

NAME: \_\_\_\_\_

## **Matrices and Matrix Calculations - Spring 2017**

### **Midterm Exam I, February 16, 2017**

In all multiple choice problems you don't have to show your work. In all non-multiple choice problems you are required to show all your work and provide the necessary explanations everywhere to get full credit.

This print-out should have 17 questions. Multiple-choice questions may continue on the next column or page – find all choices before answering.

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**FinM4a24**  
**001 10.0 points**

Pandit is an aging dog who has to be kept on a strict diet containing, among other things, 2.5 grams of protein and 1.8 grams of fat. Two dog foods are available to Pandit's owner.

Food  $A$  has 8% protein and 6% fat, while

Food  $B$  has 3% protein and 2% fat.

How many grams of food  $A$  should Pandit's owner use in his diet?

1. # grams food  $A$  = 20
2. # grams food  $A$  = 21
3. # grams food  $A$  = 19
4. # grams food  $A$  = 22
5. # grams food  $A$  = 23

is the unique parabola passing through the points

$$(1, 7), \quad (-1, 1), \quad (-3, 3),$$

determine  $b$ .

1.  $b = 2$
2.  $b = 6$
3.  $b = 4$
4.  $b = 5$
5.  $b = 3$

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**FitParabola01b**  
**002 10.0 points**

When the graph of the function

$$y = ax^2 + bx + c$$

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**LinearSystemT/F01a**  
003 10.0 points

Elementary row operations on an augmented matrix never change the solution set of the associated linear system.

True or False?

1. TRUE
2. FALSE

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**RowReduceMan02a**  
005 10.0 points

The augmented matrix of a linear system of equations has been reduced by row operations to

$$\begin{bmatrix} 1 & 2 & -3 & 7 \\ 0 & 1 & -1 & 3 \\ 0 & 0 & 1 & -2 \end{bmatrix}.$$

(a) *Continue row operations to write the matrix in reduced row echelon form.*

(b) *Then determine the solution set of the original system.*

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**LinSysUniqueTF02**  
004 10.0 points

If a system of linear equations has no free variables, then it has a unique solution.

True or False?

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**AxisIntersect01a**  
**006 10.0 points**

When  $P$  is the plane in  $\mathbb{R}^3$  given in vector form by

$$\mathbf{x} = \begin{bmatrix} -1 \\ -2 \\ 1 \end{bmatrix} + s \begin{bmatrix} -2 \\ 2 \\ 4 \end{bmatrix} + t \begin{bmatrix} 3 \\ -4 \\ -4 \end{bmatrix},$$

determine where  $P$  intersects the  $z$ -axis.

1.  $z = -7$
2.  $z = -8$
3.  $z = -9$
4.  $z = -5$
5.  $z = 6$

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**M340LSpanM02**  
**007 10.0 points**

Given

$$\mathbf{v}_1 = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}, \quad \mathbf{v}_2 = \begin{bmatrix} 2 \\ 4 \\ 2 \end{bmatrix}, \quad \mathbf{v}_3 = \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix},$$

determine all values of  $\lambda$  for which

$$\mathbf{w} = \begin{bmatrix} 2 \\ 1 \\ \lambda \end{bmatrix}$$

is a vector in  $\text{Span}\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$ ?

1.  $\lambda = 3$
2.  $\lambda = 1, 3$
3.  $\lambda = -1, 1$
4.  $\lambda = -1$
5.  $\lambda = 1$
6.  $\lambda = -1, 3$

If  $\mathbf{u}, \mathbf{v}$  are vectors in  $\mathbb{R}^3$ , when can  $\text{Span}\{\mathbf{u}, \mathbf{v}\}$  be visualized as a plane through the origin in  $\mathbb{R}^3$ .

True or False?

1. ALWAYS
2. SOMETIMES
3. NEVER

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### Consistent01d

**009 10.0 points**

Describe geometrically the conditions on a vector  $\mathbf{b}$  in  $\mathbb{R}^2$  under which the equation

$$\begin{bmatrix} 2 & 3 \\ 6 & 9 \end{bmatrix} \mathbf{x} = \mathbf{b}$$

has a solution in  $\mathbb{R}^2$ .

