

”ChiRV(3)”

$$[x \mapsto \frac{x^2 e^{-1/2 x^2} \sqrt{2}}{\sqrt{\pi}}]$$

$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = 1/2 \frac{\sqrt{x} \sqrt{2} e^{-x/2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = \frac{\operatorname{erf}\left(\frac{1}{2} \sqrt{x} \sqrt{2}\right) \sqrt{\pi} - \sqrt{x} \sqrt{2} e^{-x/2}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -\frac{-\sqrt{x} \sqrt{2} e^{-x/2} + \operatorname{erf}\left(\frac{1}{2} \sqrt{x} \sqrt{2}\right) \sqrt{\pi} - \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{x} \sqrt{2} e^{-x/2}}{-\sqrt{x} \sqrt{2} e^{-x/2} + \operatorname{erf}\left(\frac{1}{2} \sqrt{x} \sqrt{2}\right) \sqrt{\pi} - \sqrt{\pi}}$$

Mean

$$\mu = 3$$

Variance

$$\sigma^2 = 6$$

Moment Function

$$m(x) = 1/2 \frac{\sqrt{2} \Gamma(r + 3/2) (1/2)^{-r-3/2}}{\sqrt{\pi}}$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} - \frac{\sqrt{x} e^{1/2 x (2t-1)} \sqrt{2} \sqrt{1-2t} - \sqrt{\pi} \operatorname{erf} \left(1/2 \sqrt{2} \sqrt{1-2t} \sqrt{x} \right)}{(1-2t)^{3/2} \sqrt{\pi}} \quad 1$$

$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x) = 2 \frac{x^5 e^{-1/2 x^4} \sqrt{2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = - \frac{x^2 \sqrt{2} e^{-1/2 x^4} - \sqrt{\pi} \operatorname{erf} \left(1/2 x^2 \sqrt{2} \right)}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf} \left(-Z^2 \sqrt{2} e^{-1/2 -Z^4} - \sqrt{\pi} \operatorname{erf} \left(1/2 -Z^2 \sqrt{2} \right) + s \sqrt{\pi} \right)]$$

Survivor Function

$$S(x) = \frac{x^2 \sqrt{2} e^{-1/2 x^4} - \sqrt{\pi} \operatorname{erf} \left(1/2 x^2 \sqrt{2} \right) + \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = 2 \frac{x^5 e^{-1/2 x^4} \sqrt{2}}{x^2 \sqrt{2} e^{-1/2 x^4} - \sqrt{\pi} \operatorname{erf} \left(1/2 x^2 \sqrt{2} \right) + \sqrt{\pi}}$$

Mean

$$\mu = 3/2 \frac{\sqrt[4]{2} \Gamma(3/4)}{\sqrt{\pi}}$$

Variance

$$\sigma^2 = 1/4 \frac{\sqrt{2} \left(-9 \left(\Gamma(3/4) \right)^2 \sqrt{\pi} + 8 \pi \right)}{\pi^{3/2}}$$

Moment Function

$$m(x) = \frac{2^{1+r/4} \Gamma(r/4 + 3/2)}{\sqrt{\pi}}$$

Moment Generating Function

$$1/24 \frac{1}{\sqrt{\pi}\Gamma(3/4)} \left(5 \pi {}_1F_3(9/4; 5/4, 3/2, 7/4; \frac{t^4}{128}) \sqrt[4]{2} t^3 + 24 \sqrt{2} \Gamma(3/4) {}_1F_3(2; 3/4, 5/4, 3/2; \frac{t^4}{128}) \right)$$

$$t \mapsto t^{-1}$$

Probability Distribution Function

$$f(x) = \frac{\sqrt{2}}{x^4 \sqrt{\pi}} e^{-1/2 x^{-2}}$$

Cumulative Distribution Function

$$F(x) = \frac{1}{x \sqrt{\pi}} \left(-\sqrt{\pi} \operatorname{erf} \left(1/2 \frac{\sqrt{2}}{x} \right) x + x \sqrt{\pi} + \sqrt{2} e^{-1/2 x^{-2}} \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = -\frac{1}{x \sqrt{\pi}} \left(-\sqrt{\pi} \operatorname{erf} \left(1/2 \frac{\sqrt{2}}{x} \right) x + \sqrt{2} e^{-1/2 x^{-2}} \right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2}}{x^3} e^{-1/2 x^{-2}} \left(-\sqrt{\pi} \operatorname{erf} \left(1/2 \frac{\sqrt{2}}{x} \right) x + \sqrt{2} e^{-1/2 x^{-2}} \right)^{-1}$$

Mean

$$mu = \frac{\sqrt{2}}{\sqrt{\pi}}$$

Variance

$$sigma^2 = 1 - 2 \pi^{-1}$$

Moment Function

$$m(x) = \frac{2^{1-r/2} \Gamma(-r/2 + 3/2)}{\sqrt{\pi}}$$

Moment Generating Function

$$2 \frac{G_{0,3}^{3,0} \left(1/8 t^2 \mid 3/2, 1/2, 0 \right)}{\pi}$$

$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = \frac{\sqrt{2} (\sin(x))^2}{\sqrt{\pi} (\cos(x))^4} e^{-1/2 \frac{(\sin(x))^2}{(\cos(x))^2}}$$

Cumulative Distribution Function

$$F(x) = \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{(\sin(t))^2}{(\cos(t))^4} e^{-1/2 \frac{(\sin(t))^2}{(\cos(t))^2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -\frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{(\sin(t))^2}{(\cos(t))^4} e^{-1/2 \frac{(\sin(t))^2}{(\cos(t))^2}} dt - \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2} (\sin(x))^2}{(\cos(x))^4} e^{-1/2 \frac{(\sin(x))^2}{(\cos(x))^2}} \left(\sqrt{2} \int_0^x \frac{(\sin(t))^2}{(\cos(t))^4} e^{-1/2 \frac{(\sin(t))^2}{(\cos(t))^2}} dt - \sqrt{\pi} \right)^{-1}$$

Mean

$$mu = -2 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\pi/2} \frac{x (-1 + \cos(2x))}{(\cos(2x) + 1)^2} e^{1/2 \frac{-1 + \cos(2x)}{\cos(2x) + 1}} dx$$

