

"HyperExponentialRV([1/2,1/2],[3,4])"

$$[x \mapsto 3/2 e^{-3x} + 2 e^{-4x}]$$

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$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = 1/4 \frac{e^{-3\sqrt{x}} (4e^{-\sqrt{x}} + 3)}{\sqrt{x}}$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( 2e^{4\sqrt{x}} - e^{\sqrt{x}} - 1 \right) e^{-4\sqrt{x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto (\ln(\text{RootOf}(1 + (2s - 2)Z^4 + Z)))^2]$$

Survivor Function

$$S(x) = 1/2 e^{-3\sqrt{x}} + 1/2 e^{-4\sqrt{x}}$$

Hazard Function

$$h(x) = 1/2 \frac{4e^{-\sqrt{x}} + 3}{\sqrt{x}(e^{-\sqrt{x}} + 1)}$$

Mean

$$\mu = \frac{25}{144}$$

Variance

$$\sigma^2 = \frac{3419}{20736}$$

Moment Function

$$m(x) = 2^{-1-4r} \Gamma(1+2r) + 1/2 3^{-2r} \Gamma(1+2r)$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} -1/4 \frac{\sqrt{\pi}}{\sqrt{-t}} e^{-4t^{-1}} \left( 4 \operatorname{erf} \left( \frac{t\sqrt{x} - 2}{\sqrt{-t}} \right) + 3 \operatorname{erf} \left( 1/2 \frac{2t\sqrt{x} - 3}{\sqrt{-t}} \right) e^{7/4 t^{-1}} + 3 e^{7/4 t^{-1}} \operatorname{erf} \left( 3/2 \frac{1}{\sqrt{-t}} \right) \right)$$

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$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x) = e^{-3x^2} \left( 3 + 4e^{-x^2} \right) x$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( 2e^{4x^2} - e^{x^2} - 1 \right) e^{-4x^2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \sqrt{\ln \left( RootOf \left( 1 + (2s - 2) \_Z^4 + \_Z \right) \right)}]$$

Survivor Function

$$S(x) = 1/2 \left( e^{x^2} + 1 \right) e^{-4x^2}$$

Hazard Function

$$h(x) = 2 \frac{\left( 3e^{x^2} + 4 \right) x}{e^{x^2} + 1}$$

Mean

$$\mu = 1/12 \sqrt{3} \sqrt{\pi} + 1/8 \sqrt{\pi}$$

Variance

$$\sigma^2 = \frac{7}{24} - \frac{7\pi}{192} - 1/48 \sqrt{3}\pi$$

Moment Function

$$m(x) = 1/2 3^{-r/2} \Gamma(1 + r/2) + 2^{-1-r} \Gamma(1 + r/2)$$

Moment Generating Function

$$1 + 1/12 t \sqrt{\pi} e^{1/12 t^2} \sqrt{3} \operatorname{erf} \left( 1/6 t \sqrt{3} \right) + 1/8 t \sqrt{\pi} e^{1/16 t^2} \operatorname{erf} (t/4) + 1/12 t \sqrt{\pi} e^{1/12 t^2} \sqrt{3} + 1/8 t \sqrt{\pi} e^{1/16 t^2}$$


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$$t \mapsto t^{-1}$$

Probability Distribution Function

$$f(x) = 1/2 \frac{1}{x^2} e^{-3x^{-1}} \left( 3 + 4 e^{-x^{-1}} \right)$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( e^{x^{-1}} + 1 \right) e^{-4x^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto (\ln (\text{RootOf} (2 s Z^4 - Z - 1)))^{-1}]$$

Survivor Function

$$S(x) = 1/2 \left( 2 e^{4x^{-1}} - e^{x^{-1}} - 1 \right) e^{-4x^{-1}}$$

Hazard Function

$$h(x) = \frac{3 e^{x^{-1}} + 4}{x^2} \left( 2 e^{4x^{-1}} - e^{x^{-1}} - 1 \right)^{-1}$$

Mean

$$\mu = \infty$$

Variance

$$\sigma^2 = \text{undefined}$$

Moment Function

$$m(x) = 1/2 3^r \Gamma(1-r) + 2^{-1+2r} \Gamma(1-r)$$

Moment Generating Function

$$\left( \sqrt{3} K_1 \left( 2 \sqrt{-t} \sqrt{3} \right) + 2 K_1 \left( 4 \sqrt{-t} \right) \right) \sqrt{-t_1}$$

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$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = 1/2 e^{-3 \tan(x)} \left( 3 + 4 e^{-\tan(x)} \right) \left( 1 + (\tan(x))^2 \right)$$

Cumulative Distribution Function

$$F(x) = \begin{cases} 1/2 \left( 2 e^{4 \tan(x)} - e^{\tan(x)} - 1 \right) e^{-4 \tan(x)} & x \leq \pi/2 \\ \infty & \pi/2 < x \end{cases}$$

