

Neha Maddali
ID: 110122037
Signature: Neha Maddali

Problem 1:

a)

	Best subset	forward	backward	Criteria value
M1	$Y \sim X_1$	$Y \sim X_1$	$Y \sim X_1$	AIC
M2	$Y \sim X_2 + X_4$	$Y \sim X_2 + X_4$	$Y \sim X_2 + X_4$	AIC
M3	$Y \sim X_1 + X_2 + X_3$	$Y \sim X_1 + X_2 + X_3$	$Y \sim X_1 + X_2 + X_3$	BIC
M4	$Y \sim X_1 + X_2 + X_3 + X_4$	$Y \sim X_1 + X_2 + X_3 + X_4$	$Y \sim X_1 + X_2 + X_3 + X_4$	AIC
Final model	$Y \sim X_1$	$Y \sim X_1$	$Y \sim X_1$	Adjusted R^2

- b) I think the student did a good job using the 10-fold CV to find the optimal tuning parameter. However, there is an alternative way. If a different training or test set or number of folds were selected for CV, the optimal λ and test error would also change. Instead, using the one-standard error rule can fix this issue. Instead of picking the λ that produces the smallest CV error, we pick the model whose CV error is within one standard error of the lowest point on the curve of the cross-validation error as a function of λ . This value would then be the $\lambda^{\text{ridge}_{1se}}$
- c) False. When $\lambda = 0$, the bias is small but there will be a higher variance. When $\lambda = \infty$ the variance is small but the bias is high
- d) True. Lasso is more flexible than least squares linear regression. Lasso will have a better prediction accuracy when its increase in variance is less than its decrease in bias

Problem 2:

```
glm(formula = chd ~ age, family = "binomial", data = heart)

Deviance Residuals:
    Min       1Q   Median       3Q      Max
-1.4321  -0.9215  -0.5392   1.0952   2.2433

Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -3.521710   0.416031  -8.465  < 2e-16 ***
age          0.064108   0.008532   7.513 5.76e-14 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 596.11  on 461  degrees of freedom
Residual deviance: 525.56  on 460  degrees of freedom
AIC: 529.56

Number of Fisher Scoring iterations: 4
```

a)

The maximum likelihood estimate of $b_0 = -3.521710$ and $b_1 = 0.064108$
 $\exp(\beta_0 + \beta_1 \cdot 462) / (1 + \exp(\beta_0 + \beta_1 \cdot 462)) = 1$

- b) Predicted probability = 0.4215756
- c) standard error = 0

```
B = 2000
n=462
medhat = rep(NA,2000)
for(b in 1:B){
  index = sample(1:n,n,replace=TRUE)
  bootstrap = heart[index,]
  medhat[b] = median(bootstrap$chd, na.rm=TRUE)
}
sqrt(sum((medhat-mean(medhat))^2)/(B-1))
```

- d) At the age of 55

Problem 3:

	101	102	103	104	105
0.61158280	0.11903050	0.17727017	0.08279173	0.17219104	
	106	107	108	109	110
0.62235930	0.53401573	0.38208696	0.33339837	0.05302398	

- a)
- First 10 predicted probabilities from training set
- b) Threshold of 0.4 gives us a misclassification rate of 0.3181

glm.pred	0	1
No	3	0
Yes	14	27

- c) Threshold of 0.5 gives us the smallest false positive rate. But the misclassification rate will then be 0.3421 which is larger than that of part b

glm.pred	0	1
No	3	2
Yes	11	22

- d) An issue is that regularized regression is often used to control for effects of other predictors. In this scenario, least squares/regularized regression are not appropriate because they are not built for classifying data points. Logistic regression performs a better job at classifying these data points and has a better logarithmic loss function