

```
> restart;
read("c:/appl/appl7.txt");
```

#### PROCEDURES:

*AllPermutations(n), AllCombinations(n, k), Benford(X), BootstrapRV(Data),*  
*CDF:CHF:HF:IDF:PDF:SF(X, [x]), CoefOfVar(X), Convolution(X, Y),*  
*ConvolutionIID(X, n), CriticalPoint(X, prob), Determinant(MATRIX), Difference(X, Y),*  
*Display(X), ExpectedValue(X, [g]), KSTest(X, Data, Parameters), Kurtosis(X),*  
*Maximum(X, Y), MaximumIID(X, n), Mean(X), MGF(X), Minimum(X, Y),*  
*MinimumIID(X, n), Mixture(MixParameters, MixRVs),*  
*MLE(X, Data, Parameters, [Rightcensor]), MLENHPP(X, Data, Parameters, obstime),*  
*MLEWeibull(Data, [Rightcensor]), MOM(X, Data, Parameters),*  
*NextCombination(Previous, size), NextPermutation(Previous), OrderStat(X, n, r, ["wo"]),*  
*PlotDist(X, [low], [high]), PlotEmpCDF(Data, [low], [high]),*  
*PlotEmpCIF(Data, [low], [high]), PlotEmpSF(Data, Censor),*  
*PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),*  
*PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),*  
*PlotEmpVsFittedSF(X, Data, Parameters, Censor, low, high),*  
*PPPlot(X, Data, Parameters), Product(X, Y), ProductIID(X, n),*  
*QQPlot(X, Data, Parameters), RangeStat(X, n, ["wo"]), Skewness(X), Transform(X, g),*  
*Truncate(X, low, high), Variance(X), VerifyPDF(X)*

#### Procedure Notation:

*X and Y are random variables*

*Greek letters are numeric or symbolic parameters*

*x is numeric or symbolic*

*n and r are positive integers,  $n \geq r$*

*low and high are numeric*

*g is a function*

*Brackets [] denote optional parameters*

*"double quotes" denote character strings*

*MATRIX is a 2 x 2 array of random variables*

*A capitalized parameter indicates that it must be  
entered as a list --> ex. Data := [1, 12.4, 34, 52.45, 63]*

#### Variate Generation:

*ArcTanVariate(alpha, phi), BinomialVariate(n, p, m), ExponentialVariate(lambda),*  
*NormalVariate(mu, sigma), UniformVariate(), WeibullVariate(lambda, kappa, m)*

#### DATA SETS:

*BallBearing, HorseKickFatalities, Hurricane, MP6, RatControl, RatTreatment, USSHalfBeak*

*ArcSinRV(), ArcTanRV(alpha, phi), BetaRV(alpha, beta), CauchyRV(a, alpha), ChiRV(n),*

*ChiSquareRV(n), ErlangRV(lambda, n), ErrorRV(mu, alpha, d), ExponentialRV(lambda),  
 ExponentialPowerRV(lambda, kappa), ExtremeValueRV(alpha, beta), FRV(n1, n2),  
 GammaRV(lambda, kappa), GeneralizedParetoRV(gamma, delta, kappa),  
 GompertzRV(delta, kappa), HyperbolicSecantRV(), HyperExponentialRV(p, l),  
 HypoExponentialRV(l), IDBRV(gamma, delta, kappa), InverseGaussianRV(lambda, mu),  
 InvertedGammaRV(alpha, beta), KSRV(n), LaPlaceRV(omega, theta),  
 LogGammaRV(alpha, beta), LogisticRV(kappa, lambda), LogLogisticRV(lambda, kappa),  
 LogNormalRV(mu, sigma), LomaxRV(kappa, lambda), MakehamRV(gamma, delta, kappa),  
 MuthRV(kappa), NormalRV(mu, sigma), ParetoRV(lambda, kappa), RayleighRV(lambda),  
 StandardCauchyRV(), StandardNormalRV(), StandardTriangularRV(m),  
 StandardUniformRV(), TRV(n), TriangularRV(a, m, b), UniformRV(a, b),  
 WeibullRV(lambda, kappa)*

Error, attempting to assign to `DataSets` which is protected.  
 Try declaring `local DataSets`; see ?protect for details.

```

> bf := WeibullRV(a,b);
    bfname := "WeibullRV(a,b)";
Originally a, renamed a~:
    is assumed to be: RealRange(Open(0),infinity)

Originally b, renamed b~:
    is assumed to be: RealRange(Open(0),infinity)