Inverse Cumulative Distribution Function

$$F^{-1} = []$$

Survivor Function

$$S(x) = \begin{cases} 1/2 \left( e^{\tan(x)} + 1 \right) e^{-4 \tan(x)} & x \leq \pi/2 \\ -\infty & \pi/2 < x \end{cases}$$

Hazard Function

$$h(x) = \begin{cases} \frac{(3 e^{\tan(x)} + 4)(1 + (\tan(x))^2)}{e^{\tan(x)} + 1} & x \leq \pi/2 \\ 0 & \pi/2 < x \end{cases}$$

Mean

$$\mu = 1/2 \int_0^{\pi/2} \frac{x}{(\cos(x))^2} e^{-3 \frac{\sin(x)}{\cos(x)}} \left( 3 + 4 e^{-\frac{\sin(x)}{\cos(x)}} \right) dx$$

Variance

$$\sigma^2 = 1/2 \int_0^{\pi/2} \frac{x^2}{(\cos(x))^2} e^{-3 \frac{\sin(x)}{\cos(x)}} \left( 3 + 4 e^{-\frac{\sin(x)}{\cos(x)}} \right) dx - 1/4 \left( \int_0^{\pi/2} \frac{x}{(\cos(x))^2} e^{-3 \frac{\sin(x)}{\cos(x)}} \left( 3 + 4 e^{-\frac{\sin(x)}{\cos(x)}} \right) dx \right)^2$$

Moment Function

$$m(x) = \int_0^{\pi/2} 1/2 x^r e^{-3 \tan(x)} \left( 3 + 4 e^{-\tan(x)} \right) (1 + (\tan(x))^2) dx$$

Moment Generating Function

$$1/2 \int_0^{\pi/2} \frac{1}{(\cos(x))^2} \left( 4 e^{-\frac{-tx \cos(x) + 4 \sin(x)}{\cos(x)}} + 3 e^{-\frac{-tx \cos(x) + 3 \sin(x)}{\cos(x)}} \right) dx_1$$

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$$t \mapsto e^t$$

Probability Distribution Function

$$f(x) = 1/2 \frac{3x + 4}{x^5}$$

Cumulative Distribution Function

$$F(x) = 1/2 \frac{2x^4 - x - 1}{x^4}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf} \left( (1 + (2s - 2)Z^4 + Z) \right)]$$

Survivor Function

$$S(x) = 1/2 \frac{x + 1}{x^4}$$

Hazard Function

$$h(x) = \frac{3x + 4}{x(x + 1)}$$

Mean

$$\mu = \frac{17}{12}$$

Variance

$$\sigma^2 = \frac{71}{144}$$

Moment Function

$$m(x) = \lim_{x \rightarrow \infty} 1/2 \frac{3x^{r-4}rx + 4rx^{r-4} - 12x^{r-4}x - 12x^{r-4} - 7r + 24}{(-3 + r)(r - 4)}$$

Moment Generating Function

$$\lim_{x \rightarrow \infty} 1/12 \frac{-Ei(1, -tx)t^4x^4 + Ei(1, -t)t^4x^4 + e^t t^3 x^4 - 3Ei(1, -tx)t^3x^4 + 3Ei(1, -t)t^3x^4 + 4e^t t^2 x^4 - 3Ei(1, -tx)t^2x^4 + 3Ei(1, -t)t^2x^4 + 4e^t t x^4 - 3Ei(1, -tx)t x^4 + 3Ei(1, -t)t x^4 + 4e^t x^4 - 3Ei(1, -tx)x^4 + 3Ei(1, -t)x^4 + 4e^t - 3Ei(1, -tx) + 3Ei(1, -t)}{1}$$


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$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = 1/2 e^{-3e^x+x} (3 + 4e^{-e^x})$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( 2 e^{4e^x} - e^{e^x} - 1 \right) e^{-4e^x}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [ln^{(2)} \circ s \mapsto RootOf \left( 1 + (2 s - 2) _Z^4 + _Z \right)]$$

Survivor Function

$$S(x) = 1/2 \left( e^{e^x} + 1 \right) e^{-4e^x}$$

Hazard Function

$$h(x) = \frac{\left( 3 e^{e^x} + 4 \right) e^x}{e^{e^x} + 1}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 1/2 x e^{-3e^x+x} \left( 3 + 4 e^{-e^x} \right) dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 1/2 x^2 e^{-3e^x+x} \left( 3 + 4 e^{-e^x} \right) dx - \left( \int_{-\infty}^{\infty} 1/2 x e^{-3e^x+x} \left( 3 + 4 e^{-e^x} \right) dx \right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 1/2 x^r e^{-3e^x+x} \left( 3 + 4 e^{-e^x} \right) dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 1/2 \left( 3 + 4 e^{-e^x} \right) e^{tx-3e^x+x} dx_1$$

