This print-out should have 12 questions. Multiple-choice questions may continue on the next column or page – find all choices before answering.

MatrixProp01a 001 10.0 points

Compute $AA^T - A^TA$ for the matrix

$$A = \begin{bmatrix} 1 & -1 \\ -2 & 3 \end{bmatrix}.$$

1.
$$AA^T - A^TA = \begin{bmatrix} 3 & 2 \\ 2 & -3 \end{bmatrix}$$

2.
$$AA^T - A^TA = \begin{bmatrix} 3 & -2 \\ -2 & -3 \end{bmatrix}$$

3.
$$AA^T - A^TA = \begin{bmatrix} -3 & -2 \\ 2 & 3 \end{bmatrix}$$

4.
$$AA^T - A^TA = \begin{bmatrix} 3 & -2 \\ 2 & -3 \end{bmatrix}$$

5.
$$AA^T - A^TA = \begin{bmatrix} -3 & 2 \\ 2 & 3 \end{bmatrix}$$

6.
$$AA^T - A^TA = \begin{bmatrix} -3 & -2 \\ -2 & 3 \end{bmatrix}$$

InverseMatrix01b 002 10.0 points

Solve for X when A(X + B) = C,

$$A = \begin{bmatrix} 5 & 2 \\ -3 & -1 \end{bmatrix}, \quad B = \begin{bmatrix} 2 & -2 \\ 1 & 5 \end{bmatrix},$$

and

$$C = \begin{bmatrix} 2 & 2 \\ -1 & 5 \end{bmatrix}.$$

LUDecomp06h 00310.0 points

Find L in an LU decomposition of

$$A = \begin{bmatrix} -1 & 5 & 3 & 4 \\ -1 & 5 & 4 & 2 \\ -5 & 25 & 18 & 15 \end{bmatrix}.$$

$$1. \ L = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ -5 & -3 & 1 \end{bmatrix}$$

2.
$$L = \begin{bmatrix} -1 & 0 & 0 \\ 1 & -1 & 0 \\ 5 & 3 & -1 \end{bmatrix}$$

3. $L = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 5 & 3 & 1 \end{bmatrix}$

3.
$$L = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 5 & 3 & 1 \end{bmatrix}$$

4.
$$L = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ 5 & -3 & 1 \end{bmatrix}$$

5.
$$L = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ -5 & 3 & 1 \end{bmatrix}$$

6.
$$L = \begin{bmatrix} 2 & 0 & 0 \\ 1 & 2 & 0 \\ 5 & 3 & 2 \end{bmatrix}$$

Subspace02a 004 10.0 points

Which of the following describes

$$H = \operatorname{Span}\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$$

when

$$\mathbf{v}_1 = \begin{bmatrix} 1 \\ 1 \\ -3 \end{bmatrix}, \ \mathbf{v}_2 = \begin{bmatrix} -2 \\ -1 \\ 7 \end{bmatrix}, \ \mathbf{v}_3 = \begin{bmatrix} 1 \\ 4 \\ 0 \end{bmatrix}.$$

- 1. *H* is a plane through origin
- **2.** $H = \mathbb{R}^3$
- **3.** H is a line
- **4.** *H* is a plane not through origin

- **1.** i
- **2.** ii
- 3. i and ii
- 4. All of these
- 5. ii and iii
- **6.** None of these

Rank02e 006 10.0 points

Determine the rank of the matrix

$$A = \begin{bmatrix} 1 & 0 & 1 \\ -3 & 1 & -2 \\ 0 & 1 & 2 \end{bmatrix}.$$

- 1. $\operatorname{rank}(A) = 1$
- **2.** rank(A) = 3
- **3.** rank(A) = 4
- **4.** rank(A) = 2
- 5. rank(A) = 5

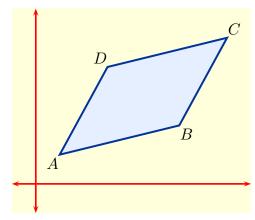
Invertible02 005 10.0 points

A is an $n \times n$ matrix. Which of the following statements are equivalent to A being invertible?

