RxODE user manual

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Introduction

Welcome to the RxODE user guide; **RxODE** is an R package for solving and simulating from ode-based models. These models are convert the RxODE minilanguage to C and create a compiled dll for fast solving. ODE solving using RxODE has a few key parts:

- RxODE() which creates the C code for fast ODE solving based on a simple syntax (Chapter 5) related to Leibnitz notation.
- The event data, which can be:
 - a NONMEM or deSolve compatible data frame (Chapter 6), or
 - created with et() or EventTable() for easy simulation of events(Chapter ??)
 - The data frame can be augmented by adding time varying or adding individual covariates (iCov= as needed)
- rxSolve() which solves the system of equations using initial conditions and parameters to make predictions
 - With multiple subject data, this may be parallelized.
 - With single subject the output data frame is adaptive
 - Covariances and other metrics of uncertanty can be used to simulate while solving.

While this is the user guide, there are other places that you can visit for help:

This book was assembled on Tue Dec 15 18:00:51 2020 with RxODE version 1.0.0.0 automatically by github actions.

Related R packages

2.1 ODE solving

This is a brief comparison of pharmacometric ODE solving R packages to RxODE.

There are several R packages for differential equations. The most popular is deSolve.

However for pharmacometrics-specific ODE solving, there are only 2 packages other than RxODE released on CRAN. Each uses compiled code to have faster ODE solving.

- mrgsolve, which uses C++ lsoda solver to solve ODE systems. The user is required to write hybrid R/C++ code to create a mrgsolve model which is translated to C++ for solving.
 - In contrast, RxODE has a R-like mini-language that is parsed into C code that solves the ODE system.
 - Unlike RxODE, mrgsolve does not currently support symbolic manipulation of ODE systems, like automatic Jacobian calculation or forward sensitivity calculation (RxODE currently supports this and this is the basis of nlmixr's FOCEi algorithm)
- dMod, which uses a unique syntax to create "reactions". These reactions create the underlying ODEs and then created c code for a compiled deSolve model

In contrast RxODE defines ODE systems at a lower level. RxODE's parsing of the mini-language comes from C, whereas dMod's parsing comes from R.

Like RxODE, dMod supports symbolic manipulation of ODE systems and calculates forward sensitivities and adjoint sensitivities of systems.

Unlike RxODE, dMod is not thread-safe since deSolve is not yet thread-safe.

And there is one package that is not released on CRAN:

PKPDsim which defines models in an R-like syntax and converts the system to compiled code.

Like mrgsolve, PKPDsim does not currently support symbolic manipulation of ODE systems.

PKPDsim is not thread-safe.

The open pharmacometrics open source community is fairly friendly, and the RxODE maintainers has had positive interactions with all of the ODE-solving pharmacometric projects listed.

2.2 PK Solved systems

RxODE supports 1-3 compartment models with gradients (using stan math's auto-differentiation). This currently uses the same equations as PKADVAN to allow time-varying covariates.

RxODE can mix ODEs and solved systems.

2.2.1 The following packages for solved PK systems are on CRAN

- mrgsolve currently has 1-2 compartment (poly-exponential models) models built-in. The solved systems and ODEs cannot currently be mixed.
- pmxTools currently have 1-3 compartment (super-positioning) models built-in. This is a R-only implementation.
- PKPDmodels has a one-compartment model with gradients.

2.2.2 Non-CRAN libraries:

PKADVAN Provides 1-3 compartment models using non-superpositioning.
 This allows time-varying covariates.

Installation

You can install the released version of RxODE from CRAN with:

```
install.packages("RxODE")
```

To build models with RxODE, you need a working c compiler. To use parallel threaded solving in RxODE, this c compiler needs to support open-mp.

You can check to see if R has working c compiler you can check with:

```
## install.packages("pkgbuild")
pkgbuild::has_build_tools(debug = TRUE)
```

If you do not have the toolchain, you can set it up as described by the platform information below:

3.0.1 Windows

In windows you may simply use install rto install rtools:

```
install.packages("installr")
library(installr)
install.rtools()
```

Alternatively you can download and install rtools directly.

3.0.2 Mac OSX

To get the most speed you need OpenMP enabled and compile RxODE against that binary. Here is some discussion about this:

https://mac.r-project.org/openmp/

3.0.3 Linux

To install on linux make sure you install gcc (with openmp support) and gfortran using your distribution's package manager.

3.1 Development Version

Since the development version of RxODE uses StanHeaders, you will need to make sure your compiler is setup to support C++14, as described in the rstan setup page

Once the C++ toolchain is setup appropriately, you can install the development version from GitHub with:

```
# install.packages("devtools")
devtools::install_github("nlmixrdevelopment/RxODE")
```

Getting Started

The model equations can be specified through a text string, a model file or an R expression. Both differential and algebraic equations are permitted. Differential equations are specified by d/dt(var_name) =. Each equation can be separated by a semicolon.

To load RxODE package and compile the model:

```
library(RxODE)

#> RxODE 1.0.0.0 using 4 threads (see ?getRxThreads)

library(units)
```

#> udunits system database from /usr/share/xml/udunits

```
mod1 <-RxODE({
    C2 = centr/V2;
    C3 = peri/V3;
    d/dt(depot) =-KA*depot;
    d/dt(centr) = KA*depot - CL*C2 - Q*C2 + Q*C3;
    d/dt(peri) = Q*C2 - Q*C3;
    d/dt(eff) = Kin - Kout*(1-C2/(EC50+C2))*eff;
})</pre>
```

#> qs v0.23.4.

4.1 Specify ODE parameters and initial conditions

Model parameters can be defined as named vectors. Names of parameters in the vector must be a superset of parameters in the ODE model, and the order of parameters within the vector is not important.

```
theta <-
c(KA=2.94E-01, CL=1.86E+01, V2=4.02E+01, # central
Q=1.05E+01, V3=2.97E+02, # peripheral
Kin=1, Kout=1, EC50=200) # effects
```

Initial conditions (ICs) can be defined through a vector as well. If the elements are not specified, the initial condition for the compartment is assumed to be zero.

```
inits <- c(eff=1);</pre>
```

If you want to specify the initial conditions in the model you can add:

```
eff(0) = 1
```

4.2 Specify Dosing and sampling in RxODE

RXODE provides a simple and very flexible way to specify dosing and sampling through functions that generate an event table. First, an empty event table is generated through the "eventTable()" function:

```
ev <- eventTable(amount.units='mg', time.units='hours')</pre>
```

Next, use the add.dosing() and add.sampling() functions of the EventTable object to specify the dosing (amounts, frequency and/or times, etc.) and observation times at which to sample the state of the system. These functions can be called multiple times to specify more complex dosing or sampling regiments. Here, these functions are used to specify 10mg BID dosing for 5 days, followed by 20mg QD dosing for 5 days:

If you wish you can also do this with the mattigr pipe operator %>%

The functions get.dosing() and get.sampling() can be used to retrieve information from the event table.

```
head(ev$get.dosing())
     id low time high
                            cmt
                                  amt rate ii addl evid ss dur
        NA
               0
                   NA (default) 10000
                                         0 12
                                                 9
                                                      1
        NA
                   NA (default) 20000
                                         0 24
           120
head(ev$get.sampling())
                        cmt amt rate ii addl evid ss dur
     id low time high
#> 1 1
                   NA (obs)
                                                O NA
               0
                                                      NA
         NA
                             NA
                                  NA NA
                                          NΑ
#> 2
     1
         NA
               1
                   NA (obs)
                             NA
                                  NA NA
                                          NA
                                                O NA
                                                      NA
#> 3 1
        NA
               2
                  NA (obs)
                             NA
                                 NA NA
                                          NA
                                                O NA
                                                      NA
         NA
               3
                   NA (obs)
                             NA
                                  NA NA
                                          NA
                                                O NA
                                                      NA
                                                O NA
#> 5 1 NA
               4
                   NA (obs)
                                  NA NA
                                                      NA
                             NA
                                          NA
#> 6 1 NA
               5
                   NA (obs)
                            NA
                                  NA NA
                                          NA
                                                O NA
                                                      NA
```

You may notice that these are similar to NONMEM event tables; If you are more familiar with NONMEM data and events you could use them directly with the event table function et

```
ev <- et(amountUnits="mg", timeUnits="hours") %>%
  et(amt=10000, addl=9,ii=12,cmt="depot") %>%
  et(time=120, amt=2000, addl=4, ii=14, cmt="depot") %>%
  et(0:240) # Add sampling
```

You can see from the above code, you can dose to the compartment named in the RxODE model. This slight deviation from NONMEM can reduce the need for compartment renumbering.

These events can also be combined and expanded (to multi-subject events and complex regimens) with rbind, c, seq, and rep. For more information about creating complex dosing regimens using RxODE see the RxODE events vignette.

4.3 Solving ODEs

The ODE can now be solved by calling the model object's run or solve function. Simulation results for all variables in the model are stored in the output matrix **x**

```
x <- mod1$solve(theta, ev, inits);
knitr::kable(head(x))
```

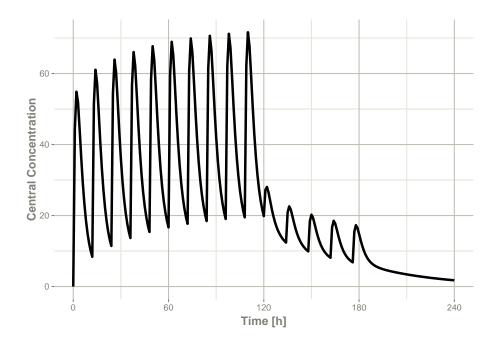
time	C2	C3	depot	centr	peri	eff
0	0.00000	0.0000000	10000.000	0.000	0.0000	1.000000
1	44.37555	0.9198298	7452.765	1783.897	273.1895	1.084664
2	54.88296	2.6729825	5554.370	2206.295	793.8758	1.180825
3	51.90343	4.4564927	4139.542	2086.518	1323.5783	1.228914
4	44.49738	5.9807076	3085.103	1788.795	1776.2702	1.234610
5	36.48434	7.1774981	2299.255	1466.670	2131.7169	1.214742

You can also solve this and create a RxODE data frame:

```
x <- mod1 %>% rxSolve(theta, ev, inits);
#> _____ Solved RxODE object _____
#> -- Parameters (x$params): ------
#>
      ٧2
            VЗ
                   ΚA
                         CL
                                Q
                                     Kin
                                           Kout
#> 40.200 297.000
                0.294 18.600 10.500 1.000
                                          1.000 200.000
#> -- Initial Conditions (x$inits): ------
#> depot centr peri
                  eff
#>
     0
          0
               0
#> -- First part of data (object): -----
#> # A tibble: 241 x 7
#>
    time
           C2
                СЗ
                  depot centr peri
#>
     [h] <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                  10000
#> 1
       0
         0 0
                          0
                               0
#> 2
         44.4 0.920 7453. 1784.
                             273. 1.08
       1
       2 54.9 2.67
                   5554. 2206. 794. 1.18
#> 4
                   4140. 2087. 1324. 1.23
       3 51.9 4.46
#> 5
       4 44.5 5.98
                   3085. 1789. 1776. 1.23
       5 36.5 7.18
                   2299. 1467. 2132. 1.21
#> # ... with 235 more rows
#> ______
```

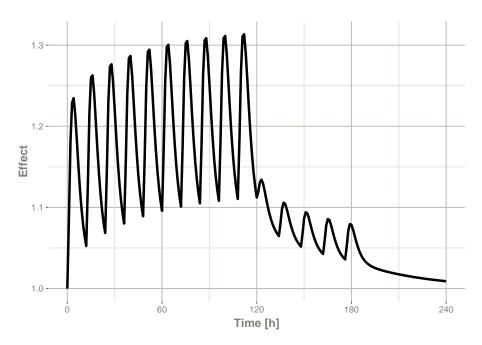
This returns a modified data frame. You can see the compartment values in the plot below:

```
library(ggplot2)
plot(x,C2) + ylab("Central Concentration")
```



Or,

```
plot(x,eff) + ylab("Effect")
```



Note that the labels are automatically labeled with the units from the initial event table. RxODE extracts units to label the plot (if they are present).

RxODE syntax

This briefly describes the syntax used to define models that RxODE will translate into R-callable compiled code. It also describes the communication of variables between R and the RxODE modeling specification.

5.1 Example

5.2 Syntax

An RxODE model specification consists of one or more statements optionally terminated by semi-colons; and optional comments (comments are delimited by # and an end-of-line).

A block of statements is a set of statements delimited by curly braces, { . . . }.

Statements can be either assignments, conditional if/else if/else, while loops (can be exited by break), special statements, or printing statements (for debugging/testing)

Assignment statements can be:

- simple assignments, where the left hand is an identifier (i.e., variable)
- special **time-derivative** assignments, where the left hand specifies the change of the amount in the corresponding state variable (compartment) with respect to time e.g., d/dt(depot):
- special initial-condition assignments where the left hand specifies the compartment of the initial condition being specified, e.g. depot(0) = 0
- special model event changes including bioavailability (f(depot)=1), lag time (alag(depot)=0), modeled rate (rate(depot)=2) and modeled duration (dur(depot)=2). An example of these model features and the event specification for the modeled infusions the RxODE data specification is found in RxODE events vignette.
- special change point syntax, or model times. These model times are specified by mtime(var)=time
- special Jacobian-derivative assignments, where the left hand specifies the change in the compartment ode with respect to a variable. For example, if d/dt(y) = dy, then a Jacobian for this compartment can be specified as df(y)/dy(dy) = 1. There may be some advantage to obtaining the solution or specifying the Jacobian for very stiff ODE systems. However, for the few stiff systems we tried with LSODA, this actually slightly slowed down the solving.

Note that assignment can be done by =, <- or \sim .

When assigning with the ~ operator, the **simple assignments** and **time-derivative** assignments will not be output.

Special statements can be:

• Compartment declaration statements, which can change the default dosing compartment and the assumed compartment number(s) as well as add extra compartment names at the end (useful for multiple-endpoint nlmixr models); These are specified by cmt(compartmentName)

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• Parameter declaration statements, which can make sure the input parameters are in a certain order instead of ordering the parameters by the order they are parsed. This is useful for keeping the parameter order the same when using 2 different ODE models. These are specified by param(par1, par2,...)

