

"GammaRV(2.2)"

$$[x \mapsto 4 x e^{-2 x}]$$

$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = 2 e^{-2 \sqrt{x}}$$

Cumulative Distribution Function

$$F(x) = 1 - 2 \sqrt{x} e^{-2 \sqrt{x}} - e^{-2 \sqrt{x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/4 \left(W \left((-1 + s) e^{-1} \right) + 1 \right)^2]$$

Survivor Function

$$S(x) = e^{-2 \sqrt{x}} (2 \sqrt{x} + 1)$$

Hazard Function

$$h(x) = 2 (2 \sqrt{x} + 1)^{-1}$$

Mean

$$mu = 3/2$$

Variance

$$sigma^2 = \frac{21}{4}$$

Moment Function

$$m(x) = 2 \frac{\Gamma(r) \Gamma(r + 1/2) r^2}{\sqrt{\pi}} + \frac{\Gamma(r) \Gamma(r + 1/2) r}{\sqrt{\pi}}$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} -2 \frac{1}{(-t)^{3/2}} \left(\sqrt{-t} e^{tx - 2 \sqrt{x}} - \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt{x} t - 1}{\sqrt{-t}} \right) e^{-t^{-1}} - \sqrt{\pi} e^{-t^{-1}} \operatorname{erf} \left(\frac{1}{\sqrt{-t}} \right) - \sqrt{-t} \right)_1$$

$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x)=8\,x^3\mathrm{e}^{-2\,x^2}$$

Cumulative Distribution Function

$$F(x)=-2\,\mathrm{e}^{-2\,x^2}\,x^2-\mathrm{e}^{-2\,x^2}+1$$

Inverse Cumulative Distribution Function

$$F^{-1}=$$

Survivor Function

$$S(x)=\mathrm{e}^{-2\,x^2}\left(2\,x^2+1\right)$$

Hazard Function

$$h(x)=8\,\frac{x^3}{2\,x^2+1}$$

Mean

$$\mu=3/8\,\sqrt{2}\sqrt{\pi}$$

Variance

$$\sigma^2=1-\frac{9\,\pi}{32}$$

Moment Function

$$m(x)=2^{-r/2}\Gamma\left(2+r/2\right)$$

Moment Generating Function

$$1/8\,t^2+1/32\,t^3\sqrt{\pi}\mathrm{e}^{1/8\,t^2}\sqrt{2}\mathrm{erf}\left(1/4\,t\sqrt{2}\right)+3/8\,t\sqrt{\pi}\mathrm{e}^{1/8\,t^2}\sqrt{2}\mathrm{erf}\left(1/4\,t\sqrt{2}\right)+1+1/32\,t^3\sqrt{\pi}\mathrm{e}^{1/8\,t^2}\sqrt{2}$$

$$t\mapsto t^{-1}$$

Probability Distribution Function

$$f(x)=4\,\frac{1}{x^3}\mathrm{e}^{-2\,x^{-1}}$$

Cumulative Distribution Function

$$F(x)=\frac{x+2}{x}\mathrm{e}^{-2\,x^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -2 \left(W \left(-s e^{-1} \right) + 1 \right)^{-1}]$$

Survivor Function

$$S(x) = -\frac{1}{x} \left(e^{-2x^{-1}} x + 2 e^{-2x^{-1}} - x \right)$$

Hazard Function

$$h(x) = -4 \frac{1}{x^2} e^{-2x^{-1}} \left(e^{-2x^{-1}} x + 2 e^{-2x^{-1}} - x \right)^{-1}$$

Mean

$$\mu = 2$$

Variance

$$\sigma^2 = \infty$$

Moment Function

$$m(x) = 2^r \Gamma(2 - r)$$

Moment Generating Function

$$-4 t K_0 \left(2 \sqrt{-t} \sqrt{2} \right) + 2 \sqrt{-t} \sqrt{2} K_1 \left(2 \sqrt{-t} \sqrt{2} \right)_1$$

$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = 4 \tan(x) e^{-2 \tan(x)} \left(1 + (\tan(x))^2 \right)$$

