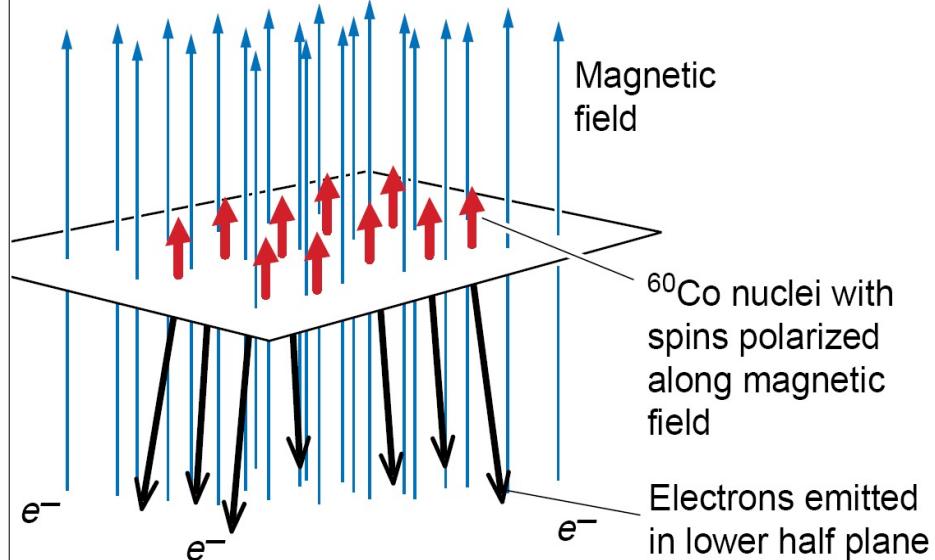


Wu, Lee and Yang (1957)

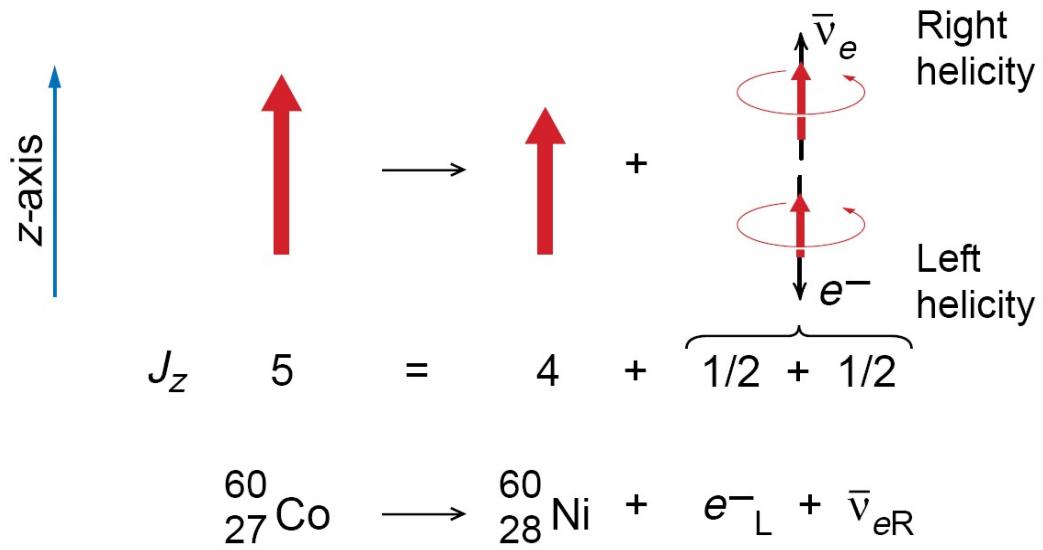
10

★ The 1st bad news: neutrinos seemed to have no mass (left-handed). Chien-shiung Wu *et al*/ aligned the spins of Cobalt-60 nuclei along external magnetic field and then measured directions of the emitted electrons. They saw maximal parity violation.

(c) Maximum Parity Violation in the Cobalt-60 Experiment



(d) Explanation of Cobalt-60 Experiment



(Leon Lederman *et al* observed similar effects in leptonic pion decays).

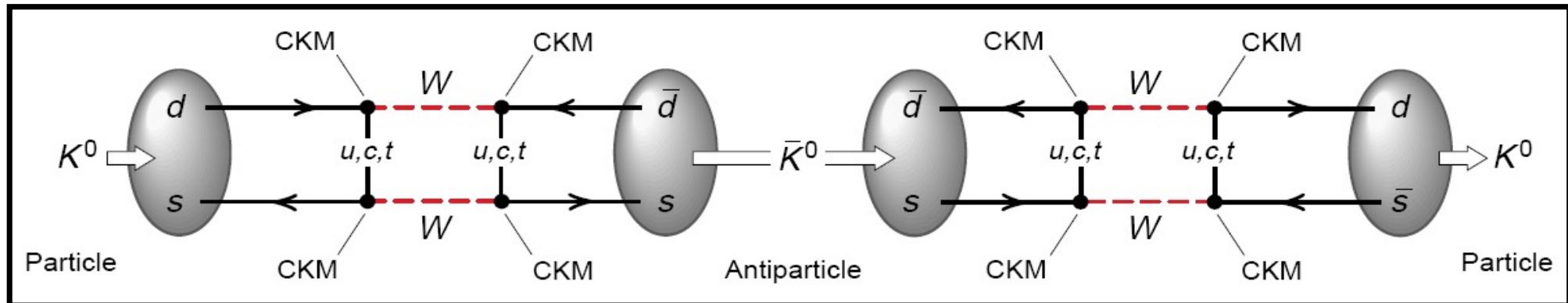
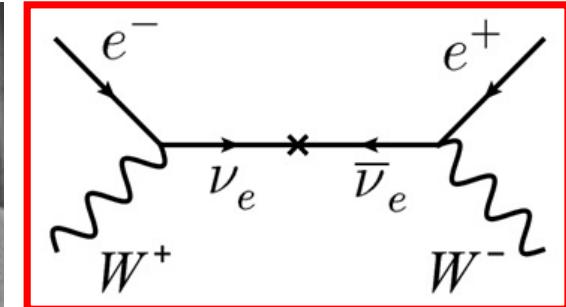
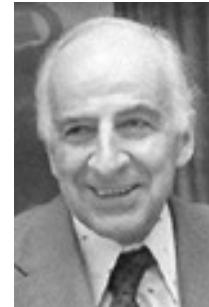
Tsung-Dao Lee and Chen-Ning Yang proposed the two-component theory: neutrinos are left-handed and exactly massless!



Pontecorvo (1957) and V-A (1958)

11

- ★ Bruno Pontecorvo's conjecture in 1957:
 - The two-component ν -theory is wrong.
 - Lepton number is violated (Majorana).
 - Transition between electron ν & anti- ν .



