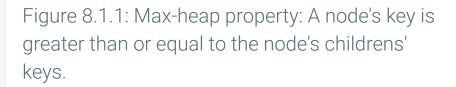
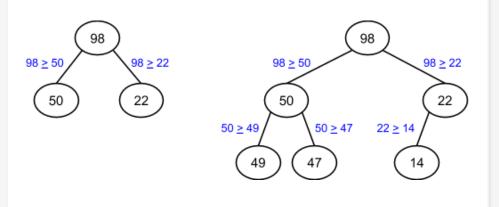
8.1 Heaps

Heap concept

Some applications require fast access to and removal of the maximum item in a changing set of items. For example, a computer may execute jobs one at a time; upon finishing a job, the computer executes the pending job having maximum priority. Ex: Four pending jobs have priorities 22, 14, 98, and 50; the computer should execute 98, then 50, then 22, and finally 14. New jobs may arrive at any time.

Maintaining jobs in fully-sorted order requires more operations than necessary, since only the maximum item is needed. A **max-heap** is a complete binary tree that maintains the simple property that a node's key is greater than or equal to the node's childrens' keys. (Actually, a max-heap may be any tree, but is commonly a binary tree). Because $x \ge y$ and $y \ge z$ implies $x \ge z$, the property results in a node's key being greater than or equal to all the node's descendants' keys. Therefore, a max-heap's root always has the maximum key in the entire tree.



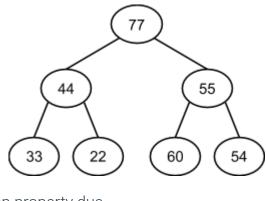


PARTICIPATION ACTIVITY

8.1.1: Max-heap property.

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Consider this binary tree:



- 1) 33 violates the max-heap property due to being greater than 22.
 - True
 - C False
- 2) 54 violates the max-heap property due to being greater than 44.
 - O True
 - O False
- 3) 60 violates the max-heap property due to being greater than 55.
 - O True
 - O False
- 4) A max-heap's root must have the maximum key.
 - O True
 - C False

Max-heap insert and remove operations

An **insert** into a max-heap starts by inserting the node in the tree's last level, and then swapping the node with its parent until no max-heap property violation occurs. Inserts fill a level (left-to-right) before adding another level, so the tree's height is always the minimum possible. The upward movement of a node in a max-heap is called percolating.

A remove from a max-heap is always a removal of the root, and is done by replacing the root with the last level's last node, and swapping that node with its greatest child until no max-heap property violation occurs. Because upon completion that node will occupy another node's location (which was swapped upwards), the tree height remains the minimum possible.

PARTICIPATION **ACTIVITY**

8.1.2: Max-heap insert and remove operations.

Animation captions:

- 1. This tree is a max-heap. A new node gets initially inserted in the last level...
- 2. ...and then percolate node up until the max-heap property isn't violated.
- 3. Removing a node (always the root): Replace with last node, then percolate node down.

PARTICIPATION ACTIVITY	8.1.3: Max-heap inserts and deletes.	©zyBooks 05/10/21 12:45 728163 Neha Maddali IASTATECOMS228Spring2021
max-heap		
and 3, with inserting a	ax-heap with levels 0, 1, 2, In the last level not full, after In new node, what is the Inpossible swaps needed?	
is the wors insert, ass		
	ax-heap with N nodes, what applexity for removing the	
O 0(N	$(Q_{ij})_{ij}$	©zyBooks 05/10/21 12:45 728163 Neha Maddali IASTATECOMS228Spring2021

Min-heap

A **min-heap** is similar to a max-heap, but a node's key is less than or equal to its children's keys.

Example 8.1.1: Online tech support waiting lines commonly use min heaps.

Many companies have online technical support that lets a customer chat with a support agent. If the number of customers seeking support is greater than the number of available agents, customers enter a virtual waiting line. Each customer has a priority that determines their place in line. The customer with the highest priority is served by the next available 45 728163 agent.

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A min heap is commonly used to manage prioritized queues of customers awaiting support. Customers that entered the line earlier and/or have a more urgent issue get assigned a lower number, which corresponds to a higher priority. When an agent becomes available, the customer with the lowest number is removed from the heap and served by the agent.