Variance

$$sigma^2 = -2 \frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_0^{\pi/2} \frac{x^2 (-1 + \cos(2x))}{(\cos(2x) + 1)^2} e^{1/2 \frac{-1 + \cos(2x)}{\cos(2x) + 1}} dx \pi + 4 \left(\int_0^{\pi/2} \frac{x (-1 + \cos(2x))}{(\cos(2x) + 1)^2} e^{1/2 \frac{-1 + \cos(2x)}{\cos(2x) + 1}} dx \right)^2 \right)$$

Moment Function

$$m(x) = \int_0^{\pi/2} \frac{x^r \sqrt{2} (\sin(x))^2}{(\cos(x))^4 \sqrt{\pi}} e^{-1/2 \frac{(\sin(x))^2}{(\cos(x))^2}} dx$$

Moment Generating Function

$$-2 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\pi/2} \frac{-1 + \cos(2x)}{(\cos(2x) + 1)^2} e^{1/2 \frac{2tx \cos(2x) + 2tx + \cos(2x) - 1}{\cos(2x) + 1}} dx$$

1

$$t \mapsto e^t$$

Probability Distribution Function

$$f(x) = \frac{(\ln(x))^2 e^{-1/2 (\ln(x))^2} \sqrt{2}}{x \sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = -\frac{\ln(x) \sqrt{2} e^{-1/2 (\ln(x))^2} - \operatorname{erf}(1/2 \ln(x) \sqrt{2}) \sqrt{\pi}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = \frac{\ln(x) \sqrt{2} e^{-1/2 (\ln(x))^2} - \operatorname{erf}(1/2 \ln(x) \sqrt{2}) \sqrt{\pi} + \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = \frac{(\ln(x))^2 e^{-1/2 (\ln(x))^2} \sqrt{2}}{x (\ln(x) \sqrt{2} e^{-1/2 (\ln(x))^2} - \operatorname{erf}(1/2 \ln(x) \sqrt{2}) \sqrt{\pi} + \sqrt{\pi})}$$

Mean

$$mu = \frac{2 \sqrt{\pi} e^{1/2} + 2 \sqrt{\pi} e^{1/2} \operatorname{erf}(1/2 \sqrt{2}) + \sqrt{2}}{\sqrt{\pi}}$$

Variance

$$\sigma^2 = -\frac{4e(\operatorname{erf}(1/2\sqrt{2}))^2\pi^{3/2} + 8e\operatorname{erf}(1/2\sqrt{2})\pi^{3/2} + 4\sqrt{2}e^{1/2}\operatorname{erf}(1/2\sqrt{2})\pi + 4e\pi^{3/2} - 5}{\pi^{3/2}}$$

Moment Function

$$m(x) = \frac{\sqrt{2}\left(r + 1/2r^2\sqrt{\pi}e^{1/2r^2}\sqrt{2}\operatorname{erf}(1/2r\sqrt{2}) + 1/2\sqrt{\pi}e^{1/2r^2}\sqrt{2}\operatorname{erf}(1/2r\sqrt{2}) + 1/2r^2\sqrt{\pi}e^{1/2r^2}\right)}{\sqrt{\pi}}$$

Moment Generating Function

$$\int_1^\infty \frac{(\ln(x))^2 \sqrt{2}e^{tx-1/2(\ln(x))^2}}{x\sqrt{\pi}} dx_1$$

$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = \frac{e^{3x-1/2e^{2x}}\sqrt{2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = 1/2 \frac{\sqrt{2}\left(\sqrt{\pi}\sqrt{2}\operatorname{erf}(1/2\sqrt{2}e^x) - 2e^{x-1/2e^{2x}}\right)}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf}\left(-e^{2-Z} + \ln(2) - \ln(\pi) - \ln\left(\left(-s + \operatorname{erf}\left(1/2\sqrt{2}e^{-Z}\right)\right)^2\right) + 2-Z\right)]$$

Survivor Function

$$S(x) = \frac{\sqrt{2}e^{x-1/2e^{2x}} - \sqrt{\pi}\operatorname{erf}(1/2\sqrt{2}e^x) + \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = \frac{e^{3x-1/2e^{2x}}\sqrt{2}}{\sqrt{2}e^{x-1/2e^{2x}} - \sqrt{\pi}\operatorname{erf}(1/2\sqrt{2}e^x) + \sqrt{\pi}}$$

Mean

$$\mu = \int_{-\infty}^{\infty} \frac{x e^{3x-1/2 e^{2x}} \sqrt{2}}{\sqrt{\pi}} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} \frac{x^2 e^{3x-1/2 e^{2x}} \sqrt{2}}{\sqrt{\pi}} dx - \left(\int_{-\infty}^{\infty} \frac{x e^{3x-1/2 e^{2x}} \sqrt{2}}{\sqrt{\pi}} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} \frac{x^r e^{3x-1/2 e^{2x}} \sqrt{2}}{\sqrt{\pi}} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} \frac{\sqrt{2} e^{tx+3x-1/2 e^{2x}}}{\sqrt{\pi}} dx_1$$

$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = \frac{(\ln(x))^2 e^{-1/2 (\ln(x))^2} \sqrt{2}}{x \sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = -\frac{\ln(x) \sqrt{2} e^{-1/2 (\ln(x))^2} - \operatorname{erf}\left(\frac{1}{2} \ln(x) \sqrt{2}\right) \sqrt{\pi} - \sqrt{\pi}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = \frac{\ln(x) \sqrt{2} e^{-1/2 (\ln(x))^2} - \operatorname{erf}\left(\frac{1}{2} \ln(x) \sqrt{2}\right) \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = \frac{(\ln(x))^2 e^{-1/2 (\ln(x))^2} \sqrt{2}}{x (\ln(x) \sqrt{2} e^{-1/2 (\ln(x))^2} - \operatorname{erf}\left(\frac{1}{2} \ln(x) \sqrt{2}\right) \sqrt{\pi})}$$