```

$$bf := \left[ \left[ x \rightarrow b^{\sim} a^{\sim b^{\sim}} x^{b^{\sim}-1} e^{-(a^{\sim} x)^{b^{\sim}}} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

$$bfname := "WeibullRV(a,b)"$$

(1)

```

> #plot(1/csch(t)+1, t = 0..0.0010);
#plot(diff(1/csch(t),t), t=0..0.0010);
#limit(1/csch(t), t=0);
> solve(exp(-t) = y, t);

```

$$-\ln(y)$$

(2)

```

> # discarded -ln(t + 1), t-> csch(t), t->arccsch(t), t -> tan(t),
> #name of the file for latex output
filename := "C:/Latex_Output_2/Weibull_Gen.tex";

glist := [t -> t^2, t -> sqrt(t), t -> 1/t, t -> arctan(t), t
-> exp(t), t -> ln(t), t -> exp(-t), t -> -ln(t), t -> ln(t+1),
t -> 1/(ln(t+2)), t -> tanh(t), t -> sinh(t), t -> arcsinh(t),
t-> csch(t+1), t->arccsch(t+1), t-> 1/tanh(t+1), t-> 1/sinh(t+1),
t-> 1/arcsinh(t+1), t-> 1/csch(t)+1, t-> tanh(1/t), t->csch
(1/t), t-> arccsch(1/t), t-> arctanh(1/t) ]:

base := t -> PDF(bf, t):

print(base(x)):

```

```

#begin latex file formatting
appendto(filename);
printf("\\documentclass[12pt]{article} \n");
printf("\\usepackage{amsfonts} \n");
printf("\\begin{document} \n");
print(bfname);
printf("$\$");
latex(bf[1]);
printf("$\$");
writeto(terminal);

#begin loopint through transformations
for i from 1 to 22 do
#for i from 1 to 3 do
    print( "i is", i, " -----"
-----
-----");

    g := glist[i]:
    l := bf[2][1];
    u := bf[2][2];
    Temp := Transform(bf, [[unapply(g(x), x)], [l,u]]);

#terminal output
print( "l and u", l, u );
print("g(x)", g(x), "base", base(x),bfname);
print("f(x)", PDF(Temp, x));

#latex output
appendto(filename);
printf("----- \\\");
printf("$\$");
latex(glist[i]);
printf("$\$");
printf("Probability Distribution Function \n$$ f(x)=");
latex(PDF(Temp,x));
printf(" \\qquad");
latex(Temp[2][1]);
printf(" < x < ");
latex(Temp[2][2]);
printf("$\$");

writeto(terminal);

od;

#final latex output
appendto(filename);
printf("\\end{document}\n");
writeto(terminal);

```

$filename := "C:/Latex\_Output\_2/Weibull\_Gen.tex"$

$$b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$$

"i is", 1,

"-----"  
-----"

$$g := t \rightarrow t^2$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow \frac{1}{2} b \sim a \sim y^{\frac{1}{2} b \sim - 1} e^{-a \sim y^{\frac{1}{2} b \sim}} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $x^2$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$f(x), \frac{1}{2} b \sim a \sim x^{\frac{1}{2} b \sim - 1} e^{-a \sim x^{\frac{1}{2} b \sim}}$$

"i is", 2,

"-----"  
-----"

$$g := t \rightarrow \sqrt{t}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow \frac{2 b \sim a \sim (y^2)^{b \sim} e^{-a \sim (y^2)^{b \sim}}}{y \sim} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\sqrt{x}$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$f(x), \frac{2 b \sim a \sim (x^2)^{b \sim} e^{-a \sim (x^2)^{b \sim}}}{x}$$

"i is", 3,

"-----"  
-----"

$$g := t \rightarrow \frac{1}{t}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow \frac{b \sim a \sim \left( \frac{1}{y \sim} \right)^{b \sim} e^{-a \sim \left( \frac{1}{y \sim} \right)^{b \sim}}}{y \sim} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\frac{1}{x}$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } \frac{b \sim a \sim \left(\frac{1}{x}\right)^{b \sim} e^{-a \sim \left(\frac{1}{x}\right)^{b \sim}}}{x}$$

"i is", 4,

"-----"  
-----"

$$g := t \rightarrow \arctan(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow b \sim a \sim \tan(y \sim)^{b \sim - 1} e^{-a \sim \tan(y \sim)^{b \sim}} (1 + \tan(y \sim)^2) \right], \left[ 0, \frac{1}{2} \pi \right], \right.$$

