This print-out should have 11 questions. Multiple-choice questions may continue on the next column or page – find all choices before answering.

QuadApprox02a 001 10.0 points

Find the quadratic approximation to

$$f(x, y) = \cos(2x + y) - \sin(x - y)$$

at P(0, 0).

1.
$$Q(x, y) = 2 - x + y + 2x^2 - 2xy + y^2$$

2.
$$Q(x, y) = 1 + x - y + 2x^2 - 2xy + y^2$$

3.
$$Q(x, y) = 2 - x + y - 2x^2 + 2xy - \frac{1}{2}y^2$$

4.
$$Q(x, y) = 2 - x + y + 2x^2 + 2xy - \frac{1}{2}y^2$$

5.
$$Q(x, y) = 1 - x + y - 2x^2 - 2xy - \frac{1}{2}y^2$$

6.
$$Q(x, y) = 1 + x - y - 2x^2 + 2xy + y^2$$

$\begin{array}{cc} CalC15g19b \\ 002 & 10.0 \text{ points} \end{array}$

Locate and classify the critical point of $f(x,y) = \ln(xy) + 2y^2 - 2y - 2xy + 4,$ for x,y>0.

- **1.** local minimum at $\left(\frac{1}{2}, 1\right)$
- **2.** saddle-point at $\left(1, \frac{1}{2}\right)$
- **3.** local maximum at $\left(1, \frac{1}{2}\right)$
- **4.** local maximum at $\left(\frac{1}{2}, 1\right)$
- **5.** saddle-point at $\left(\frac{1}{2}, 1\right)$
- **6.** local minimum at $\left(1, \frac{1}{2}\right)$

3.
$$\mathbf{r}(t) = (t+2)\mathbf{i} + (t+5)\mathbf{j} - (2t^2 - 2t)\mathbf{k}$$

4.
$$\mathbf{r}(t) = (t+2)\mathbf{i} - (t-5)\mathbf{j} - (2t^2 + 2t)\mathbf{k}$$

5.
$$\mathbf{r}(t) = (t-2)\mathbf{i} + (t+5)\mathbf{j} - (2t^2+2t)\mathbf{k}$$

6.
$$\mathbf{r}(t) = (t+2)\mathbf{i} - (t-5)\mathbf{j} - (2t^2 - 2t)\mathbf{k}$$

CalC14d16s 003 10.0 points

Determine the position vector, $\mathbf{r}(t)$, of a particle having acceleration

$$\mathbf{a}(t) = -4\,\mathbf{k}$$

when its initial velocity and position are given by

$$\mathbf{v}(0) = \mathbf{i} + \mathbf{j} - 2\mathbf{k}, \quad \mathbf{r}(0) = 2\mathbf{i} + 5\mathbf{j}$$

respectively.

1.
$$\mathbf{r}(t) = (t-2)\mathbf{i} + (t+5)\mathbf{j} - (2t^2 - 2t)\mathbf{k}$$

2.
$$\mathbf{r}(t) = (t+2)\mathbf{i} + (t+5)\mathbf{j} - (2t^2+2t)\mathbf{k}$$

$\begin{array}{cc} CalC14c04a \\ 004 & 10.0 \ points \end{array}$

The curve C is parametrized by

$$\mathbf{c}(t) = (4+2t)\mathbf{i} + \ln(2t)\mathbf{j} + (3+t^2)\mathbf{k}.$$

Find the arc length of C between $\mathbf{c}(1)$ and $\mathbf{c}(3)$.

$\begin{array}{cc} GradVectorField01a \\ 005 & 10.0 \ points \end{array}$

If f(x, y) is a potential function for the gradient vector field

$$\mathbf{F}(x, y) = (3x - y)\mathbf{i} - (x + 2y)\mathbf{j},$$

evaluate

$$f(1, 2) - f(0, 1)$$
.

$\begin{array}{c} {\rm Curl 01a} \\ 006 & 10.0 \ {\rm points} \end{array}$

Find the curl of the vector field

$$\mathbf{F}(x,\,y,\,z) \;=\; 3zx\,\mathbf{i} + xy\,\mathbf{j} - 2yz\,\mathbf{k}\,.$$

1. curl
$$\mathbf{F} = -2z\,\mathbf{i} + 3x\,\mathbf{j} + y\,\mathbf{k}$$

2.
$$\operatorname{curl} \mathbf{F} = -2z \mathbf{i} - 3x \mathbf{j} + y \mathbf{k}$$

3.
$$\operatorname{curl} \mathbf{F} = 3x \mathbf{i} + y \mathbf{j} - 2z \mathbf{k}$$

4. curl
$$\mathbf{F} = x \, \mathbf{i} + 2y \, \mathbf{j} - 3z \, \mathbf{k}$$

5.
$$\operatorname{curl} \mathbf{F} = x \mathbf{i} - 2y \mathbf{j} + 3z \mathbf{k}$$

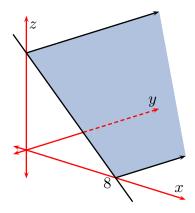
6. curl
$$\mathbf{F} = 3z \, \mathbf{i} - x \, \mathbf{j} - 2y \, \mathbf{k}$$

CalC16b01a 007 10.0 points

The graph of the function

$$z = f(x, y) = 8 - x$$

is the plane shown in



Determine the value of the double integral

$$I = \int \int_A f(x, y) \, dx dy$$

over the region

$$A = \{(x,y) : 0 \le x \le 3, \ 0 \le y \le 4 \}$$

in the xy-plane by first identifying it as the volume of a solid below the graph of f.

1.
$$I = 77$$
 cu. units

2.
$$I = 78$$
 cu. units

3.
$$I = 76$$
 cu. units

4.
$$I = 75$$
 cu. units

5.
$$I = 74$$
 cu. units

CalC16c05s 008 10.0 points

Evaluate the iterated integral

$$I = \int_0^{3\pi/2} \int_0^{\cos(\theta)} 2 e^{\sin(\theta)} dr d\theta.$$

1.
$$I = 2e$$

2.
$$I = 2\left(\frac{1}{e} - 1\right)$$

3.
$$I = 2(e-1)$$

4.
$$I = 0$$

5.
$$I = e - 2$$

6.
$$I = \frac{1}{e} - 2$$

$\begin{array}{cc} CalC16g01a \\ 009 & 10.0 \ points \end{array}$

Evaluate the triple integral

$$I = \int_0^1 \int_0^x \int_0^{x+y} (2x - y) \, dz \, dy \, dx \, .$$

1.
$$I = \frac{3}{8}$$

2.
$$I = \frac{5}{8}$$

3.
$$I = \frac{17}{24}$$

4.
$$I = \frac{13}{24}$$

5.
$$I = \frac{11}{24}$$

Div01a 010 10.0 points

Find the divergence of the vector field

$$\mathbf{F}(x, y, z) = 2x^2yz\,\mathbf{i} - xy^2z\,\mathbf{j} + 3xyz^2\,\mathbf{k}.$$

- 1. $\operatorname{div} \mathbf{F} = 8xyz$
- $\mathbf{2.} \ \operatorname{div} \mathbf{F} = 11xyz$
- 3. $\operatorname{div} \mathbf{F} = 12xyz$
- 4. $\operatorname{div} \mathbf{F} = 10xyz$
- 5. $\operatorname{div} \mathbf{F} = 9xyz$

CalC15h04exam 011 10.0 points

Determine the maximum value of

$$f(x, y) = 4x - 3y + 2$$

subject to the constraint

$$g(x, y) = x^2 + y^2 - 1 = 0.$$