

”ExponentialRV(2)”

$$[x \mapsto 2 e^{-2 x}]$$

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$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = \frac{e^{-2 \sqrt{x}}}{\sqrt{x}}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-2 \sqrt{x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/4 (\ln (1 - s))^2]$$

Survivor Function

$$S(x) = e^{-2 \sqrt{x}}$$

Hazard Function

$$h(x) = \frac{1}{\sqrt{x}}$$

Mean

$$mu = 1/2$$

Variance

$$sigma^2 = 5/4$$

Moment Function

$$m(x) = \frac{r \Gamma (r) \Gamma (r + 1/2)}{\sqrt{\pi}}$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} -\frac{\sqrt{\pi}}{\sqrt{-t}} e^{-t^{-1}} \left( \operatorname{erf} \left( \frac{t \sqrt{x} - 1}{\sqrt{-t}} \right) + \operatorname{erf} \left( \frac{1}{\sqrt{-t}} \right) \right)_1$$

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$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x) = 4 \mathrm{e}^{-2 x^2} x$$

Cumulative Distribution Function

$$F(x) = 1 - \mathrm{e}^{-2 x^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 \sqrt{2} \sqrt{-\ln (1-s)}]$$

Survivor Function

$$S(x) = \mathrm{e}^{-2 x^2}$$

Hazard Function

$$h(x) = 4 x$$

Mean

$$\mu = 1/4 \sqrt{2} \sqrt{\pi}$$

Variance

$$\sigma^2 = 1/2 - \pi/8$$

Moment Function

$$m(x) = 2^{-r/2} \Gamma (r/2 + 1)$$

Moment Generating Function

$$1 + 1/4 t \sqrt{\pi} \mathrm{e}^{1/8 t^2} \sqrt{2} \operatorname{erf} \left( 1/4 t \sqrt{2} \right) + 1/4 t \sqrt{\pi} \mathrm{e}^{1/8 t^2} \sqrt{2}_1$$

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$$t \mapsto t^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{1}{x^2} \mathrm{e}^{-2 x^{-1}}$$

Cumulative Distribution Function

$$F(x) = \mathrm{e}^{-2 x^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -2 (\ln(s))^{-1}]$$

Survivor Function

$$S(x) = 1 - e^{-2x^{-1}}$$

Hazard Function

$$h(x) = -2 \frac{1}{x^2} e^{-2x^{-1}} \left( -1 + e^{-2x^{-1}} \right)^{-1}$$

Mean

$$mu = \infty$$

Variance

$$sigma^2 = undefined$$

Moment Function

$$m(x) = 2^r \Gamma(1 - r)$$

Moment Generating Function

$$2 \sqrt{-t} \sqrt{2} K_1 \left( 2 \sqrt{-t} \sqrt{2} \right)_1$$

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$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = 2 e^{-2 \tan(x)} (1 + (\tan(x))^2)$$

Cumulative Distribution Function

$$F(x) = \begin{cases} 1 - e^{-2 \tan(x)} & x \leq \pi/2 \\ \infty & \pi/2 < x \end{cases}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = \begin{cases} e^{-2 \tan(x)} & x \leq \pi/2 \\ -\infty & \pi/2 < x \end{cases}$$

Hazard Function

$$h(x) = \begin{cases} 2 (\cos(x))^{-2} & x \leq \pi/2 \\ 0 & \pi/2 < x \end{cases}$$

Mean

$$\mu = 2 \int_0^{\pi/2} \frac{x}{(\cos(x))^2} e^{-2 \frac{\sin(x)}{\cos(x)}} dx$$

Variance

$$\sigma^2 = 2 \int_0^{\pi/2} \frac{x^2}{(\cos(x))^2} e^{-2 \frac{\sin(x)}{\cos(x)}} dx - 4 \left( \int_0^{\pi/2} \frac{x}{(\cos(x))^2} e^{-2 \frac{\sin(x)}{\cos(x)}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\pi/2} 2 x^r e^{-2 \tan(x)} (1 + (\tan(x))^2) dx$$

Moment Generating Function

$$2 \int_0^{\pi/2} \frac{1}{(\cos(x))^2} e^{-\frac{-tx \cos(x) + 2 \sin(x)}{\cos(x)}} dx_1$$