Cumulative Distribution Function

$$F(x) = \begin{cases} 1 - 2 \tan(x) e^{-2 \tan(x)} - e^{-2 \tan(x)} & x \leq \pi/2 \\ -\infty & \pi/2 < x \end{cases}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\arctan(1/2 W((-1 + s) e^{-1}) + 1/2)]$$

Survivor Function

$$S(x) = \begin{cases} e^{-2 \tan(x)} (2 \tan(x) + 1) & x \leq \pi/2 \\ \infty & \pi/2 < x \end{cases}$$

Hazard Function

$$h(x) = \begin{cases} 4 \frac{\sin(x)}{(\cos(x))^2 (2 \sin(x) + \cos(x))} & x \leq \pi/2 \\ 0 & \pi/2 < x \end{cases}$$

Mean

$$\mu = 4 \int_0^{\pi/2} x \tan(x) e^{-2 \tan(x)} (1 + (\tan(x))^2) dx$$

Variance

$$\sigma^2 = 4 \int_0^{\pi/2} x^2 \tan(x) e^{-2 \tan(x)} (1 + (\tan(x))^2) dx - 16 \left(\int_0^{\pi/2} x \tan(x) e^{-2 \tan(x)} (1 + (\tan(x))^2) dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\pi/2} 4 x^r \tan(x) e^{-2 \tan(x)} (1 + (\tan(x))^2) dx$$

Moment Generating Function

$$4 \int_0^{\pi/2} \tan(x) (1 + (\tan(x))^2) e^{tx-2 \tan(x)} dx$$

$$t \mapsto e^t$$

Probability Distribution Function

$$f(x) = 4 \frac{\ln(x)}{x^3}$$

Cumulative Distribution Function

$$F(x) = -\frac{-x^2 + 2 \ln(x) + 1}{x^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \frac{1}{\sqrt{\frac{s-1}{W((s-1)e^{-1})}}}]$$

Survivor Function

$$S(x) = \frac{2 \ln(x) + 1}{x^2}$$

Hazard Function

$$h(x) = 4 \frac{\ln(x)}{x(2 \ln(x) + 1)}$$

Mean

$$\mu = 4$$

Variance

$$\sigma^2 = \infty$$

$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = 4e^{2x-2e^x}$$

Cumulative Distribution Function

$$F(x) = 1 - 2e^{x-2e^x} - e^{-2e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf} \left(-Z + \ln(2) - \ln(1 - e^{-2e^{-Z}} - s) - 2e^{-Z} \right)]$$

Survivor Function

$$S(x) = 2e^{x-2e^x} + e^{-2e^x}$$

Hazard Function

$$h(x) = 4 \frac{e^{2x-2e^x}}{2e^{x-2e^x} + e^{-2e^x}}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 4xe^{2x-2e^x} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 4x^2 e^{2x-2e^x} dx - \left(\int_{-\infty}^{\infty} 4x e^{2x-2e^x} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 4x^r e^{2x-2e^x} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 4e^{tx+2x-2e^x} dx_1$$

$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = -4 \ln(x) x$$

Cumulative Distribution Function

$$F(x) = -x^2 (2 \ln(x) - 1)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \sqrt{-\frac{s}{W(-se^{-1})}}]$$

Survivor Function

$$S(x) = 2 \ln(x) x^2 - x^2 + 1$$

Hazard Function

$$h(x) = -4 \frac{\ln(x) x}{2 \ln(x) x^2 - x^2 + 1}$$

Mean

$$\mu = 4/9$$

Variance

$$\sigma^2 = \frac{17}{324}$$

Moment Function

$$m(x) = 4 \left(r^2 + 4 r + 4 \right)^{-1}$$

Moment Generating Function

$$4 \frac{-1 + \gamma + \ln(-t) + e^t + Ei(1, -t)}{t^2} \quad 1$$

$$t \mapsto -\ln(t)$$

Probability Distribution Function

$$f(x) = 4 e^{-2x-2e^{-x}}$$

Cumulative Distribution Function

$$F(x) = (2 + e^x) e^{-(xe^x+2)e^{-x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto RootOf \left(\ln \left(\frac{s}{2 + e^{-Z}} \right) e^{-Z} + -Z e^{-Z} + 2 \right)]$$

