

# IST 772 Homework 2

Due October 19, 2021 at 8:00AM EDT

Homework 2 by Nora Lin: I produced the material below with no assistance.

## Excercise 1 p.35:

```
#Flipping a fair coin nine times:  
#1 trial of 9 fair coin tosses in each trial  
table(rbinom(n=1, size=9, prob=0.5))
```

```
##  
## 7  
## 1
```

```
#100,000 trails of 9 fair coin tosses in each trial  
table(rbinom(n=100000, size=9, prob=0.5))
```

```
##  
##      0      1      2      3      4      5      6      7      8      9  
## 163 1725 7127 16327 24534 24832 16297 7017 1781 197
```

## Excercise 2 p.35:

```
barplot(table( rbinom(n=100000, size=9, prob=0.5)))
```

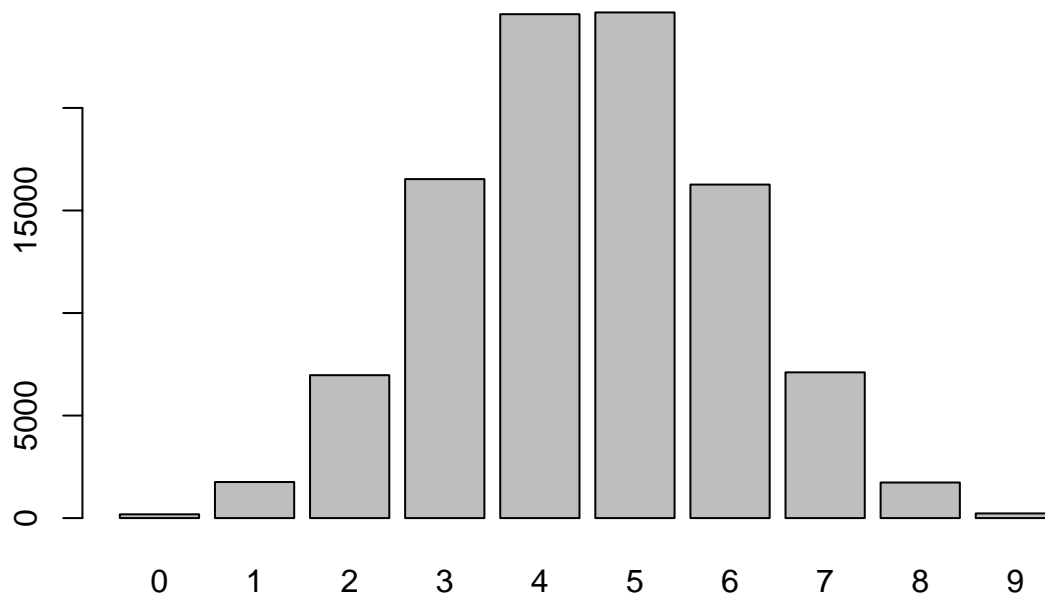
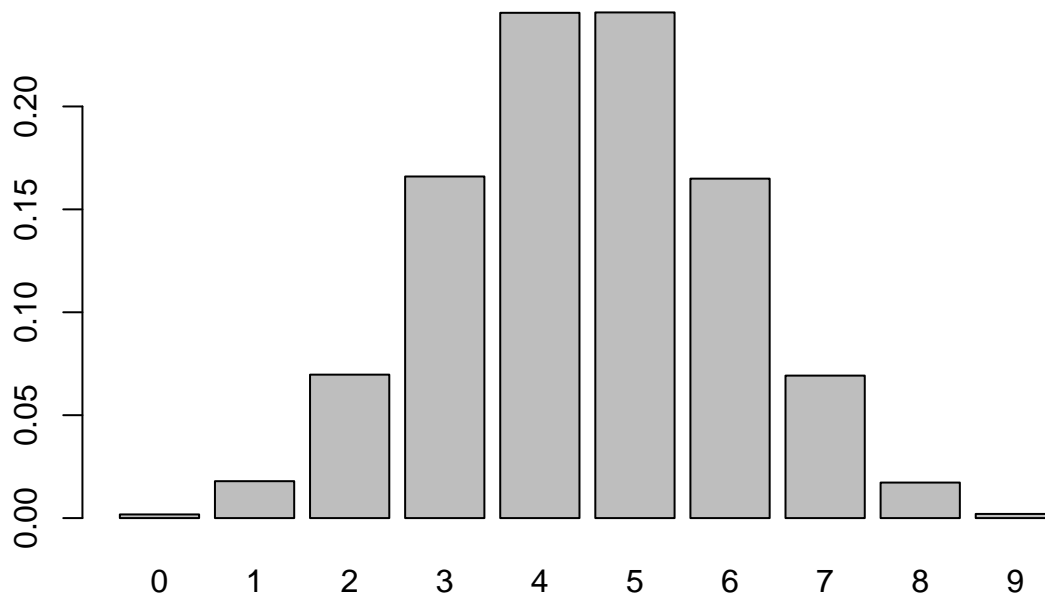


