

"LogNormalRV(1, 2)"

$$[x \mapsto 1/4 \frac{\sqrt{2}e^{-1/8 (\ln(x)-1)^2}}{\sqrt{\pi}x}]$$

$$t \mapsto t^2$$

Probability Distribution Function

$$f(x) = 1/8 \frac{\sqrt{2}e^{-1/32 (\ln(x)-2)^2}}{\sqrt{\pi}x}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/8 \sqrt{2} (\ln(x) - 2)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto e^{2+4 \sqrt{2} \operatorname{RootOf}(-\operatorname{erf}(-Z)-1+2 s)}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/8 \sqrt{2} (\ln(x) - 2)\right)$$

Hazard Function

$$h(x) = -1/4 \frac{\sqrt{2}e^{-1/32 (\ln(x)-2)^2}}{\sqrt{\pi}x (-1 + \operatorname{erf}(1/8 \sqrt{2} (\ln(x) - 2)))}$$

Mean

$$mu = e^{10}$$

Variance

$$sigma^2 = e^{36} - e^{20}$$

Moment Function

$$m(x) = e^{8r^2+2r}$$

Moment Generating Function

$$\int_0^\infty 1/8 \frac{\sqrt{2}e^{-1/8-1/32 (\ln(x))^2+tx}}{\sqrt{\pi}} x^{-\frac{7}{8}} dx_1$$

$$t \mapsto \sqrt{t}$$

Probability Distribution Function

$$f(x) = 1/2 \frac{\sqrt{2}e^{-1/8(\ln(x^2)-1)^2}}{\sqrt{\pi}x}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 \sqrt{2}(2 \ln(x) - 1)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto e^{1/2+\sqrt{2}\operatorname{RootOf}(-\operatorname{erf}(_Z)-1+2s)}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 \sqrt{2}(2 \ln(x) - 1)\right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2}e^{-1/8(\ln(x^2)-1)^2}}{\sqrt{\pi}x(-1 + \operatorname{erf}(1/4 \sqrt{2}(2 \ln(x) - 1)))}$$

Mean

$$\mu = e$$

Variance

$$\sigma^2 = e^3 - e^2$$

Moment Function

$$m(x) = \int_0^\infty 1/2 \frac{x^r \sqrt{2}e^{-1/8(\ln(x^2)-1)^2}}{\sqrt{\pi}x} dx$$

Moment Generating Function

$$\int_0^\infty 1/2 \frac{\sqrt{2}e^{-1/8-1/2(\ln(x))^2+tx}}{\sqrt{\pi}\sqrt{x}} dx_1$$

$$t \mapsto t^{-1}$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8(\ln(x^{-1})-1)^2}}{\sqrt{\pi}x}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(x) + 1)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto e^{-1+2\sqrt{2}\operatorname{RootOf}(-\operatorname{erf}(-Z)-1+2s)}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(x) + 1)\right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2}e^{-1/8(\ln(x^{-1})-1)^2}}{\sqrt{\pi}x(-1 + \operatorname{erf}(1/4 \sqrt{2} (\ln(x) + 1)))}$$

Mean

$$mu = e$$

Variance

$$sigma^2 = e^6 - e^2$$

Moment Function

$$m(x) = \int_0^\infty 1/4 \frac{x^r \sqrt{2}e^{-1/8(\ln(x^{-1})-1)^2}}{\sqrt{\pi}x} dx$$

Moment Generating Function

$$\int_0^\infty 1/4 \frac{\sqrt{2}e^{-1/8-1/8(\ln(x))^2+tx}}{\sqrt{\pi}x^{5/4}} dx_1$$

$$t \mapsto \arctan(t)$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8(\ln(\tan(x))-1)^2} (1 + (\tan(x))^2)}{\sqrt{\pi} \tan(x)}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(\tan(x)) - 1)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [\arctan \circ s \mapsto e^{1+2\sqrt{2}\operatorname{RootOf}(-\operatorname{erf}(-Z)-1+2s)}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(\tan(x)) - 1)\right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2}e^{-1/8(\ln(\tan(x))-1)^2} (1 + (\tan(x))^2)}{\sqrt{\pi} \tan(x) (-1 + \operatorname{erf}(1/4 \sqrt{2} (\ln(\tan(x)) - 1)))}$$

Mean

$$\mu = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\pi/2} \frac{e^{-1/8(\ln(\sin(x))-\ln(\cos(x))-1)^2} x}{\sin(x) \cos(x)} dx$$

Variance

$$\sigma^2 = 1/8 \frac{1}{\pi^{3/2}} \left(2 \sqrt{2} \int_0^{\pi/2} \frac{e^{-1/8(\ln(\sin(x))-\ln(\cos(x))-1)^2} x^2}{\sin(x) \cos(x)} dx \pi - \left(\int_0^{\pi/2} \frac{e^{-1/8(\ln(\sin(x))-\ln(\cos(x))-1)^2} x}{\sin(x) \cos(x)} dx \right)^2 \right)$$