Survivor Function

$$S(x) = -e^{-2e^{-x}} - 2e^{-2e^{-x}-x} + 1$$

Hazard Function

$$h(x) = -4 \frac{e^{-2x-2e^{-x}}}{e^{-2e^{-x}} + 2e^{-2e^{-x}-x} - 1}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 4 x e^{-2x-2e^{-x}} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 4 x^2 e^{-2x-2e^{-x}} dx - \left(\int_{-\infty}^{\infty} 4 x e^{-2x-2e^{-x}} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 4 x^r e^{-2x-2e^{-x}} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 4 e^{tx-2x-2e^{-x}} dx_1$$

$$t \mapsto \ln(t+1)$$

Probability Distribution Function

$$f(x) = 4 (e^x - 1) e^{-2e^x+2+x}$$

Cumulative Distribution Function

$$F(x) = 1 - 2e^{-2e^x+2+x} + e^{2-2e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf} \left(-Z + \ln(2) - \ln(1 + e^{2-2e^{-Z}} - s) + 2 - 2e^{-Z} \right)]$$

Survivor Function

$$S(x) = 2e^{-2e^x+2+x} - e^{2-2e^x}$$

Hazard Function

$$h(x) = 4 \frac{(e^x - 1) e^{-2e^x+2+x}}{2e^{-2e^x+2+x} - e^{2-2e^x}}$$

Mean

$$\mu = \int_0^{\infty} 4x (e^x - 1) e^{-2e^x+2+x} dx$$

Variance

$$\sigma^2 = \int_0^{\infty} 4x^2 (e^x - 1) e^{-2e^x+2+x} dx - \left(\int_0^{\infty} 4x (e^x - 1) e^{-2e^x+2+x} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\infty} 4x^r (e^x - 1) e^{-2e^x+2+x} dx$$

Moment Generating Function

$$\int_0^{\infty} 4 (e^x - 1) e^{tx-2e^x+2+x} dx_1$$

$$t \mapsto (\ln(t+2))^{-1}$$

Probability Distribution Function

$$f(x) = 4 \frac{e^{x^{-1}} - 2}{x^2} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}}$$

Cumulative Distribution Function

$$F(x) = e^{4-2e^{x^{-1}}} (2e^{x^{-1}} - 3)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto (-\ln(2) + \ln(-W(-se^{-1}) + 3))]^{-1}$$

Survivor Function

$$S(x) = -2e^{4-2e^{x^{-1}}+x^{-1}} + 3e^{4-2e^{x^{-1}}} + 1$$

Hazard Function

$$h(x) = 4 \frac{e^{x^{-1}} - 2}{x^2} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} \left(-2e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} + 3e^{4-2e^{x^{-1}}} + 1 \right)^{-1}$$

Mean

$$mu = 4 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} - 2}{x} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx$$

Variance

$$sigma^2 = 4 \int_0^{(\ln(2))^{-1}} (e^{x^{-1}} - 2) e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx - 16 \left(\int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} - 2}{x} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} 4 \frac{x^r (e^{x^{-1}} - 2)}{x^2} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx$$

Moment Generating Function

$$4 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} - 2}{x^2} e^{-\frac{-tx^2+2e^{x^{-1}}x-4x-1}{x}} dx_1$$

$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = 4 \frac{\operatorname{arctanh}(x)}{(x+1)^2}$$

Cumulative Distribution Function

$$F(x) = -\frac{\ln(1-x)x - \ln(x+1)x + 4 \operatorname{arctanh}(x) + \ln(1-x) - \ln(x+1) - 2x}{x+1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -e^{\operatorname{RootOf}(-\ln(-e^{-Z}+2)e^{-Z}+_{-Z}e^{-Z}+se^{-Z}+2\ln(-e^{-Z}+2)+4\operatorname{arctanh}(e^{-Z}-1)-2e^{-Z}-2_{-Z}-2s+2)+1}]$$

