

# Pay Attention to MLPs

# 1. Introduction

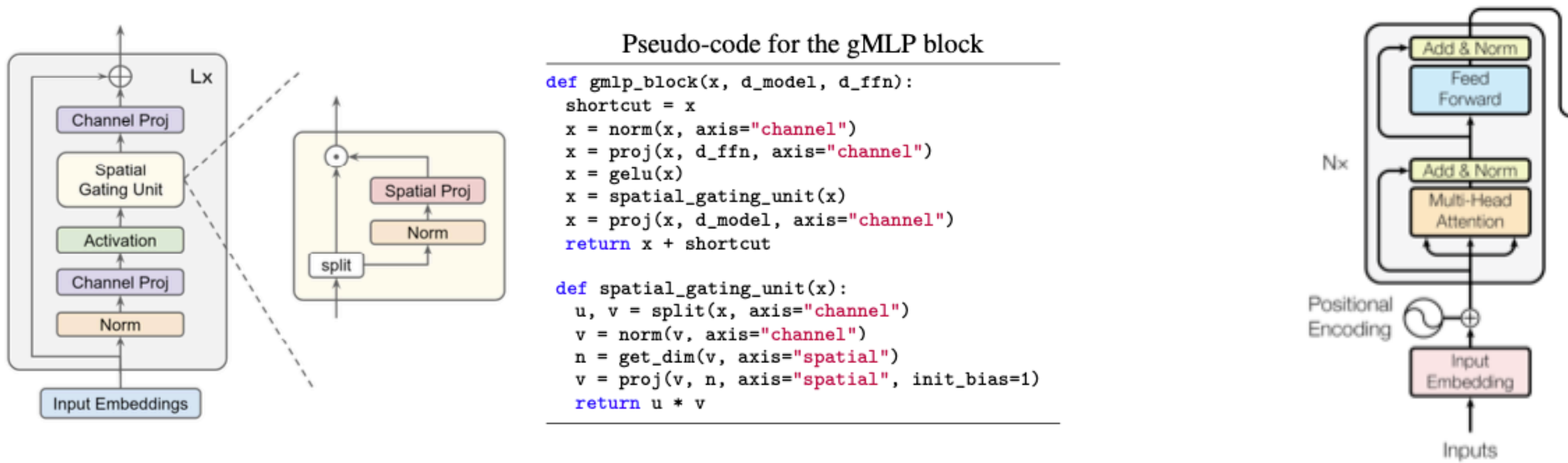
## Motivation

- It remains an open question whether the inductive bias in self-attention is essential to the remarkable effectiveness of Transformers.
- Study the necessity of self-attention modules in key language and vision applications

| MLP   | Self-Attention   |
|---|--|
| MLPs with static parameterization can represent arbitrary functions | The attention mechanism introduces the inductive bias that the model can be dynamically parameterized based on the input representations |

- Propose gMLP, and show experiments [image classification, Masked Language Model]
  - both pretraining and finetuning metrics for gMLPs improve as quickly as for Transformers
- Transformers can be more practically advantageous over gMLPs on tasks that require cross-sentence alignment (e.g., by 1.8% on MNLI), even with similar capacity and pretraining perplexity.
- Overall, our results suggest that self-attention is not a necessary ingredient for scaling up machine learning models

2. Model



- Unlike Transformers, gMLPs do not require positional encodings, nor is it necessary to mask out the paddings during NLP finetuning.

| <div><math display="block">Z = \sigma(XU)</math><math display="block">\tilde{Z} = s(Z)</math><math display="block">Y = \tilde{Z}V</math></div> | <ul style="list-style-type: none"><li>• <b>Spatial Gating Unit:</b> a layer which captures spatial interactions<ul style="list-style-type: none"><li>→ our major focuses is therefore to design a good <math>s</math> capable of capturing complex spatial interactions across tokens</li><li>→ our model <i>does not require position embeddings</i> because such information will be captured in <math>s(\cdot)</math></li></ul></li></ul> |
|--|--|