Figure 1: Barplot of  $n=100,000$  trials of nine flips each

```
table( rbinom(n=100000, size=9, prob=0.5))/100000
```

```
##
##      0      1      2      3      4      5      6      7      8      9
## 0.00208 0.01758 0.07170 0.16469 0.24521 0.24733 0.16286 0.06892 0.01741 0.00222
```

```
barplot(table( rbinom(n=100000, size=9, prob=0.5))/100000)
```



**Figure 2:** Bar plot of probabilities of each trial for n=100,000 trials in a binomial distribution

#### Analysis:

Figure 1 signifies a bar plot of 9 fair coins being flipped 100,000 times. The x-axis shows the number of times Heads was recorded. The y-axis shows the raw count for the corresponding number of Heads. In 100,000 trials of flipping a fair coin 9 times, there were 1,856 counts of 1 Head and 9 Tails.

Figure 2 signifies a bar plot of the probabilities of each trial for n=100,000 trails in a binomial distribution. The x-axis is the same as Figure 1. The Y-axis is the probability of each trial. In 100,000 trials of flipping a fair coin 9 times, the probability of getting three heads is 0.16292 or %16.29.

Figure 1 and 2 are related in that figure 1 is the raw counts and figure 2 is the probabilities of those raw counts.

The shape of both figures are normally distributed and centered around 4.5. This makes sense because of central tendency.

#### Exercise 6 p.36:

```
stat_test <- matrix(c(33,17,50,47,3,50,80,20,100),ncol=3,byrow=TRUE)
colnames(stat_test)<- c("Pass","Fail","Row totals")
rownames(stat_test)<- c("High school students","College students","Column totals")
stat_test <- as.table(stat_test)
stat_test
```

```
##               Pass Fail Row totals
```

```
## High school students 33 17 50
## College students 47 3 50
## Column totals 80 20 100
```

**Table 1.1: Two-by-Two Contingency Table with statistics test labels, data, and marginal totals**

```
stat_testProbs <- stat_test/100
stat_testProbs
```

```
##          Pass Fail Row totals
## High school students 0.33 0.17 0.50
## College students 0.47 0.03 0.50
## Column totals 0.80 0.20 1.00
```

**Table 1.2: Two-by-Two Contingency Table with frequencies converted to probabilities.**

If one were to only focus on high school students, the probability that a student would pass the test would be 0.33 or 33%.

### Excercise 7 p.36:

```
UKhomes <- matrix(c(2,69,71,93933,5996,99929,93935,6065,100000),ncol=3,byrow=TRUE)
#UKhomes
colnames(UKhomes) <- c("Pass","Fail","Row total")
rownames(UKhomes) <- c("Defaulting mortgage","Not defaulting mortgage", "Column Total")
UKhomes <-as.table(UKhomes)
UKhomes
```

```
##          Pass  Fail Row total
## Defaulting mortgage      2    69      71
## Not defaulting mortgage 93933 5996 99929
## Column Total      93935 6065 100000
```

**Table 2.1: Two-by-Two Contingency Table with frequencies converted to probabilities**

```
UKhomesProbs <- UKhomes/100000
UKhomesProbs
```

```
##          Pass  Fail Row total
## Defaulting mortgage 0.00002 0.00069 0.00071
## Not defaulting mortgage 0.93933 0.05996 0.99929
## Column Total      0.93935 0.06065 1.00000
```

**Table 2.2: Two-by-Two Contingency Table with UK home repossession labels, data, and marginal totals**

0.93935 or 93.94% of homes both passed the Barclays Bank test and do not have their homes repossessed.

### Excercise 8 p.36:

```

norm_UKhomesProb <- matrix(c(UKhomesProbs[1,2],(UKhomesProbs[1,2]/UKhomesProbs[3,2]),
                             UKhomesProbs[2,2],(UKhomesProbs[2,2]/UKhomesProbs[3,2]),
                             UKhomesProbs[3,2],(UKhomesProbs[3,2]/UKhomesProbs[3,2])),
                             ncol=2,byrow=TRUE)
#norm_UKhomesProb
colnames(norm_UKhomesProb) <- c("Raw Fail Prob", "Norm Fail Prob")
rownames(norm_UKhomesProb) <-c("Defaulting mortgage","Not defaulting mortgage","Marginal")
norm_UKhomesProb

```

```

##              Raw Fail Prob Norm Fail Prob
## Defaulting mortgage      0.00069      0.01137675
## Not defaulting mortgage    0.05996      0.98862325
## Marginal                  0.06065      1.00000000

```

**Table 2.3: Excerpt of Table Showing UK home reposessions with Normalized Probabilities**

There is a 0.01137675 or 0.11% probability that this new customer who failed the Barclays Bank screening test will actually default on his or her mortgage.

End of Homework Assignment #2