Survivor Function

$$S(x) = \frac{\ln(1-x)x - \ln(x+1)x + \ln(1-x) - \ln(x+1) + 4 \operatorname{arctanh}(x) - x + 1}{x+1}$$

Hazard Function

$$h(x) = 4 \frac{\operatorname{arctanh}(x)}{(x+1)(\ln(1-x)x - \ln(x+1)x + \ln(1-x) - \ln(x+1) + 4 \operatorname{arctanh}(x) - x + 1)}$$

Mean

$$\mu = 1/6 \pi^2 - 1$$

Variance

$$\sigma^2 = 4 \ln(2) - 1/36 \pi^4$$

Moment Function

$$m(x) = \int_0^1 4 \frac{x^r \operatorname{arctanh}(x)}{(x+1)^2} dx$$

Moment Generating Function

$$4 \int_0^1 \frac{e^{tx} \operatorname{arctanh}(x)}{(x+1)^2} dx_1$$

$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = 4 \frac{\operatorname{arcsinh}(x)}{(x + \sqrt{x^2 + 1})^2 \sqrt{x^2 + 1}}$$

Cumulative Distribution Function

$$F(x) = 4x^2 \ln(-x + \sqrt{x^2 + 1}) - 2x^2 - 4x\sqrt{x^2 + 1} \ln(-x + \sqrt{x^2 + 1}) + 2x\sqrt{x^2 + 1} + 2 \ln(-x + \sqrt{x^2 + 1})$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 \frac{-s + 1 + W((s - 1)e^{-1})}{W((s - 1)e^{-1})} \frac{1}{\sqrt{\frac{s-1}{W((s-1)e^{-1})}}}]$$

Survivor Function

$$S(x) = 1 - 4x^2 \ln(-x + \sqrt{x^2 + 1}) + 2x^2 + 4x\sqrt{x^2 + 1} \ln(-x + \sqrt{x^2 + 1}) - 2x\sqrt{x^2 + 1} - 2 \ln(-x + \sqrt{x^2 + 1})$$

Hazard Function

$$h(x) = 4 \frac{\operatorname{arcsinh}(x)}{(x + \sqrt{x^2 + 1})^2 \sqrt{x^2 + 1} (1 - 4x^2 \ln(-x + \sqrt{x^2 + 1}) + 2x^2 + 4x\sqrt{x^2 + 1} \ln(-x + \sqrt{x^2 + 1}) - 2x\sqrt{x^2 + 1} - 2 \ln(-x + \sqrt{x^2 + 1}))}$$

Mean

$$\mu = \frac{16}{9}$$

Variance

$$\sigma^2 = \infty$$

Moment Function

$$m(x) = \int_0^\infty 4 \frac{x^r \operatorname{arcsinh}(x)}{(x + \sqrt{x^2 + 1})^2 \sqrt{x^2 + 1}} dx$$

Moment Generating Function

$$\int_0^\infty 4 \frac{e^{tx} \operatorname{arcsinh}(x)}{(x + \sqrt{x^2 + 1})^2 \sqrt{x^2 + 1}} dx_1$$

$$t \mapsto \operatorname{arcsinh}(t)$$

Probability Distribution Function

$$f(x) = 4 \sinh(x) e^{-2 \sinh(x)} \cosh(x)$$

Cumulative Distribution Function

$$F(x) = - \left(e^{(2xe^x+1)e^{-x}} + e^{(xe^x+1)e^{-x}} - e^{e^x+x} - e^{e^{-x}} \right) e^{-e^x-x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf} \left(e^{(2-Ze^{-Z}+1)e^{-Z}} + se^{-Z+e^{-Z}} + e^{(-Ze^{-Z}+1)e^{-Z}} - e^{-Z+e^{-Z}} - e^{e^{-Z}} \right)]$$

