

"GeneralizedParetoRV(2,3,4)"

$$[x \mapsto \frac{e^{-2x}}{(1+x/3)^4} (2+4(x+3)^{-1})]$$

$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = 81 \frac{(\sqrt{x} + 5) e^{-2\sqrt{x}}}{(\sqrt{x} + 3)^5 \sqrt{x}}$$

Cumulative Distribution Function

$$F(x) = -\frac{-12x^{3/2} - x^2 + 81e^{-2\sqrt{x}} - 108\sqrt{x} - 54x - 81}{x^2 + 12x^{3/2} + 54x + 108\sqrt{x} + 81}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = 81 \frac{e^{-2\sqrt{x}}}{x^2 + 12x^{3/2} + 54x + 108\sqrt{x} + 81}$$

Hazard Function

$$h(x) = \frac{(\sqrt{x} + 5) (x^2 + 12x^{3/2} + 54x + 108\sqrt{x} + 81)}{(\sqrt{x} + 3)^5 \sqrt{x}}$$

Mean

$$\mu = -141 + 972e^6 Ei(1, 6)$$

Variance

$$\sigma^2 = -944784 (Ei(1, 6))^2 e^{12} + 309420 e^6 Ei(1, 6) - 25011$$

Moment Function

$$m(x) = 2^{-2-2r} \left(-19008 \Gamma(2r-3) r - 82080 \Gamma(2r-3) r^2 - 27648 \Gamma(2r-3) r^3 - 3456 \Gamma(2r-3) r^4 \right)$$

Moment Generating Function

$$\int_0^{\infty} 81 \frac{(\sqrt{x} + 5) e^{tx - 2\sqrt{x}}}{(\sqrt{x} + 3)^5 \sqrt{x}} dx_1$$

$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x) = 324 \frac{(x^2 + 5) e^{-2x^2} x}{(x^2 + 3)^5}$$

Cumulative Distribution Function

$$F(x) = -\frac{-x^8 - 12x^6 - 54x^4 - 108x^2 + 81e^{-2x^2} - 81}{(x^2 + 3)^4}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = 81 \frac{e^{-2x^2}}{(x^2 + 3)^4}$$

Hazard Function

$$h(x) = 4 \frac{(x^2 + 5) x}{x^2 + 3}$$

Mean

$$\mu = \frac{463\sqrt{3}\pi e^6 \operatorname{erf}(\sqrt{2}\sqrt{3})}{32} - \frac{463\sqrt{3}\pi e^6}{32} + \frac{111\sqrt{2}\sqrt{\pi}}{16}$$

Variance

$$\sigma^2 = -108e^6 Ei(1, 6) + 16 - \frac{643107\pi^2 e^{12} (\operatorname{erf}(\sqrt{2}\sqrt{3}))^2}{1024} + \frac{643107\pi^2 e^{12} \operatorname{erf}(\sqrt{2}\sqrt{3})}{512} - \frac{51393\sqrt{3}\pi e^6}{1024}$$

Moment Function

$$m(x) = 1/9 \sqrt{32}^{-7/2-r/2} \left(-28512 \sqrt{6} r \Gamma(-3+r/2) - 30780 \sqrt{6} r^2 \Gamma(-3+r/2) - 2592 \sqrt{6} r^3 \Gamma(-3+r/2) \right)$$

Moment Generating Function

$$\int_0^\infty 324 \frac{(x^2 + 5) x e^{x(t-2x)}}{(x^2 + 3)^5} dx_1$$

$$t \mapsto t^{-1}$$

Probability Distribution Function

$$f(x) = 162 \frac{x^2 (1 + 5x)}{(1 + 3x)^5} e^{-2x^{-1}}$$

Cumulative Distribution Function

$$F(x) = 81 \frac{x^4}{81x^4 + 108x^3 + 54x^2 + 12x + 1} e^{-2x^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \left(2 \operatorname{W} \left(3/2 \frac{e^{3/2}}{\sqrt[4]{s}} \right) - 3 \right)^{-1}]$$

Survivor Function

$$S(x) = -\frac{1}{81x^4 + 108x^3 + 54x^2 + 12x + 1} \left(81x^4 e^{-2x^{-1}} - 81x^4 - 108x^3 - 54x^2 - 12x - 1 \right)$$

Hazard Function

$$h(x) = -162 \frac{x^2 (1 + 5x)}{1 + 3x} e^{-2x^{-1}} \left(81x^4 e^{-2x^{-1}} - 81x^4 - 108x^3 - 54x^2 - 12x - 1 \right)^{-1}$$

Mean

$$mu = \infty$$

Variance

$$sigma^2 = undefined$$

Moment Function

$$m(x) = 9 \cdot 2^r \left(264 \Gamma(-r-3) r - 570 \Gamma(-r-3) r^2 + 96 \Gamma(-r-3) r^3 - 6 \Gamma(-r-3) r^4 + 9000 \Gamma \right.$$

Moment Generating Function

$$\int_0^\infty 162 \frac{x^2 (1 + 5x)}{(1 + 3x)^5} e^{\frac{tx^2-2}{x}} dx_1$$

$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = 162 \frac{(\tan(x) + 5) e^{-2 \tan(x)} (1 + (\tan(x))^2)}{(\tan(x) + 3)^5}$$