Murray Gell-mann and Abraham Pais 1955

Note: a single leptonic flavor cannot oscillate!

★ The V-A structure of weak interactions was formulated in 1958, inspired by measurement of maximal parity violation:

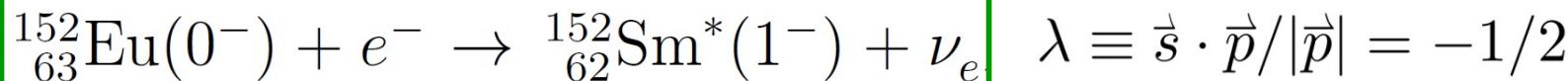
- George Sudarshan and Robert Marshak
- Richard Feynman and Murray Gell-Mann

$$P(\nu_e \rightarrow \bar{\nu}_e) = \frac{m_\nu^2}{E^2} |K|^2$$



Goldhaber (1958) and Sakata (1962) 12

★ The 2nd bad news: a neutrino did have the negative helicity and thus should have no mass. A proof of this was first done by Maurice Goldhaber et al in 1958.



★ The Nagoya school's conjectures: neutrinos are massive and mixed.

Progress of Theoretical Physics, Vol. 28, No. 5, November 1962

Remarks on the Unified Model of Elementary Particles

Ziro MAKI, Masami NAKAGAWA and Shoichi SAKATA

*Institute for Theoretical Physics
Nagoya University, Nagoya*



(Received June 25, 1962)

their original notation:

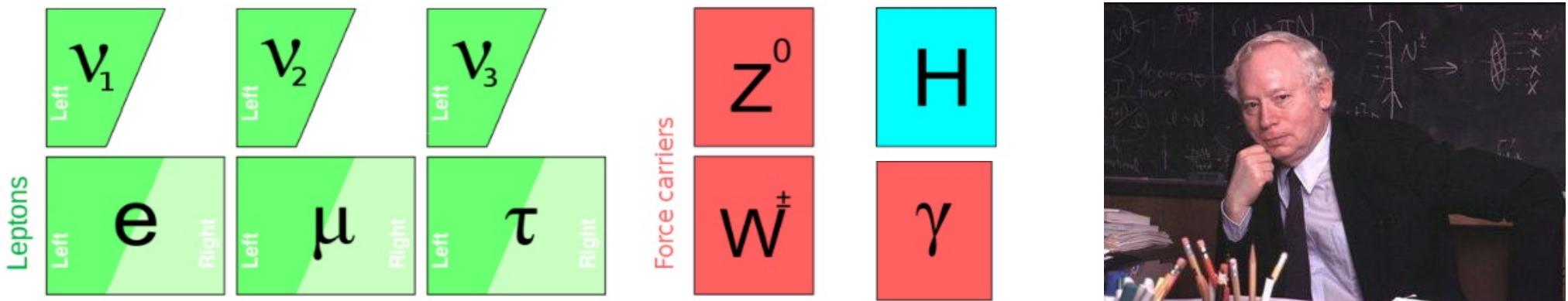
$$\nu_e = \nu_1 \cos \delta - \nu_2 \sin \delta,$$
$$\nu_\mu = \nu_1 \sin \delta + \nu_2 \cos \delta.$$

Inspired by Murray Gell-Mann + Maurice Levy 1960

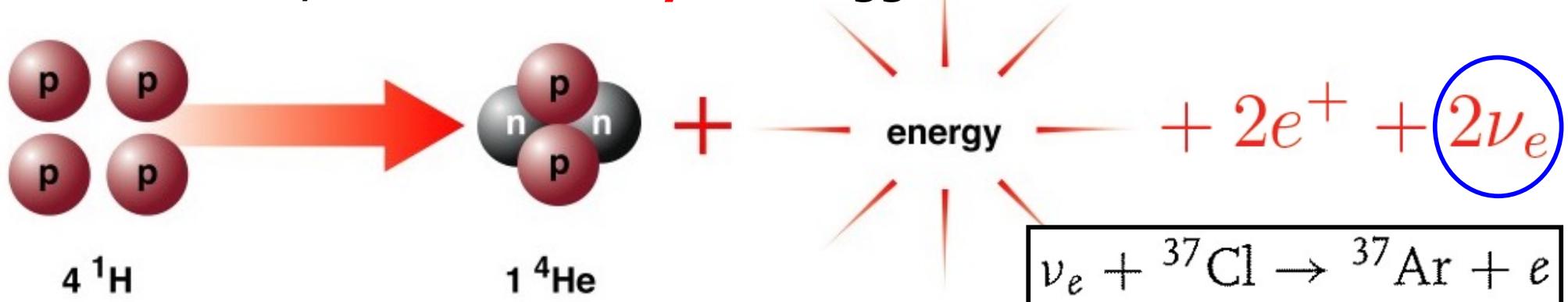
Weinberg (1967) and Davis (1968)

13

- ★ Steven Weinberg built a rigid framework for the electroweak theory in 1967 by putting aside right-handed neutrinos.

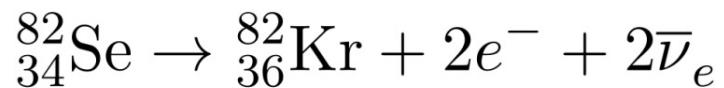


- ★ The 2nd good news: the solar neutrinos were observed by Raymond Davis in 1968, and an anomaly was suggestive of

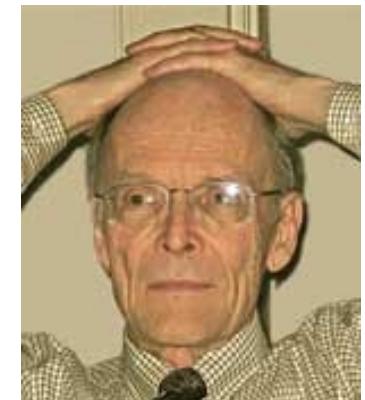


How can we tell what is going on inside the Sun? Photons take 1000 years to work their way out from the center to the surface, and what we see from the earth does not tell us much about the interior.

★ The 3rd good news: the double-beta decay of Se-82 was first observed by Michael Moe et al in 1987.



Tom Bonner Prize in nuclear physics 2013



VOLUME 59, NUMBER 18

PHYSICAL REVIEW LETTERS

2 NOVEMBER 1987

Direct Evidence for Two-Neutrino Double-Beta Decay in ^{82}Se

S. R. Elliott, A. A. Hahn, and M. K. Moe

Department of Physics, University of California, Irvine, Irvine, California 92717

(Received 31 August 1987)

The two-neutrino mode of double-beta decay in ^{82}Se has been observed in a time-projection chamber at a half-life of $(1.1 \pm 0.3) \times 10^{20}$ yr (68% confidence level). This result from direct counting confirms the earlier geochemical measurements and helps provide a standard by which to test the double-beta-decay matrix elements of nuclear theory. It is the rarest natural decay process ever observed directly in the laboratory.