Survivor Function

$$S(x) = -e^{-e^x-x+e^{-x}} + e^{-e^x-x+(2xe^x+1)e^{-x}} + e^{-e^x-x+(xe^x+1)e^{-x}}$$

Hazard Function

$$h(x) = 4 \frac{\sinh(x) e^{-2 \sinh(x)} \cosh(x)}{e^{-(e^2x-xe^x-1)e^{-x}} + e^{-(e^2x-1)e^{-x}} - e^{-(e^2x+xe^x-1)e^{-x}}}$$

Mean

$$mu = \int_0^\infty 2xe^{-2 \sinh(x)} \sinh(2x) \, dx$$

Variance

$$sigma^2 = \int_0^\infty 2x^2e^{-2 \sinh(x)} \sinh(2x) \, dx - \left(\int_0^\infty 2xe^{-2 \sinh(x)} \sinh(2x) \, dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 4x^r \sinh(x) e^{-2 \sinh(x)} \cosh(x) \, dx$$

Moment Generating Function

$$\int_0^\infty 2e^{tx-2 \sinh(x)} \sinh(2x) \, dx_1$$

$$t \mapsto \operatorname{csch}(t+1)$$

Probability Distribution Function

$$f(x) = 4 \frac{(-1 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = 4 \int_0^x \frac{(-1 + \operatorname{arccsch}(t)) e^{2-2 \operatorname{arccsch}(t)}}{\sqrt{t^2 + 1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 4 \int_0^x \frac{(-1 + \operatorname{arccsch}(t)) e^{2-2 \operatorname{arccsch}(t)}}{\sqrt{t^2 + 1} |t|} dt$$

Hazard Function

$$h(x) = -4 \frac{(-1 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1} |x|} \left(-1 + 4 \int_0^x \frac{(-1 + \operatorname{arccsch}(t)) e^{2-2 \operatorname{arccsch}(t)}}{\sqrt{t^2 + 1} |t|} dt \right)^{-1}$$

Mean

$$mu = 4 \int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1}} dx$$

Variance

$$sigma^2 = 4 \int_0^{2 \frac{e}{e^2-1}} \frac{x (-1 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1}} dx - 16 \left(\int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{-2(-e+e^{-1})^{-1}} 4 \frac{x^r (-1 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1} |x|} dx$$

Moment Generating Function

$$4 \int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arccsch}(x)) e^{tx+2-2 \operatorname{arccsch}(x)}}{x \sqrt{x^2 + 1}} dx_1$$

$$t \mapsto \operatorname{arccsch}(t + 1)$$

Probability Distribution Function

$$f(x) = -4 \frac{(\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{2 \frac{\sinh(x)-1}{\sinh(x)}}$$

Cumulative Distribution Function

$$F(x) = \frac{-e^{2x} + 4e^x + 1}{e^{2x} - 1} e^{-2 \frac{-e^{2x} + 1 + 2e^x}{e^{2x} - 1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = \frac{1}{e^{2x} - 1} \left(e^{2 \frac{e^{2x} - 1 - 2e^x}{e^{2x} - 1} + 2x} - 4e^{2 \frac{e^{2x} - 1 - 2e^x}{e^{2x} - 1} + x} + e^{2x} - e^{2 \frac{e^{2x} - 1 - 2e^x}{e^{2x} - 1}} - 1 \right)$$

Hazard Function

$$h(x) = -4 \frac{(\sinh(x) - 1) \cosh(x) (e^{2x} - 1)}{(\sinh(x))^3} e^{2 \frac{\sinh(x)-1}{\sinh(x)}} \left(e^{-2 \frac{-xe^{2x} + 2e^x - e^{2x} + x + 1}{e^{2x} - 1}} - 4e^{-\frac{-xe^{2x} + 4e^x - 2e^{2x} + x + 1}{e^{2x} - 1}} \right)$$

Mean

$$mu = -4 \int_0^{\ln(1+\sqrt{2})} \frac{x (\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{2 \frac{\sinh(x)-1}{\sinh(x)}} dx$$