Cumulative Distribution Function

$$F(x) = \begin{cases} -\frac{1}{28 (\cos(x))^4 + 96 (\cos(x))^3 \sin(x) + 52 (\cos(x))^2 + 12 \sin(x) \cos(x) + 1} \left(81 (\cos(x))^4 e^{-2 \frac{\sin(x)}{\cos(x)}} - 1 - 28 (\cos(x))^3 \sin(x) \right) \\ \frac{\infty ((\cos(x))^4 + (\cos(x))^2 + 1)}{28 (\cos(x))^4 + 96 (\cos(x))^3 \sin(x) + 52 (\cos(x))^2 + 12 \sin(x) \cos(x) + 1} \end{cases}$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = \begin{cases} 81 \frac{(\cos(x))^4}{28 (\cos(x))^4 + 96 (\cos(x))^3 \sin(x) + 52 (\cos(x))^2 + 12 \sin(x) \cos(x) + 1} e^{-2 \frac{\sin(x)}{\cos(x)}} & x \leq \pi/2 \\ -\infty & \pi/2 < x \end{cases}$$

Hazard Function

$$h(x) = \begin{cases} 2 \frac{\sin(x) + 5 \cos(x)}{(\sin(x) + 3 \cos(x)) (\cos(x))^2} & x \leq \pi/2 \\ 0 & \pi/2 < x \end{cases}$$

Mean

$$mu = -162 \int_0^{\pi/2} \frac{(\sin(x) + 5 \cos(x)) (\cos(x))^2 x}{12 (\cos(x))^5 - 316 (\cos(x))^4 \sin(x) - 240 (\cos(x))^3 - 88 (\cos(x))^2 \sin(x) - 1} dx$$

Variance

$$sigma^2 = -162 \int_0^{\pi/2} \frac{(\sin(x) + 5 \cos(x)) (\cos(x))^2 x^2}{12 (\cos(x))^5 - 316 (\cos(x))^4 \sin(x) - 240 (\cos(x))^3 - 88 (\cos(x))^2 \sin(x) - 1} dx$$

Moment Function

$$m(x) = \int_0^{\pi/2} 162 \frac{x^r (\tan(x) + 5) e^{-2 \tan(x)} (1 + (\tan(x))^2)}{(\tan(x) + 3)^5} dx$$

Moment Generating Function

$$-162 \int_0^{\pi/2} \frac{(\sin(x) + 5 \cos(x)) (\cos(x))^2}{12 (\cos(x))^5 - 316 (\cos(x))^4 \sin(x) - 240 (\cos(x))^3 - 88 (\cos(x))^2 \sin(x) - 15 \cos(x)}$$

$$t \mapsto e^t$$

Probability Distribution Function

$$f(x) = 162 \frac{\ln(x) + 5}{(\ln(x) + 3)^5 x^3}$$

Cumulative Distribution Function

$$F(x) = \frac{x^2 (\ln(x))^4 + 12 x^2 (\ln(x))^3 + 54 x^2 (\ln(x))^2 + 108 x^2 \ln(x) + 81 x^2 - 81}{x^2 ((\ln(x))^4 + 12 (\ln(x))^3 + 54 (\ln(x))^2 + 108 \ln(x) + 81)}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = 81 \frac{1}{x^2 ((\ln(x))^4 + 12 (\ln(x))^3 + 54 (\ln(x))^2 + 108 \ln(x) + 81)}$$

Hazard Function

$$h(x) = 2 \frac{\ln(x) + 5}{x (\ln(x) + 3)}$$

Mean

$$mu = -\frac{27 e^3 Ei(1, 3)}{2} + 5$$

Variance

$$sigma^2 = -22 - \frac{729 e^6 (Ei(1, 3))^2}{4} + 135 e^3 Ei(1, 3)$$

Moment Function

$$m(x) = 162 \lim_{-u \rightarrow \infty} - \frac{e^{-3r} \left(-1458 r^3 e^{3r} + 5346 r^2 e^{3r} + 2187 i e^6 r^4 \pi \left(\text{signum}(-2+r) \right)^2 - 13122 i e \right)}{x^3}$$

Moment Generating Function

$$\int_1^\infty 162 \frac{e^{tx} (\ln(x) + 5)}{(\ln(x) + 3)^5 x^3} dx_1$$

$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = 162 \frac{(e^x + 5) e^{-2e^x + x}}{(e^x + 3)^5}$$

Cumulative Distribution Function

$$F(x) = \frac{e^{4x} + 12e^{3x} + 54e^{2x} + 108e^x + 81 - 81e^{-2e^x}}{e^{4x} + 12e^{3x} + 54e^{2x} + 108e^x + 81}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = 81 \frac{e^{-2e^x}}{e^{4x} + 12e^{3x} + 54e^{2x} + 108e^x + 81}$$

Hazard Function

$$h(x) = 2 \frac{(e^x + 5) e^x}{e^x + 3}$$

Mean

$$mu = \int_{-\infty}^\infty 162 \frac{x (e^x + 5) e^{-2e^x + x}}{(e^x + 3)^5} dx$$

Variance

$$sigma^2 = \int_{-\infty}^\infty 162 \frac{x^2 (e^x + 5) e^{-2e^x + x}}{(e^x + 3)^5} dx - \left(\int_{-\infty}^\infty 162 \frac{x (e^x + 5) e^{-2e^x + x}}{(e^x + 3)^5} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 162 \frac{x^r (e^x + 5) e^{-2e^x+x}}{(e^x + 3)^5} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 162 \frac{(e^x + 5) e^{tx-2e^x+x}}{(e^x + 3)^5} dx_1$$

$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = 162 \frac{(\ln(x) - 5) x}{(\ln(x) - 3)^5}$$

Cumulative Distribution Function

$$F(x) = \begin{cases} 81 \frac{x^2}{(\ln(x))^4 - 12(\ln(x))^3 + 54(\ln(x))^2 - 108 \ln(x) + 81} & x \leq e^3 \\ \text{undefined} & e^3 < x \end{cases}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [\exp \circ s \mapsto \text{RootOf}(s_Z^4 - 12 s_Z^3 + 54 s_Z^2 - 81 e^{2-Z} - 108 s_Z + 81 s)]$$