["Continuous", "PDF"]

"l and u", 0,  $\infty$

"g(x)",  $\arctan(x)$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } b \sim a \sim \tan(x)^{b \sim - 1} e^{-a \sim \tan(x)^{b \sim}} (1 + \tan(x)^2)$$

"i is", 5,

"-----"  
-----"

$$g := t \rightarrow e^t$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow \frac{b \sim a \sim \ln(y \sim)^{b \sim - 1} e^{-a \sim \ln(y \sim)^{b \sim}}}{y \sim} \right], [1, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $e^x$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } \frac{b \sim a \sim \ln(x)^{b \sim - 1} e^{-a \sim \ln(x)^{b \sim}}}{x}$$

"i is", 6,

"-----"  
-----"

$$g := t \rightarrow \ln(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow b \sim a \sim e^{-a \sim b \sim e^{b \sim y \sim} + b \sim y \sim} \right], [-\infty, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\ln(x)$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } b \sim a \sim^{b \sim} e^{-a \sim^{b \sim} e^{b \sim x} + b \sim x}$$

"i is", 7,

"-----"

$$g := t \rightarrow e^{-t}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow \frac{b \sim a \sim^{b \sim} (-\ln(y \sim))^{b \sim - 1} e^{-a \sim^{b \sim} (-\ln(y \sim))^{b \sim}}}{y \sim} \right], [0, 1], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", } e^{-x}, \text{"base", } b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}, \text{"WeibullRV(a,b)"}$$

$$\text{"f(x)", } \frac{b \sim a \sim^{b \sim} (-\ln(x))^{b \sim - 1} e^{-a \sim^{b \sim} (-\ln(x))^{b \sim}}}{x}$$

"i is", 8,

"-----"

$$g := t \rightarrow -\ln(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow b \sim a \sim^{b \sim} e^{-a \sim^{b \sim} e^{-b \sim y \sim} - b \sim y \sim} \right], [-\infty, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", } -\ln(x), \text{"base", } b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}, \text{"WeibullRV(a,b)"}$$

$$\text{"f(x)", } b \sim a \sim^{b \sim} e^{-a \sim^{b \sim} e^{-b \sim x} - b \sim x}$$

"i is", 9,

"-----"

$$g := t \rightarrow \ln(t + 1)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow b \sim a \sim^{b \sim} (e^{y \sim} - 1)^{b \sim - 1} e^{-a \sim^{b \sim} (e^{y \sim} - 1)^{b \sim} + y \sim} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", } \ln(x + 1), \text{"base", } b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}, \text{"WeibullRV(a,b)"}$$

$$\text{"f(x)", } b \sim a \sim^{b \sim} (e^x - 1)^{b \sim - 1} e^{-a \sim^{b \sim} (e^x - 1)^{b \sim} + x}$$

"i is", 10,

"-----"

$$g := t \rightarrow \frac{1}{\ln(t + 2)}$$

$$\begin{aligned}
& l := 0 \\
& u := \infty \\
Temp &:= \left[ \left[ y \rightarrow \frac{b \tilde{a}^{\tilde{b}} \left( e^{\frac{1}{y}} - 2 \right)^{b-1} - \frac{a^{\tilde{b}} \left( e^{\frac{1}{y}} - 2 \right)^{\tilde{b}}}{y-1}}{y^2} e^{\frac{a^{\tilde{b}} \left( e^{\frac{1}{y}} - 2 \right)^{\tilde{b}}}{y}} \right], \left[ 0, \frac{1}{\ln(2)} \right], \right. \\
& \left. ["Continuous", "PDF"] \right]
\end{aligned}$$

$$\begin{aligned}
& "l \text{ and } u", 0, \infty \\
& "g(x)", \frac{1}{\ln(x+2)}, "base", b \tilde{a}^{\tilde{b}} x^{b-1} e^{-(a \tilde{x})^{\tilde{b}}}, "WeibullRV(a,b)" \\
& "f(x)", \frac{b \tilde{a}^{\tilde{b}} \left( e^{\frac{1}{x}} - 2 \right)^{b-1} - \frac{a^{\tilde{b}} \left( e^{\frac{1}{x}} - 2 \right)^{\tilde{b}}}{x-1}}{x^2} e^{\frac{a^{\tilde{b}} \left( e^{\frac{1}{x}} - 2 \right)^{\tilde{b}}}{x}}
\end{aligned}$$