An example model is shown below:

```
# simple assignment
C2 = centr/V2;

# time-derivative assignment
d/dt(centr) = F*KA*depot - CL*C2 - Q*C2 + Q*C3;
```

Expressions in assignment and if statements can be numeric or logical, however, no character nor integer expressions are currently supported.

Numeric expressions can include the following numeric operators +, -, *, /, and those mathematical functions defined in the C or the R math libraries (e.g., fabs, exp, log, sin, abs).

You may also access the R's functions in the R math libraries, like lgammafn for the log gamma function.

The RxODE syntax is case-sensitive, i.e., ABC is different than abc, Abc, etc.

5.2.1 Identifiers

Like R, Identifiers (variable names) may consist of one or more alphanumeric, underscore _ or period . characters, but the first character cannot be a digit or underscore _.

Identifiers in a model specification can refer to:

- State variables in the dynamic system (e.g., compartments in a pharmacokinetics model).
- Implied input variable, t (time), tlast (last time point), and podo (oral dose, in the undocumented case of absorption transit models).
- Special constants like pi or R's predefined constants.
- Model parameters (e.g., ka rate of absorption, CL clearance, etc.)
- Others, as created by assignments as part of the model specification; these are referred as *LHS* (left-hand side) variable.

Currently, the RxODE modeling language only recognizes system state variables and "parameters", thus, any values that need to be passed from R to the ODE

model (e.g., age) should be either passed in the params argument of the integrator function rxSolve() or be in the supplied event data-set.

There are certain variable names that are in the RxODE event tables. To avoid confusion, the following event table-related items cannot be assigned, or used as a state but can be accessed in the RxODE code:

- cmt
- dvid
- addl
- SS
- rate
- id

However the following variables are cannot be used in a model specification - evid - ii

Sometimes RxODE generates variables that are fed back to RxODE. Similarly, nlmixr generates some variables that are used in nlmixr estimation and simulation. These variables start with the either the rx or nlmixr prefixes. To avoid any problems, it is suggested to not use these variables starting with either the rx or nlmixr prefixes.

5.3 Logical Operators

Logical operators support the standard R operators ==, != >= <= > and <. Like R these can be in if() or while() statements, ifelse() expressions. Additionally they can be in a standard assignment. For instance, the following is valid:

```
cov1 = covm*(sexf == "female") + covm*(sexf != "female")
```

Notice that you can also use character expressions in comparisons. This convenience comes at a cost since character comparisons are slower than numeric expressions. Unlike R, as.numeric or as.integer for these logical statements is not only not needed, but will cause an syntax error if you try to use the function.

5.4 cmt() changing compartment numbers for states

The compartment order can be changed with the cmt() syntax in the model. To understand what the cmt() can do you need to understand how RxODE numbers the compartments.

Below is an example of how RxODE numbers compartments

5.4.1 How RxODE numbers compartments

RxODE automatically assigns compartment numbers when parsing. For example, with the Mavoglurant PBPK model the following model may be used:

```
library(RxODE)
pbpk <- RxODE({</pre>
    KbBR = exp(1KbBR)
   KbMU = exp(1KbMU)
   KbAD = exp(1KbAD)
    CLint= exp(lCLint + eta.LClint)
   KbBO = exp(1KbBO)
   KbRB = exp(1KbRB)
    ## Regional blood flows
    # Cardiac output (L/h) from White et al (1968)
    CO = (187.00*WT^0.81)*60/1000;
    QHT = 4.0 *CO/100;
    QBR = 12.0*C0/100;
    QMU = 17.0*CO/100;
    QAD = 5.0 *CO/100;
    QSK = 5.0 *CO/100;
    QSP = 3.0 *CO/100;
    QPA = 1.0 *CO/100;
    QLI = 25.5*CO/100;
    QST = 1.0 *CO/100;
    QGU = 14.0*CO/100;
    # Hepatic artery blood flow
    QHA = QLI - (QSP + QPA + QST + QGU);
    QBO = 5.0 *CO/100;
    QKI = 19.0*CO/100;
    QRB = CO - (QHT + QBR + QMU + QAD + QSK + QLI + QBO + QKI);
    QLU = QHT + QBR + QMU + QAD + QSK + QLI + QBO + QKI + QRB;
    ## Organs' volumes = organs' weights / organs' density
   VLU = (0.76 *WT/100)/1.051;
   VHT = (0.47 *WT/100)/1.030;
    VBR = (2.00 *WT/100)/1.036;
   VMU = (40.00*WT/100)/1.041;
   VAD = (21.42*WT/100)/0.916;
   VSK = (3.71 *WT/100)/1.116;
   VSP = (0.26 *WT/100)/1.054;
   VPA = (0.14 *WT/100)/1.045;
   VLI = (2.57 *WT/100)/1.040;
   VST = (0.21 *WT/100)/1.050;
   VGU = (1.44 *WT/100)/1.043;
```

```
VBO = (14.29*WT/100)/1.990;
VKI = (0.44 *WT/100)/1.050;
VAB = (2.81 *WT/100)/1.040;
VVB = (5.62 *WT/100)/1.040;
VRB = (3.86 *WT/100)/1.040;
## Fixed parameters
BP = 0.61; # Blood:plasma partition coefficient
fup = 0.028; # Fraction unbound in plasma
fub = fup/BP; # Fraction unbound in blood
KbLU = exp(0.8334);
KbHT = exp(1.1205);
KbSK = exp(-.5238);
KbSP = exp(0.3224);
KbPA = exp(0.3224);
KbLI = exp(1.7604);
KbST = exp(0.3224);
KbGU = \exp(1.2026);
KbKI = exp(1.3171);
S15 = VVB*BP/1000;
C15 = Venous_Blood/S15
d/dt(Lungs) = QLU*(Venous_Blood/VVB - Lungs/KbLU/VLU);
d/dt(Heart) = QHT*(Arterial Blood/VAB - Heart/KbHT/VHT);
d/dt(Brain) = QBR*(Arterial Blood/VAB - Brain/KbBR/VBR);
d/dt(Muscles) = QMU*(Arterial_Blood/VAB - Muscles/KbMU/VMU);
d/dt(Adipose) = QAD*(Arterial Blood/VAB - Adipose/KbAD/VAD);
d/dt(Skin) = QSK*(Arterial_Blood/VAB - Skin/KbSK/VSK);
d/dt(Spleen) = QSP*(Arterial_Blood/VAB - Spleen/KbSP/VSP);
d/dt(Pancreas) = QPA*(Arterial_Blood/VAB - Pancreas/KbPA/VPA);
d/dt(Liver) = QHA*Arterial_Blood/VAB + QSP*Spleen/KbSP/VSP +
  QPA*Pancreas/KbPA/VPA + QST*Stomach/KbST/VST +
  QGU*Gut/KbGU/VGU - CLint*fub*Liver/KbLI/VLI - QLI*Liver/KbLI/VLI;
d/dt(Stomach) = QST*(Arterial_Blood/VAB - Stomach/KbST/VST);
d/dt(Gut) = QGU*(Arterial_Blood/VAB - Gut/KbGU/VGU);
d/dt(Bones) = QBO*(Arterial_Blood/VAB - Bones/KbBO/VBO);
d/dt(Kidneys) = QKI*(Arterial_Blood/VAB - Kidneys/KbKI/VKI);
d/dt(Arterial_Blood) = QLU*(Lungs/KbLU/VLU - Arterial_Blood/VAB);
d/dt(Venous_Blood) = QHT*Heart/KbHT/VHT + QBR*Brain/KbBR/VBR +
  QMU*Muscles/KbMU/VMU + QAD*Adipose/KbAD/VAD + QSK*Skin/KbSK/VSK +
  QLI*Liver/KbLI/VLI + QBO*Bones/KbBO/VBO + QKI*Kidneys/KbKI/VKI +
```

VLU = (0.76 * WT/100)/1.051

#>

```
QRB*Rest_of_Body/KbRB/VRB - QLU*Venous_Blood/VVB;
   d/dt(Rest_of_Body) = QRB*(Arterial_Blood/VAB - Rest_of_Body/KbRB/VRB);
})
If you look at the summary, you can see where RxODE assigned the compart-
ment number(s)
summary(pbpk)
#> RxODE 1.0.0-0 model named rx b16bf3219bce4489d0dc93c431c7a8a0 model (ready).
#> DLL: /home/matt/.cache/R/RxODE/rx_b16bf3219bce4489d0dc93c431c7a8a0__.rxd/rx_b16bf3219bce4489d0
#> NULL
#>
#> Calculated Variables:
                                "CLint" "KbBO"
#> [1] "KbBR"
                        "KbAD"
                                                         "CO"
                                                                 "QHT"
                                                                         "QBR"
                "KbMU"
                                                 "KbRB"
#> [10] "QMU"
                "QAD"
                        "QSK"
                                "QSP"
                                        "QPA"
                                                 "QLI"
                                                         "QST"
                                                                 "QGU"
                                                                         "QHA"
#> [19] "QBO"
                "QKI"
                                        "VLU"
                                                 "VHT"
                                                         "VBR"
                                                                 "UMU"
                                                                         "VAD"
                        "QRB"
                                "QLU"
#> [28] "VSK"
                "VSP"
                        "VPA"
                                "VLI"
                                        "VST"
                                                 "VGU"
                                                         "VBO"
                                                                 "VKI"
                                                                         "VAB"
                "VRB"
                                                        "KbSP"
#> [37] "VVB"
                                "KbLU"
                                        "KbHT"
                                                 "KbSK"
                                                                 "KbPA" "KbLI"
                        "fub"
#> [46] "KbST" "KbGU" "KbKI" "S15"
                                        "C15"
            _____ RxODE Model Syntax _____
#> RxODE({
#>
       KbBR = exp(1KbBR)
#>
       KbMU = exp(1KbMU)
#>
       KbAD = exp(1KbAD)
#>
       CLint = exp(lCLint + eta.LClint)
#>
       KbBO = exp(1KbBO)
#>
       KbRB = exp(1KbRB)
#>
       CO = (187 * WT^0.81) * 60/1000
#>
       QHT = 4 * CO/100
#>
       QBR = 12 * CO/100
#>
       QMU = 17 * CO/100
#>
       QAD = 5 * CO/100
#>
       QSK = 5 * CO/100
       QSP = 3 * CO/100
#>
#>
       QPA = 1 * CO/100
#>
       QLI = 25.5 * CO/100
#>
       QST = 1 * CO/100
#>
       QGU = 14 * CO/100
#>
       QHA = QLI - (QSP + QPA + QST + QGU)
#>
       QBO = 5 * CO/100
#>
       QKI = 19 * CO/100
#>
       QRB = CO - (QHT + QBR + QMU + QAD + QSK + QLI + QBO + QKI)
#>
       QLU = QHT + QBR + QMU + QAD + QSK + QLI + QBO + QKI + QRB
```

```
#>
       VHT = (0.47 * WT/100)/1.03
       VBR = (2 * WT/100)/1.036
#>
#>
       VMU = (40 * WT/100)/1.041
#>
       VAD = (21.42 * WT/100)/0.916
#>
       VSK = (3.71 * WT/100)/1.116
#>
       VSP = (0.26 * WT/100)/1.054
#>
       VPA = (0.14 * WT/100)/1.045
#>
       VLI = (2.57 * WT/100)/1.04
       VST = (0.21 * WT/100)/1.05
#>
#>
       VGU = (1.44 * WT/100)/1.043
#>
       VBO = (14.29 * WT/100)/1.99
#>
       VKI = (0.44 * WT/100)/1.05
#>
       VAB = (2.81 * WT/100)/1.04
#>
       VVB = (5.62 * WT/100)/1.04
#>
       VRB = (3.86 * WT/100)/1.04
#>
       BP = 0.61
#>
       fup = 0.028
#>
       fub = fup/BP
#>
       KbLU = exp(0.8334)
#>
       KbHT = exp(1.1205)
#>
       KbSK = exp(-0.5238)
#>
       KbSP = exp(0.3224)
#>
       KbPA = exp(0.3224)
#>
       KbLI = exp(1.7604)
#>
       KbST = exp(0.3224)
#>
       KbGU = exp(1.2026)
#>
       KbKI = exp(1.3171)
#>
       S15 = VVB * BP/1000
#>
       C15 = Venous Blood/S15
#>
       d/dt(Lungs) = QLU * (Venous_Blood/VVB - Lungs/KbLU/VLU)
#>
       d/dt(Heart) = QHT * (Arterial_Blood/VAB - Heart/KbHT/VHT)
#>
       d/dt(Brain) = QBR * (Arterial_Blood/VAB - Brain/KbBR/VBR)
#>
       d/dt(Muscles) = QMU * (Arterial_Blood/VAB - Muscles/KbMU/VMU)
#>
       d/dt(Adipose) = QAD * (Arterial_Blood/VAB - Adipose/KbAD/VAD)
#>
       d/dt(Skin) = QSK * (Arterial_Blood/VAB - Skin/KbSK/VSK)
#>
       d/dt(Spleen) = QSP * (Arterial_Blood/VAB - Spleen/KbSP/VSP)
#>
       d/dt(Pancreas) = QPA * (Arterial_Blood/VAB - Pancreas/KbPA/VPA)
#>
       d/dt(Liver) = QHA * Arterial_Blood/VAB + QSP * Spleen/KbSP/VSP +
#>
           QPA * Pancreas/KbPA/VPA + QST * Stomach/KbST/VST + QGU *
           Gut/KbGU/VGU - CLint * fub * Liver/KbLI/VLI - QLI * Liver/KbLI/VLI
#>
#>
       d/dt(Stomach) = QST * (Arterial_Blood/VAB - Stomach/KbST/VST)
#>
       d/dt(Gut) = QGU * (Arterial_Blood/VAB - Gut/KbGU/VGU)
#>
       d/dt(Bones) = QBO * (Arterial_Blood/VAB - Bones/KbBO/VBO)
#>
       d/dt(Kidneys) = QKI * (Arterial_Blood/VAB - Kidneys/KbKI/VKI)
       d/dt(Arterial Blood) = QLU * (Lungs/KbLU/VLU - Arterial Blood/VAB)
#>
#>
       d/dt(Venous_Blood) = QHT * Heart/KbHT/VHT + QBR * Brain/KbBR/VBR +
```

In this case, Venous_Blood is assigned to compartment 15. Figuring this out can be inconvenient and also lead to re-numbering compartment in simulation or estimation datasets. While it is easy and probably clearer to specify the compartment by name, other tools only support compartment numbers. Therefore, having a way to number compartment easily can lead to less data modification between multiple tools.