Survivor Function

$$S(x) = \begin{cases} \frac{(\ln(x))^4 - 12(\ln(x))^3 + 54(\ln(x))^2 - 81 x^2 - 108 \ln(x) + 81}{(\ln(x))^4 - 12(\ln(x))^3 + 54(\ln(x))^2 - 108 \ln(x) + 81} & x \leq e^3 \\ \text{undefined} & e^3 < x \end{cases}$$

Hazard Function

$$h(x) = \begin{cases} 162 \frac{(\ln(x)-5)x}{((\ln(x))^4 - 12(\ln(x))^3 + 54(\ln(x))^2 - 81 x^2 - 108 \ln(x) + 81)(\ln(x)-3)} & x \leq e^3 \\ \text{undefined} & e^3 < x \end{cases}$$

Mean

$$mu = -36 + \frac{729 e^9 Ei(1, 9)}{2}$$

Variance

$$\sigma^2 = 1728 e^{12} Ei(1, 12) - 1429 + 26244 e^9 Ei(1, 9) - \frac{531441 e^{18} (Ei(1, 9))^2}{4}$$

Moment Function

$$m(x) = -9/2 r^3 - \frac{33 r^2}{2} - 16 r + 162 e^{6+3r} Ei(1, 6+3r) r^2 + 108 e^{6+3r} Ei(1, 6+3r) r + \frac{27 e^{6+3r} Ei(1, 6+3r)^2}{2}$$

Moment Generating Function

$$162 \int_0^1 \frac{e^{tx} (\ln(x) - 5) x}{(\ln(x) - 3)^5} dx_1$$

$$t \mapsto -\ln(t)$$

Probability Distribution Function

$$f(x) = 162 \frac{e^{(3xe^x-2)e^{-x}} (1+5e^x)}{(1+3e^x)^5}$$

Cumulative Distribution Function

$$F(x) = 81 \frac{e^{2(2xe^x-1)e^{-x}}}{81e^{4x} + 108e^{3x} + 54e^{2x} + 12e^x + 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto RootOf \left(4 e^{-Z} \ln(3) - e^{-Z} \ln \left(s (3 e^{-Z} + 1)^4 \right) + 4 - Z e^{-Z} - 2 \right)]$$

Survivor Function

$$S(x) = \frac{81 e^{4x} + 108 e^{3x} + 54 e^{2x} + 12 e^x - 81 e^{2(2xe^x-1)e^{-x}} + 1}{81 e^{4x} + 108 e^{3x} + 54 e^{2x} + 12 e^x + 1}$$

Hazard Function

$$h(x) = 162 \frac{e^{(3xe^x-2)e^{-x}} (1+5e^x)}{(81 e^{4x} + 108 e^{3x} + 54 e^{2x} + 12 e^x - 81 e^{2(2xe^x-1)e^{-x}} + 1) (1+3e^x)}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 162 \frac{x (1 + 5 e^x) e^{(3 x e^x - 2) e^{-x}}}{(1 + 3 e^x)^5} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 162 \frac{x^2 (1 + 5 e^x) e^{(3 x e^x - 2) e^{-x}}}{(1 + 3 e^x)^5} dx - \left(\int_{-\infty}^{\infty} 162 \frac{x (1 + 5 e^x) e^{(3 x e^x - 2) e^{-x}}}{(1 + 3 e^x)^5} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 162 \frac{x^r (1 + 5 e^x) e^{(3 x e^x - 2) e^{-x}}}{(1 + 3 e^x)^5} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 162 \frac{(1 + 5 e^x) e^{(t x e^x + 3 x e^x - 2) e^{-x}}}{(1 + 3 e^x)^5} dx_1$$

$$t \mapsto \ln(t + 1)$$

Probability Distribution Function

$$f(x) = 162 \frac{(e^x + 4) e^{-2 e^x + 2 + x}}{(e^x + 2)^5}$$

Cumulative Distribution Function

$$F(x) = \frac{-81 e^{2 - 2 e^x} + e^{4 x} + 8 e^{3 x} + 24 e^{2 x} + 32 e^x + 16}{e^{4 x} + 8 e^{3 x} + 24 e^{2 x} + 32 e^x + 16}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = 81 \frac{e^{2 - 2 e^x}}{e^{4 x} + 8 e^{3 x} + 24 e^{2 x} + 32 e^x + 16}$$

Hazard Function

$$h(x) = 2 \frac{(e^x + 4) e^x}{e^x + 2}$$

Mean

$$mu = \int_0^{\infty} 162 \frac{x (e^x + 4) e^{-2e^x+2+x}}{(e^x + 2)^5} dx$$

Variance

$$sigma^2 = \int_0^{\infty} 162 \frac{x^2 (e^x + 4) e^{-2e^x+2+x}}{(e^x + 2)^5} dx - \left(\int_0^{\infty} 162 \frac{x (e^x + 4) e^{-2e^x+2+x}}{(e^x + 2)^5} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\infty} 162 \frac{x^r (e^x + 4) e^{-2e^x+2+x}}{(e^x + 2)^5} dx$$

Moment Generating Function

$$\int_0^{\infty} 162 \frac{(e^x + 4) e^{tx-2e^x+2+x}}{(e^x + 2)^5} dx_1$$

$$t \mapsto (\ln(t + 2))^{-1}$$

Probability Distribution Function

$$f(x) = 162 \frac{e^{x^{-1}} + 3}{(e^{x^{-1}} + 1)^5 x^2} e^{-\frac{2e^{x^{-1}} x - 4x - 1}{x}}$$