"i is", 11,

"-----"

$$\begin{aligned}
& g := t \rightarrow \tanh(t) \\
& l := 0 \\
& u := \infty \\
Temp &:= \left[ \left[ y \rightarrow -\frac{b \tilde{a}^{\tilde{b}} \operatorname{arctanh}(y)^{b-1} e^{-a^{\tilde{b}} \operatorname{arctanh}(y)^{\tilde{b}}}}{y^2 - 1} \right], [0, 1], ["Continuous", \right. \\
& \left. "PDF"] \right]
\end{aligned}$$

$$\begin{aligned}
& "l \text{ and } u", 0, \infty \\
& "g(x)", \tanh(x), "base", b \tilde{a}^{\tilde{b}} x^{b-1} e^{-(a \tilde{x})^{\tilde{b}}}, "WeibullRV(a,b)" \\
& "f(x)", -\frac{b \tilde{a}^{\tilde{b}} \operatorname{arctanh}(x)^{b-1} e^{-a^{\tilde{b}} \operatorname{arctanh}(x)^{\tilde{b}}}}{x^2 - 1}
\end{aligned}$$

"i is", 12,

"-----"

$$\begin{aligned}
& g := t \rightarrow \sinh(t) \\
& l := 0 \\
& u := \infty \\
Temp &:= \left[ \left[ y \rightarrow \frac{b \tilde{a}^{\tilde{b}} \operatorname{arsinh}(y)^{b-1} e^{-a^{\tilde{b}} \operatorname{arsinh}(y)^{\tilde{b}}}}{\sqrt{y^2 + 1}} \right], [0, \infty], ["Continuous", "PDF"] \right]
\end{aligned}$$

"l and u", 0,  $\infty$   
 "g(x)",  $\sinh(x)$ , "base",  $b \sim a \sim x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"  
 "f(x)",  $\frac{b \sim a \sim^{\sim} \operatorname{arcsinh}(x)^{b \sim - 1} e^{-a \sim^{\sim} \operatorname{arcsinh}(x)^{b \sim}}}{\sqrt{x^2 + 1}}$   
 "i is", 13,  
 "-----"  
 -----"

$g := t \rightarrow \operatorname{arcsinh}(t)$   
 $l := 0$   
 $u := \infty$   
 $Temp := \left[ \left[ y \sim \rightarrow b \sim a \sim^{\sim} \sinh(y \sim)^{b \sim - 1} e^{-a \sim^{\sim} \sinh(y \sim)^{b \sim}} \cosh(y \sim) \right], [0, \infty], ["Continuous", "PDF"] \right]$   
 "l and u", 0,  $\infty$   
 "g(x)",  $\operatorname{arcsinh}(x)$ , "base",  $b \sim a \sim^{\sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"  
 "f(x)",  $b \sim a \sim^{\sim} \sinh(x)^{b \sim - 1} e^{-a \sim^{\sim} \sinh(x)^{b \sim}} \cosh(x)$   
 "i is", 14,  
 "-----"  
 -----"

$g := t \rightarrow \operatorname{csch}(t + 1)$   
 $l := 0$   
 $u := \infty$   
 $Temp := \left[ \left[ y \sim \rightarrow \frac{b \sim a \sim^{\sim} (-1 + \operatorname{arccsch}(y \sim))^{b \sim - 1} e^{-a \sim^{\sim} (-1 + \operatorname{arccsch}(y \sim))^{b \sim}}}{\sqrt{y \sim^2 + 1} |y \sim|} \right], \left[ 0, \frac{2}{e - e^{-1}} \right], ["Continuous", "PDF"] \right]$   
 "l and u", 0,  $\infty$   
 "g(x)",  $\operatorname{csch}(x + 1)$ , "base",  $b \sim a \sim^{\sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"  
 "f(x)",  $\frac{b \sim a \sim^{\sim} (-1 + \operatorname{arccsch}(x))^{b \sim - 1} e^{-a \sim^{\sim} (-1 + \operatorname{arccsch}(x))^{b \sim}}}{\sqrt{x^2 + 1} |x|}$   
 "i is", 15,  
 "-----"  
 -----"

