

```
> restart;
read("c:/appl/appl7.txt");
```

PROCEDURES:

AllPermutations(n), AllCombinations(n, k), Benford(X), BootstrapRV(Data),
CDF:CHF:HF:IDF:PDF:SF(X, [x]), CoefOfVar(X), Convolution(X, Y),
ConvolutionIID(X, n), CriticalPoint(X, prob), Determinant(MATRIX), Difference(X, Y),
Display(X), ExpectedValue(X, [g]), KSTest(X, Data, Parameters), Kurtosis(X),
Maximum(X, Y), MaximumIID(X, n), Mean(X), MGF(X), Minimum(X, Y),
MinimumIID(X, n), Mixture(MixParameters, MixRVs),
MLE(X, Data, Parameters, [Rightcensor]), MLENHPP(X, Data, Parameters, obstime),
MLEWeibull(Data, [Rightcensor]), MOM(X, Data, Parameters),
NextCombination(Previous, size), NextPermutation(Previous), OrderStat(X, n, r, ["wo"]),
PlotDist(X, [low], [high]), PlotEmpCDF(Data, [low], [high]),
PlotEmpCIF(Data, [low], [high]), PlotEmpSF(Data, Censor),
PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),
PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),
PlotEmpVsFittedSF(X, Data, Parameters, Censor, low, high),
PPPlot(X, Data, Parameters), Product(X, Y), ProductIID(X, n),
QQPlot(X, Data, Parameters), RangeStat(X, n, ["wo"]), Skewness(X), Transform(X, g),
Truncate(X, low, high), Variance(X), VerifyPDF(X)

Procedure Notation:

X and Y are random variables

Greek letters are numeric or symbolic parameters

x is numeric or symbolic

n and r are positive integers, $n \geq r$

low and high are numeric

g is a function

Brackets [] denote optional parameters

"double quotes" denote character strings

MATRIX is a 2 x 2 array of random variables

*A capitalized parameter indicates that it must be
entered as a list --> ex. Data := [1, 12.4, 34, 52.45, 63]*

Variate Generation:

ArcTanVariate(alpha, phi), BinomialVariate(n, p, m), ExponentialVariate(lambda),
NormalVariate(mu, sigma), UniformVariate(), WeibullVariate(lambda, kappa, m)

DATA SETS:

BallBearing, HorseKickFatalities, Hurricane, MP6, RatControl, RatTreatment, USSHalfBeak

ArcSinRV(), ArcTanRV(alpha, phi), BetaRV(alpha, beta), CauchyRV(a, alpha), ChiRV(n),

*ChiSquareRV(n), ErlangRV(lambda, n), ErrorRV(mu, alpha, d), ExponentialRV(lambda),
 ExponentialPowerRV(lambda, kappa), ExtremeValueRV(alpha, beta), FRV(n1, n2),
 GammaRV(lambda, kappa), GeneralizedParetoRV(gamma, delta, kappa),
 GompertzRV(delta, kappa), HyperbolicSecantRV(), HyperExponentialRV(p, l),
 HypoExponentialRV(l), IDBRV(gamma, delta, kappa), InverseGaussianRV(lambda, mu),
 InvertedGammaRV(alpha, beta), KSRV(n), LaPlaceRV(omega, theta),
 LogGammaRV(alpha, beta), LogisticRV(kappa, lambda), LogLogisticRV(lambda, kappa),
 LogNormalRV(mu, sigma), LomaxRV(kappa, lambda), MakehamRV(gamma, delta, kappa),
 MuthRV(kappa), NormalRV(mu, sigma), ParetoRV(lambda, kappa), RayleighRV(lambda),
 StandardCauchyRV(), StandardNormalRV(), StandardTriangularRV(m),
 StandardUniformRV(), TRV(n), TriangularRV(a, m, b), UniformRV(a, b),
 WeibullRV(lambda, kappa)*

Error, attempting to assign to `DataSets` which is protected.
 Try declaring `local DataSets`; see ?protect for details.

```

> bf := ExponentialPowerRV(2,3);
bfname := "ExponentialPowerRV(2,3)";
      bf :=  $\left[ \left[ x \rightarrow 6 e^1 - e^{2x^3} e^{2x^3} x^2 \right], [0, \infty], ["Continuous", "PDF"] \right]$ 
      bfname := "ExponentialPowerRV(2,3)"

```

(1)

```

> #plot(1/csch(t)+1, t = 0..0.0010);
#plot(diff(1/csch(t),t), t=0..0.0010);
#limit(1/csch(t), t=0);
> solve(exp(-t) = y, t);
      -ln(y)

```

(2)

```

> # discarded -ln(t + 1), t-> csch(t), t->arccsch(t), t -> tan(t),
> #name of the file for latex output
filename := "C:/LatexOutput/Trash.tex";

glist := [t -> t^2, t -> sqrt(t), t -> 1/t, t -> arctan(t), t
-> exp(t), t -> ln(t), t -> exp(-t), t -> -ln(t), t -> ln(t+1),
t -> 1/(ln(t+2)), t -> tanh(t), t -> sinh(t), t -> arcsinh(t),
t-> csch(t+1), t->arccsch(t+1), t-> 1/tanh(t+1), t-> 1/sinh(t+1),
t-> 1/arcsinh(t+1), t-> 1/csch(t)+1, t-> tanh(1/t), t->csch
(1/t), t-> arccsch(1/t), t-> arctanh(1/t) ]:

base := t -> PDF(bf, t):

print(base(x)):

#begin loopint through transformations
for i from 1 to 22 do
#for i from 1 to 3 do
    print( "i is", i, " -----"
-----

```

```
-----");  
  
g := glist[i]:  
l := bf[2][1];  
u := bf[2][2];  
Temp := Transform(bf, [[unapply(g(x), x)], [l,u]]);  
  
#terminal output  
  
PlotDist(PDF(Temp), 0, 40);  
PlotDist(HF(Temp), 0, 40);  
  
od;
```

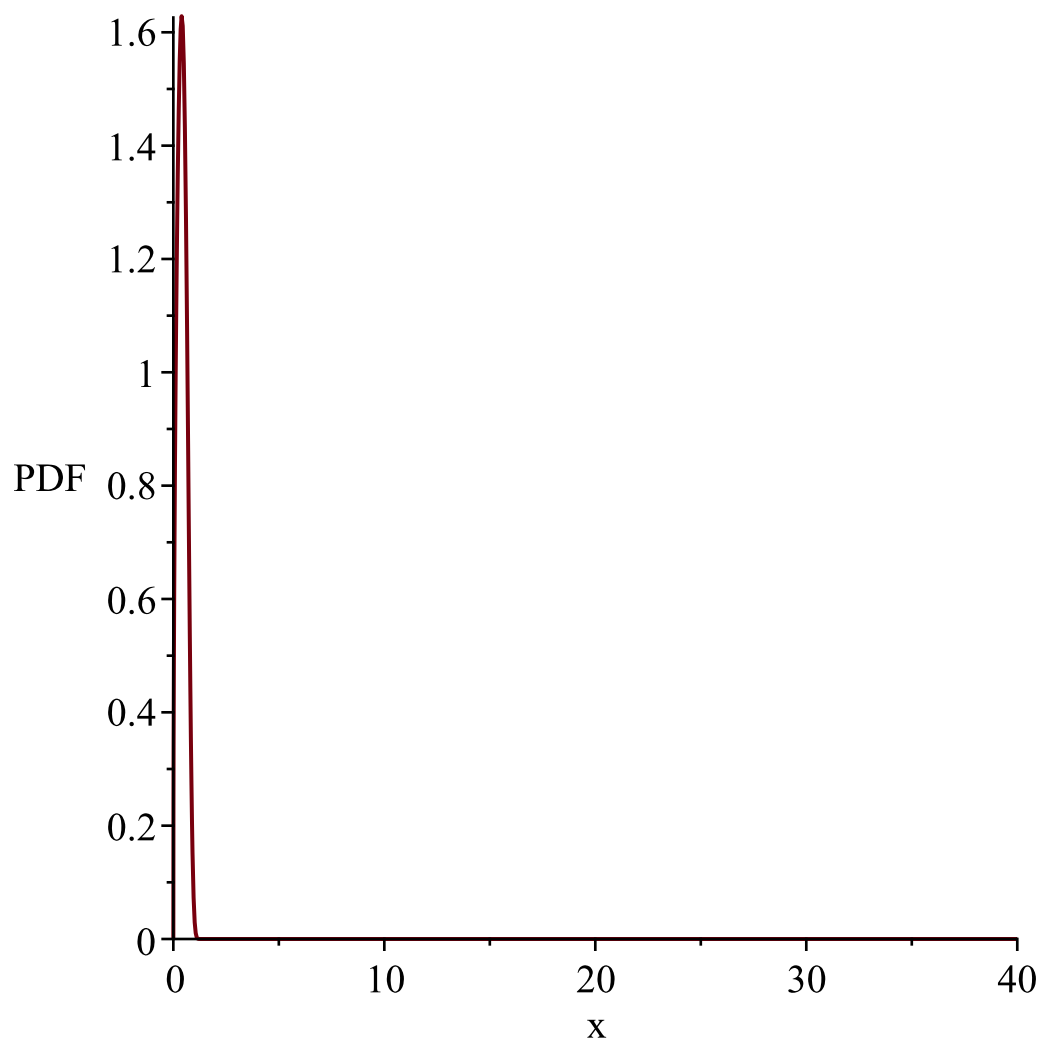
filename := "C:/LatexOutput/Trash.tex"

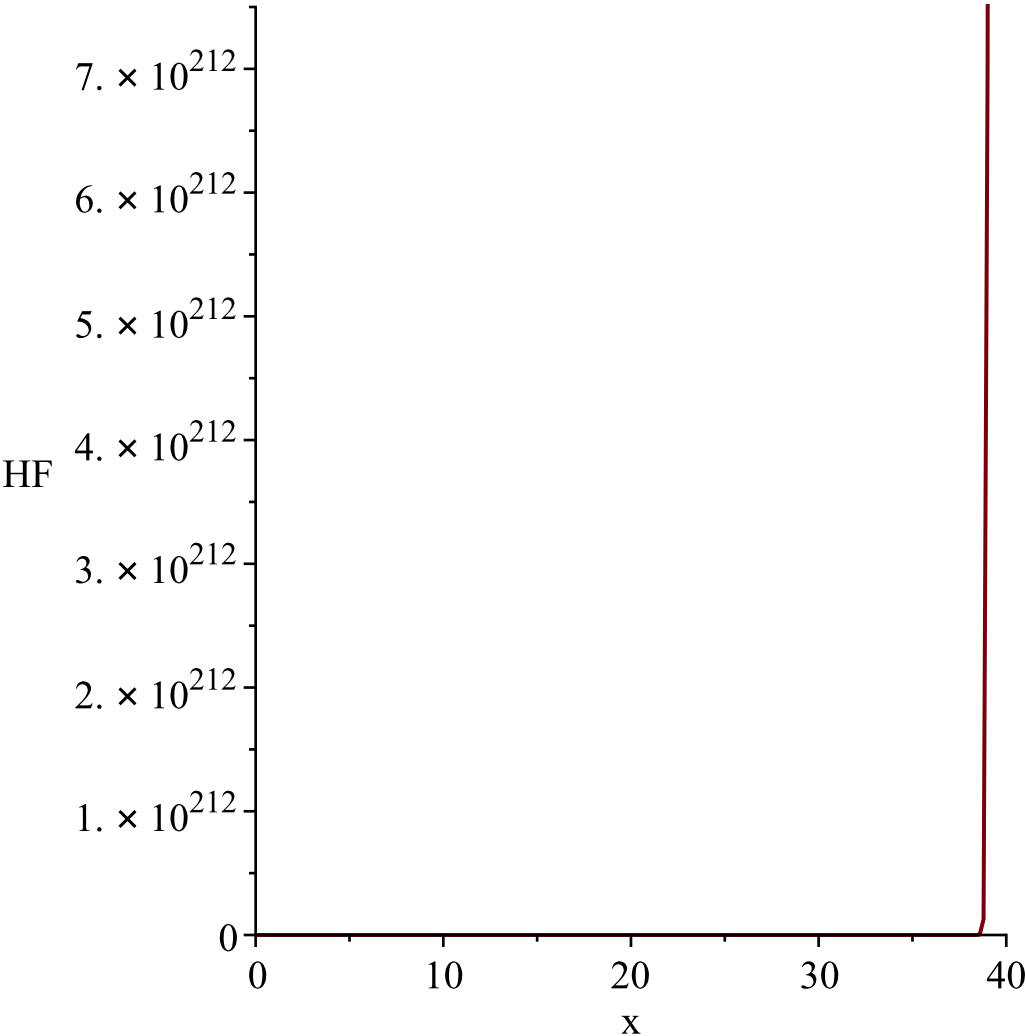
$$6 e^{1-e^{2 x^3}} e^{2 x^3} x^2$$

"i is", 1,
"-----"
-----"

$$\begin{aligned} g &:= t \rightarrow t^2 \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

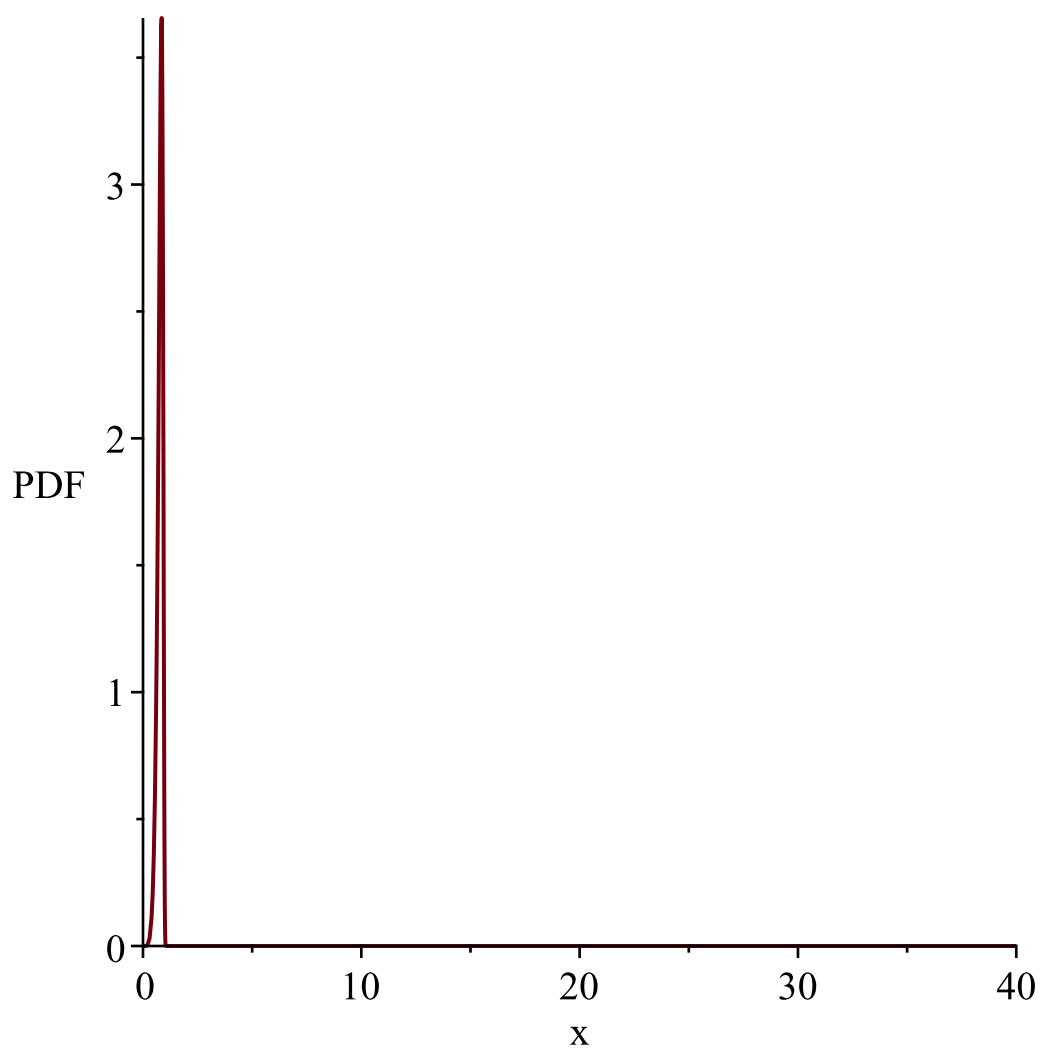
$$Temp := \left[\left[y \rightarrow 3 e^{1-e^{2 y^{3/2}}} + 2 y^{3/2} \sqrt{y} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

