

```
> restart;  
read("c:/appl/appl7.txt");
```

#### PROCEDURES:

*AllPermutations(n), AllCombinations(n, k), Benford(X), BootstrapRV(Data),  
CDF:CHF:HF:IDF:PDF:SF(X, [x]), CoefOfVar(X), Convolution(X, Y),  
ConvolutionIID(X, n), CriticalPoint(X, prob), Determinant(MATRIX), Difference(X, Y),  
Display(X), ExpectedValue(X, [g]), KSTest(X, Data, Parameters), Kurtosis(X),  
Maximum(X, Y), MaximumIID(X, n), Mean(X), MGF(X), Minimum(X, Y),  
MinimumIID(X, n), Mixture(MixParameters, MixRVs),  
MLE(X, Data, Parameters, [Rightcensor]), MLENHPP(X, Data, Parameters, obstime),  
MLEWeibull(Data, [Rightcensor]), MOM(X, Data, Parameters),  
NextCombination(Previous, size), NextPermutation(Previous), OrderStat(X, n, r, ["wo"]),  
PlotDist(X, [low], [high]), PlotEmpCDF(Data, [low], [high]),  
PlotEmpCIF(Data, [low], [high]), PlotEmpSF(Data, Censor),  
PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),  
PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),  
PlotEmpVsFittedSF(X, Data, Parameters, Censor, low, high),  
PPPlot(X, Data, Parameters), Product(X, Y), ProductIID(X, n),  
QQPlot(X, Data, Parameters), RangeStat(X, n, ["wo"]), Skewness(X), Transform(X, g),  
Truncate(X, low, high), Variance(X), VerifyPDF(X)*

#### Procedure Notation:

*X and Y are random variables*

*Greek letters are numeric or symbolic parameters*

*x is numeric or symbolic*

*n and r are positive integers,  $n \geq r$*

*low and high are numeric*

*g is a function*

*Brackets [] denote optional parameters*

*"double quotes" denote character strings*

*MATRIX is a 2 x 2 array of random variables*

*A capitalized parameter indicates that it must be  
entered as a list --> ex. Data := [1, 12.4, 34, 52.45, 63]*

#### Variate Generation:

*ArcTanVariate(alpha, phi), BinomialVariate(n, p, m), ExponentialVariate(lambda),  
NormalVariate(mu, sigma), UniformVariate(), WeibullVariate(lambda, kappa, m)*

#### DATA SETS:

*BallBearing, HorseKickFatalities, Hurricane, MP6, RatControl, RatTreatment, USSHalfBeak*

*ArcSinRV(), ArcTanRV(alpha, phi), BetaRV(alpha, beta), CauchyRV(a, alpha), ChiRV(n),*

*ChiSquareRV(n), ErlangRV(lambda, n), ErrorRV(mu, alpha, d), ExponentialRV(lambda),  
 ExponentialPowerRV(lambda, kappa), ExtremeValueRV(alpha, beta), FRV(n1, n2),  
 GammaRV(lambda, kappa), GeneralizedParetoRV(gamma, delta, kappa),  
 GompertzRV(delta, kappa), HyperbolicSecantRV(), HyperExponentialRV(p, l),  
 HypoExponentialRV(l), IDBRV(gamma, delta, kappa), InverseGaussianRV(lambda, mu),  
 InvertedGammaRV(alpha, beta), KSRV(n), LaPlaceRV(omega, theta),  
 LogGammaRV(alpha, beta), LogisticRV(kappa, lambda), LogLogisticRV(lambda, kappa),  
 LogNormalRV(mu, sigma), LomaxRV(kappa, lambda), MakehamRV(gamma, delta, kappa),  
 MuthRV(kappa), NormalRV(mu, sigma), ParetoRV(lambda, kappa), RayleighRV(lambda),  
 StandardCauchyRV(), StandardNormalRV(), StandardTriangularRV(m),  
 StandardUniformRV(), TRV(n), TriangularRV(a, m, b), UniformRV(a, b),  
 WeibullRV(lambda, kappa)*