5.4.2 Changing compartments by pre-declaring with cmt()

To add the compartments to the RxODE model in the order you desire you simply need to pre-declare the compartments with cmt. For example specifying is Venous_Blood and Skin to be the 1st and 2nd compartments, respectively, is simple:

```
pbpk2 <- RxODE({</pre>
  ## Now this is the first compartment, ie cmt=1
  cmt(Venous Blood)
  ## Skin may be a compartment you wish to dose to as well,
  ## so it is now cmt=2
  cmt(Skin)
  KbBR = exp(1KbBR)
  KbMU = exp(1KbMU)
  KbAD = exp(1KbAD)
  CLint= exp(lCLint + eta.LClint)
  KbBO = exp(1KbBO)
  KbRB = exp(1KbRB)
  ## Regional blood flows
  # Cardiac output (L/h) from White et al (1968)m
  CO = (187.00*WT^0.81)*60/1000;
  QHT = 4.0 *CO/100;
  QBR = 12.0*C0/100;
  QMU = 17.0*CO/100;
  QAD = 5.0 *CO/100;
  QSK = 5.0 *CO/100;
```

```
QSP = 3.0 *CO/100;
QPA = 1.0 *CO/100;
QLI = 25.5*CO/100;
QST = 1.0 *CO/100;
QGU = 14.0*CO/100;
QHA = QLI - (QSP + QPA + QST + QGU); # Hepatic artery blood flow
QBO = 5.0 *CO/100;
QKI = 19.0*CO/100;
QRB = CO - (QHT + QBR + QMU + QAD + QSK + QLI + QBO + QKI);
QLU = QHT + QBR + QMU + QAD + QSK + QLI + QBO + QKI + QRB;
## Organs' volumes = organs' weights / organs' density
VLU = (0.76 *WT/100)/1.051;
VHT = (0.47 *WT/100)/1.030;
VBR = (2.00 *WT/100)/1.036;
VMU = (40.00*WT/100)/1.041;
VAD = (21.42*WT/100)/0.916;
VSK = (3.71 *WT/100)/1.116;
VSP = (0.26 *WT/100)/1.054;
VPA = (0.14 *WT/100)/1.045;
VLI = (2.57 *WT/100)/1.040;
VST = (0.21 *WT/100)/1.050;
VGU = (1.44 *WT/100)/1.043;
VBO = (14.29*WT/100)/1.990;
VKI = (0.44 *WT/100)/1.050;
VAB = (2.81 *WT/100)/1.040;
VVB = (5.62 *WT/100)/1.040;
VRB = (3.86 *WT/100)/1.040;
## Fixed parameters
BP = 0.61; # Blood:plasma partition coefficient
fup = 0.028; # Fraction unbound in plasma
fub = fup/BP; # Fraction unbound in blood
KbLU = exp(0.8334);
KbHT = exp(1.1205);
KbSK = exp(-.5238);
KbSP = exp(0.3224);
KbPA = exp(0.3224);
KbLI = exp(1.7604);
KbST = exp(0.3224);
KbGU = \exp(1.2026);
KbKI = exp(1.3171);
```

```
S15 = VVB*BP/1000;
  C15 = Venous_Blood/S15
  d/dt(Lungs) = QLU*(Venous_Blood/VVB - Lungs/KbLU/VLU);
  d/dt(Heart) = QHT*(Arterial_Blood/VAB - Heart/KbHT/VHT);
  d/dt(Brain) = QBR*(Arterial_Blood/VAB - Brain/KbBR/VBR);
  d/dt(Muscles) = QMU*(Arterial_Blood/VAB - Muscles/KbMU/VMU);
  d/dt(Adipose) = QAD*(Arterial_Blood/VAB - Adipose/KbAD/VAD);
  d/dt(Skin) = QSK*(Arterial_Blood/VAB - Skin/KbSK/VSK);
  d/dt(Spleen) = QSP*(Arterial_Blood/VAB - Spleen/KbSP/VSP);
  d/dt(Pancreas) = QPA*(Arterial_Blood/VAB - Pancreas/KbPA/VPA);
  d/dt(Liver) = QHA*Arterial_Blood/VAB + QSP*Spleen/KbSP/VSP +
    QPA*Pancreas/KbPA/VPA + QST*Stomach/KbST/VST + QGU*Gut/KbGU/VGU -
    CLint*fub*Liver/KbLI/VLI - QLI*Liver/KbLI/VLI;
  d/dt(Stomach) = QST*(Arterial_Blood/VAB - Stomach/KbST/VST);
  d/dt(Gut) = QGU*(Arterial_Blood/VAB - Gut/KbGU/VGU);
  d/dt(Bones) = QBO*(Arterial_Blood/VAB - Bones/KbBO/VBO);
  d/dt(Kidneys) = QKI*(Arterial_Blood/VAB - Kidneys/KbKI/VKI);
  d/dt(Arterial_Blood) = QLU*(Lungs/KbLU/VLU - Arterial_Blood/VAB);
  d/dt(Venous_Blood) = QHT*Heart/KbHT/VHT + QBR*Brain/KbBR/VBR +
    QMU*Muscles/KbMU/VMU + QAD*Adipose/KbAD/VAD + QSK*Skin/KbSK/VSK +
    QLI*Liver/KbLI/VLI + QBO*Bones/KbBO/VBO + QKI*Kidneys/KbKI/VKI +
    QRB*Rest_of_Body/KbRB/VRB - QLU*Venous_Blood/VVB;
  d/dt(Rest_of_Body) = QRB*(Arterial_Blood/VAB - Rest_of_Body/KbRB/VRB);
})
```

You can see this change in the simple printout

```
pbpk2
```

```
#> RxODE 1.0.0-0 model named rx_1fda8295091ca6d0012077b24d579018 model (ready).
#> x$state: Venous_Blood, Skin, Lungs, Heart, Brain, Muscles, Adipose, Spleen, Pancreas, Liver, S
#> x$params: 1KbBR, 1KbMU, 1KbAD, 1CLint, eta.LClint, 1KbBO, 1KbRB, WT, BP, fup
#> x$lhs: KbBR, KbMU, KbAD, CLint, KbBO, KbRB, CO, QHT, QBR, QMU, QAD, QSK, QSP, QPA, QLI, QST, Q
```

The first two compartments are Venous_Blood followed by Skin.

5.4.3 Appending compartments to the model with cmt()

You can also append "compartments" to the model. Because of the ODE solving internals, you cannot add fake compartments to the model until after all the differential equations are defined.

For example this is legal:

```
ode.1c.ka <- RxODE({
    C2 = center/V;
    d / dt(depot) = -KA * depot
    d/dt(center) = KA * depot - CL*C2
    cmt(eff);
})
print(ode.1c.ka)
#> RxODE 1.0.0-0 model named rx_673f6105e66276a1ff77b53712cdf722 model (ready).
#> $state: depot, center
#> $stateExtra: eff
#> $params: V, KA, CL
#> $1hs: C2
But compartments defined before all the differential equations is not supported;
So the model below:
ode.1c.ka <- RxODE({
    cmt(eff);
    C2 = center/V;
    d / dt(depot) = -KA * depot
    d/dt(center) = KA * depot - CL*C2
})
will give an error:
Error in rxModelVars_(obj) :
  Evaluation error: Compartment 'eff' needs differential equations defined.
```

RxODE events

In general, RxODE event tables follow NONMEM dataset convention with the exceptions:

- The compartment data item (cmt) can be a string/factor with compartment names
 - You may turn off a compartment with a negative compartment number or "-cmt" where cmt is the compartment name.
 - The compartment data item (cmt) can still be a number, the number of the compartment is defined by the appearance of the compartment name in the model. This can be tedious to count, so you can specify compartment numbers easier by using the cmt(cmtName) at the beginning of the model.
- An additional column, dur can specify the duration of infusions;
 - Bioavailability changes will change the rate of infusion since dur/amt are fixed in the input data.
 - Similarly, when specifying rate/amt for an infusion, the bioavailability will change the infusion duration since rate/amt are fixed in the input data.
- Some infrequent NONMEM columns are not supported: pcmt, call.
- Additional events are supported:
 - evid=5 or replace event; This replaces the value of a compartment with the value specified in the amt column. This is equivalent to deSolve=replace.
 - evid=6 or multiply event; This multiplies the value in the compartment with the value specified by the amt column. This is equivalent to deSolve=multiply.

Here are the legal entries to a data table:

Data		
Item	Meaning	Notes
id	Individual identifier	Can be a integer, factor, character, or numeric
time	Individual time	Numeric for each time.
amt	dose amount	Positive for doses zero/NA for observations
rate	infusion rate	When specified the infusion duration will be dur=amt/rate
		rate = -1, rate modeled; rate = -2, duration modeled
dur	$rac{1}{2}$ infusion $rac{1}{2}$	When specified the infusion rate will be rate = amt/dur
evid	event ID	0=Observation; 1=Dose; 2=Other; 3=Reset; 4=Reset+Dose; 5=Replace; 6=Multiply
cmt	Compartment	Represents compartment #/name for dose/observation
SS	Steady State Flag	0 = non-steady-state; 1=steady state; 2=steady state +prior states
ii	Inter-dose	Time between doses.
	Interval	
addl	# of additional doses	Number of doses like the current dose.

Other notes:

- $\bullet\,$ The evid can be the classic RxODE (described here) or the NONMEM-style evid described above.
- NONMEM's DV is not required; RxODE is a ODE solving framework.
- NONMEM's MDV is not required, since it is captured in EVID.
- \bullet Instead of NONMEM-compatible data, it can accept ${\tt deSolve}$ compatible data-frames.

When returning the RxODE solved data-set there are a few additional event ids (EVID) that you may see depending on the solving options:

- EVID = -1 is when a modeled rate ends (corresponds to rate = -1)
- EVID = -2 is when a modeled duration ends (corresponds to rate=-2)
- EVID = -10 when a rate specified zero-order infusion ends (corresponds to rate > 0)
- EVID = -20 when a duration specified zero-order infusion ends (corresponds to dur > 0)

• EVID = 101, 102, 103,... These correspond to the 1, 2, 3, ... modeled time (mtime).

These can only be accessed when solving with the option combination addDosing=TRUE and subsetNonmem=FALSE. If you want to see the classic EVID equivalents you can use addDosing=NA.

To illustrate the event types we will use the model from the original RxODE tutorial.

```
library(RxODE)
## Model from RxODE tutorial
m1 <-RxODE({
    KA=2.94E-01;
    CL=1.86E+01;
    V2=4.02E+01;
    Q=1.05E+01;
    V3=2.97E+02;
    Kin=1;
    Kout=1;
    EC50=200;
    ## Added modeled bioavaiblity, duration and rate
    fdepot = 1;
    durDepot = 8;
    rateDepot = 1250;
    C2 = centr/V2;
    C3 = peri/V3;
    d/dt(depot) =-KA*depot;
    f(depot) = fdepot
    dur(depot) = durDepot
    rate(depot) = rateDepot
    d/dt(centr) = KA*depot - CL*C2 - Q*C2 + Q*C3;
    d/dt(peri) =
                                      Q*C2 - Q*C3;
    d/dt(eff) = Kin - Kout*(1-C2/(EC50+C2))*eff;
    eff(0) = 1
});
```

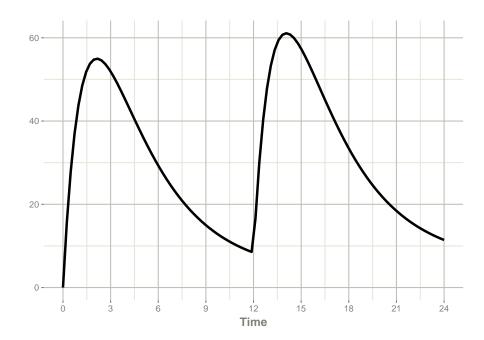
6.1 Bolus/Additive Doses

A bolus dose is the default type of dose in RxODE and only requires the amt/dose. Note that this uses the convenience function et() described in the RxODE event tables

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12,until=24) %>%
    et(seq(0, 24, length.out=100))
```

```
#> ------ EventTable with 101 records -----
#>
#>
     1 dosing records (see x$get.dosing(); add with add.dosing or et)
     100 observation times (see x$get.sampling(); add with add.sampling or et)
#>
     multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: ------
#> # A tibble: 101 x 5
#>
         time
               \mathtt{amt}
                    ii addl evid
          [h] <dbl>
                    [h] <int> <evid>
#>
                         NA 0:Observation
#> 1 0.0000000
                   NA
                   12
                          2 1:Dose (Add)
#> 2 0.0000000 10000
#> 3 0.2424242 NA NA NA 0:Observation
#> 4 0.4848485 NA NA NA 0:Observation
#> 5 0.7272727 NA NA NA 0:Observation
#> 6 0.9696970 NA NA NA 0:Observation
#> 7 1.2121212 NA NA NA 0:Observation
#> 8 1.4545455 NA NA NA 0:Observation
#> 9 1.6969697
                   NA NA 0:Observation
               NA
#> 10 1.9393939
              NA
                     NA NA 0:Observation
#> # ... with 91 more rows
```