## 2.1 Spatial Gating Unit

| Equations   | Plot  |
|---|---|
| $f_{W,b}(Z) = WZ + b$ $s(Z) = Z_1 \odot f_{W,b}(Z_2)$ | <p>The diagram illustrates the architecture of the Spatial Gating Unit. At the bottom, a blue grid representing input <math>\mathbf{X}</math> with dimensions <math>(n, d)</math> is shown. Above it is a purple trapezoidal block representing the gating function <math>\mathbf{U}</math> with dimensions <math>(d, d_{ff})</math>. The output of this block is a green grid <math>Z = \sigma(\mathbf{X}\mathbf{U})</math> with dimensions <math>(n, d_{ff})</math>. A code snippet <code>u, v = x.chunk(2, dim=-1)</code> is shown next to the <math>Z</math> grid. From the <math>Z</math> grid, two paths emerge: one leads to a green grid <math>Z_1</math> (3x8), and the other leads to a yellow grid <math>Z_2</math> (3x8) after passing through a yellow rectangular block <math>\mathbf{W}</math>. The final output <math>s(Z)</math> is represented by a circle with a dot inside, which is the element-wise product of <math>Z_1</math> and <math>Z_2</math>.</p> |

- For training stability, we find it critical to **initialize  $\mathbf{W}$**  as near-zero values and  $\mathbf{b}$  as ones, meaning that  $s(\cdot)$  is approximately an identity mapping at the beginning of training.
- the magnitude for each element in  $Z$  can be rapidly tuned according to the gating function  $f_{w,b}(\cdot)$