Moment Function

$$m(x) = \int_0^{\pi/2} \frac{1}{4} \frac{x^r \sqrt{2} e^{-1/8(\ln(\tan(x))-1)^2} (1 + (\tan(x))^2)}{\sqrt{\pi} \tan(x)} dx$$

Moment Generating Function

$$1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\pi/2} \frac{(\cos(x))^{1/4 \ln(\sin(x)) - 5/4} e^{-1/8 + tx - 1/8 (\ln(\sin(x)))^2 - 1/8 (\ln(\cos(x)))^2}}{(\sin(x))^{3/4}} dx$$

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$$t \mapsto e^t$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2} e^{-1/8 (\ln(\ln(x)) - 1)^2}}{\sqrt{\pi} \ln(x) x}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(\ln(x)) - 1)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [\exp \circ s \mapsto e^{1+2 \sqrt{2} \operatorname{RootOf}(-\operatorname{erf}(-Z) - 1 + 2 s)}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(\ln(x)) - 1)\right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2} e^{-1/8 (\ln(\ln(x)) - 1)^2}}{\sqrt{\pi} \ln(x) x (-1 + \operatorname{erf}(1/4 \sqrt{2} (\ln(\ln(x)) - 1)))}$$

Mean

$$\mu = \infty$$

Variance

$$\sigma^2 = \text{undefined}$$

Moment Function

$$m(x) = \infty$$

Moment Generating Function

$$\int_1^\infty 1/4 \frac{\sqrt{2} e^{-1/8 - 1/8 (\ln(\ln(x)))^2 + tx}}{\sqrt{\pi} (\ln(x))^{3/4} x} dx$$

$$t \mapsto \ln(t)$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8(x-1)^2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 x \sqrt{2} - 1/4 \sqrt{2}\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 \left(\sqrt{2} + 4 \operatorname{RootOf}(-\operatorname{erf}(-Z) - 1 + 2s) \right) \sqrt{2}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 x \sqrt{2} - 1/4 \sqrt{2}\right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2}e^{-1/8(x-1)^2}}{\sqrt{\pi}(-1 + \operatorname{erf}(1/4 x \sqrt{2} - 1/4 \sqrt{2}))}$$

Mean

$$\mu = 1$$

Variance

$$\sigma^2 = 4$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 1/4 \frac{x^r \sqrt{2}e^{-1/8(x-1)^2}}{\sqrt{\pi}} dx$$

Moment Generating Function

$$e^{t(2t+1)}_1$$

$$t \mapsto e^{-t}$$

Probability Distribution Function

$$f(x) = -1/4 \frac{\sqrt{2}e^{-1/8 (\ln(-\ln(x))-1)^2}}{\sqrt{\pi} \ln(x) x}$$

Cumulative Distribution Function

$$F(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(-\ln(x)) - 1)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto e^{-e^{1+2 \sqrt{2} \operatorname{RootOf}(\operatorname{erf}(-Z)-1+2 s)}}]$$

Survivor Function

$$S(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 \sqrt{2} (\ln(-\ln(x)) - 1)\right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2}e^{-1/8 (\ln(-\ln(x))-1)^2}}{\sqrt{\pi} \ln(x) x (1 + \operatorname{erf}(1/4 \sqrt{2} (\ln(-\ln(x)) - 1)))}$$

Mean

$$\mu = -1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{e^{-1/8 (\ln(-\ln(x))-1)^2}}{\ln(x)} dx$$

Variance

$$\sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_0^1 \frac{e^{-1/8 (\ln(-\ln(x))-1)^2}}{\ln(x)} dx \right)^2 \sqrt{\pi} + 2 \sqrt{2} \int_0^1 \frac{x e^{-1/8 (\ln(-\ln(x))-1)^2}}{\ln(x)} dx \pi \right)$$

Moment Function

$$m(x) = \int_0^1 -1/4 \frac{x^r \sqrt{2} e^{-1/8 (\ln(-\ln(x))-1)^2}}{\sqrt{\pi} \ln(x) x} dx$$

Moment Generating Function

$$1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{e^{-1/8 - 1/8 (\ln(-\ln(x)))^2 + tx}}{x (-\ln(x))^{3/4}} dx$$

$$t \mapsto -\ln(t)$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8(x+1)^2}}{\sqrt{\pi}}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 x \sqrt{2} + 1/4 \sqrt{2}\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 \left(-\sqrt{2} + 4 \operatorname{RootOf}(-\operatorname{erf}(-Z) - 1 + 2s)\right) \sqrt{2}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 x \sqrt{2} + 1/4 \sqrt{2}\right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2}e^{-1/8(x+1)^2}}{\sqrt{\pi}(-1 + \operatorname{erf}(1/4 x \sqrt{2} + 1/4 \sqrt{2}))}$$