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$$t \mapsto e^t$$

Probability Distribution Function

$$f(x) = 2 x^{-3}$$

Cumulative Distribution Function

$$F(x) = \frac{x^2 - 1}{x^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \frac{1}{\sqrt{-s + 1}}]$$

Survivor Function

$$S(x) = x^{-2}$$

Hazard Function

$$h(x) = 2 x^{-1}$$

Mean

$$mu = 2$$

Variance

$$sigma^2 = \infty$$

Moment Function

$$m(x) = \lim_{x \rightarrow \infty} 2 \frac{x^{r-2} - 1}{r - 2}$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} - \frac{Ei(1, -tx) t^2 x^2 - Ei(1, -t) t^2 x^2 - e^t t x^2 - e^t x^2 + t e^{tx} x + e^{tx}}{x^2} 1$$


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$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = 2 e^{-2 e^x + x}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-2 e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln(2) + \ln(-\ln(1 - s))]$$

Survivor Function

$$S(x) = e^{-2 e^x}$$

Hazard Function

$$h(x) = 2 e^x$$

Mean

$$mu = \int_{-\infty}^{\infty} 2 x e^{-2 e^x + x} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 2x^2 e^{-2e^x+x} dx - \left( \int_{-\infty}^{\infty} 2x e^{-2e^x+x} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 2x^r e^{-2e^x+x} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 2e^{tx-2e^x+x} dx_1$$


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$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = 2x$$

Cumulative Distribution Function

$$F(x) = x^2$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \sqrt{s}]$$

Survivor Function

$$S(x) = -x^2 + 1$$

Hazard Function

$$h(x) = -2 \frac{x}{x^2 - 1}$$

Mean

$$\mu = 2/3$$

Variance

$$\sigma^2 = 1/18$$

Moment Function

$$m(x) = 2(r+2)^{-1}$$

Moment Generating Function

$$2 \frac{e^{t^2} - e^t + 1}{t^2} - 1$$

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$$t \mapsto -\ln(t)$$

Probability Distribution Function

$$f(x) = 2 e^{-2 e^{-x} - x}$$

Cumulative Distribution Function

$$F(x) = e^{-2 e^{-x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \ln(2) - \ln(-\ln(s))]$$

Survivor Function

$$S(x) = 1 - e^{-2 e^{-x}}$$

Hazard Function

$$h(x) = -2 \frac{e^{-2 e^{-x} - x}}{-1 + e^{-2 e^{-x}}}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 2 x e^{-2 e^{-x} - x} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 2 x^2 e^{-2 e^{-x} - x} dx - \left( \int_{-\infty}^{\infty} 2 x e^{-2 e^{-x} - x} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 2 x^r e^{-2 e^{-x} - x} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 2 e^{tx - 2 e^{-x} - x} dx$$

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$$t \mapsto \ln(t+1)$$

Probability Distribution Function

$$f(x) = 2e^{-2e^x+2+x}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{2-2e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln(2) + \ln(2 - \ln(1 - s))]$$

Survivor Function

$$S(x) = e^{2-2e^x}$$

Hazard Function

$$h(x) = 2e^x$$

Mean

$$mu = \int_0^\infty 2xe^{-2e^x+2+x} dx$$

Variance

$$sigma^2 = \int_0^\infty 2x^2e^{-2e^x+2+x} dx - \left( \int_0^\infty 2xe^{-2e^x+2+x} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2x^r e^{-2e^x+2+x} dx$$

Moment Generating Function

$$\int_0^\infty 2e^{tx-2e^x+2+x} dx_1$$


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$$t \mapsto (\ln(t+2))^{-1}$$



Probability Distribution Function

$$f(x) = 2 \frac{1}{x^2} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}}$$

Cumulative Distribution Function

$$F(x) = e^{-2e^{x^{-1}}+4}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto (-\ln(2) + \ln(4 - \ln(s)))^{-1}]$$

Survivor Function

$$S(x) = 1 - e^{-2e^{x^{-1}}+4}$$

Hazard Function

$$h(x) = -2 \frac{1}{x^2 (-1 + e^{-2e^{x^{-1}}+4})} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}}$$