### 3. Image Classification

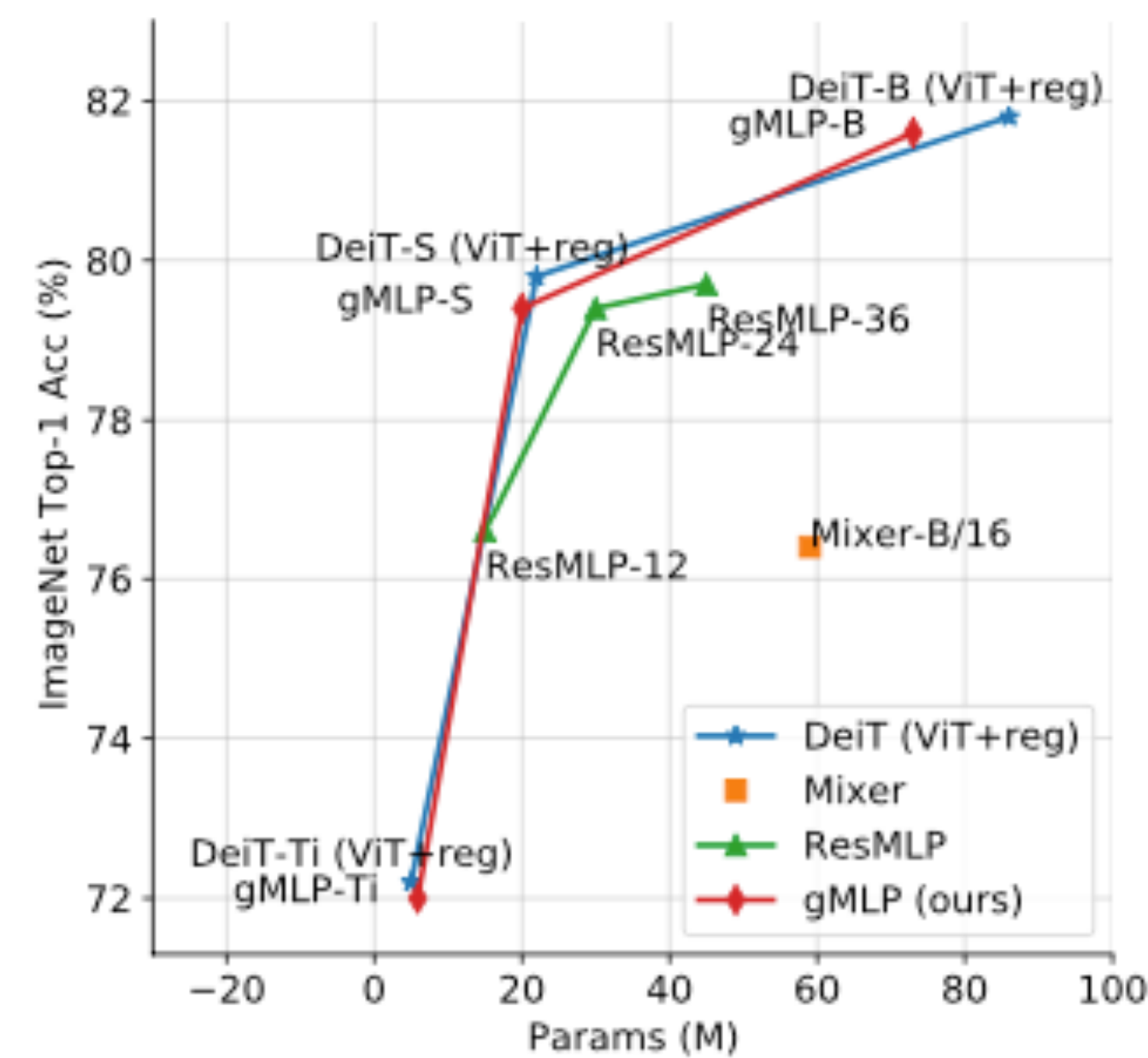


Figure 2: ImageNet accuracy vs model capacity.

- We compare our attention-free models with recent attentive models based on vanilla Transformers, including Vision Transformer (ViT) [7], DeiT [8] (ViT with improved regularization), and several other representative convolutional networks.
- The accuracy-parameter/FLOPs tradeoff of gMLPs surpasses all concurrently proposed MLP-like architectures , which we attribute to the effectiveness of our Spatial Gating Unit