Mean

$$\mu = -\frac{2\sqrt{\pi}\operatorname{erf}\left(\frac{1}{2}\sqrt{2}\right)e^{1/2}-2\sqrt{\pi}e^{1/2}+\sqrt{2}}{\sqrt{\pi}}$$

Variance

$$\sigma^2 = -\frac{4e\left(\operatorname{erf}\left(\frac{1}{2}\sqrt{2}\right)\right)^2\pi^{3/2}-8e\operatorname{erf}\left(\frac{1}{2}\sqrt{2}\right)\pi^{3/2}+4\sqrt{2}e^{1/2}\operatorname{erf}\left(\frac{1}{2}\sqrt{2}\right)\pi+4e\pi^{3/2}+5}{\pi^{3/2}}$$

Moment Function

$$m(x) = \frac{\sqrt{2}\left(-r-\frac{1}{2}r^2\sqrt{\pi}e^{1/2}r^2\sqrt{2}\operatorname{erf}\left(\frac{1}{2}r\sqrt{2}\right)-\frac{1}{2}\sqrt{\pi}e^{1/2}r^2\sqrt{2}\operatorname{erf}\left(\frac{1}{2}r\sqrt{2}\right)+\frac{1}{2}r^2\sqrt{\pi}\right)}{\sqrt{\pi}}$$

Moment Generating Function

$$\frac{\sqrt{2}}{\sqrt{\pi}}\int_0^1\frac{\left(\ln\left(x\right)\right)^2e^{tx-1/2\left(\ln\left(x\right)\right)^2}}{x}dx$$

$$t\mapsto -\ln\left(t\right)$$

Probability Distribution Function

$$f(x) = \frac{e^{-1/2e^{-2x}-3x}\sqrt{2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = \frac{-\sqrt{\pi}\operatorname{erf}\left(\frac{1}{2}\sqrt{2}e^{-x}\right)+\sqrt{2}e^{-1/2e^{-2x}-x}+\sqrt{\pi}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1}=\left[s\mapsto RootOf\left(e^{2-Z}\ln\left(\left(s+\operatorname{erf}\left(\frac{1}{2}\sqrt{2}e^{-Z}\right)-1\right)^2\right)-e^{2-Z}\ln\left(2\right)+e^{2-Z}\ln\left(\pi\right)+2-Z\right)\right]$$

Survivor Function

$$S(x) = -\frac{-\sqrt{\pi}\operatorname{erf}\left(\frac{1}{2}\sqrt{2}e^{-x}\right)+\sqrt{2}e^{-1/2e^{-2x}-x}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = -\frac{e^{-1/2}e^{-2x-3x}\sqrt{2}}{-\sqrt{\pi}\operatorname{erf}\left(1/2\sqrt{2}e^{-x}\right) + \sqrt{2}e^{-1/2}e^{-2x-x}}$$

Mean

$$mu = \int_{-\infty}^{\infty} \frac{xe^{-1/2}e^{-2x-3x}\sqrt{2}}{\sqrt{\pi}} dx$$

Variance

$$sigma^2 = \int_{-\infty}^{\infty} \frac{x^2e^{-1/2}e^{-2x-3x}\sqrt{2}}{\sqrt{\pi}} dx - \left(\int_{-\infty}^{\infty} \frac{xe^{-1/2}e^{-2x-3x}\sqrt{2}}{\sqrt{\pi}} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} \frac{x^r e^{-1/2}e^{-2x-3x}\sqrt{2}}{\sqrt{\pi}} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} \frac{\sqrt{2}e^{tx-1/2}e^{-2x-3x}}{\sqrt{\pi}} dx_1$$

$$t \mapsto \ln(t+1)$$

Probability Distribution Function

$$f(x) = \frac{(e^x - 1)^2 e^{-1/2}e^{2x+e^x-1/2+x}\sqrt{2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = -\frac{\left(-\operatorname{erf}\left(1/2\sqrt{2}\left(e^x-1\right)\right)e^{1/2}e^{2x}\sqrt{\pi} + \sqrt{2}e^{x+e^x-1/2} - \sqrt{2}e^{e^x-1/2}\right)e^{-1/2}e^{2x}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf}\left(-e^{2-Z} + 2e^{-Z} + \ln(2) - 2\ln\left(\sqrt{\pi}\operatorname{erf}\left(1/2\sqrt{2}\left(e^{-Z}-1\right)\right) + \sqrt{2}e^{-1/2}\left(e^{-Z}-1\right)\right)\right)]$$

Survivor Function

$$S(x) = -\frac{\operatorname{erf}\left(\frac{1}{2}\sqrt{2}\left(e^x - 1\right)\right)\sqrt{\pi} - \sqrt{2}e^{-1/2}e^{2x+e^x-1/2+x} + \sqrt{2}e^{e^x-1/2-1/2}e^{2x} - \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = \frac{(e^x - 1)^2 e^{-1/2}e^{2x+e^x-1/2+x}\sqrt{2}}{-\operatorname{erf}\left(\frac{1}{2}\sqrt{2}\left(e^x - 1\right)\right)\sqrt{\pi} + \sqrt{2}e^{-1/2}e^{2x+e^x-1/2+x} - \sqrt{2}e^{e^x-1/2-1/2}e^{2x} + \sqrt{\pi}}$$

Mean

$$mu = \int_0^\infty \frac{x(e^x - 1)^2 e^{-1/2}e^{2x+e^x-1/2+x}\sqrt{2}}{\sqrt{\pi}} dx$$

Variance

$$sigma^2 = \int_0^\infty \frac{x^2(e^x - 1)^2 e^{-1/2}e^{2x+e^x-1/2+x}\sqrt{2}}{\sqrt{\pi}} dx - \left(\int_0^\infty \frac{x(e^x - 1)^2 e^{-1/2}e^{2x+e^x-1/2+x}\sqrt{2}}{\sqrt{\pi}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty \frac{x^r(e^x - 1)^2 e^{-1/2}e^{2x+e^x-1/2+x}\sqrt{2}}{\sqrt{\pi}} dx$$

