

”WeibullRV(1,2)”

$$[x \mapsto 2\, x e^{-x^2}]$$

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$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = e^{-x}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln (1 - s)]$$

Survivor Function

$$S(x) = e^{-x}$$

Hazard Function

$$h(x) = 1$$

Mean

$$\mu = 1$$

Variance

$$\sigma^2 = 1$$

Moment Function

$$m(x) = \Gamma \left( r + 1 \right)$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} \frac{e^{x(t-1)} - 1}{t - 1} \quad 1$$

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$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x) = 4\,x^3\mathrm{e}^{-x^4}$$

Cumulative Distribution Function

$$F(x) = 1 - \mathrm{e}^{-x^4}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \sqrt[4]{-\ln(1-s)}]$$

Survivor Function

$$S(x) = \mathrm{e}^{-x^4}$$

Hazard Function

$$h(x) = 4\,x^3$$

Mean

$$\mu = 1/4\,\frac{\pi\sqrt{2}}{\Gamma(3/4)}$$

Variance

$$\sigma^2 = 1/2\sqrt{\pi} - 1/8\,\frac{\pi^2}{(\Gamma(3/4))^2}$$

Moment Function

$$m(x) = \Gamma(r/4 + 1)$$

Moment Generating Function

$$1/8\,\frac{1}{\Gamma(3/4)\sqrt{\pi}}\left((\Gamma(3/4))^2{}_0\mathrm{F}_2\left(\,;\,5/4,3/2;\,\frac{t^4}{256}\right)t^3\sqrt{\pi} + 2\pi^{3/2}\sqrt{2}{}_0\mathrm{F}_2\left(\,;\,1/2,3/4;\,\frac{t^4}{256}\right)t + 2\pi\,\Gamma\left(\frac{3}{4}\right)\right)$$

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$$t \mapsto t^{-1}$$

Probability Distribution Function

$$f(x) = 2\,\frac{1}{x^3}\mathrm{e}^{-x^{-2}}$$

Cumulative Distribution Function

$$F(x) = \mathrm{e}^{-x^{-2}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{ERROR}(IDF) : \text{Could not find the appropriate inverse}$$

$$[s \mapsto \frac{1}{\sqrt{-\ln(s)}}]$$

Survivor Function

$$S(x) = 1 - e^{-x^{-2}}$$

Hazard Function

$$h(x) = -2 \frac{1}{x^3} e^{-x^{-2}} \left( -1 + e^{-x^{-2}} \right)^{-1}$$

Mean

$$\mu = \sqrt{\pi}$$

Variance

$$\sigma^2 = \infty$$

Moment Function

$$m(x) = \Gamma(-r/2 + 1)$$

Moment Generating Function

$$\frac{G_{0,3}^{3,0} \left( 1/4 t^2 \middle|_{1,1/2,0} \right)}{\sqrt{\pi}} \quad 1$$


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$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = 2 \frac{\sin(x)}{(\cos(x))^3} e^{-\frac{(\sin(x))^2}{(\cos(x))^2}}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-\frac{(\sin(x))^2}{(\cos(x))^2}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \arctan \left( \sqrt{-\ln(1-s)} \right)]$$

Survivor Function

$$S(x) = e^{-\frac{(\sin(x))^2}{(\cos(x))^2}}$$

Hazard Function

$$h(x) = 2 \frac{\sin(x)}{(\cos(x))^3}$$

Mean

$$mu = 2 \int_0^{\pi/2} \frac{x \sin(x)}{(\cos(x))^3} e^{\frac{-1+\cos(2x)}{\cos(2x)+1}} dx$$

Variance

$$sigma^2 = 2 \int_0^{\pi/2} \frac{x^2 \sin(x)}{(\cos(x))^3} e^{\frac{-1+\cos(2x)}{\cos(2x)+1}} dx - 4 \left( \int_0^{\pi/2} \frac{x \sin(x)}{(\cos(x))^3} e^{\frac{-1+\cos(2x)}{\cos(2x)+1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\pi/2} 2 \frac{x^r \sin(x)}{(\cos(x))^3} e^{-\frac{(\sin(x))^2}{(\cos(x))^2}} dx$$

Moment Generating Function

$$2 \int_0^{\pi/2} \frac{\sin(x)}{(\cos(x))^3} e^{\frac{tx \cos(2x) + tx + \cos(2x) - 1}{\cos(2x) + 1}} dx_1$$

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Probability Distribution Function

$$f(x) = 2 \frac{\ln(x) e^{-(\ln(x))^2}}{x}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-(\ln(x))^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto e^{\sqrt{\ln(-(-1+s)^{-1})}}]$$

