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Homework 1.3

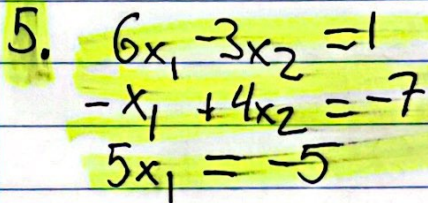
$$-V = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$$

$$-2v = \begin{bmatrix} 6 \\ 2 \end{bmatrix}$$

$$u+v = \begin{bmatrix} -4 \\ 1 \end{bmatrix}$$

$$u-v = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$u - 2v = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$$



7.

$$a = u - 2v$$
$$b = 2u - 2v$$
$$c = 2u - 3.5v$$
$$d = 3u - 4v$$

9.
$$x_1 \begin{bmatrix} 0 \\ 4 \\ -1 \end{bmatrix} + x_2 \begin{bmatrix} 1 \\ 6 \\ 3 \end{bmatrix} + x_3 \begin{bmatrix} 5 \\ -1 \\ -8 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$x_2, 13, 15, 19$

12.
$$\begin{aligned} x_1 + 2x_3 &= -5 \\ -2x_1 + 5x_2 &= 11 \\ 2x_1 + 5x_2 + 8x_3 &= -7 \end{aligned}$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 2 & -5 \\ -2 & 5 & 0 & 11 \\ 2 & 5 & 8 & -7 \end{array} \right]$$

$R_3 + R_2 \rightarrow R_3$

$$\left[\begin{array}{ccc|c} 1 & 0 & 2 & -5 \\ 0 & 10 & 8 & 4 \\ 2 & 5 & 8 & -7 \end{array} \right] \quad -2R_1 + R_3 \rightarrow R_3$$
$$\left[\begin{array}{ccc|c} 1 & 0 & 2 & -5 \\ 0 & 10 & 8 & 4 \\ 0 & 5 & 4 & 3 \end{array} \right]$$

$\frac{1}{2}R_2 \rightarrow R_2$

$$\left[\begin{array}{ccc|c} 1 & 0 & 2 & -5 \\ 0 & 5 & 4 & 2 \\ 0 & 5 & 4 & 3 \end{array} \right] \quad -R_2 + R_3 \rightarrow R_3$$
$$\left[\begin{array}{ccc|c} 1 & 0 & 2 & -5 \\ 0 & 5 & 4 & 2 \\ 0 & 0 & 0 & 1 \end{array} \right]$$

$b \neq$ linear
combo

13.
$$\left[\begin{array}{ccc|c} 1 & -4 & 2 & 3 \\ 0 & 3 & 5 & -7 \\ -2 & 8 & -4 & -3 \end{array} \right] \quad 2R_1 + R_3 \rightarrow R_3$$

$$\left[\begin{array}{ccc|c} 1 & -4 & 2 & 3 \\ 0 & 3 & 5 & -7 \\ 0 & 0 & 0 & 3 \end{array} \right]$$

$b \neq$ linear
combo

15, 18, 24, 25

15. $\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} = 0\vec{v}_1 + 0\vec{v}_2$

$$0\vec{v}_1 + 2 \begin{bmatrix} -5 \\ 3 \\ 0 \end{bmatrix} = \begin{bmatrix} -10 \\ 6 \\ 0 \end{bmatrix}$$

$$2 \begin{bmatrix} 7 \\ 1 \\ -6 \end{bmatrix} + 0\vec{v}_2 = \begin{bmatrix} 14 \\ 2 \\ -12 \end{bmatrix}$$

$$0\vec{v}_1 + 3 \begin{bmatrix} -5 \\ 3 \\ 0 \end{bmatrix} = \begin{bmatrix} -15 \\ 9 \\ 0 \end{bmatrix}$$

$$3 \begin{bmatrix} 7 \\ 1 \\ -6 \end{bmatrix} + 0\vec{v}_2 = \begin{bmatrix} 21 \\ 3 \\ -18 \end{bmatrix}$$

19. $\text{Span}\{\vec{v}_1, \vec{v}_2\}$ is a plane (2d) that hits 0 and both \vec{v}_1 and \vec{v}_2

24. a. False, ~~vectors are ordered~~ if list is unordered
True if list is ordered

b. True, $\vec{v} + (\vec{u} - \vec{v})$ is true because matrix addition is associative

c. False, the result would be a zero vector which is allowed

d. True, all linear vectors start at zero

24. cont

e. True, because b is a non pivot column

25. $\left[\begin{array}{ccc|c} 1 & 0 & -4 & 4 \\ 0 & 3 & -2 & 1 \\ -2 & 6 & 3 & -4 \end{array} \right] = [a_1 \ a_2 \ a_3 \ b]$

$2R_1 + R_3 \rightarrow R_3$

$$\left[\begin{array}{ccc|c} 1 & 0 & -4 & 4 \\ 0 & 3 & -2 & 1 \\ 0 & 0 & 5 & 4 \end{array} \right] \quad -2R_2 + R_3 \rightarrow R_3$$

$$\left[\begin{array}{ccc|c} 1 & 0 & -4 & 4 \\ 0 & 3 & -2 & 1 \\ 0 & 0 & -1 & 2 \end{array} \right] \quad -R_3 \rightarrow R_3$$

$$\left[\begin{array}{ccc|c} 1 & 0 & -4 & 4 \\ 0 & 3 & -2 & 1 \\ 0 & 0 & 1 & -2 \end{array} \right]$$

= there is a solution = consistent
= this means b is in the span W

S.T. 1.3

Q. A span is a set of all possible linear combos of given vectors