Mean

$$\mu = -1$$

Variance

$$\sigma^2 = 4$$

Moment Function

$$m(x) = \int_{-\infty}^{\infty} 1/4 \frac{x^r \sqrt{2}e^{-1/8(x+1)^2}}{\sqrt{\pi}} dx$$

Moment Generating Function

$$e^{t(2t-1)}_1$$

$$t \mapsto \ln(t+1)$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8-1/8 (\ln(e^x-1))^2+x}}{\sqrt{\pi} (e^x - 1)^{3/4}}$$

Cumulative Distribution Function

$$F(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{e^{-1/8-1/8 (\ln(e^t-1))^2+t}}{(e^t - 1)^{3/4}} dt$$

Inverse Cumulative Distribution Function

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(-\sqrt{2} \int_0^x \frac{e^{-1/8-1/8 (\ln(e^t-1))^2+t}}{(e^t - 1)^{3/4}} dt + 4 \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2}e^{-1/8-1/8 (\ln(e^x-1))^2+x}}{(e^x - 1)^{3/4}} \left(-\sqrt{2} \int_0^x \frac{e^{-1/8-1/8 (\ln(e^t-1))^2+t}}{(e^t - 1)^{3/4}} dt + 4 \sqrt{\pi} \right)^{-1}$$

Mean

$$mu = \int_0^\infty 1/4 \frac{x\sqrt{2}e^{-1/8-1/8 (\ln(e^x-1))^2+x}}{\sqrt{\pi} (e^x - 1)^{3/4}} dx$$

Variance

$$sigma^2 = \int_0^\infty 1/4 \frac{x^2\sqrt{2}e^{-1/8-1/8 (\ln(e^x-1))^2+x}}{\sqrt{\pi} (e^x - 1)^{3/4}} dx - \left(\int_0^\infty 1/4 \frac{x\sqrt{2}e^{-1/8-1/8 (\ln(e^x-1))^2+x}}{\sqrt{\pi} (e^x - 1)^{3/4}} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 1/4 \frac{x^r\sqrt{2}e^{-1/8-1/8 (\ln(e^x-1))^2+x}}{\sqrt{\pi} (e^x - 1)^{3/4}} dx$$

Moment Generating Function

$$\int_0^\infty 1/4 \frac{\sqrt{2}e^{tx-1/8-1/8 (\ln(e^x-1))^2+x}}{\sqrt{\pi} (e^x - 1)^{3/4}} dx_1$$

$$t \mapsto (\ln(t+2))^{-1}$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi} (e^{x^{-1}} - 2) x^2} e^{-1/8} \frac{(\ln(e^{x^{-1}} - 2))^2 x - 2 \ln(e^{x^{-1}} - 2) x + x - 8}{x}$$

Cumulative Distribution Function

$$F(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{1}{(e^{t^{-1}} - 2) t^2} e^{-1/8} \frac{(\ln(e^{t^{-1}} - 2))^2 t - 2 \ln(e^{t^{-1}} - 2) t + t - 8}{t} dt$$

Inverse Cumulative Distribution Function

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(-\sqrt{2} \int_0^x \frac{1}{(e^{t^{-1}} - 2) t^2} e^{-1/8} \frac{(\ln(e^{t^{-1}} - 2))^2 t - 2 \ln(e^{t^{-1}} - 2) t + t - 8}{t} dt + 4 \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2}}{(e^{x^{-1}} - 2) x^2} e^{-1/8} \frac{(\ln(e^{x^{-1}} - 2))^2 x - 2 \ln(e^{x^{-1}} - 2) x + x - 8}{x} \left(-\sqrt{2} \int_0^x \frac{1}{(e^{t^{-1}} - 2) t^2} e^{-1/8} \frac{(\ln(e^{t^{-1}} - 2))^2 t - 2 \ln(e^{t^{-1}} - 2) t + t - 8}{t} dt + 4 \sqrt{\pi} \right)$$

Mean

$$\mu = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{(\ln(2))^{-1}} \frac{1}{x (e^{x^{-1}} - 2)} e^{-1/8} \frac{(\ln(e^{x^{-1}} - 2))^2 x - 2 \ln(e^{x^{-1}} - 2) x + x - 8}{x} dx$$

Variance

$$\sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_0^{(\ln(2))^{-1}} \frac{1}{x (e^{x^{-1}} - 2)} e^{-1/8} \frac{(\ln(e^{x^{-1}} - 2))^2 x - 2 \ln(e^{x^{-1}} - 2) x + x - 8}{x} dx \right)^2 \sqrt{\pi} - 2 \sqrt{\pi} \right)$$