All agents busy Agent becomes available 4 18 16 18 16 Customers wait for next available agent Customers with lowest number (4) is removed from min heap and served by the agent

PARTICIPATION ACTIVITY

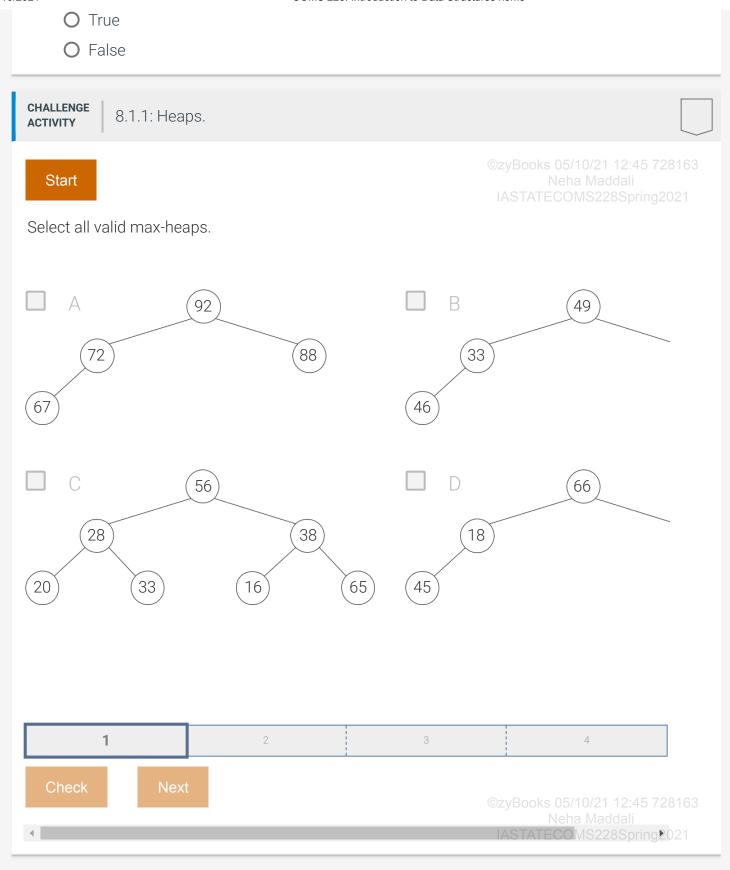
8.1.4: Min heaps and customer support.

1) A customer with a higher priority has a lower numerical value in the min heap.

O True

O False

2) If 2,000 customers are waiting for technical support, removing a customer from the min heap requires about 2,000 operations.



8.2 Heaps using arrays

Heap storage

Heaps are typically stored using arrays. Given a tree representation of a heap, the heap's array form is produced by traversing the tree's levels from left to right and top to bottom. The root node is always the entry at index 0 in the array, the root's left child is the entry at index 1, the root's right child is the entry at index 2, and so on.

PARTICIPATION ACTIVITY

8.2.1: Max-heap stored using an array.

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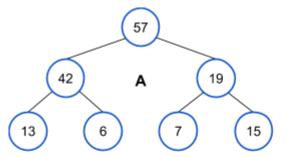
Animation captions:

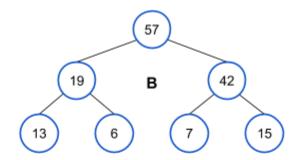
- 1. The max-heap's array form is produced by traversing levels left to right and top to bottom.
- 2. When 63 is inserted, the percolate-up operation happens within the array.

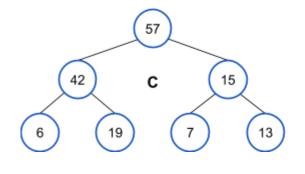
PARTICIPATION ACTIVITY

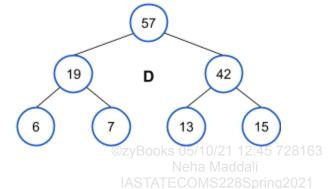
8.2.2: Heap storage.

Match each max-heap to the corresponding storage array.