Survivor Function

$$S(x) = e^{-(\ln(x))^2}$$

Hazard Function

$$h(x) = 2 \frac{\ln(x)}{x}$$

Mean

$$mu = 1 + 1/2 \sqrt{\pi} e^{1/4} \operatorname{erf}(1/2) + 1/2 \sqrt{\pi} e^{1/4}$$

Variance

$$sigma^2 = \sqrt{\pi} e \operatorname{erf}(1) + \sqrt{\pi} e - \sqrt{\pi} e^{1/4} \operatorname{erf}(1/2) - \sqrt{\pi} e^{1/4} - 1/4 \pi e^{1/2} (\operatorname{erf}(1/2))^2 - 1/2 \pi e^{1/2} \operatorname{erf}(1/2)$$

Moment Function

$$m(x) = 1 + 1/2 r \sqrt{\pi} e^{1/4 r^2} \operatorname{erf}(r/2) + 1/2 r \sqrt{\pi} e^{1/4 r^2}$$

Moment Generating Function

$$\int_1^\infty 2 \frac{\ln(x) e^{tx - (\ln(x))^2}}{x} dx_1$$

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$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = 2 e^{2x - e^2 x}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-e^2 x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 \ln(-\ln(1-s))]$$

Survivor Function

$$S(x) = e^{-e^2 x}$$

Hazard Function

$$h(x) = 2e^{2x}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 2xe^{2x-e^{2x}} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 2x^2e^{2x-e^{2x}} dx - \left( \int_{-\infty}^{\infty} 2xe^{2x-e^{2x}} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 2x^r e^{2x-e^{2x}} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 2e^{tx+2x-e^{2x}} dx$$

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$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = -2 \frac{\ln(x) e^{-(\ln(x))^2}}{x}$$

Cumulative Distribution Function

$$F(x) = e^{-(\ln(x))^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{ERROR(IDF)} : \text{Could not find the appropriate inverse}$$

$$[s \mapsto e^{-\sqrt{-\ln(s)}}]$$

Survivor Function

$$S(x) = 1 - e^{-(\ln(x))^2}$$

Hazard Function

$$h(x) = 2 \frac{\ln(x) e^{-(\ln(x))^2}}{x (-1 + e^{-(\ln(x))^2})}$$

Mean

$$\mu = 1 + 1/2 \sqrt{\pi} e^{1/4} \operatorname{erf}(1/2) - 1/2 \sqrt{\pi} e^{1/4}$$

Variance

$$\sigma^2 = \sqrt{\pi} \operatorname{erf}(1) - \sqrt{\pi} e - \sqrt{\pi} e^{1/4} \operatorname{erf}(1/2) + \sqrt{\pi} e^{1/4} - 1/4 \pi e^{1/2} (\operatorname{erf}(1/2))^2 + 1/2 \pi e^{1/2} \operatorname{erf}(1/2)$$

Moment Function

$$m(x) = 1 + 1/2 r \sqrt{\pi} e^{1/4 r^2} \operatorname{erf}(r/2) - 1/2 r \sqrt{\pi} e^{1/4 r^2}$$

Moment Generating Function

$$-2 \int_0^1 \frac{\ln(x) e^{tx - (\ln(x))^2}}{x} dx$$

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$$t \mapsto -\ln(t)$$

Probability Distribution Function

$$f(x) = 2 e^{-2x - e^{-2x}}$$

Cumulative Distribution Function

$$F(x) = e^{-e^{-2x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -1/2 \ln(-\ln(s))]$$

Survivor Function

$$S(x) = 1 - e^{-e^{-2x}}$$

Hazard Function

$$h(x) = -2 \frac{e^{-2x - e^{-2x}}}{-1 + e^{-e^{-2x}}}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 2x e^{-2x - e^{-2x}} dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 2x^2 e^{-2x - e^{-2x}} dx - \left( \int_{-\infty}^{\infty} 2x e^{-2x - e^{-2x}} dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 2x^r e^{-2x - e^{-2x}} dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 2e^{tx - 2x - e^{-2x}} dx$$

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$$t \mapsto \ln(t + 1)$$

Probability Distribution Function

$$f(x) = 2(e^x - 1)e^{-e^{2x} + 2e^x + x - 1}$$

Cumulative Distribution Function

$$F(x) = (-e^{2e^x - 1} + e^{e^{2x}})e^{-e^{2x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln(2) + \ln(1 + \text{RootOf}(e^{-Z} + se^{1/4(-Z+1)^2} - e^{1/4(-Z+1)^2}))]$$