Error, attempting to assign to `DataSets` which is protected.  
 Try declaring `local DataSets`; see ?protect for details.

```

> bf := MuthRV(a);
  bfname := "MuthRV(a)";
Originally a, renamed a~:
  is assumed to be: RealRange(Open(0),1)

```

$$bf := \left[ \left[ x \rightarrow (e^{a \sim x} - a) e^{-\frac{e^{a \sim x}}{a \sim} + a \sim x + \frac{1}{a \sim}} \right], [0, \infty], ["Continuous", "PDF"] \right]$$

*bfname := "MuthRV(a)"*

(1)

```

> #plot(1/csch(t)+1, t = 0..0.0010);
  #plot(diff(1/csch(t),t), t=0..0.0010);
  #limit(1/csch(t), t=0);
> solve(exp(-t) = y, t);

```

$$-\ln(y)$$

(2)

```

> # discarded -ln(t + 1), t-> csch(t), t->arccsch(t), t -> tan(t),
> #name of the file for latex output
  filename := "C:/Latex_Output_2/Muth_Gen.tex";

```

```

glist := [t -> t^2, t -> sqrt(t), t -> 1/t, t -> arctan(t), t
-> exp(t), t -> ln(t), t -> exp(-t), t -> -ln(t), t -> ln(t+1),
t -> 1/(ln(t+2)), t -> tanh(t), t -> sinh(t), t -> arcsinh(t),
t-> csch(t+1), t->arccsch(t+1), t-> 1/tanh(t+1), t-> 1/sinh(t+1),
t-> 1/arcsinh(t+1), t-> 1/csch(t)+1, t-> tanh(1/t), t->csch
(1/t), t-> arccsch(1/t), t-> arctanh(1/t) ]:

```

```

base := t -> PDF(bf, t):

```

```

print(base(x)):

```

```

#begin latex file formatting
appendto(filename);

```

```

printf("\\documentclass[12pt]{article} \n");
printf("\\usepackage{amsfonts} \n");
printf("\\begin{document} \n");
print(bfname);
printf("$\$");
latex(bf[1]);
printf("$\$");
writeto(terminal);

#begin loopint through transformations
for i from 1 to 22 do
#for i from 1 to 3 do
    print( "i is", i, " -----"
-----" );

    g := glist[i];
    l := bf[2][1];
    u := bf[2][2];
    Temp := Transform(bf, [[unapply(g(x), x)], [l,u]]);

#terminal output
print( "l and u", l, u );
print("g(x)", g(x), "base", base(x),bfname);
print("f(x)", PDF(Temp, x));

#latex output
appendto(filename);
printf("----- \\\");
printf("$\$");
latex(glist[i]);
printf("$\$");
printf("Probability Distribution Function \n$$ f(x)=");
latex(PDF(Temp,x));
printf(" \\qquad");
latex(Temp[2][1]);
printf(" < x < ");
latex(Temp[2][2]);
printf("$\$");

writeto(terminal);

od;

#final latex output
appendto(filename);
printf("\\end{document}\n");
writeto(terminal);

```

$filename := "C:/Latex\_Output\_2/Muth\_Gen.tex"$

$$\left(e^{a\sim x}-a\sim\right)e^{-\frac{e^{a\sim x}}{a\sim}+a\sim x+\frac{1}{a\sim}}$$

"i is", 1,

"-----  
-----"

$$g:=t\rightarrow t^2$$

$$l:=0$$

$$u:=\infty$$

$$Temp:=\left[\left[y\sim\rightarrow\frac{1}{2}\frac{\left(e^{a\sim\sqrt{y\sim}}-a\sim\right)e^{-\frac{-a\sim^2\sqrt{y\sim}+e^{a\sim\sqrt{y\sim}}-1}{a\sim}}}{\sqrt{y\sim}}\right],[0,\infty],[\text{"Continuous"},\right.\\ \left.\text{"PDF"}]\right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", }x^2,\text{"base", }\left(e^{a\sim x}-a\sim\right)e^{-\frac{e^{a\sim x}}{a\sim}+a\sim x+\frac{1}{a\sim}},\text{"MuthRV(a)"}$$

$$\text{"f(x)", }\frac{1}{2}\frac{\left(e^{a\sim\sqrt{x}}-a\sim\right)e^{-\frac{-a\sim^2\sqrt{x}+e^{a\sim\sqrt{x}}-1}{a\sim}}}{\sqrt{x}}$$