Variance

$$sigma^2 = -4 \int_0^{\ln(1+\sqrt{2})} \frac{x^2 (\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{2 \frac{\sinh(x)-1}{\sinh(x)}} dx - 16 \left(\int_0^{\ln(1+\sqrt{2})} \frac{x (\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{2 \frac{\sinh(x)-1}{\sinh(x)}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\ln(1+\sqrt{2})} -4 \frac{x^r (\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{2 \frac{\sinh(x)-1}{\sinh(x)}} dx$$

Moment Generating Function

$$-4 \int_0^{\ln(1+\sqrt{2})} \frac{(\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{\frac{tx \sinh(x) + 2 \sinh(x) - 2}{\sinh(x)}} dx_1$$

$$t \mapsto (\tanh(t + 1))^{-1}$$

Probability Distribution Function

$$f(x) = 4 \frac{(-1 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1}$$

Cumulative Distribution Function

$$F(x) = 4 \int_1^x \frac{(-1 + \operatorname{arctanh}(t^{-1})) e^{2-2 \operatorname{arctanh}(t^{-1})}}{t^2 - 1} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 4 \int_1^x \frac{(-1 + \operatorname{arctanh}(t^{-1})) e^{2-2 \operatorname{arctanh}(t^{-1})}}{t^2 - 1} dt$$

Hazard Function

$$h(x) = -4 \frac{(-1 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} \left(-1 + 4 \int_1^x \frac{(-1 + \operatorname{arctanh}(t^{-1})) e^{2-2 \operatorname{arctanh}(t^{-1})}}{t^2 - 1} dt \right)$$

Mean

$$mu = 4 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x (-1 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx$$

Variance

$$sigma^2 = 4 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^2 (-1 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx - 16 \left(\int_1^{\frac{e^2+1}{e^2-1}} \frac{x (-1 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx \right)^2$$

Moment Function

$$m(x) = \int_1^{\frac{-e-e^{-1}}{-e+e^{-1}}} 4 \frac{x^r (-1 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx$$

Moment Generating Function

$$4 \int_1^{\frac{e^2+1}{e^2-1}} \frac{(-1 + \operatorname{arctanh}(x^{-1})) e^{tx+2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx_1$$

$$t \mapsto (\sinh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 4 \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1} |x|}$$

Cumulative Distribution Function

$$F(x) = \frac{x^2 e^2 (-1 + 2 \ln(\sqrt{x^2+1} + 1) - 2 \ln(x))}{x^2 + 2 + 2 \sqrt{x^2+1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf} \left(-Z^2 - e^{2 \operatorname{RootOf} \left(e^{\frac{-se^{-Z-2}+2-Ze^{-Z}-e^{-Z}-4-Z+2}}{e^{-Z-2}} - e^{2-Z} + 2e^{-Z} \right)} + 2e^{\operatorname{RootOf} \left(e^{\frac{-se^{-Z-2}+2-Ze^{-Z}-e^{-Z}-4-Z+2}}{e^{-Z-2}} \right)} \right)$$

Survivor Function

$$S(x) = -\frac{2x^2 e^2 \ln(\sqrt{x^2+1} + 1) - 2x^2 e^2 \ln(x) - x^2 e^2 - x^2 - 2\sqrt{x^2+1} - 2}{x^2 + 2 + 2\sqrt{x^2+1}}$$

Hazard Function

$$h(x) = 4 \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{2-2 \operatorname{arcsinh}(x^{-1})} (x^2 + 2 + 2\sqrt{x^2+1})}{\sqrt{x^2+1} |x| (-2x^2 e^2 \ln(\sqrt{x^2+1} + 1) + 2x^2 e^2 \ln(x) + x^2 e^2 + x^2 + 2\sqrt{x^2+1} + 2)}$$

Mean

$$mu = 4 \int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx$$

Variance

$$\sigma^2 = 4 \int_0^{2\frac{e}{e^2-1}} \frac{x(-1 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx - 16 \left(\int_0^{2\frac{e}{e^2-1}} \frac{(-1 + \operatorname{arcsinh}(x^{-1}))}{\sqrt{x^2+1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2(e-e^{-1})^{-1}} 4 \frac{x^r (-1 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1} |x|} dx$$