The introduction of this paper is very informative:

- ◆ The $2\nu 2\beta$ transition was first suggested by Eugene Wigner in 1930.
- ◆ Wendell Furry remarked that $2\nu 2\beta$ could never be observed, but $0\nu 2\beta$ could.
- ◆ Ironically $2\nu 2\beta$ instead of $0\nu 2\beta$ was seen. Neutrino could be of Dirac nature.

Super-Kamiokande (1998)

15

★ The 4th good news: neutrinos do oscillate, so they must be massive.

Sun: Yoichiro Suzuki (4/6)

"Modest" Conclusions

- (1) Flux: $\phi^8 B = 2.44 \pm 0.05 (\text{stat.}) \pm 0.07 (\text{syst.}) \times 10^6 / \text{cm}^2 \cdot \text{sec}$:
(0.368 for BP95, 0.474 for BP98)
- (2) No seasonal variations.
- (3) $(D-N)/(D+N) = -0.023 \pm 0.020 (\text{stat.}) \pm 0.014 (\text{syst.})$
no difference:

excluded regions
extended into "small angle sol"

No core enhancement found.

(4) Day-Night+E-shape analysis.

(a) "No oscillation" is disfavoured
@ 1~5% C.L.

(b) L.A. solution is disfavoured
@ 1~5% C.L.

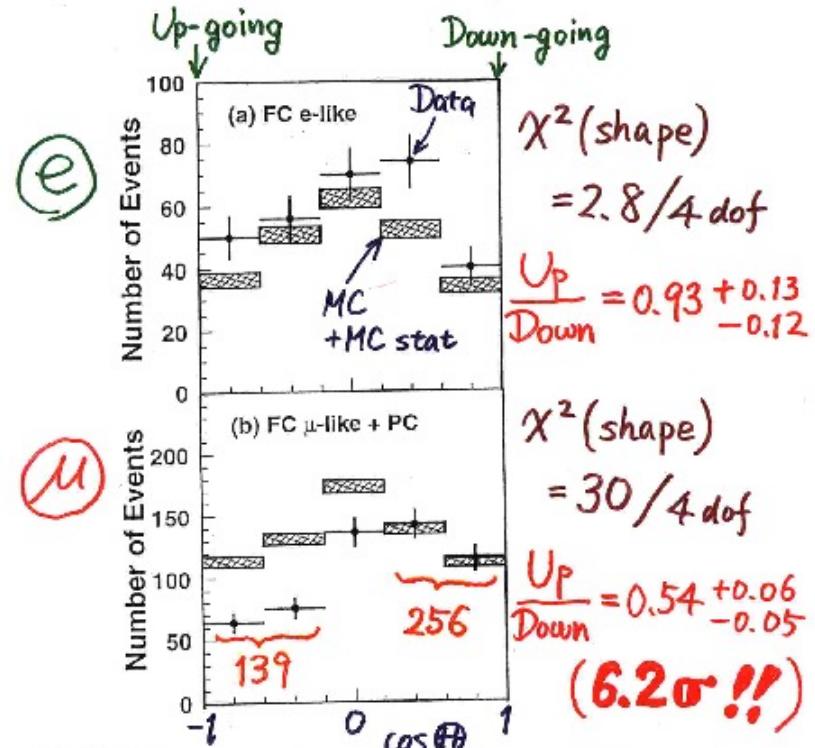
(c) V.O. regions are favoured
(than MSW regions)
@ 95% C.L.

(MSW is OK for 99% C.L.)



Atmosphere: Takaaki Kajita (5/6)

Zenith angle dependence (Multi-GeV)



* Up/Down syst. error for μ -like

Prediction (flux calculation $\leq 1\%$, 1km rock above SK 1.5%,) 1.8%

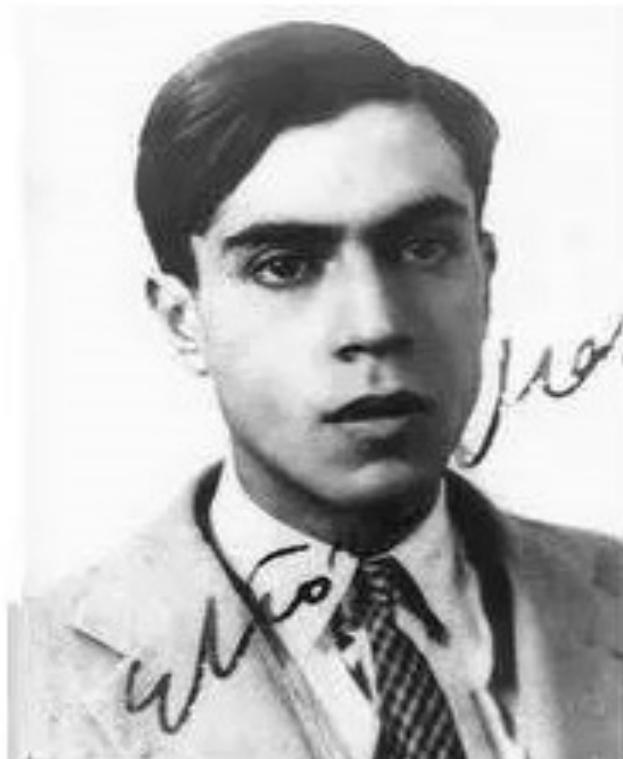
Data (Energy calib. for $\uparrow \downarrow$ 0.7%, Non ν Background < 2%) 2.1%

Neutrino98
TAKAYAMA

last question:
MAJORANA

OUTLINE

- A brief history: ideas and facts oscillated
- Salient properties of Majorana neutrinos



Palermo, 26 marzo 1938 - 1939
Caro Corradi,
Spero che tu non avrai troppo
tempo per leggermi e la lettera. Io sono un po' affaticato
e ritengo dovermi all'albergo Bologna, viaggiando per
una qualsiasi strada possibile. Ho poi intenzione di rimanere
all'incontro con te. Non mi piacerebbe per me ragionare
sull'argomento perché il caso è difficile. Come è ben detto
dovevi per interro chiedere.