$g := t \rightarrow \operatorname{arccsch}(t + 1)$   
 $l := 0$   
 $u := \infty$



$$Temp := \left[ \left[ y \rightarrow - \frac{b \sim a \sim^{b \sim} \left( - \frac{\sinh(y \sim) - 1}{\sinh(y \sim)} \right)^{b \sim} e^{-a \sim^{b \sim} \left( - \frac{\sinh(y \sim) - 1}{\sinh(y \sim)} \right)^{b \sim}} \cosh(y \sim)}{(\sinh(y \sim) - 1) \sinh(y \sim)} \right], [0, \ln(1 + \sqrt{2})], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\operatorname{arccsch}(x + 1)$ , "base",  $b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } - \frac{b \sim a \sim^{b \sim} \left( - \frac{\sinh(x) - 1}{\sinh(x)} \right)^{b \sim} e^{-a \sim^{b \sim} \left( - \frac{\sinh(x) - 1}{\sinh(x)} \right)^{b \sim}} \cosh(x)}{(\sinh(x) - 1) \sinh(x)}$$

"i is", 16,

"-----"  
 -----"

$$g := t \rightarrow \frac{1}{\tanh(t + 1)}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \frac{b \sim a \sim^{b \sim} \left( -1 + \operatorname{arctanh}\left(\frac{1}{y \sim}\right) \right)^{b \sim - 1} e^{-a \sim^{b \sim} \left( -1 + \operatorname{arctanh}\left(\frac{1}{y \sim}\right) \right)^{b \sim}}}{y \sim^2 - 1} \right], \left[ 1, \frac{e + e^{-1}}{e - e^{-1}} \right], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\frac{1}{\tanh(x + 1)}$ , "base",  $b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } \frac{b \sim a \sim^{b \sim} \left( -1 + \operatorname{arctanh}\left(\frac{1}{x}\right) \right)^{b \sim - 1} e^{-a \sim^{b \sim} \left( -1 + \operatorname{arctanh}\left(\frac{1}{x}\right) \right)^{b \sim}}}{x^2 - 1}$$

"i is", 17,

"-----"  
 -----"

$$g := t \rightarrow \frac{1}{\sinh(t + 1)}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \frac{b \sim a \sim^{b \sim} \left( -1 + \operatorname{arcsinh} \left( \frac{1}{y \sim} \right) \right)^{b \sim - 1} e^{-a \sim^{b \sim} \left( -1 + \operatorname{arcsinh} \left( \frac{1}{y \sim} \right) \right)^{b \sim}}}{\sqrt{y \sim^2 + 1} \mid y \sim} \right], \left[ 0, \right. \right. \\ \left. \left. \frac{2}{e - e^{-1}} \right], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\frac{1}{\sinh(x + 1)}$ , "base",  $b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } \frac{b \sim a \sim^{b \sim} \left( -1 + \operatorname{arcsinh} \left( \frac{1}{x} \right) \right)^{b \sim - 1} e^{-a \sim^{b \sim} \left( -1 + \operatorname{arcsinh} \left( \frac{1}{x} \right) \right)^{b \sim}}}{\sqrt{x^2 + 1} \mid x|}$$

"i is", 18,

"-----"  
 -----"

$$g := t \rightarrow \frac{1}{\operatorname{arcsinh}(t + 1)}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \frac{b \sim a \sim^{b \sim} \left( -1 + \sinh \left( \frac{1}{y \sim} \right) \right)^{b \sim - 1} e^{-a \sim^{b \sim} \left( -1 + \sinh \left( \frac{1}{y \sim} \right) \right)^{b \sim}} \cosh \left( \frac{1}{y \sim} \right)}{y \sim^2} \right], \left[ 0, \right. \right. \\ \left. \left. \frac{1}{\ln(1 + \sqrt{2})} \right], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

"g(x)",  $\frac{1}{\operatorname{arcsinh}(x + 1)}$ , "base",  $b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}$ , "WeibullRV(a,b)"

$$\text{"f(x)", } \frac{b \sim a \sim^{b \sim} \left( -1 + \sinh \left( \frac{1}{x} \right) \right)^{b \sim - 1} e^{-a \sim^{b \sim} \left( -1 + \sinh \left( \frac{1}{x} \right) \right)^{b \sim}} \cosh \left( \frac{1}{x} \right)}{x^2}$$