Moment Generating Function

$$\int_0^\infty \frac{(e^x - 1)^2 \sqrt{2}e^{tx-1/2}e^{2x+e^x-1/2+x}}{\sqrt{\pi}} dx_1$$

$$t \mapsto (\ln(t + 2))^{-1}$$

Probability Distribution Function

$$f(x) = \frac{\left(e^{x^{-1}} - 2\right)^2 \sqrt{2}}{\sqrt{\pi}x^2} e^{-1/2}e^{\frac{1}{x}\left(e^{2x^{-1}}x - 4e^{x^{-1}}x + 4x - 2\right)}$$

Cumulative Distribution Function

$$F(x) = \frac{1}{\sqrt{\pi}} \left(-\sqrt{\pi} \operatorname{erf}\left(\frac{1}{2}\sqrt{2}\left(e^{x^{-1}} - 2\right)\right) e^{1/2}e^{2x^{-1}} + \sqrt{2}e^{\frac{2e^{x^{-1}}x - 2x + 1}{x}} - 2\sqrt{2}e^{2e^{x^{-1}} - 2} + e^{1/2}e^{2x^{-1}} \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -2 \left(-e^{\frac{2 \operatorname{RootOf}\left(-e^{2-Z} + \ln(2) - 2 \ln\left(2\sqrt{2}e^{-1/2}\left(e^{-Z}-2\right)^2 + s\sqrt{\pi} + \sqrt{\pi}\operatorname{erf}\left(1/2\sqrt{2}\left(e^{-Z}-2\right)\right) - \sqrt{\pi}\right) + 4e^{-Z} + 2}{s}}\right)} \right)$$

Survivor Function

$$S(x) = \frac{1}{\sqrt{\pi}} \left(\sqrt{\pi} \operatorname{erf}\left(1/2\sqrt{2}\left(e^{x^{-1}}-2\right)\right) - \sqrt{2}e^{-1/2\frac{1}{x}\left(e^{2x^{-1}}x-4e^{x^{-1}}x+4x-2\right)} + 2\sqrt{2}e^{2e^{x^{-1}}-2-1/2e^{2x^{-1}}x-4x+2}\right)$$

Hazard Function

$$h(x) = -\frac{\left(e^{x^{-1}}-2\right)^2\sqrt{2}}{x^2}e^{1/2\frac{1}{x}\left(4e^{x^{-1}}x-e^{2x^{-1}}x-4x+2\right)}\left(\sqrt{2}e^{1/2\frac{1}{x}\left(4e^{x^{-1}}x-e^{2x^{-1}}x-4x+2\right)}-2\sqrt{2}e^{2e^{x^{-1}}-2-1/2e^{2x^{-1}}x-4x+2}\right)$$

Mean

$$mu = \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{(\ln(2))^{-1}} \frac{\left(e^{x^{-1}}-2\right)^2}{x} e^{1/2\frac{1}{x}\left(4e^{x^{-1}}x-e^{2x^{-1}}x-4x+2\right)} dx$$

Variance

$$sigma^2 = \frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_0^{(\ln(2))^{-1}} \left(e^{x^{-1}}-2\right)^2 e^{1/2\frac{1}{x}\left(4e^{x^{-1}}x-e^{2x^{-1}}x-4x+2\right)} dx \pi - 2 \left(\int_0^{(\ln(2))^{-1}} \frac{\left(e^{x^{-1}}-2\right)^2}{x} e^{1/2\frac{1}{x}\left(4e^{x^{-1}}x-e^{2x^{-1}}x-4x+2\right)} dx \right) \right)$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} \frac{x^r \left(e^{x^{-1}}-2\right)^2 \sqrt{2}}{\sqrt{\pi} x^2} e^{-1/2\frac{1}{x}\left(e^{2x^{-1}}x-4e^{x^{-1}}x+4x-2\right)} dx$$

Moment Generating Function

$$\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{(\ln(2))^{-1}} \frac{\left(e^{x^{-1}}-2\right)^2}{x^2} e^{1/2\frac{1}{x}\left(-e^{2x^{-1}}x+2tx^2+4e^{x^{-1}}x-4x+2\right)} dx$$

1

$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = -\frac{(\operatorname{arctanh}(x))^2 e^{-1/2(\operatorname{arctanh}(x))^2} \sqrt{2}}{\sqrt{\pi}(x^2 - 1)}$$

Cumulative Distribution Function

$$F(x) = -\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{(\operatorname{arctanh}(t))^2 e^{-1/2(\operatorname{arctanh}(t))^2}}{t^2 - 1} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = \frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{(\operatorname{arctanh}(t))^2 e^{-1/2(\operatorname{arctanh}(t))^2}}{t^2 - 1} dt + \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{(\operatorname{arctanh}(x))^2 e^{-1/2(\operatorname{arctanh}(x))^2} \sqrt{2}}{x^2 - 1} \left(\sqrt{2} \int_0^x \frac{(\operatorname{arctanh}(t))^2 e^{-1/2(\operatorname{arctanh}(t))^2}}{t^2 - 1} dt + \sqrt{\pi} \right)^{-1}$$

Mean

$$mu = -\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{x (\operatorname{arctanh}(x))^2 e^{-1/2(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx$$

Variance

$$sigma^2 = -\frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_0^1 \frac{x^2 (\operatorname{arctanh}(x))^2 e^{-1/2(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx \pi + 2 \left(\int_0^1 \frac{x (\operatorname{arctanh}(x))^2 e^{-1/2(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx \right)^2 \right)$$

Moment Function

$$m(x) = \int_0^1 -\frac{x^r (\operatorname{arctanh}(x))^2 e^{-1/2(\operatorname{arctanh}(x))^2} \sqrt{2}}{\sqrt{\pi}(x^2 - 1)} dx$$

Moment Generating Function

$$-\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{(\operatorname{arctanh}(x))^2 e^{tx-1/2(\operatorname{arctanh}(x))^2}}{x^2-1} dx$$

$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = \frac{(\operatorname{arcsinh}(x))^2 e^{-1/2(\operatorname{arcsinh}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2+1}}$$