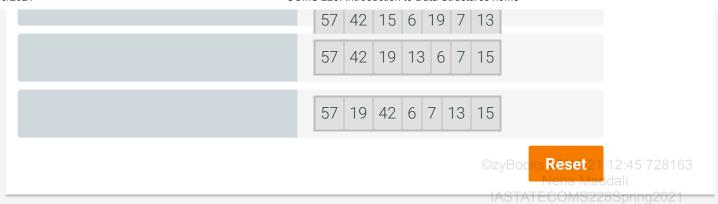
Heap B

Heap A

Heap C

Heap D

57 | 19 | 42 | 13 | 6 | 7 | 15



Parent and child indices

Because heaps are not implemented with node structures and parent/child pointers, traversing from a node to parent or child nodes requires referring to nodes by index. The table below shows parent and child index formulas for a heap.

Table 8.2.1: Parent and child indices for a heap.

Node index	Parent index	Child indices
0	N/A	1, 2
1	0	3, 4
2	0	5, 6
3	1	7, 8
4	1	9, 10
5	2	11, 12
i	$\lfloor (i-1)/2 floor$	2*i+1,2*i+2

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PARTICIPATION ACTIVITY

8.2.3: Heap parent and child indices.

- 1) What is the parent index for a node at index 12?
 - **O** 3
 - O 4

O 5	
O 6	
2) What are the child indices for a node at index 6?	
O 7 and 8	
O 12 and 13	©zyBooks 05/10/21 12:45 728163 Neha Maddali
O 13 and 14	IASTATECOMS228Spring2021
O 12 and 24	
3) The formula for computing parent node index should not be used on the root node.O True	
O False	
4) The formula for computing child node indices does not work on the root node.	
O True	
O False	
5) The formula for computing a child index evaluates to -1 if the parent is a leaf node.	
O True	
O False	
Percolate algorithm	
Following is the pseudocode for the array-based percolate-up functions operate on an array that represents a max-heap and	·
Figure 8.2.1: Max-heap percolate up algorithm.	©zyBooks 05/10/21 12:45 728163 Neha Maddali IASTATECOMS228Spring2021

```
MaxHeapPercolateUp(nodeIndex, heapArray) {
  while (nodeIndex > 0) {
    parentIndex = (nodeIndex - 1) / 2
    if (heapArray[nodeIndex] <= heapArray[parentIndex])
        return
    else {
        swap heapArray[nodeIndex] and heapArray[parentIndex]
        nodeIndex = parentIndex
    }
  }
}</pre>
```

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Figure 8.2.2: Max-heap percolate down algorithm.

```
MaxHeapPercolateDown(nodeIndex, heapArray, arraySize) {
   childIndex = 2 * nodeIndex + 1
   value = heapArray[nodeIndex]
  while (childIndex < arraySize) {</pre>
      // Find the max among the node and all the node's children
      maxValue = value
      maxIndex = -1
      for (i = 0; i < 2 \&\& i + childIndex < arraySize; i++) {
         if (heapArray[i + childIndex] > maxValue) {
            maxValue = heapArray[i + childIndex]
            maxIndex = i + childIndex
         }
      }
      if (maxValue == value) {
         return
      else {
         swap heapArray[nodeIndex] and heapArray[maxIndex]
         nodeIndex = maxIndex
         childIndex = 2 * nodeIndex + 1
      }
   }
}
```

PARTICIPATION ACTIVITY

8.2.4: Percolate algorithm.

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1) MaxHeapPercolateUp works for a node index of 0.

- O True
- O False
- 2) MaxHeapPercolateDown has a

precondition that nodeIndex is < arraySize.	
O True	
O False	
3) MaxHeapPercolateDown checks the node's left child first, and immediately swaps the nodes if the left child has a greater key.	©zyBooks 05/10/21 12:45 728163 Neha Maddali IASTATECOMS228Spring2021
O True	
O False	
4) In MaxHeapPercolateUp, the while loop's condition nodeIndex > 0 guarantees that parentIndex is >= 0.	
O True	
O False	
CHALLENGE ACTIVITY 8.2.1: Heaps using arrays.	
Start 95	
62 72 48 40	
What is the above max-heap's array form?	
Ex: 86, 75, 30 (comma between values)	©zyBooks 05/10/21 12:45 728163
	Neha Maddali IASTATECOMS228Spring2021
1 2 3 4	5
Charle	
Check Next	

8.3 Heap sort

Heapify operation

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Heapsort is a sorting algorithm that takes advantage of a max-heap's properties by repeatedly removing the max and building a sorted array in reverse order. An array of unsorted values must first be converted into a heap. The **heapify** operation is used to turn an array into a heap. Since leaf nodes already satisfy the max heap property, heapifying to build a max-heap is achieved by percolating down on every non-leaf node in reverse order.