### 3. Image Classification

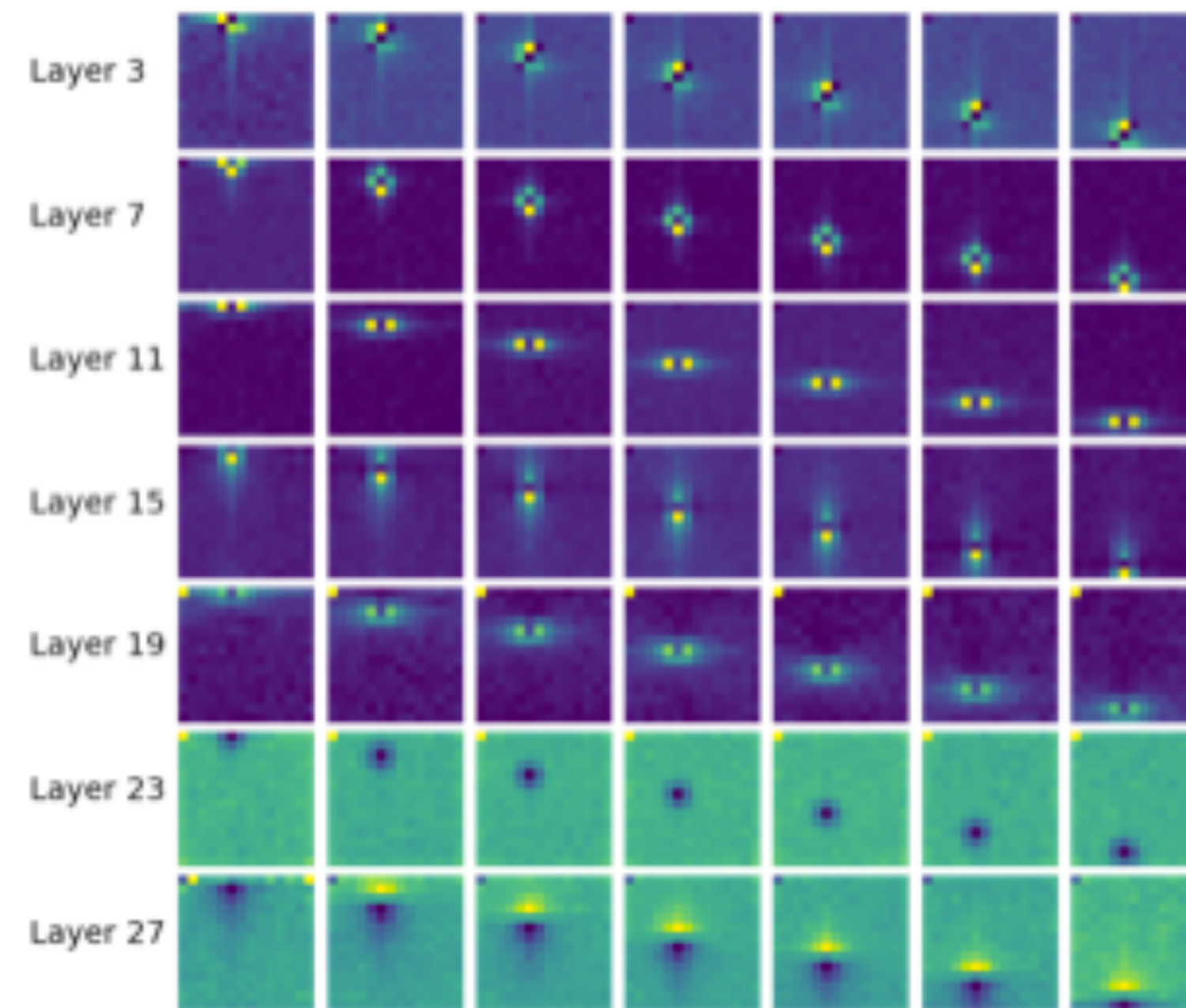


Figure 3: Spatial projection weights in gMLP-B. Each row shows the filters (reshaped into 2D) for a selected set of tokens in the same layer.

- The spatial weights after learning exhibit both locality and spatial invariance. In other words, each spatial projection matrix effectively learns to perform convolution with a data-driven, irregular (non-square) kernel shape.



## 4. Masked Language Modeling with BERT

- We do not use positional encodings.
- We also find it unnecessary to mask out <pad> tokens in gMLP blocks during finetuning as the model can quickly learn to ignore them.