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$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = 1/2 x^2 \left( 3 + 4 x \right)$$

Cumulative Distribution Function

$$F(x) = 1/2 x^4 + 1/2 x^3$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf}(-Z^4 + Z^3 - 2s)]$$

Survivor Function

$$S(x) = 1 - 1/2 x^4 - 1/2 x^3$$

Hazard Function

$$h(x) = -\frac{x^2(3 + 4x)}{x^4 + x^3 - 2}$$

Mean

$$\mu = \frac{31}{40}$$

Variance

$$\sigma^2 = \frac{157}{4800}$$

Moment Function

$$m(x) = 1/2 \frac{7r + 24}{r^2 + 7r + 12}$$

Moment Generating Function

$$1/2 \frac{7e^t t^3 - 18e^t t^2 + 30e^t t - 24e^t - 6t + 24}{t^4} \quad 1$$


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$$t \mapsto -\ln(t)$$

Probability Distribution Function

$$f(x) = 1/2 e^{-3e^{-x}-x} \left(3 + 4e^{-e^{-x}}\right)$$

Cumulative Distribution Function

$$F(x) = 1/2 \left(e^{e^{-x}} + 1\right) e^{-4e^{-x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln(\ln(\text{RootOf}(2sZ^4 - Z - 1)))]$$

Survivor Function

$$S(x) = 1/2 \left(2e^{4e^{-x}} - e^{e^{-x}} - 1\right) e^{-4e^{-x}}$$

Hazard Function

$$h(x) = \frac{\left(3e^{e^{-x}} + 4\right)e^{-x}}{2e^{4e^{-x}} - e^{e^{-x}} - 1}$$

Mean

$$\mu = \int_{-\infty}^{\infty} 1/2 x e^{-3e^{-x}-x} \left(3 + 4e^{-e^{-x}}\right) dx$$

Variance

$$\sigma^2 = \int_{-\infty}^{\infty} 1/2 x^2 e^{-3e^{-x}-x} \left(3 + 4e^{-e^{-x}}\right) dx - \left(\int_{-\infty}^{\infty} 1/2 x e^{-3e^{-x}-x} \left(3 + 4e^{-e^{-x}}\right) dx\right)^2$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 1/2 x^r e^{-3e^{-x}-x} \left(3 + 4e^{-e^{-x}}\right) dx$$

Moment Generating Function

$$\int_{-\infty}^{\infty} 1/2 \left(3 + 4e^{-e^{-x}}\right) e^{tx-3e^{-x}-x} dx_1$$


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$$t \mapsto \ln(t+1)$$

Probability Distribution Function

$$f(x) = 1/2 \left(3e^{-3e^x+3} + 4e^{-4e^x+4}\right)e^x$$

Cumulative Distribution Function

$$F(x) = 1 - 1/2 e^{-3e^x+3} - 1/2 e^{-4e^x+4}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \ln(1 - \ln(\text{RootOf}(-Z^4 + -Z^3 + 2s - 2)))]$$

Survivor Function

$$S(x) = 1/2 e^{-3e^x+3} + 1/2 e^{-4e^x+4}$$



Hazard Function

$$h(x) = \frac{(3e^{-3e^x+3} + 4e^{-4e^x+4})e^x}{e^{-3e^x+3} + e^{-4e^x+4}}$$

Mean

$$\mu = \int_0^\infty 1/2 x (3e^{-3e^x+3} + 4e^{-4e^x+4}) e^x dx$$

Variance

$$\sigma^2 = \int_0^\infty 1/2 x^2 (3e^{-3e^x+3} + 4e^{-4e^x+4}) e^x dx - \left( \int_0^\infty 1/2 x (3e^{-3e^x+3} + 4e^{-4e^x+4}) e^x dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 1/2 x^r (3e^{-3e^x+3} + 4e^{-4e^x+4}) e^x dx$$

Moment Generating Function

$$\int_0^\infty 1/2 (3e^{-3e^x+3} + 4e^{-4e^x+4}) e^{x(t+1)} dx_1$$

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$$t \mapsto (\ln(t+2))^{-1}$$

Probability Distribution Function

$$f(x) = 1/2 \frac{(3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8})e^{x^{-1}}}{x^2}$$

Cumulative Distribution Function

$$F(x) = 1/2 (e^{6+e^{x^{-1}}} + e^8) e^{-4e^{x^{-1}}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto (\ln(2 + \ln(\text{RootOf}(2s_Z^4 - _Z - 1))))^{-1}]$$