PARTICIPATION ACTIVITY

8.3.1: Heapify operation.

Animation captions:

- 1. If the original array is represented in tree form, the tree is not a valid max-heap.
- 2. Leaf nodes always satisfy the max heap property, since no child nodes exist that can contain larger keys. Heapification will start on node 92.
- 3. 92 is greater than 24 and 42, so percolating 92 down ends immediately.
- 4. Percolating 55 down results in a swap with 98.
- 5. Percolating 77 down involves a swap with 98. The resulting array is a valid max-heap.

The heapify operation starts on the internal node with the largest index and continues down to, and including, the root node at index 0. Given a binary tree with N nodes, the largest internal node index is $\lfloor N/2 \rfloor$ - 1.

Table 8.3.1: Max-heap largest internal node index.

Number of nodes in binary heap	Largest internal node index
1	-1 (no internal nodes)
2	0
3	0
4	1

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5	1	
6	2	
7	2	
N	$\lfloor N/2 floor$ - 1	©zyBooks 05/10/21 12:45 728163 Neha Maddali
		IASTATECOMS228Spring2021
PARTICIPATION 8.3.2: Heapify ope	ration.	
1) For an array with 7 nodes, how percolate-down operations are necessary to heapify the array. Check Show answer 2) For an array with 10 nodes, how percolate-down operations are necessary to heapify the array. Check Show answer	w many	
PARTICIPATION 8.3.3: Heapify ope	ration - critical thinking.	
An array sorted in ascending of already a wallid may been	rder is	
already a valid max-heap. O True		@=vDooks 05/40/24 42:45 720462
O False		©zyBooks 05/10/21 12:45 728163 Neha Maddali IASTATECOMS228Spring2021
Which array could be heapified fewest number of operations, i all swaps used for percolating?	ncluding	
O (10, 20, 30, 40)		
O (30, 20, 40, 10)		
-		

O (10, 10, 10, 10)

Heapsort overview

Heapsort begins by heapifying the array into a max-heap and initializing an end index value to the size of the array minus 1. Heapsort repeatedly removes the maximum value, stores that value at the end index, and decrements the end index. The removal loop repeats until the end index is 0.12:45 728163

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PARTICIPATION ACTIVITY

8.3.4: Heapsort.

Animation captions:

- 1. The array is heapified first. Each internal node is percolated down, from highest node index to lowest.
- 2. The end index is initialized to 6, to refer to the last item. 94's "removal" starts by swapping with 68.
- 3. Removing from a heap means that the rightmost node on the lowest level disappears before the percolate down. End index is decremented after percolating.
- 4. 88 is swapped with 49, the last node disappears, and 49 is percolated down.
- 5. The process continues until end index is 0.
- 6. The array is sorted.

PARTICIPATION 8.3.5: Heapsort.	
Suppose the original array to be heapified is (11, 21, 12, 13, 19, 15)).
The percolate down operation must be performed on which nodes?	
O 15, 19, and 13	
O 12, 21, and 11	
O All nodes in the heap	
2) What are the first 2 elements swapped?	©zyBooks 05/10/21 12:45 728163 Neha Maddali
O 11 and 21	IASTATECOMS228Spring2021
O 21 and 13	
O 12 and 15	
3) What are the last 2 elements swapped?	
O 11 and 19	

O 11 and 21	
O 19 and 21	
4) What is the heapified array?	
O (11, 21, 12, 13, 19, 15)	
O (21, 19, 15, 13, 12, 11)	
O (21, 19, 15, 13, 11, 12)	©zyBooks 05/10/21 12:45 728163 Neha Maddali JASTATE COMS 228 Spring 2021

Heapsort algorithm

Heapsort uses 2 loops to sort an array. The first loop heapifies the array using MaxHeapPercolateDown. The second loop removes the maximum value, stores that value at the end index, and decrements the end index, until the end index is 0.

```
Figure 8.3.1: Heap sort.
```

```
Heapsort(numbers, numbersSize) {
   // Heapify numbers array
   for (i = numbersSize / 2 - 1; i >= 0; i--) {
      MaxHeapPercolateDown(i, numbers, numbersSize)
   }
   for (i = numbersSize - 1; i > 0; i--) {
      Swap numbers[0] and numbers[i]
      MaxHeapPercolateDown(0, numbers, i)
   }
}
```

1) How many times will

MaxHeapPercolateDown be called by
Heapsort when sorting an array with
10 elements?