Moment Function

$$m(x) = \int_0^{(\ln(2))^{-1}} 1/4 \frac{x^r \sqrt{2}}{\sqrt{\pi} (e^{x^{-1}} - 2) x^2} e^{-1/8} \frac{(\ln(e^{x^{-1}} - 2))^2 x - 2 \ln(e^{x^{-1}} - 2) x + x - 8}{x} dx$$

Moment Generating Function

$$1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{(\ln(2))^{-1}} \frac{1}{(e^{x^{-1}} - 2) x^2} e^{-1/8 \frac{(\ln(e^{x^{-1}} - 2))^2}{x-8} \ln(e^{x^{-1}} - 2) x + x - 8} dx$$

$$t \mapsto \tanh(t)$$

Probability Distribution Function

$$f(x) = -1/4 \frac{\sqrt{2} e^{-1/8 (\ln(\operatorname{arctanh}(x)) - 1)^2}}{\sqrt{\pi} \operatorname{arctanh}(x) (x^2 - 1)}$$

Cumulative Distribution Function

$$F(x) = -1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{e^{-1/8 (\ln(\operatorname{arctanh}(t)) - 1)^2}}{\operatorname{arctanh}(t) (t^2 - 1)} dt$$

Inverse Cumulative Distribution Function

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{e^{-1/8 (\ln(\operatorname{arctanh}(t)) - 1)^2}}{\operatorname{arctanh}(t) (t^2 - 1)} dt + 4 \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2} e^{-1/8 (\ln(\operatorname{arctanh}(x)) - 1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} \left(\sqrt{2} \int_0^x \frac{e^{-1/8 (\ln(\operatorname{arctanh}(t)) - 1)^2}}{\operatorname{arctanh}(t) (t^2 - 1)} dt + 4 \sqrt{\pi} \right)^{-1}$$

Mean

$$mu = -1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{x e^{-1/8 (\ln(\operatorname{arctanh}(x)) - 1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} dx$$

Variance

$$sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_0^1 \frac{x e^{-1/8 (\ln(\operatorname{arctanh}(x)) - 1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} dx \right)^2 \sqrt{\pi} + 2 \sqrt{2} \int_0^1 \frac{x^2 e^{-1/8 (\ln(\operatorname{arctanh}(x)) - 1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} dx \right)$$

Moment Function

$$m(x) = \int_0^1 -1/4 \frac{x^r \sqrt{2} e^{-1/8 (\ln(\operatorname{arctanh}(x)) - 1)^2}}{\sqrt{\pi} \operatorname{arctanh}(x) (x^2 - 1)} dx$$

Moment Generating Function

$$-1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{e^{-1/8-1/8 (\ln(\operatorname{arctanh}(x)))^2+tx}}{(\operatorname{arctanh}(x))^{3/4} (x^2-1)} dx$$

$$t \mapsto \sinh(t)$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8 (\ln(\operatorname{arcsinh}(x))-1)^2}}{\sqrt{\pi} \operatorname{arcsinh}(x) \sqrt{x^2+1}}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf} \left(1/4 \sqrt{2} \left(\ln \left(-\ln \left(-x + \sqrt{x^2+1} \right) \right) - 1 \right) \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto 1/2 e^{e^{1+2\sqrt{2}\operatorname{RootOf}(-\operatorname{erf}(-Z)-1+2s)}} - 1/2 e^{-e^{1+2\sqrt{2}\operatorname{RootOf}(-\operatorname{erf}(-Z)-1+2s)}}]$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf} \left(1/4 \sqrt{2} \left(\ln \left(-\ln \left(-x + \sqrt{x^2+1} \right) \right) - 1 \right) \right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2}e^{-1/8 (\ln(\operatorname{arcsinh}(x))-1)^2}}{\sqrt{\pi} \operatorname{arcsinh}(x) \sqrt{x^2+1} (-1 + \operatorname{erf} (1/4 \sqrt{2} (\ln (-\ln (-x + \sqrt{x^2+1})) - 1)))}$$

Mean

$$mu = \infty$$

Variance

$$sigma^2 = \text{undefined}$$

Moment Function

$$m(x) = \infty$$

Moment Generating Function

$$\int_0^\infty 1/4 \frac{e^{-1/8-1/8 (\ln(\operatorname{arcsinh}(x)))^2+tx} \sqrt{2}}{(\operatorname{arcsinh}(x))^{3/4} \sqrt{x^2+1} \sqrt{\pi}} dx_1$$

$$t \mapsto \operatorname{arcsinh}(t)$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8(\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)}$$

Cumulative Distribution Function

$$F(x) = 1/2 - 1/2 \operatorname{erf}\left(1/4 \sqrt{2}(-\ln(e^x - 1) - \ln(e^x + 1) + \ln(2) + x + 1)\right)$$