```
rxSolve(m1, ev) %>% plot(C2) +
    xlab("Time")
```



6.2 Infusion Doses

There are a few different type of infusions that RxODE supports:

- Constant Rate Infusion (rate)
- Constant Duration Infusion (dur)
- Estimated Rate of Infusion
- Estimated Duration of Infusion

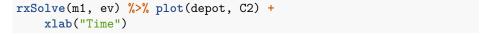
6.2.1 Constant Infusions (in terms of duration and rate)

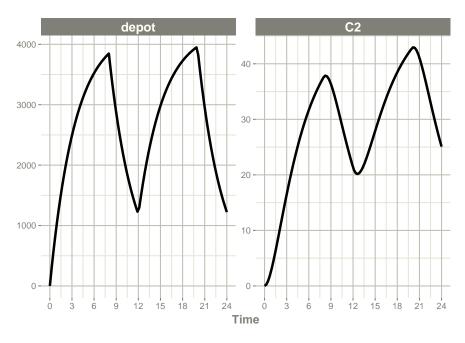
The next type of event is an infusion; There are two ways to specify an infusion; The first is the dur keyword.

An example of this is:

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12,until=24, dur=8) %>%
    et(seq(0, 24, length.out=100))
ev
```

```
----- EventTable with 101 records ------
#>
#>
     1 dosing records (see x$get.dosing(); add with add.dosing or et)
     100 observation times (see x$get.sampling(); add with add.sampling or et)
#>
     multiple doses in 'addl' columns, expand with x=expand(); or etExpand(x)
#>
  -- First part of x: -----
  # A tibble: 101 x 6
#>
          time
                 amt
                        ii addl evid
                                                dur
           [h] <dbl>
                       [h] <int> <evid>
                                                [h]
#>
   1 0.0000000
#>
                       NA
                             NA 0:Observation
                                                 NA
   2 0.0000000 10000
                             2 1:Dose (Add)
                                                 8
   3 0.2424242
                        NA
                             NA 0:Observation
                                                 NA
   4 0.4848485
                       NA
                             NA 0:Observation
                                                 NA
   5 0.7272727
                             NA 0:Observation
                                                 NA
                  NA
                       NA
   6 0.9696970
                  NA
                             NA 0:Observation
                                                 NA
   7 1.2121212
                             NA 0:Observation
                  NA
                       NA
                                                 NA
   8 1.4545455
                  NA
                        NA
                             NA 0:Observation
                                                 NA
   9 1.6969697
                  NA
                        NA
                             NA 0:Observation
                                                 NA
#> 10 1.9393939
                             NA 0:Observation
                                                 NA
                  NA
                        NA
#> # ... with 91 more rows
```



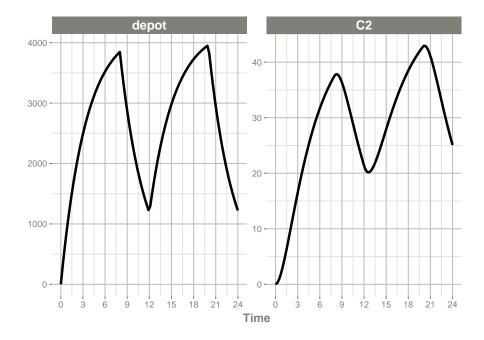


It can be also specified by the rate component:

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12,until=24, rate=10000/8) %>%
    et(seq(0, 24, length.out=100))
```

```
#> ----- EventTable with 101 records -----
#>
#>
     1 dosing records (see x$get.dosing(); add with add.dosing or et)
     100 observation times (see x$get.sampling(); add with add.sampling or et)
     multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: ------
#> # A tibble: 101 x 6
#>
         time amt rate
                             ii addl evid
          [h] <dbl> <rate/dur> [h] <int> <evid>
#>
#> 1 0.0000000 NA NA
                             NA
                                 NA 0:Observation
#> 2 0.0000000 10000 1250
                             12
                                   2 1:Dose (Add)
#> 3 0.2424242 NA NA
                             NA NA 0:Observation
#> 4 0.4848485 NA NA
                             NA NA 0:Observation
#> 5 0.7272727 NA NA
                            NA NA 0:Observation
                            NA NA 0:Observation
#> 6 0.9696970 NA NA
#> 7 1.2121212 NA NA
                            NA NA 0:Observation
#> 8 1.4545455 NA NA
                            NA NA 0:Observation
#> 9 1.6969697
                             NA NA 0:Observation
               NA NA
#> 10 1.9393939
              NA NA
                             NA NA 0:Observation
#> # ... with 91 more rows
```

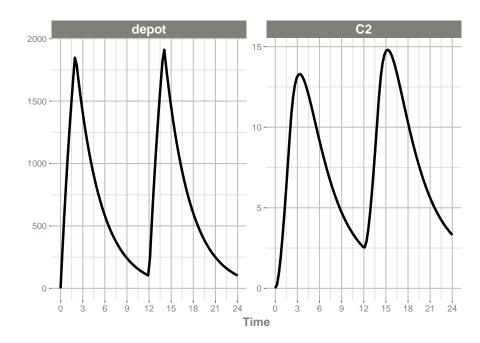
```
rxSolve(m1, ev) %>% plot(depot, C2) +
    xlab("Time")
```



These are the same with the exception of how bioavailability changes the infusion.

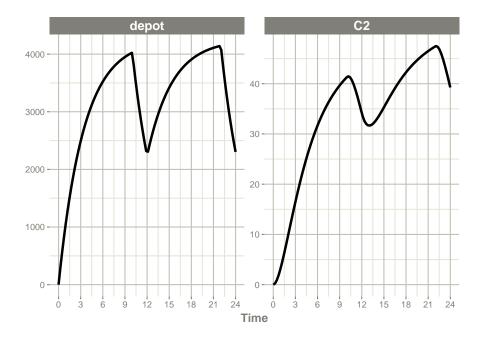
In the case of modeling rate, a bioavailability decrease, decreases the infusion duration, as in NONMEM. For example:

```
rxSolve(m1, ev, c(fdepot=0.25)) %>% plot(depot, C2) +
    xlab("Time")
```



Similarly increasing the bioavailability increases the infusion duration.

```
rxSolve(m1, ev, c(fdepot=1.25)) %>% plot(depot, C2) +
    xlab("Time")
```

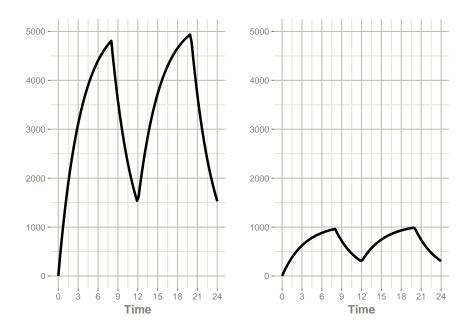


The rationale for this behavior is that the rate and amt are specified by the event table, so the only thing that can change with a bioavailability increase is the duration of the infusion.

If you specify the amt and dur components in the event table, bioavailability changes affect the rate of infusion.

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12,until=24, dur=8) %>%
    et(seq(0, 24, length.out=100))
```

You can see the side-by-side comparison of bioavailability changes affecting rate instead of duration with these records in the following plots:



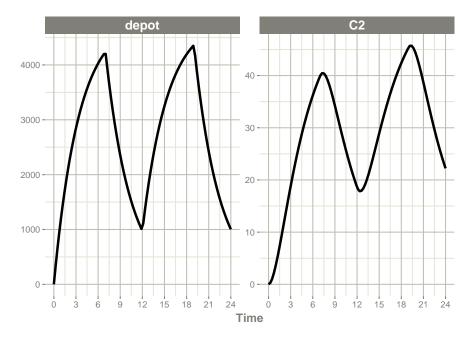
6.2.2 Modeled Rate and Duration of Infusion

You can model the duration, which is equivalent to NONMEM's rate=-2. As a mnemonic you can use the dur=model instead of rate=-2

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12,until=24, dur=model) %>%
    et(seq(0, 24, length.out=100))
ev
```

```
#> ----- EventTable with 101 records -----
#>
#>
     1 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
     100 observation times (see x$get.sampling(); add with add.sampling or et)
     multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: -----
#> # A tibble: 101 x 6
                              ii addl evid
#>
         time amt rate
          [h] <dbl> <rate/dur> [h] <int> <evid>
#>
#> 1 0.0000000
                             NA NA 0:Observation
              NA NA
#> 2 0.0000000 10000 -2:dur
                             12
                                     2 1:Dose (Add)
                              NA
#> 3 0.2424242 NA NA
                                     NA 0:Observation
#> 4 0.4848485 NA NA
                              NA NA 0:Observation
                             NA NA 0:Observation
#> 5 0.7272727 NA NA
                             NA NA 0:Observation
NA NA 0:Observation
NA NA 0:Observation
#> 6 0.9696970 NA NA
#> 7 1.2121212 NA NA
#> 8 1.4545455 NA NA
#> 9 1.6969697 NA NA
                               NA NA 0:Observation
#> 10 1.9393939
              NA NA
                               NA NA 0:Observation
#> # ... with 91 more rows
```

```
rxSolve(m1, ev, c(durDepot=7)) %>% plot(depot, C2) +
    xlab("Time")
```

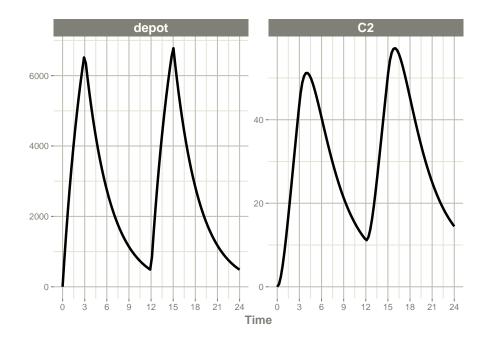


Similarly, you may also model rate. This is equivalent to NONMEM's rate=-1 and is how RxODE's event table specifies the data item as well. You can also use rate=model as a mnemonic:

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12,until=24, rate=model) %>%
    et(seq(0, 24, length.out=100))
ev
            ----- EventTable with 101 records ------
#>
#>
      1 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
      100 observation times (see x$get.sampling(); add with add.sampling or et)
      multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: --
#> # A tibble: 101 x 6
#>
                 amt rate
          time
                                    ii addl evid
#>
            [h] <dbl> <rate/dur>
                                   [h] <int> <evid>
   1 0.0000000
                   NA NA
                                   NA
                                          NA 0:Observation
#>
   2 0.0000000 10000 -1:rate
                                           2 1:Dose (Add)
#>
                                    12
   3 0.2424242
                   NA NA
                                    NA
                                          NA 0:Observation
   4 0.4848485
                  NA NA
                                    NA
                                          NA 0:Observation
  5 0.7272727
                   NA NA
                                    NA
                                          NA 0:Observation
#> 6 0.9696970
                  NA NA
                                    NA
                                          NA 0:Observation
```

```
#>
   7 1.2121212
                   NA NA
                                     NA
                                           NA 0:Observation
#>
   8 1.4545455
                   NA NA
                                     NA
                                           NA 0:Observation
#> 9 1.6969697
                   NA NA
                                           NA 0:Observation
                                     NA
#> 10 1.9393939
                   NA NA
                                     NA
                                           NA 0:Observation
#> # ... with 91 more rows
```

```
rxSolve(m1, ev, c(rateDepot=10000/3)) %>% plot(depot, C2) +
    xlab("Time")
```

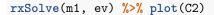


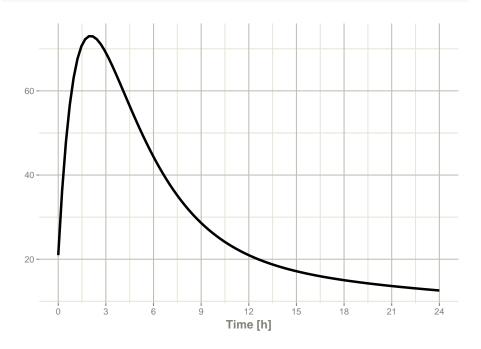
6.3 Steady State

#>

These doses are solved until a steady state is reached with a constant inter-dose interval.

```
#>
      1 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
      100 observation times (see x$get.sampling(); add with add.sampling or et)
#> -- First part of x: -----
  # A tibble: 101 x 5
#>
#>
           time
                  amt
                         ii evid
                                             SS
#>
            [h] <dbl>
                        [h] <evid>
                                          <int>
#>
   1 0.0000000
                         NA 0:Observation
                                             NA
   2 0.0000000 10000
#>
                         12 1:Dose (Add)
                                              1
   3 0.2424242
                         NA 0:Observation
#>
                   NA
                                             NA
#>
   4 0.4848485
                   NA
                         NA 0:Observation
                                             NA
   5 0.7272727
                         NA 0:Observation
                                             NA
   6 0.9696970
                   NA
                         NA 0:Observation
                                             NA
   7 1.2121212
                   NA
                         NA 0:Observation
                                             NA
   8 1.4545455
                         NA 0:Observation
                                             NA
                   NA
   9 1.6969697
                   NA
                         NA 0:Observation
                                             NA
                         NA 0:Observation
#> 10 1.9393939
                   NA
                                             NA
#> # ... with 91 more rows
```





6.3.1 Steady state for complex dosing

By using the ss=2 flag, you can use the super-positioning principle in linear kinetics to get steady state nonstandard dosing (i.e. morning 100 mg vs evening

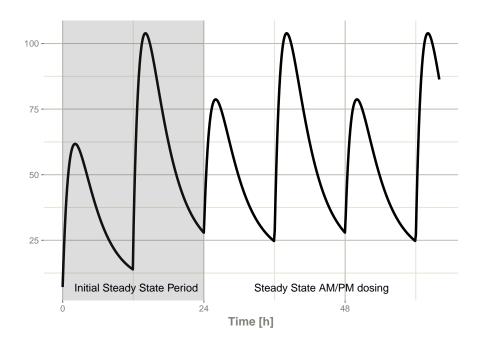
150 mg). This is done by:

- Saving all the state values
- Resetting all the states and solving the system to steady state
- Adding back all the prior state values