O 5

O 10

O 14

O 20

2) Calling Heapsort on an array with 1 element will cause an out of bounds

array access.	
O True	
O False	
3) Heapsort's worst-case runtime is O(N log N).	
O True	©zyBooks 05/10/21 12:45 728163 Neha Maddali
O False	IASTATECOMS228Spring2021
4) Heapsort uses recursion.	
O True	
O False	
CHALLENGE 8.3.1: Heap sort.	
Given the array: 87 88 39 72 17 32 78 Heapify into a max-heap.	
87 88 39 72 17 32 78	
87 88 39 72 17 32 78 Heapify into a max-heap.	
87 88 39 72 17 32 78 Heapify into a max-heap.	
87 88 39 72 17 32 78 Heapify into a max-heap. Ex: 86, 75, 30	
87 88 39 72 17 32 78 Heapify into a max-heap.	3 ©zyBooks 05/10/21 12:45 728163
87 88 39 72 17 32 78 Heapify into a max-heap. Ex: 86, 75, 30	
87 88 39 72 17 32 78 Heapify into a max-heap. Ex: 86, 75, 30	©zyBooks 05/10/21 12:45 728163 Neha Maddali

8.4 Priority queue abstract data type (ADT)

Priority queue abstract data type

A *priority queue* is a queue where each item has a priority, and items with higher priority are closer to the front of the queue than items with lower priority. The priority queue *enqueue* operation inserts an item such that the item is closer to the front than all items of lower priority, and closer to the end than all items of equal or higher priority. The priority queue *dequeue* operation removes and returns the item at the front of the queue, which has the highest priority.

PARTICIPATION 8.4.1: Priority queue enqueue and dequeue. **ACTIVITY Animation content:** undefined **Animation captions:** 1. Enqueueing a single item with priority 7 initializes the priority queue with 1 item. 2. If a lower numerical value indicates higher priority, enqueueing 11 adds the item to the end of the queue. 3. Since 5 < 7, enqueueing 5 puts the item at the priority gueue's front. 4. When enqueueing items of equal priority, the first-in-first-out rules apply. The 2nd item with priority 7 comes after the first. 5. Dequeue removes from the front of the gueue, which is always the highest priority item. **PARTICIPATION** 8.4.2: Priority queue enqueue and dequeue. **ACTIVITY** Assume that lower numbers have higher priority and that a priority queue currently holds items: 54, 71, 86 (front is 54). 1) Where would an item with priority 60 reside after being enqueued? O Before 54 O After 54 O After 86 2) Where would an additional item with priority 54 reside after being enqueued? O Before the first 54

After the first 54	
O After 86	
3) The dequeue operation would return which item?	
O 54	
O 71	©zyBooks 05/10/21 12:45 728163 Neha Maddali
O 86	IASTATECOMS228Spring2021

Common priority queue operations

In addition to enqueue and dequeue, a priority queue usually supports peeking and length querying. A **peek** operation returns the highest priority item, without removing the item from the front of the queue.

Table 8.4.1: Common priority queue ADT operations.

Operation	Description	Example starting with priority queue: 42, 61, 98 (front is 42)
Enqueue(PQueue, x)	Inserts x after all equal or higher priority items	Enqueue(PQueue, 87). PQueue: 42, 61, 87, 98
Dequeue(PQueue)	Returns and removes the item at the front of PQueue	Dequeue(PQueue) returns 42. PQueue: 61, 98
Peek(PQueue)	Returns but does not remove the item at the front of PQueue	Peek(PQueue) returns 42. PQueue: 42, 61, 98
IsEmpty(PQueue)	Returns true if PQueue has no items	IsEmpty(PQueue) returns false.
GetLength(PQueue)	Returns the number of items in PQueue	GetLength(PQueue) returns 3.

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PARTICIPATION ACTIVITY

8.4.3: Common priority queue ADT operations.