Mean

$$\mu = 2 \int_0^{(\ln(2))^{-1}} \frac{1}{x} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx$$

Variance

$$\sigma^2 = 2 \int_0^{(\ln(2))^{-1}} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx - 4 \left( \int_0^{(\ln(2))^{-1}} \frac{1}{x} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} 2 \frac{x^r}{x^2} e^{-\frac{2e^{x^{-1}}x-4x-1}{x}} dx$$

Moment Generating Function

$$2 \int_0^{(\ln(2))^{-1}} \frac{1}{x^2} e^{-\frac{-tx^2+2e^{x^{-1}}x-4x-1}{x}} dx_1$$

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$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = 2 (x + 1)^{-2}$$

Cumulative Distribution Function

$$F(x) = 2 \frac{x}{x + 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\frac{s}{-2 + s}]$$

Survivor Function

$$S(x) = -\frac{x - 1}{x + 1}$$

Hazard Function

$$h(x) = -2 (x^2 - 1)^{-1}$$

Mean

$$mu = -1 + 2 \ln(2)$$

Variance

$$sigma^2 = -4 (\ln(2))^2 + 2$$

Moment Function

$$m(x) = \frac{r}{r - 1} - (r - 1)^{-1} + 2 r \operatorname{LerchPhi}(-1, 1, -r) + 2 \pi \csc(\pi r) r$$

Moment Generating Function

$$2 e^{-t} Ei(1, -t) t - 2 e^{-t} Ei(1, -2 t) t - e^t + 2_1$$

$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = 2 \frac{1}{(x + \sqrt{x^2 + 1})^2 \sqrt{x^2 + 1}}$$

Cumulative Distribution Function

$$F(x) = 2 x \sqrt{x^2 + 1} - 2 x^2$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 \frac{s}{\sqrt{-s+1}}]$$

Survivor Function

$$S(x) = 1 - 2x\sqrt{x^2+1} + 2x^2$$

Hazard Function

$$h(x) = -2 \frac{1}{(x + \sqrt{x^2+1})^2 \sqrt{x^2+1} (2x\sqrt{x^2+1} - 2x^2 - 1)}$$

Mean

$$mu = \frac{G_{3,3}^{2,3} \left( 1 \left| \begin{smallmatrix} -1, -1/2, 0 \\ -1/2, -1/2, -5/2 \end{smallmatrix} \right. \right)}{\pi}$$

Variance

$$sigma^2 = - \frac{-\infty \pi^2 + i \Im \left( \left( G_{3,3}^{2,3} \left( 1 \left| \begin{smallmatrix} -1, -1/2, 0 \\ -1/2, -1/2, -5/2 \end{smallmatrix} \right. \right) \right)^2 \right)}{\pi^2}$$

Moment Function

$$m(x) = \frac{1}{\pi} \left( - \frac{\Gamma(1/2 + r/2) \pi^{3/2} \csc(1/2 \pi r)}{\Gamma(1 + r/2)} + 2 \frac{\Gamma(3/2 + r/2) \pi^{3/2} \csc(1/2 \pi r)}{\Gamma(2 + r/2)} \right)$$

Moment Generating Function

$$\int_0^\infty 2 \frac{e^{tx}}{(x + \sqrt{x^2+1})^2 \sqrt{x^2+1}} dx_1$$

$$t \mapsto \operatorname{arcsinh}(t)$$

Probability Distribution Function

$$f(x) = 2 e^{-2 \sinh(x)} \cosh(x)$$

Cumulative Distribution Function

$$F(x) = 1 - e^{e^{-x} - e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln(2) + \ln\left(-\ln(1-s) + \sqrt{(\ln(1-s))^2 + 4}\right)]$$

Survivor Function

$$S(x) = e^{e^{-x} - e^x}$$

Hazard Function

$$h(x) = 2 \cosh(x) e^{-2 \sinh(x) - e^{-x} + e^x}$$

Mean

$$\mu = \int_0^\infty 2x e^{-2 \sinh(x)} \cosh(x) \, dx$$

Variance

$$\sigma^2 = \int_0^\infty 2x^2 e^{-2 \sinh(x)} \cosh(x) \, dx - \left( \int_0^\infty 2x e^{-2 \sinh(x)} \cosh(x) \, dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2x^r e^{-2 \sinh(x)} \cosh(x) \, dx$$