Inverse Cumulative Distribution Function

$$F^{-1} = [s \mapsto \ln\left(\operatorname{RootOf}\left(-Z^2 + \left(-2e^{1/2\sqrt{2}(-4\operatorname{RootOf}(\operatorname{erf}(-Z)-1+2s)+\sqrt{2})} - 2\right) - Z + 2e^{1/2\sqrt{2}(-4\operatorname{RootOf}(\operatorname{erf}(-Z)-1+2s)+\sqrt{2})}\right)\right)$$

Survivor Function

$$S(x) = 1/2 + 1/2 \operatorname{erf}\left(1/4 \sqrt{2}(-\ln(e^x - 1) - \ln(e^x + 1) + \ln(2) + x + 1)\right)$$

Hazard Function

$$h(x) = 1/2 \frac{\sqrt{2}e^{-1/8(\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x) (1 + \operatorname{erf}(1/4 \sqrt{2}(-\ln(e^x - 1) - \ln(e^x + 1) + \ln(2) + x + 1)))}$$

Mean

$$mu = \int_0^\infty 1/4 \frac{x \sqrt{2}e^{-1/8(\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx$$

Variance

$$sigma^2 = \int_0^\infty 1/4 \frac{x^2 \sqrt{2}e^{-1/8(\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx - \left(\int_0^\infty 1/4 \frac{x \sqrt{2}e^{-1/8(\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 1/4 \frac{x^r \sqrt{2}e^{-1/8(\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx$$

Moment Generating Function

"Unable to find MGF"

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8 (\ln(-1+\operatorname{arctanh}(x^{-1}))-1)^2}}{\sqrt{\pi} (-1 + \operatorname{arctanh}(x^{-1})) (x^2 - 1)}$$

Cumulative Distribution Function

$$F(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^x \frac{e^{-1/8 (\ln(-1+\operatorname{arctanh}(t^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(t^{-1})) (t^2 - 1)} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(-\sqrt{2} \int_1^x \frac{e^{-1/8 (\ln(-1+\operatorname{arctanh}(t^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(t^{-1})) (t^2 - 1)} dt + 4\sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2}e^{-1/8 (\ln(-1+\operatorname{arctanh}(x^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(x^{-1})) (x^2 - 1)} \left(-\sqrt{2} \int_1^x \frac{e^{-1/8 (\ln(-1+\operatorname{arctanh}(t^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(t^{-1})) (t^2 - 1)} dt + 4\sqrt{\pi} \right)^{-1}$$

Mean

$$mu = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^{\frac{e^2+1}{e^2-1}} \frac{x e^{-1/8 (\ln(-1+\operatorname{arctanh}(x^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(x^{-1})) (x^2 - 1)} dx$$

Variance

$$sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_1^{\frac{e^2+1}{e^2-1}} \frac{x e^{-1/8 (\ln(-1+\operatorname{arctanh}(x^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(x^{-1})) (x^2 - 1)} dx \right)^2 \sqrt{\pi} - 2\sqrt{2} \int_1^{\frac{e^2+1}{e^2-1}} \frac{x^2 e^{-1/8 (\ln(-1+\operatorname{arctanh}(x^{-1}))-1)^2}}{(-1 + \operatorname{arctanh}(x^{-1})) (x^2 - 1)} dx \right)$$

Moment Function

$$m(x) = \int_1^{\frac{e+e^{-1}}{e-e^{-1}}} 1/4 \frac{x^r \sqrt{2} e^{-1/8 (\ln(-1+\operatorname{arctanh}(x^{-1}))-1)^2}}{\sqrt{\pi} (-1 + \operatorname{arctanh}(x^{-1})) (x^2 - 1)} dx$$

Moment Generating Function

$$1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^{\frac{e^2+1}{e^2-1}} \frac{e^{-1/8-1/8(\ln(-1+\operatorname{arctanh}(x^{-1})))^2+tx}}{(-1+\operatorname{arctanh}(x^{-1}))^{3/4}(x^2-1)} dx$$

$$t \mapsto (\sinh(t+1))^{-1}$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8(\ln(-1+\operatorname{arcsinh}(x^{-1}))-1)^2}}{\sqrt{\pi}\sqrt{x^2+1}(-1+\operatorname{arcsinh}(x^{-1}))|x|}$$