Assume servicePQueue is a priority queue with contents: 11, 22, 33, 44, 55.

1) What does GetLength(servicePQueue)

0/2021	COMS 228: Introduction to Data St	tructures home
return	?	
0	5	
0	11	
0	55	
2) What oreturn?	does Dequeue(servicePQueue) ?	©zyBooks 05/10/21 12:45 728163
0	5	Neha Maddali IASTATECOMS228Spring2021
0	11	
0	55	
	dequeuing an item, what will servicePQueue) return?	
0	11	
0	22	
0	33	
a total	calling Dequeue(servicePQueue) I of 5 times, what will ngth(servicePQueue) return?	
0	-1	
0	0	
0	Undefined	
Enqueueing items with priority A priority queue can be implemented such that each item's priority can be determined from the item		
	customer object may contain information about a cu a service priority number. In this case, the priority resid	3
A priority queue may also be implemented such that all priorities are specified during a call to EnqueueWithPriority : An enqueue operation that includes an argument for the enqueued item's priority. ©zyBooks 05/10/21 12:45 728163		
PARTICIPATI ACTIVITY	8.4.4: Priority queue EnqueueWithPriority opera	Neha Maddali

Animation content:

undefined

Animation captions:

- 1. Calls to EnqueueWithPriority() enqueue objects A, B, and C into the priority queue with the specified priorities.
- 2. In this implementation, the objects enqueued into the queue do not have data members representing priority.
- 3. Priorities specified during each EnqueueWithPriority() call are stored alongside the queue's objects.

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PARTICIPATION 8.4.5: EnqueueWithPriority operation.	
1) A priority queue implementation that requires objects to have a data member storing priority would implement the function.	
O Enqueue	
O EnqueueWithPriority	
2) A priority queue implementation that does not require objects to have a data member storing priority would implement the function.	
O Enqueue	
O EnqueueWithPriority	

Implementing priority queues with heaps

A priority queue is commonly implemented using a heap. A heap will keep the highest priority item in the root node and allow access in O(1) time. Adding and removing items from the queue will operate in worst-case O(logN) time.

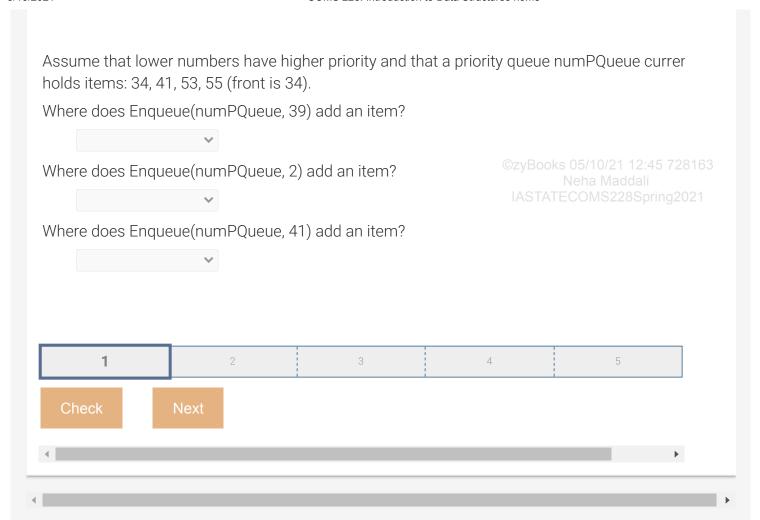
Table 8.4.2: Implementing priority queues with heaps.

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		T TOTAL TYTA GALL
Priority queue operation	Heap functionality used to implement operation	Worst-case runtime complexity
Enqueue	Insert	O(logN)
Dequeue	Remove	O(logN)

Peek	Return value in root node	0(1)
IsEmpty	Return true if no nodes in heap, false otherwise	O(1)
GetLength	Return number of nodes (expected to be stored in the heap's member data)	O(1)