Survivor Function

$$S(x) = e^{-e^{2x} + 2e^x - 1}$$

Hazard Function

$$h(x) = 2(e^x - 1)e^x$$

Mean

$$\mu = \int_0^{\infty} 2x(e^x - 1)e^{-e^{2x} + 2e^x + x - 1} dx$$



Variance

$$\sigma^2 = \int_0^\infty 2x^2 (e^x - 1) e^{-e^2 x + 2e^x + x - 1} dx - \left( \int_0^\infty 2x (e^x - 1) e^{-e^2 x + 2e^x + x - 1} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2x^r (e^x - 1) e^{-e^2 x + 2e^x + x - 1} dx$$

Moment Generating Function

$$\int_0^\infty 2(e^x - 1) e^{tx - e^2 x + 2e^x + x - 1} dx_1$$


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$$t \mapsto (\ln(t + 2))^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{e^{x^{-1}} - 2}{x^2} e^{-\frac{1}{x} (e^{2x^{-1}} x - 4e^{x^{-1}} x + 4x - 1)}$$

Cumulative Distribution Function

$$F(x) = e^{-e^{2x^{-1}} + 4e^{x^{-1}} - 4}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \left( \ln \left( 2 + \sqrt{-\ln(s)} \right) \right)^{-1}]$$

Survivor Function

$$S(x) = 1 - e^{-e^{2x^{-1}} + 4e^{x^{-1}} - 4}$$

Hazard Function

$$h(x) = -2 \frac{e^{x^{-1}} - 2}{x^2} e^{-\frac{1}{x} (e^{2x^{-1}} x - 4e^{x^{-1}} x + 4x - 1)} \left( -1 + e^{-e^{2x^{-1}} + 4e^{x^{-1}} - 4} \right)^{-1}$$

Mean

$$\mu = 2 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} - 2}{x} e^{-\frac{1}{x} (e^{2x^{-1}} x - 4e^{x^{-1}} x + 4x - 1)} dx$$

Variance

$$sigma^2 = 2 \int_0^{(\ln(2))^{-1}} \left( e^{x^{-1}} - 2 \right) e^{-\frac{1}{x} \left( e^{2x^{-1}x-4} e^{x^{-1}x+4} x-1 \right)} dx - 4 \left( \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} - 2}{x} e^{-\frac{1}{x} \left( e^{2x^{-1}x-4} e^{x^{-1}x+4} x-1 \right)} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} 2 \frac{x^r \left( e^{x^{-1}} - 2 \right)}{x^2} e^{-\frac{1}{x} \left( e^{2x^{-1}x-4} e^{x^{-1}x+4} x-1 \right)} dx$$

Moment Generating Function

$$2 \int_0^{(\ln(2))^{-1}} \frac{e^{x^{-1}} - 2}{x^2} e^{-\frac{1}{x} \left( e^{2x^{-1}x-tx^2-4} e^{x^{-1}x+4} x-1 \right)} dx_1$$


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$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = -2 \frac{\operatorname{arctanh}(x) e^{-(\operatorname{arctanh}(x))^2}}{x^2 - 1}$$

Cumulative Distribution Function

$$F(x) = \frac{\sqrt[4]{e^{(\ln(1-x))^2}} - \sqrt{(1-x)^{\ln(x+1)}} e^{-1/4 (\ln(x+1))^2}}{\sqrt[4]{e^{(\ln(1-x))^2}}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = \frac{\sqrt{(x+1)^{\ln(1-x)}} e^{-1/4 (\ln(x+1))^2}}{\sqrt[4]{e^{(\ln(1-x))^2}}}$$

Hazard Function

$$h(x) = -2 \frac{\operatorname{arctanh}(x) e^{1/4 (\ln(x+1)-2 \operatorname{arctanh}(x))(\ln(x+1)+2 \operatorname{arctanh}(x))} \sqrt[4]{e^{(\ln(1-x))^2}}}{\sqrt{(1-x)^{\ln(x+1)}} (x^2 - 1)}$$

Mean

$$\mu = -2 \int_0^1 \frac{x \operatorname{arctanh}(x) e^{-(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx$$

Variance

$$\sigma^2 = -2 \int_0^1 \frac{x^2 \operatorname{arctanh}(x) e^{-(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx - 4 \left( \int_0^1 \frac{x \operatorname{arctanh}(x) e^{-(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 -2 \frac{x^r \operatorname{arctanh}(x) e^{-(\operatorname{arctanh}(x))^2}}{x^2 - 1} dx$$

Moment Generating Function

$$-2 \int_0^1 \frac{\operatorname{arctanh}(x) e^{tx - (\operatorname{arctanh}(x))^2}}{x^2 - 1} dx_1$$


