```
> restart;
  read("c:/appl/appl7.txt");
                                     PROCEDURES:
AllPermutations(n), AllCombinations(n, k), Benford(X), BootstrapRV(Data),
   CDF: CHF: HF: IDF: PDF: SF(X, [x])), CoefOfVar(X), Convolution(X, Y),
   Convolution IID(X, n), Critical Point(X, prob), Determinant(MATRIX), Difference(X, Y),
   Display(X), ExpectedValue(X, [g]), KSTest(X, Data, Parameters), Kurtosis(X),
   Maximum(X, Y), MaximumIID(X, n), Mean(X), MGF(X), Minimum(X, Y),
   MinimumIID(X, n), Mixture(MixParameters, MixRVs),
   MLE(X, Data, Parameters, [Rightcensor]), MLENHPP(X, Data, Parameters, obstime),
   MLEWeibull(Data, [Rightcensor]), MOM(X, Data, Parameters),
   NextCombination(Previous, size), NextPermutation(Previous), OrderStat(X, n, r, ["wo"]),
   PlotDist(X, [low], [high]), PlotEmpCDF(Data, [low], [high]),
   PlotEmpCIF(Data, [low], [high]), PlotEmpSF(Data, Censor),
   PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),
   PlotEmpVsFittedCDF(X, Data, Parameters, [low], [high]),
   PlotEmpVsFittedSF(X, Data, Parameters, Censor, low, high),
   PPPlot(X, Data, Parameters), Product(X, Y), ProductIID(X, n),
   QQPlot(X, Data, Parameters), RangeStat(X, n, ["wo"]), Skewness(X), Transform(X, g),
   Truncate(X, low, high), Variance(X), VerifyPDF(X)
```

## Procedure Notation:

X and Y are random variables

Greek letters are numeric or symbolic parameters

x is numeric or symbolic

n and r are positive integers, n >= r

low and high are numeric

g is a function

Brackets [] denote optional parameters

"double quotes" denote character strings

MATRIX is a 2 x 2 array of random variables

A capitalized parameter indicates that it must be
entered as a list --> ex. Data := [1, 12.4, 34, 52.45, 63]

## Variate Generation:

ArcTanVariate(alpha, phi), BinomialVariate(n, p, m), ExponentialVariate(lambda), NormalVariate(mu, sigma), UniformVariate(), WeibullVariate(lambda, kappa, m)

## DATA SETS:

BallBearing, HorseKickFatalities, Hurricane, MP6, RatControl, RatTreatment, USSHalfBeak

ArcSinRV(), ArcTanRV(alpha, phi), BetaRV(alpha, beta), CauchyRV(a, alpha), ChiRV(n),

```
ChiSquareRV(n), ErlangRV(lambda, n), ErrorRV(mu, alpha, d), ExponentialRV(lambda),
   ExponentialPowerRV(lambda, kappa), ExtremeValueRV(alpha, beta), FRV(n1, n2),
   GammaRV(lambda, kappa), GeneralizedParetoRV(gamma, delta, kappa),
   GompertzRV(delta, kappa), HyperbolicSecantRV(), HyperExponentialRV(p, l),
   HypoExponentialRV(l), IDBRV(gamma, delta, kappa), InverseGaussianRV(lambda, mu),
   InvertedGammaRV(alpha, beta), KSRV(n), LaPlaceRV(omega, theta),
   LogGammaRV(alpha, beta), LogisticRV(kappa, lambda), LogLogisticRV(lambda, kappa),
   LogNormalRV(mu, sigma), LomaxRV(kappa, lambda), MakehamRV(gamma, delta, kappa),
   MuthRV(kappa), NormalRV(mu, sigma), ParetoRV(lambda, kappa), RayleighRV(lambda),
   StandardCauchyRV(), StandardNormalRV(), StandardTriangularRV(m),
   StandardUniformRV(), TRV(n), TriangularRV(a, m, b), UniformRV(a, b),
   WeibullRV(lambda, kappa)
Error, attempting to assign to `DataSets` which is protected.
                   `local DataSets`; see ?protect for details.
> bf := LogNormalRV(1, 2);
  bfname := "LogNormalRV(1, 2)";
          bf := \left[ \left[ x \to \frac{1}{4} \, \frac{\sqrt{2} \, e^{-\frac{1}{8} \, (\ln(x) \, -1)^2}}{\sqrt{\pi} \, x} \right], [0, \, \infty], ["Continuous", "PDF"] \right]
                           bfname := "LogNormalRV(1, 2)"
> \#plot(1/csch(t)+1, t = 0..0.0010);
  #plot(diff(1/csch(t),t), t=0..0.0010);
  #limit(1/csch(t), t=0);
```