	©zyBooks 05/10/21 12:45 728163
PARTICIPATION 8.4.6: Implementing priority queues with heaps.	Neha Maddali IASTATECOMS228Spring2021
 The Dequeue and Peek operations both return the value in the root, and therefore have the same worst-case runtime complexity. True False 	
2) When implementing a priority queue with a heap, no operation will have a runtime complexity worse than O(logN).O True	
O False	
 3) If items in a priority queue with a lower numerical value have higher priority, then a max-heap should be used to implement the priority queue. O True O False 	
4) A priority queue is always implemented using a heap.O True	
O False	©zyBooks 05/10/21 12:45 728163 Neha Maddali IASTATECOMS228Spring2021
CHALLENGE ACTIVITY 8.4.1: Priority queue abstract data type.	
Start	



8.5 Treaps

Treap basics

A BST built from inserts of N nodes having random-ordered keys stays well-balanced and thus has near-minimum height, meaning searches, inserts, and deletes are O(logN). Because insertion order may not be controllable, a data structure that somehow randomizes BST insertions is desirable. A **treap** uses a main key that maintains a binary search tree ordering property, and a secondary key generated randomly (often called "priority") during insertions that maintains a heap property. The combination usually keeps the tree balanced. The word "treap" is a mix of tree and heap. This section assumes the heap is a max-heap. Algorithms for basic treap operations/include5/10/21 12:45 728163

- A treap **search** is the same as a BST search using the main key, since the treap is a BST.²⁰²¹
- A treap *insert* initially inserts a node as in a BST using the main key, then assigns a random priority to the node, and percolates the node up until the heap property is not violated. In a heap, a node is moved up via a swap with the node's parent. In a treap, a node is moved up via a *rotation at the parent*. Unlike a swap, a rotation maintains the BST property.
- A treap delete can be done by setting the node's priority such that the node should be a leaf (-∞ for a max-heap), percolating the node down using rotations until the node is a leaf, and then

removing the node.

PARTICIPATION ACTIVITY

8.5.1: Treap insert: First insert as a BST, then randomly assign a priority and use rotations to percolate node up to maintain heap.

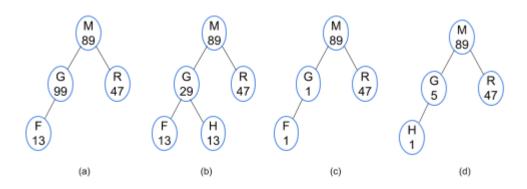
Animation captions:

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- 1. The keys maintain a BST, the priorities a heap. Insert B as a BST... Neha Maddali
- 2. Assign random priority (70). Rotate (which keep a BST) the node up until the priorities maintain a heap: 20 not > 70: Rotate. 47 not > 70: Rotate. 80 > 70: Done.

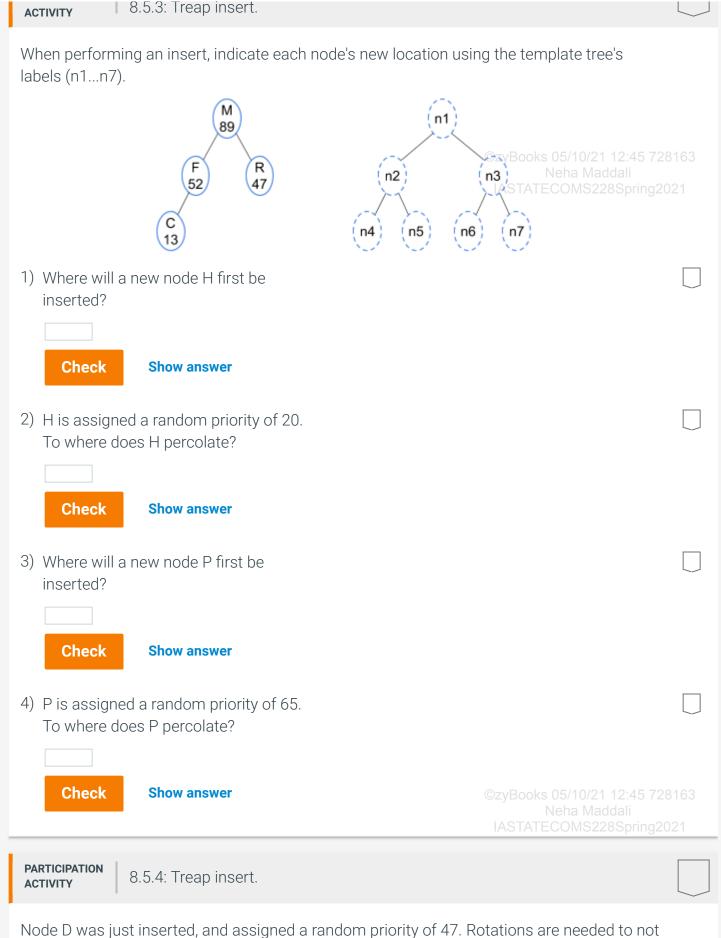
PARTICIPATION ACTIVITY

8.5.2: Recognizing treaps.