Ettore Majorana

Weinberg's taste

17

VOLUME 19, NUMBER 21

PHYSICAL REVIEW LETTERS

20 NOVEMBER 1967

A MODEL OF LEPTONS*

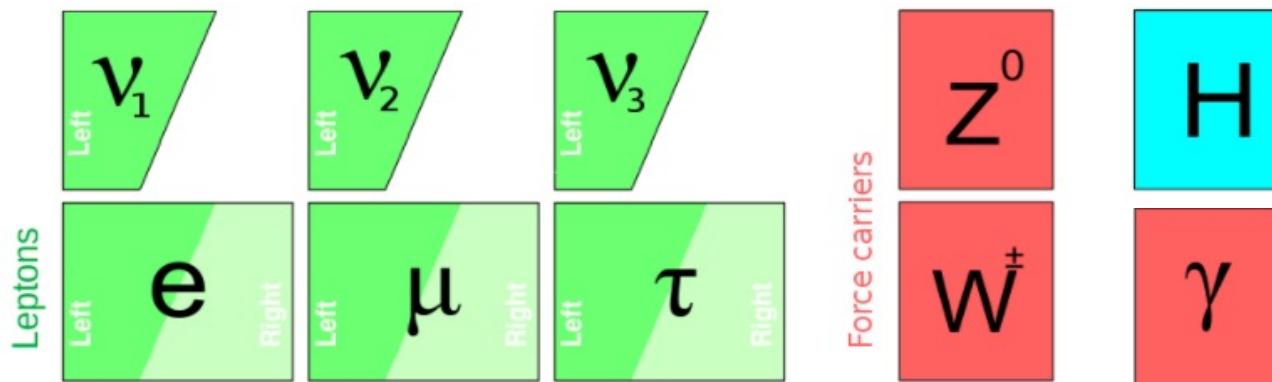
Steven Weinberg†

Laboratory for Nuclear Science and Physics Department,
Massachusetts Institute of Technology, Cambridge, Massachusetts
(Received 17 October 1967)



Theoretical ingredients: it's got what it matters (五脏俱全)

Particle content: no neutrino mass, no quarks, no flavor mixing & CPV



My style is usually not to propose **specific models** that will lead to specific experimental predictions, but rather to interpret in a broad way what is going on and make very **general remarks**, like with the development of the point of view associated with effective field theory ---- **Weinberg 2021@CERN Courier**

Go beyond the SM

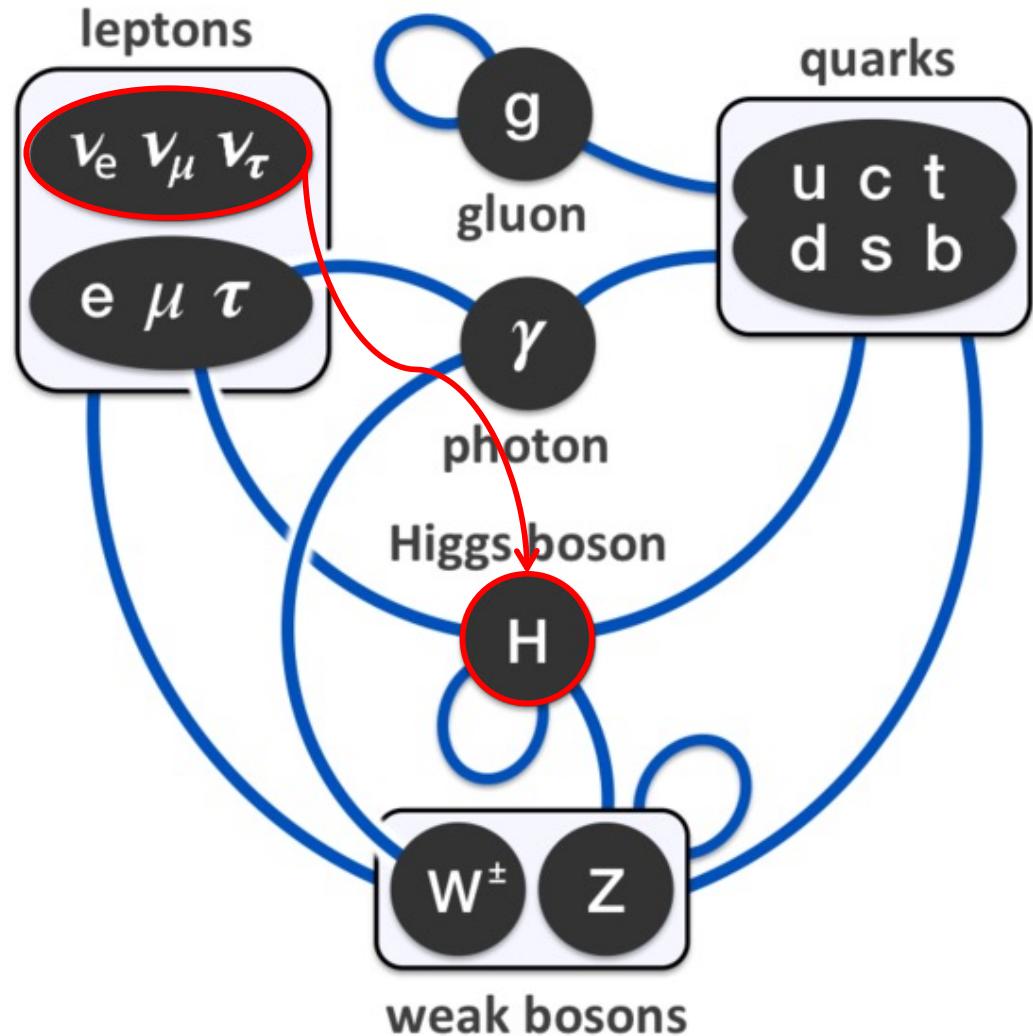
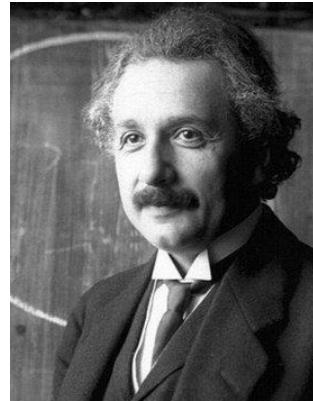
18

Albert Einstein: Everything should be made as simple as possible, but not simpler!

maximal P violation

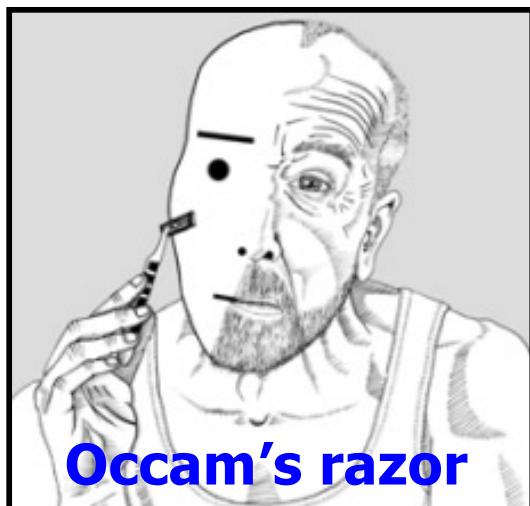
$$\begin{pmatrix} u_L \\ d_L \end{pmatrix} \longleftrightarrow u_R \quad \begin{pmatrix} d_L \\ u_R \end{pmatrix}$$

$$\begin{pmatrix} \nu_{eL} \\ e_L \end{pmatrix} \longleftrightarrow e_R \quad \text{with } \nu_{eL} \text{ and } e_L \text{ swapped}$$



- Theoretically unnatural
- Experimentally natural

cut off 7
physical
parameters



Occam's razor

★ The least cost to generate v -mass is a Yukawa coupling

★ Use charge-conjugated fields of left-handed v 's?
Pay with the scalar fields

Majorana is more natural

19

★ The simplest way to extend the SM is to introduce the right-handed neutrino fields and write out a **Dirac** mass term.