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=24, ss=1) %>%
    et(time=12, amt=15000, ii=24, ss=2) %>%
    et(time=24, amt=10000, ii=24, addl=3) %>%
    et(time=36, amt=15000, ii=24, addl=3) %>%
    et(seq(0, 64, length.out=500))

library(ggplot2)

rxSolve(m1, ev,maxsteps=10000) %>% plot(C2) +
    annotate("rect", xmin=0, xmax=24, ymin=-Inf, ymax=Inf, alpha=0.2) +
    annotate("text", x=12.5, y=7, label="Initial Steady State Period") +
    annotate("text", x=44, y=7, label="Steady State AM/PM dosing")
```



You can see that it takes a full dose cycle to reach the true complex steady state dosing.

6.3.2 Steady state for constant infusion or zero order processes

The last type of steady state that RxODE supports is steady-state constant infusion rate. This can be specified the same way as NONMEM, that is:

- No inter-dose interval ii=0
- A steady state dose, ie ss=1
- Either a positive rate (rate>0) or a estimated rate rate=-1.
- A zero dose, ie amt=0
- Once the steady-state constant infusion is achieved, the infusion is turned off when using this record, just like NONMEM.

Note that rate=-2 where we model the duration of infusion doesn't make much sense since we are solving the infusion until steady state. The duration is specified by the steady state solution.

Also note that bioavailability changes on this steady state infusion also do not make sense because they neither change the rate or the duration of the steady state infusion. Hence modeled bioavailability on this type of dosing event is ignored.

Here is an example:

```
ev <- et(timeUnits="hr") %>%
    et(amt=0, ss=1,rate=10000/8)

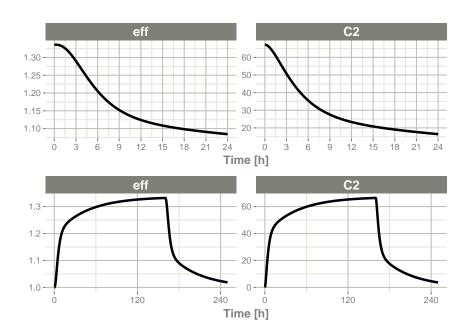
p1 <- rxSolve(m1, ev) %>% plot(C2, eff)

ev <- et(timeUnits="hr") %>%
    et(amt=200000, rate=10000/8) %>%
    et(0, 250, length.out=1000)

p2 <- rxSolve(m1, ev) %>% plot(C2, eff)

library(patchwork)

p1 / p2
```



Not only can this be used for PK, it can be used for steady-state disease processes.

6.4 Reset Events

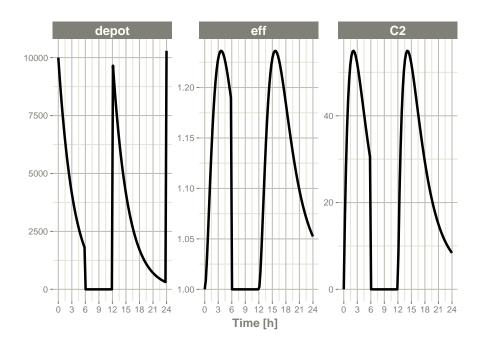
Reset events are implemented by evid=3 or evid=reset, for reset and evid=4 for reset and dose.

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12, addl=3) %>%
    et(time=6, evid=reset) %>%
    et(seq(0, 24, length.out=100))
```

```
#>
             [h] <dbl>
                         [h] <int> <evid>
#>
    1 0.0000000
                    NA
                          NA
                                 NA 0:Observation
    2 0.0000000 10000
                          12
                                 3 1:Dose (Add)
    3 0.2424242
                                 NA 0:Observation
#>
                    NA
                          NA
    4 0.4848485
#>
                    NA
                          NA
                                NA 0:Observation
                    NA
    5 0.7272727
                          NA
                                NA 0:Observation
#>
    6 0.9696970
                    NA
                          NA
                                NA 0:Observation
#>
    7 1.2121212
                    NA
                          NA
                                NA 0:Observation
    8 1.4545455
                                NA 0:Observation
#>
                    NA
                          NA
    9 1.6969697
#>
                    NA
                          NA
                                NA 0:Observation
#> 10 1.9393939
                    NA
                          NA
                                 NA 0:Observation
#> # ... with 92 more rows
```

The solving show what happens in this system when the system is reset at 6 hours post-dose.

```
rxSolve(m1, ev) %>% plot(depot,C2, eff)
```



You can see all the compartments are reset to their initial values. The next dose start the dosing cycle over.

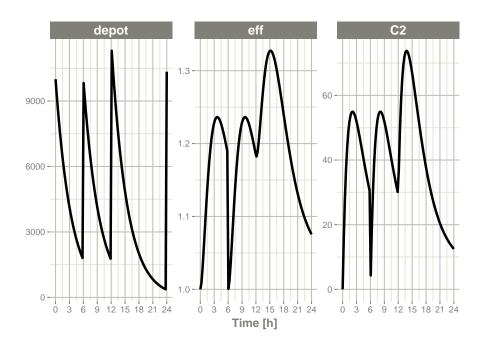
```
ev <- et(timeUnits="hr") %>%
  et(amt=10000, ii=12, addl=3) %>%
  et(time=6, amt=10000, evid=4) %>%
```

```
et(seq(0, 24, length.out=100))
ev
```

```
#> ----- EventTable with 102 records -----
#>
     2 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
#>
     100 observation times (see x$get.sampling(); add with add.sampling or et)
     multiple doses in 'add1' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: ------
#> # A tibble: 102 x 5
#>
         time
               amt
                     ii addl evid
#>
          [h] <dbl>
                     [h] <int> <evid>
  1 0.0000000
#>
              NA
                     NA
                         NA 0:Observation
   2 0.0000000 10000
                           3 1:Dose (Add)
#>
                     12
#> 3 0.2424242
             NA NA NA 0:Observation
#> 4 0.4848485
              NA NA NA 0:Observation
#> 5 0.7272727 NA NA NA 0:Observation
#>
   6 0.9696970
              NA NA NA 0:Observation
#> 7 1.2121212 NA NA NA 0:Observation
#> 8 1.4545455 NA
                     NA NA 0:Observation
#> 9 1.6969697
                NA
                     NA
                        NA 0:Observation
#> 10 1.9393939
                NA
                     NA
                          NA 0:Observation
#> # ... with 92 more rows
```

In this case, the whole system is reset and the dose is given

```
rxSolve(m1, ev) %>% plot(depot,C2, eff)
```



6.5 Turning off compartments

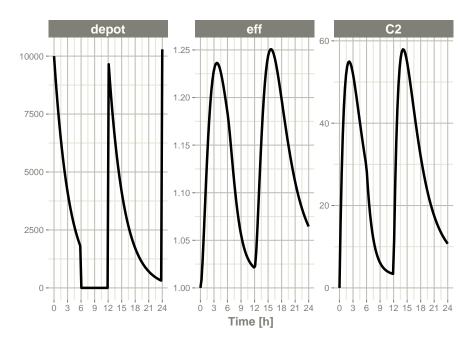
You may also turn off a compartment, which is similar to a reset event.

```
ev <- et(timeUnits="hr") %>%
   et(amt=10000, ii=12, addl=3) %>%
   et(time=6, cmt="-depot", evid=2) %>%
   et(seq(0, 24, length.out=100))
ev
      ----- EventTable with 102 records -----
     2 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
     100 observation times (see x$get.sampling(); add with add.sampling or et)
     multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: -----
#> # A tibble: 102 x 6
                              ii addl evid
#>
         time cmt
                       amt
                      <dbl>
                              [h] <int> <evid>
#>
          [h] <chr>
#> 1 0.0000000 (obs) NA NA
                                  NA 0:Observation
#> 2 0.0000000 (default) 10000 12 3 1:Dose (Add)
#> 3 0.2424242 (obs) NA NA 0:Observation
```

```
#>
    4 0.4848485 (obs)
                              NA
                                     NA
                                           NA 0:Observation
    5 0.7272727 (obs)
                              NA
                                     NA
                                           NA 0:Observation
#>
    6 0.9696970 (obs)
                              NA
                                     NA
                                           NA 0:Observation
                                           NA 0:Observation
#>
    7 1.2121212 (obs)
                              NA
                                     NA
#>
   8 1.4545455 (obs)
                              NA
                                    NA
                                           NA 0:Observation
   9 1.6969697 (obs)
                              NA
                                     NA
                                           NA 0:Observation
#> 10 1.9393939 (obs)
                                     NA
                                           NA 0:Observation
                              NA
#> # ... with 92 more rows
```

Solving shows what this does in the system:

```
rxSolve(m1, ev) %>% plot(depot,C2, eff)
```

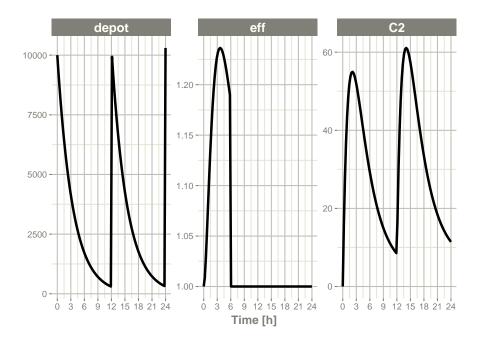


In this case, the depot is turned off, and the depot compartment concentrations are set to the initial values but the other compartment concentrations/levels are not reset. When another dose to the depot is administered the depot compartment is turned back on.

Note that a dose to a compartment only turns back on the compartment that was dosed. Hence if you turn off the effect compartment, it continues to be off after another dose to the depot.

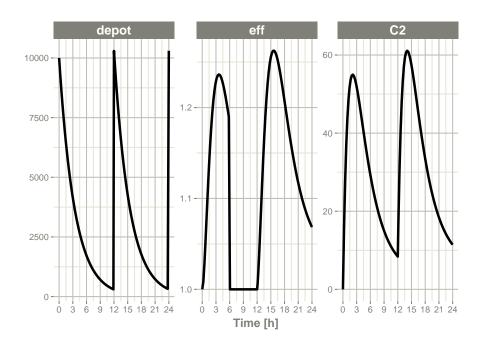
```
ev <- et(timeUnits="hr") %>%
  et(amt=10000, ii=12, addl=3) %>%
  et(time=6, cmt="-eff", evid=2) %>%
```

```
et(seq(0, 24, length.out=100))
rxSolve(m1, ev) %>% plot(depot,C2, eff)
```



To turn back on the compartment, a zero-dose to the compartment or a evid=2 with the compartment would be needed.

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, ii=12, addl=3) %>%
    et(time=6, cmt="-eff", evid=2) %>%
    et(time=12,cmt="eff",evid=2) %>%
    et(seq(0, 24, length.out=100))
rxSolve(m1, ev) %>% plot(depot,C2, eff)
```



6.6 Classic RxODE events

Originally RxODE supported compound event IDs; RxODE still supports these parameters, but it is often more useful to use the the normal NONMEM dataset standard that is used by many modeling tools like NONMEM, Monolix and nlmixr, described in the RxODE event types article.

Classically, RxODE supported event coding in a single event id evid described in the following table.

100+ cmt	Infusion/Event Flag	<99 Cmt	SS flag & Turning of Compartment
100+ cmt	0 = bolus dose	< 99 cmt	1 = dose
	1 = infusion (rate)		10 = Steady state 1 (equivalent to $SS=1$)
	2 = infusion (dur)		20 = Steady state 2 (equivalent to SS=2)
	6 = turn off		30 = Turn off a compartment
	modeled duration		(equivalent to -CMT $w/EVID=2$)
	7 = turn off		
	modeled rate		
	8 = turn on		
	modeled duration		

100+	Infusion/Event	<99	SS flag & Turning of Compartment
cmt	Flag	Cmt	
	9 = turn on modeled rate 4 = replace event 5 = multiply event		

The classic EVID concatenate the numbers in the above table, so an infusion would to compartment 1 would be 10101 and an infusion to compartment 199 would be 119901.

EVID = 0 (observations), EVID=2 (other type event) and EVID=3 are all supported. Internally an EVID=9 is a non-observation event and makes sure the system is initialized to zero; EVID=9 should not be manually set. EVID 10-99 represents modeled time interventions, similar to NONMEM's MTIME. This along with amount (amt) and time columns specify the events in the ODE system.

For infusions specified with EVIDs > 100 the amt column represents the rate value.

For Infusion flags 1 and 2 +amt turn on the infusion to a specific compartment -amt turn off the infusion to a specific compartment. To specify a dose/duration you place the dosing records at the time the duration starts or stops.

For modeled rate/duration infusion flags the on infusion flag must be followed by an off infusion record.

These number are concatenated together to form a full RxODE event ID, as shown in the following examples:

6.6.1 Bolus Dose Examples

A 100 bolus dose to compartment #1 at time 0

time	evid	amt
0	101	100
0.5	0	0
1	0	0

A 100 bolus dose to compartment #99 at time 0

	amt
9901	100
0	0
0	0
	0

A 100 bolus dose to compartment #199 at time 0

time	evid	amt
0	109901	100
0.5	0	0
1	0	0

6.6.2 Infusion Event Examples

Bolus infusion with rate 50 to compartment 1 for 1.5 hr, (modeled bioavailability changes duration of infusion)

time	evid	amt
0	10101	50
0.5	0	0
1	0	0
1.5	10101	-50

Bolus infusion with rate 50 to compartment 1 for 1.5 hr (modeled bioavailability changes rate of infusion)

$_{\rm time}$	evid	amt
0	20101	50
0.5	0	0
1	0	0
1.5	20101	-50

Modeled rate with amount of 50

time	evid	amt
0	90101	50
0	70101	50
0.5	0	0

57

time	evid	amt
1	0	0

Modeled duration with amount of 50

time	evid	amt
0	80101	50
0	60101	50
0.5	0	0
1	0	0

6.6.3 Steady State for classic RxODE EVID example

Steady state dose to cmt 1

time	evid	amt
0	110	50

Steady State with super-positioning principle for am 50 and pm $100~\mathrm{dose}$

time	evid	amt
0	110	50
12	120	100

6.6.4 Turning off a compartment with classic RxODE $\overline{\text{EVID}}$

Turn off the first compartment at time 12

time	evid	amt
0	110	50
12	130	NA

Event coding in RxODE is encoded in a single event number evid. For compartments under 100, this is coded as:

• This event is 0 for observation events.

- For a specified compartment a bolus dose is defined as:
 - -100*(Compartment Number) + 1
 - The dose is then captured in the amt
- For IV bolus doses the event is defined as:
 - -10000 + 100*(Compartment Number) + 1
 - The infusion rate is captured in the amt column
 - The infusion is turned off by subtracting amt with the same evid at the stop of the infusion.

For compartments greater or equal to 100, the 100s place and above digits are transferred to the 100,000th place digit. For doses to the 99th compartment the evid for a bolus dose would be 9901 and the evid for an infusion would be 19901. For a bolus dose to the 199th compartment the evid for the bolus dose would be 109901. An infusion dosing record for the 199th compartment would be 119901.

Chapter 7

Easily creating RxODE events

An event table in RxODE is a specialized data frame that acts as a container for all of RxODE's events and observation times.

To create an RxODE event table you may use the code eventTable(), et(), or even create your own data frame with the right event information contained in it. This is closely related to the types of events that RxODE supports.

With this event table you can add sampling/observations or doses by piping or direct access.

This is a short table of the two main functions to create dosing

add.dosing()	et()	Description
dose nbr.doses dosing.interval dosing.to rate start.time	amt addl ii cmt rate time dur	Dose/Rate/Duration amount Additional doses or number of doses Dosing Interval Dosing Compartment Infusion rate Dosing start time Infusion Duration

Sampling times can be added with add.sampling(sampling times) or et(sampling times). Dosing intervals and sampling windows are also supported.

For these models, we can illustrate by using the model shared in the RxODE tutorial:

```
## Model from RxODE tutorial
m1 <-RxODE({
   KA=2.94E-01;
    CL=1.86E+01;
   V2=4.02E+01;
    Q=1.05E+01;
    V3=2.97E+02;
    Kin=1;
    Kout=1;
    EC50=200;
    ## Added modeled bioavaiblity, duration and rate
    fdepot = 1;
    durDepot = 8;
    rateDepot = 1250;
    C2 = centr/V2;
    C3 = peri/V3;
    d/dt(depot) =-KA*depot;
    f(depot) = fdepot
    dur(depot) = durDepot
    rate(depot) = rateDepot
    d/dt(centr) = KA*depot - CL*C2 - Q*C2 + Q*C3;
    d/dt(peri) =
                                     Q*C2 - Q*C3;
    d/dt(eff) = Kin - Kout*(1-C2/(EC50+C2))*eff;
    eff(0) = 1
})
```

7.1 Adding doses to the event table

Once created you can add dosing to the event table by the add.dosing(), and et() functions.

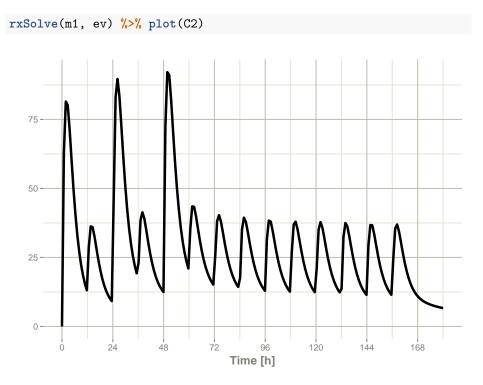
Using the add.dosing() function you have:

argument	meaning
dose nbr.doses dosing.interval dosing.to rate	dose amount Number of doses; Should be at least 1. Dosing interval; By default this is 24. Compartment where dose is administered. Infusion rate
start.time	The start time of the dose

```
ev <- eventTable(amount.units="mg", time.units="hr")</pre>
## The methods ar attached to the event table, so you can use them
## directly
ev$add.dosing(dose=10000, nbr.doses = 3)# loading doses
## Starts at time 0; Default dosing interval is 24
## You can also pipe the event tables to these methods.
ev <- ev %>%
    add.dosing(dose=5000, nbr.doses=14, dosing.interval=12)# maintenance
#> ----- EventTable with 2 records -----
#>
     2 dosing records (see x$get.dosing(); add with add.dosing or et)
     O observation times (see x$get.sampling(); add with add.sampling or et)
     multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: ------
#> # A tibble: 2 x 5
     time
                  ii addl evid
#>
      [h] [mg]
                  [h] <int> <evid>
#> 1
        0 10000
                  24
                         2 1:Dose (Add)
#> 2
                        13 1:Dose (Add)
        0 5000
                  12
```

Notice that the units were specified in the table. When specified, the units use the units package to keep track of the units and convert them if needed. Additionally, ggforce uses them to label the ggplot axes. The set_units and drop_units are useful to set and drop the RxODE event table units.

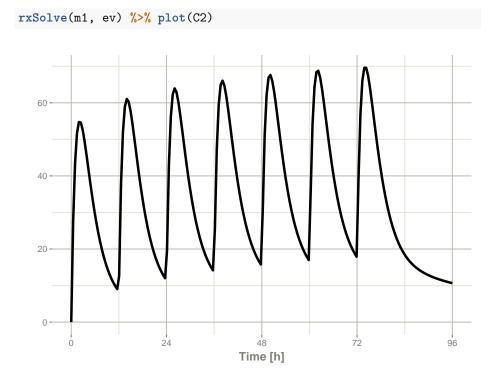
In this example, you can see the time axes is labeled:



If you are more familiar with the NONMEM/RxODE event records, you can also specify dosing using et with the dose elements directly:

```
ev <- et(timeUnits="hr") %>%
   et(amt=10000, until = set_units(3, days), ii=12) # loading doses
  ----- EventTable with 1 records -----
#>
#>
     1 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
     O observation times (see x$get.sampling(); add with add.sampling or et)
     multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#>
#> -- First part of x: ------
#> # A tibble: 1 x 5
#>
     time
                  ii addl evid
            \mathtt{amt}
      [h] <dbl>
                 [h] <int> <evid>
#>
#> 1
        0 10000
                  12
                         6 1:Dose (Add)
```

Which gives:



This shows how easy creating event tables can be.

7.2 Adding sampling to an event table

If you notice in the above examples, RxODE generated some default sampling times since there was not any sampling times. If you wish more control over the sampling time, you should add the samples to the RxODE event table by add.sampling or et

```
ev <- eventTable(amount.units="mg", time.units="hr")

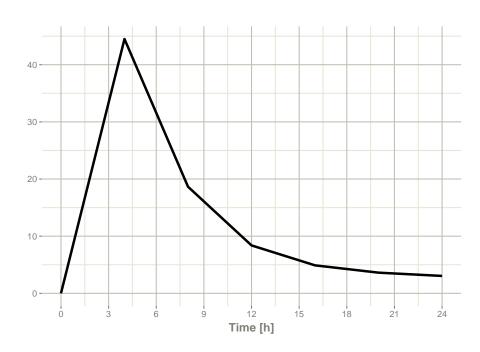
## The methods ar attached to the event table, so you can use them
## directly
ev$add.dosing(dose=10000, nbr.doses = 3)# loading doses
ev$add.sampling(seq(0,24,by=4))</pre>
ev
```

#> ------ EventTable with 8 records ------

```
#>
#>
      1 dosing records (see x$get.dosing(); add with add.dosing or et)
#>
      7 observation times (see x$get.sampling(); add with add.sampling or et)
#>
      multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: -----
#> # A tibble: 8 x 5
#>
      time
             \mathtt{amt}
                    ii addl evid
#>
       [h]
                   [h] <int> <evid>
            [mg]
                          NA 0:Observation
#> 1
        0
              NA
                    NA
#> 2
        0 10000
                           2 1:Dose (Add)
                    24
#> 3
        4
              NA
                    NA
                          NA 0:Observation
#> 4
        8
              NA
                    NA
                          NA 0:Observation
#> 5
                          NA 0:Observation
        12
              NA
                    NA
                          NA 0:Observation
#> 6
       16
              NA
                    NA
#> 7
                          NA 0:Observation
        20
              NA
                    NA
#> 8
        24
              NA
                    NA
                          NA 0:Observation
```

Which gives:

solve(m1, ev) %>% plot(C2)



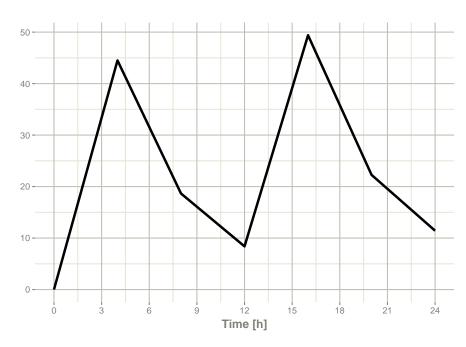
Or if you use et you can simply add them in a similar way to add.sampling:

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, until = set_units(3, days), ii=12) %>% # loading doses
    et(seq(0,24,by=4))
ev
```

```
#> ----- EventTable with 8 records -----
#>
#>
    1 dosing records (see x$get.dosing(); add with add.dosing or et)
    7 observation times (see x$get.sampling(); add with add.sampling or et)
    multiple doses in 'addl' columns, expand with x$expand(); or etExpand(x)
#> -- First part of x: -----
#> # A tibble: 8 x 5
    time amt ii addl evid
#>
     [h] <dbl>
               [h] <int> <evid>
#>
#> 1
     0
          NA NA NA 0:Observation
#> 2
     0 10000 12 6 1:Dose (Add)
#> 3
      4 NA NA NA O:Observation
         NA NA NA O:Observation
#> 4
      8
#> 5
    12 NA NA NA 0:Observation
#> 6 16 NA NA NA 0:Observation
#> 7 20 NA NA NA 0:Observation
      24 NA NA NA 0:Observation
#> 8
```

which gives the following RxODE solve:

```
solve(m1, ev) %>% plot(C2)
```



Note the jagged nature of these plots since there was only a few sample times.

7.3 Expand the event table to a multi-subject event table.

The only thing that is needed to expand an event table is a list of IDs that you want to expand;

```
ev <- et(timeUnits="hr") %>%
    et(amt=10000, until = set_units(3, days), ii=12) %>% # loading doses
    et(seq(0,48,length.out=200)) %>%
    et(id=1:4)
```

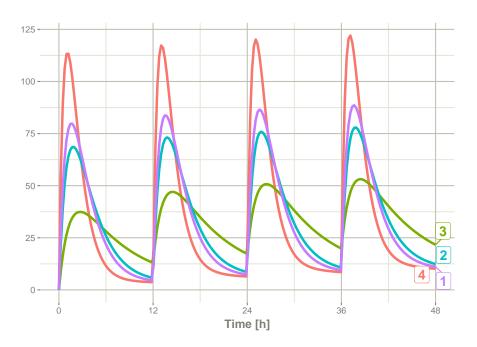
7.3. EXPAND THE EVENT TABLE TO A MULTI-SUBJECT EVENT TABLE.67

```
#>
      <int>
                  [h] <dbl>
                              [h] <int> <evid>
#>
   1
          1 0.0000000
                         NA
                               NA
                                     NA 0:Observation
          1 0.0000000 10000
                               12
                                      6 1:Dose (Add)
   3
          1 0.2412060
                                     NA 0:Observation
                         NA
                               NA
          1 0.4824121
                                     NA 0:Observation
#>
                         NA
                               NA
   5
         1 0.7236181
                         NA
                               NA
                                     NA 0:Observation
#>
  6
         1 0.9648241
                         NA
                               NA
                                     NA 0:Observation
         1 1.2060302
                                     NA 0:Observation
#>
                        NA
                               NA
  8
          1 1.4472362
                                     NA 0:Observation
#>
                         NA
                               NA
#> 9
          1 1.6884422
                         NA
                               NA
                                     NA 0:Observation
#> 10
          1 1.9296482
                                     NA 0:Observation
#> # ... with 794 more rows
```

You can see in the following simulation there are 4 individuals that are solved for:

```
set.seed(42)
solve(m1, ev,
    params=data.frame(KA=0.294*exp(rnorm(4)), 18.6*exp(rnorm(4)))) %>%
    plot(C2)
```

- #> Warning: 'ID' missing in 'parameters' dataset
- #> individual parameters are assumed to have the same order as the event dataset



7.4 Add doses and samples within a sampling window

In addition to adding fixed doses and fixed sampling times, you can have windows where you sample and draw doses from. For dosing windows you specify the time as an ordered numerical vector with the lowest dosing time and the highest dosing time inside a list.