"i is", 19,

"-----"  
 -----"

$$g := t \rightarrow \frac{1}{\operatorname{csch}(t)} + 1$$

$$l := 0$$

$$Temp := \left[ \left[ \begin{array}{c} u := \infty \\ y \rightarrow \frac{b \sim a \sim^{b \sim} \operatorname{arccsch}\left(\frac{1}{y \sim - 1}\right)^{b \sim - 1} e^{-a \sim^{b \sim} \operatorname{arccsch}\left(\frac{1}{y \sim - 1}\right)^{b \sim}}}{\sqrt{y \sim^2 - 2 y \sim + 2}} \end{array} \right], [1, \infty], \right. \\ \left. ["Continuous", "PDF"] \right]$$

$$\begin{array}{l} \text{"l and u", } 0, \infty \\ \text{"g(x)", } \frac{1}{\operatorname{csch}(x)} + 1, \text{"base", } b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}, \text{"WeibullRV(a,b)" } \\ \text{"f(x)", } \frac{b \sim a \sim^{b \sim} \operatorname{arccsch}\left(\frac{1}{x - 1}\right)^{b \sim - 1} e^{-a \sim^{b \sim} \operatorname{arccsch}\left(\frac{1}{x - 1}\right)^{b \sim}}}{\sqrt{x^2 - 2 x + 2}} \end{array}$$

"i is", 20,  
"-----"  
"-----"

$$\begin{array}{l} g := t \rightarrow \tanh\left(\frac{1}{t}\right) \\ l := 0 \\ u := \infty \\ Temp := \left[ \left[ \begin{array}{c} y \rightarrow - \frac{b \sim a \sim^{b \sim} \left(\frac{1}{\operatorname{arctanh}(y \sim)}\right)^{b \sim} e^{-a \sim^{b \sim} \left(\frac{1}{\operatorname{arctanh}(y \sim)}\right)^{b \sim}}}{\operatorname{arctanh}(y \sim) (y \sim^2 - 1)} \end{array} \right], [0, 1], ["Continuous", \\ "PDF"] \right] \end{array}$$

$$\begin{array}{l} \text{"l and u", } 0, \infty \\ \text{"g(x)", } \tanh\left(\frac{1}{x}\right), \text{"base", } b \sim a \sim^{b \sim} x^{b \sim - 1} e^{-(a \sim x)^{b \sim}}, \text{"WeibullRV(a,b)" } \\ \text{"f(x)", } - \frac{b \sim a \sim^{b \sim} \left(\frac{1}{\operatorname{arctanh}(x)}\right)^{b \sim} e^{-a \sim^{b \sim} \left(\frac{1}{\operatorname{arctanh}(x)}\right)^{b \sim}}}{\operatorname{arctanh}(x) (x^2 - 1)} \end{array}$$

"i is", 21,  
"-----"  
"-----"

$$g := t \rightarrow \operatorname{csch}\left(\frac{1}{t}\right)$$

$$\begin{aligned}
& l := 0 \\
& u := \infty \\
Temp := & \left[ \left[ y \rightarrow \frac{b \, a^{b-1} \operatorname{arcsch}(y)^{-b-1} e^{-a^{b-1} \operatorname{arcsch}(y)^{-b}}}{\sqrt{y^2 + 1} |y|} \right], [0, \infty], ["Continuous", \right. \\
& \left. "PDF"] \right] \\
& "l and u", 0, \infty \\
& "g(x)", \operatorname{csch}\left(\frac{1}{x}\right), "base", b \, a^{b-1} x^{b-1} e^{-(a x)^b}, "WeibullRV(a,b)" \\
& "f(x)", \frac{b \, a^{b-1} \operatorname{arcsch}(x)^{-b-1} e^{-a^{b-1} \operatorname{arcsch}(x)^{-b}}}{\sqrt{x^2 + 1} |x|} \\
& "i is", 22, \\
& "-----" \\
& "-----" \\
& g := t \rightarrow \operatorname{arcsch}\left(\frac{1}{t}\right) \\
& l := 0 \\
& u := \infty \\
Temp := & \left[ \left[ y \rightarrow b \, a^{b-1} \sinh(y)^{b-1} e^{-a^{b-1} \sinh(y)^b} \cosh(y) \right], [0, \infty], ["Continuous", \right. \\
& \left. "PDF"] \right] \\
& "l and u", 0, \infty \\
& "g(x)", \operatorname{arcsch}\left(\frac{1}{x}\right), "base", b \, a^{b-1} x^{b-1} e^{-(a x)^b}, "WeibullRV(a,b)" \\
& "f(x)", b \, a^{b-1} \sinh(x)^{b-1} e^{-a^{b-1} \sinh(x)^b} \cosh(x)
\end{aligned}$$

(3)