Cumulative Distribution Function

$$F(x) = \frac{-\sqrt{\pi} \operatorname{erf}\left(\frac{1}{2} \ln(-x + \sqrt{x^2+1}) \sqrt{2}\right) + \ln(-x + \sqrt{x^2+1}) \sqrt{2} e^{-1/2(\ln(-x + \sqrt{x^2+1}))^2}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = -\frac{\ln(-x + \sqrt{x^2+1}) \sqrt{2} e^{-1/2(\ln(-x + \sqrt{x^2+1}))^2} - \sqrt{\pi} \operatorname{erf}\left(\frac{1}{2} \ln(-x + \sqrt{x^2+1}) \sqrt{2}\right) - \sqrt{\pi}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = -\frac{(\operatorname{arcsinh}(x))^2 e^{-1/2(\operatorname{arcsinh}(x))^2} \sqrt{2}}{\sqrt{x^2+1} \left(\ln(-x + \sqrt{x^2+1}) \sqrt{2} e^{-1/2(\ln(-x + \sqrt{x^2+1}))^2} - \sqrt{\pi} \operatorname{erf}\left(\frac{1}{2} \ln(-x + \sqrt{x^2+1}) \sqrt{2}\right) \right)}$$

Mean

$$mu = \int_0^\infty \frac{x (\operatorname{arcsinh}(x))^2 e^{-1/2(\operatorname{arcsinh}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2+1}} dx$$

Variance

$$sigma^2 = \int_0^\infty \frac{x^2 (\operatorname{arcsinh}(x))^2 e^{-1/2(\operatorname{arcsinh}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2+1}} dx - \left(\int_0^\infty \frac{x (\operatorname{arcsinh}(x))^2 e^{-1/2(\operatorname{arcsinh}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2+1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty \frac{x^r (\operatorname{arcsinh}(x))^2 e^{-1/2 (\operatorname{arcsinh}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 + 1}} dx$$

Moment Generating Function

$$\int_0^\infty \frac{(\operatorname{arcsinh}(x))^2 \sqrt{2} e^{tx - 1/2 (\operatorname{arcsinh}(x))^2}}{\sqrt{\pi} \sqrt{x^2 + 1}} dx_1$$

$$t \mapsto \operatorname{arcsinh}(t)$$

Probability Distribution Function

$$f(x) = \frac{(\sinh(x))^2 e^{-1/2 (\sinh(x))^2} \sqrt{2} \cosh(x)}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = 1/2 \frac{\left(2 \sqrt{\pi} \operatorname{erf}\left(1/4 \sqrt{2} (e^x - e^{-x})\right) e^{1/8 (e^{4x} + 8 x e^{2x} + 1) e^{-2x}} - \sqrt{2} e^{1/4 + 2x} + \sqrt{2} e^{1/4} \right) e^{-1/8 (e^{4x} + 8 x e^{2x} + 1) e^{-2x}}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf}\left(e^{4-Z} + 4 e^{2-Z} \ln\left(\frac{(s + \operatorname{erf}(1/4 \sqrt{2} (-e^{-Z} + e^{-Z})))^2}{(e^{2-Z} - 1)^2}\right) + 4 e^{2-Z} \ln(\pi) + 4\right)]$$

Survivor Function

$$S(x) = -1/2 \frac{\sqrt{2} e^{-1/8 (e^{4x} + 8 x e^{2x} - 2 e^{2x} + 1) e^{-2x}} - \sqrt{2} e^{-1/8 (e^{4x} - 8 x e^{2x} - 2 e^{2x} + 1) e^{-2x}} + 2 \sqrt{\pi} \operatorname{erf}(1/4 \sqrt{2} (e^x - e^{-x}))}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = 2 \frac{(\sinh(x))^2 e^{-1/2 (\sinh(x))^2} \sqrt{2} \cosh(x)}{\sqrt{2} e^{-1/8 (e^{4x} - 8 x e^{2x} - 2 e^{2x} + 1) e^{-2x}} - \sqrt{2} e^{-1/8 (e^{4x} + 8 x e^{2x} - 2 e^{2x} + 1) e^{-2x}} - 2 \sqrt{\pi} \operatorname{erf}(1/4 \sqrt{2} (e^x - e^{-x}))}$$

Mean

$$mu = \int_0^\infty \frac{e^{1/4 - 1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2} x}{\sqrt{\pi}} dx$$

Variance

$$\sigma^2 = \int_0^\infty \frac{e^{1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2} x^2}{\sqrt{\pi}} dx - \left(\int_0^\infty \frac{e^{1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x)}{\sqrt{\pi}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty \frac{x^r (\sinh(x))^2 e^{-1/2 (\sinh(x))^2} \sqrt{2} \cosh(x)}{\sqrt{\pi}} dx$$

Moment Generating Function

$$\int_0^\infty \frac{e^{tx+1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2}}{\sqrt{\pi}} dx_1$$

$$t \mapsto \operatorname{csch}(t+1)$$

Probability Distribution Function

$$f(x) = \frac{(-1 + \operatorname{arccsch}(x))^2 e^{-1/2 (-1 + \operatorname{arccsch}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{(-1 + \operatorname{arccsch}(t))^2 e^{-1/2 (-1 + \operatorname{arccsch}(t))^2}}{\sqrt{t^2 + 1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -\frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{(-1 + \operatorname{arccsch}(t))^2 e^{-1/2 (-1 + \operatorname{arccsch}(t))^2}}{\sqrt{t^2 + 1} |t|} dt - \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{(-1 + \operatorname{arccsch}(x))^2 e^{-1/2 (-1 + \operatorname{arccsch}(x))^2} \sqrt{2}}{\sqrt{x^2 + 1} |x|} \left(\sqrt{2} \int_0^x \frac{(-1 + \operatorname{arccsch}(t))^2 e^{-1/2 (-1 + \operatorname{arccsch}(t))^2}}{\sqrt{t^2 + 1} |t|} dt \right)$$

Mean

$$\mu = \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{2^{\frac{e}{e^2-1}}} \frac{(-1 + \operatorname{arccsch}(x))^2 e^{-1/2(-1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2+1}} dx$$

Variance

$$\sigma^2 = -\frac{1}{\pi^{3/2}} \left(2 \left(\int_0^{2^{\frac{e}{e^2-1}}} \frac{(-1 + \operatorname{arccsch}(x))^2 e^{-1/2(-1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2+1}} dx \right)^2 \sqrt{\pi} - \sqrt{2} \int_0^{2^{\frac{e}{e^2-1}}} \frac{x(-1 + \operatorname{arccsch}(x))^2 e^{-1/2(-1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2+1}} dx \right)$$

