$$f(x) = \frac{x^{a-1}e^{-x^2/2}}{2^{a/2-1}\Gamma(a/2)} \qquad x, a, b > 0$$

	General							Exa	ample: ($\overline{\text{Gamma}(2,2)}$		
Transformation	PDF	PDF	CDF	$_{ m HF}$	IDF	μ	σ^2	MF	MGF	HF Shape	Support	Comment
x^2	√	√	√	√	√	√	√	√	∂	IFR	$0, \infty$	
\sqrt{x}	✓	✓	\checkmark	\checkmark	∂	\checkmark	\checkmark	\checkmark	\checkmark	$_{ m IFR}$	$0, \infty$	
x^{-1}	✓	\checkmark	\checkmark	\checkmark		\checkmark	\checkmark	\checkmark	\checkmark	$_{ m UBT}$	$0, \infty$	
$\arctan(x)$	✓	\checkmark	∂	∂		∂	∂	∂	∂	$_{ m UBT}$	$0, \pi/2$	
e^x	✓	\checkmark	\checkmark	\checkmark		\checkmark	\checkmark	\checkmark	∂	$_{ m UBT}$	$1, \infty$	
$\ln(x)$	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	∂		$-\infty, \infty$	
e^{-x}	✓	\checkmark	\checkmark	\checkmark		\checkmark	\checkmark	\checkmark	∂	$_{ m IFR}$	0, 1	
$-\ln(x)$	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	∂	$_{ m IFR}$	$-\infty, \infty$	
$\ln(x+1)$	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	∂		$0, \infty$	
$1/\ln(x+2)$	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	∂	$_{ m IFR}$	$0, 1/\ln(2)$	
$\tanh(x)$	✓	\checkmark	∂	∂	∂	∂	∂	∂	∂	$_{ m IFR}$	0, 1	
$\sinh(x)$	✓	\checkmark	\checkmark	\checkmark		∂	∂	∂	∂	UBT	$0, \infty$	
$\operatorname{arcsinh}(x)$	✓	\checkmark	\checkmark	\checkmark		∂	∂	∂	∂		$0, \infty$	
$\operatorname{csch}(x+1)$	✓	\checkmark	∂	∂		∂	∂	∂	∂	$_{ m IFR}$	$0, 2/(-e + e^{-1})$	
$\operatorname{arccsch}(x+1)$	✓	\checkmark	∂	∂		∂	∂	∂	∂		$0, \ln(1 + \sqrt{2})$	
$1/\tanh(x+1)$	✓	\checkmark	∂	∂		∂	∂	∂	∂	$_{ m UBT}$	$1, (e + e^{-1})/(e - e^{-1})$	Bimodal HF
$1/\sinh(x+1)$	✓	\checkmark	\checkmark	\checkmark		∂	∂	∂	∂	$_{ m IFR}$	$2,2/(e-e^{-1})$	
$1/\operatorname{arcsinh}(x+1)$	✓	✓									$0, 1/\ln(1+\sqrt{2})$	
$1/\operatorname{csch}(x) + 1$	✓	✓	∂	∂		∂	∂	∂	∂	UBT	$1, \infty$	
$\tanh(x^{-1})$	✓	✓	∂	∂		∂	∂	∂	∂	$_{ m IFR}$	0, 1	
$\operatorname{csch}(x^{-1})$	✓	✓	∂	∂		∂	∂	∂	∂		$1, \infty$	
$\operatorname{arccsch}(x^{-1})$	✓	✓	∂	∂		∂	∂	∂	∂		$0,\infty$	

Legend

Symbol	Meaning
\checkmark	Exists, Closed Form
∂	Exists, Not Closed Form
Ø	Not Possible
	Not Calculated

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