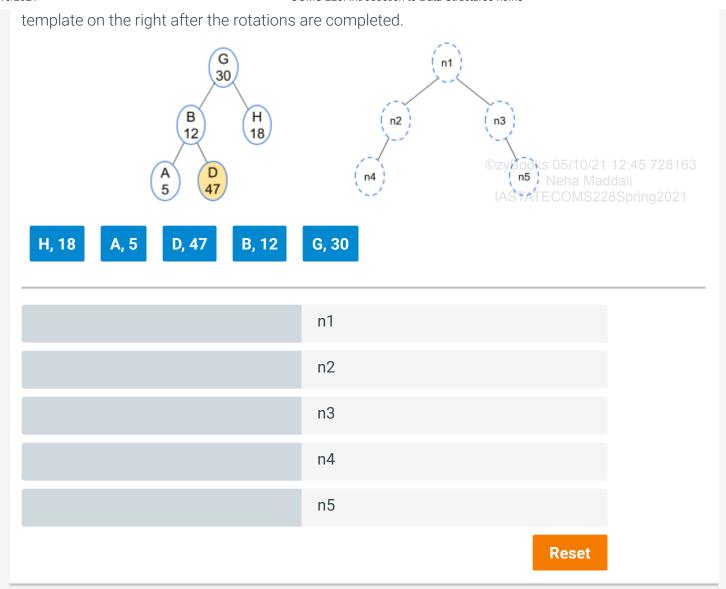


- 1) (a)
 - O Treap
 - O Not a treap
- 2) (b)
 - O Treap
 - O Not a treap
- 3) (c)
 - O Treap
 - O Not a treap
- 4) (d)
 - O Treap
 - O Not a treap

PARTICIPATION



violate the heap property. Match the node value to the corresponding location in the tree



Treap delete

A treap delete could be done by first doing a BST delete (copying the successor to the node-to-delete, then deleting the original successor), followed by percolating the node down until the heap property is not violated. However, a simpler approach just sets the node-to-delete's priority to -∞ (for a max-heap), percolates the node down until a leaf, and removes the node. Percolating the node down uses rotations, not swaps, to maintain the BST property. Also, the node is rotated in the direction of the lower-priority child, so that the node rotated up has a higher priority than that child, to keep the heap property.

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PARTICIPATION ACTIVITY 8.5.5: Treap delete: Set priority such that node must become a leaf, then ring 202 percolate down using rotations.

Animation captions:

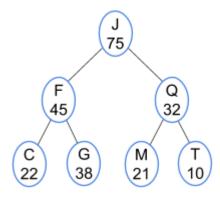
- 1. Node F is to be deleted. First set F's priority to -∞.
- 2. Rotate (to keep a BST) until the node becomes a leaf node. 29 > 13: Rotate right.

- 3. Rotate until node becomes a leaf node. Rotate left (the only option).
- 4. Remove leaf node.

PARTICIPATION ACTIVITY

8.5.6: Treap delete algorithm.

Each question starts from the original tree. Use this text notation for the tree (J (F (C,G), Q728163 (M, T))). A - means the child does not exist.



- 1) What is the tree after removing G?
 - \bigcirc (J (F (C, -), Q (M, T)))
 - O (J (C (-, F), Q (M, T)))
- 2) What is the tree after removing Q?
 - \bigcirc (J (F (C, G), M(-, T))
 - O (J (F (C, G), T(M, -))

PARTICIPATION ACTIVITY

8.5.7: Treaps.

- A treap's nodes have random main keys.
 - O True
 - O False
- 2) A treap's nodes have random priorities.
 - O True
 - O False
- 3) Suppose a treap is built by inserting nodes with main keys in this order: A, B, C, D, E, F, G. The treap will have 7 levels,

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with each level having one node with a right child.	
O True	
O False	

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