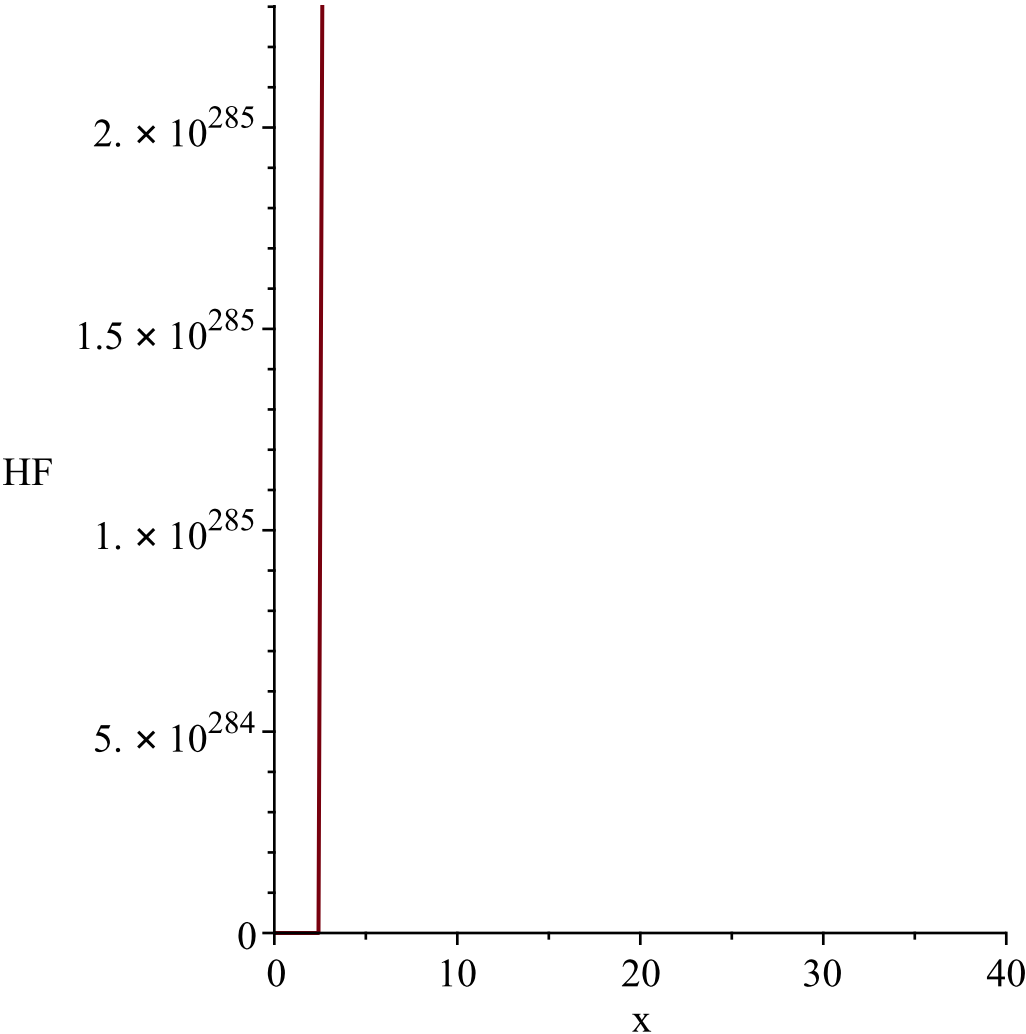




"i is", 2,
"-----"
-----"

$$\begin{aligned} g &:= t \rightarrow \sqrt{t} \\ l &:= 0 \\ u &:= \infty \\ Temp &:= \left[\left[y \rightsquigarrow 12 \, \mathrm{e}^1 - \mathrm{e}^{2 \, y \rightsquigarrow 6} + 2 \, y \rightsquigarrow 6 \, y \rightsquigarrow 5 \right], [0, \infty], ["Continuous", "PDF"] \right] \end{aligned}$$





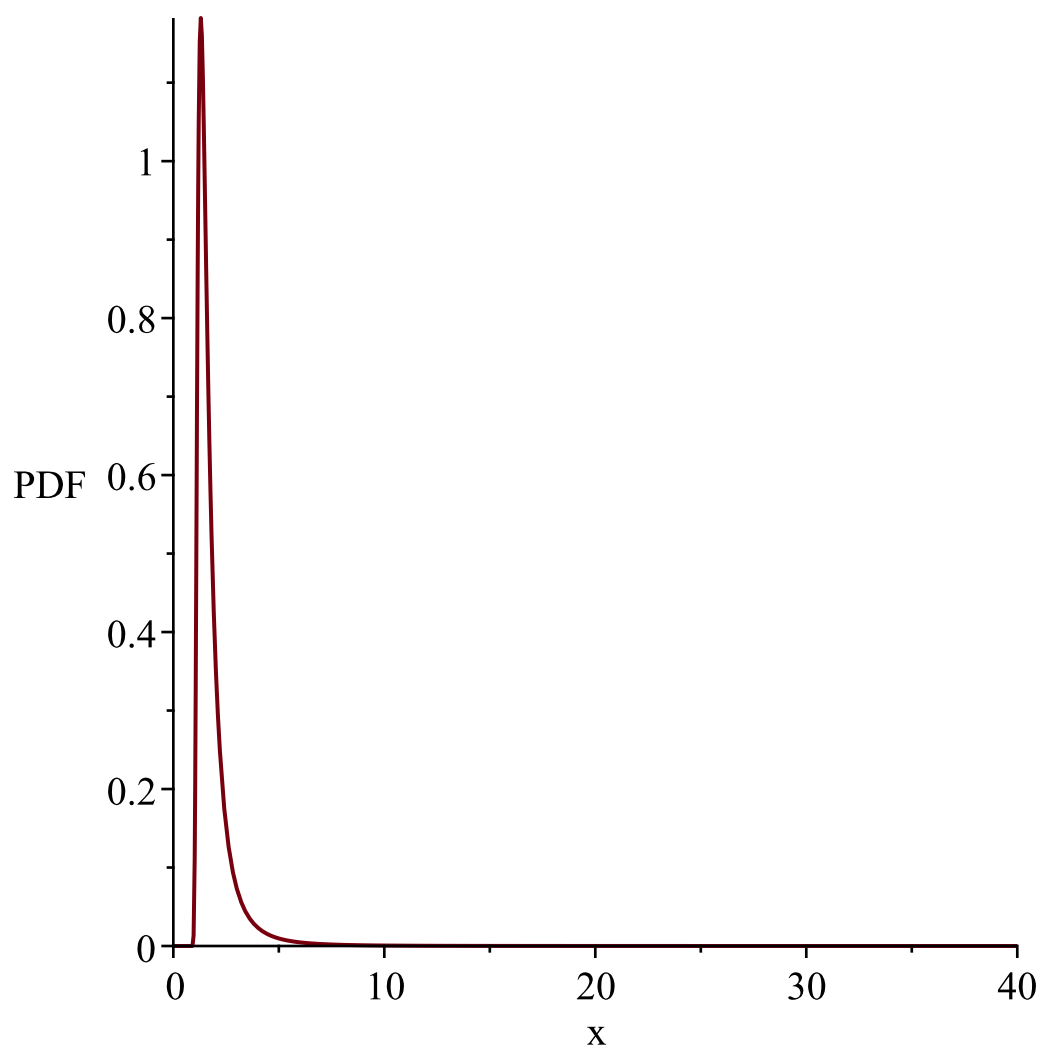
"i is", 3,
"-----"
-----"

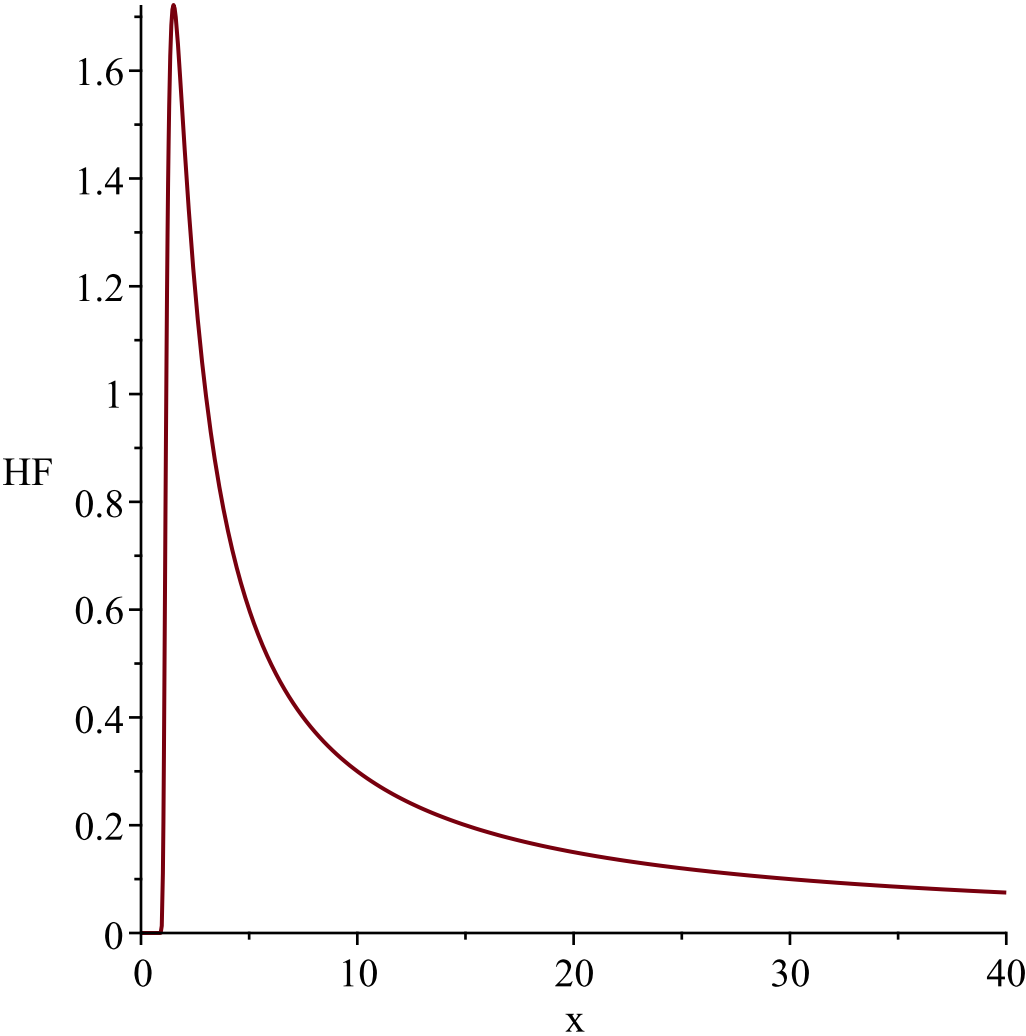
$$g:=t\rightarrow \frac{1}{t}$$

$$l:=0$$

$$u:=\infty$$

$$Temp:=\left[\left[\frac{\frac{2}{e^{y^3}}y^3-y^3-2}{y^3}}{y\rightarrow \frac{6\,e}{y^4}}\right],\left[0,\infty\right],\left["Continuous","PDF"\right]\right]$$

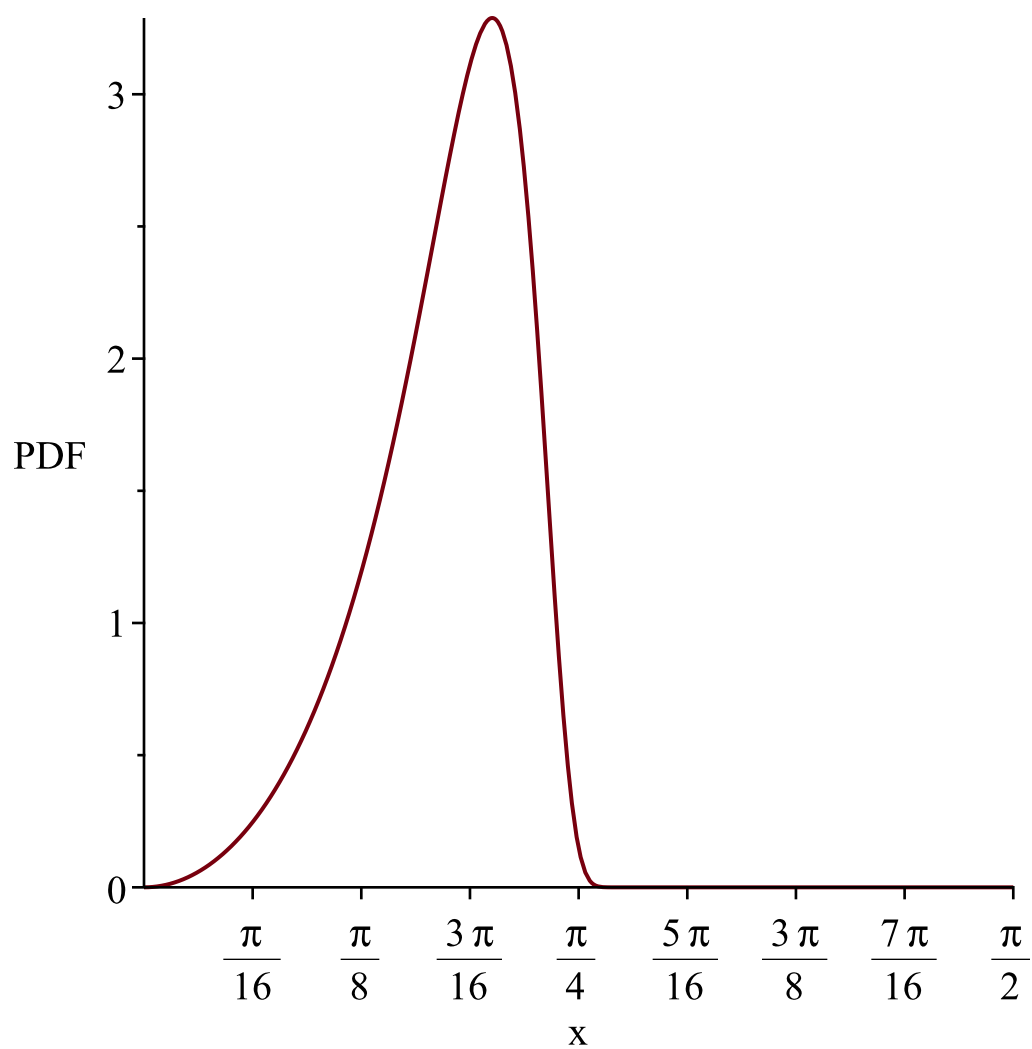




"i is", 4,
"-----"
-----"

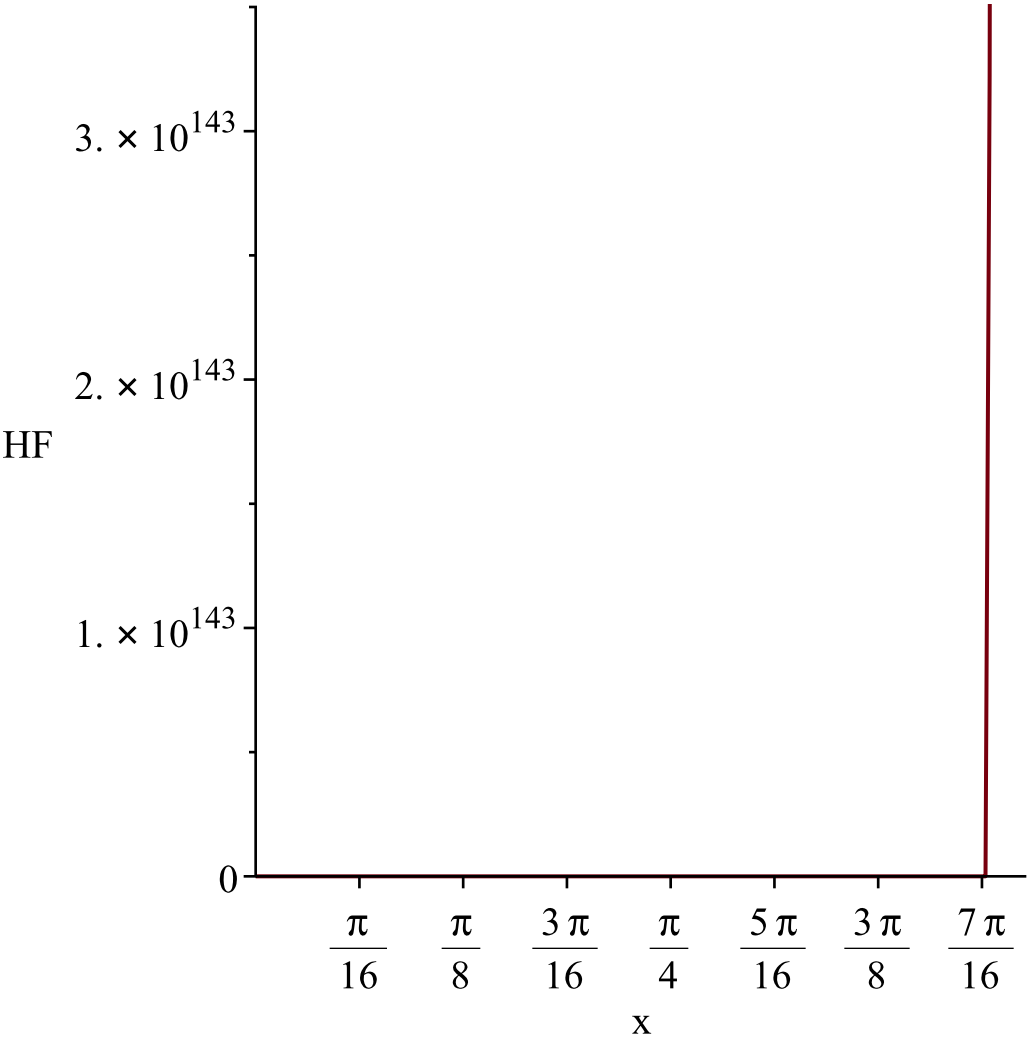
```
g := t→arctan(t)
l := 0
u := ∞
Temp := [ [y~→6 e1 - e2 tan(y~)3 + 2 tan(y~)3 tan(y~)2 (1 + tan(y~)2)], [0,  $\frac{1}{2} \pi$ ], ["Continuous",
"PDF"] ]
```

*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\frac{1}{2} \pi$
Resetting high to RV's maximum support value*



*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\frac{1}{2} \pi$*

Resetting high to RV's maximum support value



"i is", 5,
"-----"
-----"