1.  $\mathbf{b}$  lies on line  $y + 3x = 0$
2.  $\mathbf{b}$  lies on line  $y - 3x = 0$
3. arbitrary  $\mathbf{b}$  in  $\mathbb{R}^2$
4. any  $\mathbf{b}$  not on line  $y + 3x = 0$
5. any  $\mathbf{b}$  not on line  $y - 3x = 0$

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**VectorEquTF01e**  
**008 10.0 points**

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**SolSetsLinSysTF03****011 10.0 points**

If the equation  $A\mathbf{x} = \mathbf{b}$  has more than one solution, then so does the homogeneous equation  $A\mathbf{x} = \mathbf{0}$ .

True or False?

1. FALSE
2. TRUE

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**MatEquTF02b****010 10.0 points**

If the matrix equation  $A\mathbf{x} = \mathbf{b}$  is consistent, then  $\mathbf{b}$  is in the set spanned by the columns of  $A$ .

True or False?

1. TRUE
2. FALSE

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**ThreePoints01a****012 10.0 points**

Determine the linear equation of the unique plane in  $\mathbb{R}^3$  containing the points

$$P(1, 2, 1), \quad Q(-1, -1, 0),$$

and

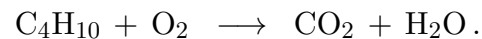
$$R(-1, -4, -2).$$

1.  $3x - 4y + 6z = 1$
2.  $3x + 4y - 6z + 1 = 0$
3.  $3x - 4y - 6z + 1 = 0$
4.  $3x + 4y + 6z = 1$
5.  $3x + 4y - 6z = 1$
6.  $3x - 4y + 6z + 1 = 0$

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**BalChemEq01a****013 10.0 points**

When butane  $\text{C}_4\text{H}_{10}$  burns in the presence of oxygen  $\text{O}_2$  it produces carbon dioxide  $\text{CO}_2$  and water  $\text{H}_2\text{O}$ , represented chemically by



If 60 molecules of water were produced in one particular reaction, how many molecules of butane were burned in that reaction?

1. # molecules = 15
2. # molecules = 14
3. # molecules = 11
4. # molecules = 13
5. # molecules = 12

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**LinIndependMan01a**  
**014    10.0 points**

Find all values  $h$  for which the vectors

$$\begin{bmatrix} 2 \\ -2 \\ 4 \end{bmatrix}, \quad \begin{bmatrix} 4 \\ -6 \\ 7 \end{bmatrix}, \quad \begin{bmatrix} -2 \\ 2 \\ h \end{bmatrix}$$

are linearly independent.

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**LinIndepTF01c**  
**015    10.0 points**

The columns of any  $4 \times 5$  matrix are linearly dependent.

True or False?

1. FALSE
2. TRUE



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**LinTransform01e**
**016 10.0 points**

A transformation  $T : \mathbb{R}^n \rightarrow \mathbb{R}^m$  is linear if and only if

$$T(c_1\mathbf{v}_1 + c_2\mathbf{v}_2) = c_1T(\mathbf{v}_1) + c_2T(\mathbf{v}_2)$$

for all vectors  $\mathbf{v}_1, \mathbf{v}_2$  in  $\mathbb{R}^n$  and all scalars  $c_1, c_2$ .

True or False?

1. FALSE
2. TRUE

1.  $A = \begin{bmatrix} \sqrt{3} & 1 \\ -1 & \sqrt{3} \end{bmatrix}$

2.  $A = \frac{1}{2} \begin{bmatrix} \sqrt{3} & -1 \\ 1 & \sqrt{3} \end{bmatrix}$

3.  $A = \frac{1}{2} \begin{bmatrix} 1 & \sqrt{3} \\ -\sqrt{3} & 1 \end{bmatrix}$

4.  $A = \frac{1}{2} \begin{bmatrix} \sqrt{3} & 1 \\ -1 & \sqrt{3} \end{bmatrix}$

5.  $A = \begin{bmatrix} 1 & -\sqrt{3} \\ \sqrt{3} & 1 \end{bmatrix}$

6.  $A = \frac{1}{2} \begin{bmatrix} 1 & -\sqrt{3} \\ \sqrt{3} & 1 \end{bmatrix}$

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**MatrixTrans01a**
**017 10.0 points**

Determine the Standard Matrix for the transformation rotating the plane counter-clockwise about the origin through  $60^\circ$ .