**Dirac
mass**

$$\bar{\ell}_L Y_\nu \tilde{H} N_R \longrightarrow M_D = Y_\nu \langle H \rangle$$

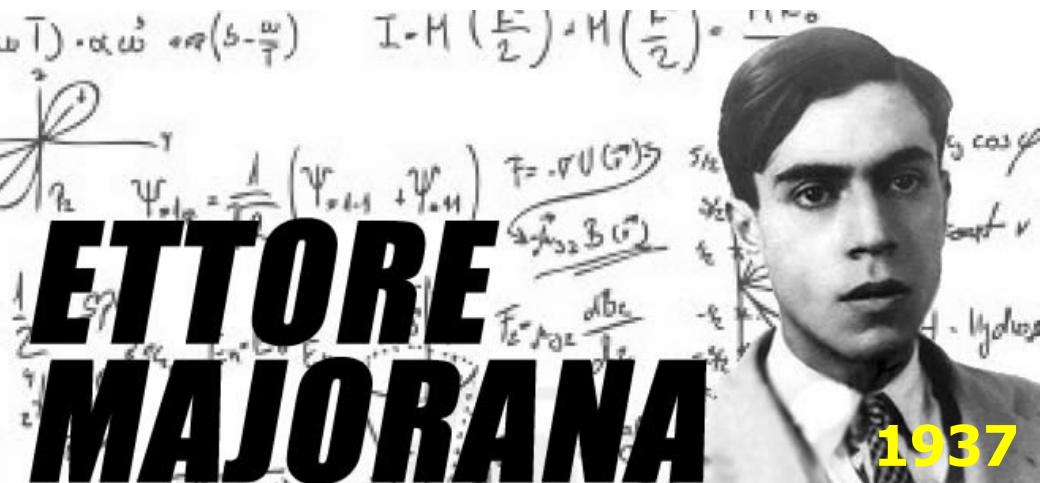
Murray Gell-Mann: everything not forbidden is compulsory!

**Majorana
mass**

$$\frac{1}{2} \overline{N_R^c} M_R N_R$$



It is lepton-number-violating.



mass state: **antineutrino=neutrino**

In the SM, **L** and **B** are violated by instantons, only **B – L** is conserved.

$$-\mathcal{L}_{\nu+N} = \overline{\nu_L} M_D N_R + \frac{1}{2} \overline{(N_R)^c} M_R N_R + \text{h.c.} = \frac{1}{2} [\nu_L \quad (N_R)^c] \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \begin{pmatrix} (\nu_L)^c \\ N_R \end{pmatrix} + \text{h.c.}$$

P. Minkowski 1977, T. Yanagida 1979:

$$M_\nu \simeq -M_D M_R^{-1} M_D^T = -\langle H \rangle^2 Y_\nu M_R^{-1} Y_\nu^T$$

★ This **seesaw** picture is consistent with the **Weinberg** operator (1979):

$$\mathcal{O}_{\text{Weinberg}} = \frac{\kappa_{\alpha\beta}}{2} \left[\overline{\ell_{\alpha L}} \tilde{H} \tilde{H}^T \ell_{\beta L}^c \right]$$

LFV and LNV

20

★ Diagonalizing the **6×6 neutrino mass matrix by a 6×6 unitary matrix**

$$\begin{pmatrix} U & R \\ S & U' \end{pmatrix}^\dagger \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \begin{pmatrix} U & R \\ S & U' \end{pmatrix}^* = \begin{pmatrix} D_\nu & 0 \\ 0 & D_N \end{pmatrix}$$

$$D_\nu \equiv \text{Diag}\{m_1, m_2, m_3\}, D_N \equiv \text{Diag}\{M_1, M_2, M_3\}$$

$$\overline{(N_R)^c} M_D^T (\nu_L)^c = [(N_R)^T \mathcal{C} M_D^T \mathcal{C} \overline{\nu_L}^T]^T = \overline{\nu_L} M_D N_R$$

Majorana mass states:

$$\nu' = \begin{bmatrix} \nu'_L \\ (N'_R)^c \end{bmatrix} + \begin{bmatrix} (\nu'_L)^c \\ N'_R \end{bmatrix} = \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ N_1 \\ N_2 \\ N_3 \end{pmatrix}$$

$$(\nu')^c = \nu'$$

Three flavor states are linear combinations of six mass states (LFV):

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}_L = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}_L + R \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix}_L$$

$$UU^\dagger + RR^\dagger = I$$

★ The standard weak charged-current interactions:

$$-\mathcal{L}_{cc} = \frac{g}{\sqrt{2}} \overline{(e \ \mu \ \tau)_L} \gamma^\mu \left[U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}_L + R \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix}_L \right] W_\mu^- + \text{h.c.}$$