Moment Function

$$m(x) = \int_0^{-2(-e+e^{-1})^{-1}} \frac{x^r (-1 + \operatorname{arccsch}(x))^2 e^{-1/2(-1+\operatorname{arccsch}(x))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2+1} |x|} dx$$

Moment Generating Function

$$\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{2^{\frac{e}{e^2-1}}} \frac{(-1 + \operatorname{arccsch}(x))^2 e^{-1/2(\operatorname{arccsch}(x))^2+tx+\operatorname{arccsch}(x)-1/2}}{x \sqrt{x^2+1}} dx$$

$$t \mapsto \operatorname{arccsch}(t+1)$$

Probability Distribution Function

$$f(x) = \frac{\sqrt{2} ((\cosh(x))^2 - 2 \sinh(x)) \cosh(x)}{\sqrt{\pi} (\sinh(x))^4} e^{-1/2 \frac{(\sinh(x)-1)^2}{(\sinh(x))^2}}$$

Cumulative Distribution Function

$$F(x) = -\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{(-(\cosh(t))^2 + 2 \sinh(t)) \cosh(t)}{(\sinh(t))^4} e^{-1/2 \frac{(\sinh(t)-1)^2}{(\sinh(t))^2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = \frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{(-(\cosh(t))^2 + 2 \sinh(t)) \cosh(t)}{(\sinh(t))^4} e^{-1/2 \frac{(\sinh(t)-1)^2}{(\sinh(t))^2}} dt + \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2} ((\cosh(x))^2 - 2 \sinh(x)) \cosh(x)}{(\sinh(x))^4} e^{-1/2 \frac{(\sinh(x)-1)^2}{(\sinh(x))^2}} \left(\sqrt{2} \int_0^x \frac{-(\cosh(t))^2 + 2 \sinh(t)}{(\sinh(t))^4} dt \right)$$

Mean

$$\mu = -4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) (-(\cosh(x))^2 + 2 \sinh(x)) x}{(-1 + \cosh(2x))^2} e^{\frac{-(\cosh(x))^2 + 2 \sinh(x)}{-1 + \cosh(2x)}} dx$$

Variance

$$\sigma^2 = 4 \frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) (-(\cosh(x))^2 + 2 \sinh(x)) x^2}{(-1 + \cosh(2x))^2} e^{\frac{-(\cosh(x))^2 + 2 \sinh(x)}{-1 + \cosh(2x)}} dx \pi - \mu^2 \right)$$

Moment Function

$$m(x) = \int_0^{\ln(1+\sqrt{2})} \frac{x^r \sqrt{2} ((\cosh(x))^2 - 2 \sinh(x)) \cosh(x)}{\sqrt{\pi} (\sinh(x))^4} e^{-1/2 \frac{(\sinh(x)-1)^2}{(\sinh(x))^2}} dx$$

Moment Generating Function

$$-4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) (-(\cosh(x))^2 + 2 \sinh(x))}{(-1 + \cosh(2x))^2} e^{\frac{2(\cosh(x))^2 tx - (\cosh(x))^2 - 2tx + 2 \sinh(x)}{-1 + \cosh(2x)}} dx$$

1

$$t \mapsto (\tanh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = \frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2 (-1 + \operatorname{arctanh}(x^{-1}))^2} \sqrt{2}}{\sqrt{\pi} (x^2 - 1)}$$

Cumulative Distribution Function

$$F(x) = \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^x \frac{(-1 + \operatorname{arctanh}(t^{-1}))^2 e^{-1/2 (-1 + \operatorname{arctanh}(t^{-1}))^2}}{t^2 - 1} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -\frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_1^x \frac{(-1 + \operatorname{arctanh}(t^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(t^{-1}))^2}{t^2 - 1} dt - \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(x^{-1}))^2 \sqrt{2}}{x^2 - 1} \left(\sqrt{2} \int_1^x \frac{(-1 + \operatorname{arctanh}(t^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(t^{-1}))^2}{t^2 - 1} dt - \sqrt{\pi} \right)$$

Mean

$$mu = \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^{\frac{e^2+1}{e^2-1}} x \frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(x^{-1}))^2}{x^2 - 1} dx$$

Variance

$$sigma^2 = \frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_1^{\frac{e^2+1}{e^2-1}} x^2 \frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(x^{-1}))^2}{x^2 - 1} dx \pi - 2 \left(\int_1^{\frac{e^2+1}{e^2-1}} x \frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(x^{-1}))^2}{x^2 - 1} dx \right)^2 \right)$$

Moment Function

$$m(x) = \int_1^{\frac{-e-e^{-1}}{-e+e^{-1}}} x^r \frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2} (-1 + \operatorname{arctanh}(x^{-1}))^2 \sqrt{2}}{\sqrt{\pi} (x^2 - 1)} dx$$

Moment Generating Function

$$\frac{\sqrt{2}}{\sqrt{\pi}} \int_1^{\frac{e^2+1}{e^2-1}} \frac{(-1 + \operatorname{arctanh}(x^{-1}))^2 e^{-1/2} (\operatorname{arctanh}(x^{-1}))^2 + tx + \operatorname{arctanh}(x^{-1}) - 1/2}{x^2 - 1} dx$$

$$t \mapsto (\sinh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = \frac{(-1 + \operatorname{arcsinh}(x^{-1}))^2 e^{-1/2} (-1 + \operatorname{arcsinh}(x^{-1}))^2 \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = \frac{\left(x^{\ln(\sqrt{x^2+1}+1)}\sqrt{2}e^{-1/2}\sqrt{x^2+1}\ln(\sqrt{x^2+1}+1) - x^{\ln(\sqrt{x^2+1}+1)}\sqrt{2}e^{-1/2}\sqrt{x^2+1}\ln(x) - \sqrt{2}e^{-1/2}\sqrt{x^2+1}\ln(x) - \sqrt{2}e^{-1/2}\sqrt{x^2+1}\ln(x)\right)}{1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = -\frac{\left(\sqrt{x^2+1}+1\right)^{\ln(x)}e^{-1/2}\left(\ln(\sqrt{x^2+1}+1)\right)^2-1/2(\ln(x))^2-1/2\ln(\sqrt{x^2+1}+1)\sqrt{x^2+1}\sqrt{2}-\left(\sqrt{x^2+1}\sqrt{2}\right)}{1}$$