Survivor Function

$$S(x) = 1 - 1/2 e^{-3e^{x^{-1}}+6} - 1/2 e^{-4e^{x^{-1}}+8}$$

Hazard Function

$$h(x) = -\frac{\left(3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8}\right)e^{x^{-1}}}{x^2\left(-2 + e^{-3e^{x^{-1}}+6} + e^{-4e^{x^{-1}}+8}\right)}$$

Mean

$$\mu = 1/2 \int_0^{(\ln(2))^{-1}} \frac{\left(3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8}\right)e^{x^{-1}}}{x} dx$$

Variance

$$\sigma^2 = 1/2 \int_0^{(\ln(2))^{-1}} \left(3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8}\right)e^{x^{-1}} dx - 1/4 \left( \int_0^{(\ln(2))^{-1}} \frac{\left(3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8}\right)e^{x^{-1}}}{x} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} \frac{x^r \left(3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8}\right)e^{x^{-1}}}{1/2 x^2} dx$$

Moment Generating Function

$$1/2 \int_0^{(\ln(2))^{-1}} \frac{3e^{-3e^{x^{-1}}+6} + 4e^{-4e^{x^{-1}}+8}}{x^2} e^{\frac{tx^2+1}{x}} dx_1$$


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$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = 1/2 \frac{-4x + 3\sqrt{-x^2+1} + 4}{(x+1)^3}$$

Cumulative Distribution Function

$$F(x) = 1/2 \frac{x^2 + x\sqrt{-x^2+1} + 6x - \sqrt{-x^2+1} + 1}{x^2 + 2x + 1}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf}((2s^2 - 2s + 1)Z^4 + (8s^2 - 16s + 5)Z^3 + (12s^2 - 28s + 19)Z^2 + (8s^2 - 16s + 5)Z + 2)]$$

Survivor Function

$$S(x) = -1/2 \frac{x\sqrt{-x^2+1} - x^2 - \sqrt{-x^2+1} + 2x - 1}{x^2 + 2x + 1}$$

Hazard Function

$$h(x) = -\frac{-4x + 3\sqrt{-x^2+1} + 4}{(x\sqrt{-x^2+1} - x^2 - \sqrt{-x^2+1} + 2x - 1)(x+1)}$$

Mean

$$\mu = 4 - 3/4\pi - 2\ln(2)$$

Variance

$$\sigma^2 = -\frac{25}{2} + 9/4\pi + 8\ln(2) - (4 - 3/4\pi - 2\ln(2))^2$$

Moment Function

$$m(x) = -r+1/2-r(r+1)\text{LerchPhi}(-1,1,-r)-\pi\csc(\pi r)r(r+1)+3/4\frac{1}{\sqrt{\pi}}\left(1/2\frac{\pi\Gamma(r/2+1)}{\Gamma(r/2+1)}\right)$$

Moment Generating Function

$$1/2 \int_0^1 \frac{e^{tx}(-4x + 3\sqrt{-x^2+1} + 4)}{(x+1)^3} dx_1$$

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$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = 1/2 \frac{3x + 3\sqrt{x^2+1} + 4}{(x + \sqrt{x^2+1})^4 \sqrt{x^2+1}}$$

Cumulative Distribution Function

$$F(x) = 1/2-2\sqrt{x^2+1}x^2-1/2\sqrt{x^2+1}+2x^3+3/2x+4\sqrt{x^2+1}x^3+2\sqrt{x^2+1}x-4x^4-4x^2$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf}((16s - 16)Z^4 + (-8s + 8)Z^3 + (16s - 16)Z^2 + (-6s + 7)Z + 2s^2 - 1)]$$

Survivor Function

$$S(x) = 1/2 + 2\sqrt{x^2 + 1}x^2 + 1/2\sqrt{x^2 + 1} - 2x^3 - 3/2x - 4\sqrt{x^2 + 1}x^3 - 2\sqrt{x^2 + 1}x + 4x^4 + 4x^2$$

Hazard Function

$$h(x) = -\frac{3x + 3\sqrt{x^2 + 1} + 4}{(x + \sqrt{x^2 + 1})^4 \sqrt{x^2 + 1} (8\sqrt{x^2 + 1}x^3 - 8x^4 - 4\sqrt{x^2 + 1}x^2 + 4x^3 + 4\sqrt{x^2 + 1}x - 8x^2)}$$

Mean

$$\mu = 1/16 \frac{3\pi + 32 G_{3,3}^{2,3} \left( 1 \middle| \begin{smallmatrix} -2, -3/2, -1 \\ -1/2, -3/2, -9/2 \end{smallmatrix} \right)}{\pi}$$

Variance

$$\sigma^2 = \frac{1}{\pi} \left( 3/2 G_{3,3}^{2,3} \left( 1 \middle| \begin{smallmatrix} -2, -3/2, 0 \\ -1/2, -1/2, -9/2 \end{smallmatrix} \right) + \frac{83\pi}{420} \right) - \frac{\left( 3\pi + 32 G_{3,3}^{2,3} \left( 1 \middle| \begin{smallmatrix} -2, -3/2, -1 \\ -1/2, -3/2, -9/2 \end{smallmatrix} \right) \right)^2}{256\pi^2}$$