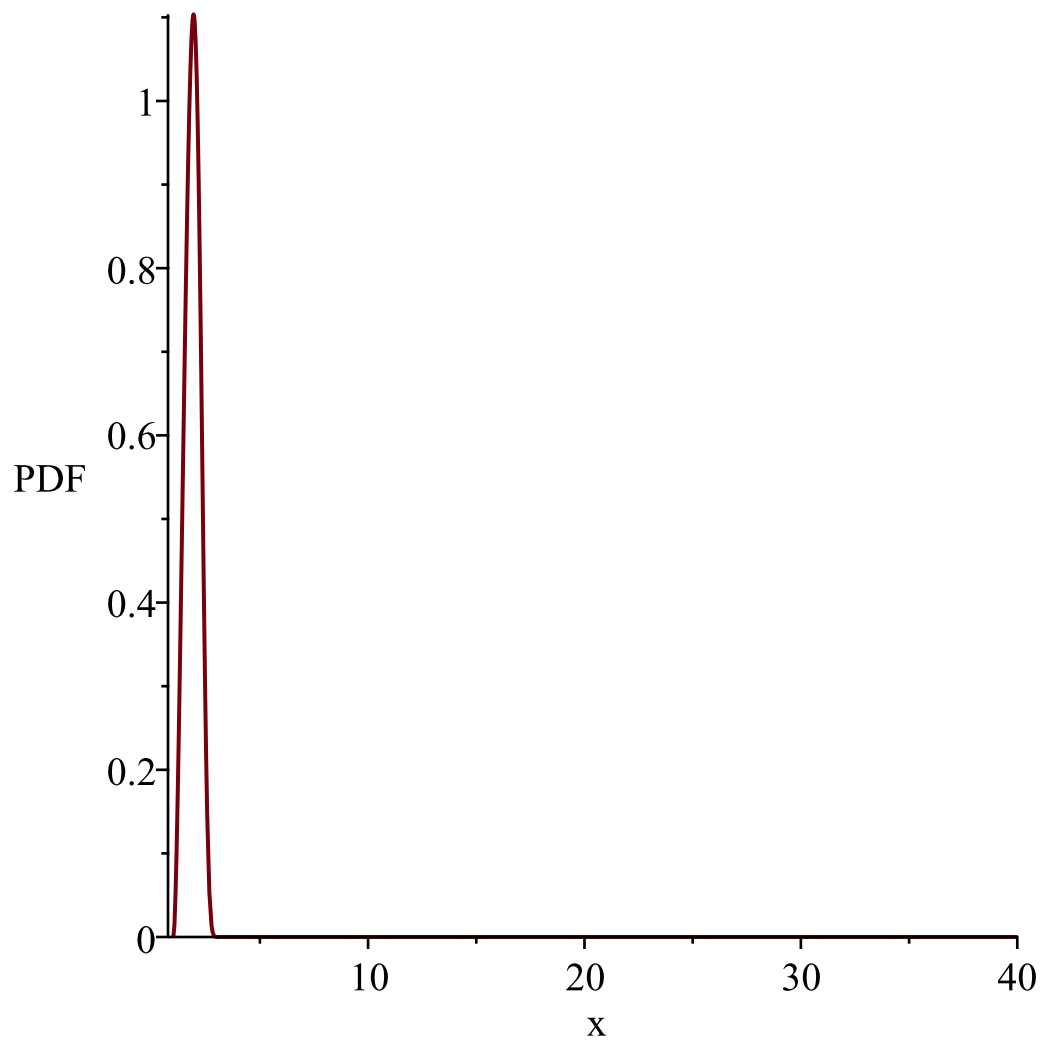
$$\begin{aligned} g &:= t \rightarrow \mathbf{e}^t \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

$$Temp := \left[\left[y \rightsquigarrow \frac{6 \mathbf{e}^1 - \mathbf{e}^{2 \ln(y \sim)} + 2 \ln(y \sim)^3 \ln(y \sim)^2}{y \sim} \right], [1, \infty], ["Continuous", "PDF"] \right]$$

*WARNING(PlotDist): Low value provided by user, 0
is less than minimum support value of random variable*

1

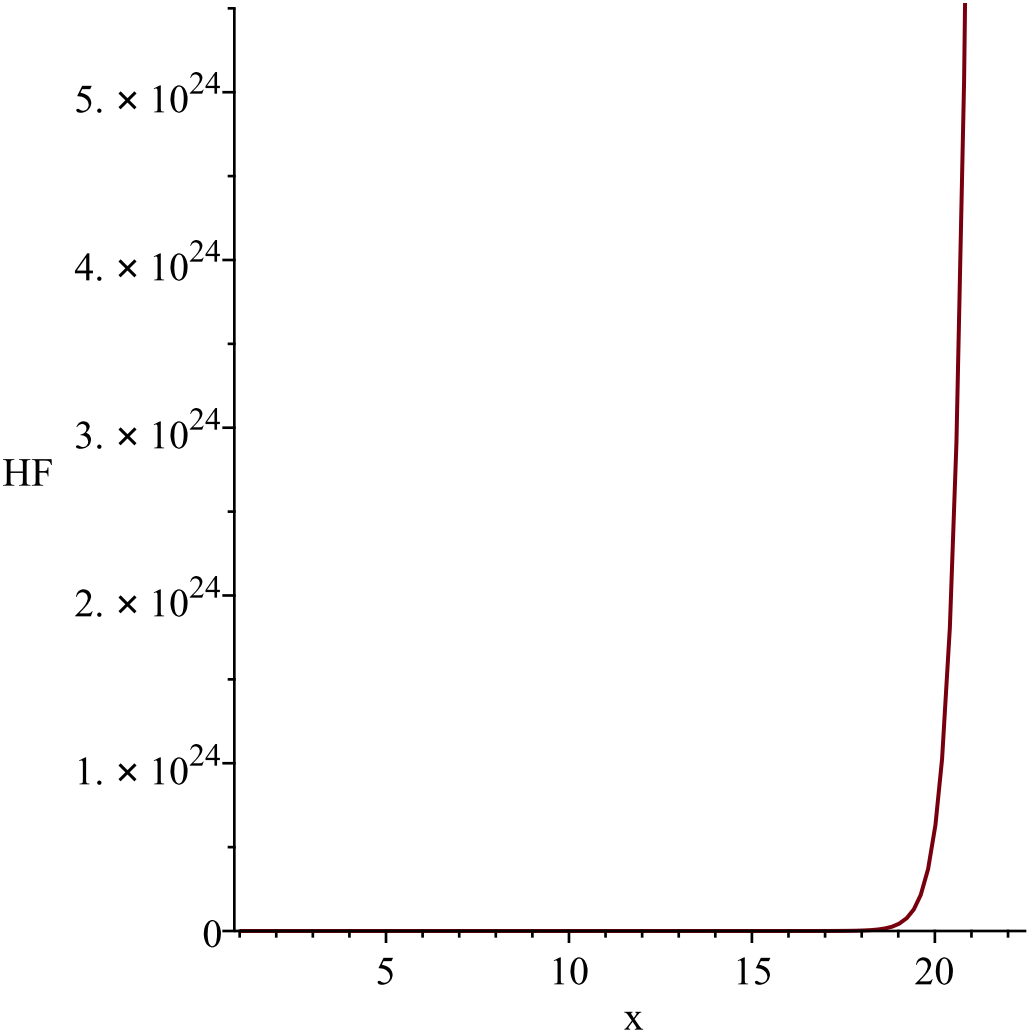
Resetting low to RV's minimum support value



*WARNING(PlotDist): Low value provided by user, 0
is less than minimum support value of random variable*

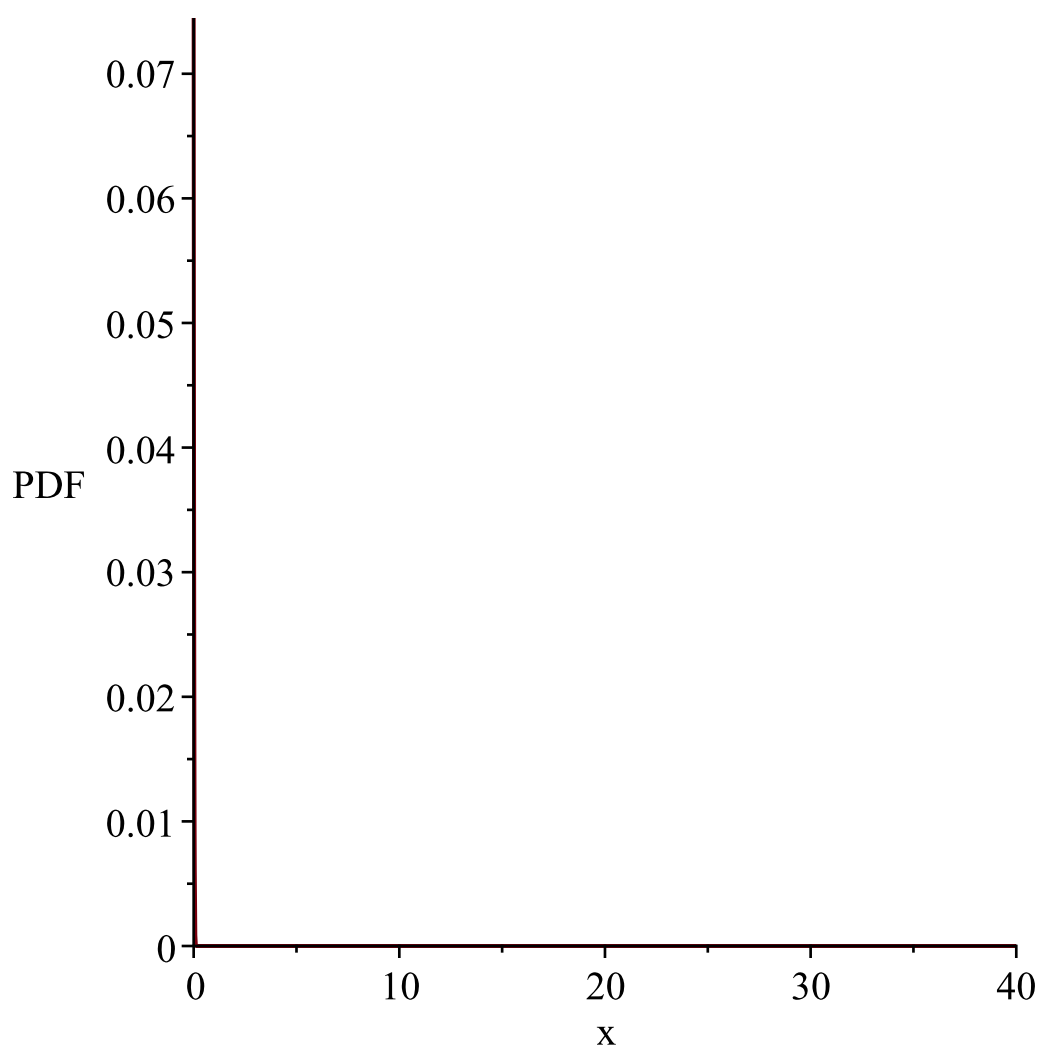
1

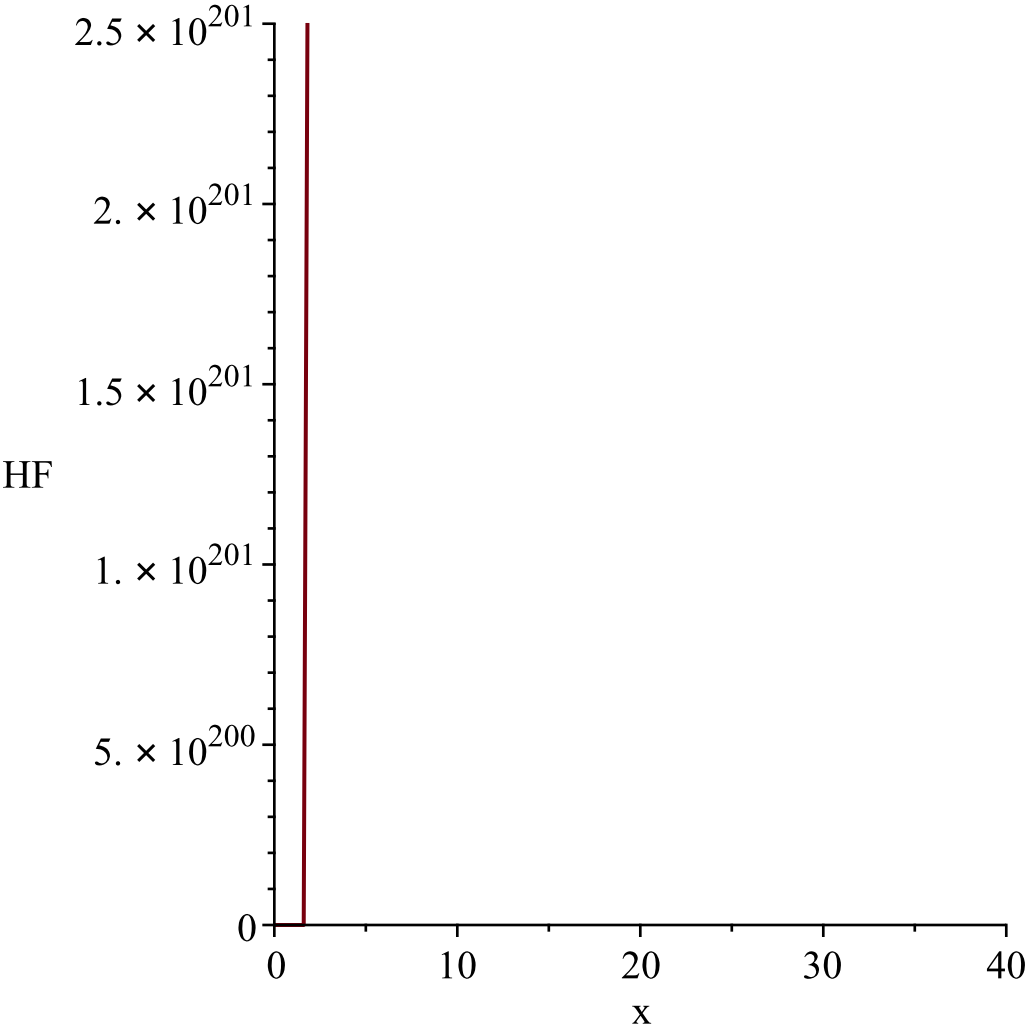
Resetting low to RV's minimum support value



"i is", 6,
" _____
-----"

$$\begin{aligned} g &:= t \rightarrow \ln(t) \\ l &:= 0 \\ u &:= \infty \\ Temp &:= \Big[\Big[y \leadsto 6 \, \mathrm{e}^1 - \mathrm{e}^2 \, \mathrm{e}^3 y \leadsto + 2 \, \mathrm{e}^3 y \leadsto + 3 y \leadsto \Big], [-\infty, \infty], ["Continuous", "PDF"] \Big] \end{aligned}$$





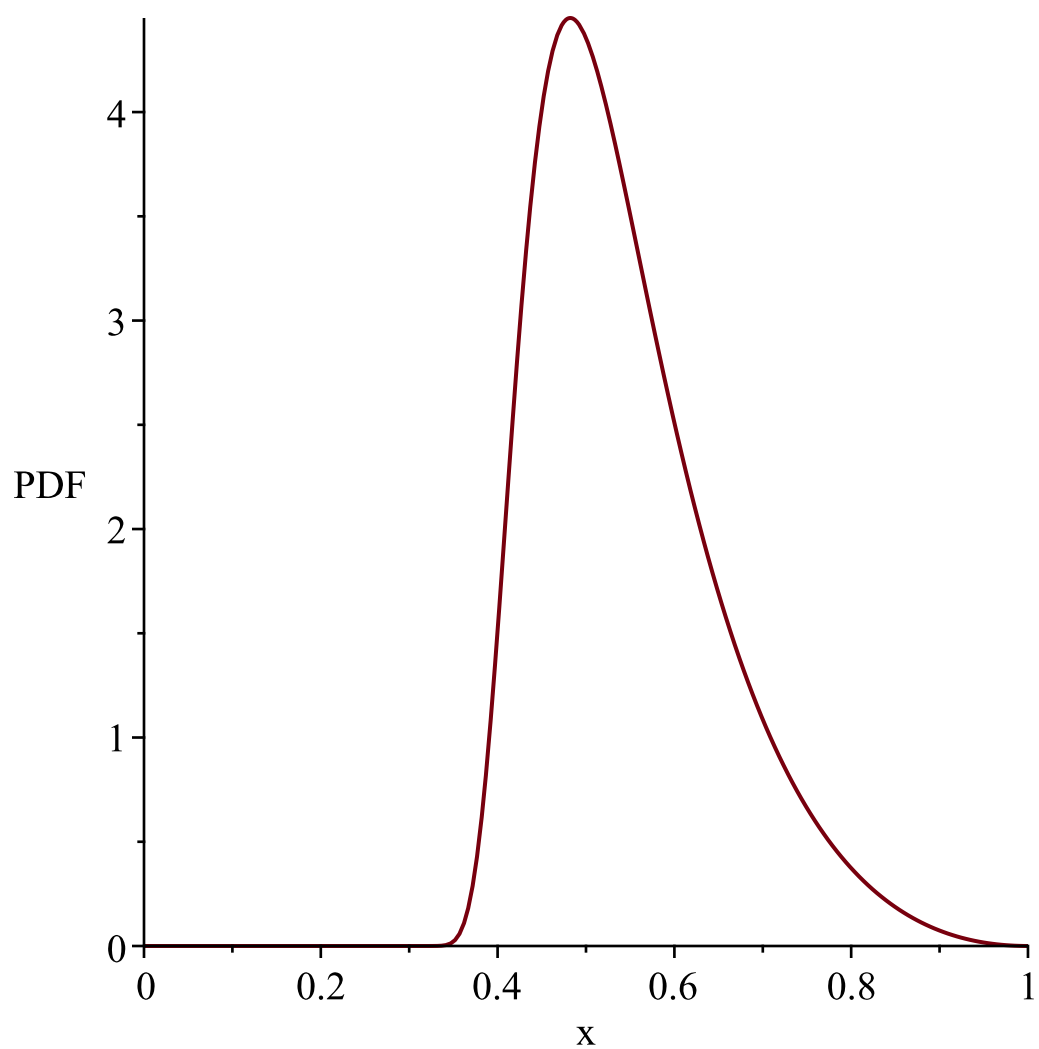
"i is", 7,
"-----"
-----"

$$\begin{aligned} g &:= t \rightarrow e^{-t} \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