Cumulative Distribution Function

$$F(x) = 81 e^{4-2e^{x^{-1}}} \left(e^{4x^{-1}} + 4e^{3x^{-1}} + 6e^{2x^{-1}} + 4e^{x^{-1}} + 1 \right)^{-1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = -1 \left(-e^{4x^{-1}} - 4e^{3x^{-1}} - 6e^{2x^{-1}} - 4e^{x^{-1}} + 81e^{4-2e^{x^{-1}}} - 1 \right) \left(e^{4x^{-1}} + 4e^{3x^{-1}} + 6e^{2x^{-1}} + 4e^{x^{-1}} + 1 \right)^{-1}$$

Hazard Function

$$h(x) = -162 \frac{e^{x^{-1}} + 3}{x^2 (e^{x^{-1}} + 1)} e^{-\frac{2e^{x^{-1}} x - 4x - 1}{x}} \left(-e^{4x^{-1}} - 4e^{3x^{-1}} - 6e^{2x^{-1}} - 4e^{x^{-1}} + 81e^{4-2e^{x^{-1}}} - 1 \right)^{-1}$$

Mean

$$mu = 162 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} + 3}{x (e^{x^{-1}} + 1)^5} e^{-\frac{2e^{x^{-1}} x - 4x - 1}{x}} dx$$

Variance

$$sigma^2 = 162 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} + 3}{(e^{x^{-1}} + 1)^5} e^{-\frac{2e^{x^{-1}} x - 4x - 1}{x}} dx - 26244 \left(\int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} + 3}{x (e^{x^{-1}} + 1)^5} e^{-\frac{2e^{x^{-1}} x - 4x - 1}{x}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} 162 \frac{x^r (e^{x^{-1}} + 3)}{(e^{x^{-1}} + 1)^5 x^2} e^{-\frac{2e^{x^{-1}} x - 4x - 1}{x}} dx$$

Moment Generating Function

$$162 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} + 3}{(e^{x^{-1}} + 1)^5 x^2} e^{-\frac{-tx^2 + 2e^{x^{-1}} x - 4x - 1}{x}} dx_1$$

$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = 162 \frac{\operatorname{arctanh}(x) + 5}{(\operatorname{arctanh}(x) + 3)^5 (x + 1)^2}$$

Cumulative Distribution Function

$$F(x) = \frac{x (\operatorname{arctanh}(x))^4 + (\operatorname{arctanh}(x))^4 + 12x (\operatorname{arctanh}(x))^3 + 12 (\operatorname{arctanh}(x))^3 + 54x (\operatorname{arctanh}(x))^2 + 108x \operatorname{arctanh}(x) + 81x + 81}{x (\operatorname{arctanh}(x))^4 + 12x (\operatorname{arctanh}(x))^3 + 54x (\operatorname{arctanh}(x))^2 + 108x \operatorname{arctanh}(x) + 81x + 81}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = -81 \frac{x (\operatorname{arctanh}(x))^4 + 12x (\operatorname{arctanh}(x))^3 + 54x (\operatorname{arctanh}(x))^2 + 108x \operatorname{arctanh}(x) + 81x + 81}{x (\operatorname{arctanh}(x))^4 + 12x (\operatorname{arctanh}(x))^3 + 54x (\operatorname{arctanh}(x))^2 + 108x \operatorname{arctanh}(x) + 81x + 81}$$

Hazard Function

$$h(x) = -2 \frac{\operatorname{arctanh}(x) + 5}{(\operatorname{arctanh}(x) + 3)(x^2 - 1)}$$

Mean

$$mu = 162 \int_0^1 \frac{x (\operatorname{arctanh}(x) + 5)}{(\operatorname{arctanh}(x) + 3)^5 (x + 1)^2} dx$$

Variance

$$sigma^2 = 162 \int_0^1 \frac{x^2 (\operatorname{arctanh}(x) + 5)}{(\operatorname{arctanh}(x) + 3)^5 (x + 1)^2} dx - 26244 \left(\int_0^1 \frac{x (\operatorname{arctanh}(x) + 5)}{(\operatorname{arctanh}(x) + 3)^5 (x + 1)^2} dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 162 \frac{x^r (\operatorname{arctanh}(x) + 5)}{(\operatorname{arctanh}(x) + 3)^5 (x + 1)^2} dx$$

Moment Generating Function

$$162 \int_0^1 \frac{e^{tx} (\operatorname{arctanh}(x) + 5)}{(\operatorname{arctanh}(x) + 3)^5 (x + 1)^2} dx_1$$

$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = 162 \frac{\operatorname{arcsinh}(x) + 5}{(\operatorname{arcsinh}(x) + 3)^5 (x + \sqrt{x^2 + 1})^2 \sqrt{x^2 + 1}}$$

Cumulative Distribution Function

$$F(x) = \frac{(\ln(-x + \sqrt{x^2 + 1}))^4 - 12 (\ln(-x + \sqrt{x^2 + 1}))^3 + 54 (\ln(-x + \sqrt{x^2 + 1}))^2 + 162 \sqrt{x^2 + 1}}{(\ln(-x + \sqrt{x^2 + 1}))^4 - 12 (\ln(-x + \sqrt{x^2 + 1}))^3 + 54 (\ln(-x + \sqrt{x^2 + 1}))^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \frac{1}{72 \sqrt{-s + 1}} \left(16 \left(W \left(3/2 \frac{e^{3/2}}{\sqrt[4]{-s + 1}} \right) \right)^4 s - 16 \left(W \left(3/2 \frac{e^{3/2}}{\sqrt[4]{-s + 1}} \right) \right)^4 + 81 \right) \left(W \left(3/2 \frac{e^{3/2}}{\sqrt[4]{-s + 1}} \right) \right)^4$$

Survivor Function

$$S(x) = -81 \frac{2\sqrt{x^2+1}x - 2x^2 - 1}{(\ln(-x + \sqrt{x^2+1}))^4 - 12(\ln(-x + \sqrt{x^2+1}))^3 + 54(\ln(-x + \sqrt{x^2+1}))^2 - 108\ln(-x + \sqrt{x^2+1}) + 27}$$