"i is", 2,

"-----  
-----"

$$g:=t\rightarrow\sqrt{t}$$

$$l:=0$$

$$u:=\infty$$

$$Temp:=\left[\left[y\sim\rightarrow2\left(e^{a\sim y\sim^2}-a\sim\right)e^{-\frac{-a\sim^2y\sim^2+e^{a\sim y\sim^2}-1}{a\sim}}\right]_{y\sim},[0,\infty],[\text{"Continuous"},\text{"PDF"}]\right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", }\sqrt{x},\text{"base", }\left(e^{a\sim x}-a\sim\right)e^{-\frac{e^{a\sim x}}{a\sim}+a\sim x+\frac{1}{a\sim}},\text{"MuthRV(a)"}$$

$$\text{"f(x)", }2\left(e^{a\sim x^2}-a\sim\right)e^{-\frac{-a\sim^2x^2+e^{a\sim x^2}-1}{a\sim}}x$$

"i is", 3,

"-----  
-----"

$$g:=t\rightarrow\frac{1}{t}$$

$$\begin{aligned}
& l := 0 \\
& u := \infty \\
& Temp := \left[ \left[ y \rightarrow \frac{\left( e^{\frac{a}{y}} - a \right) e^{-\frac{\frac{a}{y} y - a^2 - y}}}{y^2} \right], [0, \infty], ["Continuous", "PDF"] \right] \\
& \text{"l and u", } 0, \infty \\
& \text{"g(x)", } \frac{1}{x}, \text{"base", } \left( e^{a^x} - a \right) e^{-\frac{e^{a^x}}{a} + a^x + \frac{1}{a}}, \text{"MuthRV(a)} \\
& \text{"f(x)", } \frac{\left( e^{\frac{a}{x}} - a \right) e^{-\frac{\frac{a}{x} x - a^2 - x}}{a^x}}{x^2}
\end{aligned}$$

"i is", 4,

"-----"

$$\begin{aligned}
& g := t \rightarrow \arctan(t) \\
& l := 0 \\
& u := \infty \\
& Temp := \left[ \left[ y \rightarrow \left( e^{a^{\tan(y)}} - a \right) e^{-\frac{-a^2 \tan(y) + e^{a^{\tan(y)}} - 1}{a}} \left( 1 + \tan(y)^2 \right) \right], \left[ 0, \frac{1}{2} \pi \right], \right. \\
& \left. ["Continuous", "PDF"] \right]
\end{aligned}$$

$$\begin{aligned}
& \text{"l and u", } 0, \infty \\
& \text{"g(x)", } \arctan(x), \text{"base", } \left( e^{a^x} - a \right) e^{-\frac{e^{a^x}}{a} + a^x + \frac{1}{a}}, \text{"MuthRV(a)} \\
& \text{"f(x)", } \left( e^{a^{\tan(x)}} - a \right) e^{-\frac{-a^2 \tan(x) + e^{a^{\tan(x)}} - 1}{a}} \left( 1 + \tan(x)^2 \right)
\end{aligned}$$

"i is", 5,

"-----"

$$\begin{aligned}
& g := t \rightarrow e^t \\
& l := 0 \\
& u := \infty \\
& Temp := \left[ \left[ y \rightarrow \frac{e^{-\frac{y^a - 1}{a}} \left( -y^a a + y^{2a} \right)}{y} \right], [1, \infty], ["Continuous", "PDF"] \right] \\
& \text{"l and u", } 0, \infty \\
& \text{"g(x)", } e^x, \text{"base", } \left( e^{a^x} - a \right) e^{-\frac{e^{a^x}}{a} + a^x + \frac{1}{a}}, \text{"MuthRV(a)}
\end{aligned}$$

$$\text{"f(x)", } \frac{e^{-\frac{x^{a\sim}-1}{a\sim}} \left( -x^{a\sim} a\sim + x^{2 a\sim} \right)}{x}$$