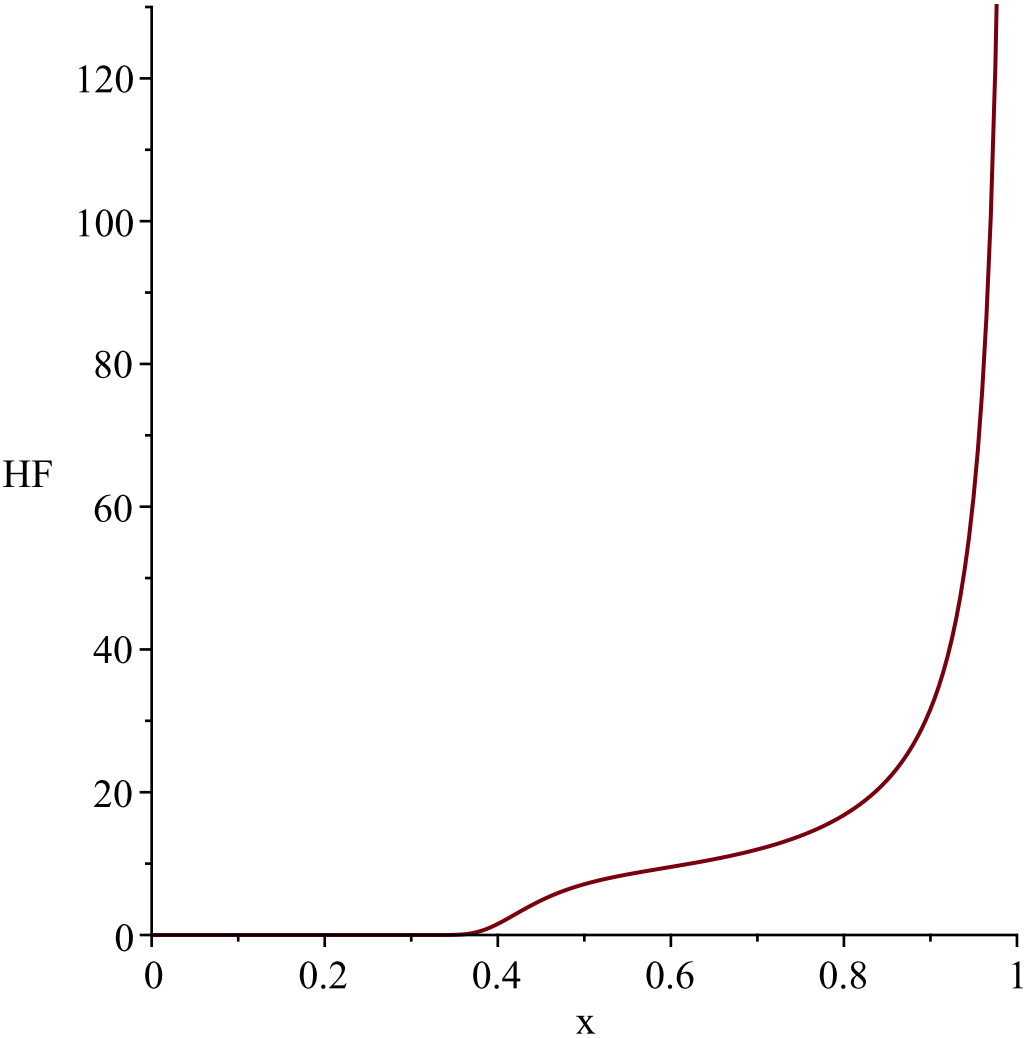
$$Temp := \left[\left[y \sim \rightarrow \frac{6 e^{1 - e^{-2 \ln(y \sim)^3} - 2 \ln(y \sim)^3 \ln(y \sim)^2}}{y \sim} \right], [0, 1], ["Continuous", "PDF"] \right]$$

*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, 1*

Resetting high to RV's maximum support value

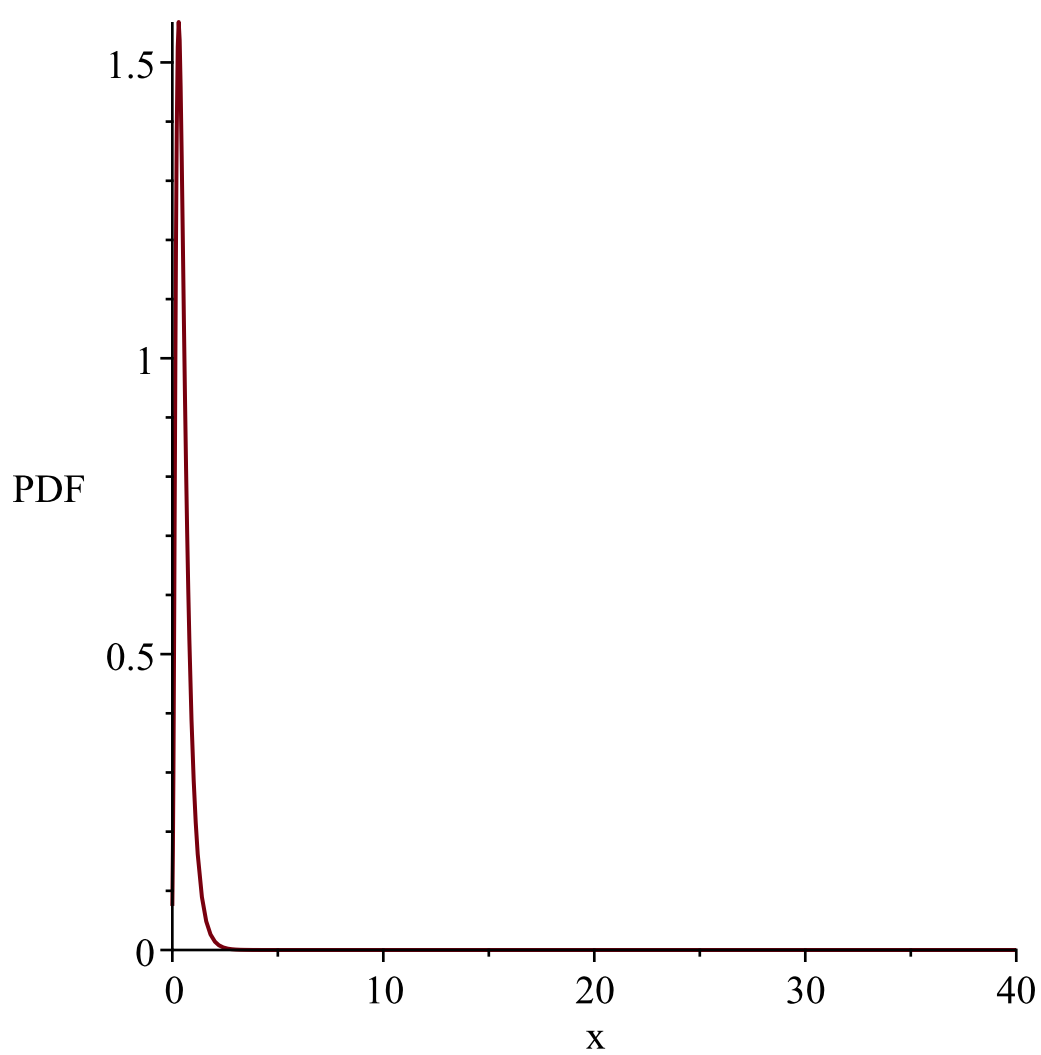


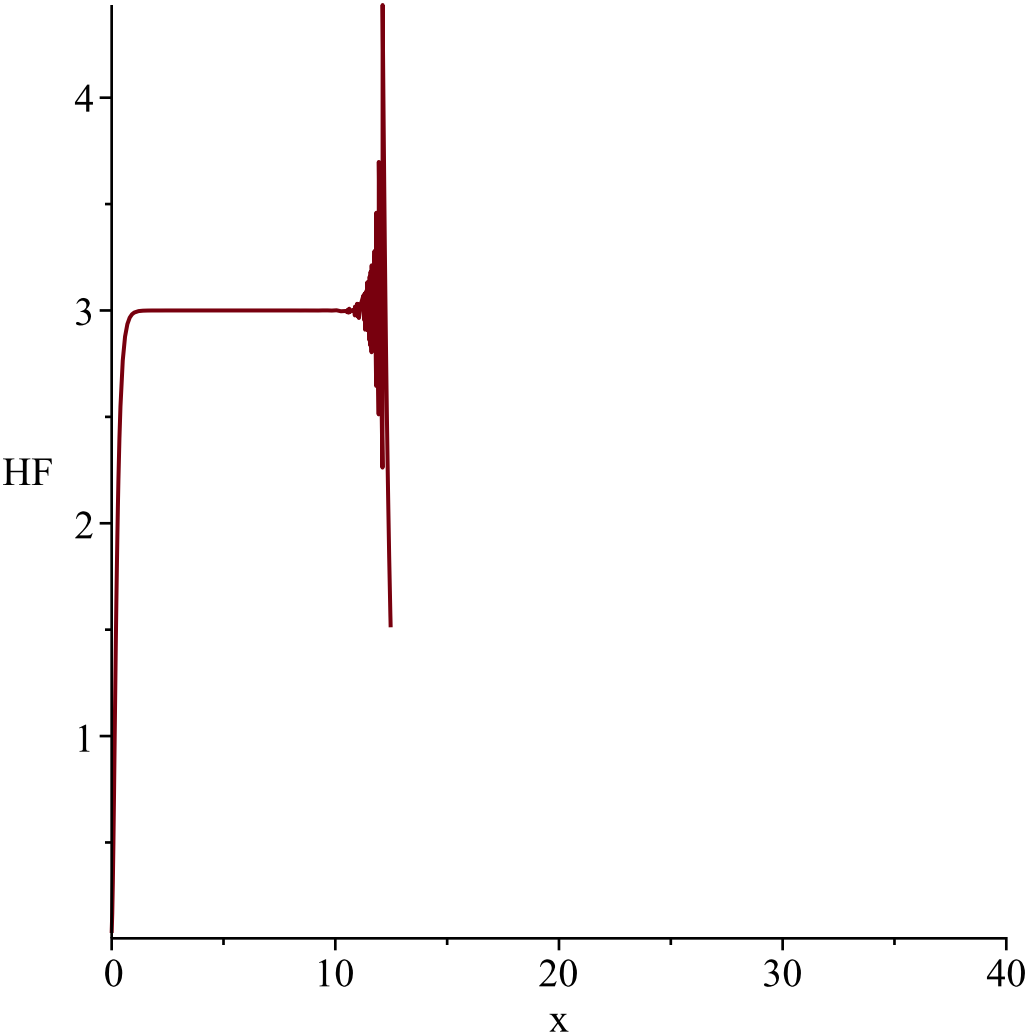
*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, 1
Resetting high to RV's maximum support value*



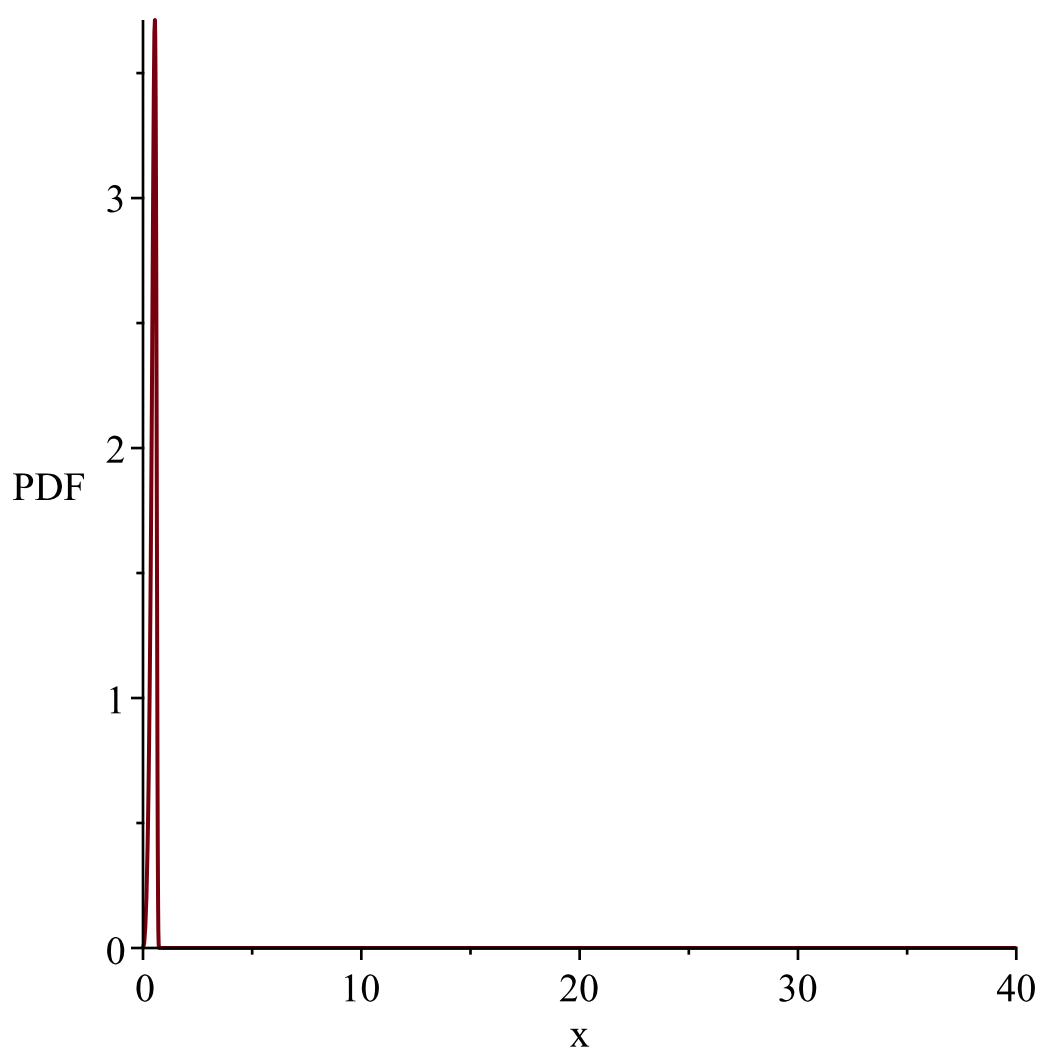
"i is", 8,
" _____"
-----"

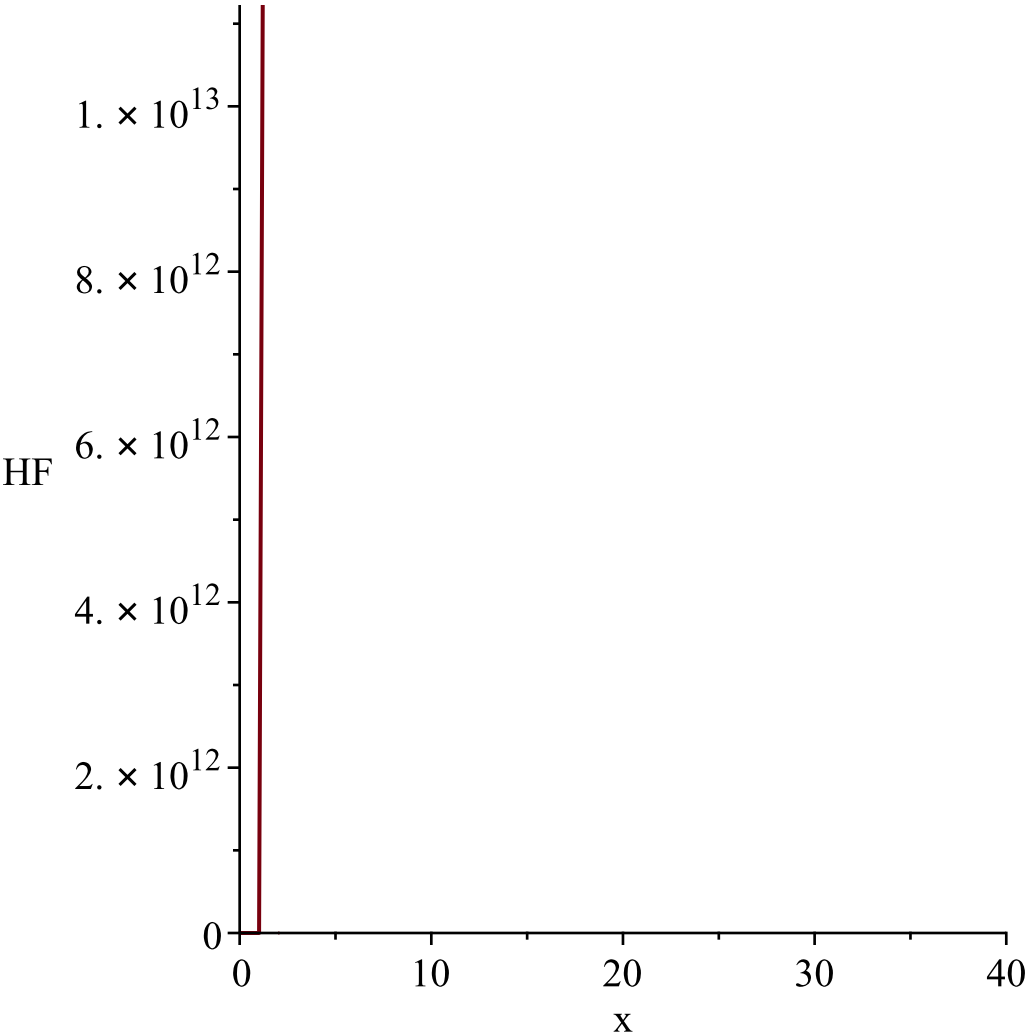
$$g := t \rightarrow -\ln(t)$$
$$l := 0$$
$$u := \infty$$
$$Temp := \Big[\Big[y \sim \rightarrow 6 \, \mathrm{e}^1 - \mathrm{e}^2 \mathrm{e}^{-3 y \sim} + 2 \, \mathrm{e}^{-3 y \sim} - 3 y \sim \Big], [-\infty, \infty], ["Continuous", "PDF"] \Big]$$





```
"i is", 9,  
" -----"  
-----"  
  
g := t→ln(t + 1)  
l := 0  
u := ∞  
  
Temp := [[y~→6 e2 e3 y~ - 6 e2 y~ + 6 ey~ - e2 (ey~ - 1)3 + y~ - 1 (ey~ - 1)2], [0, ∞], ["Continuous",  
"PDF"]]
```