Cumulative Distribution Function

$$F(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{e^{-1/8(\ln(-1+\operatorname{arcsinh}(t^{-1}))-1)^2}}{\sqrt{t^2+1}(-1+\operatorname{arcsinh}(t^{-1}))|t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(-\sqrt{2} \int_0^x \frac{e^{-1/8(\ln(-1+\operatorname{arcsinh}(t^{-1}))-1)^2}}{\sqrt{t^2+1}(-1+\operatorname{arcsinh}(t^{-1}))|t|} dt + 4\sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2}e^{-1/8(\ln(-1+\operatorname{arcsinh}(x^{-1}))-1)^2}}{\sqrt{x^2+1}(-1+\operatorname{arcsinh}(x^{-1}))|x|} \left(-\sqrt{2} \int_0^x \frac{e^{-1/8(\ln(-1+\operatorname{arcsinh}(t^{-1}))-1)^2}}{\sqrt{t^2+1}(-1+\operatorname{arcsinh}(t^{-1}))|t|} dt + 4\sqrt{\pi} \right)^{-1}$$

Mean

$$mu = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{\frac{e}{e^2-1}} \frac{e^{-1/8(\ln(-1+\operatorname{arcsinh}(x^{-1}))-1)^2}}{\sqrt{x^2+1}(-1+\operatorname{arcsinh}(x^{-1}))} dx$$

Variance

$$sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_0^{\frac{e}{e^2-1}} \frac{e^{-1/8(\ln(-1+\operatorname{arcsinh}(x^{-1}))-1)^2}}{\sqrt{x^2+1}(-1+\operatorname{arcsinh}(x^{-1}))} dx \right)^2 \sqrt{\pi} - 2\sqrt{2} \int_0^{\frac{e}{e^2-1}} \frac{xe^{-1/8(\ln(-1+\operatorname{arcsinh}(x^{-1}))-1)^2}}{\sqrt{x^2+1}} dx \right)$$

Moment Function

$$m(x) = \int_0^{2(e-e^{-1})^{-1}} \frac{1}{4} \frac{x^r \sqrt{2} e^{-1/8} (\ln(-1 + \operatorname{arcsinh}(x^{-1})) - 1)^2}{\sqrt{\pi} \sqrt{x^2 + 1} (-1 + \operatorname{arcsinh}(x^{-1})) |x|} dx$$

Moment Generating Function

$$\frac{1}{4} \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{2 \frac{e}{e^2-1}} \frac{e^{-1/8-1/8} (\ln(-1 + \operatorname{arcsinh}(x^{-1})) - 1)^2 + tx}{(-1 + \operatorname{arcsinh}(x^{-1}))^{3/4} x \sqrt{x^2 + 1}} dx$$

$$t \mapsto (\operatorname{arcsinh}(t + 1))^{-1}$$

Probability Distribution Function

$$f(x) = \frac{1}{4} \frac{\sqrt{2} e^{-1/8} (\ln(-1 + \sinh(x^{-1})) - 1)^2 \cosh(x^{-1})}{\sqrt{\pi} (-1 + \sinh(x^{-1})) x^2}$$

Cumulative Distribution Function

$$F(x) = 1/2 + 1/2 \operatorname{erf} \left(\frac{1}{4} \frac{\sqrt{2}}{x} \left(\ln(2) x - \ln(e^{2x^{-1}} - 2e^{x^{-1}} - 1) x + x + 1 \right) \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/2 - 1/2 \operatorname{erf} \left(\frac{1}{4} \frac{\sqrt{2}}{x} \left(\ln(2) x - \ln(e^{2x^{-1}} - 2e^{x^{-1}} - 1) x + x + 1 \right) \right)$$

Hazard Function

$$h(x) = -1/2 \frac{\sqrt{2} e^{-1/8} (\ln(-1 + \sinh(x^{-1})) - 1)^2 \cosh(x^{-1})}{\sqrt{\pi} (-1 + \sinh(x^{-1})) x^2} \left(-1 + \operatorname{erf} \left(\frac{1}{4} \frac{\sqrt{2}}{x} \left(\ln(2) x - \ln(e^{2x^{-1}} - 2e^{x^{-1}} - 1) x + x + 1 \right) \right) \right)$$

Mean

$$mu = \frac{1}{4} \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{e^{-1/8} (\ln(-1 + \sinh(x^{-1})) - 1)^2 \cosh(x^{-1})}{x (-1 + \sinh(x^{-1}))} dx$$

Variance

$$\sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{e^{-1/8 (\ln(-1+\sinh(x^{-1}))-1)^2} \cosh(x^{-1})}{x(-1+\sinh(x^{-1}))} dx \right)^2 \sqrt{\pi} - 2\sqrt{2} \int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{e^{-1/8 (\ln(-1+\sinh(x^{-1}))-1)^2} \cosh(x^{-1})}{x(-1+\sinh(x^{-1}))} dx \right)$$

Moment Function

$$m(x) = \int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{1}{4} \frac{x^r \sqrt{2} e^{-1/8 (\ln(-1+\sinh(x^{-1}))-1)^2} \cosh(x^{-1})}{\sqrt{\pi} (-1+\sinh(x^{-1})) x^2} dx$$