### 4.1 Ablation: The Importance of Gating in gMLP for BERT’s Pretraining

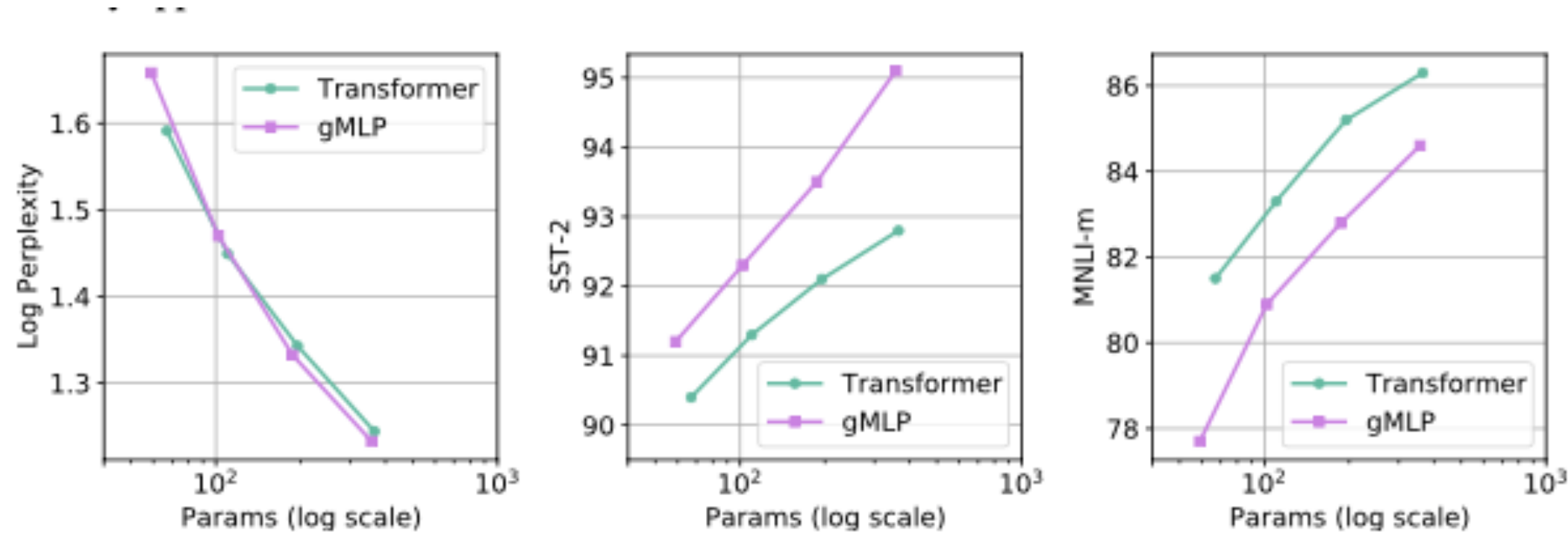
| Model  | Perplexity | Params (M) |
|--|------------|------------|
| BERT <sub>base</sub> <small>BERT with a Transformer architecture and learnable absolute position embeddings.</small>               | 4.37       | 110        |
| BERT <sub>base</sub> + rel pos <small>BERT with a Transformer architecture and T5-style learnable relative position biases</small> | 4.26       | 110        |
| BERT <sub>base</sub> + rel pos - attn  | 5.64       | 96         |
| Linear gMLP, $s(Z) = f(Z)$   | 5.14       | 92         |
| Additive gMLP, $s(Z) = Z + f(Z)$   | 4.97       | 92         |
| Multiplicative gMLP, $s(Z) = Z \odot f(Z)$   | 4.53       | 92         |
| Multiplicative, Split gMLP, $s(Z) = Z_1 \odot f(Z_2), Z = Z_1    Z_2$  | 4.35       | 102        |

1. SGU outperforms other variants in perplexity
2. gMLP with SGU also achieves perplexity comparable to Transformer.

4.2 Case Study: The Behavior of gMLP as Model Size Increases

| Model       | #L    | Params (M) | Perplexity  | SST-2 | MNLI-m |
|-------------|-------|------------|-------------|-------|--------|
| Transformer | 6+6   | 67         | <b>4.91</b> | 90.4  | 81.5   |
|             | 18    | 59         | 5.25        | 91.2  | 77.7   |
| Transformer | 12+12 | 110        | <b>4.26</b> | 91.3  | 83.3   |
|             | 36    | 102        | 4.35        | 92.3  | 80.9   |
| Transformer | 24+24 | 195        | 3.83        | 92.1  | 85.2   |
|             | 72    | 187        | <b>3.79</b> | 93.5  | 82.8   |
| Transformer | 48+48 | 365        | 3.47        | 92.8  | 86.3   |
|             | 144   | 357        | <b>3.43</b> | 95.1  | 84.6   |