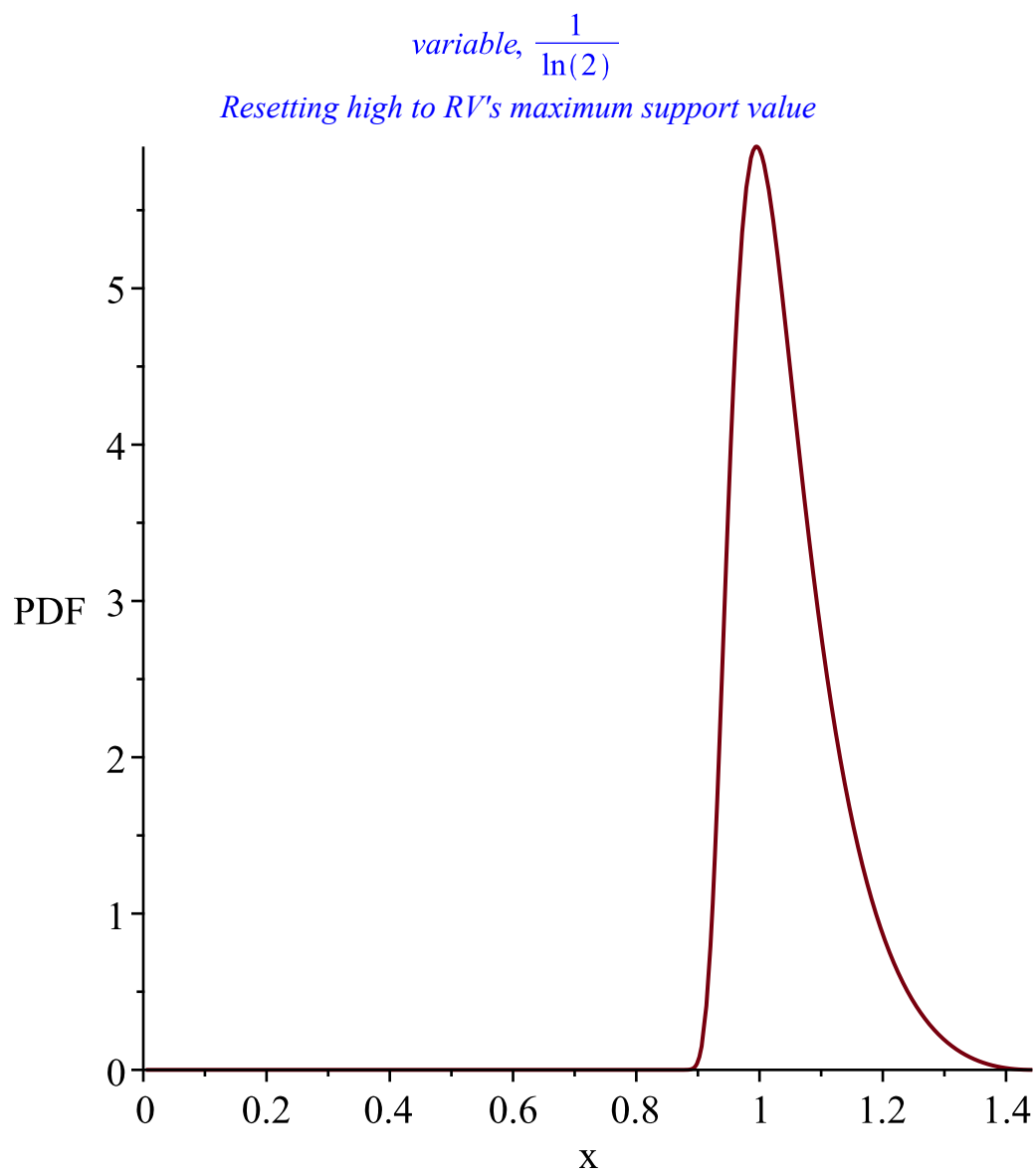




"i is", 10,
 "-----"
 "-----"

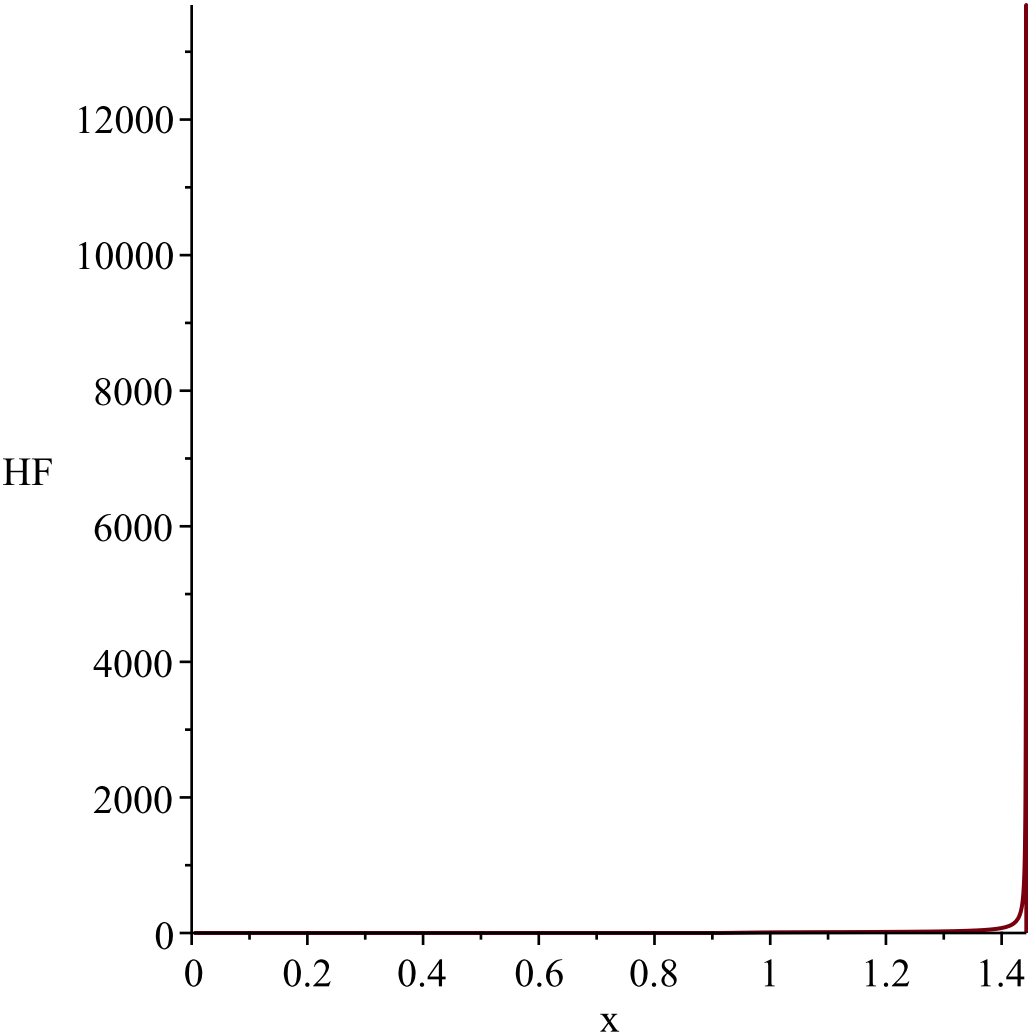
$$\begin{aligned}
 g &:= t \rightarrow \frac{1}{\ln(t+2)} \\
 l &:= 0 \\
 u &:= \infty \\
 Temp &:= \left[\left[y \rightarrow \frac{6 \left(e^{\frac{1}{y}} - 2 \right)^2 e^{\frac{\frac{3}{2} e^{\frac{1}{y}} y - 12 e^{\frac{2}{y}} y - e^2 \left(e^{\frac{1}{y}} - 2 \right)^3 y + 24 e^{\frac{1}{y}} y - 15 y + 1}}{y}}}{y^2} \right], \left[0, \right. \right. \\
 &\quad \left. \left. \frac{1}{\ln(2)} \right], ["Continuous", "PDF"] \right]
 \end{aligned}$$

*WARNING(PlotDist): High value provided by user, 40
 is greater than maximum support value of the random*



*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random*

variable, $\frac{1}{\ln(2)}$
Resetting high to RV's maximum support value



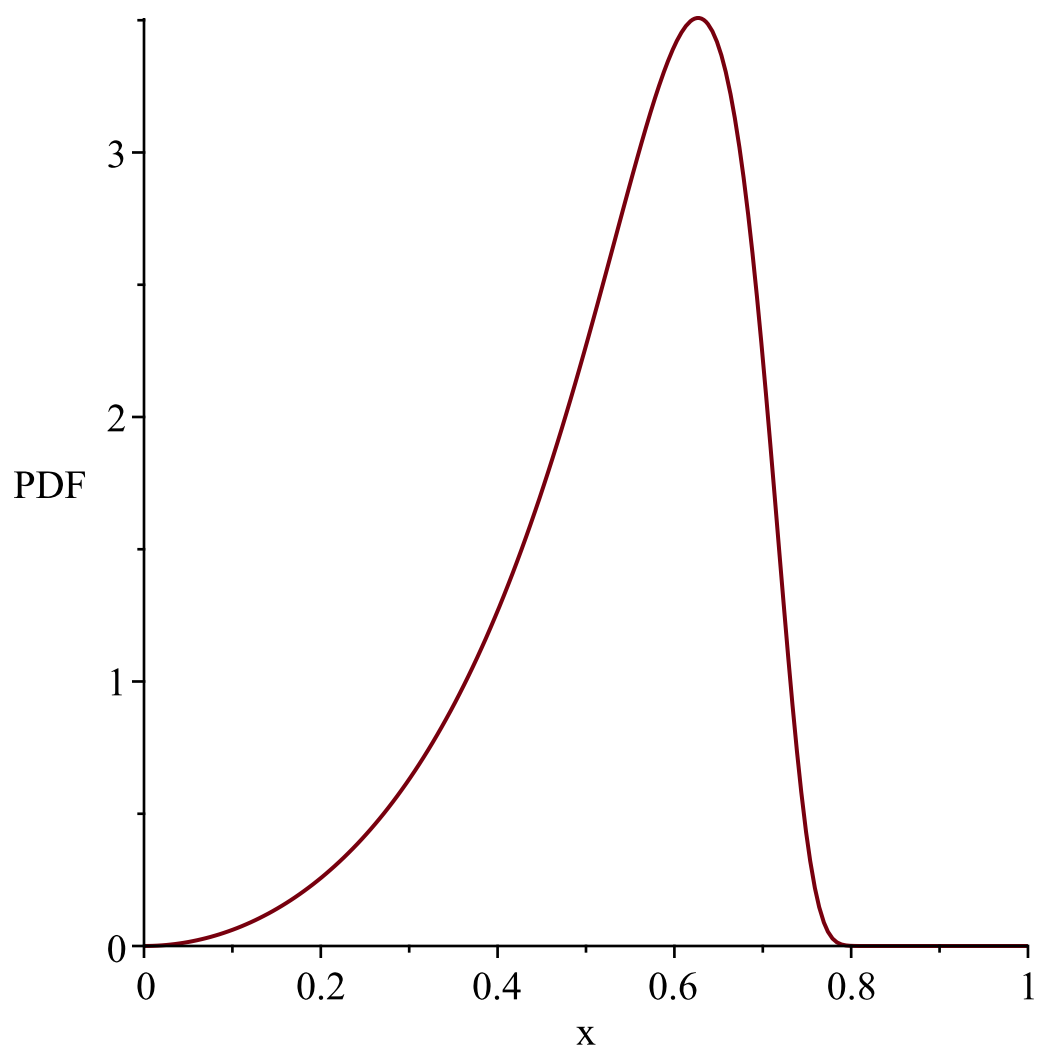
"i is", 11,
"-----"
-----"

$$g := t \rightarrow \tanh(t)$$
$$l := 0$$
$$u := \infty$$

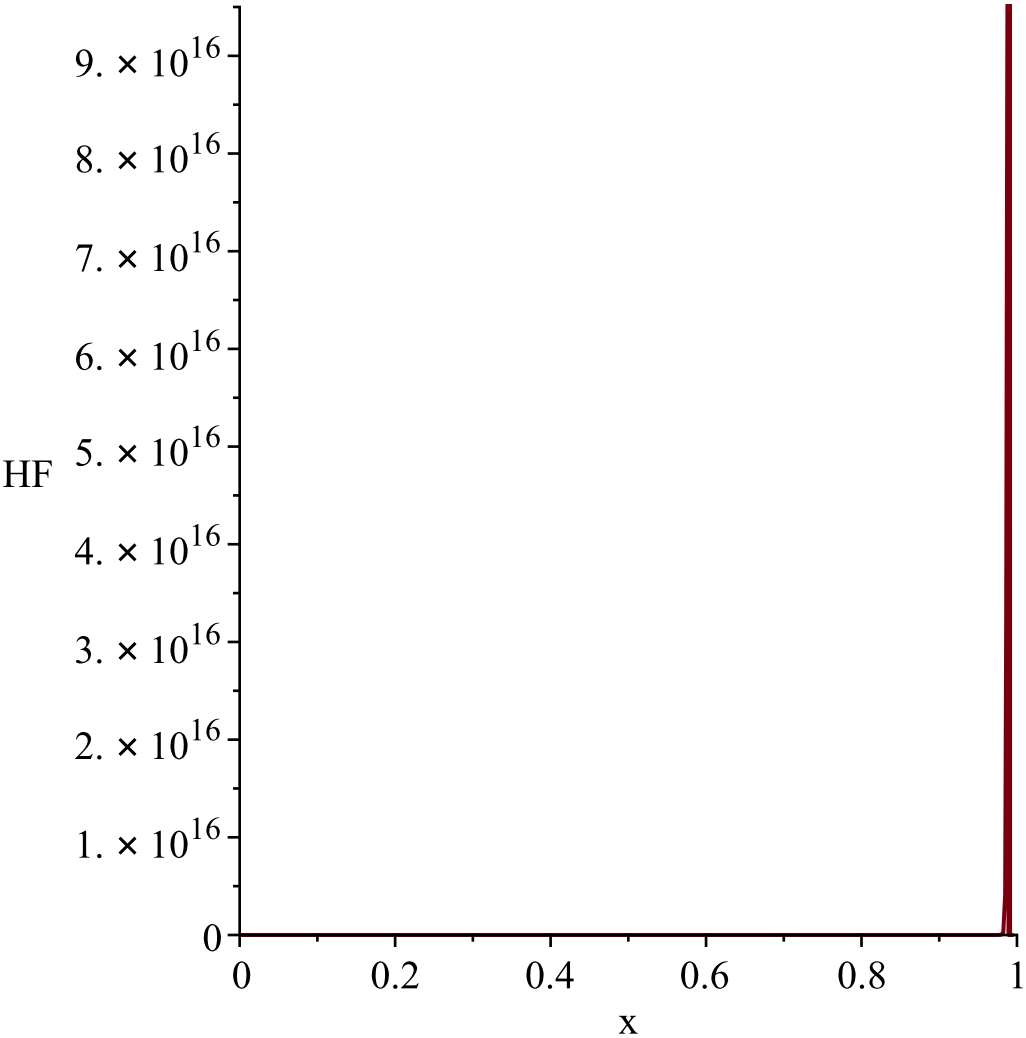
$$Temp := \left[\left[y \rightsquigarrow - \frac{6 e^{1 - e^{2 \operatorname{arctanh}(y \rightsquigarrow)^3}} + 2 \operatorname{arctanh}(y \rightsquigarrow)^3 \operatorname{arctanh}(y \rightsquigarrow)^2}{y \rightsquigarrow^2 - 1} \right], [0, 1], ["Continuous",$$

"PDF"]

*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, 1
Resetting high to RV's maximum support value*

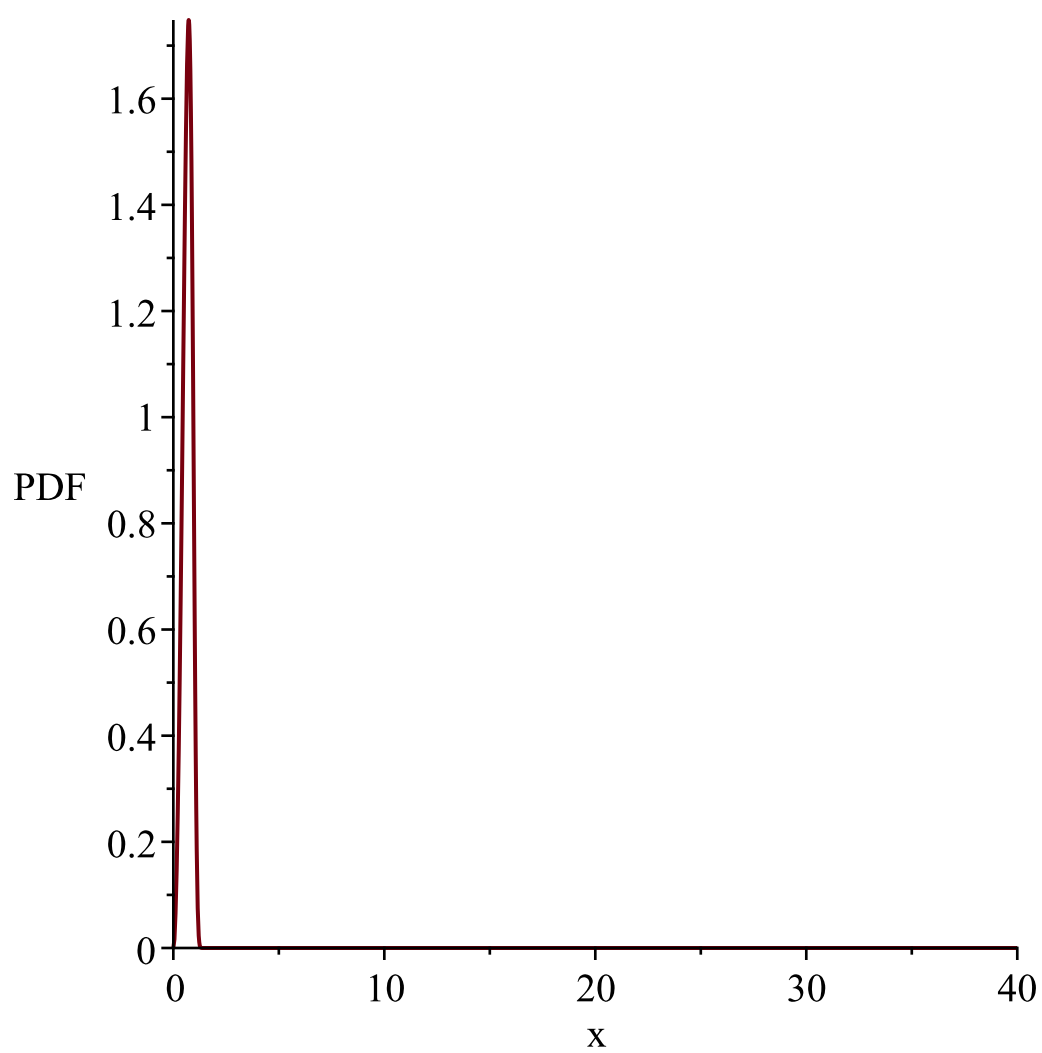


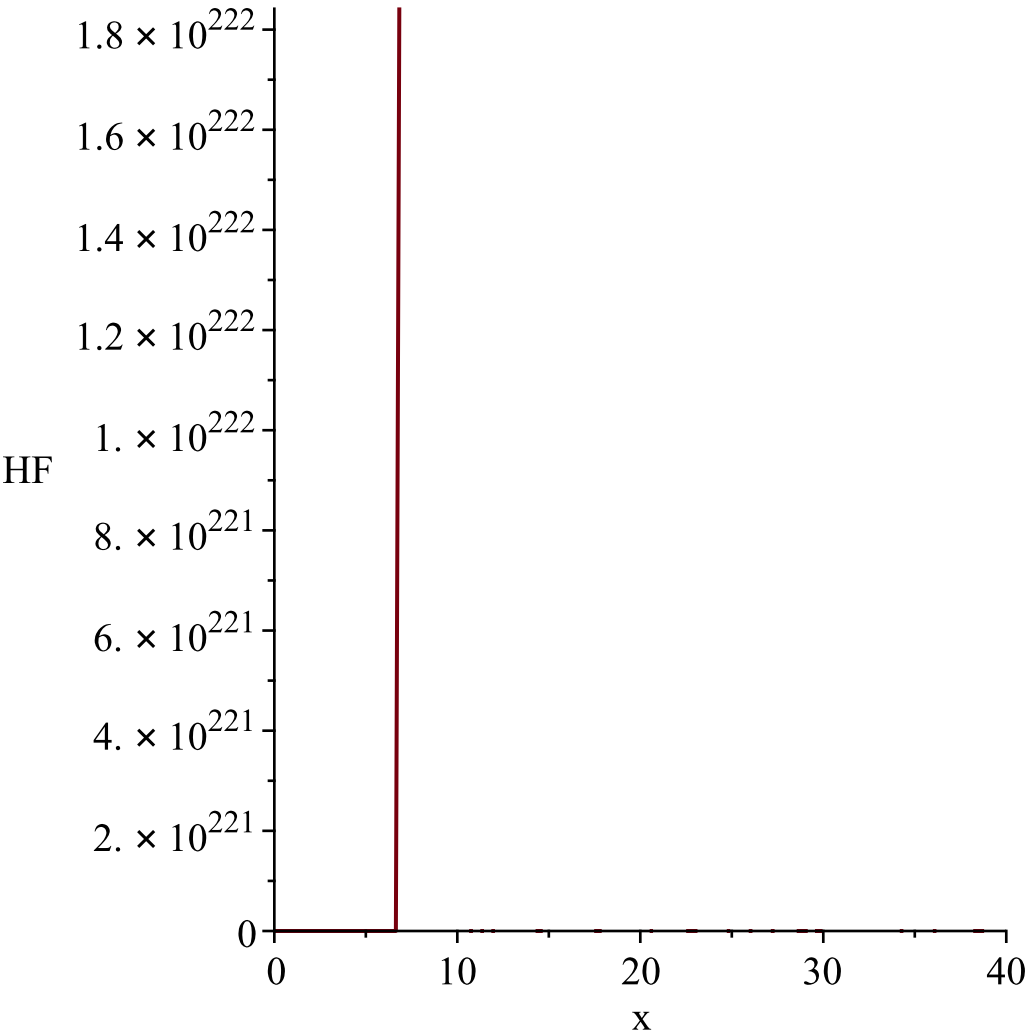
*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, 1
Resetting high to RV's maximum support value*