Moment Function

$$m(x) = 3/2 \frac{1}{\pi} \left( -2\sqrt{\pi} \Gamma(3/2 + r/2) \Gamma(-1 - r/2) {}_3F_2(-3/2, 5/2, 3/2 + r/2; 3/2, 2 + r/2; 1) - 1 \right)$$

Moment Generating Function

$$\int_0^\infty 1/2 \frac{e^{tx} (3x + 3\sqrt{x^2 + 1} + 4)}{(x + \sqrt{x^2 + 1})^4 \sqrt{x^2 + 1}} dx_1$$

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$$t \mapsto \operatorname{arcsinh}(t)$$

Probability Distribution Function

$$f(x) = 1/2 e^{-3 \sinh(x)} (4 e^{-\sinh(x)} + 3) \cosh(x)$$

Cumulative Distribution Function

$$F(x) = -1/2 e^{-3/2 (e^{2x} - 1)e^{-x}} + 1 - 1/2 e^{-2 (e^{2x} - 1)e^{-x}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto -\ln \left( \ln \left( \operatorname{RootOf} \left( -Z^4 + -Z^3 + 2s - 2 \right) \right) + \sqrt{\left( \ln \left( \operatorname{RootOf} \left( -Z^4 + -Z^3 + 2s - 2 \right) \right) \right)^2} \right)]$$

Survivor Function

$$S(x) = 1/2 e^{-3/2 (e^2 x - 1) e^{-x}} + 1/2 e^{-2 (e^2 x - 1) e^{-x}}$$

Hazard Function

$$h(x) = \frac{e^{-3 \sinh(x)} (4 e^{-\sinh(x)} + 3) \cosh(x)}{e^{-3/2 (e^2 x - 1) e^{-x}} + e^{-2 (e^2 x - 1) e^{-x}}}$$

Mean

$$\mu = \int_0^\infty 1/2 x e^{-3 \sinh(x)} (4 e^{-\sinh(x)} + 3) \cosh(x) dx$$

Variance

$$\sigma^2 = \int_0^\infty 1/2 x^2 e^{-3 \sinh(x)} (4 e^{-\sinh(x)} + 3) \cosh(x) dx - \left( \int_0^\infty 1/2 x e^{-3 \sinh(x)} (4 e^{-\sinh(x)} + 3) \cosh(x) dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 1/2 x^r e^{-3 \sinh(x)} (4 e^{-\sinh(x)} + 3) \cosh(x) dx$$

Moment Generating Function

$$\int_0^\infty 1/2 (4 e^{-\sinh(x)} + 3) \cosh(x) e^{tx-3 \sinh(x)} dx_1$$

$$t \mapsto \operatorname{csch}(t+1)$$

Probability Distribution Function

$$f(x) = 1/2 \frac{3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)}}{\sqrt{x^2+1} |x|}$$

Cumulative Distribution Function

$$F(x) = 1/2 \int_0^x \frac{3 e^{3-3 \operatorname{arccsch}(t)} + 4 e^{4-4 \operatorname{arccsch}(t)}}{\sqrt{t^2+1} |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 1/2 \int_0^x \frac{3 e^{3-3 \operatorname{arccsch}(t)} + 4 e^{4-4 \operatorname{arccsch}(t)}}{\sqrt{t^2 + 1} |t|} dt$$

Hazard Function

$$h(x) = -\frac{3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1} |x|} \left( -2 + \int_0^x \frac{3 e^{3-3 \operatorname{arccsch}(t)} + 4 e^{4-4 \operatorname{arccsch}(t)}}{\sqrt{t^2 + 1} |t|} dt \right)^{-1}$$

Mean

$$\mu = 1/2 \int_0^{2 \frac{e}{e^2-1}} \frac{3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1}} dx$$

Variance

$$\sigma^2 = 1/2 \int_0^{2 \frac{e}{e^2-1}} x \frac{(3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)})}{\sqrt{x^2 + 1}} dx - 1/4 \left( \int_0^{2 \frac{e}{e^2-1}} \frac{3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)}}{\sqrt{x^2 + 1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2 \frac{e}{e^2-1}} \frac{x^r (3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)})}{\sqrt{x^2 + 1} |x|} dx$$

