

Homework 3-1

- 1) (50 points) Derive the I/O costs of different join algorithms of relations R and S given the following variables, which you may or may not use all of them. Suppose that there is 1 page of results for the join. Ignore the CPU time cost. Please write down steps to explain your answer for full credits.

$|R|=20$: Number of tuples per page in R

$|S|=20$: Number of tuples per page in S

$M=120$: Number of pages in R

$N=40$: Number of pages in S

$B=10$: Number of available main memory in pages

- a) (10 points) What is the minimal I/O cost of block nested loop join?

Use R as the outer relation.

$$\text{Total cost} = M + [M/(B-2)] * N = 120 + (120 / (10-2)) * 40 = 720$$

Use S as the outer relation.

$$\text{Total cost} = N + [N/(B-2)] * M = 40 + (40 / (10-2)) * 120 = 640 \rightarrow \text{minimal cost}$$

- b) (10 points) What is the minimal I/O cost of simple nested loop join?

Use R as the outer relation

$$\text{Total cost} = M + M * P_R * N = 120 + 120 * 20 * 40 = 96,120$$

Use S as the outer relation

$$\text{Total cost} = N + N * P_S * M = 40 + 40 * 20 * 120 = 96,040 \rightarrow \text{minimal cost}$$

- c) (10 points) What is the minimal I/O cost of indexed nested Loops Join? (Suppose the cost of retrieving a matching tuple is 3, for both R and S)

Use R as the outer relation

$$\text{Total cost} = M + M * P_R * (\text{cost of retrieve}) = 120 + 120 * 20 * 3 = 7,320$$

Use S as the outer relation

$$\text{Total cost} = N + N * P_S * (\text{cost of retrieve}) = 40 + 40 * 20 * 3 = 2,440 \rightarrow \text{minimal cost}$$

- d) (10 points) What is the minimal I/O cost of grace hash join?

Each partition fits in the B-2 pages

I/O cost for a read and write is the same

Ignore the cost of writing the join results

$$\text{Total cost} = 3 * (120 + 40) = 480$$

- e) (10 points) What is the minimal I/O cost of Sort-Merge Join? (Suppose the join is on their primary keys which are sorted already)

$$\text{Total cost} = M + N = 120 + 40 = 160$$

Submission Instruction

Please use Microsoft Words or other tools to type your answer. Don't handwrite. Submit your work in pdf through your Canvas account.