Moment Generating Function

$$4 \int_0^{2\frac{e}{e^2-1}} \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{tx+2-2\operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1} x} dx_1$$

$$t \mapsto (\operatorname{arcsinh}(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 4 \frac{(-1 + \sinh(x^{-1})) e^{2-2\sinh(x^{-1})} \cosh(x^{-1})}{x^2}$$

Cumulative Distribution Function

$$F(x) = -e^{\frac{1}{x}(-e^{2x^{-1}}x+2e^{x^{-1}}x-e^{x^{-1}}+x)}e^{-x^{-1}} \left(-e^{2x^{-1}} + e^{x^{-1}} + 1 \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \left(\operatorname{RootOf} \left(e^{-Z} \ln \left(-\frac{s}{-e^{2-Z} + e^{-Z} + 1} \right) + e^{2-Z} + -Z e^{-Z} - 2e^{-Z} - 1 \right) \right)^{-1}]$$

Survivor Function

$$S(x) = -e^{\frac{1}{x}(-e^{2x^{-1}}x+2e^{x^{-1}}x+e^{x^{-1}}+x)}e^{-x^{-1}} + e^{(-e^{2x^{-1}}+2e^{x^{-1}}+1)}e^{-x^{-1}} + e^{\frac{1}{x}(-e^{2x^{-1}}x+2e^{x^{-1}}x-e^{x^{-1}}+x)}e^{-x^{-1}}$$

Hazard Function

$$h(x) = -4 \frac{(-1 + \sinh(x^{-1})) e^{2-2\sinh(x^{-1})} \cosh(x^{-1})}{x^2} \left(e^{\frac{1}{x}(-e^{2x^{-1}}x+2e^{x^{-1}}x+e^{x^{-1}}+x)}e^{-x^{-1}} - e^{(-e^{2x^{-1}}+2e^{x^{-1}}+1)}e^{-x^{-1}} \right)$$

$$t \mapsto (\operatorname{csch}(t))^{-1} + 1$$

Probability Distribution Function

$$f(x) = 4 \frac{\operatorname{arccsch}((x-1)^{-1})}{\sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2}$$

Cumulative Distribution Function

$$F(x) = 4 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1})}{\sqrt{t^2 - 2t + 2} (t-1 + \sqrt{t^2 - 2t + 2})^2} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 4 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1})}{\sqrt{t^2 - 2t + 2} (t-1 + \sqrt{t^2 - 2t + 2})^2} dt$$

Hazard Function

$$h(x) = -4 \frac{\operatorname{arccsch}((x-1)^{-1})}{\sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2} \left(-1 + 4 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1})}{\sqrt{t^2 - 2t + 2} (t-1 + \sqrt{t^2 - 2t + 2})^2} dt \right)$$

Mean

$$mu = \int_1^\infty 4 \frac{x \operatorname{arccsch}((x-1)^{-1})}{\sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2} dx$$

Variance

$$sigma^2 = \infty - \left(\int_1^\infty 4 \frac{x \operatorname{arccsch}((x-1)^{-1})}{\sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2} dx \right)^2$$

Moment Function

$$m(x) = \int_1^\infty 4 \frac{x^r \operatorname{arccsch}((x-1)^{-1})}{\sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2} dx$$

Moment Generating Function

$$\int_1^\infty 4 \frac{e^{tx} \operatorname{arccsch}((x-1)^{-1})}{\sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2} dx_1$$

$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -4 \frac{1}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}}$$

Cumulative Distribution Function

$$F(x) = -4 \int_0^x \frac{1}{(\operatorname{arctanh}(t))^3 (t^2 - 1)} e^{-2(\operatorname{arctanh}(t))^{-1}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 + 4 \int_0^x \frac{1}{(\operatorname{arctanh}(t))^3 (t^2 - 1)} e^{-2(\operatorname{arctanh}(t))^{-1}} dt$$