"i is", 12,
"-----"
-----"

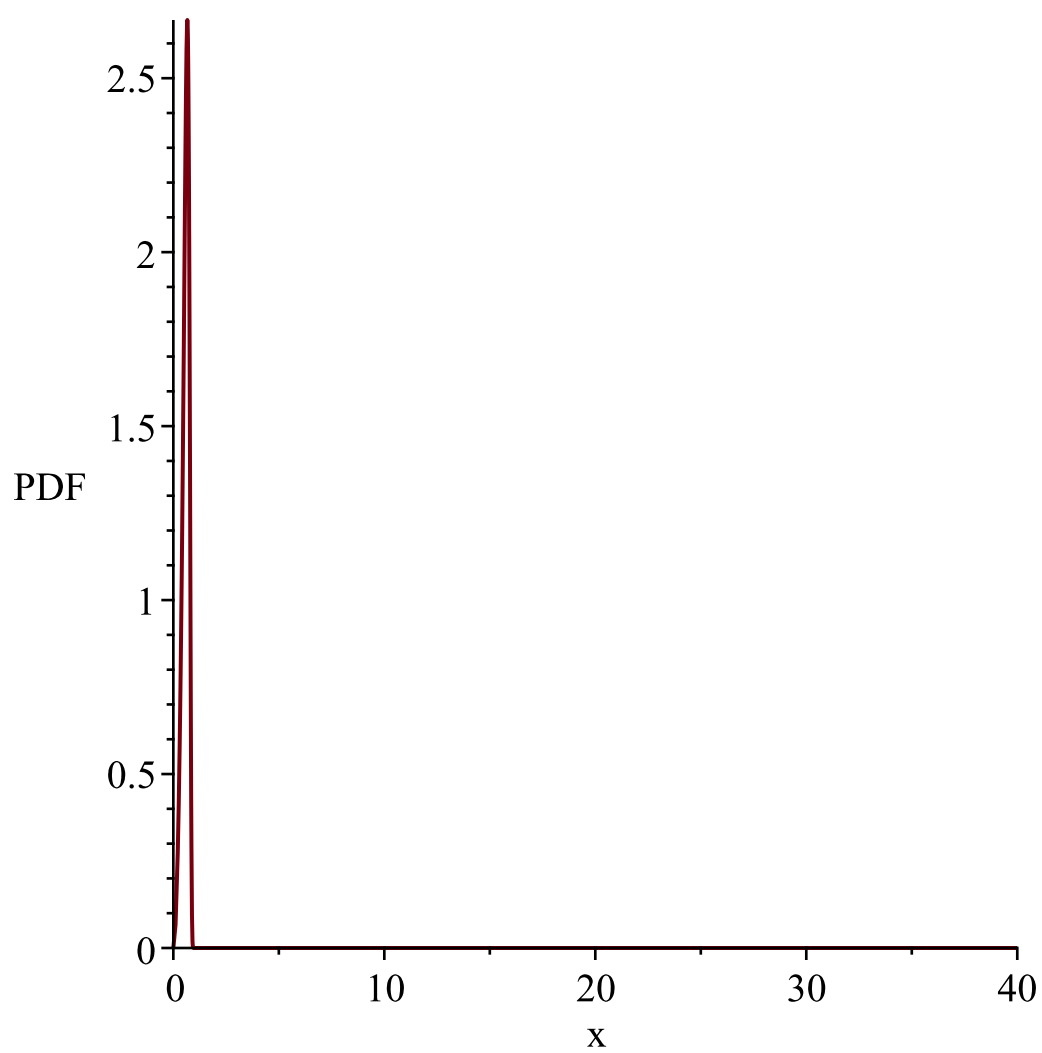
$$\begin{aligned} g &:= t \rightarrow \sinh(t) \\ l &:= 0 \\ u &:= \infty \\ Temp &:= \left[\left[y \rightsquigarrow \frac{6 \, e^1 - e^{2 \operatorname{arcsinh}(y \rightsquigarrow)^3} + 2 \operatorname{arcsinh}(y \rightsquigarrow)^3 \operatorname{arcsinh}(y \rightsquigarrow)^2}{\sqrt{y \rightsquigarrow^2 + 1}} \right], [0, \infty], ["Continuous", \right. \\ &\quad \left. "PDF"] \right] \end{aligned}$$

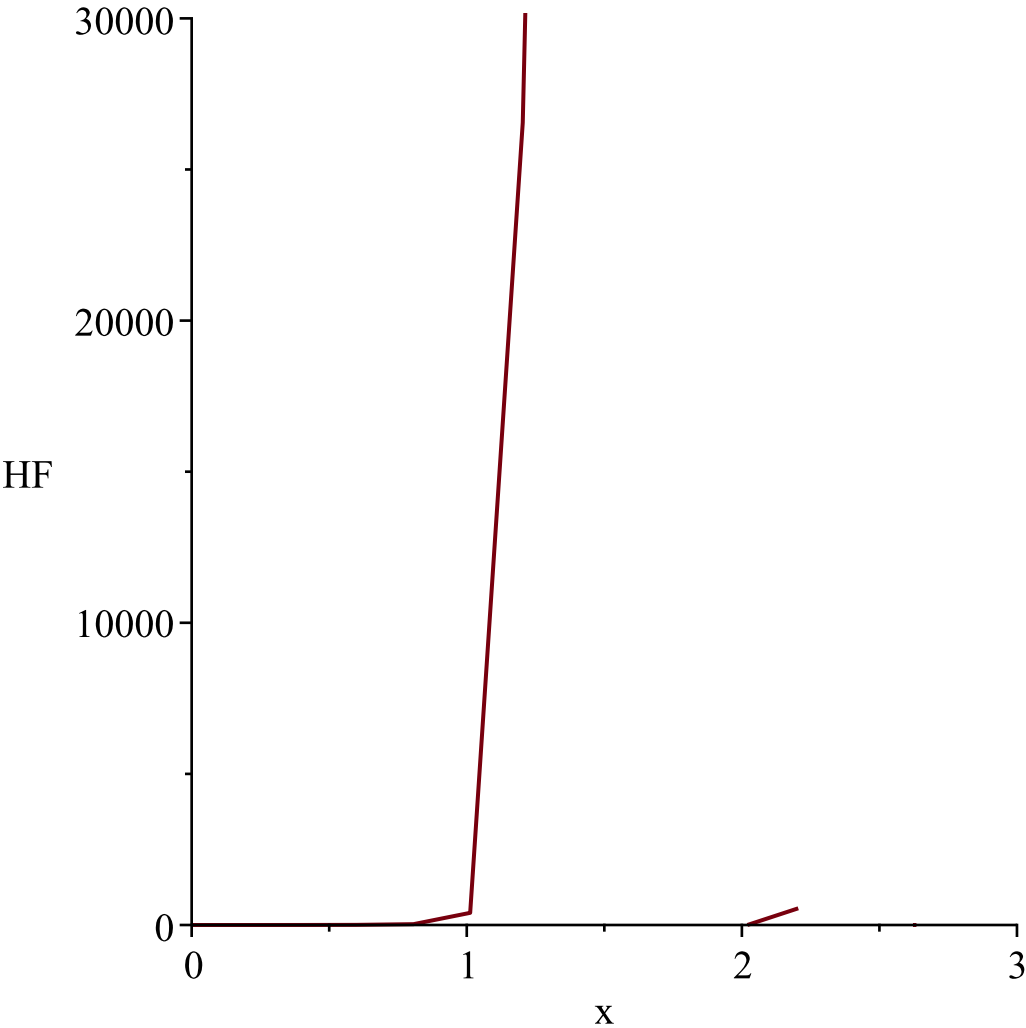




"i is", 13,
"-----"
-----"

$$g := t \rightarrow \operatorname{arcsinh}(t)$$
$$l := 0$$
$$u := \infty$$
$$Temp := \left[\left[y \sim \rightarrow 6 \, e^1 - e^{2 \sinh(y \sim)^3} + 2 \sinh(y \sim)^3 \sinh(y \sim)^2 \cosh(y \sim) \right], [0, \infty], ["Continuous", "PDF"] \right]$$



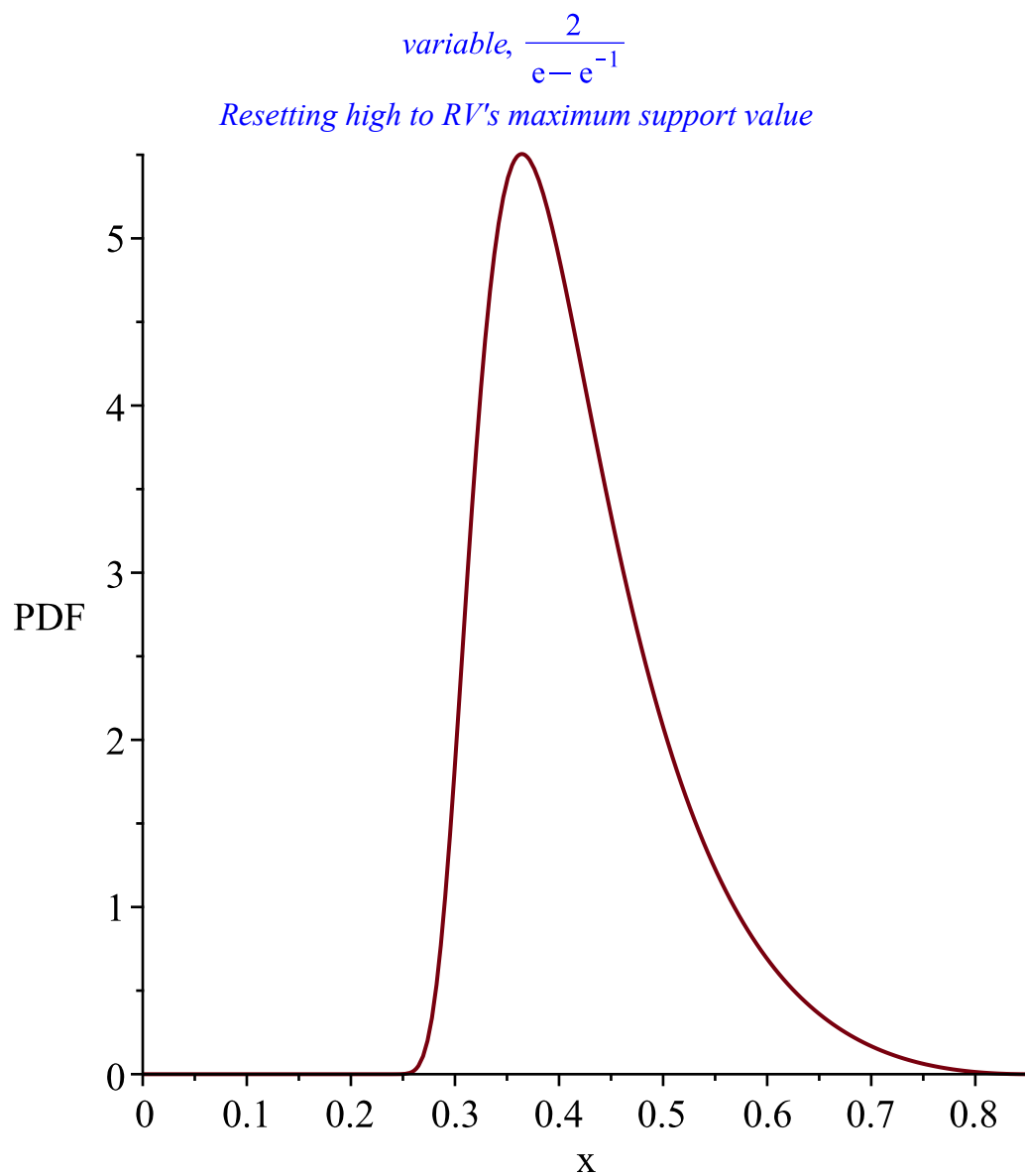


"i is", 14,
"-----"
"-----"

$$\begin{aligned} g &:= t \rightarrow \operatorname{csch}(t+1) \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

$$\begin{aligned} Temp &:= \left[\left[y_{\sim} \right. \right. \\ &\rightarrow \left. \frac{6 e^{2 \operatorname{arccsch}(y_{\sim})^3} - 6 \operatorname{arccsch}(y_{\sim})^2 + 6 \operatorname{arccsch}(y_{\sim}) - e^{2 (-1 + \operatorname{arccsch}(y_{\sim}))^3} - 1}{\sqrt{y_{\sim}^2 + 1}} (y_{\sim})^2 \right] \\ &\left. \left[0, \frac{2}{e - e^{-1}} \right], ["Continuous", "PDF"] \right] \end{aligned}$$

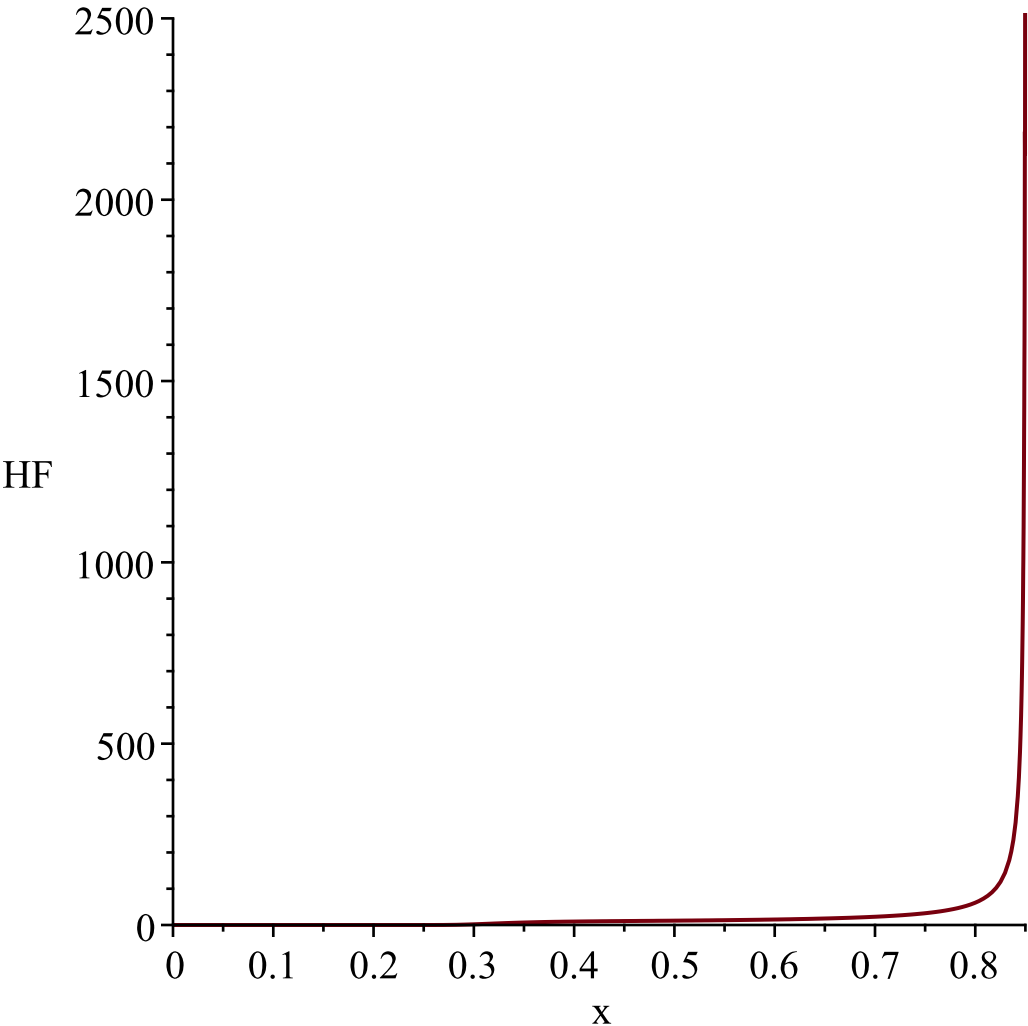
*WARNING(PlotDist): High value provided by user, 40
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*WARNING(PlotDist): High value provided by user, 40
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variable, $\frac{2}{e - e^{-1}}$