**(1)** 

```
-\ln(y)
                                                                                   (2)
|> # discarded -ln(t + 1), t-> csch(t),t->arccsch(t),t -> tan(t),
> glist := [t -> t^2 , t -> sqrt(t), t -> 1/t, t -> arctan(t), t
   -> \exp(t), t -> \ln(t), t -> \exp(-t), t -> -\ln(t), t -> \ln(t+1),
   t \rightarrow 1/(\ln(t+2)), t \rightarrow \tanh(t), t \rightarrow \sinh(t), t \rightarrow arcsinh(t),
   t \rightarrow csch(t+1), t \rightarrow arccsch(t+1), t \rightarrow 1/tanh(t+1), t \rightarrow 1/sinh(t+1),
    t-> 1/\operatorname{arcsinh}(t+1), t-> 1/\operatorname{csch}(t)+1, t-> \tanh(1/t), t-> \operatorname{csch}
   (1/t), t-> arccsch(1/t), t-> arctanh(1/t) ]:
   base := t \rightarrow PDF(bf, t):
   print(base(x)):
   for i from 22 to 22(glist) do
      print( "i is", i, " ------
      g := glist[i]:
       1 := bf[2][1];
      u := bf[2][2];
      Temp := Transform(bf, [[unapply(g(x), x)],[1,u]]);
```

> solve(exp(-t) = y, t);

```
#print( "l and u", l, u );
       #print("g(x)", g(x), "base", base(x),bfname);
print("f(x)", PDF(Temp, x));
#print("F(x)", CDF(Temp, x));
       #print("IDF(x)", IDF(Temp));
       #print("S(x)", SF(Temp, x));
print("h(x)", HF(Temp, x));
       #print("mean and variance", Mean(Temp), Variance(Temp));
       \#assume(r > 0); mf := int(x^r*PDF(Temp, x), x = Temp[2][1] ...
   Temp[2][2]);
       #print("MF", mf);
       #print("MGF", MGF(Temp));
       PlotDist(PDF(Temp), bf[2][1], bf[2][2]);
       PlotDist(HF(Temp), bf[2][1], bf[2][2]);
       latex(PDF(Temp,x));
       #print("transforming with", [[x->g(x)],[0,infinity]]);
       \#X2 := Transform(bf, [[x->g(x)],[0,infinity]]);
       #print("pdf of X2 = ", PDF(X2,x));
       #print("pdf of Temp = ", PDF(Temp,x));
   od;
                                            \frac{1}{4} \frac{\sqrt{2} e^{-\frac{1}{8} (\ln(x) - 1)^2}}{\sqrt{\pi} x}
"i is", 22,
                                             g := t \rightarrow \operatorname{arccsch}\left(\frac{1}{t}\right)
  Temp := \left[ \left[ y \sim \frac{1}{4} \frac{\sqrt{2} e^{-\frac{1}{8} (\ln(\sinh(y\sim)) - 1)^2} \cosh(y\sim)}{\sqrt{\pi} \sinh(y\sim)} \right], [0, \infty], ["Continuous", "PDF"] \right]
"f(x)", \frac{1}{4} \frac{\sqrt{2} e^{-\frac{1}{8} (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)}
"h(x)", -\frac{1}{2} \frac{\sqrt{2} e^{-\frac{1}{8} (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x) \left(-1 + \operatorname{erf}\left(\frac{1}{4} \sqrt{2} \left(\ln(e^x - 1) + \ln(e^x + 1) - \ln(2) - x - 1\right)\right)\right)}
```