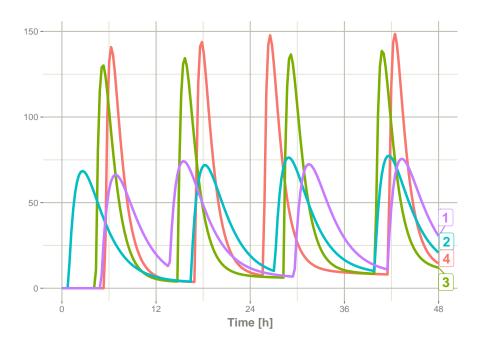
In this example, you start with a dosing time with a 6 hour dosing window:

```
set.seed(42)
ev <- et(timeUnits="hr") %>%
    et(time=list(c(0,6)), amt=10000, until = set_units(2, days), ii=12) %>% # loading
    et(id=1:4)
#> ----- EventTable with 16 records -----
#>
      4 individuals
#>
      16 dosing records (see x$get.dosing(); add with add.dosing or et)
      O observation times (see x$get.sampling(); add with add.sampling or et)
  -- First part of x: -----
  # A tibble: 16 x 6
#>
         id
              low
                        time high
                                     amt evid
#>
      <int>
              [h]
                         [h]
                               [h] <dbl> <evid>
#>
   1
         1
               0 5.4888363
                                 6 10000 1:Dose (Add)
#>
   2
          1
               12 16.9826858
                                18 10000 1:Dose (Add)
               24 25.7168372
                                30 10000 1:Dose (Add)
#>
   3
          1
               36 41.6224525
                                42 10000 1:Dose (Add)
#>
          1
#>
   5
         2
               0 4.3146735
                                6 10000 1:Dose (Add)
               12 14.7464507
#>
   6
          2
                                18 10000 1:Dose (Add)
#>
   7
          2
               24 28.2303887
                                30 10000 1:Dose (Add)
#>
   8
         2
               36 39.9419537
                                42 10000 1:Dose (Add)
#>
   9
          3
               0 0.8079996
                                 6 10000 1:Dose (Add)
#> 10
         3
               12 16.4195299
                                18 10000 1:Dose (Add)
#> 11
          3
               24 27.1145757
                                30 10000 1:Dose (Add)
#> 12
          3
               36 39.8504731
                                42 10000 1:Dose (Add)
#> 13
               0 4.9826858
                                 6 10000 1:Dose (Add)
                                18 10000 1:Dose (Add)
#> 14
          4
               12 13.7168372
#> 15
          4
               24 29.6224525
                                30 10000 1:Dose (Add)
#> 16
          4
               36 41.4888363
                                42 10000 1:Dose (Add)
```

You can clearly see different dosing times in the following simulation:

```
ev <- ev %>% et(seq(0,48,length.out=200))
solve(m1, ev, params=data.frame(KA=0.294*exp(rnorm(4)), 18.6*exp(rnorm(4)))) %>% plot(C2)
```

- #> Warning: 'ID' missing in 'parameters' dataset
- #> individual parameters are assumed to have the same order as the event dataset

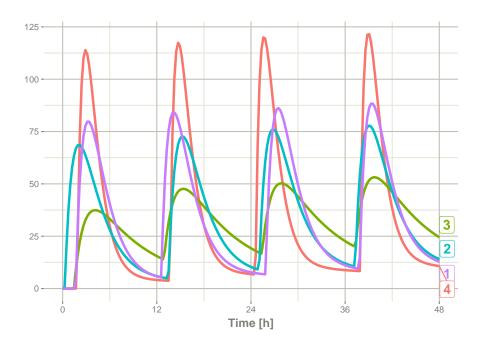


Of course in reality the dosing interval may only be 2 hours:

```
set.seed(42)
ev <- et(timeUnits="hr") %>%
    et(time=list(c(0,2)), amt=10000, until = set_units(2, days), ii=12) %>% # loading doses
    et(id=1:4) %>%
    et(seq(0,48,length.out=200))

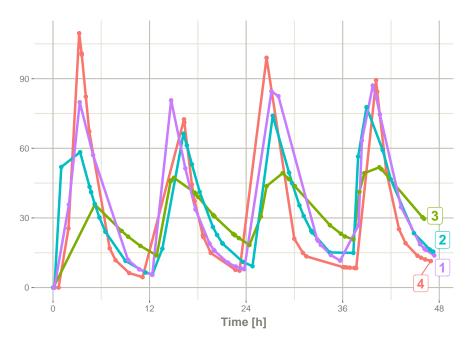
solve(m1, ev, params=data.frame(KA=0.294*exp(rnorm(4)), 18.6*exp(rnorm(4)))) %>% plot(C2)
```

- #> Warning: 'ID' missing in 'parameters' dataset
- #> individual parameters are assumed to have the same order as the event dataset



The same sort of thing can be specified with sampling times. To specify the sampling times in terms of a sampling window, you can create a list of the sampling times. Each sampling time will be a two element ordered numeric vector.

- #> Warning: 'ID' missing in 'parameters' dataset
- #> individual parameters are assumed to have the same order as the event dataset



This shows the flexibility in dosing and sampling that the RxODE event tables allow.

7.5 Combining event tables

Since you can create dosing records and sampling records, you can create any complex dosing regimen you wish. In addition, RxODE allows you to combine event tables by c, seq, rep, and rbind.

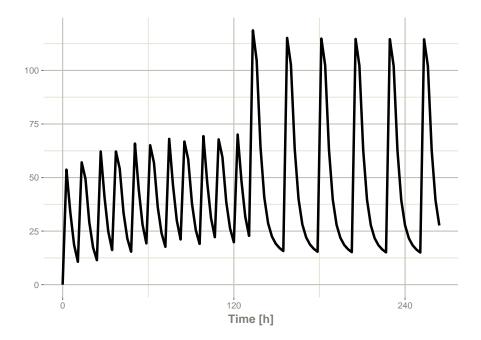
7.6 Sequencing event tables

One way to combine event table is to sequence them by c, seq or etSeq. This takes the two dosing groups and adds at least one inter-dose interval between them:

```
## bid for 5 days
bid <- et(timeUnits="hr") %>%
        et(amt=10000,ii=12,until=set_units(5, "days"))

## qd for 5 days
qd <- et(timeUnits="hr") %>%
        et(amt=20000,ii=24,until=set_units(5, "days"))
```

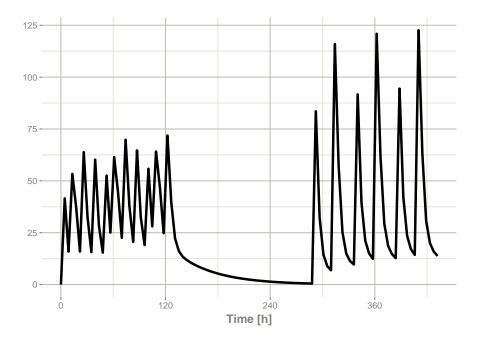
```
## bid for 5 days followed by qd for 5 days
et <- seq(bid,qd) %>% et(seq(0,11*24,length.out=100));
rxSolve(m1, et) %>% plot(C2)
```



When sequencing events, you can also separate this sequence by a period of time; For example if you wanted to separate this by a week, you could easily do that with the following sequence of event tables:

```
## bid for 5 days followed by qd for 5 days
et <- seq(bid,set_units(1, "week"), qd) %>%
    et(seq(0,18*24,length.out=100));

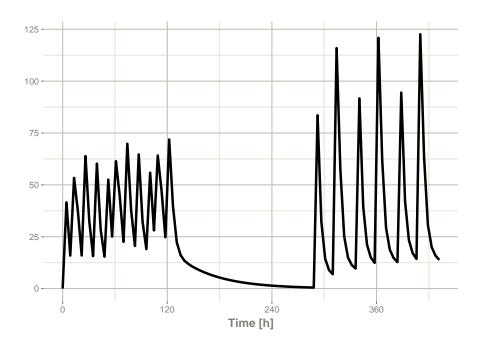
rxSolve(m1, et) %>% plot(C2)
```



Note that in this example the time between the bid and the qd event tables is exactly one week, not 1 week plus 24 hours because of the inter-dose interval. If you want that behavior, you can sequence it using the wait="+ii".

```
## bid for 5 days followed by qd for 5 days
et <- seq(bid,set_units(1, "week"), qd,wait="+ii") %>%
    et(seq(0,18*24,length.out=100));

rxSolve(m1, et) %>% plot(C2)
```

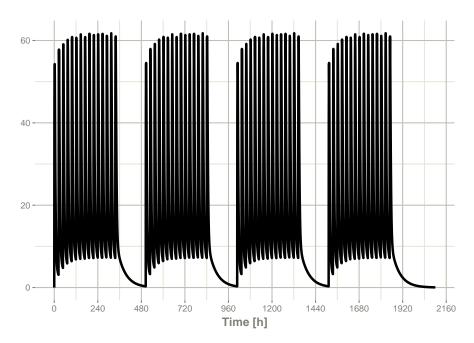


Also note, that RxODE assumes that the dosing is what you want to space the event tables by, and clears out any sampling records when you combine the event tables. If that is not true, you can also use the option samples="use"

7.7 Repeating event tables

You can have an event table that you can repeat with etRep or rep. For example 4 rounds of 2 weeks on QD therapy and 1 week off of therapy can be simply specified:

```
qd <-et(timeUnits = "hr") %>% et(amt=10000, ii=24, until=set_units(2, "weeks"), cmt="defect continuous co
```



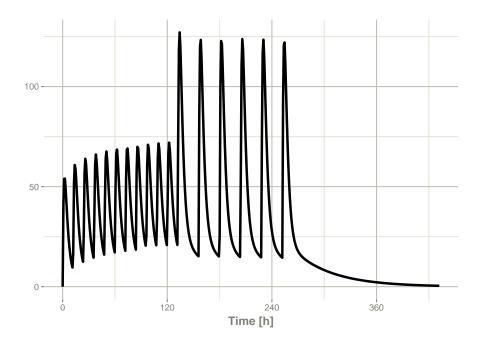
This is a simplified way to use a sequence of event tables. Therefore, many of the same options still apply; That is samples are cleared unless you use samples="use", and the time between event tables is at least the inter-dose interval. You can adjust the timing by the wait option.

7.8 Combining event tables with rbind

You may combine event tables with rbind. This does not consider the event times when combining the event tables, but keeps them the same times. If you space the event tables by a waiting period, it also does not consider the inter-dose interval.

Using the previous seq you can clearly see the difference. Here was the sequence:

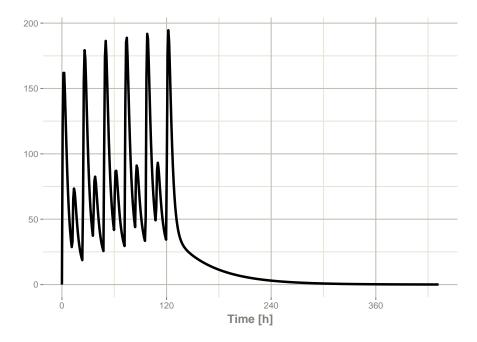
```
rxSolve(m1, et) %>% plot(C2)
```



But if you bind them together with rbind

```
## bid for 5 days
et <- rbind(bid,qd) %>%
    et(seq(0,18*24,length.out=500));

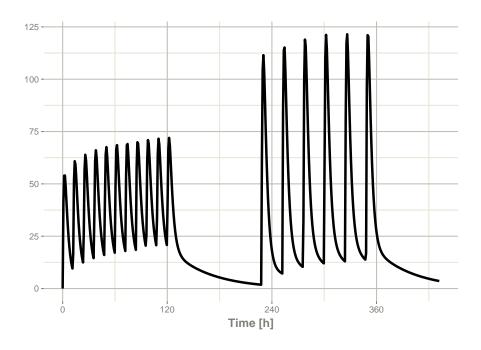
rxSolve(m1, et) %>% plot(C2)
```



Still the waiting period applies (but does not consider the inter-dose interval)

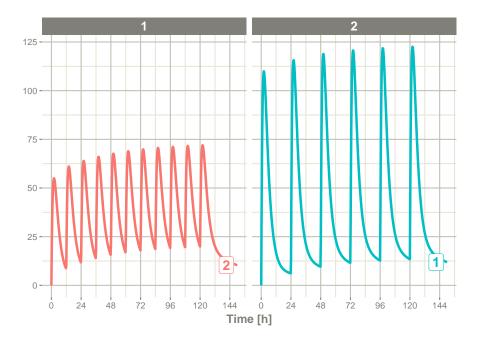
```
et <- rbind(bid,wait=set_units(10,days),qd) %>%
    et(seq(0,18*24,length.out=500));

rxSolve(m1, et) %>% plot(C2)
```



You can also bind the tables together and make each ID in the event table unique; This can be good to combine cohorts with different expected dosing and sampling times. This requires the id="unique" option; Using the first example shows how this is different in this case:

```
## bid for 5 days
et <- etRbind(bid,qd, id="unique") %>%
    et(seq(0,150,length.out=500));
library(ggplot2)
rxSolve(m1, et) %>% plot(C2) + facet_wrap(~ id)
```



Chapter 8

Solving

In general, ODEs are solved using a combination of: - A compiled model specification from RxODE(), specified with object= - Input parameters, specified with params= (and could be blank) - Input data or event table, specified with events= - Initial conditions, specified by inits= (and possibly in the model itself by state(0)=)

The solving options are given in the sections below ## object object is a either a RxODE family of objects, or a file-name with a RxODE model specification, or a string with a RxODE model specification.

8.1 params

params a numeric named vector with values for every parameter in the ODE system; the names must correspond to the parameter identifiers used in the ODE specification;

8.2 events

events an eventTable object describing the input (e.g., doses) to the dynamic system and observation sampling time points (see [eventTable()]);

8.3 inits

inits a vector of initial values of the state variables (e.g., amounts in each compartment), and the order in this vector must be the same as the state variables (e.g., PK/PD compartments);

8.4 iCov

iCov A data frame of individual non-time varying covariates to combine with the params to form a parameter data.frame.

8.5 scale

scale a numeric named vector with scaling for ode parameters of the system. The names must correspond to the parameter identifiers in the ODE specification. Each of the ODE variables will be divided by the scaling factor. For example scale=c(center=2) will divide the center ODE variable by 2.

8.6 method

method The method for solving ODEs. Currently this supports:

- "liblsoda" thread safe Isoda. This supports parallel thread-based solving, and ignores user Jacobian specification.
- "lsoda" LSODA solver. Does not support parallel thread-based solving, but allows user Jacobian specification.
- "indLin" Solving through inductive linearization. The RxODE dll must be setup specially to use this solving routine.

8.7 transitAbs

transitAbs boolean indicating if this is a transit compartment absorption

8.8 atol

atol a numeric absolute tolerance (1e-8 by default) used by the ODE solver to determine if a good solution has been achieved; This is also used in the solved linear model to check if prior doses do not add anything to the solution.

8.9. RTOL 83

8.9 rtol

rtol a numeric relative tolerance (1e-6 by default) used by the ODE solver to determine if a good solution has been achieved. This is also used in the solved linear model to check if prior doses do not add anything to the solution.

8.10 maxsteps

maxsteps maximum number of (internally defined) steps allowed during one call to the solver. (5000 by default)

8.11 hmin

hmin The minimum absolute step size allowed. The default value is 0.

8.12 hmax

hmax The maximum absolute step size allowed. When hmax=NA (default), uses the average difference + hmaxSd*sd in times and sampling events. The hmaxSd is a user specified parameter and which defaults to zero. When hmax=NULL RxODE uses the maximum difference in times in your sampling and events. The value 0 is equivalent to infinite maximum absolute step size.

$8.13 \quad \text{hmaxSd}$

 ${\tt hmaxSd}$ The number of standard deviations of the time difference to add to hmax. The default is 0

8.14 hini

hini The step size to be attempted on the first step. The default value is determined by the solver (when hini = 0)

8.15 maxordn

maxordn The maximum order to be allowed for the nonstiff (Adams) method. The default is 12. It can be between 1 and 12.