Moment Generating Function

$$1/2 \int_0^{2 \frac{e}{e^2-1}} \frac{e^{tx} (3 e^{3-3 \operatorname{arccsch}(x)} + 4 e^{4-4 \operatorname{arccsch}(x)})}{\sqrt{x^2 + 1} x} dx$$

$$t \mapsto \operatorname{arccsch}(t + 1)$$

Probability Distribution Function

$$f(x) = 1/2 \frac{\cosh(x)}{(\sinh(x))^2} e^{3 \frac{\sinh(x)-1}{\sinh(x)}} \left( 4 e^{\frac{\sinh(x)-1}{\sinh(x)}} + 3 \right)$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( e^{\frac{2e^x+1}{e^{2x}-1}} + e^{\frac{e^{2x}}{e^{2x}-1}} \right) e^{\frac{3e^{2x}-8e^x-4}{e^{2x}-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 1/2 e^{3 \frac{e^2 x - 2 e^x - 1}{e^2 x - 1}} - 1/2 e^{4 \frac{e^2 x - 2 e^x - 1}{e^2 x - 1}}$$

Hazard Function

$$h(x) = -\frac{\cosh(x)}{(\sinh(x))^2} e^{3 \frac{\sinh(x)-1}{\sinh(x)}} \left( 4 e^{\frac{\sinh(x)-1}{\sinh(x)}} + 3 \right) \left( -2 + e^{-3 \frac{-e^2 x + 2 e^x + 1}{e^2 x - 1}} + e^{-4 \frac{-e^2 x + 2 e^x + 1}{e^2 x - 1}} \right)^{-1}$$

Mean

$$\mu = \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) x}{-1 + \cosh(2x)} e^{3 \frac{\sinh(x)-1}{\sinh(x)}} \left( 4 e^{\frac{\sinh(x)-1}{\sinh(x)}} + 3 \right) dx$$

Variance

$$\sigma^2 = \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) x^2}{-1 + \cosh(2x)} e^{3 \frac{\sinh(x)-1}{\sinh(x)}} \left( 4 e^{\frac{\sinh(x)-1}{\sinh(x)}} + 3 \right) dx - \left( \int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x) x}{-1 + \cosh(2x)} e^{3 \frac{\sinh(x)-1}{\sinh(x)}} \right)^2$$

Moment Function

$$m(x) = \int_0^{\ln(1+\sqrt{2})} 1/2 \frac{x^r \cosh(x)}{(\sinh(x))^2} e^{3 \frac{\sinh(x)-1}{\sinh(x)}} \left( 4 e^{\frac{\sinh(x)-1}{\sinh(x)}} + 3 \right) dx$$

Moment Generating Function

$$\int_0^{\ln(1+\sqrt{2})} \frac{\cosh(x)}{-1 + \cosh(2x)} \left( 4 e^{\frac{tx \sinh(x) + 4 \sinh(x) - 4}{\sinh(x)}} + 3 e^{\frac{tx \sinh(x) + 3 \sinh(x) - 3}{\sinh(x)}} \right) dx_1$$


---

$$t \mapsto (\tanh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 1/2 \frac{3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})}}{x^2 - 1}$$

Cumulative Distribution Function

$$F(x) = 1/2 \int_1^x \frac{3 e^{3-3 \operatorname{arctanh}(t^{-1})} + 4 e^{4-4 \operatorname{arctanh}(t^{-1})}}{t^2 - 1} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1 - 1/2 \int_1^x \frac{3 e^{3-3 \operatorname{arctanh}(t^{-1})} + 4 e^{4-4 \operatorname{arctanh}(t^{-1})}}{t^2 - 1} dt$$

Hazard Function

$$h(x) = -\frac{3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})}}{x^2 - 1} \left( -2 + \int_1^x \frac{3 e^{3-3 \operatorname{arctanh}(t^{-1})} + 4 e^{4-4 \operatorname{arctanh}(t^{-1})}}{t^2 - 1} dt \right)$$

Mean

$$\mu = 1/2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x \left( 3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})} \right)}{x^2 - 1} dx$$

Variance

$$\sigma^2 = 1/2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^2 \left( 3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})} \right)}{x^2 - 1} dx - 1/4 \left( \int_1^{\frac{e^2+1}{e^2-1}} \frac{x \left( 3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})} \right)}{x^2 - 1} dx \right)^2$$

Moment Function

$$m(x) = \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^r \left( 3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})} \right)}{x^2 - 1} dx$$

Moment Generating Function

$$1/2 \int_1^{\frac{e^2+1}{e^2-1}} \frac{e^{tx} \left( 3 e^{3-3 \operatorname{arctanh}(x^{-1})} + 4 e^{4-4 \operatorname{arctanh}(x^{-1})} \right)}{x^2 - 1} dx$$



---


$$t \mapsto (\sinh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 1/2 \frac{3e^{3-3\operatorname{arcsinh}(x^{-1})} + 4e^{4-4\operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}|x|}$$