global rephasing

$$\ell_L(x) \rightarrow e^{i\phi} \ell_L(x)$$

$$\nu'_L(x) \rightarrow e^{i\phi} \nu'_L(x)$$

↓ LNV

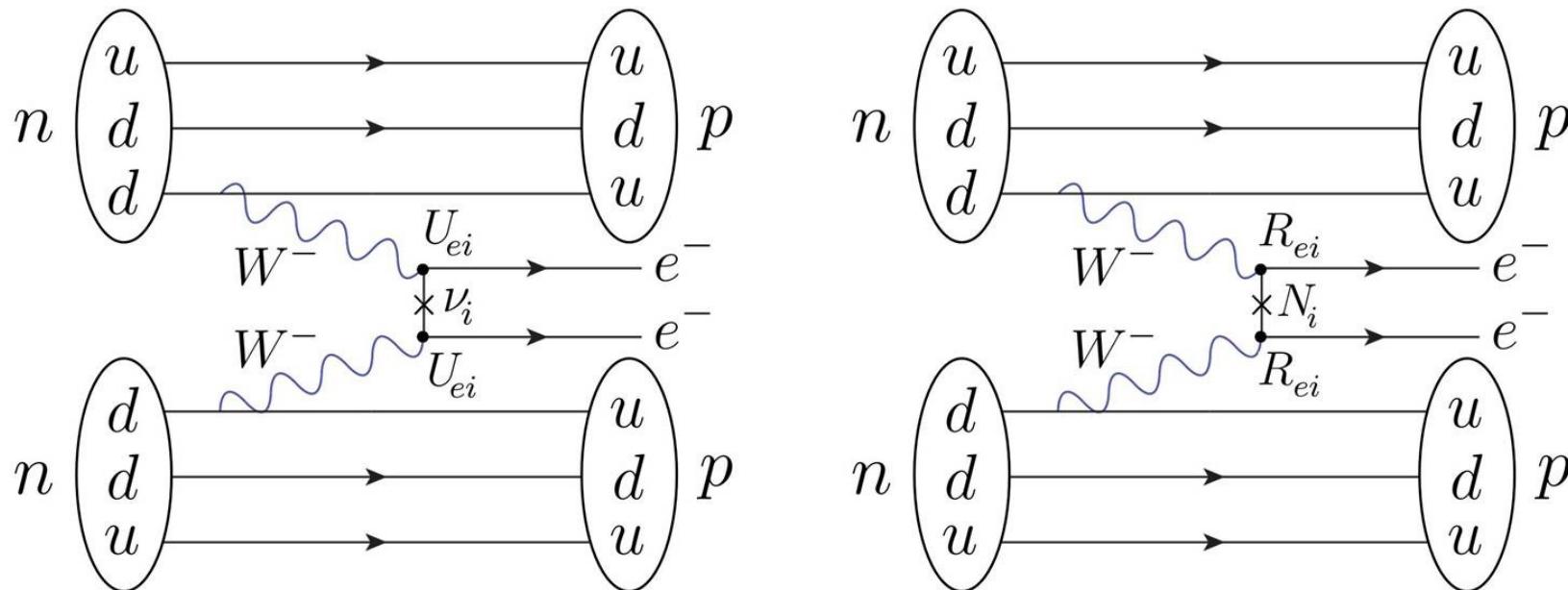
U = non-unitary light neutrino mixing.
R = small light-heavy neutrino mixing.

$$-\mathcal{L}'_\nu = \frac{1}{2} \overline{\nu'_L} D_\nu (\nu'_L)^c + \text{h.c.}$$

0ν2β decays

21

★ Lepton number violation (neutrinoless double-beta decays):



★ In most cases the contribution of heavy Majorana neutrinos to 0ν2β is negligible in the canonical type-one seesaw.
 ZZX, arXiv:0907.3014; W. Rodejohann, 0912.3388.

$$UD_\nu U^T = -RD_NR^T$$

$$\Gamma_{0\nu2\beta} \propto \left| \sum_{i=1}^3 m_i U_{ei}^2 - M_A^2 \sum_{i=1}^3 \frac{R_{ei}^2}{M_i} \mathcal{F}(A, M_i) \right|^2 = \left| \sum_{i=1}^3 M_i R_{ei}^2 \left[1 + \frac{M_A^2}{M_i^2} \mathcal{F}(A, M_i) \right] \right|^2$$

★ There're many different lepton-number-violating scenarios for 0ν2β.

Bet on the simplest seesaw?

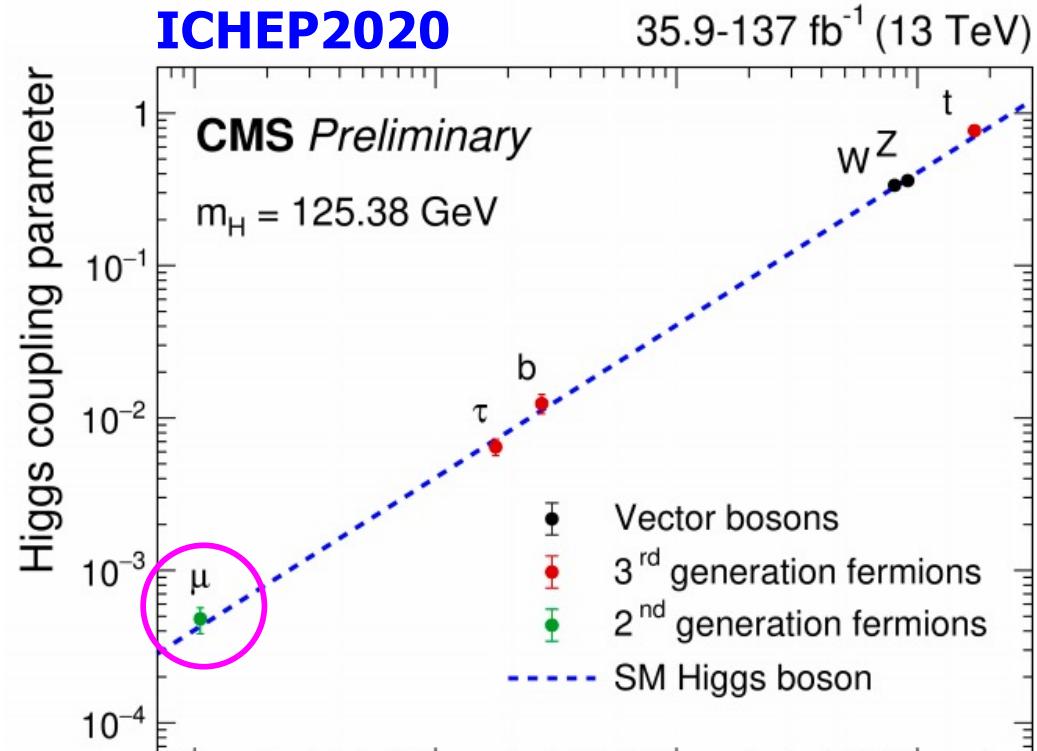
22

★ New experimental evidence for Yukawa interactions at tree level:

★ So Steven Weinberg's model in 2020 seems invalid.

★ There is no good reason for v's not to have a Yukawa interaction at tree level.

★ But it is the poor's philosophy! Many *new physics* models ...