Hazard Function

$$h(x) = -4 \frac{1}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}} \left(1 + 4 \int_0^x \frac{1}{(\operatorname{arctanh}(t))^3 (t^2 - 1)} e^{-2(\operatorname{arctanh}(t))^{-1}} dt \right)$$

Mean

$$mu = -4 \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}} dx$$

Variance

$$sigma^2 = -4 \int_0^1 \frac{x^2}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}} dx - 16 \left(\int_0^1 \frac{x}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 -4 \frac{x^r}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}} dx$$

Moment Generating Function

$$-4 \int_0^1 \frac{1}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{\frac{tx \operatorname{arctanh}(x) - 2}{\operatorname{arctanh}(x)}} dx_1$$

$$t \mapsto \operatorname{csch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 4 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3 |x|} e^{-2(\operatorname{arccsch}(x))^{-1}}$$

Cumulative Distribution Function

$$F(x) = 4 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^3 |t|} e^{-2(\operatorname{arccsch}(t))^{-1}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 4 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^3 |t|} e^{-2(\operatorname{arccsch}(t))^{-1}} dt$$

Hazard Function

$$h(x) = -4 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3 |x|} e^{-2(\operatorname{arccsch}(x))^{-1}} \left(-1 + 4 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^3 |t|} e^{-2(\operatorname{arccsch}(t))^{-1}} dt \right)$$

Mean

$$mu = \int_0^\infty 4 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3} e^{-2(\operatorname{arccsch}(x))^{-1}} dx$$

Variance

$$sigma^2 = \int_0^\infty 4 \frac{x}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3} e^{-2(\operatorname{arccsch}(x))^{-1}} dx - \left(\int_0^\infty 4 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3} e^{-2(\operatorname{arccsch}(x))^{-1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 4 \frac{x^r}{\sqrt{x^2+1} (\operatorname{arccsch}(x))^3 |x|} e^{-2(\operatorname{arccsch}(x))^{-1}} dx$$

Moment Generating Function

$$\int_0^\infty 4 \frac{1}{\sqrt{x^2+1} (\operatorname{arccsch}(x))^3 x} e^{\frac{tx \operatorname{arccsch}(x) - 2}{\operatorname{arccsch}(x)}} dx_1$$

$$t \mapsto \operatorname{arccsch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 4 e^{-2 \sinh(x)} \cosh(x) \sinh(x)$$

Cumulative Distribution Function

$$F(x) = \left(-e^{(2xe^x+1)e^{-x}} - e^{(xe^x+1)e^{-x}} + e^{e^x+x} + e^{e^{-x}} \right) e^{-e^x-x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf} \left(e^{(2-Ze^{-Z}+1)e^{-Z}} + se^{-Z+e^{-Z}} + e^{(-Ze^{-Z}+1)e^{-Z}} - e^{-Z+e^{-Z}} - e^{e^{-Z}} \right)]$$

Survivor Function

$$S(x) = -e^{-e^x-x+e^{-x}} + e^{-e^x-x+(2xe^x+1)e^{-x}} + e^{-e^x-x+(xe^x+1)e^{-x}}$$

Hazard Function

$$h(x) = 4 \frac{e^{-2 \sinh(x)} \cosh(x) \sinh(x)}{e^{-(e^2x-xe^x-1)e^{-x}} + e^{-(e^2x-1)e^{-x}} - e^{-(e^2x+xe^x-1)e^{-x}}}$$

Mean

$$mu = \int_0^\infty 2xe^{-2 \sinh(x)} \sinh(2x) dx$$

Variance

$$sigma^2 = \int_0^\infty 2x^2e^{-2 \sinh(x)} \sinh(2x) dx - \left(\int_0^\infty 2xe^{-2 \sinh(x)} \sinh(2x) dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 4x^r e^{-2 \sinh(x)} \cosh(x) \sinh(x) dx$$

Moment Generating Function

$$\int_0^\infty 2e^{tx-2 \sinh(x)} \sinh(2x) dx_1$$