Cumulative Distribution Function

$$F(x) = 1/2 \frac{e^3 x^3 (ex + \sqrt{x^2+1} + 1)}{x^4 + 8x^2 + 8 + 4\sqrt{x^2+1}x^2 + 8\sqrt{x^2+1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \operatorname{RootOf}((e^8 - 4e^4s - e^6 + 4s^2)Z^4 + (2e^7 + 12e^3s)Z^3 - 32e^4sZ^2 + 16e^3sZ - 16e^2s^2)]$$

Survivor Function

$$S(x) = -1/2 \frac{e^4 x^4 + \sqrt{x^2+1}e^3 x^3 + e^3 x^3 - 2x^4 - 8\sqrt{x^2+1}x^2 - 16x^2 - 16\sqrt{x^2+1} - 16}{x^4 + 8x^2 + 8 + 4\sqrt{x^2+1}x^2 + 8\sqrt{x^2+1}}$$

Hazard Function

$$h(x) = -\frac{(3e^{3-3\operatorname{arcsinh}(x^{-1})} + 4e^{4-4\operatorname{arcsinh}(x^{-1})})(x^4 + 8x^2 + 8 + 4\sqrt{x^2+1}x^2 + 8\sqrt{x^2+1})}{\sqrt{x^2+1}|x|(e^4 x^4 + \sqrt{x^2+1}e^3 x^3 + e^3 x^3 - 2x^4 - 8\sqrt{x^2+1}x^2 - 16x^2 - 16\sqrt{x^2+1} - 16)}$$

Mean

$$\mu = 1/2 \int_0^{2\frac{e}{e^2-1}} \frac{3e^{3-3\operatorname{arcsinh}(x^{-1})} + 4e^{4-4\operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx$$

Variance

$$\sigma^2 = 1/2 \int_0^{2\frac{e}{e^2-1}} x \frac{(3e^{3-3\operatorname{arcsinh}(x^{-1})} + 4e^{4-4\operatorname{arcsinh}(x^{-1})})}{\sqrt{x^2+1}} dx - 1/4 \left( \int_0^{2\frac{e}{e^2-1}} \frac{3e^{3-3\operatorname{arcsinh}(x^{-1})} + 4e^{4-4\operatorname{arcsinh}(x^{-1})}}{\sqrt{x^2+1}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^{2(e-e^{-1})^{-1}} \frac{x^r (3e^{3-3\operatorname{arcsinh}(x^{-1})} + 4e^{4-4\operatorname{arcsinh}(x^{-1})})}{1/2 \sqrt{x^2+1}|x|} dx$$

Moment Generating Function

$$1/2 \int_0^{2 \frac{e}{e^2-1}} \frac{e^{tx} \left( 3 e^{3-3 \operatorname{arcsinh}(x^{-1})} + 4 e^{4-4 \operatorname{arcsinh}(x^{-1})} \right)}{\sqrt{x^2+1} x} dx_1$$


---

$$t \mapsto (\operatorname{arcsinh}(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 1/2 \frac{\left( 3 e^{3-3 \sinh(x^{-1})} + 4 e^{4-4 \sinh(x^{-1})} \right) \cosh(x^{-1})}{x^2}$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( e^{1/2 (4 e^{2 x^{-1}} + 6 e^{x^{-1}} + 3) e^{-x^{-1}}} + e^{1/2 (3 e^{2 x^{-1}} + 8 e^{x^{-1}} + 4) e^{-x^{-1}}} \right) e^{-7/2 e^{x^{-1}}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \left( \ln \left( \ln \left( \operatorname{RootOf} \left( 2 s Z^4 - Z - 1 \right) \right) + 1 + \sqrt{\left( \ln \left( \operatorname{RootOf} \left( 2 s Z^4 - Z - 1 \right) \right) \right)^2 + 2} \right)$$

Survivor Function

$$S(x) = 1 - 1/2 e^{3/2 (-e^{2 x^{-1}} + 2 e^{x^{-1}} + 1) e^{-x^{-1}}} - 1/2 e^{2 (-e^{2 x^{-1}} + 2 e^{x^{-1}} + 1) e^{-x^{-1}}}$$

Hazard Function

$$h(x) = - \frac{\left( 3 e^{3-3 \sinh(x^{-1})} + 4 e^{4-4 \sinh(x^{-1})} \right) \cosh(x^{-1})}{x^2} \left( -2 + e^{3/2 (-e^{2 x^{-1}} + 2 e^{x^{-1}} + 1) e^{-x^{-1}}} + e^{2 (-e^{2 x^{-1}} + 2 e^{x^{-1}} + 1) e^{-x^{-1}}} \right)$$


---

$$t \mapsto (\operatorname{csch}(t))^{-1} + 1$$

Probability Distribution Function

$$f(x) = 1/2 \frac{3 x + 1 + 3 \sqrt{x^2 - 2 x + 2}}{(x - 1 + \sqrt{x^2 - 2 x + 2})^4 \sqrt{x^2 - 2 x + 2}}$$