Moment Generating Function

$$1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^{(\ln(1+\sqrt{2}))^{-1}} \frac{e^{-1/8+tx-1/8 (\ln(-1+\sinh(x^{-1})))^2} \cosh(x^{-1})}{(-1+\sinh(x^{-1}))^{3/4} x^2} dx$$

$$t \mapsto (\operatorname{csch}(t))^{-1} + 1$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2} e^{-1/8 (\ln(\operatorname{arccsch}((x-1)^{-1}))-1)^2}}{\sqrt{\pi} \sqrt{x^2 - 2x + 2} \operatorname{arccsch}((x-1)^{-1})}$$

Cumulative Distribution Function

$$F(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_1^x \frac{e^{-1/8 (\ln(\operatorname{arccsch}((t-1)^{-1}))-1)^2}}{\sqrt{t^2 - 2t + 2} \operatorname{arccsch}((t-1)^{-1})} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(-\sqrt{2} \int_1^x \frac{e^{-1/8 (\ln(\operatorname{arccsch}((t-1)^{-1}))-1)^2}}{\sqrt{t^2 - 2t + 2} \operatorname{arccsch}((t-1)^{-1})} dt + 4\sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2} e^{-1/8 (\ln(\operatorname{arccsch}((x-1)^{-1}))-1)^2}}{\sqrt{x^2 - 2x + 2} \operatorname{arccsch}((x-1)^{-1})} \left(-\sqrt{2} \int_1^x \frac{e^{-1/8 (\ln(\operatorname{arccsch}((t-1)^{-1}))-1)^2}}{\sqrt{t^2 - 2t + 2} \operatorname{arccsch}((t-1)^{-1})} dt + 4\sqrt{\pi} \right)$$

Mean

$$mu = \infty$$

Variance

$$sigma^2 = undefined$$

Moment Function

$$m(x) = \infty$$

Moment Generating Function

$$\int_1^\infty 1/4 \frac{e^{-1/8-1/8 \left(\ln(\operatorname{arccsch}((x-1)^{-1})) \right)^2 + tx} \sqrt{2}}{\left(\operatorname{arccsch}((x-1)^{-1}) \right)^{3/4} \sqrt{x^2 - 2x + 2} \sqrt{\pi}} dx_1$$

$$t \mapsto \tanh(t^{-1})$$

Probability Distribution Function

$$f(x) = -1/4 \frac{\sqrt{2} e^{-1/8 \left(\ln((\operatorname{arctanh}(x))^{-1}) - 1 \right)^2}}{\sqrt{\pi} \operatorname{arctanh}(x) (x^2 - 1)}$$

Cumulative Distribution Function

$$F(x) = -1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{e^{-1/8 \left(\ln((\operatorname{arctanh}(t))^{-1}) - 1 \right)^2}}{\operatorname{arctanh}(t) (t^2 - 1)} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(\sqrt{2} \int_0^x \frac{e^{-1/8 \left(\ln((\operatorname{arctanh}(t))^{-1}) - 1 \right)^2}}{\operatorname{arctanh}(t) (t^2 - 1)} dt + 4 \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = -\frac{\sqrt{2} e^{-1/8 \left(\ln((\operatorname{arctanh}(x))^{-1}) - 1 \right)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} \left(\sqrt{2} \int_0^x \frac{e^{-1/8 \left(\ln((\operatorname{arctanh}(t))^{-1}) - 1 \right)^2}}{\operatorname{arctanh}(t) (t^2 - 1)} dt + 4 \sqrt{\pi} \right)^{-1}$$

Mean

$$\mu = -1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{x e^{-1/8 (\ln(\operatorname{arctanh}(x))+1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} dx$$

Variance

$$\sigma^2 = -1/8 \frac{1}{\pi^{3/2}} \left(\left(\int_0^1 \frac{x e^{-1/8 (\ln(\operatorname{arctanh}(x))+1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} dx \right)^2 \sqrt{\pi} + 2 \sqrt{2} \int_0^1 \frac{x^2 e^{-1/8 (\ln(\operatorname{arctanh}(x))+1)^2}}{\operatorname{arctanh}(x) (x^2 - 1)} dx \right)$$

Moment Function

$$m(x) = \int_0^1 -1/4 \frac{x^r \sqrt{2} e^{-1/8 (\ln((\operatorname{arctanh}(x))^{-1})-1)^2}}{\sqrt{\pi} \operatorname{arctanh}(x) (x^2 - 1)} dx$$

Moment Generating Function

$$-1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^1 \frac{e^{-1/8 - 1/8 (\ln(\operatorname{arctanh}(x)))^2 + tx}}{(\operatorname{arctanh}(x))^{5/4} (x^2 - 1)} dx$$

$$t \mapsto \operatorname{csch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2} e^{-1/8 (\ln(\operatorname{arccsch}(x))+1)^2}}{\sqrt{\pi} \sqrt{x^2 + 1} \operatorname{arccsch}(x) |x|}$$