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$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = 2 \frac{\operatorname{arcsinh}(x) e^{-(\operatorname{arcsinh}(x))^2}}{\sqrt{x^2 + 1}}$$

Cumulative Distribution Function

$$F(x) = 1 - e^{-(\ln(-x + \sqrt{x^2 + 1}))^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{ERROR}(IDF) : \text{Could not find the appropriate inverse}$$

$$[s \mapsto 1/2 \left( e^{2\sqrt{\ln(-(1+s)^{-1})}} - 1 \right) e^{-\sqrt{\ln(-(1+s)^{-1})}}]$$

Survivor Function

$$S(x) = e^{-(\ln(-x + \sqrt{x^2 + 1}))^2}$$

Hazard Function

$$h(x) = 2 \frac{\operatorname{arcsinh}(x) e^{-(\operatorname{arcsinh}(x) - \ln(-x + \sqrt{x^2 + 1}))(\operatorname{arcsinh}(x) + \ln(-x + \sqrt{x^2 + 1}))}}{\sqrt{x^2 + 1}}$$

Mean

$$\mu = \int_0^\infty 2 \frac{x \operatorname{arcsinh}(x) e^{-(\operatorname{arcsinh}(x))^2}}{\sqrt{x^2 + 1}} dx$$

Variance

$$\sigma^2 = \int_0^\infty 2 \frac{x^2 \operatorname{arcsinh}(x) e^{-(\operatorname{arcsinh}(x))^2}}{\sqrt{x^2 + 1}} dx - \left( \int_0^\infty 2 \frac{x \operatorname{arcsinh}(x) e^{-(\operatorname{arcsinh}(x))^2}}{\sqrt{x^2 + 1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2 \frac{x^r \operatorname{arcsinh}(x) e^{-(\operatorname{arcsinh}(x))^2}}{\sqrt{x^2 + 1}} dx$$

Moment Generating Function

$$\int_0^\infty 2 \frac{\operatorname{arcsinh}(x) e^{tx - (\operatorname{arcsinh}(x))^2}}{\sqrt{x^2 + 1}} dx_1$$

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$$t \mapsto \operatorname{arcsinh}(t)$$

Probability Distribution Function

$$f(x) = 2 \sinh(x) e^{-(\sinh(x))^2} \cosh(x)$$

Cumulative Distribution Function

$$F(x) = \left( e^{1/4 (e^{4x} + 1) e^{-2x}} - e^{1/2} \right) e^{-1/4 (e^{4x} + 1) e^{-2x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{ERROR}(IDF) : \text{Could not find the appropriate inverse}$$

$$[s \mapsto -1/2 \ln \left( -2 \ln(-s + 1) + 1 - 2 \sqrt{\ln(-s + 1) (\ln(-s + 1) - 1)} \right)]$$

Survivor Function

$$S(x) = e^{-1/4 e^{2x} + 1/2 - 1/4 e^{-2x}}$$

Hazard Function

$$h(x) = 2 \sinh(x) e^{-(\cosh(x))^2 + 1/2 + 1/4 e^{2x} + 1/4 e^{-2x}} \cosh(x)$$

Mean

$$mu = \int_0^\infty e^{1/2 - 1/2 \cosh(2x)} x \sinh(2x) dx$$

Variance

$$sigma^2 = \int_0^\infty e^{1/2 - 1/2 \cosh(2x)} x^2 \sinh(2x) dx - \left( \int_0^\infty e^{1/2 - 1/2 \cosh(2x)} x \sinh(2x) dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2 x^r \sinh(x) e^{-(\sinh(x))^2} \cosh(x) dx$$

Moment Generating Function

$$\int_0^\infty e^{tx + 1/2 - 1/2 \cosh(2x)} \sinh(2x) dx_1$$

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$$t \mapsto \operatorname{csch}(t+1)$$

Probability Distribution Function

$$f(x) = 2 \frac{(-1 + \operatorname{arccsch}(x)) e^{-(1 + \operatorname{arccsch}(x))^2}}{\sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = 2 \int_0^x \frac{(-1 + \operatorname{arccsch}(t)) e^{-(1 + \operatorname{arccsch}(t))^2}}{\sqrt{t^2 + 1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{"Unable to find IDF"}$$

Survivor Function

$$S(x) = 1 - 2 \int_0^x \frac{(-1 + \operatorname{arccsch}(t)) e^{-(1+\operatorname{arccsch}(t))^2}}{\sqrt{t^2 + 1} |t|} dt$$