Hazard Function

$$h(x) = -2 \frac{(\operatorname{arcsinh}(x) + 5) \left((\ln(-x + \sqrt{x^2+1}))^4 - 12(\ln(-x + \sqrt{x^2+1}))^3 + 54(\ln(-x + \sqrt{x^2+1}))^2 - 108\ln(-x + \sqrt{x^2+1}) + 27 \right)}{(\operatorname{arcsinh}(x) + 3)^5 (x + \sqrt{x^2+1})^2 \sqrt{x^2+1} (2\sqrt{x^2+1} - x)}$$

Mean

$$\mu = -\frac{27e^3 \operatorname{Ei}(1, 3)}{4} - \frac{729e^9 \operatorname{Ei}(1, 9)}{4} + \frac{41}{2}$$

Variance

$$\sigma^2 = -\frac{729e^6 (\operatorname{Ei}(1, 3))^2}{16} - \frac{19683 \operatorname{Ei}(1, 3) \operatorname{Ei}(1, 9) e^{12}}{8} + \frac{1107e^3 \operatorname{Ei}(1, 3)}{4} - \frac{531441 e^{18} (\operatorname{Ei}(1, 9))^2}{16}$$

Moment Function

$$m(x) = \int_0^\infty 162 \frac{x^r (\operatorname{arcsinh}(x) + 5)}{(\operatorname{arcsinh}(x) + 3)^5 (x + \sqrt{x^2+1})^2 \sqrt{x^2+1}} dx$$

Moment Generating Function

$$\int_0^\infty 162 \frac{e^{tx} (\operatorname{arcsinh}(x) + 5)}{(\operatorname{arcsinh}(x) + 3)^5 (x + \sqrt{x^2+1})^2 \sqrt{x^2+1}} dx$$

Probability Distribution Function

$$f(x) = 162 \frac{(\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x) + 125}$$

Cumulative Distribution Function

$$F(x) = \frac{e^{8x} + 24e^{7x} + 212e^{6x} + 792e^{5x} + 870e^{4x} - 1296e^{(4xe^x+1)e^{-x}-e^x} - 792e^{3x} + 212e^{2x} - 24e^x + 1}{e^{8x} + 24e^{7x} + 212e^{6x} + 792e^{5x} + 870e^{4x} - 792e^{3x} + 212e^{2x} - 24e^x + 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf} \left(-e^{-Z} \ln \left(- \left(e^{2-Z} + 6 e^{-Z} - 1 \right) (s - 1) \right) + 4 e^{-Z} \ln(3) + 4 e^{-Z} \ln(2) - e^{2-Z} \right)]$$

Survivor Function

$$S(x) = 1296 \frac{e^{-(e^{2x} - 4xe^x - 1)e^{-x}}}{e^{8x} + 24e^{7x} + 212e^{6x} + 792e^{5x} + 870e^{4x} - 792e^{3x} + 212e^{2x} - 24e^x + 1}$$

Hazard Function

$$h(x) = 1/8 \frac{(\sinh(x) + 5) e^{-(2 \sinh(x)e^x - e^{2x} + 4xe^x + 1)e^{-x}} \cosh(x) (e^{8x} + 24e^{7x} + 212e^{6x} + 792e^{5x} + 870e^{4x} - 792e^{3x} + 212e^{2x} - 24e^x + 1)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x)}$$

Mean

$$\mu = \int_0^\infty 162 \frac{x (\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x)} dx$$

Variance

$$\sigma^2 = \int_0^\infty 162 \frac{x^2 (\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x)} dx$$

Moment Function

$$m(x) = \int_0^\infty 162 \frac{x^r (\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x)} dx$$

Moment Generating Function

$$\int_0^\infty 162 \frac{(\sinh(x) + 5) \cosh(x) e^{tx - 2 \sinh(x)}}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x)} dx$$

$$t \mapsto \text{csch}(t + 1)$$

Probability Distribution Function

$$f(x) = 162 \frac{(4 + \text{arccsch}(x)) e^{2 - 2 \text{arccsch}(x)}}{(2 + \text{arccsch}(x))^5 \sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = 162 \int_0^x \frac{(4 + \operatorname{arccsch}(t)) e^{2-2 \operatorname{arccsch}(t)}}{(2 + \operatorname{arccsch}(t))^5 \sqrt{t^2 + 1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 162 \int_0^x \frac{(4 + \operatorname{arccsch}(t)) e^{2-2 \operatorname{arccsch}(t)}}{(2 + \operatorname{arccsch}(t))^5 \sqrt{t^2 + 1} |t|} dt$$

Hazard Function

$$h(x) = -162 \frac{(4 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{(2 + \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} |x|} \left(-1 + 162 \int_0^x \frac{(4 + \operatorname{arccsch}(t)) e^{2-2 \operatorname{arccsch}(t)}}{(2 + \operatorname{arccsch}(t))^5 \sqrt{t^2 + 1} |t|} dt \right)^{-1}$$

Mean

$$mu = 162 \int_0^{2^{\frac{e}{e^2-1}}} \frac{(4 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{(2 + \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1}} dx$$

Variance

$$sigma^2 = 162 \int_0^{2^{\frac{e}{e^2-1}}} \frac{x (4 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{(2 + \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1}} dx - 26244 \left(\int_0^{2^{\frac{e}{e^2-1}}} \frac{(4 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{(2 + \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2^{(e-e^{-1})^{-1}}} 162 \frac{x^r (4 + \operatorname{arccsch}(x)) e^{2-2 \operatorname{arccsch}(x)}}{(2 + \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} |x|} dx$$