Cumulative Distribution Function

$$F(x) = -11 - 34x^2 + 18x^3 - 4x^4 + \frac{63x}{2} + 18\sqrt{x^2 - 2x + 2} - 17/2\sqrt{x^2 - 2x + 2} - 14\sqrt{x^2 - 2x + 2}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \text{RootOf}((16s - 16)Z^4 + (-72s + 72)Z^3 + (136s - 136)Z^2 + (-126s + 127)Z - 12)]$$

Survivor Function

$$S(x) = 12 + 34x^2 - 18x^3 + 4x^4 - \frac{63x}{2} - 18\sqrt{x^2 - 2x + 2} + 17/2\sqrt{x^2 - 2x + 2} + 14\sqrt{x^2 - 2x + 2}$$

Hazard Function

$$h(x) = -\frac{3x + 1 + 3\sqrt{x^2 - 2x + 2}}{(x - 1 + \sqrt{x^2 - 2x + 2})^4 \sqrt{x^2 - 2x + 2} (8\sqrt{x^2 - 2x + 2}x^3 - 8x^4 - 28\sqrt{x^2 - 2x + 2})}$$

Mean

$$\mu = \frac{317}{240}$$

Variance

$$\sigma^2 = \frac{10391}{57600}$$

Moment Function

$$m(x) = \int_1^\infty 1/2 \frac{x^r (3x + 1 + 3\sqrt{x^2 - 2x + 2})}{(x - 1 + \sqrt{x^2 - 2x + 2})^4 \sqrt{x^2 - 2x + 2}} dx$$

Moment Generating Function

$$\int_1^\infty 1/2 \frac{e^{tx} (3x + 1 + 3\sqrt{x^2 - 2x + 2})}{(x - 1 + \sqrt{x^2 - 2x + 2})^4 \sqrt{x^2 - 2x + 2}} dx_1$$

---


$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -1/2 \frac{1}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-3(\operatorname{arctanh}(x))^{-1}} \left( 3 + 4e^{-(\operatorname{arctanh}(x))^{-1}} \right)$$

Cumulative Distribution Function

$$F(x) = 1/2 \left( e^{2(\ln(x+1)-\ln(1-x))^{-1}} + 1 \right) e^{-8(\ln(x+1)-\ln(1-x))^{-1}}$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1 \left( e^{2(\ln(RootOf(2s-Z^4-Z-1)))^{-1}} - 1 \right) \left( e^{2(\ln(RootOf(2s-Z^4-Z-1)))^{-1}} + 1 \right)^{-1}]$$

Survivor Function

$$S(x) = 1/2 \left( 2e^{8(\ln(x+1)-\ln(1-x))^{-1}} - e^{2(\ln(x+1)-\ln(1-x))^{-1}} - 1 \right) e^{-8(\ln(x+1)-\ln(1-x))^{-1}}$$

Hazard Function

$$h(x) = -\frac{1}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{\frac{-3 \ln(x+1)+3 \ln(1-x)+8 \operatorname{arctanh}(x)}{\operatorname{arctanh}(x)(\ln(x+1)-\ln(1-x))}} \left( 3 + 4 e^{-(\operatorname{arctanh}(x))^{-1}} \right) \left( 2e^{8(\ln(x+1)-\ln(1-x))^{-1}} - e^{2(\ln(x+1)-\ln(1-x))^{-1}} - 1 \right)$$

Mean

$$\mu = -1/2 \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-3(\operatorname{arctanh}(x))^{-1}} \left( 3 + 4 e^{-(\operatorname{arctanh}(x))^{-1}} \right) dx$$

Variance

$$\sigma^2 = -1/2 \int_0^1 \frac{x^2}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-3(\operatorname{arctanh}(x))^{-1}} \left( 3 + 4 e^{-(\operatorname{arctanh}(x))^{-1}} \right) dx - 1/4 \left( \int_0^1 \frac{x}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-3(\operatorname{arctanh}(x))^{-1}} \left( 3 + 4 e^{-(\operatorname{arctanh}(x))^{-1}} \right) dx \right)^2$$

Moment Function

$$m(x) = \int_0^1 -1/2 \frac{x^r}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} e^{-3(\operatorname{arctanh}(x))^{-1}} \left( 3 + 4 e^{-(\operatorname{arctanh}(x))^{-1}} \right) dx$$

Moment Generating Function

$$-1/2 \int_0^1 \frac{1}{(\operatorname{arctanh}(x))^2 (x^2 - 1)} \left( 3 + 4 e^{-(\operatorname{arctanh}(x))^{-1}} \right) e^{\frac{tx \operatorname{arctanh}(x) - 3}{\operatorname{arctanh}(x)}} dx$$