- (i) The columns of A form a basis of \mathbb{R}^n .
- (ii) $\dim(\operatorname{Col} A) = n$.
- (iii) $\operatorname{rank} A = 0$.

DetArea03a 007 10.0 points

Compute the area of the parallelogram ABCD shown in



having vertices at

$$A = (1, 1), \qquad B = (6, 2),$$

and

$$C = (8, 5), \qquad D = (3, 4).$$

- 1. area = 11
- **2.** area = 12
- **3.** area = 10
- **4.** area = 13
- **5.** area = 14

$\begin{array}{cc} {\bf Basis Null 01b} \\ {\bf 008} & {\bf 10.0~points} \end{array}$

Find a basis for the Null space of the matrix

$$A = \begin{bmatrix} 3 & -6 & -3 & -3 \\ 1 & -4 & -5 & 3 \\ -3 & 4 & -1 & 9 \end{bmatrix}.$$

PolyCoordVec01b 010 10.0 points

Find the coordinate vector $[\mathbf{p}]_{\mathcal{B}}$ in \mathbb{R}^3 for the polynomial

$$\mathbf{p}(t) = 2 + 3t - 6t^2$$

with respect to the basis

$$\mathcal{B} = \left\{1 - t^2, \ t - t^2, \ 1 - t + t^2\right\}$$

for \mathbb{P}_2 .

1.
$$[\mathbf{p}]_{\mathcal{B}} = \begin{bmatrix} 1 \\ 3 \\ 2 \end{bmatrix}$$

$$\mathbf{2.} \ [\mathbf{p}]_{\mathcal{B}} = \begin{bmatrix} 3 \\ -2 \\ 1 \end{bmatrix}$$

3.
$$[\mathbf{p}]_{\mathcal{B}} = \begin{bmatrix} -2 \\ -1 \\ 3 \end{bmatrix}$$

4.
$$[\mathbf{p}]_{\mathcal{B}} = \begin{bmatrix} 2 \\ 1 \\ -3 \end{bmatrix}$$

5.
$$[\mathbf{p}]_{\mathcal{B}} = \begin{bmatrix} 1 \\ -3 \\ -2 \end{bmatrix}$$

$$\mathbf{6.} \ [\mathbf{p}]_{\mathcal{B}} = \begin{bmatrix} 3 \\ 2 \\ -1 \end{bmatrix}$$

$\begin{array}{c} {\rm Basis 03a} \\ {\rm 009} \quad {\rm 10.0~points} \end{array}$

In the vector space V of all real-valued functions, find a basis for the subspace

 $H = \operatorname{Span} \{ \sin t, \sin 2t, \sin t \cos t \}.$

- 1. $\{\cos t, \sin 2t, \sin t \cos t\}$
- **2.** $\{\cos t, \sin 2t\}$
- **3.** $\{ \sin t, \sin 2t \}$
- 4. $\{\sin t, \sin 2t, \sin t \cos t\}$
- $5. \left\{ \sin 2t, \, \sin t \cos t \right\}$

ChangeBasis01c 011 (part 1 of 2) 10.0 points

Determine the change of coordinates matrix $P_{\mathcal{C} \leftarrow \mathcal{B}}$ from basis $\mathcal{B} = \{\mathbf{b}_1, \mathbf{b}_2\}$ to $\mathcal{C} = \{\mathbf{c}_1, \mathbf{c}_2\}$ of a vector space V when

$$\mathbf{b}_1 = -\mathbf{c}_1 + 4\mathbf{c}_2, \quad \mathbf{b}_2 = 5\mathbf{c}_1 - 3c_2.$$

Explanation:

When

$$\mathbf{x} = 5\mathbf{b}_1 + 3\mathbf{b}_2,$$

then

$$\mathbf{x} = 5(-\mathbf{c}_1 + 4\mathbf{c}_2) + 3(5\mathbf{c}_1 - 3c_2).$$

Consequently,

$$[\mathbf{x}]_{\mathcal{C}} = \begin{bmatrix} 10\\11 \end{bmatrix}$$