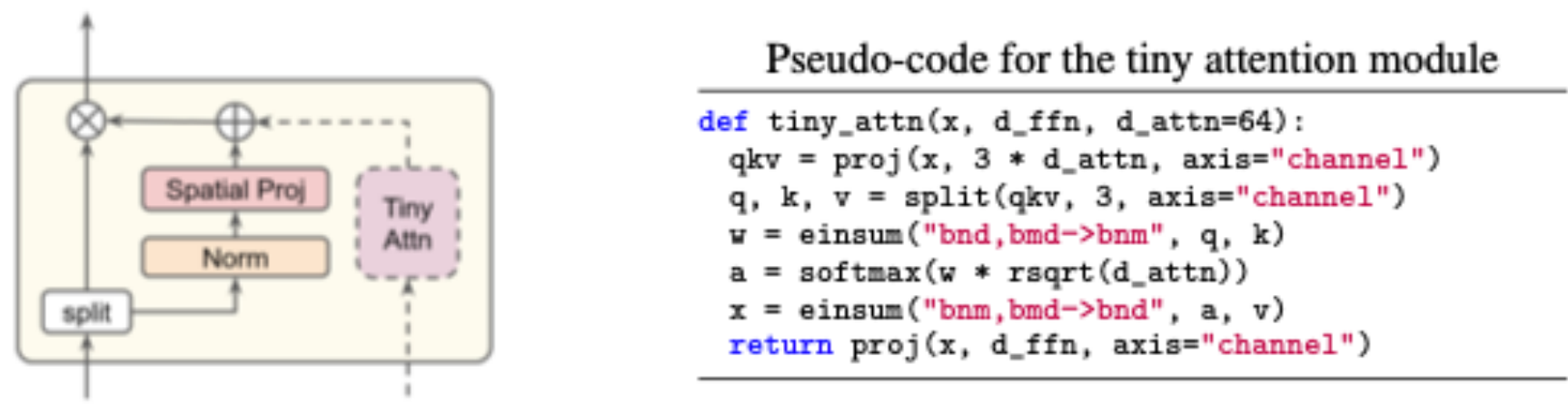
- The results above show that a deep enough gMLP is able to match and even outperform the perplexity of Transformers with comparable capacity



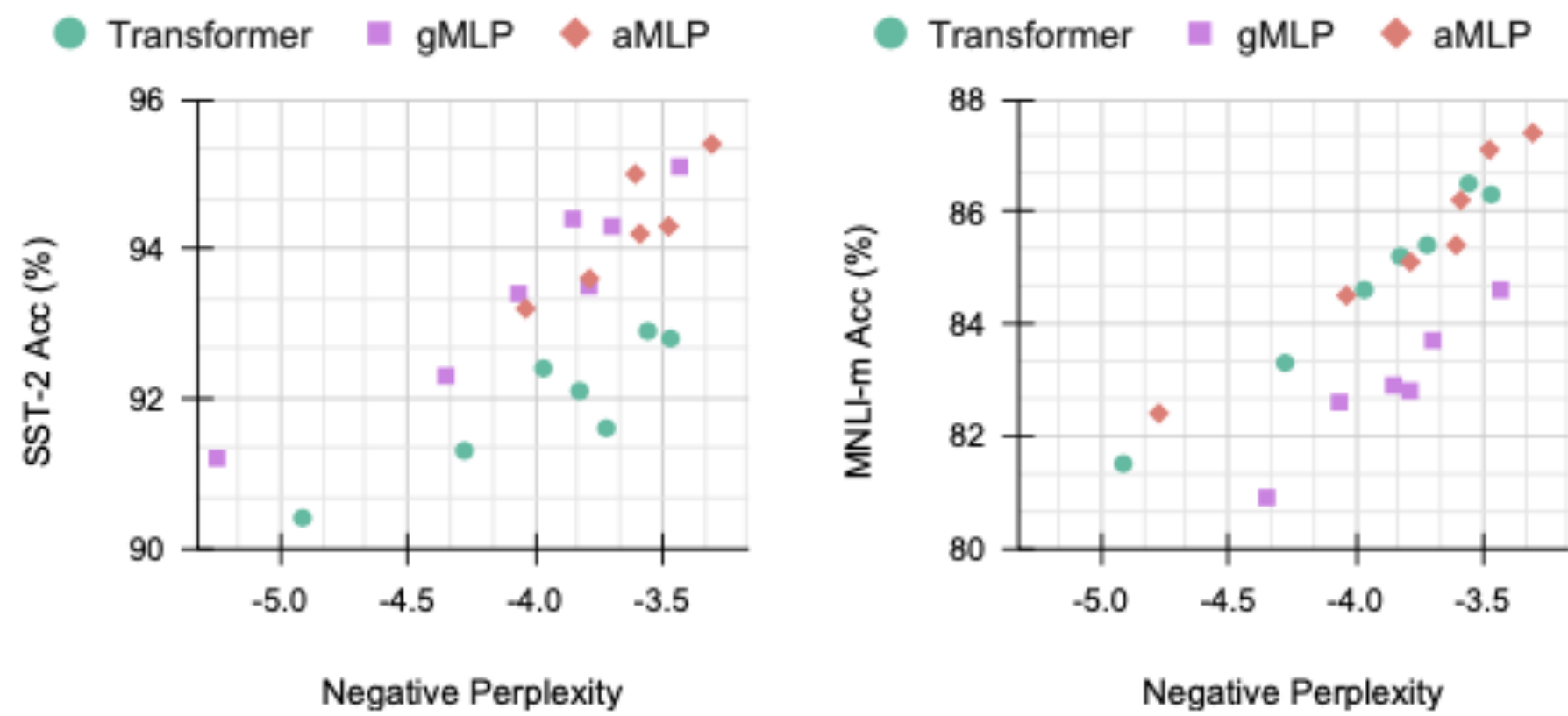
- Our attention-free model is advantageous on SST-2 but worse on MNLI is particularly informative—the former is a single-sentence task whereas the latter involves sentence pairs (premise and hypothesis)