Hazard Function

$$h(x) = -\frac{\left(\sqrt{x^2+1}\right)|x|\left(x^{\ln(\sqrt{x^2+1}+1)}e^{-1/2}\left(\ln(\sqrt{x^2+1}+1)\right)^2-1/2(\ln(x))^2-1/2\ln(\sqrt{x^2+1}+1)\sqrt{x^2+1}\sqrt{2}\right)}{1}$$

Mean

$$mu = \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{2^{\frac{e}{e^2-1}}} \frac{\left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2 e^{-1/2} \left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2}{\sqrt{x^2+1}} dx$$

Variance

$$sigma^2 = \frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_0^{2^{\frac{e}{e^2-1}}} \frac{x \left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2 e^{-1/2} \left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2}{\sqrt{x^2+1}} dx \pi - 2 \left(\int_0^{2^{\frac{e}{e^2-1}}} \frac{\left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2 e^{-1/2} \left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2}{\sqrt{x^2+1}} dx \right)^2 \right)$$

Moment Function

$$m(x) = \int_0^{-2(-e+e^{-1})^{-1}} \frac{x^r \left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2 e^{-1/2} \left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2 \sqrt{2}}{\sqrt{\pi} \sqrt{x^2+1} |x|} dx$$

Moment Generating Function

$$\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{2^{\frac{e}{e^2-1}}} \frac{\left(-1 + \operatorname{arcsinh}(x^{-1})\right)^2 e^{-1/2} \left(\operatorname{arcsinh}(x^{-1})\right)^2 + tx + \operatorname{arcsinh}(x^{-1}) - 1/2}{x \sqrt{x^2+1}} dx_1$$

$$t \mapsto (\operatorname{arcsinh}(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = -\frac{\sqrt{2} \left(-(\cosh(x^{-1}))^2 + 2 \sinh(x^{-1}) \right) e^{-1/2(-1+\sinh(x^{-1}))^2} \cosh(x^{-1})}{\sqrt{\pi} x^2}$$

$$t \mapsto (\operatorname{csch}(t))^{-1} + 1$$

Probability Distribution Function

$$f(x) = \frac{(\operatorname{arccsch}((x-1)^{-1}))^2 e^{-1/2(\operatorname{arccsch}((x-1)^{-1}))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2}}$$

Cumulative Distribution Function

$$F(x) = \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^x \frac{(\operatorname{arccsch}((t-1)^{-1}))^2 e^{-1/2(\operatorname{arccsch}((t-1)^{-1}))^2}}{\sqrt{t^2 - 2t + 2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -\frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_1^x \frac{(\operatorname{arccsch}((t-1)^{-1}))^2 e^{-1/2(\operatorname{arccsch}((t-1)^{-1}))^2}}{\sqrt{t^2 - 2t + 2}} dt - \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{(\operatorname{arccsch}((x-1)^{-1}))^2 e^{-1/2(\operatorname{arccsch}((x-1)^{-1}))^2} \sqrt{2}}{\sqrt{x^2 - 2x + 2}} \left(\sqrt{2} \int_1^x \frac{(\operatorname{arccsch}((t-1)^{-1}))^2 e^{-1/2(\operatorname{arccsch}((t-1)^{-1}))^2}}{\sqrt{t^2 - 2t + 2}} dt - \sqrt{\pi} \right)$$

Mean

$$mu = \int_1^\infty x \frac{(\operatorname{arccsch}((x-1)^{-1}))^2 e^{-1/2(\operatorname{arccsch}((x-1)^{-1}))^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2}} dx$$

Variance

$$\sigma^2 = \int_1^\infty \frac{x^2 \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2 e^{-1/2 \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2}} dx - \left(\int_1^\infty \frac{x \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2 e^{-1/2 \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2}} dx \right)^2$$

Moment Function

$$m(x) = \int_1^\infty \frac{x^r \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2 e^{-1/2 \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2} \sqrt{2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2}} dx$$

Moment Generating Function

$$\int_1^\infty \frac{\left(\operatorname{arccsch}((x-1)^{-1}) \right)^2 \sqrt{2} e^{tx - 1/2 \left(\operatorname{arccsch}((x-1)^{-1}) \right)^2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2}} dx_1$$

$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -\frac{\sqrt{2}}{(\operatorname{arctanh}(x))^4 \sqrt{\pi} (x^2 - 1)} e^{-1/2 (\operatorname{arctanh}(x))^{-2}}$$

Cumulative Distribution Function

$$F(x) = -\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{1}{(\operatorname{arctanh}(t))^4 (t^2 - 1)} e^{-1/2 (\operatorname{arctanh}(t))^{-2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = \frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{1}{(\operatorname{arctanh}(t))^4 (t^2 - 1)} e^{-1/2 (\operatorname{arctanh}(t))^{-2}} dt + \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2}}{(\operatorname{arctanh}(x))^4 (x^2 - 1)} e^{-1/2 (\operatorname{arctanh}(x))^{-2}} \left(\sqrt{2} \int_0^x \frac{1}{(\operatorname{arctanh}(t))^4 (t^2 - 1)} e^{-1/2 (\operatorname{arctanh}(t))^{-2}} dt + \sqrt{\pi} \right)$$

Mean

$$\mu = -\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^4 (x^2 - 1)} e^{-1/2 (\operatorname{arctanh}(x))^{-2}} dx$$

Variance

$$\sigma^2 = -\frac{1}{\pi^{3/2}} \left(\sqrt{2} \int_0^1 \frac{x^2}{(\operatorname{arctanh}(x))^4 (x^2 - 1)} e^{-1/2 (\operatorname{arctanh}(x))^{-2}} dx \pi + 2 \left(\int_0^1 \frac{x}{(\operatorname{arctanh}(x))^4 (x^2 - 1)} e^{-1/2 (\operatorname{arctanh}(x))^{-2}} dx \right)^2 \right)$$