"i is", 6,

"-----  
-----"

$$g := t \rightarrow \ln(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow \left( e^{a\sim e^{y\sim}} - a\sim \right) e^{-\frac{-a\sim^2 e^{y\sim} - a\sim y\sim + e^{a\sim} e^{y\sim}}{a\sim}} - 1 \right], [-\infty, \infty], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", } \ln(x), \text{"base", } \left( e^{a\sim x} - a\sim \right) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \left( e^{a\sim e^x} - a\sim \right) e^{-\frac{-a\sim^2 e^x - a\sim x + e^{a\sim} e^x - 1}{a\sim}}$$

"i is", 7,

"-----  
-----"

$$g := t \rightarrow e^{-t}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow \frac{e^{-\frac{y\sim^{-a\sim}-1}{a\sim}} \left( -y\sim^{-a\sim} a\sim + y\sim^{-2 a\sim} \right)}{y\sim} \right], [0, 1], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", } e^{-x}, \text{"base", } \left( e^{a\sim x} - a\sim \right) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \frac{e^{-\frac{x^{-a\sim}-1}{a\sim}} \left( -x^{-a\sim} a\sim + x^{-2 a\sim} \right)}{x}$$

"i is", 8,

"-----  
-----"

$$g := t \rightarrow -\ln(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow \left( e^{a\sim e^{-y\sim}} - a\sim \right) e^{-\frac{-a\sim^2 e^{-y\sim} + a\sim y\sim + e^{a\sim} e^{-y\sim}}{a\sim}} - 1 \right], [-\infty, \infty], ["Continuous",$$

"PDF"]

"l and u", 0, ∞

"g(x)",  $-\ln(x)$ , "base",  $(e^{a\sim x} - a\sim) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}$ , "MuthRV(a)"

"f(x)",  $(e^{a\sim e^{-x}} - a\sim) e^{-\frac{-a\sim^2 e^{-x} + a\sim x + e^{a\sim} e^{-x} - 1}{a\sim}}$

"i is", 9,

"-----"

$$g := t \rightarrow \ln(t + 1)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow (e^{a\sim (e^{y\sim} - 1)} - a\sim) e^{-\frac{-a\sim^2 e^{y\sim} + a\sim^2 - a\sim y\sim + e^{a\sim} (e^{y\sim} - 1) - 1}{a\sim}} \right], [0, \infty], \right]$$

["Continuous", "PDF"]

"l and u", 0, ∞

"g(x)",  $\ln(x + 1)$ , "base",  $(e^{a\sim x} - a\sim) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}$ , "MuthRV(a)"

"f(x)",  $(e^{a\sim (e^x - 1)} - a\sim) e^{-\frac{-a\sim^2 e^x + a\sim^2 - a\sim x + e^{a\sim} (e^x - 1) - 1}{a\sim}}$

"i is", 10,

"-----"

$$g := t \rightarrow \frac{1}{\ln(t + 2)}$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow \frac{\left( e^{a\sim \left( e^{\frac{1}{y\sim}} - 2 \right)} - a\sim \right) e^{-\frac{\frac{1}{e^{y\sim}} a\sim^2 y\sim + 2 a\sim^2 y\sim + e^{a\sim} \left( e^{\frac{1}{y\sim}} - 2 \right) y\sim - a\sim - y\sim}{a\sim y\sim}}}{y\sim^2} \right], \left[ 0, \right. \right]$$

$\frac{1}{\ln(2)}$ ], ["Continuous", "PDF"]

"l and u", 0, ∞

"g(x)",  $\frac{1}{\ln(x + 2)}$ , "base",  $(e^{a\sim x} - a\sim) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}$ , "MuthRV(a)"

$$\text{"f(x)", } \frac{\left( e^{a \sim \left( e^{\frac{1}{x}} - 2 \right)} - a \sim \right) e^{-\frac{\frac{1}{e^x} a \sim^2 x + 2 a \sim^2 x + e^{a \sim \left( e^{\frac{1}{x}} - 2 \right)} x - a \sim - x}}{a \sim x}}{x^2}$$