Hazard Function

$$h(x) = -2 \frac{(-1 + \operatorname{arccsch}(x)) e^{-(1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2 + 1} |x|} \left( -1 + 2 \int_0^x \frac{(-1 + \operatorname{arccsch}(t)) e^{-(1+\operatorname{arccsch}(t))^2}}{\sqrt{t^2 + 1} |t|} dt \right)$$

Mean

$$mu = 2 \int_0^{2^{\frac{e}{e^2-1}}} \frac{(-1 + \operatorname{arccsch}(x)) e^{-(1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2 + 1}} dx$$

Variance

$$sigma^2 = 2 \int_0^{2^{\frac{e}{e^2-1}}} x \frac{(-1 + \operatorname{arccsch}(x)) e^{-(1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2 + 1}} dx - 4 \left( \int_0^{2^{\frac{e}{e^2-1}}} \frac{(-1 + \operatorname{arccsch}(x)) e^{-(1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2 + 1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{-2^{(-e+e^{-1})^{-1}}} 2 \frac{x^r (-1 + \operatorname{arccsch}(x)) e^{-(1+\operatorname{arccsch}(x))^2}}{\sqrt{x^2 + 1} |x|} dx$$

Moment Generating Function

$$2 \int_0^{2^{\frac{e}{e^2-1}}} \frac{(-1 + \operatorname{arccsch}(x)) e^{-(\operatorname{arccsch}(x))^2 + tx + 2 \operatorname{arccsch}(x) - 1}}{\sqrt{x^2 + 1} x} dx_1$$

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$$t \mapsto \operatorname{arccsch}(t + 1)$$

Probability Distribution Function

$$f(x) = -2 \frac{(\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{-\frac{(\sinh(x)-1)^2}{(\sinh(x))^2}}$$

Cumulative Distribution Function

$$F(x) = e^{-\frac{e^{4x} - 4e^{3x} + 2e^{2x} + 4e^x + 1}{e^{4x} - 2e^{2x} + 1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [ln \circ s \mapsto RootOf \left( (1 + \ln(s)) \cdot Z^4 - 4 \cdot Z^3 + (-2 \ln(s) + 2) \cdot Z^2 + 4 \cdot Z + 1 + \ln(s) \right)]$$

Survivor Function

$$S(x) = 1 - e^{\frac{-e^{4x} + 4e^{3x} - 2e^{2x} - 4e^x - 1}{e^{4x} - 2e^{2x} + 1}}$$

Hazard Function

$$h(x) = 2 \frac{(\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{-\frac{(\sinh(x)-1)^2}{(\sinh(x))^2}} \left( -1 + e^{-\frac{e^{4x} - 4e^{3x} + 2e^{2x} + 4e^x + 1}{e^{4x} - 2e^{2x} + 1}} \right)^{-1}$$

Mean

$$\mu = -2 \int_0^{\ln(1+\sqrt{2})} \frac{(\sinh(x) - 1) \cosh(x) x}{(\sinh(x))^3} e^{\frac{-(\cosh(x))^2 + 2 \sinh(x)}{(\sinh(x))^2}} dx$$

Variance

$$\sigma^2 = -2 \int_0^{\ln(1+\sqrt{2})} \frac{(\sinh(x) - 1) \cosh(x) x^2}{(\sinh(x))^3} e^{\frac{-(\cosh(x))^2 + 2 \sinh(x)}{(\sinh(x))^2}} dx - 4 \left( \int_0^{\ln(1+\sqrt{2})} \frac{(\sinh(x) - 1) \cosh(x) x}{(\sinh(x))^3} e^{\frac{-(\cosh(x))^2 + 2 \sinh(x)}{(\sinh(x))^2}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\ln(1+\sqrt{2})} -2 \frac{x^r (\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{-\frac{(\sinh(x)-1)^2}{(\sinh(x))^2}} dx$$

Moment Generating Function

$$-2 \int_0^{\ln(1+\sqrt{2})} \frac{(\sinh(x) - 1) \cosh(x)}{(\sinh(x))^3} e^{\frac{(\cosh(x))^2 tx - (\cosh(x))^2 - tx + 2 \sinh(x)}{(\sinh(x))^2}} dx$$

$$t \mapsto (\tanh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{e^{-(1+\operatorname{arctanh}(x^{-1}))^2} (-1 + \operatorname{arctanh}(x^{-1}))}{x^2 - 1}$$

Cumulative Distribution Function

$$F(x) = (x-1)^{1/2 \ln(x+1)-1} (x+1) e^{-1/4 (\ln(x+1))^2 - 1/4 (\ln(x-1))^2 - 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf} \left( -(-Z+1)^{1/2 \ln(-Z-1)} e^{-1/4 (\ln(-Z+1))^2 - 1/4 (\ln(-Z-1))^2 - 1} Z - (-Z+1)^{1/2 \ln(-Z-1)} \right)]$$