Resetting high to RV's maximum support value



"i is", 15,
"-----"
"-----"

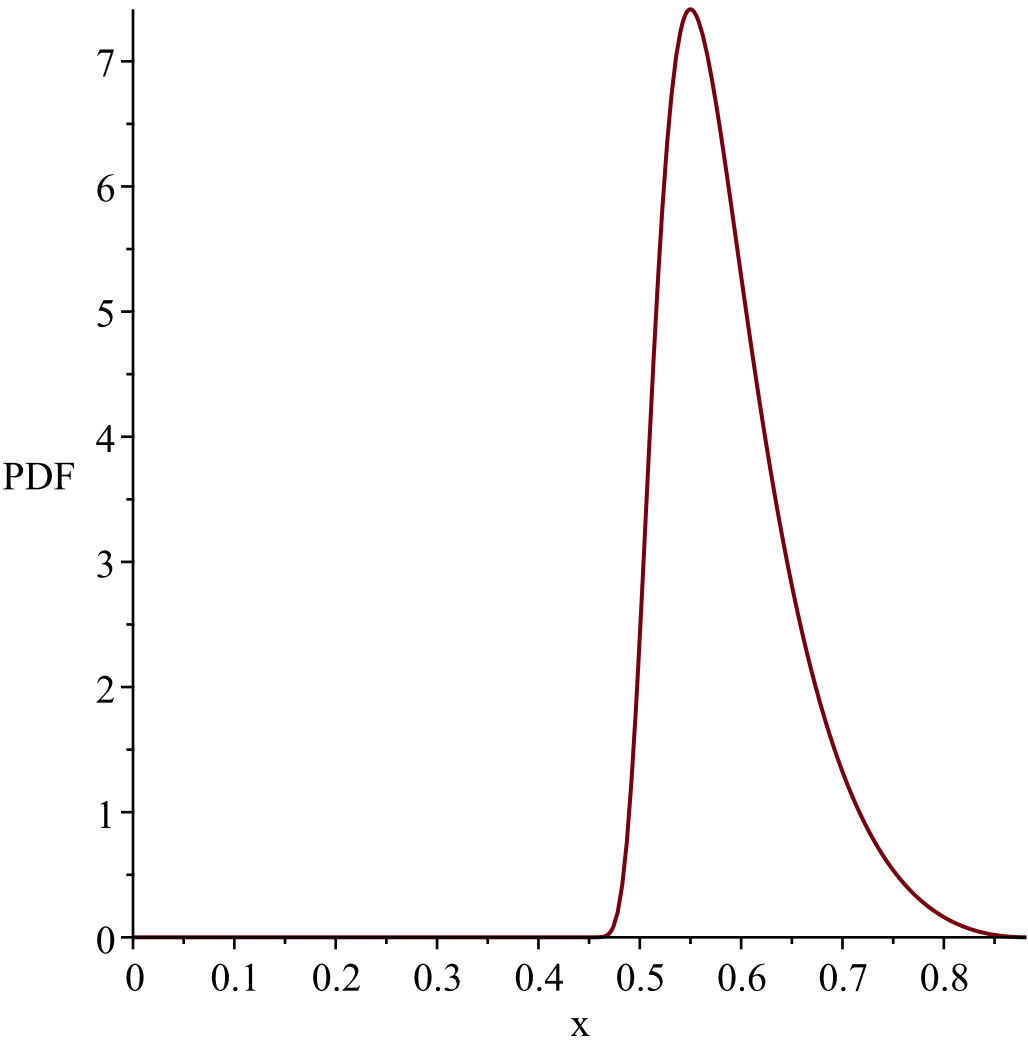
$$\begin{aligned} g &:= t \rightarrow \operatorname{arccsch}(t+1) \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

$$Temp := \left[\left[y_{\sim} \right. \right.$$

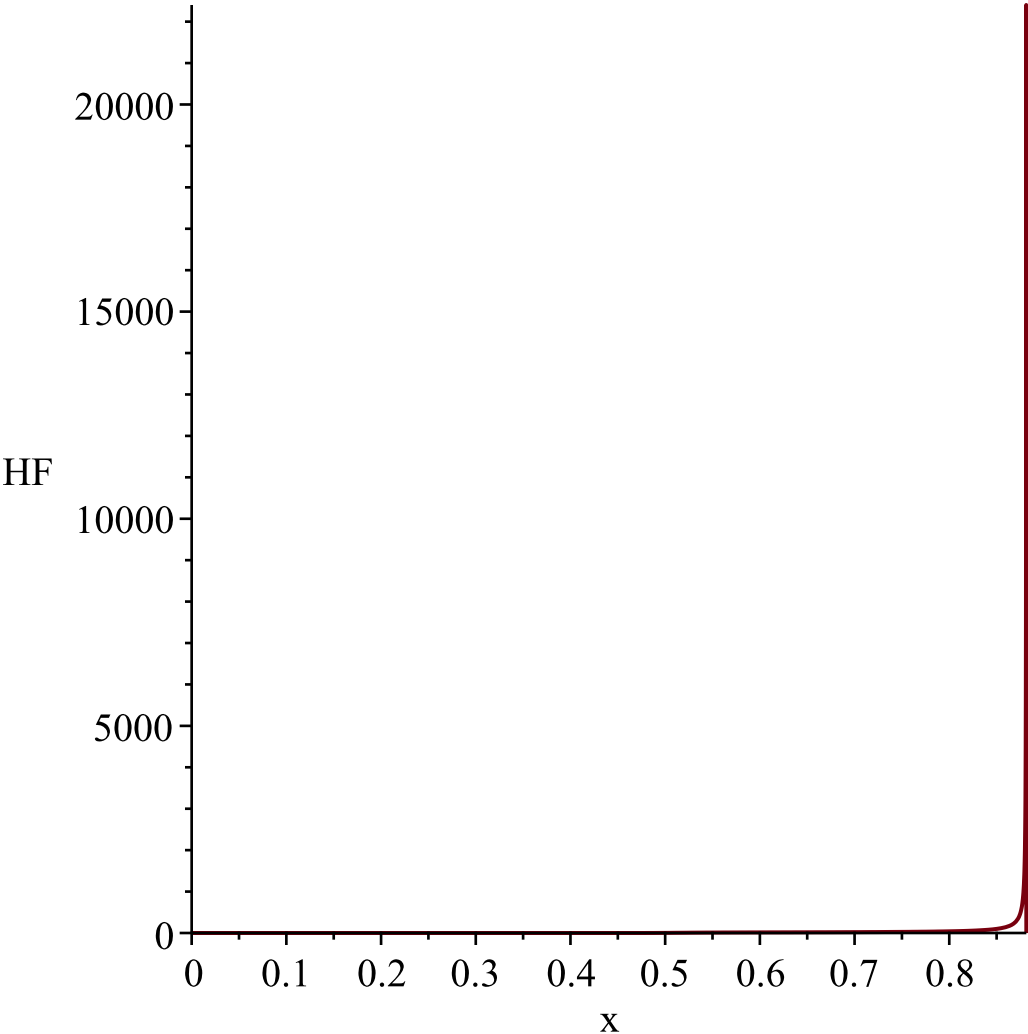
$$\rightarrow \frac{1}{\sinh(y_{\sim})^4} \left(6 e^{-\frac{2(\sinh(y_{\sim})-1)^3}{\sinh(y_{\sim})^3}} \frac{\sinh(y_{\sim})^3 + \sinh(y_{\sim})^3 - 6 \sinh(y_{\sim})^2 + 6 \sinh(y_{\sim}) - 2}{\sinh(y_{\sim})^3} (\cosh(y_{\sim})^2 \right.$$

$$\left. \left. -2 \sinh(y\sim) \right) \cosh(y\sim) \right) \right], \left[0, \ln(1 + \sqrt{2}) \right], \left[\text{"Continuous"}, \text{"PDF"} \right]$$

*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\ln(1 + \sqrt{2})$
Resetting high to RV's maximum support value*



*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\ln(1 + \sqrt{2})$
Resetting high to RV's maximum support value*



"i is", 16,
"-----"
-----"

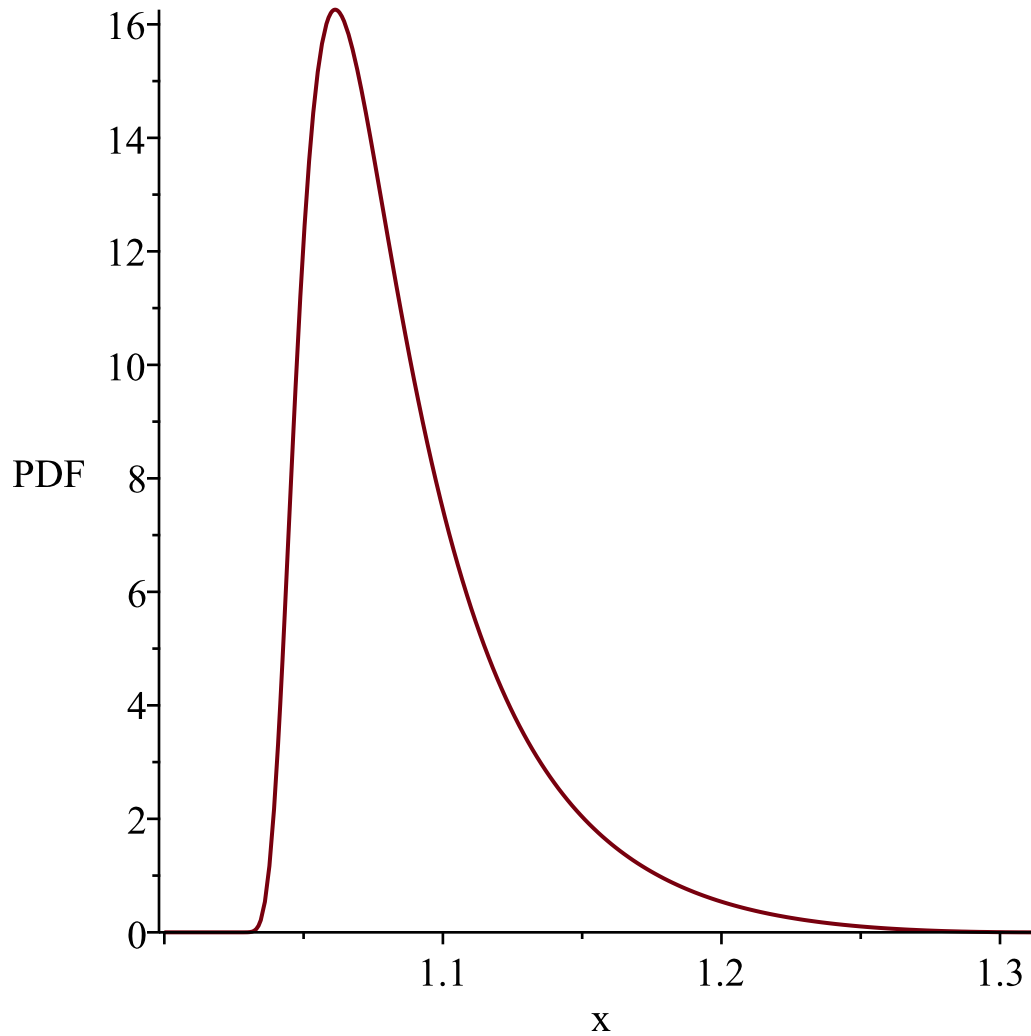
$$\begin{aligned} g &:= t \rightarrow \frac{1}{\tanh(t+1)} \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

$$\begin{aligned} Temp &:= \left[\left[y_{\sim} \right. \right. \\ &\rightarrow \frac{1}{y_{\sim}^2-1} \left(6 \, e^{2 \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right)^3} - 6 \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right)^2 - e^{2 \left(-1 + \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right) \right)^3} + 6 \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right) - 1 \left(\right. \right. \\ &\left. \left. -1 + \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right) \right)^2 \right) \right], \left[1, \frac{e+e^{-1}}{e-e^{-1}} \right], [\text{"Continuous"}, \text{"PDF"}] \end{aligned}$$

*WARNING(PlotDist): Low value provided by user, 0
is less than minimum support value of random variable
1*

*Resetting low to RV's minimum support value
WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\frac{e+e^{-1}}{e-e^{-1}}$*

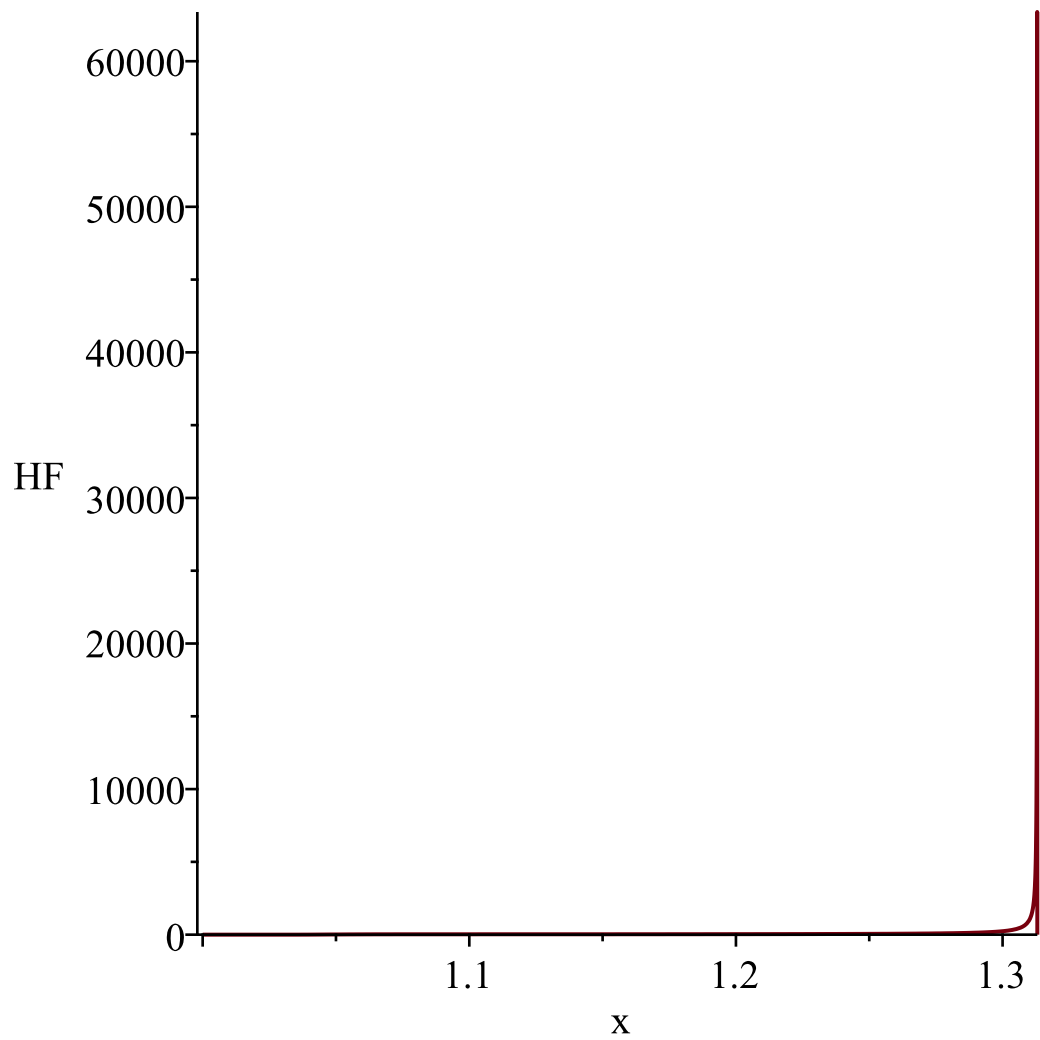
Resetting high to RV's maximum support value



*WARNING(PlotDist): Low value provided by user, 0
is less than minimum support value of random variable
1*

*Resetting low to RV's minimum support value
WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\frac{e+e^{-1}}{e-e^{-1}}$*

Resetting high to RV's maximum support value



"i is", 17,
 "-----"
 "-----"

$$g:=t\rightarrow \frac{1}{\sinh(t+1)}$$

$$l:=0$$

$$u:=\infty$$

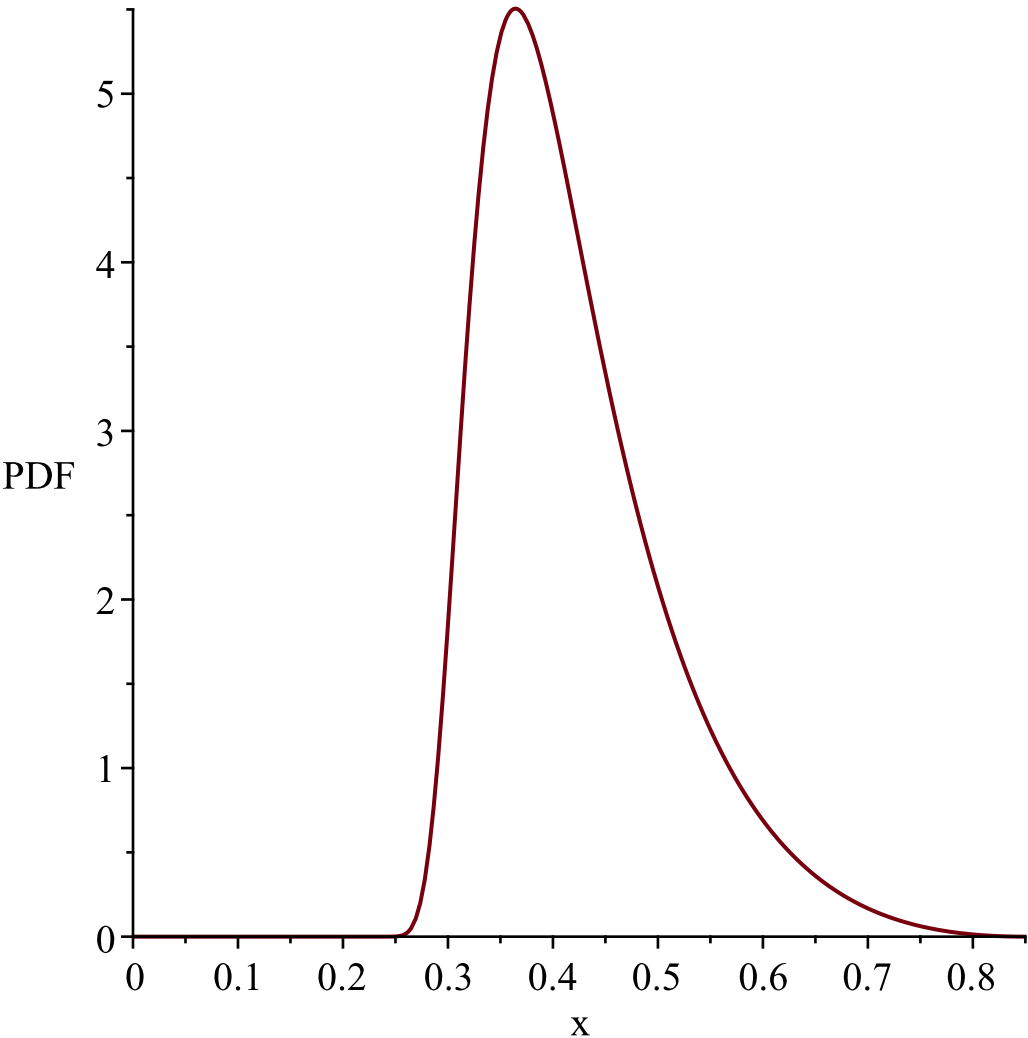
$$Temp:=\left[\left[y_{\sim}\right.\right.$$

$$\rightarrow \frac{1}{\sqrt{y_{\sim}^2+1}\left|y_{\sim}\right|}\left(6\right.$$

$$e^{\frac{2}{e} \operatorname{arcsinh}\left(\frac{1}{y}\right)^3 - 6 \operatorname{arcsinh}\left(\frac{1}{y}\right)^2 - e^2 \left(-1 + \operatorname{arcsinh}\left(\frac{1}{y}\right)\right)^3 + 6 \operatorname{arcsinh}\left(\frac{1}{y}\right) - 1} \left(-1 + \operatorname{arcsinh}\left(\frac{1}{y}\right)^2\right) \Bigg] , \left[0, \frac{2}{e - e^{-1}}\right], ["Continuous", "PDF"] \Bigg]$$