8.16 maxords

maxords The maximum order to be allowed for the stiff (BDF) method. The default value is 5. This can be between 1 and 5.

8.17 mxhnil

mxhnil maximum number of messages printed (per problem) warning that T + H = T on a step (H = step size). This must be positive to result in a non-default value. The default value is 0 (or infinite).

8.18 hmxi

hmxi inverse of the maximum absolute value of H to be used. hmxi = 0.0 is allowed and corresponds to an infinite hmax (default). hmin and hmxi may be changed at any time, but will not take effect until the next change of H is considered. This option is only considered with method=liblsoda.

8.19 ...

... Other arguments including scaling factors for each compartment. This includes S#= numeric will scale a compartment # by a dividing the compartment amount by the scale factor, like NONMEM.

8.20 cores

cores Number of cores used in parallel ODE solving. This is equivalent to calling [setRxThreads()]

8.21 covsInterpolation

covsInterpolation specifies the interpolation method for time-varying covariates. When solving ODEs it often samples times outside the sampling time specified in events. When this happens, the time varying covariates are interpolated. Currently this can be:

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• "linear" interpolation, which interpolates the covariate by solving the line between the observed covariates and extrapolating the new covariate value.

- "constant" Last observation carried forward (the default).
- "NOCB" Next Observation Carried Backward. This is the same method that NONMEM uses.
- "midpoint" Last observation carried forward to midpoint; Next observation carried backward to midpoint.

8.22 addCov

addCov A boolean indicating if covariates should be added to the output matrix or data frame. By default this is disabled.

8.23 matrix

matrix A boolean indicating if a matrix should be returned instead of the RxODE's solved object.

8.24 sigma

sigma Named sigma covariance or Cholesky decomposition of a covariance matrix. The names of the columns indicate parameters that are simulated. These are simulated for every observation in the solved system.

8.25 sigmaXform

sigmaXform When taking sigma values from the thetaMat simulations (using the separation strategy for covariance simulation), how should the thetaMat values be turned int standard deviation values:

- identity This is when standard deviation values are directly modeled by the params and thetaMat matrix
- variance This is when the params and thetaMat simulates the variance that are directly modeled by the thetaMat matrix
- log This is when the params and thetaMat simulates log(sd)

- nlmixrSqrt This is when the params and thetaMat simulates the inverse cholesky decomposed matrix with the x^2 modeled along the diagonal. This only works with a diagonal matrix.
- nlmixrLog This is when the params and thetaMat simulates the inverse cholesky decomposed matrix with the exp(x^2) along the diagonal. This only works with a diagonal matrix.
- nlmixrIdentity This is when the params and thetaMat simulates the inverse cholesky decomposed matrix. This only works with a diagonal matrix.

8.26 sigmaDf

sigmaDf Degrees of freedom of the sigma t-distribution. By default it is equivalent to Inf, or a normal distribution.

8.27 nCoresRV

nCoresRV Number of cores used for the simulation of the sigma variables. By default this is 1. To reproduce the results you need to run on the same platform with the same number of cores. This is the reason this is set to be one, regardless of what the number of cores are used in threaded ODE solving.

8.28 sigmaIsChol

sigmalsChol Boolean indicating if the sigma is in the Cholesky decomposition instead of a symmetric covariance

8.29 sigmaSeparation

sigmaSeparation separation strategy for sigma;

Tells the type of separation strategy when simulating covariance with parameter uncertainty with standard deviations modeled in the thetaMat matrix.

"lkj" simulates the correlation matrix from the rLKJ1 matrix with the distribution parameter eta equal to the degrees of freedom nu by (nu-1)/2

"separation" simulates from the identity inverse Wishart covariance matrix with nu degrees of freedom. This is then converted to a covariance matrix and augmented with the modeled standard deviations. While computationally more

complex than the "lkj" prior, it performs better when the covariance matrix size is greater or equal to 10

"auto" chooses "lkj" when the dimension of the matrix is less than 10 and "separation" when greater than equal to 10.

8.30 nDisplayProgress

nDisplayProgress An integer indicating the minimum number of c-based solves before a progress bar is shown. By default this is 10,000.

8.31 amountUnits

amountUnits This supplies the dose units of a data frame supplied instead of an event table. This is for importing the data as an RxODE event table.

8.32 timeUnits

timeUnits This supplies the time units of a data frame supplied instead of an event table. This is for importing the data as an RxODE event table.

8.33 stiff

stiff a logical (TRUE by default) indicating whether the ODE system is stiff or not.

For stiff ODE systems (stiff = TRUE), RxODE uses the LSODA (Livermore Solver for Ordinary Differential Equations) Fortran package, which implements an automatic method switching for stiff and non-stiff problems along the integration interval, authored by Hindmarsh and Petzold (2003).

For non-stiff systems (stiff = FALSE), RxODE uses DOP853, an explicit Runge-Kutta method of order 8(5, 3) of Dormand and Prince as implemented in C by Hairer and Wanner (1993).

8.34 theta

theta A vector of parameters that will be named THETA\[#\] and added to parameters

8.35 eta

eta A vector of parameters that will be named ${\tt ETA\[\#\]}$ and added to parameters

8.36 stateTrim

stateTrim When amounts/concentrations in one of the states are above this value, trim them to be this value. By default Inf. Also trims to -stateTrim for large negative amounts/concentrations. If you want to trim between a range say c(0, 2000000) you may specify 2 values with a lower and upper range to make sure all state values are in the reasonable range.

8.37 updateObject

updateObject This is an internally used flag to update the RxODE solved object (when supplying an RxODE solved object) as well as returning a new object. You probably should not modify it's FALSE default unless you are willing to have unexpected results.

8.38 returnType

returnType This tells what type of object is returned. The currently supported types are: * "rxSolve" (default) will return a reactive data frame that can change easily change different pieces of the solve and update the data frame. This is the currently standard solving method in RxODE, is used for rxSolve(object, ...), solve(object,...), * "data.frame" - returns a plain, non-reactive data frame; Currently very slightly faster than returnType="matrix" * "matrix" - returns a plain matrix with column names attached to the solved object. This is what is used object\$run as well as object\$solve * "data.table" - returns a data.table; The data.table is created by reference (ie setDt()), which should be fast. * "tbl" or "tibble" returns a tibble format.

8.39 seed

seed an object specifying if and how the random number generator should be initialized

8.40. OMEGA 89

8.40 omega

omega Estimate of Covariance matrix. When omega is a list, assume it is a block matrix and convert it to a full matrix for simulations.

8.41 omegaXform

omegaXform When taking omega values from the thetaMat simulations (using the separation strategy for covariance simulation), how should the thetaMat values be turned int standard deviation values:

- identity This is when standard deviation values are directly modeled by the params and thetaMat matrix
- variance This is when the params and thetaMat simulates the variance that are directly modeled by the thetaMat matrix
- log This is when the params and thetaMat simulates log(sd)
- nlmixrSqrt This is when the params and thetaMat simulates the inverse cholesky decomposed matrix with the x^2 modeled along the diagonal. This only works with a diagonal matrix.
- nlmixrLog This is when the params and thetaMat simulates the inverse cholesky decomposed matrix with the exp(x^2) along the diagonal. This only works with a diagonal matrix.
- nlmixrIdentity This is when the params and thetaMat simulates the inverse cholesky decomposed matrix. This only works with a diagonal matrix.

8.42 a

a when using solve, this is equivalent to the object argument. If you specify object later in the argument list it overwrites this parameter.

8.43 b

b when using solve, this is equivalent to the params argument. If you specify params as a named argument, this overwrites the output

8.44 nsim

nsim represents the number of simulations. For RxODE, if you supply single subject event tables (created with eventTable)

8.45 minSS

minSS Minimum number of iterations for a steady-state dose

$8.46 \quad \text{maxSS}$

maxSS Maximum number of iterations for a steady-state dose

8.47 strictSS

strictSS Boolean indicating if a strict steady-state is required. If a strict steady-state is (TRUE) required then at least minSS doses are administered and the total number of steady states doses will continue until maxSS is reached, or atol and rtol for every compartment have been reached. However, if ODE solving problems occur after the minSS has been reached the whole subject is considered an invalid solve. If strictSS is FALSE then as long as minSS has been reached the last good solve before ODE solving problems occur is considered the steady state, even though either atol, rtol or maxSS have not been achieved.

8.48 infSSstep

infSSstep Step size for determining if a constant infusion has reached steady state. By default this is large value, 420.

8.49 ssAtol

ssAtol Steady state atol convergence factor. Can be a vector based on each state.

8.50. SSRTOL 91

8.50 ssRtol

ssRtol Steady state rtol convergence factor. Can be a vector based on each state.

8.51 istateReset

istateReset When TRUE, reset the ISTATE variable to 1 for Isoda and libIsoda with doses, like deSolve; When FALSE, do not reset the ISTATE variable with doses.

8.52 addDosing

addDosing Boolean indicating if the solve should add RxODE EVID and related columns. This will also include dosing information and estimates at the doses. Be default, RxODE only includes estimates at the observations. (default FALSE). When addDosing is NULL, only include EVID=0 on solve and exclude any model-times or EVID=2. If addDosing is NA the classic RxODE EVID events are returned. When addDosing is TRUE add the event information in NONMEM-style format; If subsetNonmem=FALSE RxODE will also include extra event types (EVID) for ending infusion and modeled times:

- EVID=-1 when the modeled rate infusions are turned off (matches rate=-1)
- EVID=-2 When the modeled duration infusions are turned off (matches rate=-2)
- EVID=-10 When the specified rate infusions are turned off (matches rate>0)
- EVID=-20 When the specified dur infusions are turned off (matches dur>0)
- EVID=101,102,103,... Modeled time where 101 is the first model time, 102 is the second etc.

8.53 subsetNonmem

subsetNonmem subset to NONMEM compatible EVIDs only. By default TRUE.

8.54 maxAtolRtolFactor

 $\mathtt{maxAtolRtolFactor}$ The maximum $\mathtt{atol/rtol}$ that FOCEi and other routines may adjust to. By default 0.1

8.55 from

from When there is no observations in the event table, start observations at this value. By default this is zero.

8.56 to

to When there is no observations in the event table, end observations at this value. By default this is 24 + maximum dose time.

8.57 length.out

length.out The number of observations to create if there isn't any observations in the event table. By default this is 200.

8.58 by

by When there are no observations in the event table, this is the amount to increment for the observations between from and to.

8.59 keep

keep Columns to keep from either the input dataset or the iCov dataset. With the iCov dataset, the column is kept once per line. For the input dataset, if any records are added to the data LOCF (Last Observation Carried forward) imputation is performed.

8.60 drop

drop Columns to drop from the output

8.61. IDFACTOR 93

8.61 idFactor

idFactor This boolean indicates if original ID values should be maintained. This changes the default sequentially ordered ID to a factor with the original ID values in the original dataset. By default this is enabled.

8.62 warnIdSort

warnIdSort Warn if the ID is not present and RxODE assumes the order of the parameters/iCov are the same as the order of the parameters in the input dataset.

8.63 warnDrop

warnDrop Warn if column(s) were supposed to be dropped, but were not present.

8.64 safeZero

safeZero Use safe zero divide and log routines. By default this is turned on but you may turn it off if you wish.

8.65 indLinMatExpType

indLinMatExpType This is them matrix exponential type that is use for RxODE. Currently the following are supported:

- Al-Mohy Uses the exponential matrix method of Al-Mohy Higham (2009)
- arma Use the exponential matrix from RcppArmadillo
- expokit Use the exponential matrix from Roger B. Sidje (1998)

8.66 indLinMatExpOrder

indLinMatExpOrder an integer, the order of approximation to be used, for the Al-Mohy and expokit values. The best value for this depends on machine precision (and slightly on the matrix). We use 6 as a default.

8.67 indLinPhiTol

indLinPhiTol the requested accuracy tolerance on exponential matrix.

8.68 indLinPhiM

indLinPhiM the maximum size for the Krylov basis

8.69 cacheEvent

cacheEvent is a boolean. If TRUE (default), events are cached in memory to speed up solving.

8.70 sumType

sumType Sum type to use for sum() in RxODE code blocks.

pairwise uses the pairwise sum (fast, default)

fsum uses Python's fsum function (most accurate)

kahan uses Kahan correction

neumaier uses Neumaier correction

c uses no correction: default/native summing

8.71 prodType

prodType Product to use for prod() in RxODE blocks

long double converts to long double, performs the multiplication and then converts back.

double uses the standard double scale for multiplication.

8.72 sensType

sensType Sensitivity type for linCmt() model:

advan Use the direct advan solutions

8.73. LINDIFF 95

autodiff Use the autodiff advan solutions forward Use forward difference solutions central Use central differences

8.73 linDiff

linDiff This gives the linear difference amount for all the types of linear compartment model parameters where sensitivities are not calculated. The named components of this numeric vector are:

- "lag" Central compartment lag
- "f" Central compartment bioavailability
- "rate" Central compartment modeled rate
- "dur" Central compartment modeled duration
- "lag2" Depot compartment lag
- "f2" Depot compartment bioavailability
- "rate2" Depot compartment modeled rate
- "dur2" Depot compartment modeled duration

8.74 linDiffCentral

linDiffCentral This gives the which parameters use central differences for the linear compartment model parameters. The are the same components as linDiff

8.75 resample

resample A character vector of model variables to resample from the input dataset; This sampling is done with replacement. When NULL or FALSE no resampling is done. When TRUE resampling is done on all covariates in the input dataset

8.76 resampleID

resampleID boolean representing if the resampling should be done on an individual basis TRUE (ie. a whole patient is selected) or each covariate is resampled independent of the subject identifier FALSE. When resampleID=TRUE correlations of parameters are retained, where as when resampleID=FALSE ignores patient covariate correlations. Hence the default is resampleID=TRUE.

8.77 maxwhile

 ${\tt maxwhile}$ represents the maximum times a while loop is evaluated before exiting. By default this is 100000