Survivor Function

$$S(x) = -\frac{(x+1)^{1/2 \ln(x-1)} e^{-1/4 (\ln(x+1))^2 - 1/4 (\ln(x-1))^2 - 1} x + (x+1)^{1/2 \ln(x-1)} e^{-1/4 (\ln(x+1))^2 - 1/4 (\ln(x-1))^2 - 1}}{x-1}$$

Hazard Function

$$h(x) = -2 \frac{e^{-(1+\operatorname{arctanh}(x^{-1}))^2} (-1 + \operatorname{arctanh}(x^{-1}))}{\left( (x-1)^{1/2 \ln(x+1)} e^{-1/4 (\ln(x+1))^2 - 1/4 (\ln(x-1))^2 - 1} x + (x-1)^{1/2 \ln(x+1)} e^{-1/4 (\ln(x+1))^2 - 1/4 (\ln(x-1))^2 - 1} \right)}$$

Mean

$$mu = 2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x (-1 + \operatorname{arctanh}(x^{-1})) e^{-(1+\operatorname{arctanh}(x^{-1}))^2}}{x^2 - 1} dx$$

Variance

$$sigma^2 = 2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^2 (-1 + \operatorname{arctanh}(x^{-1})) e^{-(1+\operatorname{arctanh}(x^{-1}))^2}}{x^2 - 1} dx - 4 \left( \int_1^{\frac{e^2+1}{e^2-1}} \frac{x (-1 + \operatorname{arctanh}(x^{-1})) e^{-(1+\operatorname{arctanh}(x^{-1}))^2}}{x^2 - 1} dx \right)^2$$

Moment Function

$$m(x) = \int_1^{\frac{e+e^{-1}}{e-e^{-1}}} 2 \frac{x^r (-1 + \operatorname{arctanh}(x^{-1})) e^{-(1+\operatorname{arctanh}(x^{-1}))^2}}{x^2 - 1} dx$$

Moment Generating Function

$$2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{(-1 + \operatorname{arctanh}(x^{-1})) e^{-(\operatorname{arctanh}(x^{-1}))^2 + tx + 2 \operatorname{arctanh}(x^{-1}) - 1}}{x^2 - 1} dx_1$$

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$$t \mapsto (\sinh(t+1))^{-1}$$



Probability Distribution Function

$$f(x) = 2 \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{-(1 + \operatorname{arcsinh}(x^{-1}))^2}}{\sqrt{x^2 + 1} |x|}$$

Cumulative Distribution Function

$$F(x) = x^{2 \ln(\sqrt{x^2+1}+1)-2} e^{-1 - (\ln(\sqrt{x^2+1}+1))^2 - (\ln(x))^2} \left( x^2 + 2 + 2 \sqrt{x^2 + 1} \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = - \frac{(\sqrt{x^2 + 1} + 1)^{2 \ln(x)} e^{-1 - (\ln(\sqrt{x^2+1}+1))^2 - (\ln(x))^2} x^2 + 2 \sqrt{x^2 + 1} (\sqrt{x^2 + 1} + 1)^{2 \ln(x)} e^{-1 - (\ln(\sqrt{x^2+1}+1))^2 - (\ln(x))^2}}{x^2}$$

Hazard Function

$$h(x) = -2 \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{-(1 + \operatorname{arcsinh}(x^{-1}))^2}}{\sqrt{x^2 + 1} |x| \left( x^{2 \ln(\sqrt{x^2+1}+1)+2} e^{-1 - (\ln(\sqrt{x^2+1}+1))^2 - (\ln(x))^2} + 2 \sqrt{x^2 + 1} x^{2 \ln(\sqrt{x^2+1}+1)} e^{-1 - (\ln(\sqrt{x^2+1}+1))^2 - (\ln(x))^2} \right)}$$

Mean

$$mu = 2 \int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{-(1 + \operatorname{arcsinh}(x^{-1}))^2}}{\sqrt{x^2 + 1}} dx$$

Variance

$$sigma^2 = 2 \int_0^{2 \frac{e}{e^2-1}} \frac{x (-1 + \operatorname{arcsinh}(x^{-1})) e^{-(1 + \operatorname{arcsinh}(x^{-1}))^2}}{\sqrt{x^2 + 1}} dx - 4 \left( \int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{-(1 + \operatorname{arcsinh}(x^{-1}))^2}}{\sqrt{x^2 + 1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2 \frac{e}{e^2-1}} \frac{x^r (-1 + \operatorname{arcsinh}(x^{-1})) e^{-(1 + \operatorname{arcsinh}(x^{-1}))^2}}{\sqrt{x^2 + 1} |x|} dx$$