"i is", 11,

"-----"  
 -----"

$$g := t \rightarrow \tanh(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow - \frac{\left( e^{a \sim \operatorname{arctanh}(y \sim)} - a \sim \right) e^{-\frac{-a \sim^2 \operatorname{arctanh}(y \sim) + e^{a \sim \operatorname{arctanh}(y \sim)} - 1}}{a \sim}}{y \sim^2 - 1} \right], [0, 1], \right.$$

["Continuous", "PDF"]

$$\text{"l and u", } 0, \infty$$

$$\text{"g(x)", } \tanh(x), \text{"base", } \left( e^{a \sim x} - a \sim \right) e^{-\frac{e^{a \sim x}}{a \sim} + a \sim x + \frac{1}{a \sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } - \frac{\left( e^{a \sim \operatorname{arctanh}(x)} - a \sim \right) e^{-\frac{-a \sim^2 \operatorname{arctanh}(x) + e^{a \sim \operatorname{arctanh}(x)} - 1}}{a \sim}}{x^2 - 1}$$

"i is", 12,

"-----"  
 -----"

$$g := t \rightarrow \sinh(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \sim \rightarrow \frac{\left( e^{a \sim \operatorname{arcsinh}(y \sim)} - a \sim \right) e^{-\frac{-a \sim^2 \operatorname{arcsinh}(y \sim) + e^{a \sim \operatorname{arcsinh}(y \sim)} - 1}}{a \sim}}{\sqrt{y \sim^2 + 1}} \right], [0, \infty], \right.$$

["Continuous", "PDF"]

$$\text{"l and u", } 0, \infty$$

$$\text{"g(x)", } \sinh(x), \text{"base", } \left( e^{a \sim x} - a \sim \right) e^{-\frac{e^{a \sim x}}{a \sim} + a \sim x + \frac{1}{a \sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \frac{\left( e^{a \sim \operatorname{arcsinh}(x)} - a \sim \right) e^{-\frac{-a \sim^2 \operatorname{arcsinh}(x) + e^{a \sim \operatorname{arcsinh}(x)} - 1}}{a \sim}}{\sqrt{x^2 + 1}}$$



"i is", 13,

"-----"  
-----"

$$g := t \rightarrow \operatorname{arcsinh}(t)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \left( e^{a \sinh(y)} - a \right) e^{-\frac{-a^2 \sinh(y) + e^{a \sinh(y)} - 1}{a}} \cosh(y) \right], [0, \infty], \right. \\ \left. ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", arcsinh(x), "base", } \left( e^{a x} - a \right) e^{-\frac{e^{a x}}{a} + a x + \frac{1}{a}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \left( e^{a \sinh(x)} - a \right) e^{-\frac{-a^2 \sinh(x) + e^{a \sinh(x)} - 1}{a}} \cosh(x)$$

"i is", 14,

"-----"  
-----"

$$g := t \rightarrow \operatorname{csch}(t + 1)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \frac{\left( e^{a(-1 + \operatorname{arccsch}(y))} - a \right) e^{-\frac{-a^2 \operatorname{arccsch}(y) + a^2 + e^{a(-1 + \operatorname{arccsch}(y))} - 1}{a}}}{\sqrt{y^2 + 1} |y|} \right], \right. \\ \left. \left[ 0, \frac{2}{e - e^{-1}} \right], ["Continuous", "PDF"] \right]$$

"l and u", 0,  $\infty$

$$\text{"g(x)", csch(x + 1), "base", } \left( e^{a x} - a \right) e^{-\frac{e^{a x}}{a} + a x + \frac{1}{a}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \frac{\left( e^{a(-1 + \operatorname{arccsch}(x))} - a \right) e^{-\frac{-a^2 \operatorname{arccsch}(x) + a^2 + e^{a(-1 + \operatorname{arccsch}(x))} - 1}{a}}}{\sqrt{x^2 + 1} |x|}$$