Moment Function

$$m(x) = \int_0^1 -\frac{x^r \sqrt{2}}{(\operatorname{arctanh}(x))^4 \sqrt{\pi} (x^2 - 1)} e^{-1/2 (\operatorname{arctanh}(x))^{-2}} dx$$

Moment Generating Function

$$-\frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{1}{(\operatorname{arctanh}(x))^4 (x^2 - 1)} e^{1/2 \frac{2tx(\operatorname{arctanh}(x))^2 - 1}{(\operatorname{arctanh}(x))^2}} dx$$

1

$$t \mapsto \operatorname{csch}(t^{-1})$$

Probability Distribution Function

$$f(x) = \frac{\sqrt{2}}{\sqrt{\pi} \sqrt{x^2 + 1} (\operatorname{arccsch}(x))^4 |x|} e^{-1/2 (\operatorname{arccsch}(x))^{-2}}$$

Cumulative Distribution Function

$$F(x) = \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^4 |t|} e^{-1/2 (\operatorname{arccsch}(t))^{-2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -\frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^4 |t|} e^{-1/2 (\operatorname{arccsch}(t))^{-2}} dt - \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2}}{\sqrt{x^2+1}(\operatorname{arccsch}(x))^4|x|}e^{-1/2(\operatorname{arccsch}(x))^{-2}}\left(\sqrt{2}\int_0^x\frac{1}{\sqrt{t^2+1}(\operatorname{arccsch}(t))^4|t|}e^{-1/2(\operatorname{arccsch}(t))^{-2}}dt\right)$$

Mean

$$mu = \int_0^\infty \frac{\sqrt{2}}{\sqrt{\pi}\sqrt{x^2+1}(\operatorname{arccsch}(x))^4}e^{-1/2(\operatorname{arccsch}(x))^{-2}}dx$$

Variance

$$sigma^2 = \int_0^\infty \frac{x\sqrt{2}}{\sqrt{\pi}\sqrt{x^2+1}(\operatorname{arccsch}(x))^4}e^{-1/2(\operatorname{arccsch}(x))^{-2}}dx - \left(\int_0^\infty \frac{\sqrt{2}}{\sqrt{\pi}\sqrt{x^2+1}(\operatorname{arccsch}(x))^4}e^{-1/2(\operatorname{arccsch}(x))^{-2}}dx\right)^2$$

Moment Function

$$m(x) = \int_0^\infty \frac{x^r\sqrt{2}}{\sqrt{\pi}\sqrt{x^2+1}(\operatorname{arccsch}(x))^4|x|}e^{-1/2(\operatorname{arccsch}(x))^{-2}}dx$$

Moment Generating Function

$$\int_0^\infty \frac{\sqrt{2}}{(\operatorname{arccsch}(x))^4 x\sqrt{x^2+1}\sqrt{\pi}}e^{1/2\frac{2tx(\operatorname{arccsch}(x))^2-1}{(\operatorname{arccsch}(x))^2}}dx_1$$

$$t \mapsto \operatorname{arccsch}(t^{-1})$$

Probability Distribution Function

$$f(x) = \frac{\sqrt{2}e^{-1/2(\sinh(x))^2}\cosh(x)(\sinh(x))^2}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = -1/2\frac{\left(-2\sqrt{\pi}\operatorname{erf}\left(1/4\sqrt{2}(e^x-e^{-x})\right)e^{1/8(e^{4x}+8xe^{2x}+1)}e^{-2x}+\sqrt{2}e^{1/4+2x}-\sqrt{2}e^{1/4}\right)e^{-1/8}}{\sqrt{\pi}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf}\left(e^{4-Z}+4e^{2-Z}\ln(\pi)+4e^{2-Z}\ln(2)+4e^{2-Z}\ln\left(\frac{(-s+\operatorname{erf}(1/4\sqrt{2}(e^{-Z}-e^Z))e^{1/8(e^{4-Z}+8e^{2-Z}+1)}e^{-2Z}+\sqrt{2}e^{1/4+2Z}-\sqrt{2}e^{1/4}}{(e^{2-Z}-1)^2}\right)}\right)$$

Survivor Function

$$S(x) = 1/2 \frac{-2\sqrt{\pi}\operatorname{erf}\left(1/4\sqrt{2}\left(e^x - e^{-x}\right)\right) + \sqrt{2}e^{-1/8}\left(e^{4x} - 8xe^{2x} - 2e^{2x} + 1\right)e^{-2x} - \sqrt{2}e^{-1/8}\left(e^{4x} + 8xe^{2x} - 2e^{2x} + 1\right)e^{-2x}}{\sqrt{\pi}}$$

Hazard Function

$$h(x) = 2 \frac{\sqrt{2}e^{-1/2}(\sinh(x))^2 \cosh(x) (\sinh(x))^2}{-2\sqrt{\pi}\operatorname{erf}\left(1/4\sqrt{2}\left(e^x - e^{-x}\right)\right) + \sqrt{2}e^{-1/8}\left(e^{4x} - 8xe^{2x} - 2e^{2x} + 1\right)e^{-2x} - \sqrt{2}e^{-1/8}\left(e^{4x} + 8xe^{2x} - 2e^{2x} + 1\right)e^{-2x}}$$

Mean

$$mu = \int_0^\infty \frac{e^{1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2}x}{\sqrt{\pi}} dx$$

Variance

$$sigma^2 = \int_0^\infty \frac{e^{1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2}x^2}{\sqrt{\pi}} dx - \left(\int_0^\infty \frac{e^{1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2}x}{\sqrt{\pi}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty \frac{x^r \sqrt{2}e^{-1/2}(\sinh(x))^2 \cosh(x) (\sinh(x))^2}{\sqrt{\pi}} dx$$

Moment Generating Function

$$\int_0^\infty \frac{e^{tx+1/4-1/4 \cosh(2x)} (\sinh(x))^2 \cosh(x) \sqrt{2}}{\sqrt{\pi}} dx_1$$