Moment Generating Function

$$2 \int_0^{2 \frac{e}{e^2-1}} \frac{(-1 + \operatorname{arcsinh}(x^{-1})) e^{-(\operatorname{arcsinh}(x^{-1}))^2 + tx + 2 \operatorname{arcsinh}(x^{-1}) - 1}}{\sqrt{x^2 + 1} x} dx_1$$

---


$$t \mapsto (\operatorname{arcsinh}(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 2 \frac{(-1 + \sinh(x^{-1})) e^{-(1 + \sinh(x^{-1}))^2} \cosh(x^{-1})}{x^2}$$

Cumulative Distribution Function

$$F(x) = e^{-1/4 \left( e^{4x^{-1}} - 4e^{3x^{-1}} + 2e^{2x^{-1}} + 4e^{x^{-1}} + 1 \right)} e^{-2x^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto (\ln(\operatorname{RootOf}(1 + \_Z^4 - 4\_Z^3 + (4 \ln(s) + 2)\_Z^2 + 4\_Z)))^{-1}]$$

Survivor Function

$$S(x) = 1 - e^{-1/4 \left( e^{4x^{-1}} - 4e^{3x^{-1}} + 2e^{2x^{-1}} + 4e^{x^{-1}} + 1 \right)} e^{-2x^{-1}}$$

Hazard Function

$$h(x) = -2 \frac{(-1 + \sinh(x^{-1})) e^{-(1 + \sinh(x^{-1}))^2} \cosh(x^{-1})}{x^2} \left( -1 + e^{-1/4 \left( e^{4x^{-1}} - 4e^{3x^{-1}} + 2e^{2x^{-1}} + 4e^{x^{-1}} + 1 \right)} e^{-2x^{-1}} \right)$$

Mean

$$\mu = \text{"Unable to find Mean"}$$

Variance

$$\sigma^2 = \text{"Unable to find Variance"}$$

Moment Function

$$m(x) = \int_0^{(\ln(1+\sqrt{2}))^{-1}} 2 \frac{x^r (-1 + \sinh(x^{-1})) e^{-(1 + \sinh(x^{-1}))^2} \cosh(x^{-1})}{x^2} dx$$

Moment Generating Function

$$\text{"unable to calculate MGF"}$$

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Probability Distribution Function

$$f(x) = 2 \frac{\operatorname{arccsch}((x-1)^{-1}) e^{-(\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}}$$

Cumulative Distribution Function

$$F(x) = 2 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1}) e^{-(\operatorname{arccsch}((t-1)^{-1}))^2}}{\sqrt{t^2 - 2t + 2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{"Unable to find IDF"}$$

Survivor Function

$$S(x) = 1 - 2 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1}) e^{-(\operatorname{arccsch}((t-1)^{-1}))^2}}{\sqrt{t^2 - 2t + 2}} dt$$

Hazard Function

$$h(x) = -2 \frac{\operatorname{arccsch}((x-1)^{-1}) e^{-(\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}} \left( -1 + 2 \int_1^x \frac{\operatorname{arccsch}((t-1)^{-1}) e^{-(\operatorname{arccsch}((t-1)^{-1}))^2}}{\sqrt{t^2 - 2t + 2}} dt \right)$$

Mean

$$\mu = \int_1^\infty 2 \frac{x \operatorname{arccsch}((x-1)^{-1}) e^{-(\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}} dx$$

Variance

$$\sigma^2 = \int_1^\infty 2 \frac{\operatorname{arccsch}((x-1)^{-1}) x^2 e^{-(\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}} dx - \left( \int_1^\infty 2 \frac{x \operatorname{arccsch}((x-1)^{-1}) e^{-(\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}} dx \right)^2$$

Moment Function

$$m(x) = \int_1^\infty 2 \frac{x^r \operatorname{arccsch}((x-1)^{-1}) e^{-(\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}} dx$$

Moment Generating Function

$$\int_1^\infty 2 \frac{\operatorname{arccsch}((x-1)^{-1}) e^{tx - (\operatorname{arccsch}((x-1)^{-1}))^2}}{\sqrt{x^2 - 2x + 2}} dx_1$$


---

$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -2 \frac{1}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-(\operatorname{arctanh}(x))^{-2}}$$

Cumulative Distribution Function

$$F(x) = e^{-4(\ln(x+1) - \ln(1-x))^{-2}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{ERROR}(IDF) : \text{Could not find the appropriate inverse}$$

$$[s \mapsto 1 \left( e^{2 \frac{1}{\sqrt{-\ln(s)}}} - 1 \right) \left( e^{2 \frac{1}{\sqrt{-\ln(s)}}} + 1 \right)^{-1}]$$