"i is", 15,

"-----"  
-----"

$$g := t \rightarrow \operatorname{arccsch}(t + 1)$$

$$l := 0$$

$$u := \infty$$

$Temp := \left[ \left[ y_{\sim} \right. \right.$   
 $\rightarrow \frac{1}{\sinh(y_{\sim})^2} \left( \left( e^{-\frac{a_{\sim}(\sinh(y_{\sim}) - 1)}{\sinh(y_{\sim})}} \right. \right.$   
 $\left. \left. - a_{\sim} \right) e^{-\frac{a_{\sim}^2 \sinh(y_{\sim}) + e^{-\frac{a_{\sim}(\sinh(y_{\sim}) - 1)}{\sinh(y_{\sim})}} \sinh(y_{\sim}) - a_{\sim}^2 - \sinh(y_{\sim})}{\sinh(y_{\sim}) a_{\sim}}} \cosh(y_{\sim}) \right) \right], [0, \ln(1$   
 $+ \sqrt{2})], ["Continuous", "PDF"] \left. \right]$   
 $"l \text{ and } u", 0, \infty$   
 $"g(x)", \operatorname{arcsch}(x + 1), "base", (e^{a_{\sim} x} - a_{\sim}) e^{-\frac{e^{a_{\sim} x}}{a_{\sim}} + a_{\sim} x + \frac{1}{a_{\sim}}}, "MuthRV(a)"$   
 $"f(x)", \frac{\left( e^{-\frac{a_{\sim}(\sinh(x) - 1)}{\sinh(x)}} - a_{\sim} \right) e^{-\frac{a_{\sim}^2 \sinh(x) + e^{-\frac{a_{\sim}(\sinh(x) - 1)}{\sinh(x)}} \sinh(x) - a_{\sim}^2 - \sinh(x)}{\sinh(x) a_{\sim}}} \cosh(x)}{\sinh(x)^2}$   
 $"i \text{ is}", 16,$   
 $"-----"$   
 $-----"$   
 $g := t \rightarrow \frac{1}{\tanh(t + 1)}$   
 $l := 0$   
 $u := \infty$   
 $Temp := \left[ \left[ y_{\sim} \right. \right.$   
 $\rightarrow \frac{\left( e^{a_{\sim} \left( -1 + \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right) \right)} - a_{\sim} \right) e^{-\frac{-a_{\sim}^2 \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right) + a_{\sim}^2 + e^{a_{\sim} \left( -1 + \operatorname{arctanh}\left(\frac{1}{y_{\sim}}\right) \right)} - 1}{a_{\sim}}}}{y_{\sim}^2 - 1} \right], \left[ 1,$   
 $\frac{e + e^{-1}}{e - e^{-1}} \right], ["Continuous", "PDF"] \left. \right]$   
 $"l \text{ and } u", 0, \infty$

$$\text{"g(x)", } \frac{1}{\tanh(x+1)}, \text{"base", } \left( e^{a\sim x} - a\sim \right) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \frac{\left( e^{a\sim \left( -1 + \operatorname{arctanh}\left(\frac{1}{x}\right) \right)} - a\sim \right) e^{-\frac{-a\sim^2 \operatorname{arctanh}\left(\frac{1}{x}\right) + a\sim^2 + e^{a\sim \left( -1 + \operatorname{arctanh}\left(\frac{1}{x}\right) \right)} - 1}{a\sim}}}{x^2 - 1}$$