4.3 Ablation: The Usefulness of Tiny Attention in BERT’s Finetuning



- To isolate the effect of attention, we experiment with a hybrid model where a tiny self-attention block is attached to the gating function of gMLP (Figure 6)



4.4 Main Results for MLM in the BERT Setup

|                              | Perplexity | SST-2 | MNLI<br>(m/mm) | SQuAD |      | Attn Size      | Params<br>(M) |
|------------------------------|------------|-------|----------------|-------|------|----------------|---------------|
|                              |            |       |                | v1.1  | v2.0 |                |               |
| BERT <sub>base</sub> [2]     | –          | 92.7  | 84.4/-         | 88.5  | 76.3 | 768 (64 × 12)  | 110           |
| BERT <sub>base</sub> (ours)  | 4.17       | 93.8  | 85.6/85.7      | 90.2  | 78.6 | 768 (64 × 12)  | 110           |
| gMLP <sub>base</sub>         | 4.28       | 94.2  | 83.7/84.1      | 86.7  | 70.1 | –              | 130           |
| aMLP <sub>base</sub>         | 3.95       | 93.4  | 85.9/85.8      | 90.7  | 80.9 | 64             | 109           |
| BERT <sub>large</sub> [2]    | –          | 93.7  | 86.6/-         | 90.9  | 81.8 | 1024 (64 × 16) | 336           |
| BERT <sub>large</sub> (ours) | 3.35       | 94.3  | 87.0/87.4      | 92.0  | 81.0 | 1024 (64 × 16) | 336           |
| gMLP <sub>large</sub>        | 3.32       | 94.8  | 86.2/86.5      | 89.5  | 78.3 | –              | 365           |
| aMLP <sub>large</sub>        | 3.19       | 94.8  | 88.4/88.4      | 92.2  | 85.4 | 128            | 316           |

Table 6: Pretraining perplexities and dev-set results for finetuning. “ours” indicates models trained using our setup. We report accuracies for SST-2 and MNLI, and F1 scores for SQuAD v1.1/2.0.

- our gMLP<sub>large</sub> achieves 89.5% F1 on SQuAD-v1.1 without any attention or dynamic parameterization mechanism
- our hybrid model aMLP<sub>large</sub> achieves 4.4% higher F1 than Transformers on the more difficult SQuAD-v2.0 task.

5 Conclusion

- We show that gMLPs, a simple variant of MLPs with gating, can be competitive with Transformers in terms of BERT’s pretraining perplexity and ViT’s accuracy.