Moment Generating Function

$$\int_0^\infty 2 \cosh(x) e^{tx - 2 \sinh(x)} \, dx$$

$$t \mapsto \operatorname{csch}(t+1)$$

Probability Distribution Function

$$f(x) = 2 \frac{e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2+1} |x|}$$

Cumulative Distribution Function

$$F(x) = 2 \int_0^x \frac{e^{2-2 \operatorname{arccsch}(t)}}{\sqrt{t^2+1} |t|} \, dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 2 \int_0^x \frac{e^{2-2 \operatorname{arccsch}(t)}}{\sqrt{t^2+1} |t|} dt$$

Hazard Function

$$h(x) = -2 \frac{e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2+1} |x|} \left( -1 + 2 \int_0^x \frac{e^{2-2 \operatorname{arccsch}(t)}}{\sqrt{t^2+1} |t|} dt \right)^{-1}$$

Mean

$$mu = 2 \int_0^{2 \frac{e}{e^2-1}} \frac{e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2+1}} dx$$

Variance

$$sigma^2 = 2 \int_0^{2 \frac{e}{e^2-1}} \frac{x e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2+1}} dx - 4 \left( \int_0^{2 \frac{e}{e^2-1}} \frac{e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2+1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2(e-e^{-1})^{-1}} 2 \frac{x^r e^{2-2 \operatorname{arccsch}(x)}}{\sqrt{x^2+1} |x|} dx$$

Moment Generating Function

$$2 \int_0^{2 \frac{e}{e^2-1}} \frac{e^{tx+2-2 \operatorname{arccsch}(x)}}{x \sqrt{x^2+1}} dx_1$$

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$$t \mapsto \operatorname{arccsch}(t+1)$$

Probability Distribution Function

$$f(x) = 2 \frac{\cosh(x)}{(\sinh(x))^2} e^{2 \frac{\sinh(x)-1}{\sinh(x)}}$$

Cumulative Distribution Function

$$F(x) = e^{-2 \frac{e^{2x} + 2e^x + 1}{e^{2x} - 1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \ln \left( -\frac{2 + \sqrt{(\ln(s))^2 - 4 \ln(s) + 8}}{\ln(s) - 2} \right)]$$

Survivor Function

$$S(x) = 1 - e^{2 \frac{e^{2x} - 2e^x - 1}{e^{2x} - 1}}$$

Hazard Function

$$h(x) = -2 \frac{\cosh(x)}{(\sinh(x))^2} e^{2 \frac{\sinh(x) - 1}{\sinh(x)}} \left( -1 + e^{-2 \frac{e^{2x} + 2e^x + 1}{e^{2x} - 1}} \right)^{-1}$$

Mean

$$mu = 4 \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) x}{-1 + \cosh(2x)} e^{2 \frac{\sinh(x) - 1}{\sinh(x)}} dx$$

Variance

$$sigma^2 = 4 \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) x^2}{-1 + \cosh(2x)} e^{2 \frac{\sinh(x) - 1}{\sinh(x)}} dx - 16 \left( \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) x}{-1 + \cosh(2x)} e^{2 \frac{\sinh(x) - 1}{\sinh(x)}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\ln(1+\sqrt{2})} 2 \frac{x^r \cosh(x)}{(\sinh(x))^2} e^{2 \frac{\sinh(x) - 1}{\sinh(x)}} dx$$

Moment Generating Function

$$4 \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x)}{-1 + \cosh(2x)} e^{\frac{tx \sinh(x) + 2 \sinh(x) - 2}{\sinh(x)}} dx_1$$

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$$t \mapsto (\tanh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1}$$

Cumulative Distribution Function

$$F(x) = \frac{e^2 (x - 1)}{x + 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \frac{e^2 + s}{e^2 - s}]$$

Survivor Function

$$S(x) = -\frac{e^2 x - e^2 - x - 1}{x + 1}$$

Hazard Function

$$h(x) = -2 \frac{e^{2-2 \operatorname{arctanh}(x^{-1})}}{(e^2 x - e^2 - x - 1)(x - 1)}$$