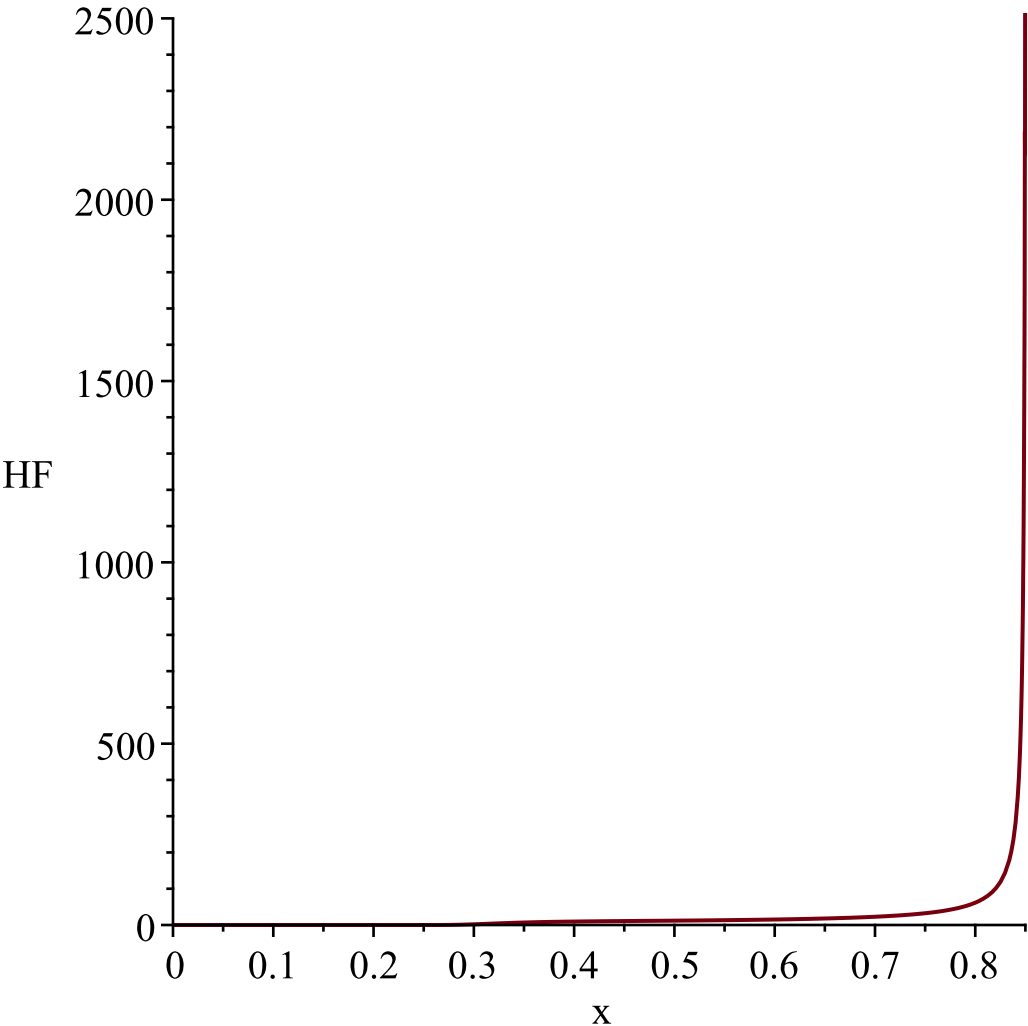
WARNING(PlotDist): High value provided by user, 40 is greater than maximum support value of the random variable, $\frac{2}{e - e^{-1}}$

Resetting high to RV's maximum support value



WARNING(PlotDist): High value provided by user, 40 is greater than maximum support value of the random variable, $\frac{2}{e - e^{-1}}$

Resetting high to RV's maximum support value



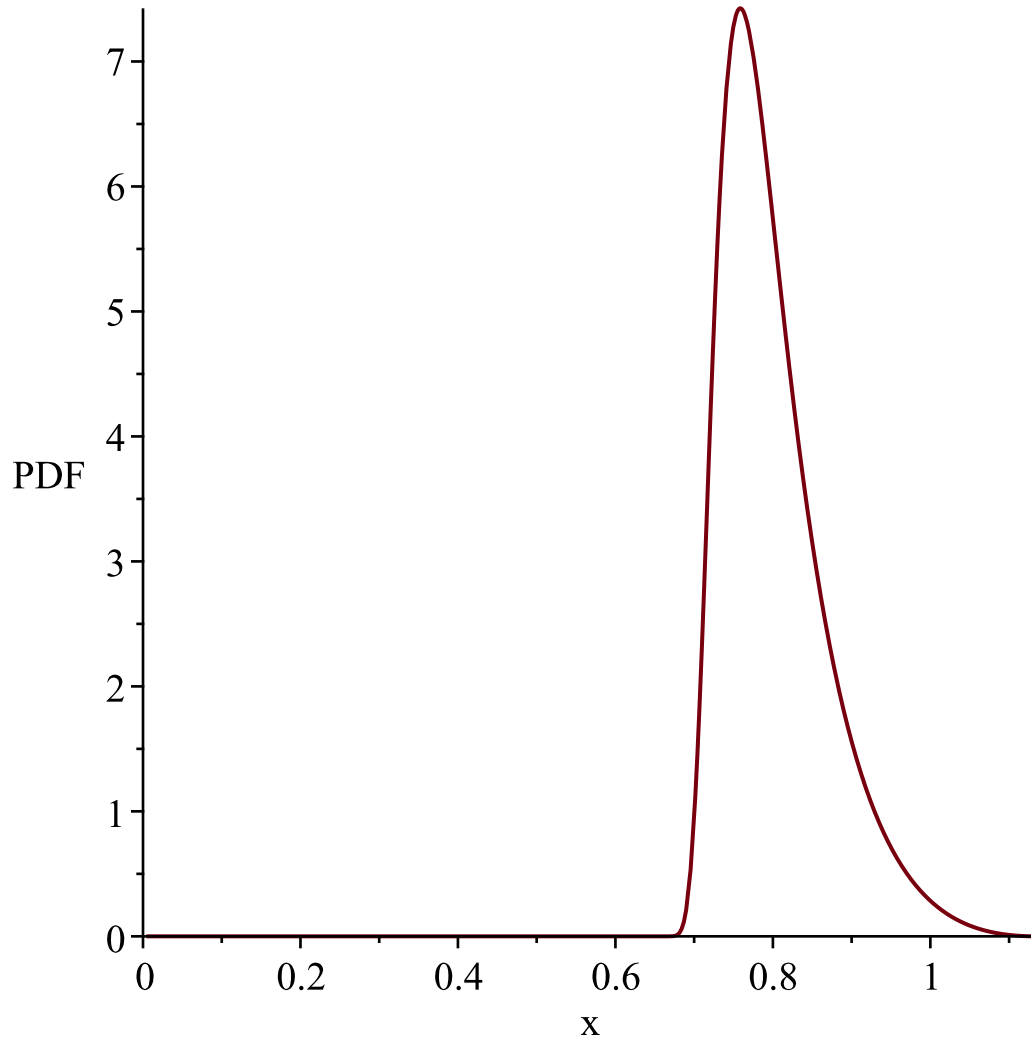
"i is", 18,
"-----"
-----"

$$\begin{aligned} g &:= t \rightarrow \frac{1}{\operatorname{arcsinh}(t+1)} \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

$$\begin{aligned} Temp &:= \left[\left[y_{\sim} \right. \right. \\ &\rightarrow \frac{1}{y_{\sim}^2} \left(6 \, \mathrm{e}^{2 \sinh \left(\frac{1}{y_{\sim}} \right)^3 - 6 \sinh \left(\frac{1}{y_{\sim}} \right)^2 - \mathrm{e}^{2 \left(-1 + \sinh \left(\frac{1}{y_{\sim}} \right) \right)^3} + 6 \sinh \left(\frac{1}{y_{\sim}} \right) - 1} \left(\cosh \left(\frac{1}{y_{\sim}} \right)^2 \right. \right. \\ &\left. \left. - 2 \sinh \left(\frac{1}{y_{\sim}} \right) \right) \cosh \left(\frac{1}{y_{\sim}} \right) \right) \right], \left[0, \frac{1}{\ln \left(1 + \sqrt{2} \right)} \right], \left[\text{"Continuous"}, \text{"PDF"} \right] \end{aligned}$$

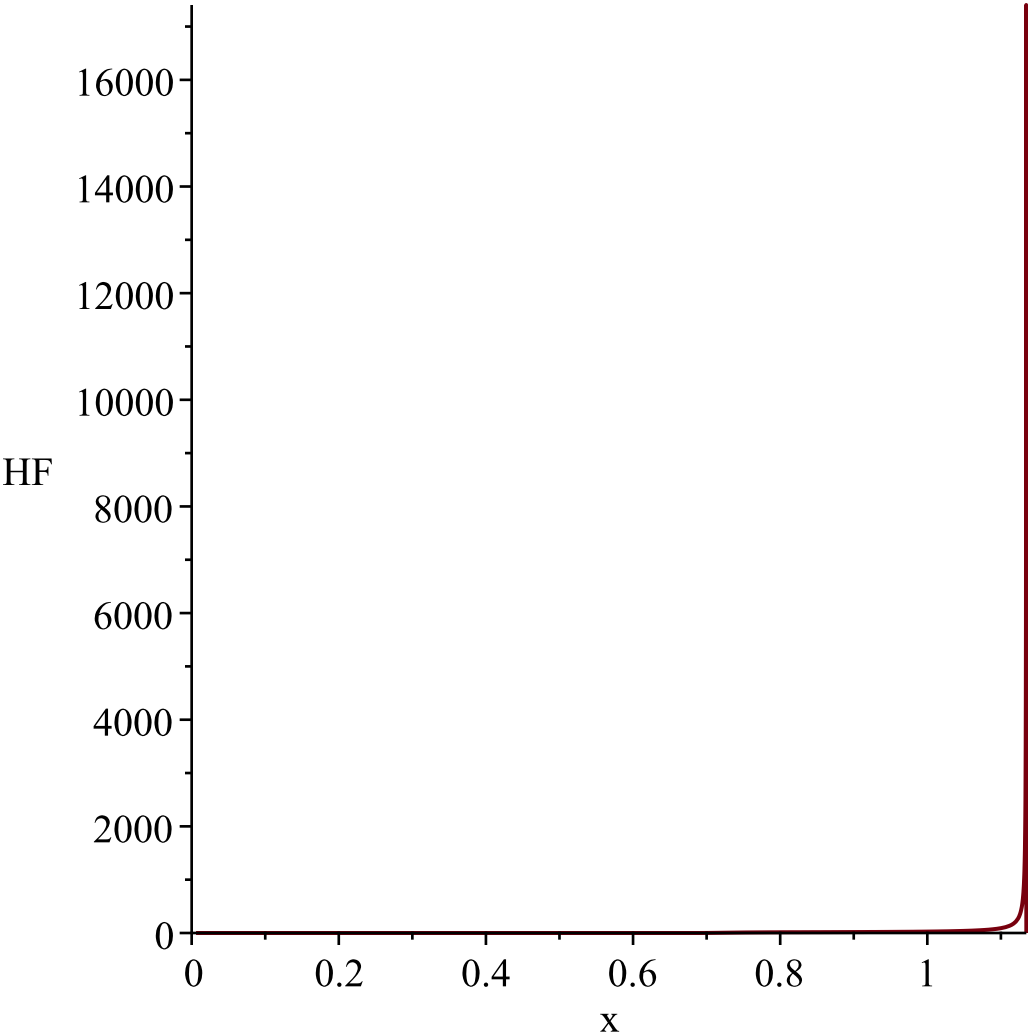
*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\frac{1}{\ln(1 + \sqrt{2})}$*

Resetting high to RV's maximum support value



*WARNING(PlotDist): High value provided by user, 40
is greater than maximum support value of the random
variable, $\frac{1}{\ln(1 + \sqrt{2})}$*

Resetting high to RV's maximum support value



"i is", 19,
"-----"
"-----"

$$g := t \mapsto \frac{1}{\operatorname{csch}(t)} + 1$$
$$l := 0$$
$$u := \infty$$

$$Temp := \left[\left[y \mapsto \frac{6 e^{1 - e^{2 \operatorname{arccsch}\left(\frac{1}{y - 1}\right)^3} + 2 \operatorname{arccsch}\left(\frac{1}{y - 1}\right)^3} \operatorname{arccsch}\left(\frac{1}{y - 1}\right)^2}{\sqrt{y^2 - 2 y + 2}} \right], [1, \infty], \right]$$

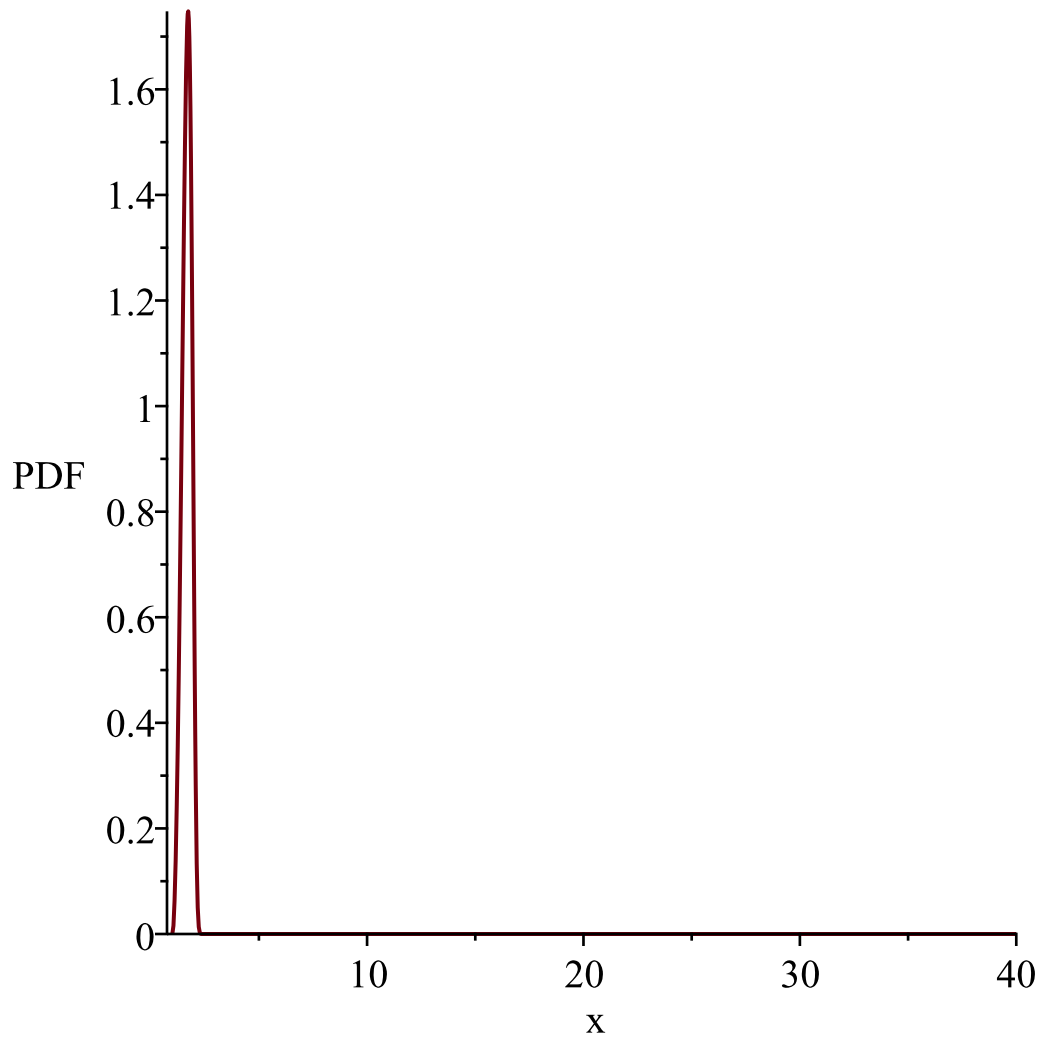
["Continuous", "PDF"]

WARNING(PlotDist): Low value provided by user, 0

is less than minimum support value of random variable

1

Resetting low to RV's minimum support value



*WARNING(PlotDist): Low value provided by user, 0
is less than minimum support value of random variable*

1

Resetting low to RV's minimum support value

Warning, computation interrupted