Decision Trees

January 17, 2020

Introduction

- ► We will now study a Machine Learning tool : Decision Trees
- ► They can be used for **classification** and for **regression**.

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- ► For instance we study two types of fishs : the possible classes are **tuna** and **salmon**.
- ► Each fish has two features : its weight and its length.
- ► The question is : are we able to **predict the class by looking at the features ?**

Problem statement

- The **Decision Tree** is a classifier that we will build from the data that will help us to **predict the class of a new datapoint**.

Problem statement

▶ When the tree is built, it will look like this. Let us analyze
  what this means :
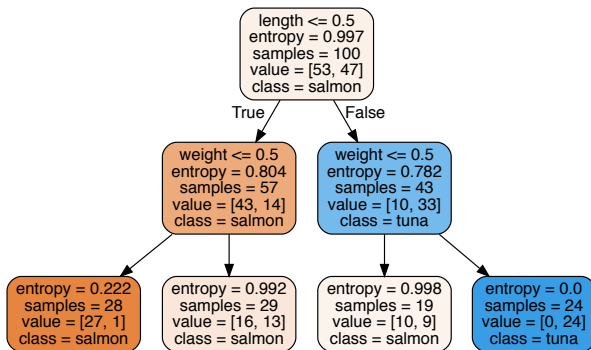
Building a tree

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- ▶ We are interested in a method that would automatically build the tree for us.
- ▶ Let us try to design such a method.

Segmentation variable

▶ We start from a simple tree with only one node.
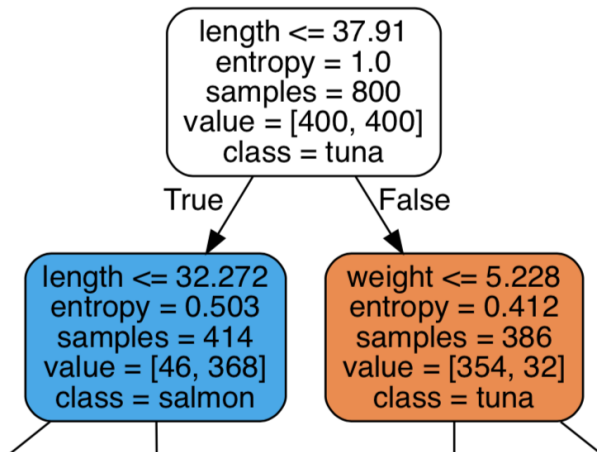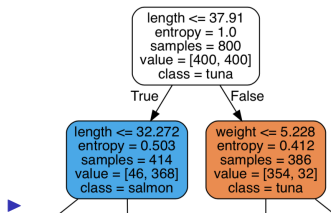
Segmentation

Figure: segmentation

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▶

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- ▶ We start from a simple tree with only one node.
- ▶ We want to find the feature that helps us to predict the class of the fish with most certainty.
- ▶ We then need a measure of the informativeness of the feature on the class.
- ▶ There are several possible measures :
  - ▶ Gini factor
  - ▶ Information gain
  - ▶ Misclassification probability

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- Let X be a random variable, that can take the values a_k with probability p_k.
- Its entopy is then

$$H = -\sum_{i=1}^{n} p_k \log p_k \qquad (1)$$

Entropy

- Usually the logarithm in base 2 is used.
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Remark : the value of the entropy does not depend on the values taken by the random variable, but only on the distribution.

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- ▶ We have a database of 800 fishes (tunas and salmon).
- ▶ the features of the fishes are stored in **numpy arrays**.
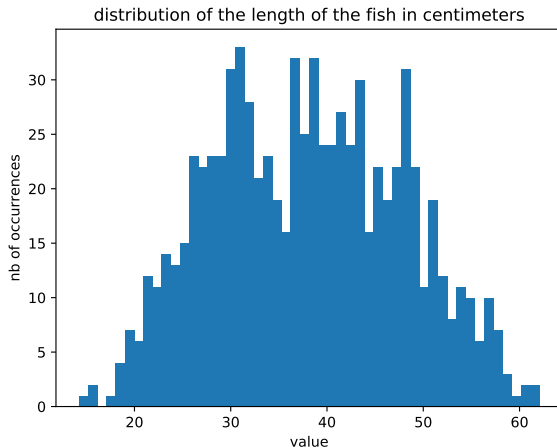
Dataset : ipython demo

```
In [44]: np.load("fish_features.npy")
Out[44]:
array([[53.75892579,  0.27022806],
       [43.5530757 ,  5.39964379],
       [48.71780521,  0.57694348],

       ...,
       [27.63229236,  4.86565666],
       [24.64053512,  5.5411517 ],
       [35.20792985,  4.22064417]])

In [45]:
```
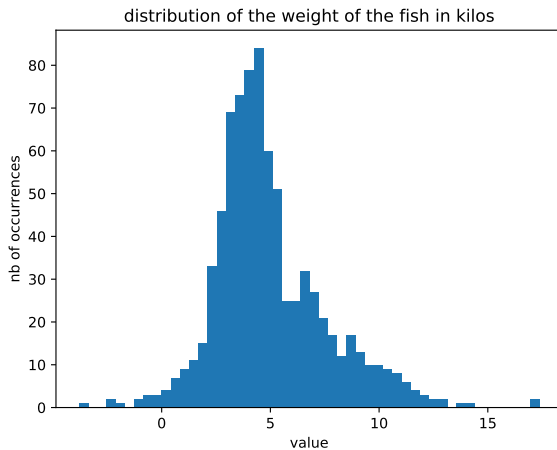
Dataset : histograms

distribution of the length of the fish in centimeters

Dataset : histograms

distribution of the weight of the fish in kilos

Visualization

What other visualization could we make ?

Exercise 1

- Given the number n of datapoints, what is the maximal number of nodes in the tree ?

Implementation

- We will use **sklearn** to build decision trees.
- https:
  //scikit-learn.org/stable/modules/generated/
  sklearn.tree.DecisionTreeClassifier.html
- https://scikit-learn.org/stable/modules/tree.html

Implementation

- **pip install sklearn**
- We will also need
    - **numpy**
    - **matploblib**

Exercise 2

- ▶ Use the file **fish_tree.py** in order to build your decision tree and plot it.
- ▶ Try to use different depths.

Exercise 3

► Uncomment the end of the file **fish_tree.py** in order to predict the class for new fishes.

Exercise 4

- Modify the file **fish_dataset.py** in order to modify the dataset by **adding a new feature to the fishes**.

Exercise 5

- ▶ Use the file **fish_tree_pruned.py** so that the obtained tree has a smaller number of nodes.
- ▶ You can use the documentation https: //scikit-learn.org/stable/modules/generated/ sklearn.tree.DecisionTreeClassifier.html
- ▶ You can modify :
  - ▶ the distributions
  - ▶ the value of the parameters **min_samles_split** and **min_impurity_decrease**

Exercise 6

- ▶ We can apply what we learned to a famous dataset, the **iris dataset**.
- ▶ please use the file **iris.py** in order to build several decision trees with different number of nodes, by changing the specifications given to sklearn.

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- ▶ When the variable to predict is continuous, we build a **regression** tree.
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Complexity analysis

Overfitting

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- ▶ To handle it, **pruning** is often performed. It consists in **removing nodes from the tree** :
  - ▶ **pre pruning :** while building the tree, we choose not to split some nodes
  - ▶ **post pruning :** after building the tree, we remove some nodes.
  - ▶ in **Exercise 5** we used prepruning.