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Models of lepton and quark masses

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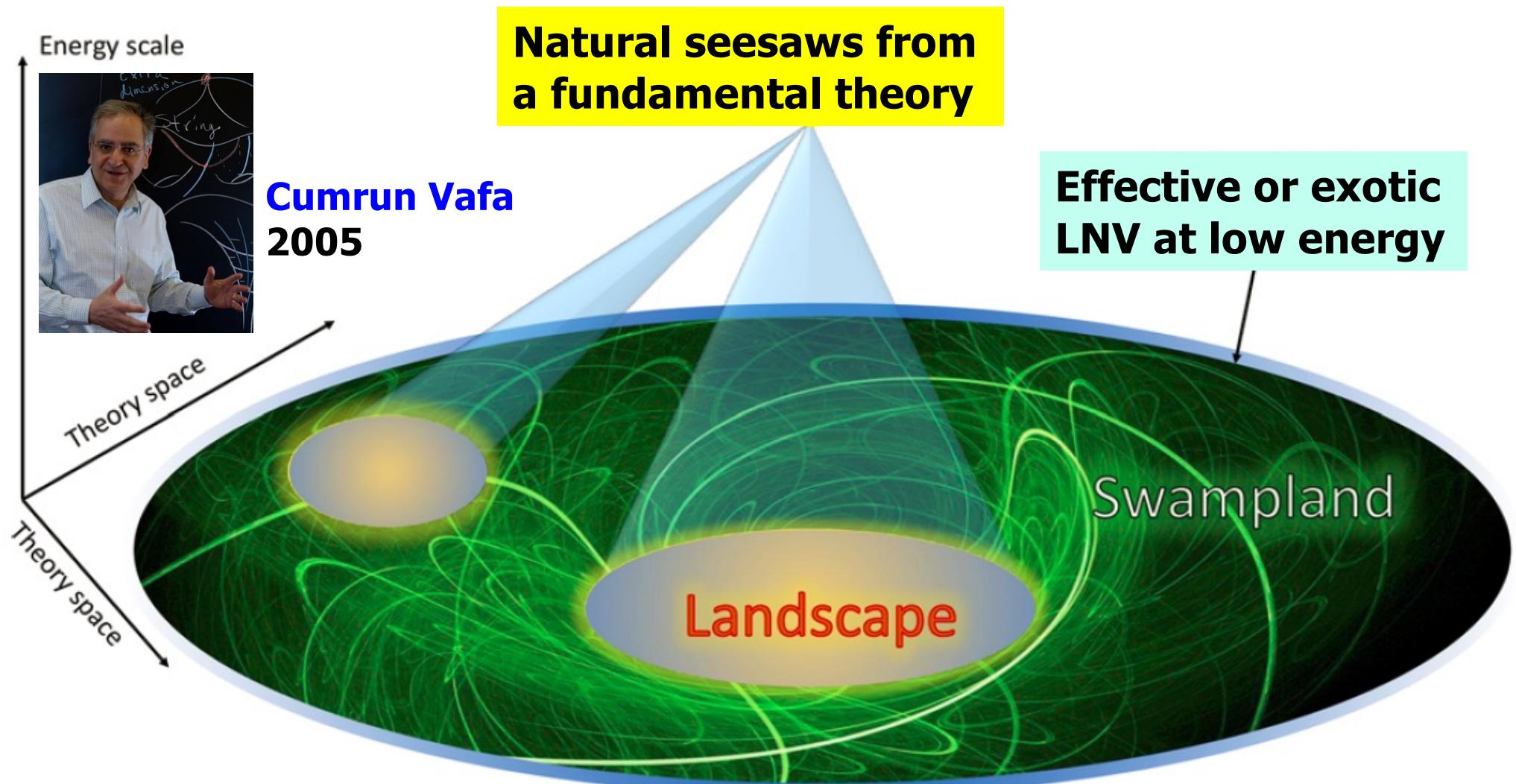
at age
of 87

A class of models is considered in which the masses only of the third generation of quarks and leptons arise in the tree approximation, while masses for the second and first generations are produced respectively by one-loop and two-loop radiative corrections. So far, for various reasons, these models are not realistic.

A $0\nu2\beta$ landscape or swampland

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- ★ **Landscape:** ν -mass models originate from a complete flavor theory.
- ★ **Swampland:** *new physics* which has nothing or little to do with ν 's.

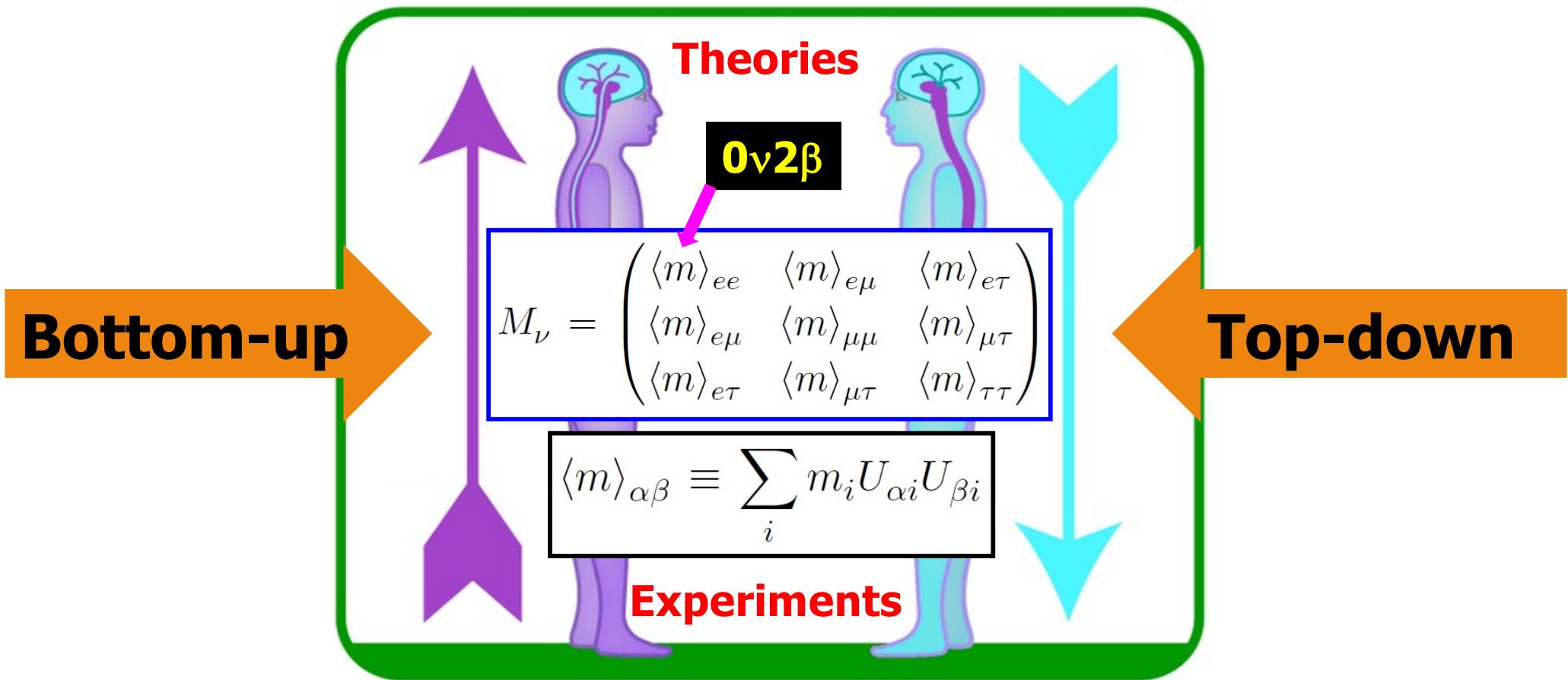


- ★ Imprints of *new physics* models on the low-energy $0\nu2\beta$ processes.