Mean

$$mu = 2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx$$

Variance

$$sigma^2 = 2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^2 e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx - 4 \left( \int_1^{\frac{e^2+1}{e^2-1}} \frac{x e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx \right)^2$$

Moment Function

$$m(x) = \int_1^{\frac{e+e^{-1}}{e-e^{-1}}} 2 \frac{x^r e^{2-2 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} dx$$

Moment Generating Function

$$\left( -e^{\frac{2te^2+2e^2+1}{e^2-1}} + e^{\frac{2te^2+3}{e^2-1}} - 2e^{\frac{2e^2+1}{e^2-1}} Ei\left(1, -2\frac{te^2}{e^2-1}\right) t + 2e^{\frac{2e^2+1}{e^2-1}} Ei(1, -2t) t + e^{\frac{2te^2+2e^2-2t+1}{e^2-1}} \right) e^{-\frac{2te^2+2e^2-2t+1}{e^2-1}}$$

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$$t \mapsto (\sinh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1} |x|}$$

Cumulative Distribution Function

$$F(x) = 2 \int_0^x \frac{e^{2-2 \operatorname{arcsinh}(t^{-1})}}{\sqrt{t^2+1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 2 \int_0^x \frac{e^{2-2 \operatorname{arcsinh}(t^{-1})}}{\sqrt{t^2+1} |t|} dt$$

Hazard Function

$$h(x) = -2 \frac{e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1} |x|} \left( -1 + 2 \int_0^x \frac{e^{2-2 \operatorname{arcsinh}(t^{-1})}}{\sqrt{t^2+1} |t|} dt \right)^{-1}$$

Mean

$$mu = 2 \int_0^{2 \frac{e}{e^2-1}} \frac{e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx$$

Variance

$$sigma^2 = 2 \int_0^{2 \frac{e}{e^2-1}} \frac{x e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx - 4 \left( \int_0^{2 \frac{e}{e^2-1}} \frac{e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2(e-e^{-1})^{-1}} 2 \frac{x^r e^{2-2 \operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1} |x|} dx$$



Moment Generating Function

$$2 \int_0^2 \frac{e^{\frac{e}{e^2-1}} e^{tx+2-2 \operatorname{arcsinh}(x^{-1})}}{x \sqrt{x^2+1}} dx_1$$


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$$t \mapsto (\operatorname{arcsinh}(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{e^{2-2 \sinh(x^{-1})} \cosh(x^{-1})}{x^2}$$

Cumulative Distribution Function

$$F(x) = e^{-e^{x^{-1}}+2+e^{-x^{-1}}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto - \left( \ln(2) - \ln \left( -\ln(s) + 2 + \sqrt{(\ln(s))^2 - 4 \ln(s) + 8} \right) \right)^{-1}]$$

Survivor Function

$$S(x) = 1 - e^{-e^{x^{-1}}+2+e^{-x^{-1}}}$$

Hazard Function

$$h(x) = -2 \frac{e^{2-2 \sinh(x^{-1})} \cosh(x^{-1})}{x^2} \left( -1 + e^{-(e^{2x^{-1}}-2e^{x^{-1}}-1)e^{-x^{-1}}} \right)^{-1}$$


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$$t \mapsto (\operatorname{csch}(t))^{-1} + 1$$

Probability Distribution Function

$$f(x) = 2 \frac{1}{\sqrt{x^2-2x+2} (x-1+\sqrt{x^2-2x+2})^2}$$

Cumulative Distribution Function

$$F(x) = -2 + 2x\sqrt{x^2-2x+2} - 2\sqrt{x^2-2x+2} - 2x^2 + 4x$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -1/2 \frac{-2s + 2 + \sqrt{-(s-1)s^2}}{s-1}]$$

Survivor Function

$$S(x) = 3 - 2x\sqrt{x^2 - 2x + 2} + 2\sqrt{x^2 - 2x + 2} + 2x^2 - 4x$$

Hazard Function

$$h(x) = -2 \frac{1}{\sqrt{x^2 - 2x + 2} (x - 1 + \sqrt{x^2 - 2x + 2})^2 (2x\sqrt{x^2 - 2x + 2} - 2x^2 - 2\sqrt{x^2 - 2x + 2} + 1)}$$