"i is", 17,  
 "-----"  
 "-----"

$$\begin{aligned} g &:= t \rightarrow \frac{1}{\sinh(t+1)} \\ l &:= 0 \\ u &:= \infty \end{aligned}$$

$$\begin{aligned} Temp &:= \left[ \left[ y\sim \right. \right. \\ &\rightarrow \left. \frac{\left( e^{a\sim \left( -1 + \operatorname{arcsinh}\left(\frac{1}{y\sim} \right) \right)} - a\sim \right) e^{-\frac{-a\sim^2 \operatorname{arcsinh}\left(\frac{1}{y\sim} \right) + a\sim^2 + e^{a\sim \left( -1 + \operatorname{arcsinh}\left(\frac{1}{y\sim} \right) \right)} - 1}{a\sim}}}{\sqrt{y\sim^2 + 1} \, |y\sim|} \right], \left[ 0, \right. \\ &\left. \left. \frac{2}{e - e^{-1}} \right], ["Continuous", "PDF"] \right] \end{aligned}$$

"l and u", 0,  $\infty$

$$\text{"g(x)", } \frac{1}{\sinh(x+1)}, \text{"base", } \left( e^{a\sim x} - a\sim \right) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \frac{\left( e^{a\sim \left( -1 + \operatorname{arcsinh}\left(\frac{1}{x}\right) \right)} - a\sim \right) e^{-\frac{-a\sim^2 \operatorname{arcsinh}\left(\frac{1}{x}\right) + a\sim^2 + e^{a\sim \left( -1 + \operatorname{arcsinh}\left(\frac{1}{x}\right) \right)} - 1}{a\sim}}}{\sqrt{x^2 + 1} \, |x|}$$

"i is", 18,  
 "-----"  
 "-----"

$$\begin{aligned} g &:= t \rightarrow \frac{1}{\operatorname{arcsinh}(t+1)} \\ l &:= 0 \end{aligned}$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \frac{\left( e^{a \left( -1 + \sinh \left( \frac{1}{y} \right) \right)} - a \right) e^{-\frac{-a^2 \sinh \left( \frac{1}{y} \right) + a^2 + e^{a \left( -1 + \sinh \left( \frac{1}{y} \right) \right)} - 1}}{a} \cosh \left( \frac{1}{y} \right)}{y^2}, \right. \right.$$

$$\left. \left[ 0, \frac{1}{\ln (1 + \sqrt{2})} \right], ["Continuous", "PDF"] \right]$$

"l and u", 0, ∞

"g(x)",  $\frac{1}{\operatorname{arcsinh}(x + 1)}$ , "base",  $(e^{a x} - a) e^{-\frac{e^{a x}}{a} + a x + \frac{1}{a}}$ , "MuthRV(a)"

"f(x)",  $\frac{\left( e^{a \left( -1 + \sinh \left( \frac{1}{x} \right) \right)} - a \right) e^{-\frac{-a^2 \sinh \left( \frac{1}{x} \right) + a^2 + e^{a \left( -1 + \sinh \left( \frac{1}{x} \right) \right)} - 1}}{a} \cosh \left( \frac{1}{x} \right)}{x^2}$

"i is", 19,  
 "-----"  
 "-----"

$$g := t \rightarrow \frac{1}{\operatorname{csch}(t)} + 1$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y \rightarrow \frac{\left( e^{a \operatorname{arccsch} \left( \frac{1}{y - 1} \right)} - a \right) e^{-\frac{-a^2 \operatorname{arccsch} \left( \frac{1}{y - 1} \right) + e^{a \operatorname{arccsch} \left( \frac{1}{y - 1} \right)} - 1}}{a} \right]}{\sqrt{y^2 - 2 y + 2}}, [1,$$

$$\infty], ["Continuous", "PDF"] \right]$$

"l and u", 0, ∞

$$\text{"g(x)", } \frac{1}{\operatorname{csch}(x)} + 1, \text{"base", } (e^{a\sim x} - a\sim) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } \frac{\left(e^{a\sim \operatorname{arccsch}\left(\frac{1}{x-1}\right)} - a\sim\right) e^{-\frac{-a\sim^2 \operatorname{arccsch}\left(\frac{1}{x-1}\right) + e^{a\sim \operatorname{arccsch}\left(\frac{1}{x-1}\right)} - 1}{a\sim}}}{\sqrt{x^2 - 2 x + 2}}$$