Concluding remarks

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Without information on the **nature of massive neutrinos** (**Majorana or not**) and **all the CP-violating phases**, one will have no way to establish a full theory of ν masses and flavor mixing. Give **$0\nu2\beta$** a chance!

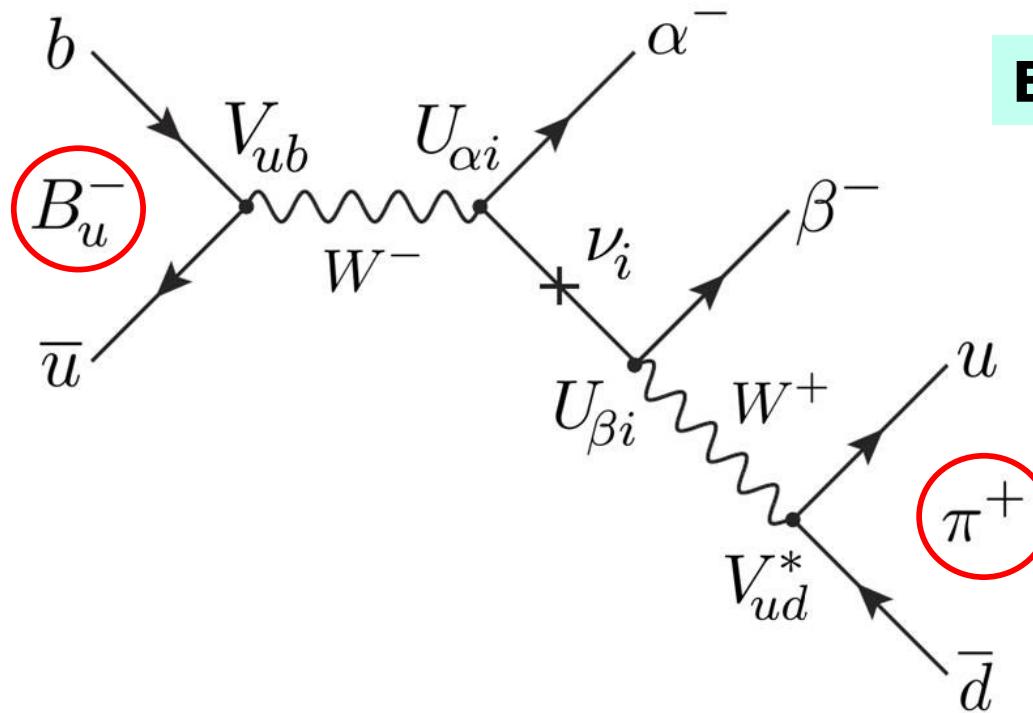


Within about **10 years**, after both the neutrino mass ordering and the **Dirac CP-violating phase** are measured, one has to try **all the possible ways** to determine the absolute mass scale and two **Majorana phases**.

Hopeless at low energies?

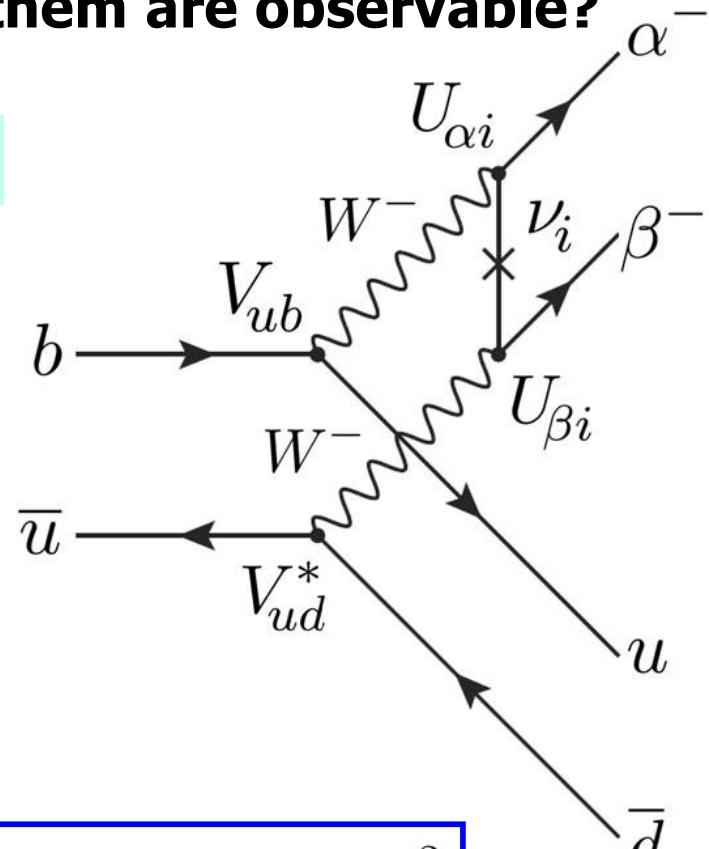
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There are many LNV processes, but none of them are observable?



Example

+



decay rates suppressed

$$\Gamma(B_u^- \rightarrow \pi^+ \alpha^- \beta^-) \propto |\langle m \rangle_{\alpha\beta}|^2 = \left| \sum_{i=1}^3 (m_i U_{\alpha i} U_{\beta i}) \right|^2$$

$$\mathcal{B}(B_u^- \rightarrow \pi^+ e^- e^-) < 2.3 \times 10^{-8} \text{ (CL = 90\%)}$$

$$\mathcal{B}(B_u^- \rightarrow \pi^+ e^- \mu^-) < 1.5 \times 10^{-7} \text{ (CL = 90\%)}$$

$$\mathcal{B}(B_u^- \rightarrow \pi^+ \mu^- \mu^-) < 4.0 \times 10^{-9} \text{ (CL = 95\%)}$$

History tells us: the fool didn't know it's impossible, so he did it and sometimes succeeded...

Majorana's poetry and distance

**Wind blow blow
Water cold cold
Strongman go go
Come back no no**

风萧萧兮，易水寒，壮士一去兮，不复还