Moment Generating Function

$$162 \int_0^{2^{\frac{e}{e^2-1}}} \frac{(4 + \operatorname{arccsch}(x)) e^{tx+2-2 \operatorname{arccsch}(x)}}{(2 + \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} x} dx$$

$$t \mapsto \operatorname{arccsch}(t+1)$$

Probability Distribution Function

$$f(x) = 162 \frac{(4 \sinh(x) + 1) \cosh(x) (\sinh(x))^2}{32 \sinh(x) (\cosh(x))^4 + 80 (\cosh(x))^4 + 16 \sinh(x) (\cosh(x))^2 - 120 (\cosh(x))^2 - 32}$$

Cumulative Distribution Function

$$F(x) = \frac{81 e^{8x} - 324 e^{6x} + 486 e^{4x} - 324 e^{2x} + 81}{16 e^{8x} + 64 e^{7x} - 128 e^{5x} + 128 e^{3x} + 32 e^{2x} + 32 e^{6x} - 80 e^{4x} - 64 e^x + 16} e^{2 \frac{e^{2x} - 2 e^x - 1}{e^{2x} - 1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = -1/16 \frac{1}{e^{8x} + 4 e^{7x} - 8 e^{5x} + 8 e^{3x} + 2 e^{2x} + 2 e^{6x} - 5 e^{4x} - 4 e^x + 1} \left(81 e^{2 \frac{e^{2x} - 2 e^x - 1}{e^{2x} - 1} + 8x} - \right)$$

Hazard Function

$$h(x) = 2592 \frac{(4 \sinh(x) + 1) \cosh(x) (\sinh(x))^2 (e^{8x} + 4 e^{7x} - 8 e^{5x} + 8 e^{3x} + 2 e^{2x} + 2 e^{6x} - 5 e^{4x} - 4 e^x + 1)}{32 \sinh(x) (\cosh(x))^4 + 80 (\cosh(x))^4 + 16 \sinh(x) (\cosh(x))^2 - 120 (\cosh(x))^2 - 32}$$

Mean

$$mu = 162 \int_0^{\ln(1+\sqrt{2})} \frac{x (4 \sinh(x) + 1) \cosh(x) (\sinh(x))^2}{32 \sinh(x) (\cosh(x))^4 + 80 (\cosh(x))^4 + 16 \sinh(x) (\cosh(x))^2 - 120 (\cosh(x))^2 - 32} dx$$

Variance

$$sigma^2 = 162 \int_0^{\ln(1+\sqrt{2})} \frac{x^2 (4 \sinh(x) + 1) \cosh(x) (\sinh(x))^2}{32 \sinh(x) (\cosh(x))^4 + 80 (\cosh(x))^4 + 16 \sinh(x) (\cosh(x))^2 - 120 (\cosh(x))^2 - 32} dx$$

Moment Function

$$m(x) = \int_0^{\ln(1+\sqrt{2})} 162 \frac{x^r (4 \sinh(x) + 1) \cosh(x) (\sinh(x))^2}{32 \sinh(x) (\cosh(x))^4 + 80 (\cosh(x))^4 + 16 \sinh(x) (\cosh(x))^2 - 120 (\cosh(x))^2 - 32} dx$$

Moment Generating Function

$$162 \int_0^{\ln(1+\sqrt{2})} \frac{(\sinh(x))^2 \cosh(x) (4 \sinh(x) + 1)}{32 \sinh(x) (\cosh(x))^4 + 80 (\cosh(x))^4 + 16 \sinh(x) (\cosh(x))^2 - 120 (\cosh(x))^2 - 32} dx$$

$$t \mapsto (\tanh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 162 \frac{(4 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{(2 + \operatorname{arctanh}(x^{-1}))^5 (x^2 - 1)}$$

Cumulative Distribution Function

$$F(x) = 1296 \frac{256 + 256x - 192 \ln(x+1) \ln(x-1)x - 48 (\ln(x+1))^2 \ln(x-1)x + 48 \ln(x+1) \ln(x-1)x^2}{(256 + 256x - 192 \ln(x+1) \ln(x-1)x - 48 (\ln(x+1))^2 \ln(x-1)x + 48 \ln(x+1) \ln(x-1)x^2)}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = -\frac{-256 - 256x + 192 \ln(x+1) \ln(x-1)x + 48 (\ln(x+1))^2 \ln(x-1)x - 48 \ln(x+1) \ln(x-1)x^2}{256 + 256x - 192 \ln(x+1) \ln(x-1)x - 48 (\ln(x+1))^2 \ln(x-1)x + 48 \ln(x+1) \ln(x-1)x^2}$$

Hazard Function

$$h(x) = 162 \frac{256 + 256x - 192 \ln(x+1) \ln(x-1)x - 48 (\ln(x+1))^2 \ln(x-1)x + 48 \ln(x+1) \ln(x-1)x^2}{(256 + 256x - 192 \ln(x+1) \ln(x-1)x - 48 (\ln(x+1))^2 \ln(x-1)x + 48 \ln(x+1) \ln(x-1)x^2)}$$

Mean

$$mu = 162 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x (4 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{(2 + \operatorname{arctanh}(x^{-1}))^5 (x^2 - 1)} dx$$

Variance

$$sigma^2 = 162 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^2 (4 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{(2 + \operatorname{arctanh}(x^{-1}))^5 (x^2 - 1)} dx - 26244 \left(\int_1^{\frac{e^2+1}{e^2-1}} \frac{x (4 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{(2 + \operatorname{arctanh}(x^{-1}))^5 (x^2 - 1)} dx \right)^2$$

Moment Function

$$m(x) = \int_1^{\frac{e+e^{-1}}{e-e^{-1}}} 162 \frac{x^r (4 + \operatorname{arctanh}(x^{-1})) e^{2-2 \operatorname{arctanh}(x^{-1})}}{(2 + \operatorname{arctanh}(x^{-1}))^5 (x^2 - 1)} dx$$