Survivor Function

$$S(x) = 1 - e^{-4(\ln(x+1) - \ln(1-x))^{-2}}$$

Hazard Function

$$h(x) = 2 \frac{1}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-(\operatorname{arctanh}(x))^{-2}} \left( -1 + e^{-4(\ln(x+1) - \ln(1-x))^{-2}} \right)^{-1}$$

Mean

$$\mu = -2 \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-(\operatorname{arctanh}(x))^{-2}} dx$$

Variance

$$\sigma^2 = -2 \int_0^1 \frac{x^2}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-(\operatorname{arctanh}(x))^{-2}} dx - 4 \left( \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-(\operatorname{arctanh}(x))^{-2}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 -2 \frac{x^r}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{-(\operatorname{arctanh}(x))^{-2}} dx$$

Moment Generating Function

$$-2 \int_0^1 \frac{1}{(\operatorname{arctanh}(x))^3 (x^2 - 1)} e^{\frac{tx(\operatorname{arctanh}(x))^2 - 1}{(\operatorname{arctanh}(x))^2}} dx_1$$


---

$$t \mapsto \operatorname{csch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3 |x|} e^{-(\operatorname{arccsch}(x))^{-2}}$$

Cumulative Distribution Function

$$F(x) = 2 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^3 |t|} e^{-(\operatorname{arccsch}(t))^{-2}} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{"Unable to find ID F"}$$

Survivor Function

$$S(x) = 1 - 2 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^3 |t|} e^{-(\operatorname{arccsch}(t))^{-2}} dt$$

Hazard Function

$$h(x) = -2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3 |x|} e^{-(\operatorname{arccsch}(x))^{-2}} \left( -1 + 2 \int_0^x \frac{1}{\sqrt{t^2 + 1} (\operatorname{arccsch}(t))^3 |t|} e^{-(\operatorname{arccsch}(t))^{-2}} dt \right)$$

Mean

$$mu = \int_0^\infty 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3} e^{-(\operatorname{arccsch}(x))^{-2}} dx$$

Variance

$$sigma^2 = \int_0^\infty 2 \frac{x}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3} e^{-(\operatorname{arccsch}(x))^{-2}} dx - \left( \int_0^\infty 2 \frac{1}{\sqrt{x^2 + 1} (\operatorname{arccsch}(x))^3} e^{-(\operatorname{arccsch}(x))^{-2}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2 \frac{x^r}{\sqrt{x^2+1} (\operatorname{arccsch}(x))^3 |x|} e^{-(\operatorname{arccsch}(x))^{-2}} dx$$

Moment Generating Function

$$\int_0^\infty 2 \frac{1}{\sqrt{x^2+1} (\operatorname{arccsch}(x))^3 x} e^{\frac{tx (\operatorname{arccsch}(x))^2 - 1}{(\operatorname{arccsch}(x))^2}} dx_1$$


---

$$t \mapsto \operatorname{arccsch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 2 e^{-(\sinh(x))^2} \cosh(x) \sinh(x)$$

Cumulative Distribution Function

$$F(x) = \left( e^{1/4 (e^{4x}+1)e^{-2x}} - e^{1/2} \right) e^{-1/4 (e^{4x}+1)e^{-2x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = \text{ERROR}(IDF) : \text{Could not find the appropriate inverse}$$

$$[s \mapsto -1/2 \ln \left( -2 \ln(-s+1) + 1 - 2 \sqrt{\ln(-s+1) (\ln(-s+1) - 1)} \right)]$$

Survivor Function

$$S(x) = e^{-1/4 e^{2x} + 1/2 - 1/4 e^{-2x}}$$

Hazard Function

$$h(x) = 2 \sinh(x) e^{-(\cosh(x))^2 + 1/2 + 1/4 e^{2x} + 1/4 e^{-2x}} \cosh(x)$$

Mean

$$\mu = \int_0^\infty e^{1/2 - 1/2 \cosh(2x)} x \sinh(2x) dx$$

Variance

$$\sigma^2 = \int_0^\infty e^{1/2 - 1/2 \cosh(2x)} x^2 \sinh(2x) dx - \left( \int_0^\infty e^{1/2 - 1/2 \cosh(2x)} x \sinh(2x) dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 2x^r e^{-(\sinh(x))^2} \cosh(x) \sinh(x) \, dx$$

Moment Generating Function

$$\int_0^\infty e^{tx+1/2-1/2 \cosh(2x)} \sinh(2x) \, dx_1$$