Cumulative Distribution Function

$$F(x) = 1/4 \frac{\sqrt{2}}{\sqrt{\pi}} \int_0^x \frac{e^{-1/8 (\ln(\operatorname{arccsch}(t))+1)^2}}{\sqrt{t^2 + 1} \operatorname{arccsch}(t) |t|} dt$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/4 \frac{1}{\sqrt{\pi}} \left(-\sqrt{2} \int_0^x \frac{e^{-1/8 (\ln(\operatorname{arccsch}(t))+1)^2}}{\sqrt{t^2 + 1} \operatorname{arccsch}(t) |t|} dt + 4 \sqrt{\pi} \right)$$

Hazard Function

$$h(x) = \frac{\sqrt{2}e^{-1/8 (\ln(\operatorname{arccsch}(x))+1)^2}}{\sqrt{x^2+1}\operatorname{arccsch}(x)|x|} \left(-\sqrt{2} \int_0^x \frac{e^{-1/8 (\ln(\operatorname{arccsch}(t))+1)^2}}{\sqrt{t^2+1}\operatorname{arccsch}(t)|t|} dt + 4\sqrt{\pi} \right)^{-1}$$

Mean

$$mu = \int_0^\infty 1/4 \frac{\sqrt{2}e^{-1/8 (\ln(\operatorname{arccsch}(x))+1)^2}}{\sqrt{\pi}\sqrt{x^2+1}\operatorname{arccsch}(x)} dx$$

Variance

$$sigma^2 = \int_0^\infty 1/4 \frac{x\sqrt{2}e^{-1/8 (\ln(\operatorname{arccsch}(x))+1)^2}}{\sqrt{\pi}\sqrt{x^2+1}\operatorname{arccsch}(x)} dx - \left(\int_0^\infty 1/4 \frac{\sqrt{2}e^{-1/8 (\ln(\operatorname{arccsch}(x))+1)^2}}{\sqrt{\pi}\sqrt{x^2+1}\operatorname{arccsch}(x)} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 1/4 \frac{x^r \sqrt{2}e^{-1/8 (\ln(\operatorname{arccsch}(x))+1)^2}}{\sqrt{\pi}\sqrt{x^2+1}\operatorname{arccsch}(x)|x|} dx$$

Moment Generating Function

$$\int_0^\infty 1/4 \frac{e^{-1/8-1/8 (\ln(\operatorname{arccsch}(x)))^2+tx}\sqrt{2}}{(\operatorname{arccsch}(x))^{5/4} x\sqrt{x^2+1}\sqrt{\pi}} dx_1$$

$$t \mapsto \operatorname{arccsch}(t^{-1})$$

Probability Distribution Function

$$f(x) = 1/4 \frac{\sqrt{2}e^{-1/8 (\ln(\sinh(x))-1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)}$$

Cumulative Distribution Function

$$F(x) = 1/2 - 1/2 \operatorname{erf} \left(1/4 \sqrt{2} (-\ln(e^x - 1) - \ln(e^x + 1) + \ln(2) + x + 1) \right)$$

Inverse Cumulative Distribution Function

$$F^{-1} =$$

Survivor Function

$$S(x) = 1/2 + 1/2 \operatorname{erf} \left(1/4 \sqrt{2} (-\ln(e^x - 1) - \ln(e^x + 1) + \ln(2) + x + 1) \right)$$

Hazard Function

$$h(x) = 1/2 \frac{\sqrt{2} e^{-1/8 (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x) (1 + \operatorname{erf} (1/4 \sqrt{2} (-\ln(e^x - 1) - \ln(e^x + 1) + \ln(2) + x + 1)))}$$

Mean

$$mu = \int_0^\infty 1/4 \frac{x \sqrt{2} e^{-1/8 (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx$$

Variance

$$sigma^2 = \int_0^\infty 1/4 \frac{x^2 \sqrt{2} e^{-1/8 (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx - \left(\int_0^\infty 1/4 \frac{x \sqrt{2} e^{-1/8 (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx \right)^2$$

Moment Function

$$m(x) = \int_0^\infty 1/4 \frac{x^r \sqrt{2} e^{-1/8 (\ln(\sinh(x)) - 1)^2} \cosh(x)}{\sqrt{\pi} \sinh(x)} dx$$

Moment Generating Function

$$\int_0^\infty 1/4 \frac{e^{-1/8 + tx - 1/8 (\ln(\sinh(x)))^2} \cosh(x) \sqrt{2}}{(\sinh(x))^{3/4} \sqrt{\pi}} dx_1$$