Moment Generating Function

$$162 \int_1^{\frac{e^2+1}{e^2-1}} \frac{(4 + \operatorname{arctanh}(x^{-1})) e^{tx+2-2\operatorname{arctanh}(x^{-1})}}{(2 + \operatorname{arctanh}(x^{-1}))^5 (x^2 - 1)} dx_1$$

$$t \mapsto (\sinh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 162 \frac{(4 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = 162 \int_0^x \frac{(4 + \operatorname{arcsinh}(t^{-1})) e^{2-2\operatorname{arcsinh}(t^{-1})}}{(2 + \operatorname{arcsinh}(t^{-1}))^5 \sqrt{t^2 + 1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 162 \int_0^x \frac{(4 + \operatorname{arcsinh}(t^{-1})) e^{2-2\operatorname{arcsinh}(t^{-1})}}{(2 + \operatorname{arcsinh}(t^{-1}))^5 \sqrt{t^2 + 1} |t|} dt$$

Hazard Function

$$h(x) = -162 \frac{(4 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2 + 1} |x|} \left(-1 + 162 \int_0^x \frac{(4 + \operatorname{arcsinh}(t^{-1})) e^{2-2\operatorname{arcsinh}(t^{-1})}}{(2 + \operatorname{arcsinh}(t^{-1}))^5 \sqrt{t^2 + 1} |t|} dt \right)$$

Mean

$$\mu = 162 \int_0^{\frac{e^2+1}{e^2-1}} \frac{(4 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2 + 1}} dx$$

Variance

$$\sigma^2 = 162 \int_0^{\frac{e^2+1}{e^2-1}} \frac{x (4 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2 + 1}} dx - 26244 \left(\int_0^{\frac{e^2+1}{e^2-1}} \frac{(4 + \operatorname{arcsinh}(x^{-1})) e^{2-2\operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2 + 1}} dx \right)^2$$

$$m(x) = \int_0^{2(e-e^{-1})^{-1}} 162 \frac{x^r (4 + \operatorname{arcsinh}(x^{-1})) e^{2-2 \operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2 + 1} |x|} dx$$
$$162 \int_0^{2 \frac{e}{e^2-1}} \frac{(4 + \operatorname{arcsinh}(x^{-1})) e^{tx+2-2 \operatorname{arcsinh}(x^{-1})}}{(2 + \operatorname{arcsinh}(x^{-1}))^5 \sqrt{x^2+1} x} dx_1$$

Variance

$$\sigma^2 = 162 \int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{(4 + \sinh(x^{-1})) e^{2-2 \sinh(x^{-1})} \cosh(x^{-1})}{\sinh(x^{-1}) (\cosh(x^{-1}))^4 + 10 (\cosh(x^{-1}))^4 + 38 \sinh(x^{-1}) (\cosh(x^{-1}))^2 + 10} dx$$

Moment Function

$$m(x) = \int_0^{(\ln(1+\sqrt{2}))^{-1}} 162 \frac{x^r (4 + \sinh(x^{-1})) e^{2-2 \sinh(x^{-1})} \cosh(x^{-1})}{x^2 (\sinh(x^{-1}) (\cosh(x^{-1}))^4 + 10 (\cosh(x^{-1}))^4 + 38 \sinh(x^{-1}) (\cosh(x^{-1}))^2 + 10)} dx$$

Moment Generating Function

$$162 \int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{(4 + \sinh(x^{-1})) \cosh(x^{-1}) e^{tx+2-2 \sinh(x^{-1})} \cosh(x^{-1})}{x^2 (\sinh(x^{-1}) (\cosh(x^{-1}))^4 + 10 (\cosh(x^{-1}))^4 + 38 \sinh(x^{-1}) (\cosh(x^{-1}))^2 + 10)} dx$$

$$t \mapsto (\operatorname{csch}(t))^{-1} + 1$$

Probability Distribution Function

$$f(x) = 162 \frac{\operatorname{arccsch}((x-1)^{-1}) + 5}{(\operatorname{arccsch}((x-1)^{-1}) + 3)^5 \sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2}$$

Cumulative Distribution Function

$$F(x) = 162 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1}) + 5}{(\operatorname{arccsch}((t-1)^{-1}) + 3)^5 \sqrt{t^2 - 2t + 2} (t-1 + \sqrt{t^2 - 2t + 2})^2} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 162 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1}) + 5}{(\operatorname{arccsch}((t-1)^{-1}) + 3)^5 \sqrt{t^2 - 2t + 2} (t-1 + \sqrt{t^2 - 2t + 2})^2} dt$$

Hazard Function

$$h(x) = -162 \frac{\operatorname{arccsch}((x-1)^{-1}) + 5}{(\operatorname{arccsch}((x-1)^{-1}) + 3)^5 \sqrt{x^2 - 2x + 2} (x-1 + \sqrt{x^2 - 2x + 2})^2} \left(-1 + 162 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1}) + 5}{(\operatorname{arccsch}((t-1)^{-1}) + 3)^5 \sqrt{t^2 - 2t + 2} (t-1 + \sqrt{t^2 - 2t + 2})^2} dt \right)$$

$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -162 \frac{(1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}}$$

Cumulative Distribution Function

$$F(x) = -162 \int_0^x \frac{(1 + 5 \operatorname{arctanh}(t)) (\operatorname{arctanh}(t))^2}{(1 + 3 \operatorname{arctanh}(t))^5 (t^2 - 1)} e^{-2 (\operatorname{arctanh}(t))^{-1}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 + 162 \int_0^x \frac{(1 + 5 \operatorname{arctanh}(t)) (\operatorname{arctanh}(t))^2}{(1 + 3 \operatorname{arctanh}(t))^5 (t^2 - 1)} e^{-2 (\operatorname{arctanh}(t))^{-1}} dt$$