Mean

$$mu = 5/3$$

Variance

$$sigma^2 = \infty$$

Moment Function

$$m(x) = \int_1^\infty 2 \frac{x^r}{\sqrt{x^2 - 2x + 2} (x - 1 + \sqrt{x^2 - 2x + 2})^2} dx$$

Moment Generating Function

$$\int_1^\infty 2 \frac{e^{tx}}{\sqrt{x^2 - 2x + 2} (x - 1 + \sqrt{x^2 - 2x + 2})^2} dx_1$$

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$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -2 \frac{1}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-2(\operatorname{arctanh}(x))^{-1}}$$

Cumulative Distribution Function

$$F(x) = e^{-4(\ln(x+1) - \ln(-x+1))^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto e^{\frac{1}{\ln(s)} \left( \ln(s) \ln(2) + \ln(s) \ln \left( \left( e^{-4 (\ln(s))^{-1} + 1} \right)^{-1} \right) - 4 \right)} - 1]$$

Survivor Function

$$S(x) = 1 - e^{-4 (\ln(x+1) - \ln(-x+1))^{-1}}$$

Hazard Function

$$h(x) = 2 \frac{1}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} \left( -1 + e^{-4 (\ln(x+1) - \ln(-x+1))^{-1}} \right)^{-1}$$

Mean

$$mu = -2 \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx$$

Variance

$$sigma^2 = -2 \int_0^1 \frac{x^2}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx - 4 \left( \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 -2 \frac{x^r}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx$$

Moment Generating Function

$$-2 \int_0^1 \frac{1}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{\frac{tx \operatorname{arctanh}(x) - 2}{\operatorname{arctanh}(x)}} dx_1$$


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$$t \mapsto \operatorname{csch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2 |x|} e^{-2 (\operatorname{arccsch}(x))^{-1}}$$

Cumulative Distribution Function

$$F(x) = 2 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^2 |t|} e^{-2 (\operatorname{arccsch}(t))^{-1}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 2 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^2 |t|} e^{-2(\operatorname{arccsch}(t))^{-1}} dt$$

Hazard Function

$$h(x) = -2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2 |x|} e^{-2(\operatorname{arccsch}(x))^{-1}} \left( -1 + 2 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^2 |t|} e^{-2(\operatorname{arccsch}(t))^{-1}} dt \right)$$

Mean

$$mu = \int_0^\infty 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2} e^{-2(\operatorname{arccsch}(x))^{-1}} dx$$

Variance

$$sigma^2 = \int_0^\infty 2 \frac{x}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2} e^{-2(\operatorname{arccsch}(x))^{-1}} dx - \left( \int_0^\infty 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2} e^{-2(\operatorname{arccsch}(x))^{-1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2 \frac{x^r}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2 |x|} e^{-2(\operatorname{arccsch}(x))^{-1}} dx$$

Moment Generating Function

$$\int_0^\infty 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^2 x} e^{\frac{tx \operatorname{arccsch}(x) - 2}{\operatorname{arccsch}(x)}} dx_1$$

$$t \mapsto \operatorname{arccsch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 2 e^{-2 \sinh(x)} \cosh(x)$$

Cumulative Distribution Function

$$F(x) = 1 - e^{e^{-x} - e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln(2) + \ln\left(-\ln(1-s) + \sqrt{(\ln(1-s))^2 + 4}\right)]$$

Survivor Function

$$S(x) = e^{e^{-x} - e^x}$$

Hazard Function

$$h(x) = 2 \cosh(x) e^{-2 \sinh(x) - e^{-x} + e^x}$$

Mean

$$\mu = \int_0^\infty 2x e^{-2 \sinh(x)} \cosh(x) \, dx$$

Variance

$$\sigma^2 = \int_0^\infty 2x^2 e^{-2 \sinh(x)} \cosh(x) \, dx - \left( \int_0^\infty 2x e^{-2 \sinh(x)} \cosh(x) \, dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2x^r e^{-2 \sinh(x)} \cosh(x) \, dx$$

Moment Generating Function

$$\int_0^\infty 2 \cosh(x) e^{tx - 2 \sinh(x)} \, dx_1$$