"i is", 20,

"-----"  
 -----"

$$g := t \rightarrow \tanh\left(\frac{1}{t}\right)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow -\frac{\left(e^{\frac{a\sim}{\operatorname{arctanh}(y\sim)}} - a\sim\right) e^{-\frac{\frac{a\sim}{e^{\operatorname{arctanh}(y\sim)}} \operatorname{arctanh}(y\sim) - a\sim^2 - \operatorname{arctanh}(y\sim)}{a\sim \operatorname{arctanh}(y\sim)}}}{\operatorname{arctanh}(y\sim)^2 (y\sim^2 - 1)} \right], [0, 1],$$

[ "Continuous", "PDF" ]

"l and u", 0,  $\infty$

$$\text{"g(x)", } \tanh\left(\frac{1}{x}\right), \text{"base", } (e^{a\sim x} - a\sim) e^{-\frac{e^{a\sim x}}{a\sim} + a\sim x + \frac{1}{a\sim}}, \text{"MuthRV(a)"}$$

$$\text{"f(x)", } -\frac{\left(e^{\frac{a\sim}{\operatorname{arctanh}(x)}} - a\sim\right) e^{-\frac{\frac{a\sim}{e^{\operatorname{arctanh}(x)}} \operatorname{arctanh}(x) - a\sim^2 - \operatorname{arctanh}(x)}{a\sim \operatorname{arctanh}(x)}}}{\operatorname{arctanh}(x)^2 (x^2 - 1)}$$

"i is", 21,

"-----"  
 -----"

$$g := t \rightarrow \operatorname{csch}\left(\frac{1}{t}\right)$$

$$l := 0$$

$$u := \infty$$

$$Temp := \left[ \left[ y\sim \rightarrow \frac{\left(e^{\frac{a\sim}{\operatorname{arccsch}(y\sim)}} - a\sim\right) e^{-\frac{\frac{a\sim}{e^{\operatorname{arccsch}(y\sim)}} \operatorname{arccsch}(y\sim) - a\sim^2 - \operatorname{arccsch}(y\sim)}{a\sim \operatorname{arccsch}(y\sim)}}}{\sqrt{y\sim^2 + 1} \operatorname{arccsch}(y\sim)^2 |y\sim|} \right], [0, \infty ],$$

["Continuous", "PDF"]

"l and u", 0, ∞

"g(x)",  $\operatorname{csch}\left(\frac{1}{x}\right)$ , "base",  $(e^{a \sim x} - a \sim) e^{-\frac{e^{a \sim x}}{a \sim} + a \sim x + \frac{1}{a \sim}}$ , "MuthRV(a)"

"f(x)",  $\frac{\left(e^{\frac{a \sim}{\operatorname{arccsch}(x)}} - a \sim\right) e^{-\frac{\frac{a \sim}{e^{\operatorname{arccsch}(x)}} \operatorname{arccsch}(x) - a \sim^2 - \operatorname{arccsch}(x)}{a \sim \operatorname{arccsch}(x)}}}{\sqrt{x^2 + 1} \operatorname{arccsch}(x)^2 |x|}$

"i is", 22,

"-----"  
 -----"

$g := t \rightarrow \operatorname{arccsch}\left(\frac{1}{t}\right)$

$l := 0$

$u := \infty$

$Temp := \left[ \left[ y \sim \rightarrow (e^{a \sim \sinh(y \sim)} - a \sim) e^{-\frac{-a \sim^2 \sinh(y \sim) + e^{a \sim \sinh(y \sim)} - 1}{a \sim}} \cosh(y \sim) \right], [0, \infty], \right.$

["Continuous", "PDF"]

"l and u", 0, ∞

"g(x)",  $\operatorname{arccsch}\left(\frac{1}{x}\right)$ , "base",  $(e^{a \sim x} - a \sim) e^{-\frac{e^{a \sim x}}{a \sim} + a \sim x + \frac{1}{a \sim}}$ , "MuthRV(a)"

"f(x)",  $(e^{a \sim \sinh(x)} - a \sim) e^{-\frac{-a \sim^2 \sinh(x) + e^{a \sim \sinh(x)} - 1}{a \sim}} \cosh(x)$

(3)