Hazard Function

$$h(x) = -162 \frac{(1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} \left(1 + 162 \int_0^x \frac{(1 + 5 \operatorname{arctanh}(t)) (\operatorname{arctanh}(t))^2}{(1 + 3 \operatorname{arctanh}(t))^5 (t^2 - 1)} e^{-2 (\operatorname{arctanh}(t))^{-1}} dt \right)$$

Mean

$$\mu = -162 \int_0^1 \frac{x (1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx$$

Variance

$$\sigma^2 = -162 \int_0^1 \frac{x^2 (1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx - 26244 \left(\int_0^1 \frac{x (1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 -162 \frac{x^r (1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{-2 (\operatorname{arctanh}(x))^{-1}} dx$$

Moment Generating Function

$$-162 \int_0^1 \frac{(1 + 5 \operatorname{arctanh}(x)) (\operatorname{arctanh}(x))^2}{(1 + 3 \operatorname{arctanh}(x))^5 (x^2 - 1)} e^{\frac{tx \operatorname{arctanh}(x) - 2}{\operatorname{arctanh}(x)}} dx_1$$

$$t \mapsto \operatorname{csch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 162 \frac{(1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} |x|} e^{-2 (\operatorname{arccsch}(x))^{-1}}$$

Cumulative Distribution Function

$$F(x) = 162 \int_0^x \frac{(1 + 5 \operatorname{arccsch}(t)) (\operatorname{arccsch}(t))^2}{(1 + 3 \operatorname{arccsch}(t))^5 \sqrt{t^2 + 1} |t|} e^{-2 (\operatorname{arccsch}(t))^{-1}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 162 \int_0^x \frac{(1 + 5 \operatorname{arccsch}(t)) (\operatorname{arccsch}(t))^2}{(1 + 3 \operatorname{arccsch}(t))^5 \sqrt{t^2 + 1} |t|} e^{-2 (\operatorname{arccsch}(t))^{-1}} dt$$

Hazard Function

$$h(x) = -162 \frac{(1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} |x|} e^{-2 (\operatorname{arccsch}(x))^{-1}} \left(-1 + 162 \int_0^x \frac{(1 + 5 \operatorname{arccsch}(t)) (\operatorname{arccsch}(t))^2}{(1 + 3 \operatorname{arccsch}(t))^5 \sqrt{t^2 + 1} |t|} e^{-2 (\operatorname{arccsch}(t))^{-1}} dt \right)$$

Mean

$$\mu = \int_0^\infty 162 \frac{(1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1}} e^{-2 (\operatorname{arccsch}(x))^{-1}} dx$$

Variance

$$\sigma^2 = \int_0^\infty 162 \frac{x (1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1}} e^{-2 (\operatorname{arccsch}(x))^{-1}} dx - \left(\int_0^\infty 162 \frac{(1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1}} e^{-2 (\operatorname{arccsch}(x))^{-1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 162 \frac{x^r (1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} |x|} e^{-2 (\operatorname{arccsch}(x))^{-1}} dx$$

Moment Generating Function

$$\int_0^\infty 162 \frac{(1 + 5 \operatorname{arccsch}(x)) (\operatorname{arccsch}(x))^2}{(1 + 3 \operatorname{arccsch}(x))^5 \sqrt{x^2 + 1} x} e^{\frac{tx \operatorname{arccsch}(x) - 2}{\operatorname{arccsch}(x)}} dx_1$$

$$t \mapsto \operatorname{arccsch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 162 \frac{(\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316}$$

Cumulative Distribution Function

$$F(x) = \frac{e^{8x} + 24 e^{7x} + 212 e^{6x} + 792 e^{5x} + 870 e^{4x} - 1296 e^{(4xe^x+1)e^{-x}-e^x} - 792 e^{3x} + 212 e^{2x} - 2}{e^{8x} + 24 e^{7x} + 212 e^{6x} + 792 e^{5x} + 870 e^{4x} - 792 e^{3x} + 212 e^{2x} - 24 e^x + 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf} \left(-e^{2-Z} + 4 e^{-Z} \ln(2) + 4 e^{-Z} \ln(3) - e^{-Z} \ln \left(- (e^{2-Z} + 6 e^{-Z} - 1)^4 (s - 1) \right) \right)]$$

Survivor Function

$$S(x) = 1296 \frac{e^{-(e^{2x}-4xe^x-1)e^{-x}}}{e^{8x} + 24 e^{7x} + 212 e^{6x} + 792 e^{5x} + 870 e^{4x} - 792 e^{3x} + 212 e^{2x} - 24 e^x + 1}$$

Hazard Function

$$h(x) = 1/8 \frac{(\sinh(x) + 5) e^{(e^{2x}-2 \sinh(x)e^x-4xe^x-1)e^{-x}} \cosh(x) (e^{8x} + 24 e^{7x} + 212 e^{6x} + 792 e^{5x} + 870 e^{4x} - 792 e^{3x} + 212 e^{2x} - 24 e^x + 1)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316}$$

Mean

$$\mu = \int_0^\infty 162 \frac{x (\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316} dx$$

Variance

$$\sigma^2 = \int_0^\infty 162 \frac{x^2 (\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2} dx$$

Moment Function

$$m(x) = \int_0^\infty 162 \frac{x^r (\sinh(x) + 5) e^{-2 \sinh(x)} \cosh(x)}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2} dx$$

Moment Generating Function

$$M(t) = \int_0^\infty 162 \frac{(\sinh(x) + 5) \cosh(x) e^{tx - 2 \sinh(x)}}{\sinh(x) (\cosh(x))^4 + 15 (\cosh(x))^4 + 88 \sinh(x) (\cosh(x))^2 + 240 (\cosh(x))^2 + 316 \sinh(x)} dx$$