Lomax Distribution

$$f(x) = \frac{k}{\lambda} (\frac{x}{\lambda})^{k-1} e^{-\frac{x}{\lambda}k}$$

	General	Example: Lomax(1,2)										
Transformation	PDF	PDF	CDF	$_{ m HF}$	IDF	μ	σ^2	MF	MGF	HF Shape	Support	Comment
x^2	✓	√	✓	√	✓	∞	U	√	√	DFR	$0, \infty$	
\sqrt{x}	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	∞	\checkmark	\checkmark	UBT	$0, \infty$	
x^{-1}	✓	✓	\checkmark	\checkmark	\checkmark	∞	U	\checkmark	\checkmark	DFR	$0, \infty$	
$\arctan(x)$	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	∂	∂	BT	$0, \frac{1}{2}\pi$	
e^x	✓	✓	\checkmark	\checkmark	\checkmark	∞	U	∞	∂	DFR	$1, \infty$	
ln(x)	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	∂	∂	$_{ m IFR}$	$-\infty, \infty$	
e^{-x}	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	∂	∂	BT	0, 1	
$-\ln(x)$	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	∂	∂	$_{ m IFR}$	$-\infty, \infty$	
$\ln(x+1)$	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	∂	∂	DFR	$0, \infty$	
$1/\ln(x+2)$	✓	✓	\checkmark	\checkmark		∂	∂	∂	∂	$_{ m IFR}$	$0, \frac{1}{\ln(2)}$	
tanh(x)	✓	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	BT	0, 1	
$\sinh(x)$	✓	✓	\checkmark	\checkmark	\checkmark	∞	U	∞	∂	DFR	$0, \infty$	
$\operatorname{arcsinh}(x)$	✓	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	∂	∂	BT	$0, \infty$	
$\operatorname{csch}(x+1)$	✓	✓	∂	∂		∂	∂	∂	∂		$0, \frac{2}{e-e^{-1}}$	
$\operatorname{arccsch}(x+1)$	✓	✓	U	U		\checkmark	\checkmark	∂	∂	IFR	$0, \ln(1 + \sqrt{2})$	
$1/\tanh(x+1)$	✓	✓	?	\checkmark	\checkmark	∂	∂	∂	∂	BT	$1, \frac{e+e^{-1}}{e-e^{-1}} \\ 0, \frac{2}{e-e^{-1}}$	
$1/\sinh(x+1)$	✓	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	BT	$0, \frac{2}{e-e^{-1}}$	
$1/\operatorname{arcsinh}(x+1)$	✓	✓	U	U		∂	∂	∂	∂	IFR	$0, \frac{1}{\ln(1+\sqrt{2})}$	
$1/\operatorname{csch}(x) + 1$	✓	✓	∂	∂		∞	U	∞	∂	DFR	$1, \infty$	
$\tanh(x^{-1})$	✓	✓	\checkmark	\checkmark	\checkmark	∂	∂	∂	∂	$_{ m IFR}$	0, 1	
$\operatorname{csch}(x^{-1})$	✓	✓	∂	∂		∞	U	∂	∂		$0, \infty$	
$\operatorname{arccsch}(x^{-1})$	✓	✓	\checkmark	✓	\checkmark	\checkmark	\checkmark	∂	∂	UBT	$0, \infty$	

Legend

Symbol	Meaning
√	Exists, Closed Form
∂	Exists, Not Closed Form
Ø	Not Possible
	Not Calculated